

TIME AND WORK

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$$1) \text{ Total work} = \text{Efficiency} \times \text{Days} // \text{Lcm of given days}$$

$$2) \text{ Efficiency} = \frac{\text{Total work}}{\text{Days}}$$

$$3) \text{ Days} = \frac{\text{Total work}}{\text{Efficiency}}$$

T&W 01 : A & B can do a piece of work alone in 3 and 6 days. In how many days they complete the work, if they work together ?

- (a) 3
 (b) 5 $\frac{(A+B) \text{ Days}}{(A+B) \text{ Efficiency}}$ ⇒ Total work
 (c) 4
 (d) 6
 (e) 2

$$\text{A's Efficiency} = \frac{\text{Tw}}{\text{A's Days}}$$

A's 1 day work $\Rightarrow \frac{6}{3} \Rightarrow 2$

$$\rightarrow \text{LCM } \{3, 6\} = 6$$

$$\Rightarrow \frac{6}{2+1} = \frac{6}{3} = 2 \text{ days}$$

$$\text{B's Efficiency} = \frac{\text{Tw}}{\text{B's Days}}$$

$$\Rightarrow \frac{6}{6} = 1$$

$$\frac{A \times B}{A+B}$$

$$\frac{3 \times 6}{3+6}$$

$$\frac{B \times A}{A+B} (2)$$

T&W 05 : A & B together can do a piece of work in 6 days. If A alone finished the work in 12 days, then how many days that B takes to finished the work?

- (a) 4 days
- (b) 6 days
- (c) 10 days
- (d) 12 days
- (e) None of these

$$\textcircled{1} \Rightarrow \frac{12}{1} = 12 \text{ days}$$

$$\begin{aligned} A + B &= 6 \\ A &= 12 \end{aligned}$$

B_1 's Days = $\frac{T \cdot w}{B_1 \text{ Effi}}$

$$(A+B) \text{ Effi.} = \frac{T \cdot w}{(A+B) \text{ Days}} = \frac{12}{6} = 2$$

$$A_1 \text{ Effi.} = \frac{T \cdot w}{A_1 \text{ Days}} = \frac{12}{12} = 1$$

$$\begin{aligned} \frac{A \times B}{A \sim B} &\rightarrow \frac{6 \times 12}{12 \sim 6} = \\ &= \frac{6 \times 12}{12 \sim 6} = \\ &= 12 \end{aligned}$$



T&W 06 : A can do a work in 15 days and B in 20 days. (If they work on it together for 4 days, then the fraction of the work that is left is?)

- (a) $\frac{1}{10}$
(b) $\frac{1}{4}$
(c) $\frac{7}{15}$
 (d) $\frac{8}{15}$
(e) none of these

