



ĐẠI HỌC ĐÀ NẴNG

TRƯỜNG ĐẠI HỌC CÔNG NGHỆ THÔNG TIN VÀ TRUYỀN THÔNG VIỆT - HÀN

Vietnam - Korea University of Information and Communication Technology

Chapter 1:

Introduction to Computers and Programming

Trịnh Thị Ngọc Linh

1.8

Number systems

Number systems

- A number system is defined as the representation of numbers by using digits or other symbols in a consistent manner.
- It is also called the system of numeration.

Types of Number Systems

- There are different types of number systems.
- Four main types are:
 - Binary number system (Base - 2)
 - Octal number system (Base - 8)
 - Decimal number system (Base - 10)
 - Hexadecimal number system (Base - 16)

Binary Number System

- The numbers in this system have a base of 2.
- The binary number system uses only two digits: 0 and 1.
- Digits 0 and 1 are called bits and 8 bits together make a byte. The data in computers is stored in terms of bits and bytes.
- For example: 10001_2 111101_2

Octal Number System

- The numbers in this system have a base of 8.
- The octal number system uses eight digits: 0, 1, 2, 3, 4, 5, 6, 7.
- For example:

35_8

141_8

Decimal Number System

- The numbers in this system have a base of 10.
- The decimal number system uses ten digits: 0, 1, 2, 3, 4, 5, 6, 7, 8, 9.
- The decimal number system is the system that we generally use to represent numbers in real life
- For example: 723_{10} 32_{10} 4257_{10}

Hexadecimal Number System

- The numbers in this system have a base of 16.
- The hexadecimal number system uses sixteen digits/alphabets:
0, 1, 2, 3, 4, 5, 6, 7, 8, 9
A, B, C, D, E, F (the numbers 10-15)
- For example: $7B3_{16}$ $6F_{16}$ $4B2A_{16}$

