# Package 'LPMachineLearning'

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Title Integrated Nonparametric Statistical Machine Learning

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Index

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<b>Description</b> Statistical modeling tools for converting a black-box ML algorithm into an interpretable conditional distribution prediction machine, which provides a wide range of facilities, including goodness-of-fit, various types of exploratory graphical diagnostics, generalized feature selection, predictive inference methods, and others. The primary reference is Mukhopadhyay, S. and Wang, K. (2020, Technical Report).
Imports graphics, methods, glmnet, caret, h2o, leaps, HDInterval, parallel
<b>Depends</b> R (>= 3.5.0),stats,orthopolynom
<b>License</b> Apache License (>= 2.0)
R topics documented:  LPMachineLearning-package
bone
bupa
DIF
HCA
rosnerFEV

**17** 

2 autompg

LPMachineLearning-package

Integrated Nonparametric Statistical Machine Learning

## Description

This package provides a unified interface to convert any black-box ML regression algorithms into an exploratory uncertainty prediction machine that is robust, interpretable, and scalable for large datasets. A large variety of modeling and predictive inference tasks can be done using the fitted model.

#### Author(s)

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#### References

Mukhopadhyay, S., and Wang, K (2020) "Statistical Machine Learning: An Integrated Approach". Technical Report.

autompg

Auto MPG data.

## Description

Modified Auto MPG data set based on the UCI Machine Learning Repository version (Bache and Lichman, 2013). we discarded examples with missing entries, ending up with 392 observations.

#### **Usage**

data(autompg)

#### **Format**

A data frame with 392 observations on the following 8 variables.

- x.cylinders Number of cylinders.
- x.displacement Engine displacement (cu. inches).
- x.horsepower Horsepower.
- x.weight Vehicle weight (lbs).
- x.acceleration Time to accelerate from O to 60 mph (seconds).
- x.model.year Model year (modulo 100).
- x.origin Origin of car (1. American, 2. European, 3. Japanese).
- y Miles per gallon.

baseball 3

baseball

Baseball data.

#### **Description**

Age and weight data for 1015 major league baseball players.

#### Usage

```
data(baseball)
```

#### **Format**

A data frame with 1015 observations on the following 2 variables.

x Age.

y Weight.

#### References

Matloff, N. (2017) "Statistical regression and classification: From linear models to machinelearning". Chapman and Hall/CRC.

bone

Bone mineral density data.

## Description

The data set contains measurements on the relative change in (spinal) bone mineral density over one year for 485 North American adolescents.

## Usage

data(bone)

#### **Format**

A data frame with 485 observations on the following 2 variables.

- x Age of the subject.
- y Relative change in (spinal) bone mineral density.

## References

Bachrach et al., (1999) "Bone mineral acquisition in healthy Asian, Hispanic, black, and Caucasian youth: a longitudinal study". The journal of clinical endocrinology & metabolism.

4 bupa

boxOffice

Movie Box-office Revenue Data

#### **Description**

Box-office revenues during opening and after the first week.

#### Usage

data(boxOffice)

#### **Format**

A data frame with 4031 observations on the following 2 variables.

- x Log of opening box-office revenues.
- y Log of box-office revenues after the first week.

#### References

Voudouris et al., (2012) "Modelling skewness and kurtosis with the BCPE density in GAMLSS". Journal of Applied Statistics, 39(6), 1279-1293.

bupa

BUPA liver disorders data.

## Description

A modified version of BUPA liver disorders data set, containing measurements of gamma-glutamyl transpeptidase (GGT) and alanine-aminotransferase (ALT) extracted from 345 male individuals' blood sample.

## Usage

data(bupa)

#### **Format**

A data frame with 345 observations on the following 2 variables.

- x Log of gamma-glutamyl transpeptidase.
- y Log of alanine-aminotransferase.

