

# Novel cross-correlation methods

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**HERA publishes a 21cm power spectrum at  $z \sim 6-7$**

**How do we convince ourselves we aren't contaminated by residual foregrounds?**

**One option: cross-correlate with a galactic emission line  
[C II], [O III], CO, H $\alpha$ , etc.**

# Taking cross-spectra is really nice

Cross-correlations with IM of different lines is well-studied,  
and with current data sets best way to make measurements

**[C II] x BOSS quasars ( $z \sim 2.6$ )**

Pullen, A. et al. 2018 MNRAS 478 1911  
arXiv:1707.06172

**21cm x DEEP2 galaxies ( $z \sim 1$ )**

Chang, T.-C. et al. 2010 Nature 466 463

**Lya x BOSS quasars ( $z \sim 3$ )**

Croft, R. et al. 2016 MNRAS 457 3541  
arXiv:1504.04088

$$P_{21, C_{II}} = r_{21, C_{II}} \sqrt{P_{21, 21} P_{C_{II}, C_{II}}}$$



what we're  
after



also challenging  
to measure (e.g.  
interlopers)

# What if we had three fields?

$$P_{21,C\text{ II}} = r_{21,C\text{ II}} \sqrt{P_{21,21} P_{C\text{ II},C\text{ II}}}$$

$$P_{21,O\text{ III}} = r_{21,O\text{ III}} \sqrt{P_{21,21} P_{O\text{ III},O\text{ III}}}$$

$$P_{C\text{ II},O\text{ III}} = r_{C\text{ II},O\text{ III}} \sqrt{P_{C\text{ II},C\text{ II}} P_{O\text{ III},O\text{ III}}}$$



$$\frac{P_{21,C\text{ II}} P_{21,O\text{ III}}}{P_{C\text{ II},O\text{ III}}} = \frac{r_{21,C\text{ II}} r_{21,O\text{ III}}}{r_{C\text{ II},O\text{ III}}} P_{21,21}$$

only cross-spectra enter!

$$\frac{P_{21, \text{C II}, \text{O III}} P_{21, \text{O III}}}{P_{\text{C II}, \text{O III}}} = \frac{r_{21, \text{C II}} r_{21, \text{O III}}}{r_{\text{C II}, \text{O III}}} P_{21, 21}$$



**Test whether this is ~ 1 in simulation:**

**1.) 21cm, halo field from old 186 Mpc sims**

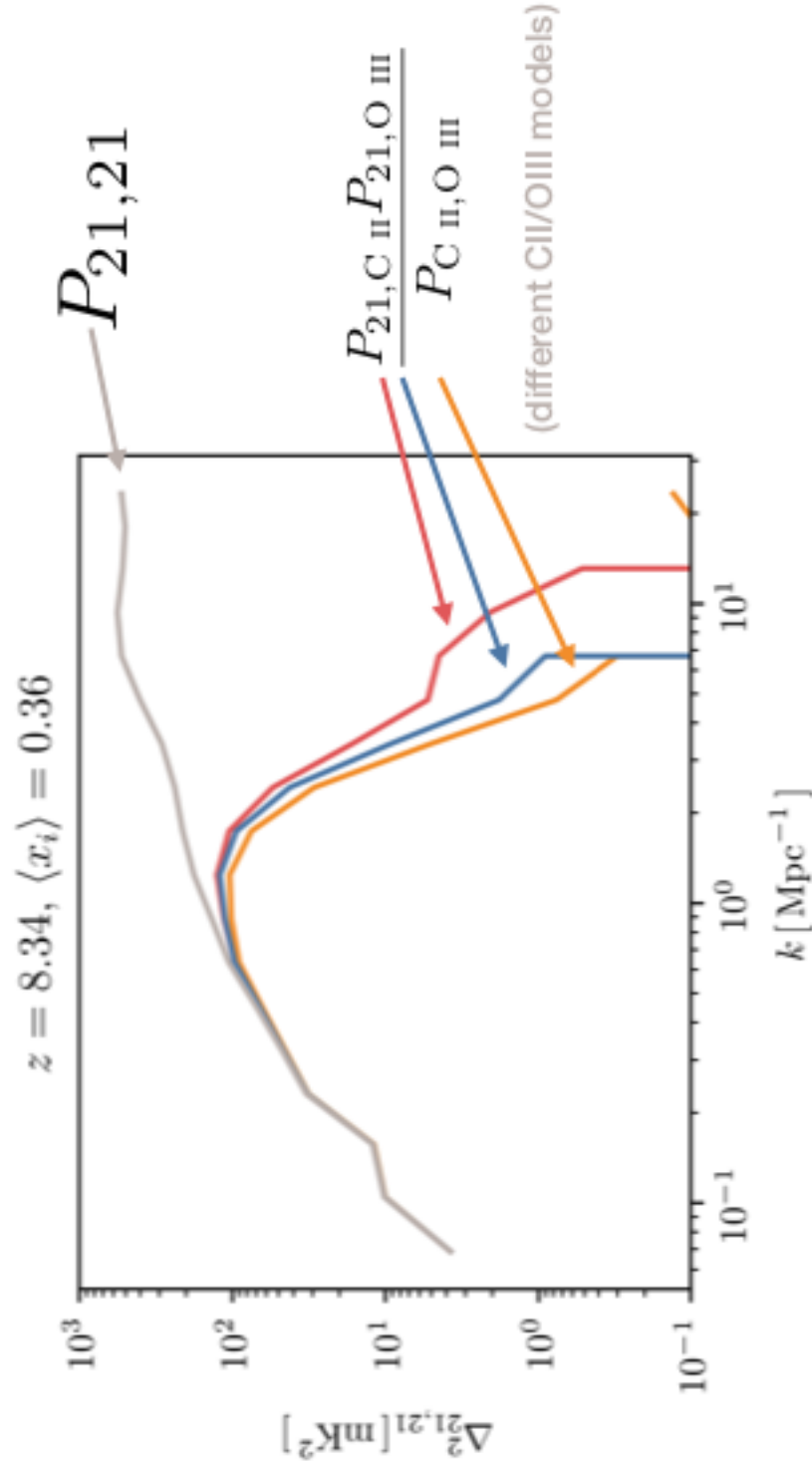
McQuinn et al. (2007) and Lidz et al. (2008)