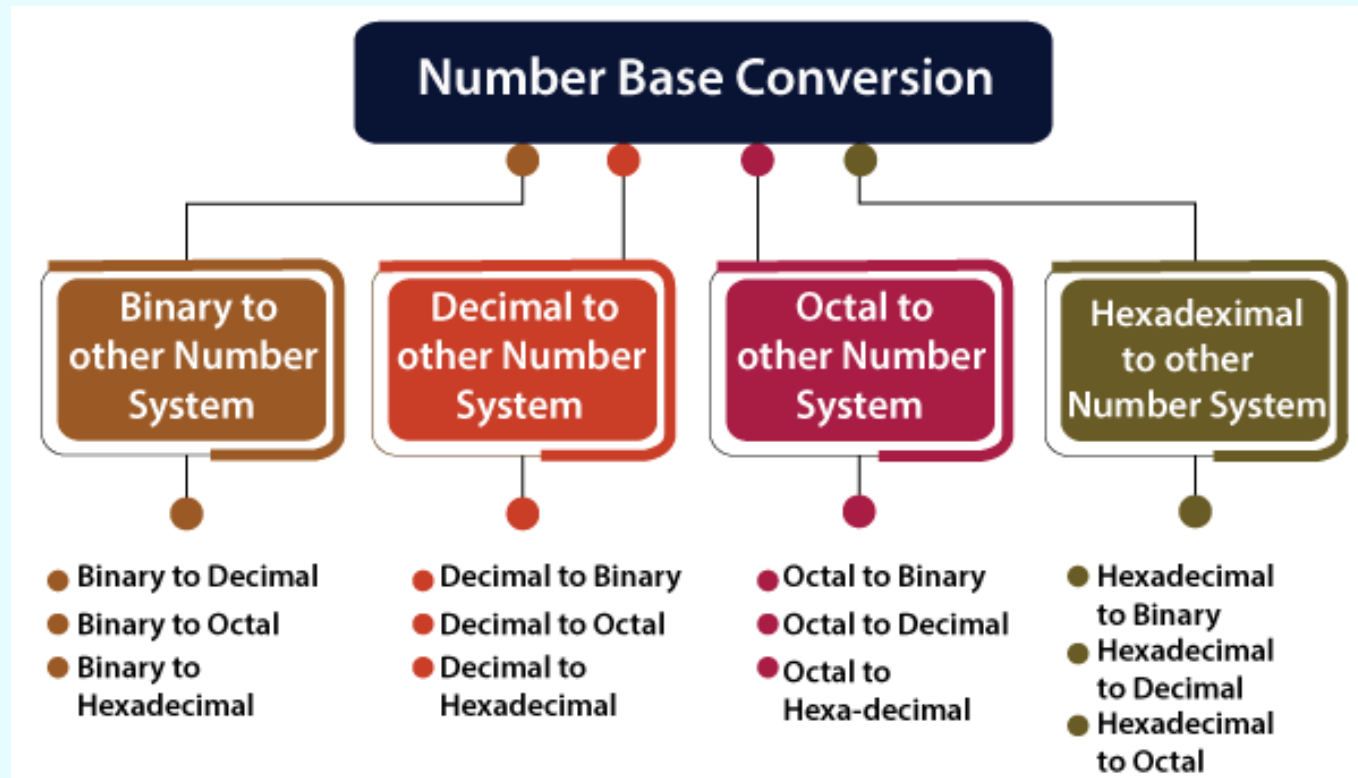
Number systems

Number Systems		
System	Base	Digits
Binary	2	0 1
Octal	8	0 1 2 3 4 5 6 7
Decimal	10	0 1 2 3 4 5 6 7 8 9
Hexadecimal	16	0 1 2 3 4 5 6 7 8 9 A B C D E F

Decimal Base-10	Binary Base-2	Octal Base-8	Hexa Decimal Base-16
0	0	0	0
1	1	1	1
2	10	2	2
3	11	3	3
4	100	4	4
5	101	5	5
6	110	6	6
7	111	7	7
8	1000	10	8
9	1001	11	9
10	1010	12	A
11	1011	13	B
12	1100	14	C
13	1101	15	D
14	1110	16	E
15	1111	17	F
16	10000	20	10

Conversion Rules of Number Systems

- A number can be converted from one number system to another number system.

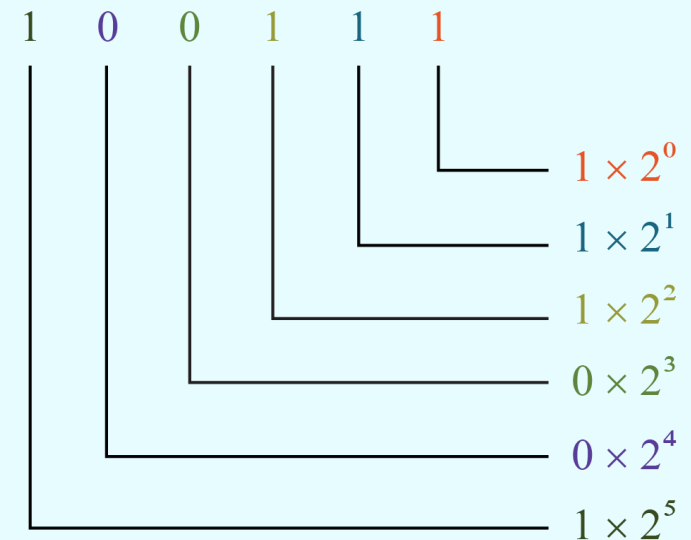


Conversion of Number Systems to Decimal Number System

- Example: Convert 100111_2 into the decimal system.
- Step 1: Identify the base of the given number.
- Here, the base of 100111_2 is 2.

Conversion of Number Systems to Decimal Number System

- Step 2:
 - Multiply each digit of the given number, starting from the rightmost digit, with the exponents of the base.
 - The exponents should start with 0 and increase by 1 every time as we move from right to left.



Conversion of Number Systems to Decimal Number System

- Step 3: We just simplify each of the above products and add them.

1	0	0	1	1	1	
						$1 \times 2^0 = 1 \times 1 = 1$
						$1 \times 2^1 = 1 \times 2 = 2$
						$1 \times 2^2 = 1 \times 4 = 4$
						$0 \times 2^3 = 0 \times 8 = 0$
						$0 \times 2^4 = 0 \times 16 = 0$
						$1 \times 2^5 = 1 \times 32 = 32$
						<hr/>
						Sum: 39

$$100111_2 = 39_{10}$$

Conversion of Number Systems to Decimal Number System

- We can use the following steps to make this process simplified.

$$\begin{aligned}100111_2 &= (1 \times 2^5) + (0 \times 2^4) + (0 \times 2^3) + (1 \times 2^2) + (1 \times 2^1) + (1 \times 2^0) \\&= (1 \times 32) + (0 \times 16) + (0 \times 8) + (1 \times 4) + (1 \times 2) + (1 \times 1) \\&= 32 + 0 + 0 + 4 + 2 + 1 \\&= 39_{10}\end{aligned}$$

Conversion of Decimal Number System to Other Number Systems

- Example: Convert 4320_{10} into the octal system
- Step 1: Identify the base of the required number.
- The base of the required number is 8

