

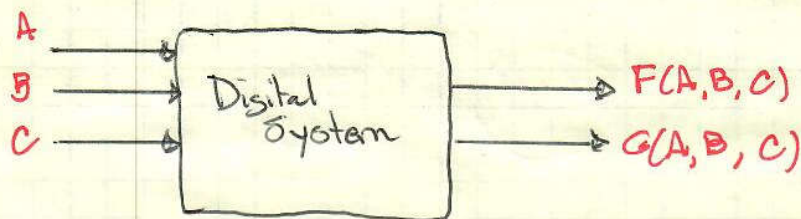
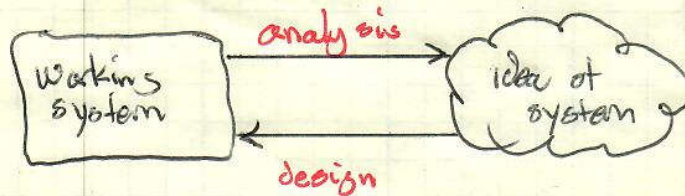
Welcome Theory & Practice of Digital Design

Few Details before we start

Lecture	Lab
Live or Zoom	Live
Canvas syllabus text book	Next Tuesday
	No pre lab
	Install Quartus software

- TA office hours
- I have office hours
- Your success is my goal

Title: Analysis & Design of Digital Systems



inputs & outputs are bits (0 or 1)

A, B, C are Boolean variables meaning they equal 0 or 1

$F(A, B, C)$ & $G(A, B, C)$ are equal to 0 or 1, depend on A, B, C

Arrangements of bits can represent many different things

- letters
- dog food codes
- Quantity (numbers)

} Bits have no meaning
only interpretation

We will focus on interpreting collections of bits as numbers

using positional numbering \equiv the left/right position of a symbol in a number determines its weight.

Ex: Decimal \equiv Base 10 \equiv 10 symbols $\equiv \{0, 1, 2, \dots, 9\}$

$$\begin{array}{ccccccc} 3 & 6 & 5 & & & & \\ 2 & 1 & 0 & & & & \end{array} \begin{array}{l} 10^2 \\ 10^1 \\ 10^0 \end{array} = 3 \times 10^2 + 6 \times 10^1 + 5 \times 10^0$$

$$= 300 + 60 + 5$$

Ex: Binary = Base 2 = 2 symbols = $\{0, 1\}$

$$\begin{array}{c} 101_2 \\ \text{2 1 0} \end{array} = 1 * 2^2 + 0 * 2^1 + 1 * 2^0$$

$$= 4 + 0 + 1 = 5$$

We just converted binary to decimal.

Try: $\begin{array}{c} 1011_2 \\ \text{3 2 1 0} \end{array}$

Convert Decimal to binary

- Represent the decimal value x as the sum of distinct powers of 2.

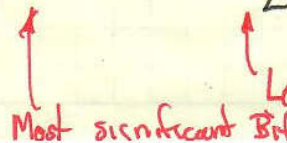
Power of 2 table

i	0	1	2	3	4	5	6	7
2^i	1	2	4	8	16	32	64	128

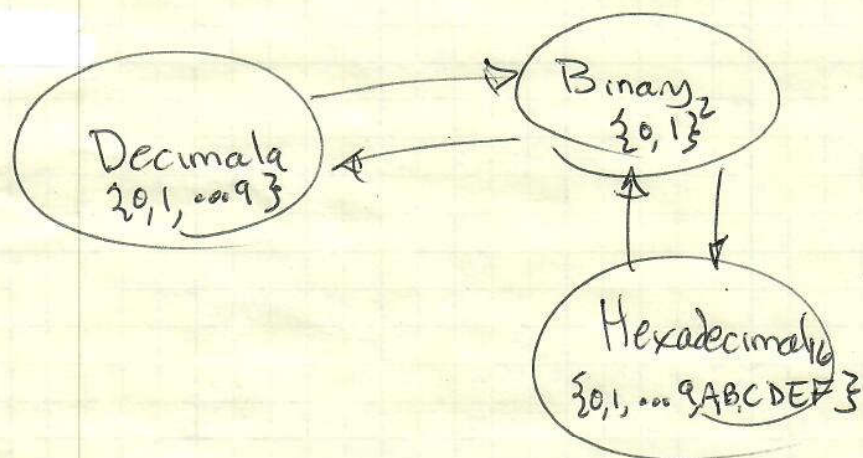
Try: $11_{10} = 8 + 2 + 1$ <find largest 2^i leg value>

$$\begin{array}{r} 11 \\ -8 \\ \hline 3 \\ -2 \\ \hline 1 \end{array} = 1 * 2^3 + 0 * 2^2 + 1 * 2^1 + 1 * 2^0 = 1011_2$$

Try: $123_{10} = 1111011_2$


 Most significant Bit (MSB)
 Least Significant Bit (LSB)

Number Conversions



Convert Hexadecimal to binary

- Convert each hex digit into its 4-bit binary code

Decimal	Binary	Hex
0	0 0 0 0	0
1	0 0 0 1	1
2	0 0 1 0	2
3	0 0 1 1	3
4	0 1 0 0	4
5	0 1 0 1	5
6	0 1 1 0	6
7	0 1 1 1	7
8	1 0 0 0	8
9	1 0 0 1	9
10	1 0 1 0	A
11	1 0 1 1	B
12	1 1 0 0	C
13	1 1 0 1	D
14	1 1 1 0	E
15	1 1 1 1	F

$$3EA_{16} = 0011 \quad 1110 \quad 1010_2$$