**2.) [C II], [O III] fields from simple model:**

$$\langle L_i \rangle (M) = L_{i,0} \left[ \frac{M}{M_0} \right]^{\alpha_i} \quad \alpha_i = 2/3, 1, 4/3$$

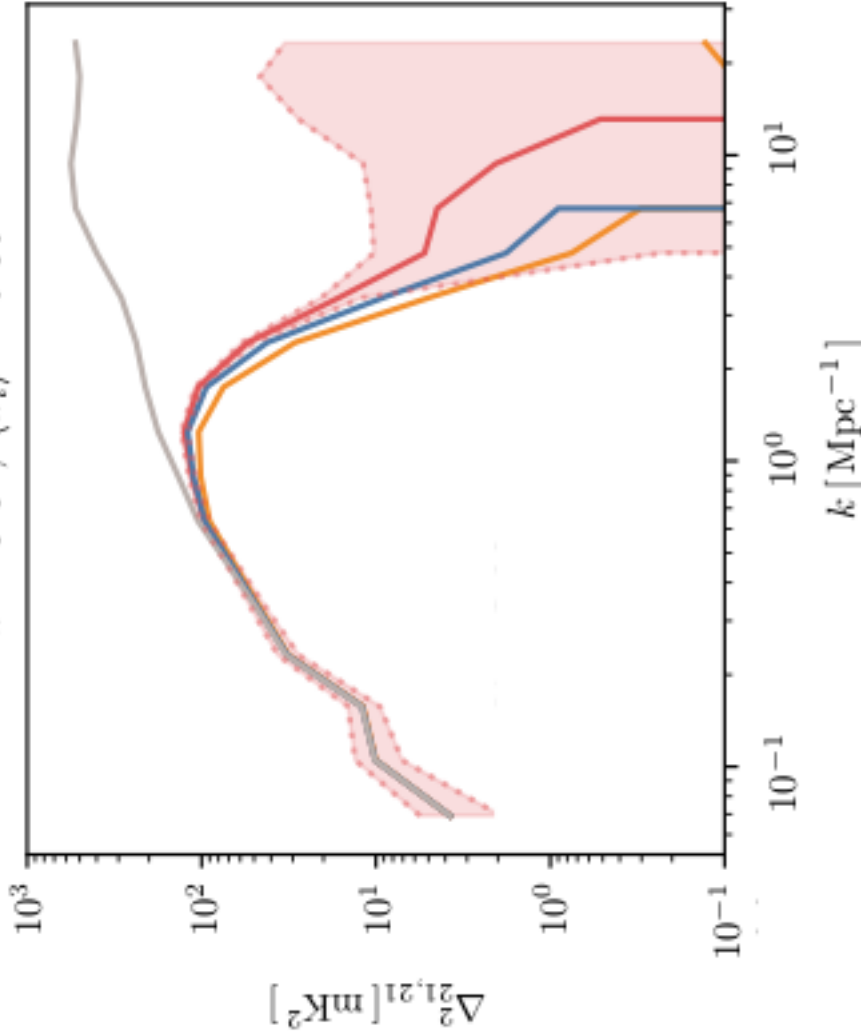
# Does it work?

$$\frac{P_{21,\text{C II}} P_{21,\text{O III}}}{P_{\text{C II},\text{O III}}} = \frac{r_{21,\text{C II}} r_{21,\text{O III}}}{r_{\text{C II},\text{O III}}} P_{21,21}$$



# Can we detect?

$z = 8.34, \langle x_i \rangle = 0.36$



futuristic survey:

[C II] and [O III] surveys of  $100 \text{ deg}^2$

$$N_{21} = P_{21,21}$$

$$N_{\text{C II}} = P_{\text{C II}, \text{C II}} \quad \text{at } k = 0.1 \text{ Mpc}^{-1}$$

$$N_{\text{O III}} = P_{\text{O III}, \text{O III}}$$

$$N_{\text{C II}} \sim 3 \times 10^9$$

$$\text{if } \langle I_{\text{C II}} \rangle = 500$$

$$N_{\text{C II}} \sim 1 \times 10^8 (\text{Jy/sr})^2 \text{ Mpc}^3$$

$$\text{if } \langle I_{\text{C II}} \rangle = 100 \text{ Jy/sr}$$

$$N_{\text{C II}} \sim 4 \times 10^6$$

$$\text{if } \langle I_{\text{C II}} \rangle = 20$$



# Side-Stepping Line Confusion

Foregrounds aren't as bad as EoR 21cm case,  
but line confusion is a serious problem