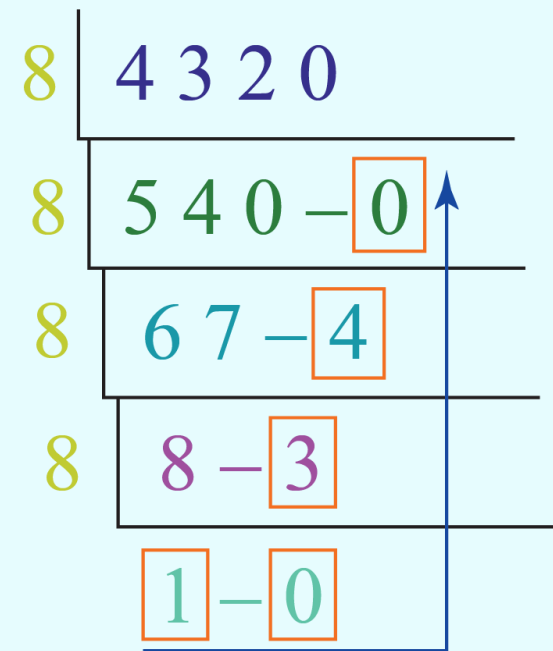
Conversion of Decimal Number System to Other Number Systems

- Step 2:
 - Divide the given number by the base of the required number and note down the quotient and the remainder in the quotient-remainder form.
 - Repeat this process (dividing the quotient again by the base) until we get the quotient to be less than the base.

$$\begin{array}{r|l} 8 & 4320 \\ \hline 8 & 540 - 0 \\ \hline 8 & 67 - 4 \\ \hline 8 & 8 - 3 \\ \hline & 1 - 0 \end{array}$$

Conversion of Decimal Number Systems to Other Number Systems

- Step 3: The required number in the octal number system is obtained just by reading all the remainders and the last quotient from bottom to top.



$$4320_{10} = 10340_8$$

Conversion of Decimal Number Systems to Other Number Systems

- Example: $2020.65625_{10} \rightarrow (?)_{16}$

For Real Part: The real part is 2020_{10}

We convert the real part from base 10 to base 16 using division method same as above.

So, $2020_{10} = 7E4_{16}$

For Fractional Part: The fractional part is 0.65625_{10}

We convert the fractional part from base 10 to base 16 using multiplication method.

	Real part	Fractional Part
0.65625×16	$10 = A$	0.5
0.5×16	8	0.0

Combining the result of real and fractional parts:
 $2020.65625_{10} = 7E4.A8_{16}$

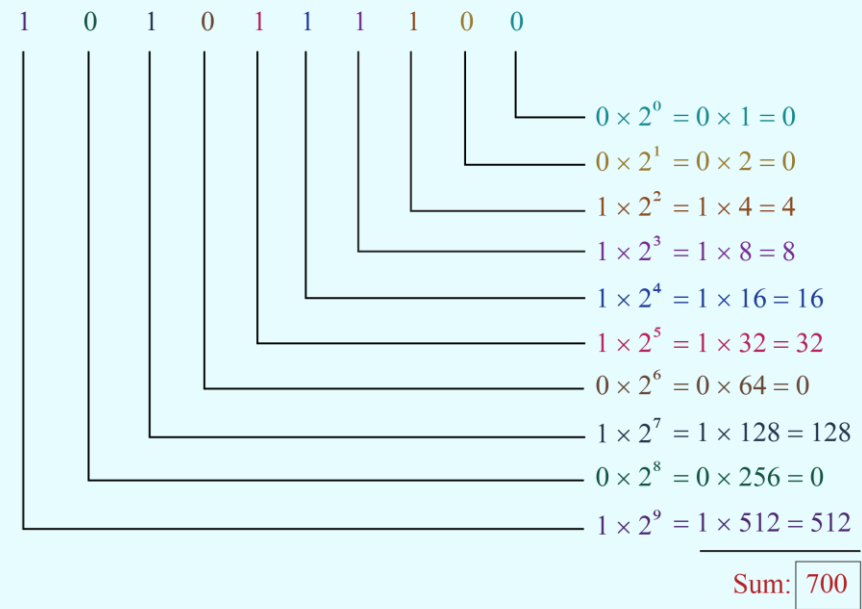
From here, $0.65625_{10} = 0.A8_{16}$

Conversion from One Number System to Another Number System

- To convert a number from one of the binary/octal/hexadecimal systems to one of the other systems:
 - Step 1: We first convert it into the decimal system.
 - Step 2: We convert it to the required systems.

Conversion from One Number System to Another Number System

- Example: Convert 1010111100_2 to the hexadecimal system.
- Step 1: Convert this number to the decimal number system as explained in the above process.



$$1010111100_2 = 700_{10}$$

Conversion from One Number System to Another Number System

- Step 2: Convert the above number (which is in the decimal system), into the required number system.

