

# Digital Design

A Datapath and Control Approach

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September 27, 2024

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## Chapter 1

# Numbering Systems

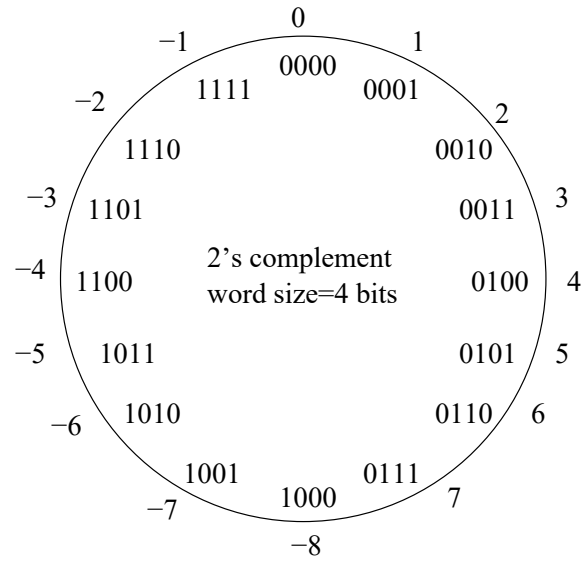
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### Helpfull Stuff

Decimal	Binary	Hexadecimal
0	0000	0
1	0001	1
2	0010	2
3	0011	3
4		4
5	0101	5
6		6
7		7
8	1000	8
9		9
10	1010	A
11		B
12	1100	C
13	1101	D
14		E
15	1111	F

i	0	1	2	3	4	5	6	7	8	9
2 <sup>i</sup>	1	2	4	8	16	32	64	128	256	512

$$\begin{aligned}
1110101011_2 &= \\
1 * 2^9 + 1 * 2^8 + 1 * 2^7 + 0 * 2^6 + 1 * 2^5 + 0 * 2^4 + 1 * 2^3 + 0 * 2^2 + 1 * 2^1 + 1 * 2^0 &= \\
2^8(0 * 2^3 + 0 * 2^2 + 1 * 2^1 + 1 * 2^0) + 2^4(1 * 2^3 + 0 * 2^2 + 1 * 2^1 + 0 * 2^0) + 2^0 * (1 * 2^3 + 0 * 2^2 + 1 * 2^1 + 1 * 2^0) &= \\
2^8(0011_2) + 2^4(1010_2) + 2^0(1011_2) &= \\
2^{4*2}(0011_2) + 2^{4*1}(1010_2) + 2^{4*0}(1011_2) &= \\
16^2(0011_2) + 16^1(1010_2) + 16^0 * (1011_2) &= \\
16^2(3) + 16^1(A) + 16^0 * (B) &= \\
3AB_{16}
\end{aligned}$$



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## Chapter 2

# Representations of Logical Functions

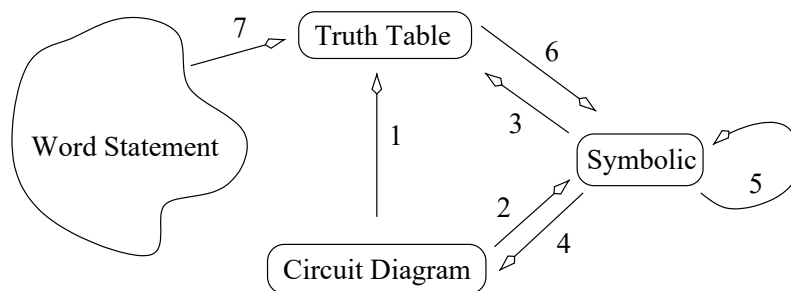
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### 2.1 Helpfull Stuff

A	B	A*B
0	0	0
0	1	0
1	0	0
1	1	1

A	B	A+B
0	0	0
0	1	1
1	0	1
1	1	1

A	A'
0	1
1	0



	Regular Algebra	Boolean Algebra
Performed First	Parenthesis	Parenthesis
	Exponents	Not
	multiplication/division	And
Performed Last	addition/subtraction	Or

