

# Clase 4 LP - Forma estándar y variables de holgura-15-oct

Puntuación \_\_\_\_\_

1. Convertir el siguiente LP a forma estándar:

$$\begin{aligned} \text{minimize } & 2x_1 + 7x_2 + x_3 \\ \text{subject to } & x_1 - x_3 = 7 \\ & 3x_1 + x_2 \geq 24 \\ & x_1 + 2x_2 + x_3 \geq 18 \\ & x_3 \geq 0 \end{aligned}$$

**Ajuste de la función objetivo:**

- (A) 
$$\begin{aligned} \text{maximize } & -2x_1 - 7x_2 - x_3 \\ \text{subject to } & x_1 - x_3 = 7 \\ & 3x_1 + x_2 \geq 24 \\ & x_1 + 2x_2 + x_3 \geq 18 \\ & x_3 \geq 0 \end{aligned}$$
- (B) 
$$\begin{aligned} \text{maximize } & 2x_1 + 7x_2 + x_3 \\ \text{subject to } & x_1 - x_3 = 7 \\ & 3x_1 + x_2 \geq 24 \\ & x_1 + 2x_2 + x_3 \geq 18 \\ & x_3 \geq 0 \end{aligned}$$
- (C) 
$$\begin{aligned} \text{minimize } & -2x_1 - 7x_2 - x_3 \\ \text{subject to } & x_1 - x_3 = 7 \\ & 3x_1 + x_2 \geq 24 \\ & x_1 + 2x_2 + x_3 \geq 18 \\ & x_3 \geq 0 \end{aligned}$$

**2.** Convertir el siguiente LP a forma estándar:

$$\begin{aligned} & \text{maximize } -2x_1 - 7x_2 - x_3 \\ & \text{subject to } x_1 - x_3 = 7 \\ & \quad 3x_1 + x_2 \geq 24 \\ & \quad x_1 + 2x_2 + x_3 \geq 18 \\ & \quad x_3 \geq 0 \end{aligned}$$

**Ajuste de restricciones "mayor o igual" (excepto las de no negatividad)**

(A)  $\begin{aligned} & \text{maximize } -2x_1 - 7x_2 - x_3 \\ & \text{subject to } x_1 - x_3 = 7 \\ & \quad 3x_1 + x_2 \leq -24 \\ & \quad x_1 + 2x_2 + x_3 \leq -18 \\ & \quad x_3 \geq 0 \end{aligned}$

(B)  $\begin{aligned} & \text{maximize } -2x_1 - 7x_2 - x_3 \\ & \text{subject to } x_1 - x_3 = 7 \\ & \quad 3x_1 + x_2 \geq 24 \\ & \quad -x_1 - 2x_2 - x_3 \leq -18 \\ & \quad x_3 \geq 0 \end{aligned}$

(C)  $\begin{aligned} & \text{maximize } -2x_1 - 7x_2 - x_3 \\ & \text{subject to } x_1 - x_3 = 7 \\ & \quad -3x_1 - x_2 \leq -24 \\ & \quad -x_1 - 2x_2 - x_3 \leq -18 \\ & \quad x_3 \geq 0 \end{aligned}$

(D)  $\begin{aligned} & \text{maximize } -2x_1 - 7x_2 - x_3 \\ & \text{subject to } x_1 - x_3 = 7 \\ & \quad -3x_1 - x_2 \leq -24 \\ & \quad x_1 + 2x_2 + x_3 \geq 18 \\ & \quad x_3 \geq 0 \end{aligned}$

**3.** Convertir el siguiente LP a forma estándar :

maximize  $-2x_1 - 7x_2 - x_3$   
subject to:  $x_1 - x_3 = 7$   
 $-3x_1 - x_2 \leq -24$   
 $-x_1 - 2x_2 - x_3 \leq -18$   
 $x_3 \geq 0$

**Ajuste de restricciones "de igualdad"**

(A) maximize  $-2x_1 - 7x_2 - x_3$

subject to:  $x_1 - x_3 \leq 7$   
 $-3x_1 - x_2 \leq -24$   
 $-x_1 - 2x_2 - x_3 \leq -18$   
 $x_3 \geq 0$

(B) maximize  $-2x_1 - 7x_2 - x_3$

subject to:  $x_1 - x_3 \leq 7$   
 $-x_1 + x_3 \leq -7$   
 $-3x_1 - x_2 \leq -24$   
 $-x_1 - 2x_2 - x_3 \leq -18$   
 $x_3 \geq 0$