A handwritten diagram showing the conversion of the decimal number 700 to hexadecimal. It consists of three rows of numbers, each preceded by a vertical line and the number 16. The first row contains '7 0 0'. The second row contains '4 3 - 12 (or) C', with 'C' enclosed in an orange box. The third row contains '2 - 11 (or) B', with '2' and 'B' enclosed in orange boxes. A blue arrow points upwards from the 'B' box to the 'C' box. Below the rows, the equation $700_{10} = 2BC_{16}$ is written.

$$700_{10} = 2BC_{16}$$

$$\begin{aligned} 1010111100_2 &= 700_{10} \\ 700_{10} &= 2BC_{16} \\ \Rightarrow 1010111100_2 &= 2BC_{16} \end{aligned}$$

21

1.9

Algorithm

What is Algorithm?

- An algorithm is a procedure or formula for solving a problem, based on conducting a sequence of specified actions.
- For an algorithm to be useful, it must satisfy five properties:
 - The inputs must be specified.
 - The outputs must be specified.
 - Definiteness.
 - Effectiveness.
 - Finiteness.

What is Algorithm?

- How can we create an algorithm to show the steps in getting ready for school?
 - Get out of bed.
 - Take a shower and clean teeth.
 - Get dressed.
 - Turn on the kettle.
 - Put bread in the toaster and turn it on.
 - Wait for the kettle to boil and make tea.
 - Wait for bread to toast, butter it and add Jam.
 - Drink tea and eat toast.
 - Gather school books and put in bag.
 - Put on shoes and coat.
 - Leave the house.

What is Algorithm?

- Build a program:
 - Problem definition
 - Requirement analysis
 - Build the algorithms
 - Coding
 - Testing and debugging
 - Maintenance
 - Documentation

Algorithm development process

- Algorithm development process consists of five major steps:
 - Step 1: Obtain a description of the problem.
 - Step 2: Analyze the problem.
 - Step 3: Develop a high-level algorithm.
 - Step 4: Refine the algorithm by adding more detail.
 - Step 5: Review the algorithm.

Presentation of Algorithm

- There are two main ways that algorithms can be represented:
 - Pseudocode
 - Pseudocode is a plain language description of the steps in an algorithm.
 - It uses programming-style constructs, but is not written in an actual programming language.
 - Flowchart
 - Flowcharts can be used to represent algorithms visually.
 - They use diagrams which use particular symbols to show the flow of data, processing and input/output that takes place within a program or task.

Pseudocode

- Example 1: Add two numbers entered by the user

Step 1: Start

Step 2: Declare variables num1, num2 and sum.

Step 3: Read values num1 and num2.

Step 4: Add num1 and num2 and assign the result to sum.

$\text{sum} \leftarrow \text{num1} + \text{num2}$

Step 5: Display sum

Step 6: Stop

Pseudocode

- Example 2: Find the largest number among three numbers

Step 1: Start

Step 2: Declare variables a,b and c.

Step 3: Read variables a,b and c.

Step 4:

if ((a >= b) && (a >= c))

 Display a is the largest number.

if ((b >= a) && (b >= c))

 Display b is the largest number.

if ((c >= a) && (c >= b))

 Display c is the largest number.

Step 5: Stop

Step 1: Start

Step 2: Declare variables a,b and c.

Step 3: Read variables a,b and c.

Step 4:

if (a >= b)

 if (a >= c)

 Display a is the largest number.

 else

 Display c is the largest number

else

 if (b >= c)

 Display b is the largest number.

 else

 Display c is the largest number.

Step 5: Stop

Pseudocode

- Example 3:
Check
whether a
number is
prime or not

Step 1: Start

Step 2: Declare variables n , i , $flag$.

Step 3: Initialize variables

$flag \leftarrow 1$

$i \leftarrow 2$

Step 4: Read n from the user.

Step 5: If $n == 2$

$flag \leftarrow 0$

Go to step 7

else

Go to step 6

Step 6: Repeat the steps until $i=(n/2)$

6.1 If remainder of $n \div i$ equals 0

$flag \leftarrow 0$

Go to step 7

6.2 $i \leftarrow i+1$

Step 7: If $flag = 0$

Display n is not prime

else

Display n is prime

Step 8: Stop

Pseudocode

- Example 4: Find the Fibonacci series till the term less than 1000

Step 1: Start

Step 2: Declare variables first_term, second_term, temp.

Step 3: Initialize variables first_term \leftarrow 0, second_term \leftarrow 1

Step 4: Display first_term and second_term

Step 5: Repeat the steps while second_term \leq 1000

5.1: temp \leftarrow second_term

5.2: second_term \leftarrow second_term + first_term

5.3: first_term \leftarrow temp

5.4: Display second_term

Step 6: Stop

Flowchart

This represents the start or end point of the flowchart.



You use this to represent data input or data output.



You use this where a decision has to be made. It is also called selection and will contain a question.