#### References

McDermott, J. & Forsyth, R.S. (2016) "Diagnosing a disorder in a classification benchmark". Pattern Recognition Letters, 73, 41-43.

butterfly 5

butterfly

The Butterfly data.

#### **Description**

The stylized simulated example used in our paper.

## Usage

```
data(butterfly)
```

#### **Format**

A data frame with 700 observations on 2 variables.

- x Values of covariate X.
- y Values of Y.

#### References

Mukhopadhyay, S., and Wang, K (2020) "Statistical Machine Learning: An Integrated Approach". Technical Report.

cholesterol

LDL cholesterol of Quail.

## Description

Completely randomized experiment investigating LDL (low-density lipoprotein) cholesterol in quails.

#### Usage

```
data(cholesterol)
```

## Format

A data frame with 39 observations on the following 2 variables.

- x Type of diet, each is mixed with a different drug compound.
- y Measurments of LDL cholesterol levels

## References

Hettmansperger, T. P. and J. W. McKean (2010), "Robust nonparametric statistical methods", CRC Press.

6 DIF

DIF	Distributional	<b>Impact</b>	Function.

## Description

This function deal with the "XYZ" problem where we observe covariates X, response Y and a binary treatment Z. The goal is capturing the heterogeneous impact from the treatment Z on the response Y, as a function of the covariate X.

## Usage

```
DIF(X, y, z, m = c(2, 4), X.test, method = "gbm", ...)
```

#### **Arguments**

Χ	A $n$ -by- $d$ feature matrix
У	A length $n$ vector of response.
z	A length $n$ binary vector. Indicating treatment.
m	An ordered pair $(m_1,m_2)$ . $m_1$ indicates how many LP-nonparametric basis to construct for each column of $X$ , $m_2$ indicates how many to construct for $y$ .
X.test	A $k$ -by- $d$ matrix providing $k$ sets of covariates for target cases to investigate.
method	Method for estimating the conditional LP-Fourier coefficients. Valid options: gbm and rf (both requires $h2o$ ).
	Extra parameters to pass into UPM.

#### Value

A list of values containing:

X.test	The X. test values of dimension $k$ -by- $d$ .
DIF	A vector of length $\boldsymbol{k}$ containing the DIF values for the X. test.
comp.DIF	A $k$ -by- $m_2$ matrix containing the components of DIF values.

## Author(s)

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## References

Mukhopadhyay, S., and Wang, K (2020) "Statistical Machine Learning: An Integrated Approach". Technical Report.

dutch 7

dutch Du	tch Boys BMI data
----------	-------------------

## **Description**

This dataset is a part of the Fourth Dutch Growth Study, which comprised of observations on age and BMI of 7294 Dutch boys. A slightly modified version that is available in gamlss.data package.

## Usage

```
data(dutch)
```

#### **Format**

A data frame with 7294 observations on the following 2 variables.

- x Subject age.
- y Subject BMI.

#### References

Fredriks et al., (2000) "Body index measurements in 1996-7 compared with 1980". Archives of disease in childhood 82(2), 107-112.

GSP

Generalized Shape Predictor.

## Description

Generalized shape predictors are those that influence the whole conditional distribution (beyond just mean) of the response Y. This function finds the most relevant attributes that are predictive for certain shapes (that user is interested in) of the conditional distribution  $f_{Y|X=x}(y)$ .

#### Usage

```
GSP(X, y, comp, mx = NULL)
```

## **Arguments**

Χ	A $n$ -by- $d$ feature matrix
У	A length $n$ vector of response.
comp	A length $l$ vector indicating the target order. comp=1 will identify the variables that affect the condtional mean of Y, comp=1:2 will find the variables that are informative for the location and scale, etc.
mx	Optional. The number of LP-nonparametric basis $\boldsymbol{m}$ to construct for each feature.

HCA

#### Value

A list of values containing:

coef A *m*-by-*l*-by-*d* array of coefficients. See example for details. signif.mat A binary matrix indicating the significant order features

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#### References

Mukhopadhyay, S., and Wang, K (2020) "Statistical Machine Learning: An Integrated Approach". Technical Report.