(C) maximize  $-2x_1 - 7x_2 - x_3$

subject to:  $x_1 - x_3 \geq 7$   
 $-x_1 + x_3 \leq 7$   
 $-3x_1 - x_2 \leq -24$   
 $-x_1 - 2x_2 - x_3 \leq -18$   
 $x_3 \geq 0$

- 4.** Convertir el siguiente LP a forma estándar:

maximize  $-2x_1 - 7x_2 - x_3$

subject to:

$$\begin{aligned}x_1 - x_3 &\leq 7 \\-x_1 + x_3 &\leq -7 \\-3x_1 - x_2 &\leq -24 \\-x_1 - 2x_2 - x_3 &\leq -18 \\x_3 &\geq 0\end{aligned}$$

**Ajuste de restricciones "de no negatividad para x1"**

- (A) maximize  $2x_{1p} + 2x_{1n} - 7x_2 - x_3$

subject to:

$$\begin{aligned}x_{1p} - x_{1n} - x_3 &\leq 7 \\x_{1p} - x_{1n} + x_3 &\leq -7 \\-3x_{1p} + 3x_{1n} - x_2 &\leq -24 \\-x_{1p} + x_{1n} - 2x_2 - x_3 &\leq -18 \\x_3 &\geq 0\end{aligned}$$

- (B) maximize  $-2x_{1p} + 2x_{1n} - 7x_2 - x_3$

subject to:

$$\begin{aligned}x_{1p} - x_{1n} - x_3 &\leq 7 \\-x_{1p} + x_{1n} + x_3 &\leq -7 \\3x_{1p} + 3x_{1n} - x_2 &\leq -24 \\-x_{1p} + x_{1n} - 2x_2 - x_3 &\leq -18 \\x_3 &\geq 0; \quad x_{1p} \geq 0, x_{1n} \geq 0\end{aligned}$$

- (C) maximize  $-2x_{1p} + 2x_{1n} - 7x_2 - x_3$

subject to:

$$\begin{aligned}x_{1p} - x_{1n} - x_3 &\leq 7 \\-x_{1p} - x_{1n} + x_3 &\leq -7 \\-3x_{1p} - 3x_{1n} - x_2 &\leq -24 \\-x_{1p} - x_{1n} - 2x_2 - x_3 &\leq -18 \\x_3 &\geq 0; \quad x_{1p} \geq 0, x_{1n} \geq 0\end{aligned}$$

- (D) maximize  $-2x_{1p} + 2x_{1n} - 7x_2 - x_3$

subject to:

$$\begin{aligned}x_{1p} - x_{1n} - x_3 &\leq 7 \\-x_{1p} + x_{1n} + x_3 &\leq -7 \\-3x_{1p} + 3x_{1n} - x_2 &\leq -24 \\-x_{1p} + x_{1n} - 2x_2 - x_3 &\leq -18 \\x_3 &\geq 0; \quad x_{1p} \geq 0, x_{1n} \geq 0\end{aligned}$$

**5.** Convertir el siguiente LP a forma estándar:

maximize  $-2x_1p + 2x_1n - 7x_2 - x_3$

subject to:

$$\begin{aligned} x_1p - x_1n - x_3 &\leq 7 \\ -x_1p + x_1n + x_3 &\leq -7 \\ -3x_1p + 3x_1n - x_2 &\leq -24 \\ -x_1p + x_1n - 2x_2 - x_3 &\leq -18 \\ x_3 &\geq 0; \quad x_1p \geq 0, \quad x_1n \geq 0 \end{aligned}$$

**Ajuste de restricciones "de no negatividad para x2"**

(A) maximize  $-2x_1p + 2x_1n - 7x_2p + 7x_2n - x_3$

subject to :

$$\begin{aligned} x_1p - x_1n - x_3 &\leq 7 \\ -x_1p + x_1n + x_3 &\leq -7 \\ -3x_1p + 3x_1n - x_2p + x_2n &\leq -24 \\ -x_1p + x_1n - 2x_2p + 2x_2n - x_3 &\leq -18 \\ x_3 &\geq 0, \quad x_1p \geq 0, \quad x_1n \geq 0 \end{aligned}$$

(B) maximize  $-2x_1p + 2x_1n - 7x_2p + 7x_2n - x_3$

subject to :

$$\begin{aligned} x_1p - x_1n - x_3 &\leq 7 \\ -x_1p + x_1n + x_3 &\leq -7 \\ -3x_1p + 3x_1n - x_2p + x_2n &\leq -24 \\ -x_1p + x_1n - 2x_2p + 2x_2n - x_3 &\leq -18 \\ x_3 &\geq 0, \quad x_1p \geq 0, \quad x_1n \geq 0, \quad x_2p \geq 0, \quad x_2n \geq 0 \end{aligned}$$