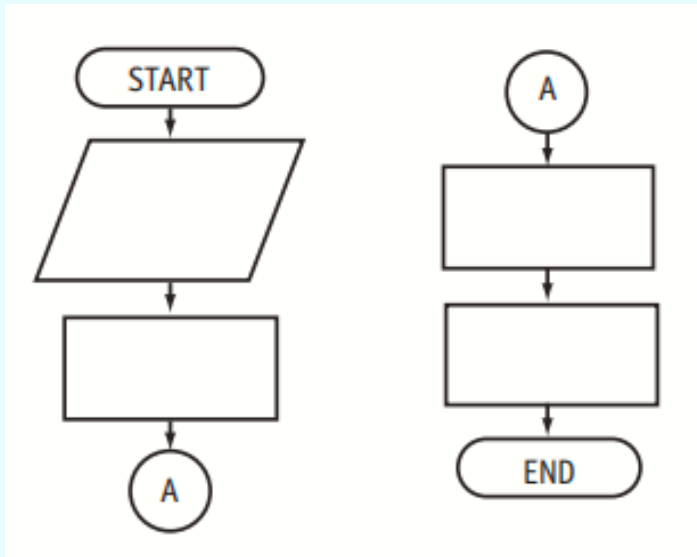


You use this to represent a process that must be carried out by the algorithm.