Ⓐ $A = 15$
Ⓑ $B = 20$

work completed = $(A+B) \times 4$

$\Rightarrow (4+3) \times 4$

$\Rightarrow 28$

not completed

$$\frac{32}{60} = \frac{8}{15}$$

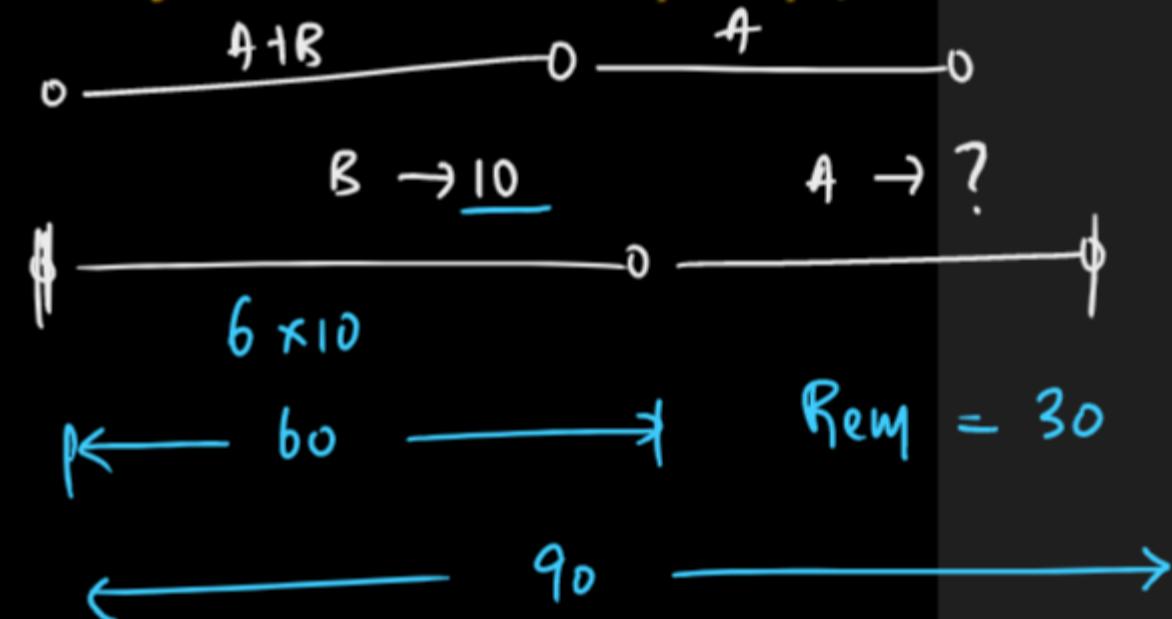
Part of / fraction of work completed
 $= \frac{28}{60} = \frac{7}{15}$



T&W 07 : A can finish a work in 18 days and B can do the same work in 15 days. B worked for 10 days and left the job. In how many days, A alone can finish the remaining work?

- (a) 8 $\textcircled{5} = \frac{90}{18} \quad A = 18 \quad > \textcircled{90}$
- (b) 5 $\cancel{5} = \frac{90}{15} \quad B = 15$
- (c) $6 \textcircled{6} = \frac{90}{15} \quad B = 15$
- (d) $5 \frac{1}{2}$
- (e) None of these

$$\begin{aligned}
 A_{\text{1s}} \text{ Days} &= \frac{\text{Rem}}{\text{T.W}} \\
 &= \frac{\text{Al}_s \text{ Effic}}{30} \\
 &= \frac{30}{5} = \boxed{6 \text{ days}}
 \end{aligned}$$



T&W 08 : A can do a piece of work in 10 days, while B can do the same work in 15 days, then their efficiency ratio?

- (a) 3 : 2
- (b) 2 : 1
- (c) 1 : 3
- (d) 2 : 3
- (e) 3 : 1

$$\begin{array}{rcl} A & = & 10 \\ & & \times (30) \\ B & = & 15 \\ & & \hline \end{array}$$

Days \propto Efficiency

$$\frac{1}{10} : \frac{1}{15} \quad 3 : 2$$

$$\begin{array}{rcl} A's \text{ eff} & : & B's \text{ eff} \\ \frac{30}{10} & : & \frac{30}{15} \\ [3 & ; & 2] \end{array}$$

$$\begin{array}{l} A = 3 \\ B = 6 \end{array}$$



T&W 09 : (A is twice efficient as B.) A and B together can finish the work in 5 days. Then work will be finished by B alone in how many days?

(a) 10

Effic

$$\begin{array}{ccc} A & & B \\ 2 & : & 1 \end{array}$$

(b) 15

(c) 20

(d) 25

(e) None of these

$$A+B = 5 \text{ days}$$

$$B^1 \text{ days} = \frac{T \cdot w}{B^1 \text{ s eff}}$$

$$= \frac{3 \times 5}{1} = 15 \text{ days}$$

$$\text{Total work} = \text{Efficiency} \times \text{Days}$$

$$(2+1) \times 5$$

$$A \text{ days} = \frac{72 \times 2}{3}$$



$$\frac{A+B+C}{3} = 4.5$$

T&W 10 : A and B can do a piece of work in 18 days, B and C in 24 days, A and C in 36 days. In what time can they do it all working together.