Simple extension of our results gives another  
way to sidestep line confusion

SPHEREx should measure  $H\alpha$ ,  $H\beta$ , and  $[O\ III]$  at  $0.5 < z < 2$

# what if we used three-point statistics?

$$B_{21,C\,\Pi,C\,\Pi}(k_1, k_2, k_3) \equiv \langle T_{21}(k_1) I_{C\,\Pi}(k_2) I_{C\,\Pi}(k_3) \rangle$$

“reduced cross-bispectrum”

$$Q_{21,C\,\Pi,C\,\Pi} \equiv \frac{B_{21,C\,\Pi,C\,\Pi} + 2 \text{ perm.}}{P_{21,C\,\Pi}(k_1) P_{21,C\,\Pi}(k_2) + 2 \text{ perm.}}$$



$$Q_{21,C\,\Pi,C\,\Pi} = \frac{Q_{\delta,\delta,\delta}}{\langle T_{21} \rangle b_{21}} + C_{21,C\,\Pi,C\,\Pi}$$



perturbation  
theory



$$Q_{21,C_{II},C_{II}} = \frac{Q_{\delta,\delta,\delta}}{\langle T_{21} \rangle b_{21}} + C_{21,C_{II},C_{II}}$$



perturbation  
theory



functions of  $k_1, k_2, \theta_{12}$

$$Q_{21, C_{II}, C_{II}} = \frac{Q_{\delta, \delta, \delta}}{\langle T_{21} \rangle b_{21}} + C_{21, C_{II}, C_{II}}$$



