## Package 'MR.Rerand'

## January 9, 2024

Title Re-Randomized Inverse-Variance Weighted Estimator in Two-Sample Mendelian Randomization with Summary-Data and Mediation Analysis in Mendelian Randomization with Summary-Data  Version 0.0.1				
			<b>Description</b> Conducting rerandomization in two sample GWAS with summary data to estimate the causal effect or in three samples GWAS to estimate the mediation effect.	
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Roxyger	nNote 7.2.3			
Imports stats, MASS, msm  License MIT + file LICENSE  Suggests knitr, rmarkdown  VignetteBuilder knitr				
			R top	ics documented:
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MAGIC	Main function for using MAGIC framework to conduct mediation analysis.			

## Description

MAGIC stands for the Mediation Analysis framework through GWAS summary data Integration with the winner's (and the loser's) curse and measurement bias Correction. Our framework efficiently integrates information stored in three independent GWAS summary data and mitigates the commonly encountered winner's curse and measurement error bias (a.k.a. instrument selection and weak instrument bias) in MR.

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#### Usage

```
MAGIC(
   beta.exposure,
   beta.mediator,
   beta.outcome,
   se.exposure,
   se.mediator,
   se.outcome,
   Conf.level = 0.95,
   pval.select = c(5e-05, 5e-05),
   eta = c(0.5, 0.5),
   seed = 0
)
```

## **Arguments**

SNP effect size's vector of the exposure vairable (GWAS(I)) beta.exposure SNP effect size's vector of the mediator vairable (GWAS(III)) beta.mediator SNP effect size's vector of the outcome vairable (GWAS(II)) beta.outcome se.exposure SNP effect size's standard errors of beta. exposure se.mediator SNP effect size's standard errors of beta.mediator SNP effect size's standard errors of beta.outcome se.outcome Conf.level Confidence level. Default is 0.95. A vector of specified pre-screening threshold in the ordering of (exposure, mepval.select diator). Default is (5e-5, 5e-5). (corresponding  $\lambda$  is 4.06) eta A vector of rerandomized scale in the ordering of (exposure, mediator). Default is (0.5,0.5). The value of the random seed. Default is 0. seed

## Value

A list

theta.hat Estimated direct effect from exposure to outcome variable tauy.hat Estimated direct effect from mediator to outcome variable taux.hat Estimated indirect effect from exposure to mediator variable tau.hat Estimated mediation effect tau\_total.hat Estimated total effect theta.se Standard error of theta.hat tauy.se Standard error of tauy.hat taux.se Standard error of taux.hat tau.se Standard error of taux.hat tau\_total.se Standard error of tau\_total.hat n.IV.exp Number of IVs used in exposure dataset n.IV.med Number of IVs used in mediator dataset Conf.Interval Confidence interval given Conf.level IV.exp The index of IVs selected in  $\mathcal{S}_{\pi}$  IV.med The index of IVs selected in  $\mathcal{S}_{\pi}$ 

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#### References

Rita Qiuran Lyu, Chong Wu, Xinwei Ma, Jingshen Wang (2023). Mediation Analysis with Mendelian Randomization and Efficient Multiple GWAS Integration. https://arxiv.org/abs/2312.10563.

pre\_screening Supplementary function for RIVW to conduct rerandomization and Rao-Blackwellization in GWAS (I).

### **Description**

```
For GWAS (I) (\hat{\beta}_{X_j}, \sigma_{X_j}), the formula is \hat{\beta}_{X_j, \text{RB}} = \hat{\beta}_{X_j} - \frac{\sigma_{X_j}}{\eta} \Big( \phi \big( A_{j,+} \big) - \phi \big( A_{j,-} \big) \Big) \Big( \frac{\mathbf{1}_{(j \in \mathcal{S}_{\mathbf{x}})}}{1 - \Phi \big( A_{j,+} \big) + \Phi \big( A_{j,-} \big)} \Big), \hat{\sigma}^2_{X_j, \text{RB}} = \sigma^2_{X_j} \Bigg( 1 - \frac{1}{\eta^2} \frac{A_{j,+} \phi (A_{j,+}) - A_{j,-} \phi (A_{j,-})}{1 - \Phi \big( A_{j,+} \big) + \Phi \big( A_{j,-} \big)} + \frac{1}{\eta^2} \Big( \frac{\phi (A_{j,+}) - \phi (A_{j,-})}{1 - \Phi \big( A_{j,+} \big) + \Phi \big( A_{j,-} \big)} \Big)^2 \Big), and \phi(\cdot) is the density function of standard normal distribution, \Phi(\cdot) is the cummulative function of standard normal distribution.
```