- 1) 12 days 2) 13 days 3) 16 days 4) 26 days 5) 15 days

$$\frac{T_2}{18} + B = 18$$

$$\frac{T_2}{24} + B + C = 24$$

$$\frac{T_2}{36} + A + C = 36$$

$$A + B + C = ?$$

$$\underline{\underline{A+B}} = 4 \rightarrow (1)$$

$$\underline{\underline{B+C}} = 3 \rightarrow (2)$$

$$\underline{\underline{A+C}} = 2 \rightarrow (3)$$

$$2(A+B+C) = (4+3+2)$$

$$A+B+C = \frac{9}{2} = 4.5$$

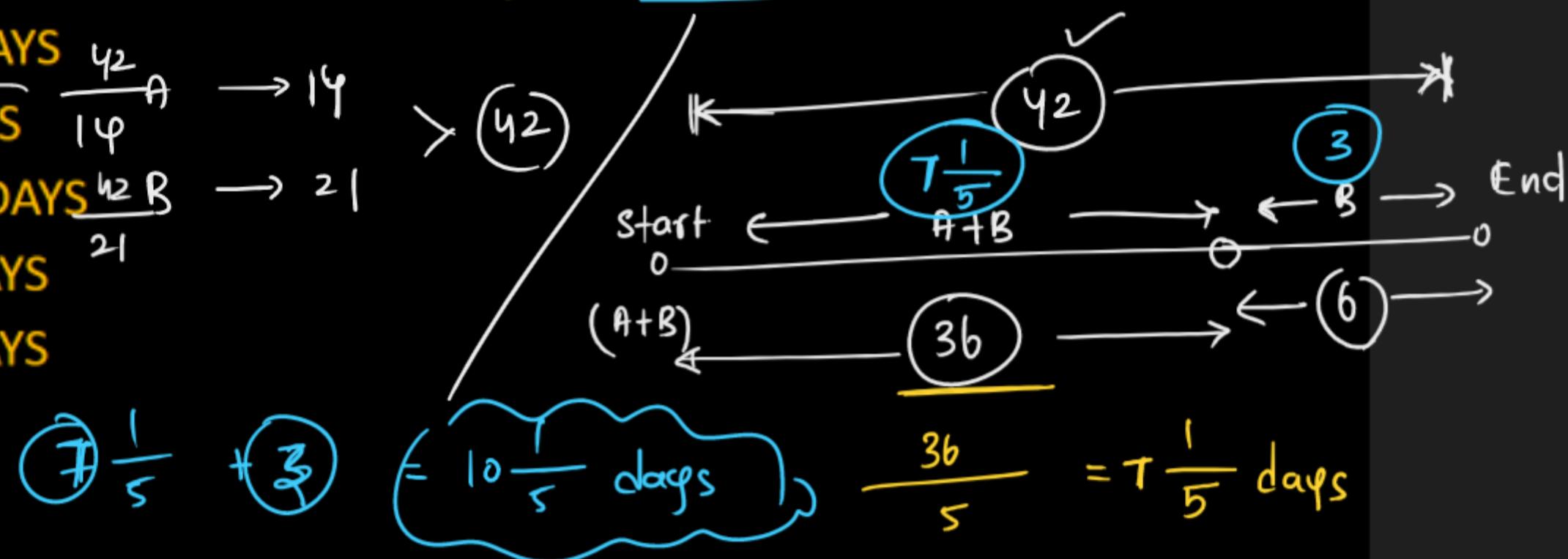
$$\text{Days} = \frac{T.W}{E.H}$$

$$\Rightarrow \frac{8 \cancel{\frac{72 \times 2}{3}}}{9}$$

$$\Rightarrow 16$$

T&W 11 : A can do a piece of work in 14 days which B can do in 21 days. They began together but 3 days before the completion of the work, A leaves off. The total number of days to complete the work?