Axiom	Primary	Dual
1.	$x+0=x$	$x*1=x$
2.	$x+1=1$	$x*0=0$
3.	$x+x=x$	$x*x=x$
4.	$x''=x$	
5.	$x+x'=1$	$x*x'=0$
6.	$x+y=y+x$	$x*y=y*x$
7.	$x+(y+z)=(x+y)+z$	$x*(y*z)=(x*y)*z$
8.	$x*(y+z)=x*y+x*z$	$x+(y*z)=(x+y)*(x+z)$
9.	$(x+y)'=x'*y'$	$(x*y)'=x'+y'$

## 2.2 Definitions

Define each of the following. Some of the definitions should use terms you've defined.

**Minterm**

**Maxterm**

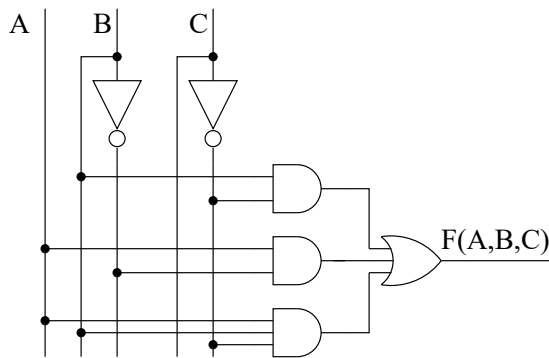
**Minterm Trick**

**Expansion Trick**

## 2.3 Problems

Solve the following problems in the space provided.

- Given the circuit diagram below, produce the corresponding truth table.



A	B	C	F(A,B,C)
0	0	0	
0	0	1	
0	1	0	
0	1	1	
1	0	0	
1	0	1	
1	1	0	
1	1	1	

- Given the symbolic expression below, produce the corresponding circuit diagram.

$$F(A,B,C)=AB'+A(B'+C)$$

3. Given the symbolic expression below, produce the corresponding circuit diagram.

$$F(A,B,C,D)=A(BC+A(C'+D))' + B'CD'$$

4. Given the symbolic expression below, produce the corresponding truth table.

$$F(A,B,C) = AB' + A(B' + C)$$

A	B	C			F(A,B,C)
0	0	0			
0	0	1			
0	1	0			
0	1	1			
1	0	0			
1	0	1			
1	1	0			
1	1	1			

5. Given the symbolic expression below, produce the corresponding truth table.

$$F(A,B,C,D)=A(BC+A(C'+D))' + B'CD'$$

A	B	C	D							F(A,B,C,D)
0	0	0	0							
0	0	0	1							
0	0	1	0							
0	0	1	1							
0	1	0	0							
0	1	0	1							
0	1	1	0							
0	1	1	1							
1	0	0	0							
1	0	0	1							
1	0	1	0							
1	0	1	1							
1	1	0	0							
1	1	0	1							
1	1	1	0							
1	1	1	1							

6. Given the truth table below, produce the corresponding symbolic expression.

A	B	C	F(A,B,C)	minterm	maxterm
0	0	0	0		
0	0	1	1		
0	1	0	1		
0	1	1	1		
1	0	0	1		
1	0	1	0		
1	1	0	0		
1	1	1	1		

7. Given the word state below, produce the corresponding truth table. Design a circuit with two 2-bit inputs called  $A = a_1a_0$  and  $B = b_1b_0$ . The single bit output  $F$  should equal 1 when  $A+B > 6$ , otherwise  $F$  should equal 0.

$a_1$	$a_0$	$b_1$	$b_0$	A	B	$F(a_1, a_0, b_1, b_0)$
0	0	0	0			
0	0	0	1			
0	0	1	0			
0	0	1	1			
0	1	0	0			
0	1	0	1			
0	1	1	0			
0	1	1	1			
1	0	0	0			
1	0	0	1			
1	0	1	0			
1	0	1	1			
1	1	0	0			
1	1	0	1			
1	1	1	0			
1	1	1	1			