#### Usage

```
pre_screening(
  gamma1.exp,
  se1.exp,
  etamean = 0.5,
  pthr = 5e-05,
  seed = 0,
  smoothing = FALSE
)
```

## **Arguments**

gamma1.exp SNP effect size's vector of the exposure vairable se1.exp SNP effect size's standard errors of beta.exposure etamean rerandomized scale of exposure variable. Default is 0.5. The specified pre-screening threshold. Default is 5e-5. (corresponding  $\lambda$  is 4.06) seed The value of the random seed. Default is 0. Smoothing Whether to use smoothing to decrease variance . Default is FALSE.

## Value

A list

filter1 Indexs of selected relevant IVs.

gamma\_exp1 Effect size in GWAS (I) after Rao-Blackwellization to eliminate the winner's curse se1 Standard errors in GWAS (I) after Rao-Blackwellization to eliminate the winner's curse weights The weights for each SNP. If smoothing is False, weights are the same for each SNP.

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#### References

Xinwei Ma, Jingshen Wang, Chong Wu. (2023). Breaking the Winner's Curse in Mendelian Randomization:Rerandomized Inverse Variance Weighted Estimator https://projecteuclid.org/journals/annals-of-statistics/volume-51/issue-1/Breaking-the-winners-curse-in-Mendelian-randoming-10.1214/22-AOS2247.full.

pre\_selection

Supplementary function for MAGIC to conduct rerandomization and Rao-Blackwellization in GWAS (I) and GWAS (III).

## Description

```
Take GWAS (I) (\hat{\beta}_{X_j}, \sigma_{X_j}) as an example, here \hat{\beta}_{X_j, \text{RB}} = \hat{\beta}_{X_j} - \frac{\sigma_{X_j}}{\eta} \Big( \phi \Big( A_{j,+} \Big) - \phi \Big( A_{j,-} \Big) \Big) \Big( \frac{\mathbf{1}_{(j \in \mathcal{S}_{\mathbf{X}})}}{\mathbf{1} - \Phi \Big( A_{j,+} \Big) + \Phi \Big( A_{j,-} \Big)} - \frac{\mathbf{1}_{(j \notin \mathcal{S}_{\mathbf{X}})}}{\Phi \Big( A_{j,+} \Big) - \Phi \Big( A_{j,-} \Big)} \Big), \hat{\sigma}^2_{X_j, \text{RB}} = \sigma^2_{X_j} \Bigg( 1 - \frac{1}{\eta^2} \frac{A_{j,+}\phi(A_{j,+}) - A_{j,-}\phi(A_{j,-})}{1 - \Phi(A_{j,+}) + \Phi(A_{j,-})} + \frac{1}{\eta^2} \Big( \frac{\phi(A_{j,+}) - \phi(A_{j,-})}{1 - \Phi(A_{j,+}) + \Phi(A_{j,-})} \Big)^2 \Bigg), and \phi(\cdot) is the density function of standard normal distribution, \Phi(\cdot) is the cummulative function of standard normal distribution.
```

#### Usage

```
pre_selection(
   gamma1.exp,
   se1.exp,
   gamma2.exp,
   se2.exp,
   etamean1 = 0.5,
   etamean2 = 0.5,
   pthr = c(5e-05, 5e-05),
   seed = 0
)
```