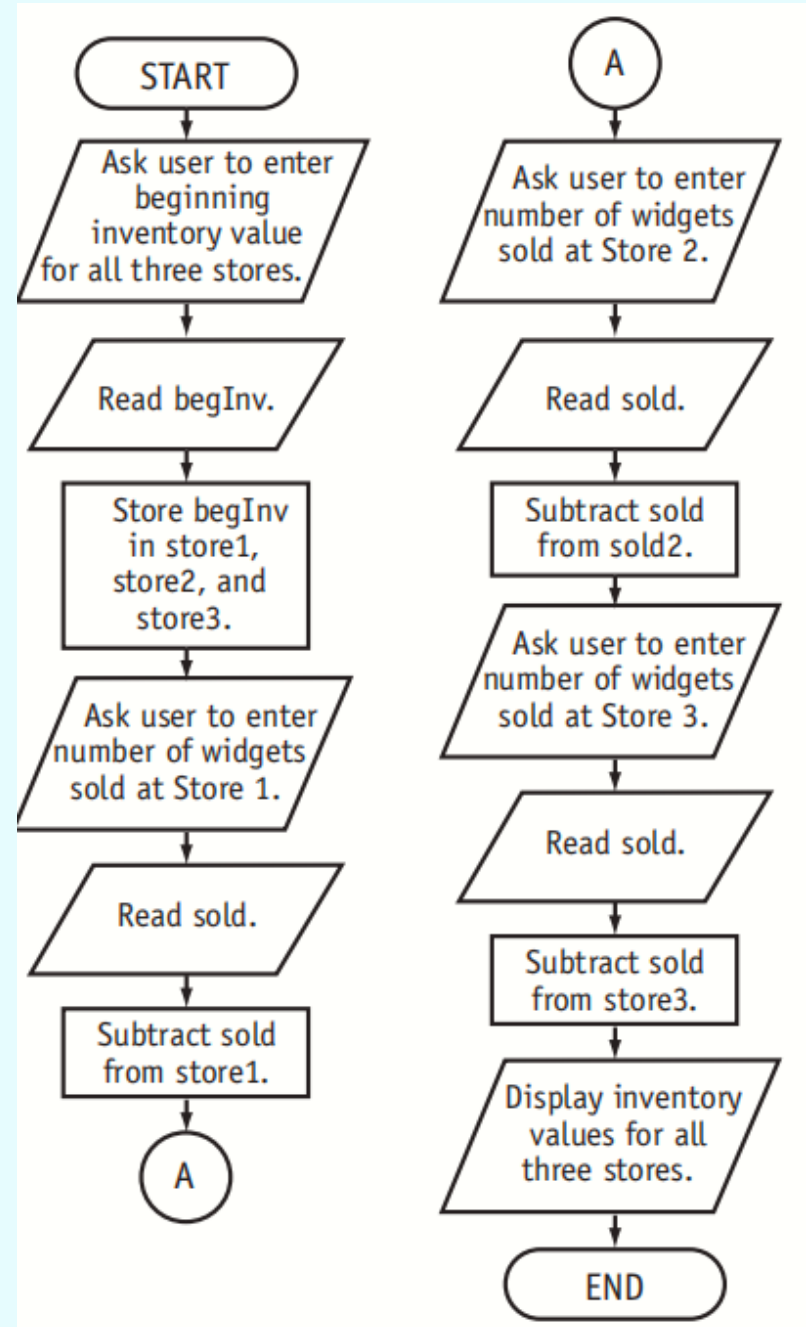


Flowchart

- Connectors



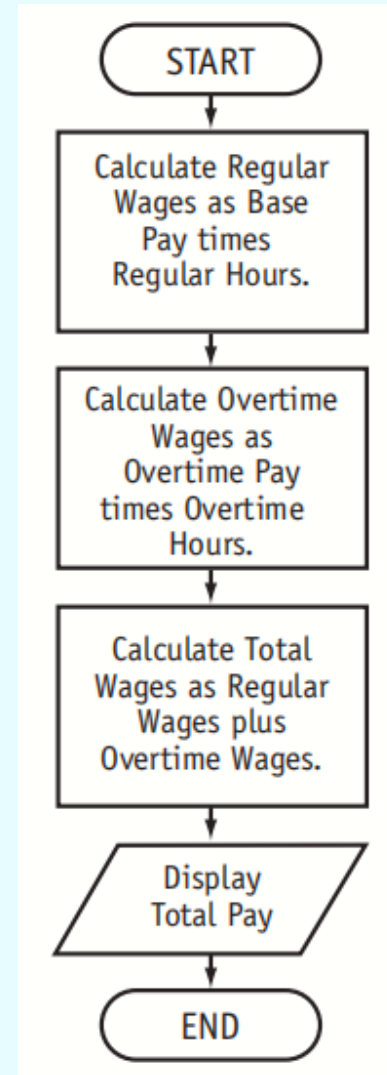
Example 5



Flowchart

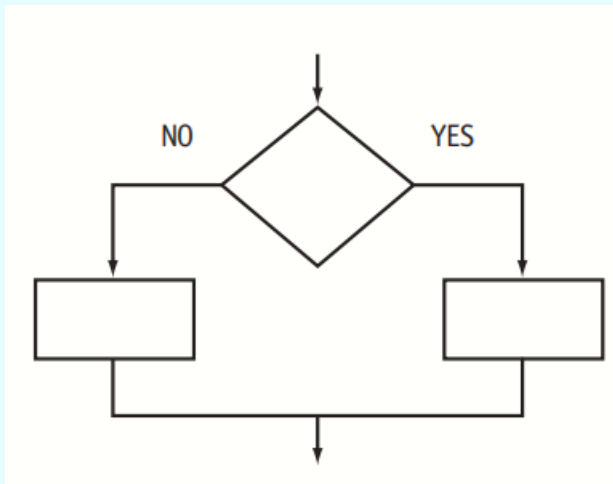
- The Sequence structure

Example 6