perturbation  
theory

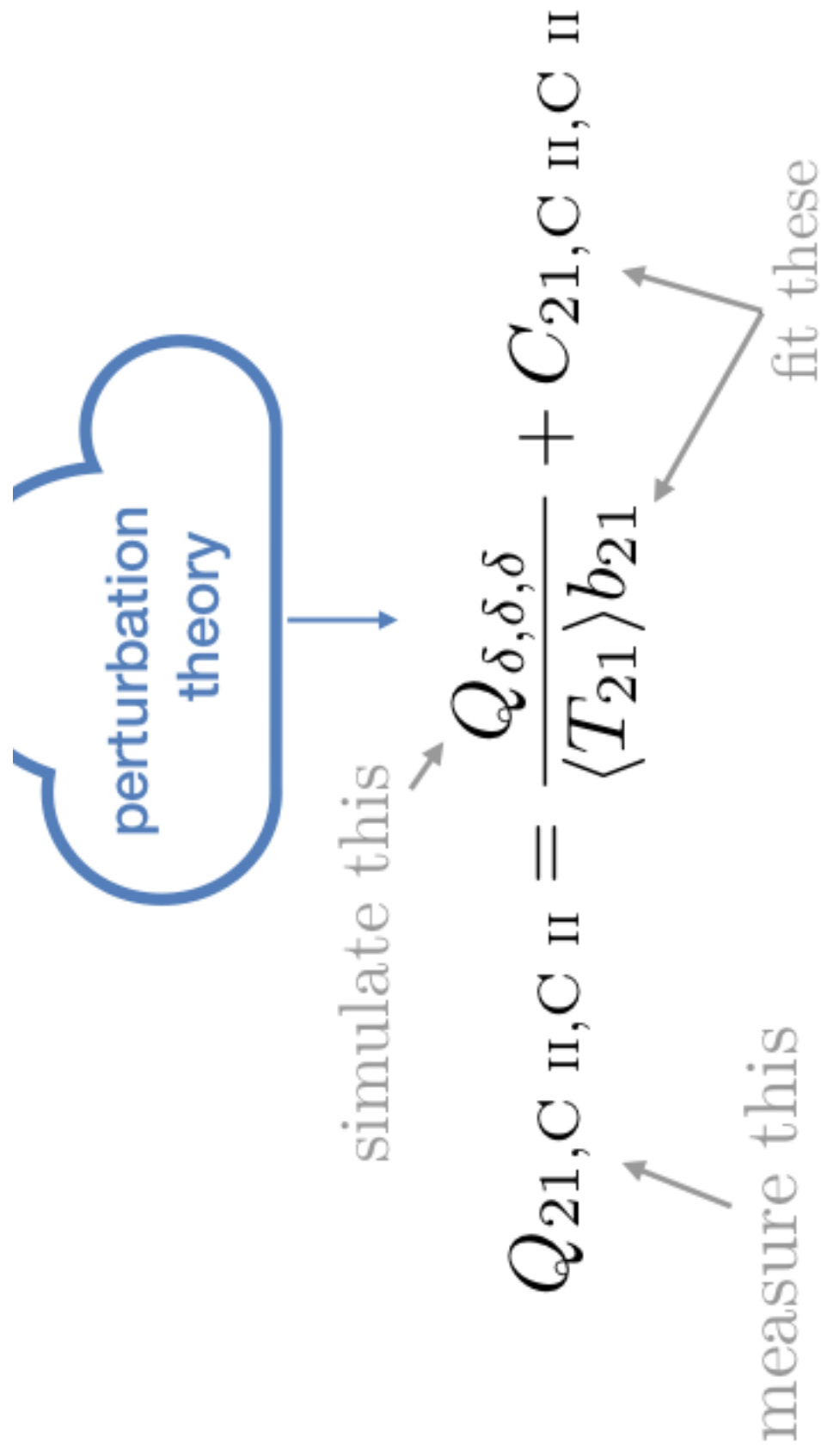


functions of  $k_1, k_2, \theta_{12}$

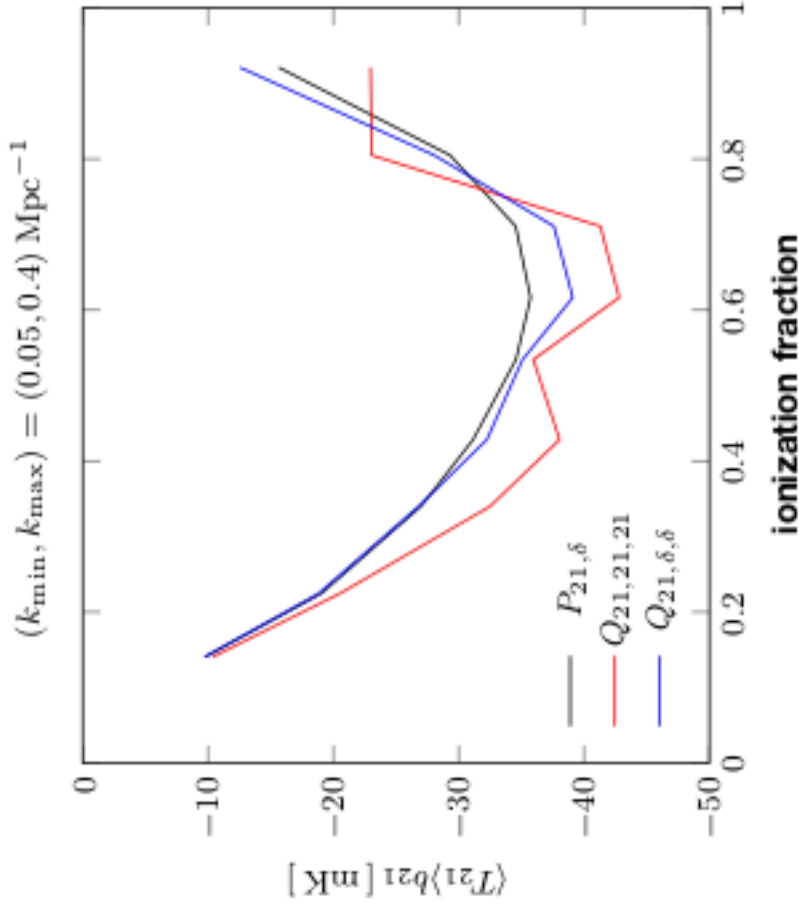
$$Q_{21,C\ II,C\ II} = \frac{Q_{\delta,\delta,\delta}}{\langle T_{21} \rangle b_{21}} + C_{21,C\ II,C\ II}$$

constant





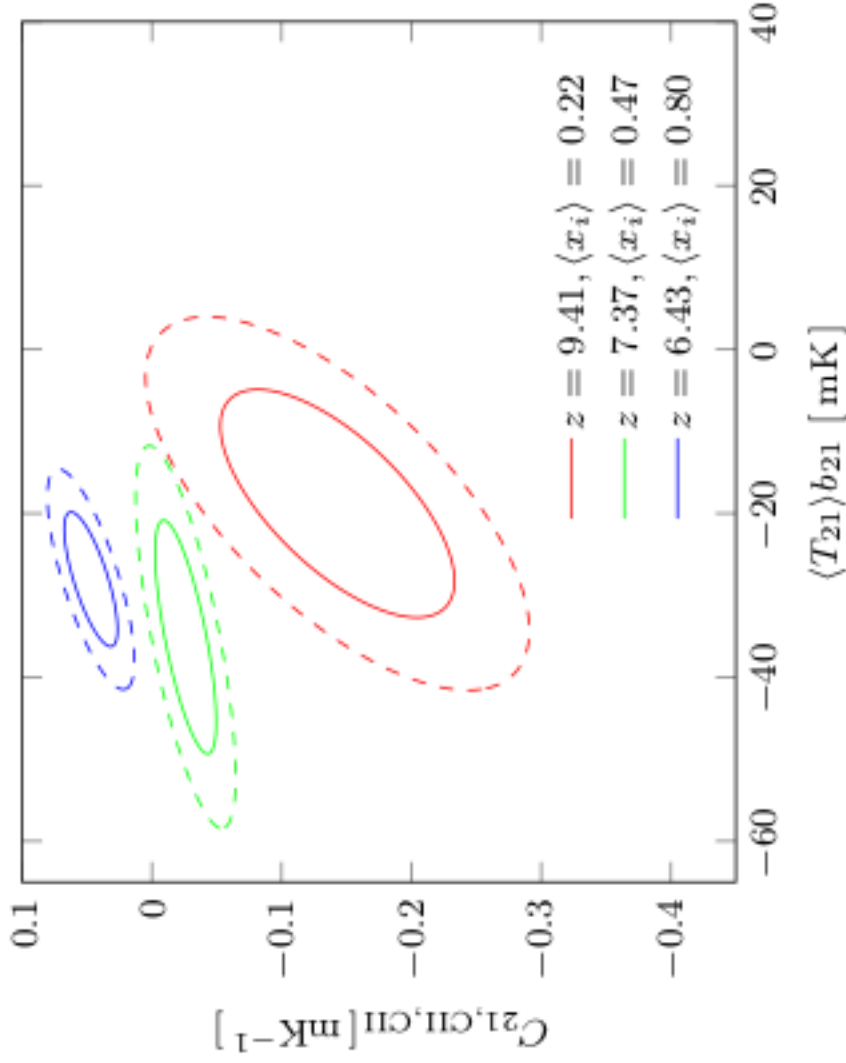
# Does it work?