## **Examples**

```
data(autompg)
X<-autompg[,-8]
y<-autompg$y
GSP.mpg<-GSP(X, y, comp=1:2, mx = 4)
#feature coefficients for location component:
GSP.mpg$coef[,1,]
#feature coefficients for scale component:
GSP.mpg$coef[,2,]
#Coefficients for features at first order LP bases:
GSP.mpg$coef[1,,]</pre>
```

HCA

Heterogeneity component analysis

## Description

This function performs heterogeneity component analysis of of the response variable Y for identifying which shape compliments are changing with the covarite X.

## Usage

```
HCA(X, y, m = c(4, 6), alpha = 0.05, method.ml = "glmnet")
```

## Arguments

Χ	A $n$ -by- $d$ feature matrix
у	A length $n$ vector of response.
m	An ordered pair $(m_1,m_2)$ . $m_1$ indicates how many LP-nonparametric basis to construct for each column of $X$ , $m_2$ indicates how many to construct for $y$ .
alpha	Threshold for p-values of F-statistics. The plot will only display LP-coefficients whose p-value is smaller than alpha.
method.ml	Method for estimating the conditional LP-Fourier coefficients. In this case, valid input includes: "glmnet", "lm", and "subset"

LP.basis 9

#### Value

A list of values containing:

f. stat A vector of length  $m_2$ . F-statistics for LP-coefficients.

dev.rate A vector of length  $m_2$ . Deviance ratios for LP-coefficients.

pval A vector of length  $m_2$ . p-values of the F-statistics.

#### Author(s)

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## References

Mukhopadhyay, S., and Wang, K (2020) "Statistical Machine Learning: An Integrated Approach". Technical Report.

## **Examples**

```
##Fig 10(b) of the paper
data(cholesterol)
attach(cholesterol)
m=c(length(unique(x))-1,4)
ldlch.hca<- HCA(x,y,m=m,alpha=NULL,method.ml="lm")

##HCA can also check the heterogeneity of residual series: (Fig 6b of the paper)
data(bone)
attach(bone)
fit.reg<- smooth.spline(x,y)
yhat<-predict(fit.reg,x)$y
y.res<-y-yhat #residuals
bone.hca<-HCA(x,y.res,m=c(2,6),alpha=NULL,method.ml="lm")</pre>
```

LP.basis

Computes LP basis function from samples.

## **Description**

This function computes m LP basis functions for samples X. User can provide an initial pivot density as starting guess.

## Usage

```
LP.basis(X, m, pivot = NULL, Fmid = TRUE)
```

10 LP.basis

#### **Arguments**

Observed values of the random variable. Can also a n-by-d matrix where each column is a realization from a random variable. In that case the function will compute m LP basis functions for each column.

M An integer denoting the number of required LP basis functions.

Pivot This accepts either (i) a function object; or (ii) a vector of sub-samples for X. Set to NULL to use the marginal ecdf. Note that for multivariate X, it is better to leave this option empty as it will attempt to use same pivot on all columns.

Fmid Whether to use mid-rank empirical distribution. Recommended for samples

with ties.

#### Value

A matrix of dimension  $n \times mk$ .

#### Author(s)

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Maintainer: Kaijun Wang <kaijunwang.19@gmail.com>

#### References

Mukhopadhyay, S. and Parzen, E. (2020) Nonparametric Universal Copula Modeling, Applied Stochastic Models in Business and Industry, special issue on "Data Science", 36(1), 77-94.

Mukhopadhyay, S. (2017) Large-Scale Mode Identification and Data-Driven Sciences. Electronic Journal of Statistics, 11 215-240.

Mukhopadhyay, S., and Wang, K (2020) "Statistical Machine Learning: An Integrated Approach". Technical Report.

