

Clase 4 LP - Forma estándar y variables de holgura-15-oct

1. Convertir el siguiente LP a forma estándar:

minimize $2x_1 + 7x_2 + x_3$
subject to $x_1 - x_3 = 7$
 $3x_1 + x_2 \geq 24$
 $x_1 + 2x_2 + x_3 \geq 18$
 $x_3 \geq 0$

Ajuste de la función objetivo:

- ☒ **A** maximize $-2x_1 - 7x_2 - x_3$
subject to $x_1 - x_3 = 7$
 $3x_1 + x_2 \geq 24$
 $x_1 + 2x_2 + x_3 \geq 18$
 $x_3 \geq 0$
- ☐ **B** maximize $2x_1 + 7x_2 + x_3$
subject to $x_1 - x_3 = 7$
 $3x_1 + x_2 \geq 24$
 $x_1 + 2x_2 + x_3 \geq 18$
 $x_3 \geq 0$
- ☐ **C** minimize $-2x_1 - 7x_2 - x_3$
subject to $x_1 - x_3 = 7$
 $3x_1 + x_2 \geq 24$
 $x_1 + 2x_2 + x_3 \geq 18$
 $x_3 \geq 0$

2. Convertir el siguiente LP a forma estándar:

maximize $-2x_1 - 7x_2 - x_3$
subject to $x_1 - x_3 = 7$
 $3x_1 + x_2 \geq 24$
 $x_1 + 2x_2 + x_3 \geq 18$
 $x_3 \geq 0$

Ajuste de restricciones "mayor o igual" (excepto las de no negatividad)

(A) maximize $-2x_1 - 7x_2 - x_3$
subject to $x_1 - x_3 = 7$
 $3x_1 + x_2 \leq -24$
 $x_1 + 2x_2 + x_3 \leq -18$
 $x_3 \geq 0$

(B) maximize $-2x_1 - 7x_2 - x_3$
subject to $x_1 - x_3 = 7$
 $3x_1 + x_2 \geq 24$
 $-x_1 - 2x_2 - x_3 \leq -18$
 $x_3 \geq 0$

(C) maximize $-2x_1 - 7x_2 - x_3$
subject to $x_1 - x_3 = 7$
 $-3x_1 - x_2 \leq -24$
 $-x_1 - 2x_2 - x_3 \leq -18$
 $x_3 \geq 0$

(D) maximize $-2x_1 - 7x_2 - x_3$
subject to $x_1 - x_3 = 7$
 $-3x_1 - x_2 \leq -24$
 $x_1 + 2x_2 + x_3 \geq 18$
 $x_3 \geq 0$

3. Convertir el siguiente LP a forma estándar :

maximize $-2x_1 - 7x_2 - x_3$
subject to: $x_1 - x_3 = 7$
 $-3x_1 - x_2 \leq -24$
 $-x_1 - 2x_2 - x_3 \leq -18$
 $x_3 \geq 0$

Ajuste de restricciones "de igualdad"

(A) maximize $-2x_1 - 7x_2 - x_3$
subject to: $x_1 - x_3 \leq 7$
 $-3x_1 - x_2 \leq -24$
 $-x_1 - 2x_2 - x_3 \leq -18$
 $x_3 \geq 0$

(B) maximize $-2x_1 - 7x_2 - x_3$
subject to: $x_1 - x_3 \leq 7$
 $-x_1 + x_3 \leq -7$
 $-3x_1 - x_2 \leq -24$
 $-x_1 - 2x_2 - x_3 \leq -18$
 $x_3 \geq 0$

(C) maximize $-2x_1 - 7x_2 - x_3$
subject to: $x_1 - x_3 \geq 7$
 $-x_1 + x_3 \leq 7$
 $-3x_1 - x_2 \leq -24$
 $-x_1 - 2x_2 - x_3 \leq -18$
 $x_3 \geq 0$

4. Convertir el siguiente LP a forma estándar:

maximize $-2x_1 - 7x_2 - x_3$
subject to:
 $x_1 - x_3 \leq 7$
 $-x_1 + x_3 \leq -7$
 $-3x_1 - x_2 \leq -24$
 $-x_1 - 2x_2 - x_3 \leq -18$
 $x_3 \geq 0$

Ajuste de restricciones "de no negatividad para x1"