- A) $6 \frac{3}{5}$ DAYS
- B) $8 \frac{1}{2}$ DAYS
- C) $10 \frac{1}{5}$ DAYS
- D) $13 \frac{1}{2}$ DAYS
- E) $10 \frac{1}{2}$ DAYS



T&W 15 A can do a certain job in 12 days. B is 60% more efficient than A. The number of days it takes B to do the same piece of work is

$$A = 12 \text{ days}$$

effic
B : 4

160 : 100

$\sqrt{8 : 5}$

$$B \text{ days} = \frac{T.w}{B \text{ % eff}} = \frac{\frac{4}{Eff} \times \frac{4}{Days}}{8}$$



Ans $\Rightarrow \frac{\cancel{5} \times 12}{\cancel{8} 2} = \frac{15}{2} \left(= 7 \frac{1}{2} \text{ days} \right)$

$\frac{5 \times 12}{8}$



T&W 16 : A is 50% as efficient as B. C does half of the work done by A and B together. If C alone does the work in 20 days, then A, B and C can do the work in?

effici

A	B	C
50	100	$\frac{A+B}{2}$
1 : 2		$\frac{3}{2}$

$$\begin{array}{r} A : B : C \\ 1 : 2 : \frac{3}{2} \end{array}$$

$$\begin{aligned} & C = \frac{A+B}{2} \\ & (A+B+C) \text{ days} = \frac{B \times 20}{\frac{3}{2}} \\ & \Rightarrow \frac{2 \times 20}{3} = 6 \frac{2}{3} \text{ days} \end{aligned}$$

T.w
Eff

$$\begin{array}{r} A : B : C \\ 2 : 4 : 3 \end{array}$$

20 days



T&W 19 : A and B can complete a piece of work in 12 and 18 days respectively. A begins to do the work and they work alternatively one at a time for one day each. The whole work will be completed in ?

$$\textcircled{3} \quad A = 12 \quad > \textcircled{36}$$

$$\textcircled{2} \quad B = 18$$

<u>A</u>	<u>B</u>	<u>A</u>	<u>B</u>	<u>A</u>	<u>B</u>	...
1 st	2 nd	3 rd	4 th	5 th	6 th	
3	2	3	2	3	2	

