The possibility that two people choose to go to same hotel now becomes $0.01*0.01/500000=2*10^{-10}$. If they visit a same hotel on 4 different days, then the possibility should be $2*10^{-10^4}=8*10^{-40}$. The number of pairs of people now becomes $\binom{5*10^9}{2}$, and the number of chosen 4 days becomes $\binom{5*10^3}{4}$ due to the changes of examples. As a result:

$${5*10^{9} \choose 2} * {5*10^{3} \choose 4} * 8 * 10^{-40}$$

$$\approx \frac{5*10^{9^{2}}}{2} * \frac{5*10^{3^{4}}}{24} * 8 * 10^{-40} \approx 2.604 * 10^{-7}$$

The number of suspect pairs should be less than $2.604 * 10^{-7}$.

Q3. For the map part, when the program deals with a user, it first connects this user with every friend as 1 degree friends, then connects every friend with every other friend as 2 degree friends. For the reduce part, when the program deals with a new data, it first check whether this belong to an exist 1 degree friendship, if yes ignore it. Then check whether this 2 degree friendship already exist, if yes, save this friendship one more times. If no, create a new stored friendship.

Below is the caught examples

924 439,2409,6995,11860,15416,43748,45881

- 8941 8940,8943,8944
- 8942 8940,8943,8944,8939
- 9019 317,9023,9022
- 9020 317,9023,9016,9017,9022,9021
- 9021 317,9023,9016,9017,9022,9020
- 9022 317,9016,9017,9023,9019,9020,9021
- 9990 13134,13478,13877,34299,34485,34642,37941
- 9992 9991,35667,9987,9989
- 9993 13134,13478,13877,34299,34485,34642,37941,9991