

ASSIGNMENT-5.

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①

Let us consider a sample dataset have one input (x_i) and one, output (y_i) and number of samples 4, Develop a simple linear regression model using MBGD.

(1) Sample	x_i	y_i
1	0.2	3.4
2	0.4	3.8
3	0.6	4.2
4	0.8	4.6

Do manual calculations for two iterations with batch size-2.

- Write the Python code to build simple linear regression model using MBGD optimizer (consider All 4 samples)

Batch 1

$$\begin{array}{c|c} x & y \\ \hline 0.2 & 3.4 \\ 0.4 & 3.8 \end{array}$$

Batch 2

$$\begin{array}{c|c} x & y \\ \hline 0.6 & 4.2 \\ 0.8 & 4.6 \end{array}$$

Step 1 : $[x, y]$, $m = 1$, $c = -1$, $\eta = 0.1$, epochs = 2, $bs = 2$

Step 2 : $nb = \frac{ns}{bs} = \frac{4}{2} = 2$

(2)

Step 3: $itr = 1$

Step 4: Batch = 1

$$\begin{aligned}\text{Step 5: } \frac{\partial \epsilon}{\partial m} &= \frac{-1}{bs} \cdot \sum_{i=1}^{bs} (y_i - mx_i - b)x_i \\ &= -\frac{1}{2} [(3 \cdot 4 - (1)(0.2) + 1)0.2] + [3.8 - 0.4 + 1] \\ &\quad 0.4] \\ &= -1.34\end{aligned}$$

$$\begin{aligned}\frac{\partial \epsilon}{\partial c} &= +\frac{1}{2} [(3 \cdot 4 - 0.2 + 1) + (3.8 - 0.4 + 1)] \\ &= -4.3\end{aligned}$$

$$\text{Step 6: } \Delta m = -(0.1)(-1.34) = 0.134$$

$$\Delta c = -(0.1)(-4.3) = 0.43$$

$$\text{Step 7: } m = m + \Delta m = 1 + 0.134 = 1.134$$

$$c = c + \Delta c = -1 + 0.43 = -0.57$$

Step 8: if (Batch + 1

$$1 + 1 = 2$$

Step 9: if (Batch > nb)

goto step 10

2 > 2

else

goto step 5

$$\begin{aligned}\text{Step 5: } \frac{\partial \epsilon}{\partial m} &= \frac{1}{2} [(4.2 - (1.134)(0.6) + 0.57)0.6 + (4.6 \\ &\quad - (1.134)(0.8) + 0.57)0.8] \\ &= -2.932\end{aligned}$$

(3)

$$\frac{\partial \epsilon}{\partial c} = -\frac{1}{2} [(4.2 - (1.134)(0.6) + 0.57) + (4.6 - (1.134)(0.8) + 0.57)]$$

$$= -4.1762$$

$$\text{Step 6 : } \Delta m = (0.1)(-2.932) = -0.2932$$

$$\Delta c = -(0.1)(-4.1762) = 0.41762$$

$$\text{Step 7 : } m + \Delta m = 1.134 + 0.2932 = 1.4272$$

$$c + \Delta c = -0.57 + 0.4176 = -0.1523$$

$$\text{Step 8 : } \text{Batch} += 1$$

$$2 + 1 = 3$$

$$\text{Step 9 : if (batch > nb)}$$

$$\text{goto step -10}$$

$$3 > 2$$

else

$$\text{goto step -5}$$

$$\text{Step 10 : } \text{itr} = \text{itr} + 1$$

$$1 + 1 = 2,$$

$$\text{Step 11 : if (itr > epochs)}$$

$$\text{goto step -12}$$

$$2 > 2$$

else

$$\text{goto step -4}$$

$$\text{Step 4 : } \text{Batch} = 1$$

(4)

$$\text{Step 5: } \frac{\partial \epsilon}{\partial m} = -\frac{1}{2} [(3.4 - (1.4272)(0.2) + 0.1523)0.2 + (3.8 - (1.4272)(0.4) + 0.1523)0.4]$$

$$= -1.0029$$

$$\frac{\partial \epsilon}{\partial c} = -\frac{1}{2} [(3.4 - (1.4272)(0.2) + 0.1523) + (3.8 - (1.4272)(0.4) + 0.1523)]$$

$$= -3.3241$$

$$\text{Step 6: } \Delta m = (-0.1)(-1.0029)$$

$$= 0.1002$$

$$\Delta c = (-0.1)(-3.3241)$$

$$= 0.332$$

$$\text{Step 7: } m+1 = \Delta m$$

$$= 1.4272 + 0.1002 = 1.5274$$

$$c+1 = \Delta c$$

$$= -0.1523 + 0.332 = 0.1797$$

$$\text{Step 8: } \text{Batch} + 1 = 1$$

$$1 + 1 = 2$$

$$\text{Step 9: if (Batch} > \text{nb)}$$

goto step -10

2 > 2

else

goto step -7

$$\text{Step 5: } \frac{\partial \epsilon}{\partial m} = -\frac{1}{2} [(4.2 - (1.5274)(0.6) - 0.1797)0.6 + (4.6 - (1.5274)(0.8) - 0.1797)0.8]$$

$$= -2.21$$

$$\frac{\partial \ell}{\partial c} = -3.151$$

$$\text{Step 6: } \Delta m = -0.1 \times 2.21$$

$$= 0.221$$

$$\Delta c = -0.1 \times -3.151$$

$$= 0.315$$

$$\text{Step 7: } m + \Delta m = 1.5274 + 0.221$$

$$= 1.748$$

$$c + \Delta c = 0.1797 + 0.315$$

$$= 0.494$$

$$\text{Step 8: Batch } t = 1$$

$$2 + 1 = 3$$

$$\text{Step 9: if (Batch } > nb)$$

goto step -10

else goto step-5

$$\text{Step 10: } itr = 1$$

$$2 + 1 = 3$$

$$\text{Step 11: if (itr } > epochs)$$

3 > 2 goto step-12

else

goto step-4

$$\text{Step 12: print } m, c$$

$$m = 1.748, c = 0.494.$$