(C) maximize  $-2x_1p + 2x_1n - 7x_2p - 7x_2n - x_3$

subject to :

$$\begin{aligned} x_1p - x_1n - x_3 &\leq 7 \\ -x_1p + x_1n + x_3 &\leq -7 \\ -3x_1p + 3x_1n - x_2p + x_2n &\leq -24 \\ -x_1p + x_1n - 2x_2p + 2x_2n - x_3 &\leq -18 \\ x_3 &\geq 0, \quad x_1p \geq 0, \quad x_1n \geq 0, \quad x_2p \geq 0, \quad x_2n \geq 0 \end{aligned}$$

(D) maximize  $-2x_1p + 2x_1n - 7x_2p + 7x_2n - x_3$

subject to :

$$\begin{aligned} x_1p - x_1n - x_3 &\leq 7 \\ -x_1p + x_1n + x_3 &\leq -7 \\ -3x_1p + 3x_1n + x_2p + x_2n &\leq -24 \\ -x_1p + x_1n - 2x_2p - 2x_2n - x_3 &\leq -18 \\ x_3 &\geq 0, \quad x_1p \geq 0, \quad x_1n \geq 0, \quad x_2p \geq 0, \quad x_2n \geq 0 \end{aligned}$$

6. Convertir el siguiente LP a forma estándar con variables de holgura:

maximize  $-2x_1p + 2x_1n - 7x_2p + 7x_2n - x_3$   
 subject to :  
 $x_1p - x_1n - x_3 \leq 7$   
 $-x_1p + x_1n + x_3 \leq -7$   
 $-3x_1p + 3x_1n - x_2p + x_2n \leq -24$   
 $-x_1p + x_1n - 2x_2p + 2x_2n - x_3 \leq -18$   
 $x_3 \geq 0, x_1p, x_1n, x_2p \geq 0, x_2n \geq 0$

**Adición de variables de holgura.**

- (A) maximize  $-2x_1p + 2x_1n - 7x_2p + 7x_2n - x_3$   
 subject to  
 $H1 = -x_1p + x_1n + x_3 + 7$   
 $H2 = x_1p - x_1n - x_3 - 7$   
 $H3 = 3x_1p - 3x_1n + x_2p - x_2n - 24$   
 $H4 = x_1p - x_1n + 2x_2p - 2x_2n + x_3 - 18$   
 $x_3 \geq 0, x_1p, x_1n, x_2p + x_2n, H1 \geq 0, H2 \geq 0, H3 \geq 0, H4 \geq 0$
- (B) maximize  $-2x_1p + 2x_1n - 7x_2p + 7x_2n - x_3$   
 subject to  
 $H1 = -x_1p + x_1n + x_3 + 7$   
 $H2 = x_1p - x_1n - x_3 - 7$   
 $H3 = 3x_1p - 3x_1n + x_2p - x_2n - 24$   
 $H4 = x_1p - x_1n + 2x_2p - 2x_2n + x_3 - 18$   
 $x_3 \geq 0, x_1p, x_1n, x_2p + x_2n$
- (C) maximize  $-2x_1p + 2x_1n - 7x_2p + 7x_2n - x_3$   
 subject to  
 $H1 = x_1p - x_1n - x_3 + 7$   
 $H2 = x_1p - x_1n - x_3 - 7$   
 $H3 = 3x_1p - 3x_1n + x_2p - x_2n - 24$   
 $H4 = x_1p - x_1n + 2x_2p - 2x_2n + x_3 - 18$   
 $x_3 \geq 0, x_1p, x_1n, x_2p + x_2n, H1 \geq 0, H2 \geq 0, H3 \geq 0, H4 \geq 0$
- (D) maximize  $-2x_1p + 2x_1n - 7x_2p + 7x_2n - x_3$   
 subject to  
 $H1 = -x_1p + x_1n + x_3 + 7$   
 $H2 = x_1p - x_1n - x_3 - 7$   
 $H3 = -3x_1p + 3x_1n - x_2p + x_2n - 24$   
 $H4 = x_1p - x_1n + 2x_2p - 2x_2n + x_3 - 18$   
 $x_3 \geq 0, x_1p, x_1n, x_2p + x_2n, H1 \geq 0, H2 \geq 0, H3 \geq 0, H4 \geq 0$