Only uses large triangles

Simulations are noisy

# Can we detect?



futuristic survey:

[C II] survey of  $50 \text{ deg}^2$

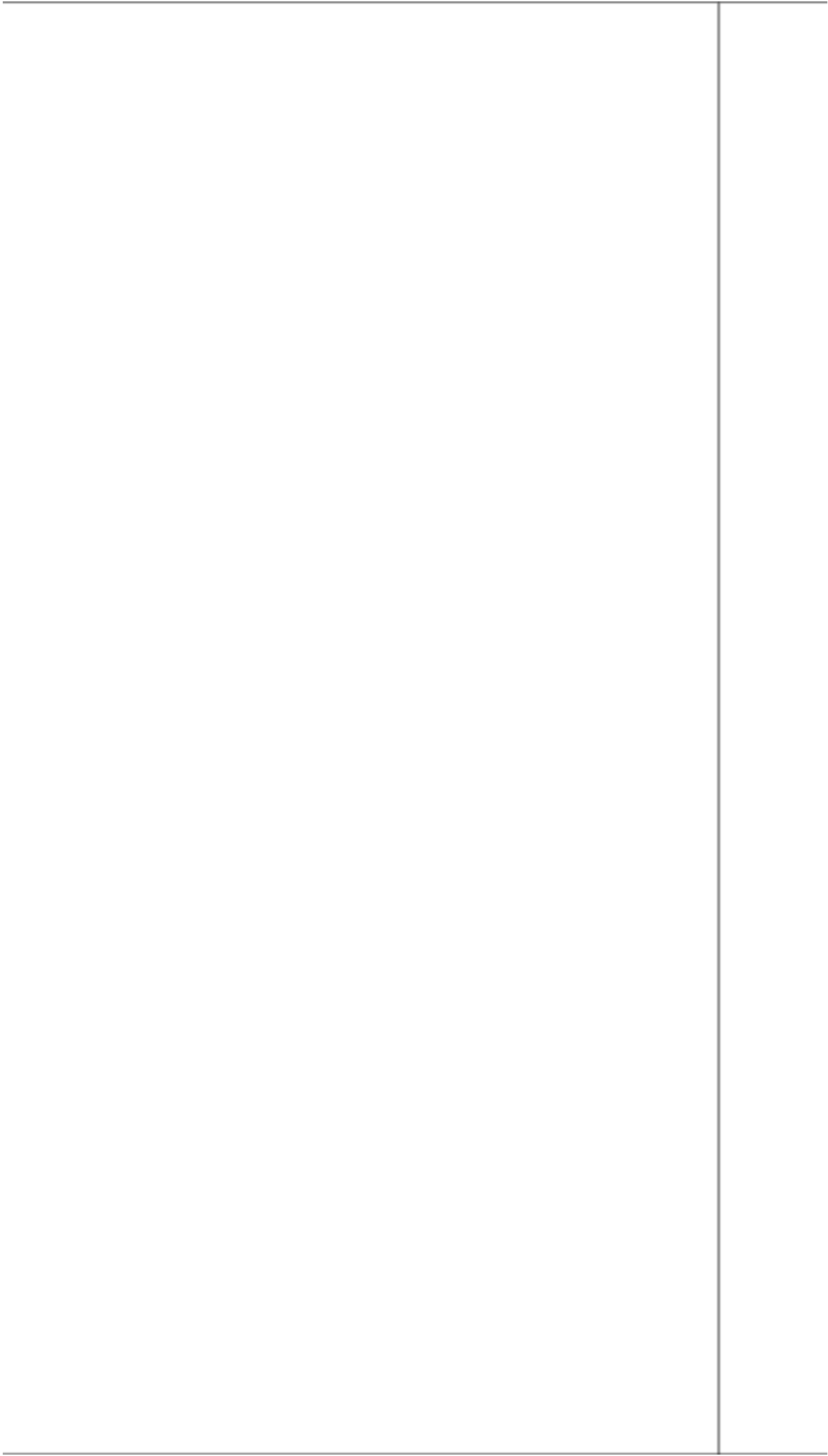
$$N_{21} = P_{21,21}$$

$$N_{\text{C II}} = P_{\text{C II}, \text{C II}} \quad \text{at } k = 0.1 \text{ Mpc}^{-1}$$

