MATLAB codes

Listing 1.1: Dummy File For Reading Data

Listing 1.2: OLS Regression

```
function [beta, sigma] = OLS_Est(X, Y)
% OLS regression
beta = inv(X' * X) * X' * Y;
eps = Y - X*beta;
sigma = sqrt((eps' * eps) / (size(Y, 1) - size(X, 2)));
end
```

Listing 1.3: MLE

```
function output = loglikelihood_ps2(init)
1
2
3
  |% init -> initial guess
5
   global D T W X Y Z
   colW = size(W, 2);
  colX = size(X, 2);
   colZ = size(Z, 2);
9
10
  % Identification auxiliary
11
   aux = [colX, ...]
12
       2 * colX, ...
13
14
       2 * colX + colZ, \dots
```

```
15
       2 * colX + colZ + colW, ...
16
       2 * colX + colZ + 2 * colW, \dots
17
       2 * colX + colZ + 3 * colW, ...
18
       2 * colX + colZ + 4 * colW, ...
19
       2 * colX + colZ + 4 * colW + 1, ...
20
       2 * colX + colZ + 4 * colW + 2, ...
21
       2 * colX + colZ + 4 * colW + 3, ...
22
       2 * colX + colZ + 4 * colW + 4, ...
23
       2 * colX + colZ + 4 * colW + 5, ...
24
       2 * colX + colZ + 4 * colW + 6, ...
25
       2 * colX + colZ + 4 * colW + 7, ...
26
       2 * colX + colZ + 4 * colW + 8, ...
27
       2 * colX + colZ + 4 * colW + 9, ...
28
       2 * colX + colZ + 4 * colW + 10, ...
29
       2 * colX + colZ + 4 * colW + 11, ...
30
       2 * colX + colZ + 4 * colW + 12, ...
31
       2 * colX + colZ + 4 * colW + 13];
32
33
  % Parameters
   beta_0 = init(1:aux(1));
34
  beta_1 = init(aux(1) + 1:aux(2));
35
36
   beta_D = init(aux(2) + 1:aux(3));
   omega_T1 = init(aux(3) + 1:aux(4));
37
38
   omega_T2 = init(aux(4) + 1:aux(5));
39
   omega_T3 = init(aux(5) + 1:aux(6));
   omega_T4 = init(aux(6) + 1:aux(7));
40
41
   sigma_0 = init(aux(7) + 1:aux(8));
42
   sigma_1 = init(aux(8) + 1:aux(9));
   sigma_T1 = init(aux(9) + 1:aux(10));
43
44
   sigma_T2 = init(aux(10) + 1:aux(11));
45
   sigma_T3 = init(aux(11) + 1:aux(12));
   sigma_T4 = init(aux(12) + 1:aux(13));
46
   alpha_0 = init(aux(13) + 1:aux(14));
47
   alpha_1 = init(aux(14) + 1:aux(15));
48
49
   alpha_I = init(aux(15) + 1:aux(16));
   alpha_T2 = init(aux(16) + 1:aux(17));
50
   alpha_T3 = init(aux(17) + 1:aux(18));
51
52
   alpha_T4 = init(aux(18) + 1:aux(19));
   sigma_theta = init(aux(19) + 1:aux(20));
53
54
   MLfunc = @(theta) (normpdf(Y - X * beta_0 - theta * alpha_0, 0,
55
      exp(sigma_0)) ...
56
       .* normpdf(Y - X * beta_1 - theta * alpha_1, 0, exp(sigma_1))
       .* normpdf(T(:, 1) - W * omega_T1 - theta, 0, exp(sigma_T1))
57
58
       .* normpdf(T(:, 2) - W * omega_T2 - theta * alpha_T2, 0, exp(
          sigma_T2)) ...
```

```
59
       .* normpdf(T(:, 3) - W * omega_T3 - theta * alpha_T3, 0, exp(
          sigma_T3)) ...
60
       .* normpdf(T(:, 4) - W * omega_T4 - theta * alpha_T4, 0, exp(
          sigma_T4)) ...
61
       .* (1 - normcdf(Z * beta_D + theta * alpha_I, 0, 1)) .^ (1 - D
          ) ...
       .* normcdf(Z * beta_D + theta * alpha_I, 0, 1) .^ D ...
62
       .* normpdf(theta, 0, exp(sigma_theta)));
63
64
65
   % Can use Gauss - Hermit or Montecarlo
66
67
   % However there is a tradeoff between computing time and
     programming G-H
68
   % integration.
   sol = integral(MLfunc, -Inf, Inf, 'ArrayValued', true);
69
70
   output = -sum(log(sol));
71
72
73
   end
```

Listing 1.4: Estimation of Parameters

```
1
   clear
   % Set Seet: LGMV
   randn('seed', 180618)
3
4
5
   % Set global
6
  global D T W X Y Z
  %check dummy file read.m
8
9
   read;
10
   [beta_T1, sigma_T1] = OLS_Est(W, T(:, 1));
11
   [beta_T2, sigma_T2] = OLS_Est(W, T(:, 2));
12
   [beta_T3, sigma_T3] = OLS_Est(W, T(:, 3));
13
14
   [beta_T4, sigma_T4] = OLS_Est(W, T(:, 4));
   [beta_D, sigma_D] = OLS_Est(Z, D); % Take sigma_D = 1, to simplify
15
   [beta_1, sigma_1] = OLS_Est(X, Y);
16
   [beta_0, sigma_0] = OLS_Est(X, Y);
17
18
19
   [alpha_T1, alpha_T2, alpha_T3, alpha_T4, alpha_I, alpha_1, alpha_0
      , sigma_theta] = deal(1);
20
21
   % Initial guesses for
22
   guesses = [beta_0; beta_1; beta_D; beta_T1; beta_T2; beta_T3;
     beta_T4; ...
23
       sigma_0; sigma_1; sigma_T1; sigma_T2; sigma_T3; sigma_T4; ...
       alpha_0; alpha_1; alpha_T2; alpha_T3; alpha_T4; ...
24
```

```
sigma_theta];
25
26
27
  tic
   options = optimoptions(@fminunc, 'Algorithm', 'quasi-newton', '
28
      Display', 'iter',...
       'GradObj', 'off', 'HessUpdate', 'bfgs', 'UseParallel', false,
29
30
       'TolFun', 1e-6, 'TolX', 1e-6, 'MaxIter', 10000, 'MaxFunEvals',
           10000);
31
   [est_beta, est_F, exitflag, output, grad, hessian] = fminunc('
      loglikelihood_ps2', guesses, options);
32
33
  runtime = toc;
34
35 se_Hess=sqrt(diag(inv(hessian)));
   [est_beta se_Hess]
36
```