$$(A+B) \text{ 2 day} \rightarrow 3+2$$

$$(A+B) \text{ } \overset{x T}{\cancel{\text{2 day}}} \rightarrow 5 \times T$$

$$(A+B) \text{ } \cancel{14 \text{ day}} \rightarrow 35$$

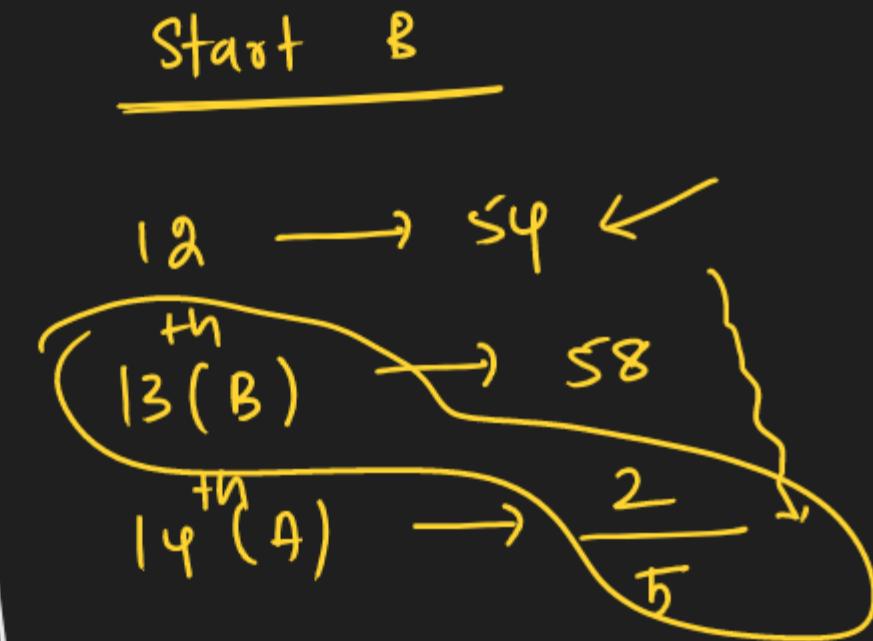
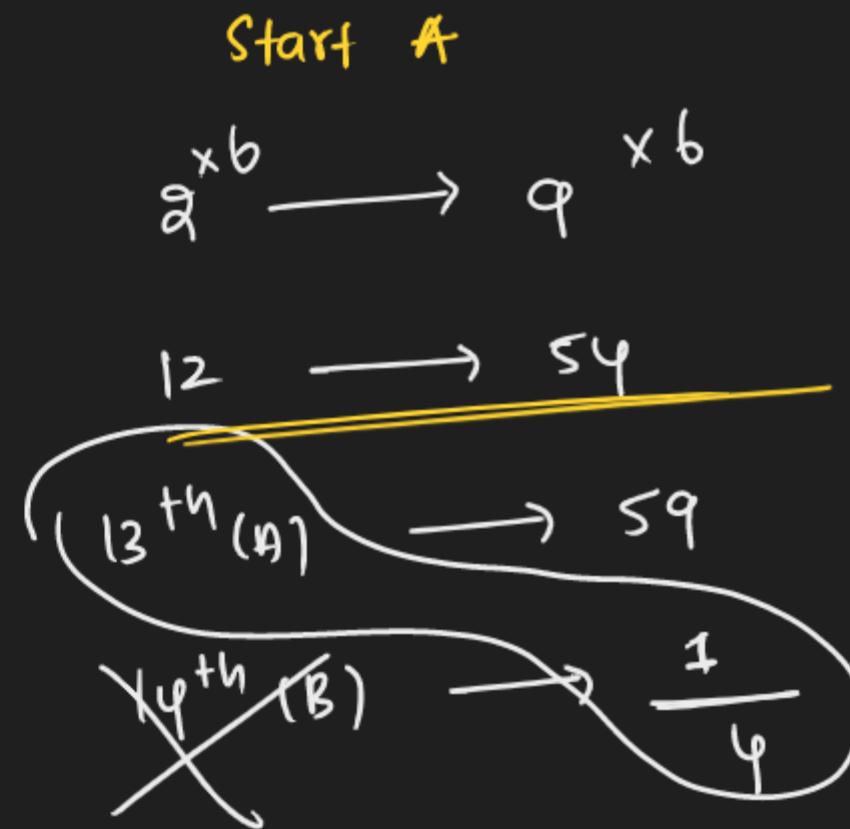
$$15^{\text{th}} (A) \Rightarrow \frac{1}{3}$$

$$\text{Ans} : 14 \frac{1}{3} \text{ days}$$



$$\begin{array}{l} \textcircled{5} \quad A = 12 \\ \textcircled{4} \quad B = 15 \end{array} \rightarrow \textcircled{60}$$

Start with A

$$12 \frac{1}{4} \text{ days}$$


$13 \frac{2}{5} \text{ days}$

T&W 18 : A can do a piece of work in 6 days and B alone can do it in 8 days. A and B undertook to do it for Rs.320 with the help of C, they finished it in 3 days. How much is paid to C.