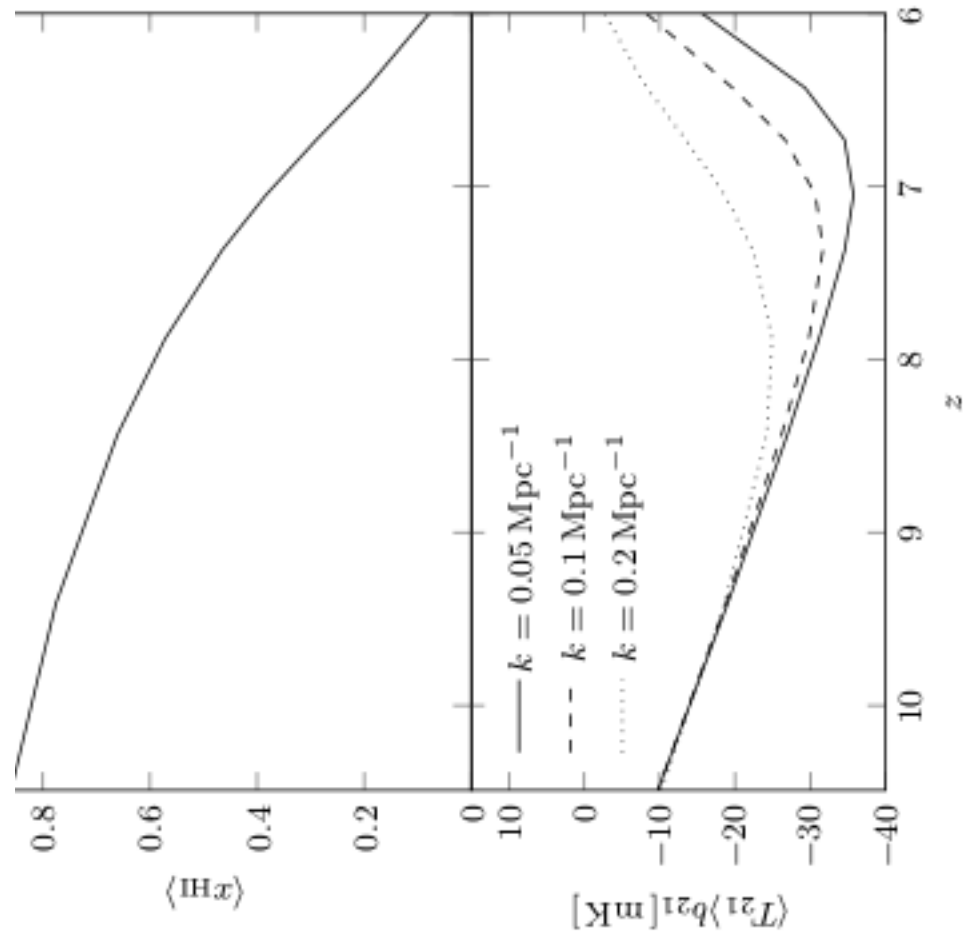


# Summary

- Want to **confirm** our 21cm power spectrum measurement
  - Have to make sure we aren't biased by residual foregrounds
  - Can directly estimate 21cm power spectrum on large scales with: a.) three field approach, b.) cross-bispectrum
  - Measurements may be in reach of next generation surveys
- Question: If you have measurements of multiple fields which are biased tracers of the underlying density field, what is the optimal way to extract information on the density field?