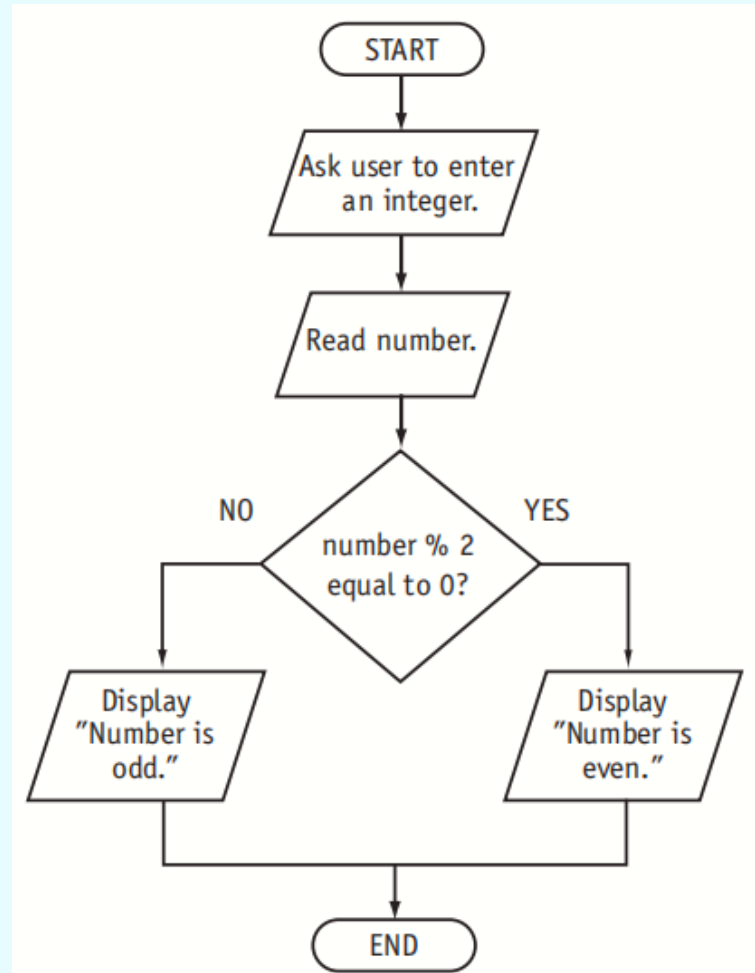


Flowchart

- The Decision Structure

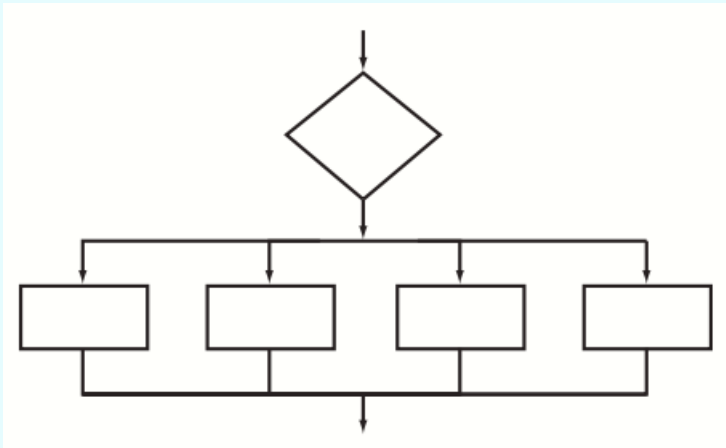


Example 7

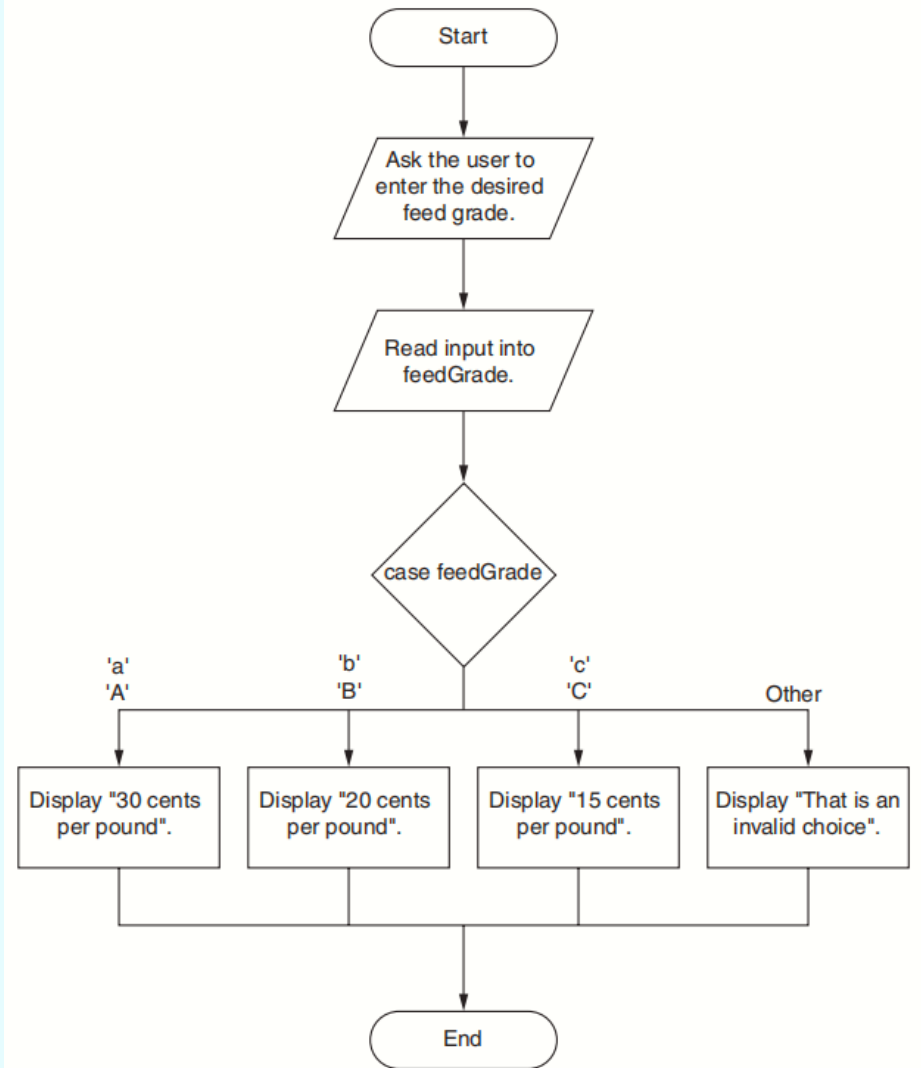


Flowchart

- The Case Structure



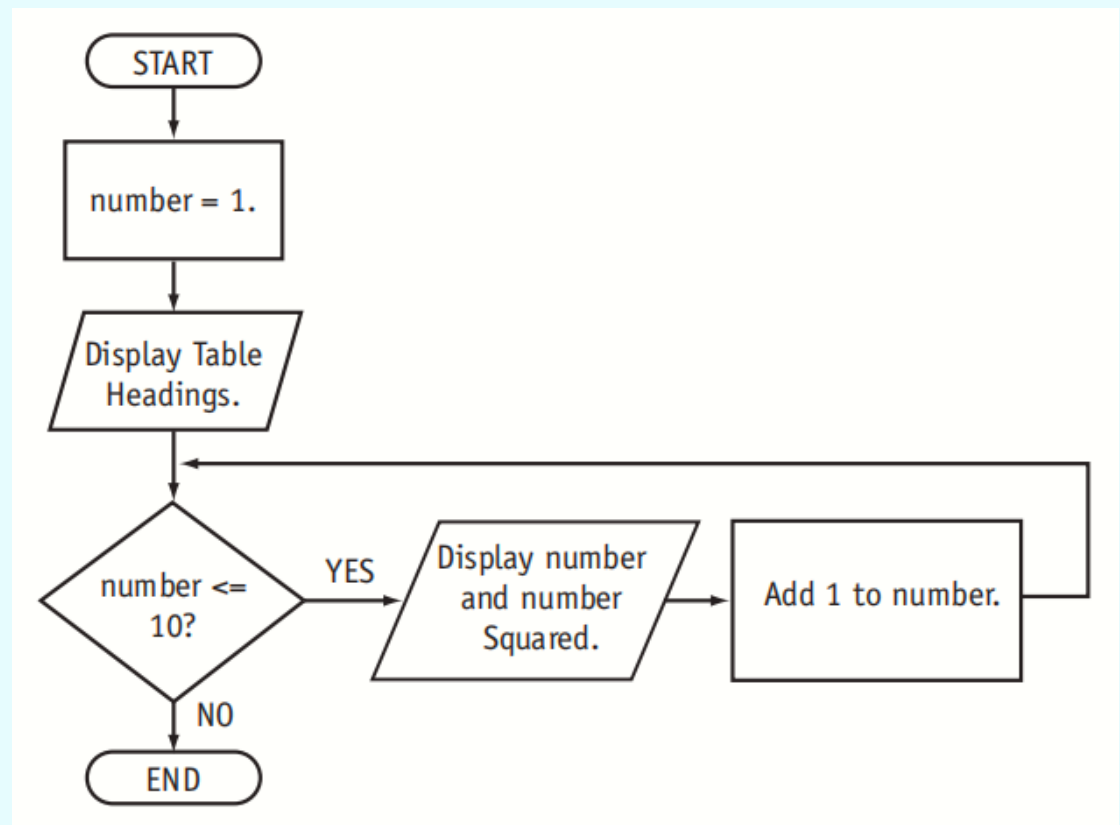