- 1) Rs.30 2) Rs.40 3) Rs.60 4) Rs.80 5) Rs. 45

Wage\$

$$\textcircled{4} \quad A = 6$$

$$\textcircled{3} \quad B = 8$$

$$\textcircled{8} \quad A+B+C = 3$$

$$\textcircled{24}$$

$$\begin{array}{c} A \qquad B \qquad C \\ \hline 4 \quad : \quad 3 \quad : \quad (1) \end{array} \leftarrow \text{Efficiency}$$

$$A's \text{ share} = \frac{1}{8} \times 320$$

$$= 40 \text{ Rs}$$



T&W 20 : A certain number of men can complete a job in 30 days. If there were 5 men more, it could be completed in 10 days less. How many men were in the beginning?

- (1) 10 (2) 15 (3) 20 (4) 25

$$\frac{m_1 \times D_1}{w_1} \times T_1 \times E_1 = \frac{m_2 \times D_2}{w_2} \times T_2 \times E_2$$

$$\begin{array}{l|l}
x \times 30 & = (x+5) (20) \\
30x & = 20x + 100 \\
\hline
10x & = 100 \\
x & = 10
\end{array}$$

$$T, \omega = m \times D$$



T&W 21 : 5 men and 12 boys finish a piece of work in 4 days, 7 men and 6 boys do it in 5 days. The Ratio between the efficiencies of a man and boy is?

- A. 1:2 B. 2:1 C. 2:3 D. 6:5

$$(5m + 12B) \times 4 = \text{Total Work}$$

$$(7m + bB) \times 5 = \text{Total work}$$

$$\overbrace{(5m+12B) \times 4}^{48} = 5 \times \overbrace{(\frac{7}{3}m+6B)}^{30}$$

$$18\beta = 15m$$

$$\frac{B}{m} = \frac{15}{18} = \frac{5}{6}$$



T&W 22 : 9 men and 12 boys finish a job in 12 days, 12 men and 12 boys finish it in 10 days. 10 men and 10 boys shall finish it in how many days?

- A. 8 B. 10 C. 12 D. 14

$$(9M + 12B) \times \cancel{12} = (12M + 12B) \times \cancel{10}$$

$$\frac{54}{60} \quad \frac{(2)}{20+10} \quad \frac{(1)}{18+12}$$

$$(10M + 10B) \times ? = (9M + 12B) \times 12$$

$$(M + 12B) \times 12 = TW \quad 12B = 6M$$

$$(M + 12B) \times 10 = TW \quad \frac{B}{M} = \frac{6}{12}$$

$$\boxed{\frac{B}{M} = \frac{1}{2}}$$

$$\cancel{30} \times ? = \cancel{30} \times 12$$

$$\boxed{? = 12 \text{ days}}$$



T&W 23 : (3 men or 6 women can do a piece of work in 20 days.) In how many days will 12 men and 8 women do the same work?

A. $\frac{7}{2}$

B. $\frac{15}{4}$

C. 5

D. 4

$$\textcircled{3m \times 20} = 6w \times 20$$

$$\frac{m}{w} = \frac{6}{3}$$

$$\boxed{\frac{m}{w} = \frac{2}{1}}$$

$$\left(\frac{12m}{24} + \frac{8w}{8} \right) \times ? = \frac{(2)}{3m} \times 20$$

$$32 \times ? = 120$$

$$? = \frac{120}{32} = \frac{30}{8} = \frac{15}{4}$$

$$\boxed{= 3 \frac{3}{4} \text{ days}}$$



T&W 25 : A company employed 200 workers to complete a certain work in 150 days. If only one-fourth of the work has been done in 50 days, then in order to complete the whole work in time, the number of additional workers to be employed was

- (1) 100 (2) 300 (3) 600 (4) 200

$$\frac{\cancel{150} \times m_1 \times D_1 \times H_1 \times E_1}{\cancel{200} w_1} = \frac{m_2 \times D_2 \times H_2 \times E_2}{w_2}$$

$$\frac{200 \times 50}{\cancel{4} \times \text{work}} = \frac{m \times 100}{\frac{3}{4} \times \text{work}}$$

$$\frac{200 \times 50}{\cancel{4}} = \frac{m \times 100}{\frac{3}{4}}$$

$$m = 300$$



T&W 25 : A company employed 200 workers to complete a certain work in 150 days. If only one-fourth of the work has been done in 50 days, then in order to complete the whole work in time, the number of additional workers to be employed was