## Arguments

gamma1.exp	SNP effect size's vector of the exposure vairable (GWAS(I))
se1.exp	SNP effect size's standard errors of beta.exposure
gamma2.exp	SNP effect size's vector of the mediator vairable (GWAS(III))
se2.exp	SNP effect size's standard errors of beta.mediator
etamean1	rerandomized scale of exposure variable. Default is 0.5.
etamean2	rerandomized scale of mediator variable. Default is 0.5.
pthr	A vector of specified pre-screening threshold in the ordering of (exposure, mediator). Default is (5e-5, 5e-5). (corresponding $\lambda$ is 4.06)
seed	The value of the random seed. Default is 0.

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#### Value

A list

**filter1** Indexs of selected relevant IVs in  $S_x$ 

**filter2** Indexs of selected relevant IVs in  $S_m$ 

gamma\_exp1 Effect size in GWAS (I) after Rao-Blackwellization to eliminate the winner's curse
 se1 Standard errors in GWAS (I) after Rao-Blackwellization to eliminate the winner's curse
 gamma\_exp2 Effect size in GWAS (III) after Rao-Blackwellization to eliminate the winner's curse
 se2 Standard errors in GWAS (III) after Rao-Blackwellization to eliminate the winner's curse
 gamma\_exp1.carve Effect size in GWAS (I) after Rao-Blackwellization to eliminate the loser's curse

gamma\_exp2.carve Effect size in GWAS (III) after Rao-Blackwellization to eliminate the loser's curse

#### References

Rita Qiuran Lyu, Chong Wu, Xinwei Ma, Jingshen Wang (2023). Mediation Analysis with Mendelian Randomization and Efficient Multiple GWAS Integration. https://arxiv.org/abs/2312.10563.

RIVW

Main function for conducting RIVW estimator.

## Description

Conventional two-sample Mendelian randomization methods often employ the same sample for selecting relevant genetic variants and for constructing final causal estimates. Such a practice often leads to biased causal effect estimates due to the well-known "winner's curse" phenomenon. To address this fundamental challenge, we propose a novel framework that not only systematically breaks the winner's curse but also provides an unbiased estimate of the genetic association effect after selection. Built upon the proposed framework, we introduce a novel randomized inverse variance weighted (RIVW) estimator that is provably consistent when selection and parameter estimation are conducted on the same sample.

## Usage

```
RIVW(
beta.exposure,
beta.outcome,
se.exposure,
se.outcome,
Conf.level = 0.95,
smoothing = FALSE,
pval.select = 5e-05,
eta = 0.5,
seed = 0
)
```

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#### **Arguments**

beta.exposure SNP effect size's vector of the exposure vairable (GWASI) beta.outcome SNP effect size's vector of the outcome vairable (GWASII)

se.exposure SNP effect size's standard errors of beta.exposure se.outcome SNP effect size's standard errors of beta.outcome

Conf. level Confidence level. Default is 0.95.

smoothing Whether to use smoothing to decrease variance. Default is FALSE.

pval.select The specified pre-screening threshold. Default is 5e-5. (corresponding  $\lambda$  is 4.06)

eta A vector of rerandomized scale. Default is 0.5. seed The value of the random seed. Default is 0.

#### Value

A list

beta.rerand Exposure dataset effect size after rerandomization.

se.rerand Exposure dataset standard errors after rerandomization.

beta.hat Estimated direct effect from exposure to outcome variable

beta.se Standard error of beta.hat

IV The index of IVs selected in Sx

n.IV Number of IVs used in exposure dataset

**F** The value of F-statistic

p.val The p-value of estimated causal effect

Conf.Interval Confidence interval of the causal effect given Conf.level

#### References

Xinwei Ma, Jingshen Wang, Chong Wu. (2023). Breaking the Winner's Curse in Mendelian Randomization:Rerandomized Inverse Variance Weighted Estimator https://projecteuclid.org/journals/annals-of-statistics/volume-51/issue-1/Breaking-the-winners-curse-in-Mendelian-randomi 10.1214/22-AOS2247.full.

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