

Graph

Concept: -

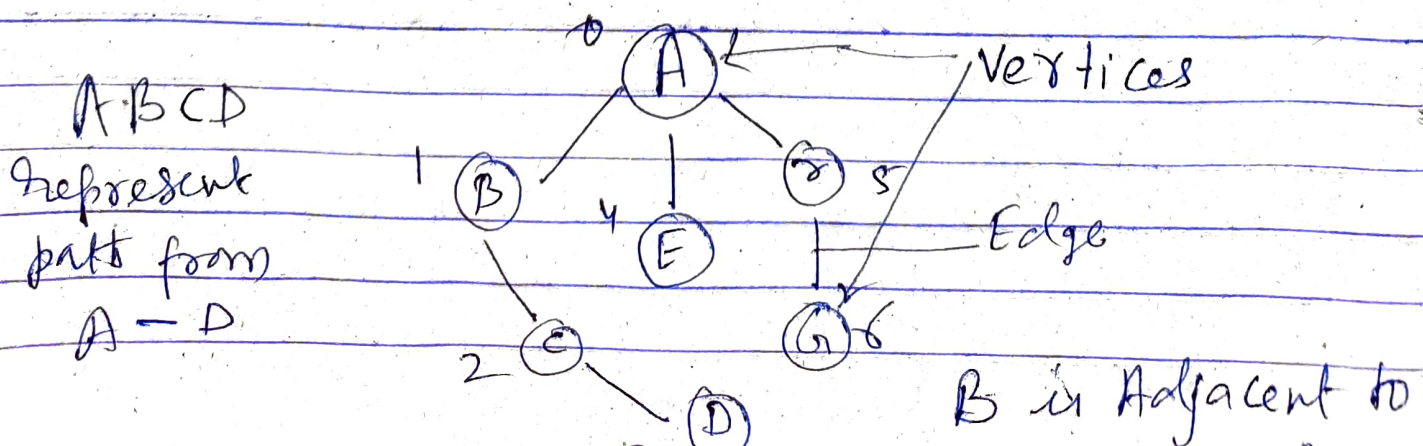
A Graph data Structure consists of a finite set of vertices (also called as nodes or points) together with a set of Edges (also called as links or lines)

In computer science a graph is meant to implement the graph concept from the field of graph theory within mathematics

The main terms related with

graph are -

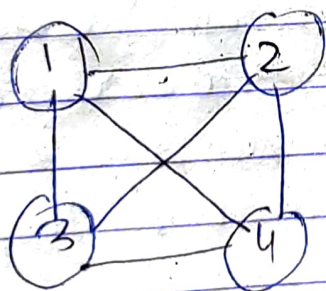
- * ~~Vertex~~ - Each node of Graph is represented as a vertex.
- * Edge - Edge represents a path between two vertices or a line between two-vertices
- * Adjacency - Two nodes or vertices are called adjacent if they are connected to each other through an edge.
- * Path - Path represents a sequence of edges between the two vertices



Graphs are used to solve many real-life problems, for example graphs are used to represent networks. Graphs may be hierarchical or non-hierarchical, in addition they may be cyclic or non-cyclic. The UNIX file and directory structure is the best example of hierarchical cyclic graph.

A Graph can be of two types - Undirected Graph & Directed Graph.

A) Undirected Graph:- A graph which has unordered pair of vertices is called Undirected graph like



For example The graph

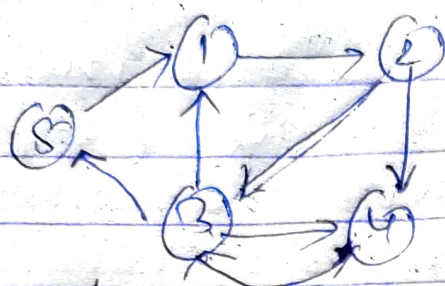
G has -

$$V(G) = \{1, 2, 3, 4\}$$

$$E(G) = \{(1, 2), (1, 3), (1, 4), (2, 3), (2, 4), (3, 4)\}$$

B) Directed Graph:- A directed graph is a graph which has ordered pair of vertices (v_1, v_2) where v_1 is the tail and v_2 is head of edges. In this type of graph each edge has direction. means (v_1, v_2) and (v_2, v_1) represent different edges, means that a direction will be

associated with that edge.



$$V(G) = \{1, 2, 3, 4, 5\}$$

$$E(G) = \{(1, 2), (2, 3), (4, 3), (4, 1), (4, 5), (5, 1)\}$$

The Graph has 5 vertices and 6 Edges.

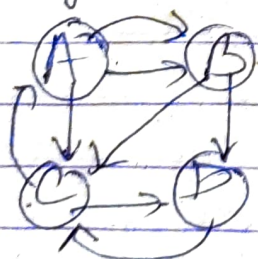
~~The~~ Matrix Representation of Graphs:

Graphs can be stored both as Array and

linked list. If stored as array, they are

stored in the form of Adjacency Matrix. Adjacency Matrix is matrix which keeps the information of Adjacent nodes. In other words we can say that it keeps the information that whether this node is adjacent to any other node or not.

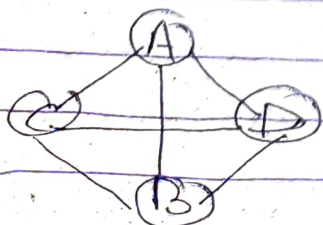
The Matrix to store a graph must be a square matrix because each row and each column of the Matrix represents a node. For ex - a graph having 4 nodes will be stored in a Matrix 4×4 as given in the figure



Directed

	A	B	C	D
A	0	1	0	1
B	1	0	1	1
C	0	0	0	1
D	1	0	1	0

Matrix $[T][j]$ will be 1 if there is an edge between node i and j and it will be 0 if there is no edge between these two nodes



Undirected

	A	B	C	D
A	0	1	1	1
B	1	0	1	1
C	1	1	0	1
D	1	1	1	0