- (1) 100 (2) 300 (3) 600 (4) 200

$$\frac{\frac{150}{200} \times m_1 \times D_1 \times H_1 \times E_1}{w_1} = \frac{m_2 \times D_2 \times H_2 \times E_2}{w_2}$$

$$\frac{200 \times 50}{\frac{1}{4}} = \frac{200 \times D}{\frac{3}{4}}$$

$$\frac{200 \times 50}{\frac{1}{4}} = \frac{200 \times D}{\frac{3}{4}}$$

$$150 = 0$$

Q. 28

$$A \times \frac{1}{4} = 4$$

$$A \times 1 = 16 \text{ days}$$

$$B \times \frac{3}{4} = 3$$

$$B \times 1 = \cancel{3} \times \frac{4}{\cancel{3}}$$

$$\boxed{B \times 1 = 4 \text{ days}}$$

Q. 29

$$(A+B+C) \times \frac{3}{4} = 12$$

$$\textcircled{5} (A+B+C) \times \underline{\frac{1}{2}} = \cancel{12} \times \frac{4}{3}$$

= 16

$$A \times 1 = 80 \text{ days}$$

$$(B+C) \times \frac{2}{5} = 8$$

$$\textcircled{4} (B+C) \times \underline{\frac{1}{2}} = \cancel{8} \times \frac{5}{4}$$

= 20

$$A \text{ days} = \frac{T \cdot w}{\text{eff}}$$

$$= \frac{\frac{3}{8} \times 80}{1}$$

$$= \frac{30}{1}$$

30 days

Book Pg. - Q. 2

$$A \rightarrow 2 \frac{3}{4} \rightarrow \frac{11}{4}$$

$$B \rightarrow 3 \frac{2}{3} \rightarrow \frac{11}{3}$$

$$A's \text{ eff} = \frac{11}{11/4} = 4$$

$$B's \text{ eff} = \frac{11}{11/3} = 3$$



$$\frac{\text{LCM of NVM}}{\text{HCF of DEN}} = \frac{11}{1} = 11$$

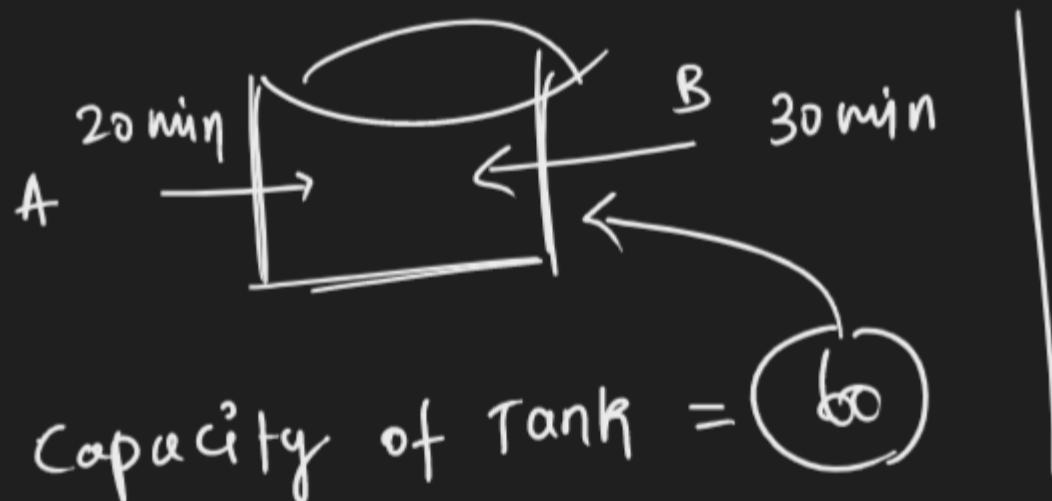
$$(A+B) \text{ Days} = \frac{T \cdot W}{(A+B) \text{ eff}}$$