#### **Examples**

```
#figure 16 of the paper
data(autompg)
m < -4
#weight
x<-sort(autompg[,4])</pre>
TX <- LP.basis(x,m)
par(mfrow=c(2,2), mar=c(3,3,3,2))
ux < -ecdf(x)(x)
plot(ux,TX[,1],type="s")
plot(ux,TX[,2],type="s")
plot(ux,TX[,3],type="s")
plot(ux,TX[,4],type="s")
#acceleration
x<-sort(autompg[,5])</pre>
TX <- LP.basis(x,m)
ux < -ecdf(x)(x)
plot(ux,TX[,1],type="s")
plot(ux,TX[,2],type="s")
plot(ux,TX[,3],type="s")
plot(ux,TX[,4],type="s")
```

onlineNews 11

onlineNews

Online news popularity data.

#### **Description**

Popularity study of online articles.

#### Usage

data(onlineNews)

#### **Format**

A data frame with 39644 observations on the following 60 variables.

- x.timedelta Days between the article publication and the dataset acquisition.
- x.n\_tokens\_title Number of words in the title.
- x.n\_tokens\_content Number of words in the content.
- x.n\_unique\_tokens Rate of unique words in the content.
- x.n\_non\_stop\_words Rate of non-stop words in the content.
- x.n\_non\_stop\_unique\_tokens Rate of unique non-stop words in the content.
- x.num\_hrefs Number of links.
- x.num\_self\_hrefs Number of links to other articles published by Mashable.
- x.num\_imgs Number of images.
- x.num\_videos Number of videos.
- x.average\_token\_length Average length of the words in the content.
- x.num\_keywords Number of keywords in the metadata.
- x.data\_channel\_is\_lifestyle Is data channel 'Lifestyle'?
- x.data\_channel\_is\_entertainment Is data channel 'Entertainment'?
- x.data\_channel\_is\_bus Is data channel 'Business'?
- x.data\_channel\_is\_socmed Is data channel 'Social Media'?
- x.data\_channel\_is\_tech Is data channel 'Tech'?
- x.data\_channel\_is\_world Is data channel 'World'?
- x.kw\_min\_min Worst keyword (min. shares).
- x.kw\_max\_min Worst keyword (max. shares).
- x.kw\_avg\_min Worst keyword (avg. shares).
- x.kw\_min\_max Best keyword (min. shares).
- x.kw\_max\_max Best keyword (max. shares).
- x.kw\_avg\_max Best keyword (avg. shares).
- x.kw\_min\_avg Avg. keyword (min. shares).
- x.kw\_max\_avg Avg. keyword (max. shares).
- x.kw\_avg\_avg Avg. keyword (avg. shares).
- x.self\_reference\_min\_shares Min. shares of referenced articles in Mashable.

12 onlineNews

```
x.self_reference_max_shares Max. shares of referenced articles in Mashable.
```

- x.self\_reference\_avg\_sharess Avg. shares of referenced articles in Mashable.
- x.weekday\_is\_monday Was the article published on a Monday?
- x.weekday\_is\_tuesday Was the article published on a Tuesday?
- x.weekday\_is\_wednesday Was the article published on a Wednesday?
- x.weekday\_is\_thursday Was the article published on a Thursday?
- x.weekday\_is\_friday Was the article published on a Friday?
- x.weekday\_is\_saturday Was the article published on a Saturday?
- x.weekday\_is\_sunday Was the article published on a Sunday?
- x.is\_weekend Was the article published on the weekend?
- x.LDA\_00 Closeness to LDA topic 0.
- x.LDA\_01 Closeness to LDA topic 1.
- x.LDA\_02 Closeness to LDA topic 2.
- x.LDA\_03 Closeness to LDA topic 3.
- x.LDA\_04 Closeness to LDA topic 4.
- x.global\_subjectivity Text subjectivity.
- x.global\_sentiment\_polarity Text sentiment polarity.
- x.global\_rate\_positive\_words Rate of positive words in the content.
- x.global\_rate\_negative\_words Rate of negative words in the content.
- x.rate\_positive\_words Rate of positive words among non-neutral tokens.
- x.rate\_negative\_words Rate of negative words among non-neutral tokens.
- x.avg\_positive\_polarity Avg. polarity of positive words.
- x.min\_positive\_polarity Min. polarity of positive words.
- x.max\_positive\_polarity Max. polarity of positive words.
- x.avg\_negative\_polarity Avg. polarity of negative words.
- x.min\_negative\_polarity Min. polarity of negative words.
- $\verb"x.max_negative_polarity" Max. polarity of negative words.$
- x.title\_subjectivity Title subjectivity.
- x.title\_sentiment\_polarity Title polarity.
- x.abs\_title\_subjectivity Absolute subjectivity level.
- x.abs\_title\_sentiment\_polarity Absolute polarity level.
- y Response variable, log of number of shares (base 10).

