

a.

$$0-180^\circ) M_z^0$$

$$0+180^\circ) -M_z^0$$

$$1-\theta) M_z' = M_z^0 (1 - 2e^{-T_z/T_1})$$

$$1+\theta) M_z' = M_z^0 (1 - 2e^{-T_z/T_1}) \cos \theta$$

In steady state; $M_z^{(n)}(0-) = M_z^{(n-1)}(0-) = M_z^{ss}(0-)$

$$1-180^\circ) M_z' = M_z^0 (1 - e^{-(T_R - T_z)/T_1})$$

$$2+180^\circ) M_z' = -M_z^0 (1 - e^{-(T_R - T_z)/T_1})$$

$$3-180^\circ) M_z' = M_z^0 (1 - 2e^{-T_z/T_1} + e^{-T_R/T_1})$$

$$3+180^\circ) M_z' = M_z^0 (1 - 2e^{-T_z/T_1} + e^{-T_R/T_1}) \cos \theta$$

$$M_z^{(n)}(0-) = M_z^{ss(n)}(0-) = M_z^{ss(n-1)}(0-) = M_z^0 (1 - 2e^{-T_z/T_1} \cos \theta + e^{-T_R/T_1})$$

$$\therefore M_z^{ss(n)}(0-) = \frac{M_z^0 (1 - 2e^{-T_z/T_1} + e^{-T_R/T_1})}{1 - e^{-T_R/T_1} \cos \theta}$$

$$\therefore M_{xy}^{(n)}(0-) = \frac{M_z^0 (1 - 2e^{-T_z/T_1} + e^{-T_R/T_1}) \sin \theta}{1 - e^{-T_R/T_1} \cos \theta}$$

b. $\therefore \frac{dM_{xy}}{dt} = \frac{M_z^0 (1 - 2e^{-T_z/T_1} + e^{-T_R/T_1}) [\cos \theta - e^{-T_R/T_1}]}{(1 - e^{-T_R/T_1} \cos \theta)^2}$

let $\frac{dM_{xy}}{dt} = 0$. get $\theta = \arccos e^{-T_R/T_1}$

c. $T_1 = T_R$. $\theta = \arccos e^{-1} = 68.4^\circ$

d. $M_{xy} = \frac{M_z^0 (1 - 2e^{-T_z/T_1} + e^{-T_R/T_1})}{1 - e^{-2T_R/T_1}} \cdot \sqrt{1 - e^{-2T_R/T_1}}$

regular- $M_{xy} = M_z^0 (1 - 2e^{-T_z/T_1} + e^{-T_R/T_1})$

while $\alpha e^{-2T_R/T_1} < 1$ the M_{xy} is bigger.