

Assignment 7.

18K41AD0538

①

Let us consider a sample dataset have one input (x_i) and one output (y_i) and Number of samples.

4. Develop a simple linear regression model using BGD.

Sample (i)	x_i	y_i
1	0.2	3.4
2	0.4	3.8
3	0.6	4.2
4	0.8	4.6

Do Manual calculations for two iterations with first two samples.

* write the python code to build simple linear regression model using BGD optimizer (consider all 4 samples)

Step 1: $[x, y]$, $m = 1$, $c = -1$, $\eta = 0.1$, epoch = 2, $ns = 2$

Step 2: $itr = 1$

$$\text{Step 3: } \frac{\partial E}{\partial m} = -\frac{1}{ns} \sum_{i=1}^{ns} (y_i - mx_i - c) x_i$$

$$= -\frac{1}{2} [(3.4 - (1)(0.2) + 1) 0.2 + (3.8 - (1)(0.4) + 1) 0.4]$$

$$= -1.34$$

$$\frac{\partial \epsilon}{\partial c} = -\frac{1}{2} [(3.4 - 0.2 \cdot 1) + (3.8 - 0.4 \cdot 1)]$$

$$= -4.3$$

$$\text{Step 4: } \Delta m = -\eta \cdot \frac{\partial \epsilon}{\partial m}$$

$$= -0.1 \times -1.34$$

$$= 0.134$$

$$\Delta c = -\eta \frac{\partial \epsilon}{\partial c}$$

$$= -0.1 \times -4.3 = 0.43$$

$$\text{Step 5: } m + \Delta m$$

$$1 + 0.134$$

$$= 1.134$$

$$c + \Delta c$$

$$= -0.1 \times 4.3$$

$$= -0.43$$

$$\text{Step 6: } \text{itr} + 1 = 1$$

$$1 + 1 = 2$$

Step 7: if (itr > epochs)

goto step 8

2 > 3

else

goto step 3

$$\text{Step 3: } \frac{\partial \epsilon}{\partial m} = -\frac{1}{2} [(3.4 - (1.134)(0.2) + 0.57)(0.2) +$$

$$(3.8) - (1.134)(0.4) + 0.57)(0.4)]$$

$$= -1.157.$$

(3)

$$\begin{aligned} \partial L &= -\frac{1}{2} [(1.84 - (1.1345(0.2) + 0.57) + (3.8) - \\ &\quad (1.134)(0.4) + 0.57)] \\ &= 3.829 \end{aligned}$$

Step 4: $\Delta m = 0.1 \times 3.829 = 0.3829$

$$\Delta c = -0.1 \times 3.829 = -0.3829$$

Step 5: $m + \Delta m$

$$= 1.134 + 0.3829$$

$$= 1.2497$$

$$c = \Delta c$$

$$= 0.57 + 0.3829 = -0.187$$

Step 6: $itr + 1$

$$2 + 1 = 3$$

Step 7: if ($itr > epochs$)

$$3 > 2 \quad \text{goto step - 8}$$

else

goto step - 3

Step 8: $m = 1.2497, c = -0.1871$