#### References

Fernandes, K., P. Vinagre, and P. Cortez (2015) "A proactive intelligent decision supportsystem for predicting the popularity of online news." Portuguese Conference on Artificial Intelligence, pp. 535-546. Springer.

rosnerFEV 13

rosnerFEV

Rosner's FEV data.

## Description

This data set consists of 654 observations on youths aged 3 to 19 from East Boston recorded duing the middle to late 1970's. Forced expiratory volume (FEV), a measure of lung capacity, is the variable of interest. We slightly modified the original data, this version only includes the covariates used in our paper.

#### Usage

data(rosnerFEV)

#### **Format**

A data frame with 654 observations on the following 3 variables.

- x Age (years).
- z A binary variable indicating whether or not the youth smokes. Nonsmoker is 0. Smoker is 1.
- y Forced expiratory volume (liters). Roughly the amount of air an individual can exhale in the first second of a forceful breath.

#### References

Rosner, B. (1995) "Fundamentals of biostatistics". Duxbury Press: New York.

UPM

Uncertainty Prediction Machine

## Description

An integrated statistical learning framework that converts an ML-procedure into an uncertainty distribution prediction machine (UPM). Using this function, one can extract the estimated conditional density, contrast density, conditional quantile, highest density prediction interval, and finally, can simulated samples.

## Usage

14 UPM

## Arguments

X	A <i>n</i> -by- <i>d</i> feature matrix
у	A length $n$ vector of response.
X.test	A $k$ -by- $d$ matrix providing $k$ sets of covariates for target cases to investigate.
pivot	Pivot density for computing conditional distribution. This accepts either (i) a function object; or (ii) a vector of sub-samples for $y$ . Set to NULL to use the marginal ecdf of $y$ as the pivot.
m	An ordered pair $(m_1, m_2)$ . $m_1$ indicates how many LP-nonparametric basis to construct for each column of $X$ , $m_2$ indicates how many to construct for $y$ .
method.ml	Method for estimating the conditional LP-Fourier coefficients. Currently supports these options: subset (lm with subset selection), glmnet, svm (requires caret), knn (requires caret), gbm (requires h2o) and rf (requires h2o).
LP_smooth	Specifies the method to use for LP coefficient smoothing (AIC or BIC). Uses BIC by default.
nsample	Number of relevance samples generated for each case. Leave at NULL to disable.
credMass	A scalar [0, 1] specifying the mass within the desired coverage of the highest-density prediction interval.
centering	Set to TRUE to allow modeling the conditional mean function and obtain the residuals $y$ using the method given in method.ml.
quantile.probs	Numeric vector of length $\boldsymbol{q}$ for target quantile values. Leave at NULL to disable quantile regression.
parallel	Use parallel computing for obtaining the relevance samples, mainly used for very huge nsample, default is FALSE.
•••	Extra parameters to pass into other functions. Currently supports the arguments for caret::knnreg(), caret::train(), h2o::h2o.gbm(), h2o::h2o.randomForest().