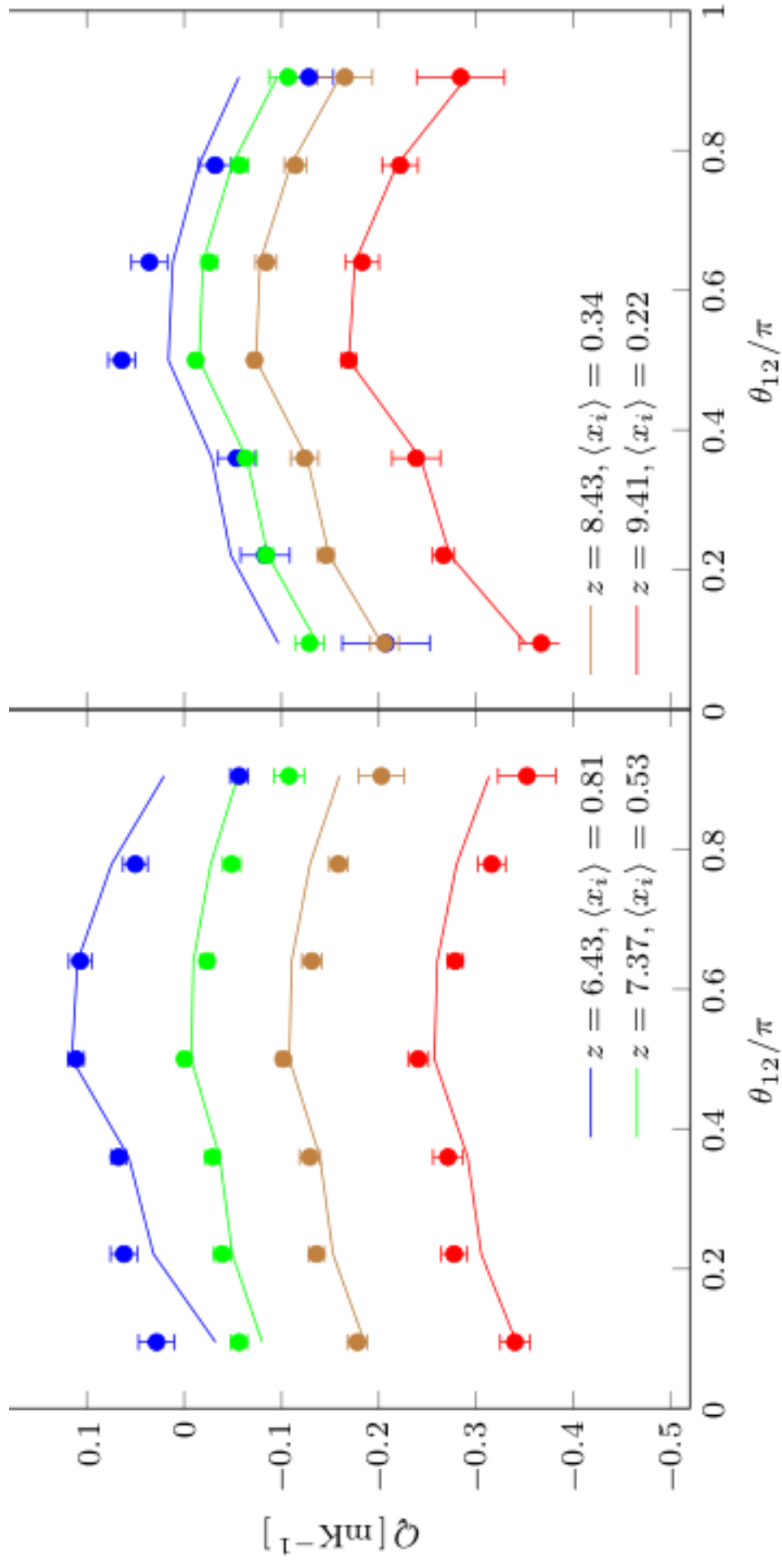
$$C_{21,\text{C II,C II}} = \frac{1}{6} \frac{b_{21}^{(2)}}{b_{21}^2} + \frac{1}{3} \frac{b_{\text{C II}}^{(2)}}{b_{21} b_{\text{C II}}}$$



$Q_{21,21,21}$

$Q_{21,\delta,\delta}$

0.2

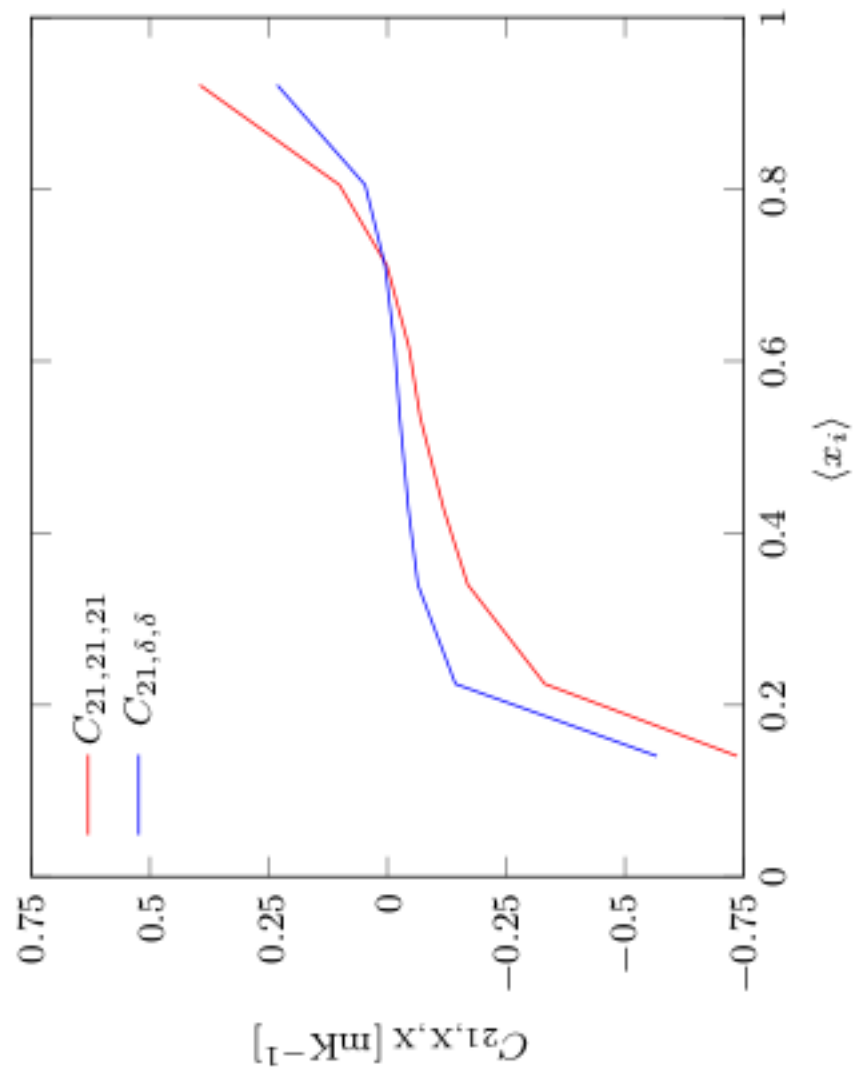


$$C_{21,21,21} = \frac{1}{2} \frac{b_{21}^{(2)}}{\langle T_{21} \rangle b_{21}^2},$$