(A) maximize $2x_{1p} + 2x_{1n} - 7x_2 - x_3$
subject to:
 $x_{1p} - x_{1n} - x_3 \leq 7$
 $x_{1p} - x_{1n} + x_3 \leq -7$
 $-3x_{1p} + 3x_{1n} - x_2 \leq -24$
 $-x_{1p} + x_{1n} - 2x_2 - x_3 \leq -18$
 $x_3 \geq 0$

(B) maximize $-2x_{1p} + 2x_{1n} - 7x_2 - x_3$
subject to:
 $x_{1p} - x_{1n} - x_3 \leq 7$
 $-x_{1p} + x_{1n} + x_3 \leq -7$
 $3x_{1p} + 3x_{1n} - x_2 \leq -24$
 $-x_{1p} + x_{1n} - 2x_2 - x_3 \leq -18$
 $x_3 \geq 0; x_{1p} \geq 0, x_{1n} \geq 0$

(C) maximize $-2x_{1p} + 2x_{1n} - 7x_2 - x_3$
subject to:
 $x_{1p} - x_{1n} - x_3 \leq 7$
 $-x_{1p} - x_{1n} + x_3 \leq -7$
 $-3x_{1p} - 3x_{1n} - x_2 \leq -24$
 $-x_{1p} - x_{1n} - 2x_2 - x_3 \leq -18$
 $x_3 \geq 0; x_{1p} \geq 0, x_{1n} \geq 0$

(D) maximize $-2x_{1p} + 2x_{1n} - 7x_2 - x_3$
subject to:
 $x_{1p} - x_{1n} - x_3 \leq 7$
 $-x_{1p} + x_{1n} + x_3 \leq -7$
 $-3x_{1p} + 3x_{1n} - x_2 \leq -24$
 $-x_{1p} + x_{1n} - 2x_2 - x_3 \leq -18$
 $x_3 \geq 0; x_{1p} \geq 0, x_{1n} \geq 0$

5. Convertir el siguiente LP a forma estándar:

maximize $-2x_{1p} + 2x_{1n} - 7x_2 - x_3$

subject to:

$$x_{1p} - x_{1n} - x_3 \leq 7$$

$$-x_{1p} + x_{1n} + x_3 \leq -7$$

$$-3x_{1p} + 3x_{1n} - x_2 \leq -24$$

$$-x_{1p} + x_{1n} - 2x_2 - x_3 \leq -18$$

$$x_3 \geq 0; x_{1p} \geq 0, x_{1n} \geq 0$$

Ajuste de restricciones "de no negatividad para x2"

(A) maximize $-2x_{1p} + 2x_{1n} - 7x_{2p} + 7x_{2n} - x_3$

subject to :

$$x_{1p} - x_{1n} - x_3 \leq 7$$

$$-x_{1p} + x_{1n} + x_3 \leq -7$$

$$-3x_{1p} + 3x_{1n} - x_{2p} + x_{2n} \leq -24$$

$$-x_{1p} + x_{1n} - 2x_{2p} + 2x_{2n} - x_3 \leq -18$$

$$x_3 \geq 0, x_{1p} \geq 0, x_{1n} \geq 0$$

(B) maximize $-2x_{1p} + 2x_{1n} - 7x_{2p} + 7x_{2n} - x_3$

subject to :

$$x_{1p} - x_{1n} - x_3 \leq 7$$

$$-x_{1p} + x_{1n} + x_3 \leq -7$$

$$-3x_{1p} + 3x_{1n} - x_{2p} + x_{2n} \leq -24$$

$$-x_{1p} + x_{1n} - 2x_{2p} + 2x_{2n} - x_3 \leq -18$$

$$x_3 \geq 0, x_{1p} \geq 0, x_{1n} \geq 0, x_{2p} \geq 0, x_{2n} \geq 0$$

(C) maximize $-2x_{1p} + 2x_{1n} - 7x_{2p} - 7x_{2n} - x_3$

subject to :