## Value

A list of values containing:

LP.coef	A $k$ -by- $m$ matrix giving the conditional LP-coefficients for $y$ residuals given each ${\sf X.test.}$
cond.mean	conditional means for $y$ given each $X.test.$
y.res	$residuals\ after\ modeling\ conditional\ mean\ function,\ equals\ to\ y\ when\ {\tt centering=FALSE}.$
cond.den	list of conditional density functions given each X.test.
dhat	list of contrast density functions $d_x$ for each X.test.
samples	A matrix with $k$ columns, each column is a set of relevance sample points generated for $X$ . target.

list of prediction intervals of y given each X. test.

quantiles A k-by-q matrix containing the quantiles for each X. test.

## Author(s)

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UPM.gof

#### References

Mukhopadhyay, S., and Wang, K (2020) "Statistical Machine Learning: An Integrated Approach". Technical Report.

#### See Also

```
UPM.gof
```

## **Examples**

```
data(butterfly)
attach(butterfly)
UPM.out<-UPM(x,y,X.test=2,method.ml='knn',nsample=NULL,centering=FALSE)
##LP coefficients:
UPM.out$LP.coef
##conditional density:
y.axe=seq(-4,4,length.out=1000)
plot(y.axe,UPM.out$cond.den[[1]](y.axe),type="l")</pre>
```

UPM.gof

Goodness-of-fit Diagnostics for UPM.

#### **Description**

This function provides diagnosis for the performance of UPM. It provides a graphical diagnostics and test statistic to check whether the models are congruent with the observed data.

## Usage

```
UPM.gof(X, y, m = c(4, 6), method, indx, ...)
```

## Arguments

Χ	A $n$ -by- $d$ feature matrix
У	A length $n$ vector of response.
m	An ordered pair. First number indicates how many LP-nonparametric basis to construct for each column of $X$ , second number indicates how many to construct for $y$ .
method	Method for estimating the conditional LP-Fourier coefficients. Currently supports these options: subset (lm with subset selection), glmnet, svm (requires caret), knn (requires caret), gbm (requires h2o) and rf (requires h2o).
indx	Indices for the observations to be used as holdout set.
• • •	Extra parameters to pass into UPM.

#### Value

A list of values containing:

q.residuals Generalized quantile-residuals for the holdout set.

qdiv qDIV statistic. pval Test p-value. 16 UPM.gof

## Author(s)

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## References

Mukhopadhyay, S., and Wang, K (2020) "Statistical Machine Learning: An Integrated Approach". Technical Report.

## **Index**

LP.basis, 9

```
*Topic Main Functions
                                                 LP. smooth (UPM), 13
    DIF, 6
                                                 lpbasis(LP.basis), 9
    GSP, 7
                                                 LPMachineLearning
    HCA, 8
                                                          (LPMachineLearning-package), 2
    LP.basis, 9
                                                 LPMachineLearning-package, 2
    UPM, 13
                                                 LPregression (UPM), 13
    UPM.gof, 15
                                                 onlineNews, 11
*Topic datasets
    autompg, 2
                                                 Predict.LP.poly(LP.basis),9
    baseball, 3
    bone, 3
                                                 rosnerFEV, 13
    boxOffice, 4
    bupa, 4
                                                 UPM, 13
    butterfly, 5
                                                 UPM.gof, 15, 15
    cholesterol, 5
    dutch, 7
                                                 z.lp.center (UPM), 13
    onlineNews, 11
    rosnerFEV, 13
*Topic package
    LPMachineLearning-package, 2
autompg, 2
baseball, 3
bone, 3
boxOffice, 4
bupa, 4
butterfly, 5
cholesterol, 5
Dfun_int (UPM.gof), 15
DIF, 6
dutch, 7
eLP.poly.predict(LP.basis), 9
eLP.univar(LP.basis), 9
g21.sampler(UPM), 13
GSP, 7
HCA, 8
LEG. fun (LP.basis), 9
```