$$= \frac{11}{7}$$

$$= 1 \frac{4}{7} \text{ days}$$



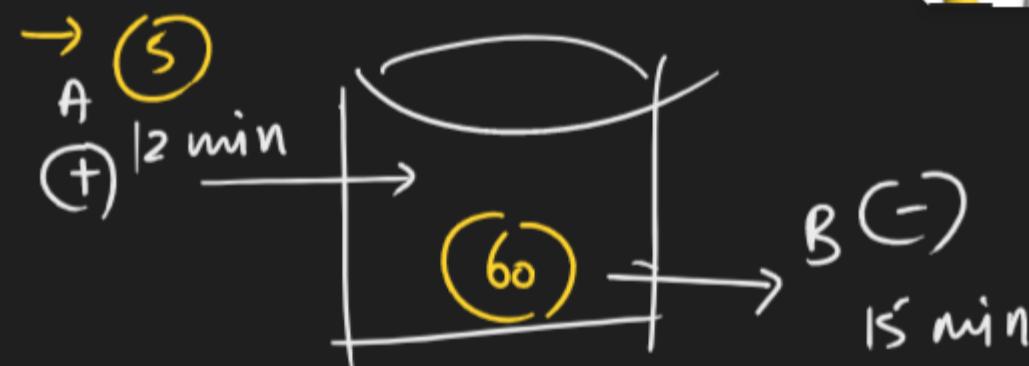
PIPES AND CISTERNS



$$A's \text{ eff} = \frac{60}{20} = 3 \text{ lit/min}$$

$$B's \text{ eff} = \frac{60}{30} = 2 \text{ lit/min}$$

$$\begin{aligned} 1 \text{ min} &\longrightarrow 5 \text{ lit} \\ ? &\longrightarrow 60 \text{ lit} \end{aligned}$$



4
1 min - 1 lit

60 min - 60 lit

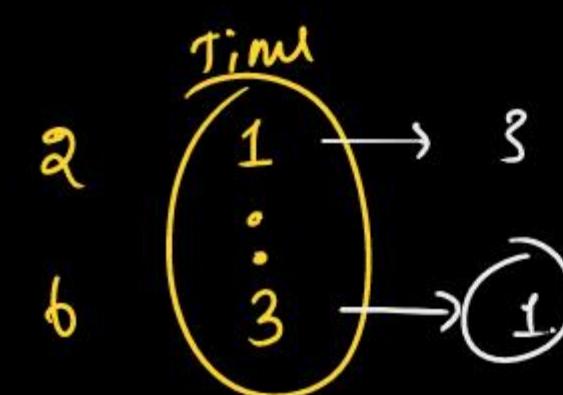


T&W 28 : A does half as much work as B in one sixth of the time.) If together they take 10 days to complete a work, how much time shall B take to do it alone? 

- (1) 70 days (2) 30 days (3) 40 days ANS (4) 50 days

work
A 1×2
B 2

Time
 1×2
6



$$B \text{ days} = \frac{T \cdot w}{B \text{ eff}} \\ = \frac{(3+1) \times 10}{1} \\ = 40$$



$\frac{3}{4} \rightarrow A$
 $\frac{1}{4} \rightarrow B$

T&W 17 : A does half as much work as B in three-fourth of the time. If together they take 18 days to complete the work, how much time shall B take to do it?

- 1) 40 days 2) 35 days 3) 25 days 4) 30 days 5) 40 days

	work	Time	T	F Ratio
A	1×2	3×2	6	3
B	2	4	4	2

$\frac{5 \times 18}{3} = \boxed{30 \text{ days}}$

Eff

2
:
3