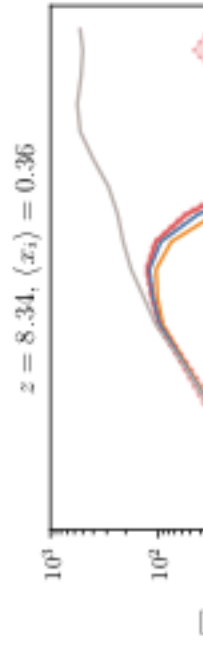
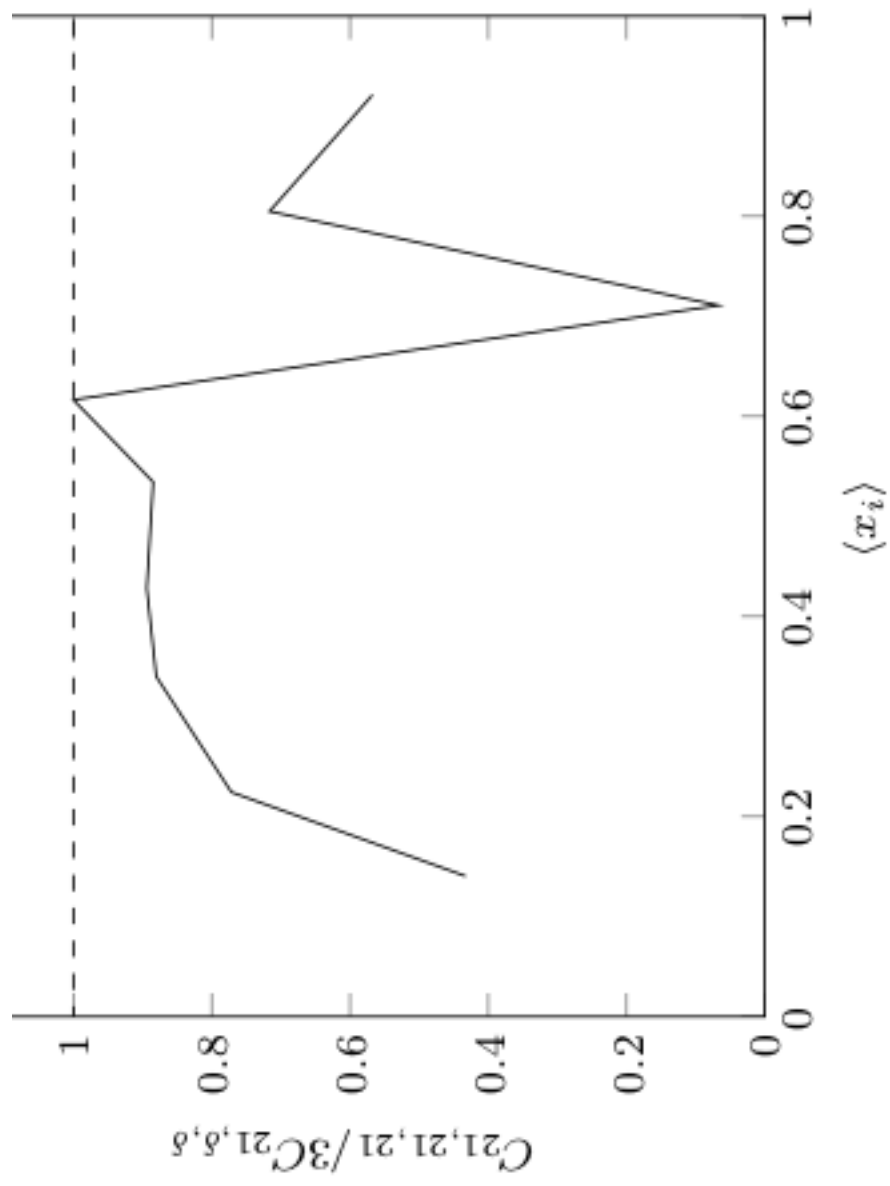
$$C_{21,\delta,\delta} = \frac{1}{6} \frac{b_{21}^{(2)}}{\langle T_{21} \rangle b_{21}^2},$$

$$C_{21,\mathrm{CII},\mathrm{CII}} = \frac{1}{6} \frac{b_{21}^{(2)}}{\langle T_{21} \rangle b_{21}^2} + \frac{1}{3} \frac{b_{\mathrm{CII}}^{(2)}}{\langle T_{21} \rangle b_{21} b_{\mathrm{CII}}}.$$

$$(k_{\mathrm{min}}, k_{\mathrm{max}}) = (0.05, 0.4) \, \mathrm{Mpc}^{-1}$$



1.2



$k = 0.10 \text{ Mpc}^{-1}$