$$x_{1p} - x_{1n} - x_3 \leq 7$$

$$-x_{1p} + x_{1n} + x_3 \leq -7$$

$$-3x_{1p} + 3x_{1n} - x_{2p} + x_{2n} \leq -24$$

$$-x_{1p} + x_{1n} - 2x_{2p} + 2x_{2n} - x_3 \leq -18$$

$$x_3 \geq 0, x_{1p} \geq 0, x_{1n} \geq 0, x_{2p} \geq 0, x_{2n} \geq 0$$

(D) maximize $-2x_{1p} + 2x_{1n} - 7x_{2p} + 7x_{2n} - x_3$

subject to :

$$x_{1p} - x_{1n} - x_3 \leq 7$$

$$-x_{1p} + x_{1n} + x_3 \leq -7$$

$$-3x_{1p} + 3x_{1n} + x_{2p} + x_{2n} \leq -24$$

$$-x_{1p} + x_{1n} - 2x_{2p} - 2x_{2n} - x_3 \leq -18$$

$$x_3 \geq 0, x_{1p} \geq 0, x_{1n} \geq 0, x_{2p} \geq 0, x_{2n} \geq 0$$

6. Convertir el siguiente LP a forma estándar con variables de holgura:

maximize $-2x_{1p} + 2x_{1n} - 7x_{2p} + 7x_{2n} - x_3$
subject to :
 $x_{1p} - x_{1n} - x_3 \leq 7$
 $-x_{1p} + x_{1n} + x_3 \leq -7$
 $-3x_{1p} + 3x_{1n} - x_{2p} + x_{2n} \leq -24$
 $-x_{1p} + x_{1n} - 2x_{2p} + 2x_{2n} - x_3 \leq -18$
 $x_3 \geq 0, x_{1p}, x_{1n}, x_{2p} \geq 0, x_{2n} \geq 0$

Adición de variables de holgura.

- (A)** maximize $-2x_{1p} + 2x_{1n} - 7x_{2p} + 7x_{2n} - x_3$
subject to
 $H1 = -x_{1p} + x_{1n} + x_3 + 7$
 $H2 = x_{1p} - x_{1n} - x_3 - 7$
 $H3 = 3x_{1p} - 3x_{1n} + x_{2p} - x_{2n} - 24$
 $H4 = x_{1p} - x_{1n} + 2x_{2p} - 2x_{2n} + x_3 - 18$
 $x_3 \geq 0, x_{1p}, x_{1n}, x_{2p} + x_{2n}, H1 \geq 0, H2 \geq 0, H3 \geq 0, H4 \geq 0$
- (B)** maximize $-2x_{1p} + 2x_{1n} - 7x_{2p} + 7x_{2n} - x_3$
subject to
 $H1 = -x_{1p} + x_{1n} + x_3 + 7$
 $H2 = x_{1p} - x_{1n} - x_3 - 7$
 $H3 = 3x_{1p} - 3x_{1n} + x_{2p} - x_{2n} - 24$
 $H4 = x_{1p} - x_{1n} + 2x_{2p} - 2x_{2n} + x_3 - 18$
 $x_3 \geq 0, x_{1p}, x_{1n}, x_{2p} + x_{2n}$
- (C)** maximize $-2x_{1p} + 2x_{1n} - 7x_{2p} + 7x_{2n} - x_3$
subject to
 $H1 = x_{1p} - x_{1n} - x_3 + 7$
 $H2 = x_{1p} - x_{1n} - x_3 - 7$
 $H3 = 3x_{1p} - 3x_{1n} + x_{2p} - x_{2n} - 24$
 $H4 = x_{1p} - x_{1n} + 2x_{2p} - 2x_{2n} + x_3 - 18$
 $x_3 \geq 0, x_{1p}, x_{1n}, x_{2p} + x_{2n}, H1 \geq 0, H2 \geq 0, H3 \geq 0, H4 \geq 0$
- (D)** maximize $-2x_{1p} + 2x_{1n} - 7x_{2p} + 7x_{2n} - x_3$
subject to
 $H1 = -x_{1p} + x_{1n} + x_3 + 7$
 $H2 = x_{1p} - x_{1n} - x_3 - 7$
 $H3 = -3x_{1p} + 3x_{1n} - x_{2p} + x_{2n} - 24$
 $H4 = x_{1p} - x_{1n} + 2x_{2p} - 2x_{2n} + x_3 - 18$
 $x_3 \geq 0, x_{1p}, x_{1n}, x_{2p} + x_{2n}, H1 \geq 0, H2 \geq 0, H3 \geq 0, H4 \geq 0$