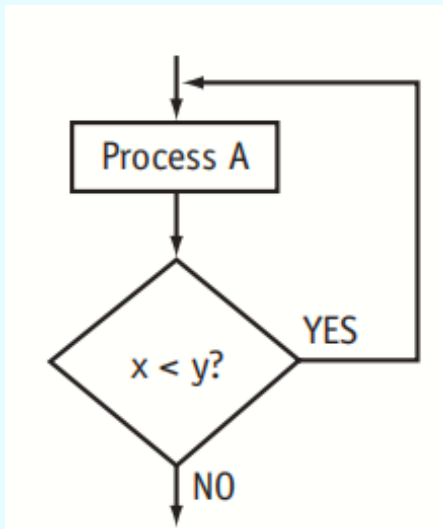
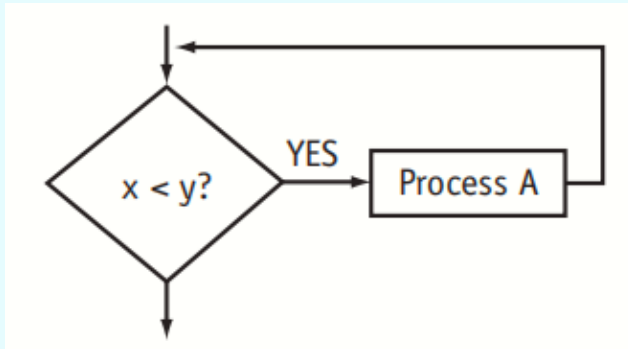
Example 8



Flowchart

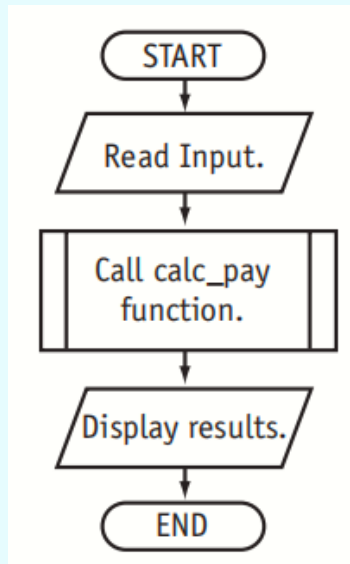
- Repetition Structures

Example 9



Flowchart

- Modules



Example 10

