

1 a) $5.75 = 0101.11$

$5 = 0101$

$\times 2$	0.75	0.11
	1.5	1
$\times 2$	1	1

decimal portion

convert whole # to binary $\rightarrow 5 = 101$

convert decimal to binary $\rightarrow 0.75 = 0.11$

combine both parts $\rightarrow 5.75 = 101.11$

b) $\frac{63}{64} = 100\ 0000.1111\ 11$

$2^6 = 64 = 0100\ 0000$

$63 = 0011\ 1111$

combine both parts with

$64 = \text{whole \#}, 63 = \text{fraction}$

$\rightarrow 100\ 0000.1111\ 11$

$\times 2$	0.984375	0.111111
	1.96875	1
$\times 2$	1.9375	1
	1.875	1
	1.75	1
	1.5	1
	1	1

decimal portion

c) $9.8125 = 1001.1101$

$9 = 1001$ 0.8125 0.1101

1.625 1

1.25 1

0.5 0

1 1

same steps as 1a)

$9 = 1001$

$0.8125 = 0.1101$

2 34.890625

sign = positive = 0 0.890625 0.111001

34 = 1000 10 1.78125 1

0.890625 = 0.111001 1.5625 1

1.125 1

combine whole # 0.25 0

and fraction 0.5 0

→ 1000 10.111001

move decimal point till only single leading 1

→ 1.00010111001 × 2⁵

get exponent by adding 127 to the exponent of 2

converting to binary → 5 + 127 = 132

132 = 1000 0100

mantissa = binary fraction portion

combine all parts

→ 0 1000 0100 0001 0111 001 0-0
 ^ next all zero's

3 sign = 0 = positive

convert exponent to decimal, then subtract 127

$$\rightarrow 01111011 = 123, 123 - 127 = -4$$

convert mantissa to decimal $\rightarrow 0.00000000 = 0.0$

add leading 1 to mantissa $\rightarrow 1.0$

multiply mantissa by 2^{exponent}

$$\rightarrow 1 \times 2^{-4} = \boxed{0.0625}$$

4 denormalized # is when the exponent is all 0's

but the mantissa isn't. You assume the smallest exponent but without the leading 1.

$$15 - 0 = -15 \text{ but assume exponent} = -14$$

smallest normalized #:

$$* 0000000000000001 = 2^{-14}$$

$$= 0.00006103515$$

largest denormalized #:

$$* 00000111111111 = (1 - 2^{-10}) \times 2^{-14}$$

$$= 0.00006047555$$

$$2^{-14} - (1 - 2^{-10}) \times 2^{-14}$$

$$= 0.0000000596$$