

# LSST Catalog-level Realization of Gravitationally-lensed Quasars

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The scale of the LSST dataset will be enormous that we need a different method to classify lensed images of quasars than manually picking the images out. We should anticipate extracting as much information out of its catalogs as possible before ever turning to the pixel-level data. In this work we explore the use of simple, low-multiplicity Gaussian mixture models for realizing gravitational lens systems in LSST catalog space, to enable both large-scale sample simulation and direct model inference.

## I. INTRODUCTION

The Large Synoptic Survey Telescope (LSST), a wide-field survey telescope with the diameter of 8.4m, will start running in Chile in 2020 [3]. This telescope has a 3.5  $deg$  of field of view, would cover around 30000  $deg^2$  in the sky, and uses  $u$ ,  $g$ ,  $r$ ,  $i$ ,  $z$ , and  $y$  filters [5]. The telescope will give an extensive amount of astronomical data that could be used for the study of Solar System, Extragalactic structures, near-Earth asteroids, radiant radio sources, Dark Matter, and Dark Energy [5].

LSST Dark Energy Science Collaboration (DESC) also anticipate to detect around 8000 strongly lensed systems that will provide useful information such as cosmological time delay or lens mass distribution [4] [9] [6]. Time delay could be used to infer cosmological parameters [1] which describes the state of the universe.

In order to perform such research, finding the lensed system among the enormous set of data is crucial. However, LSST is also expected to produce 80 terabytes of data each night [5]. Considering the amount of the data that LSST will produce, pixel-level searching with images([2]) may be impossible. In order to solve the problem, we propose the lens classification with catalog-level searching with machine learning techniques (SLRealizer).

The attempt to use Machine Learning to detect lensed system is not a completely new idea. [7] suggests that morphological classification of the lensed system using the Convolutional Neural Network(CNN) could be effective. [8] has developed 'lensextractor' that uses convolution neural network to train and test the software to detect the lensed system.

The 'SL Realizer' project largely consists of two major parts: finding the useful feature sets to classify the lensed systems from other objects and classifying the lensed systems with different machine learning algorithms.

## II. METHOD

### A. Preparation of Data

Twinkles, a simulated LSST sky with observed with six filters for ten years, provided the ten years of mock observation history. We also had OM10 mock lensed systems [9].

We assumed that OM10 mock lensed systems are composed of point-like sources. This means that the size of the galaxies as well as the quasar images had the effective radius of zero.

obsHistID	expMJD	filter	FWHMeff	fiveSigmaDepth
183767	59823.286523	g	1.093153	24.377204
183811	59823.307264	g	1.23193	24.289872
184047	59823.418685	z	0.908511	21.923566
185595	59825.256044	r	0.949096	24.128617
185736	59825.325979	g	1.242407	24.316968
185785	59825.352519	g	1.139232	24.436879
187493	59827.2603	z	0.807941	22.896684
187525	59827.278039	z	0.789221	22.990253
187546	59827.287816	z	0.748829	23.078407

TABLE I: Few entries of the twinkles mock observation history data. Full data can be accessed here.

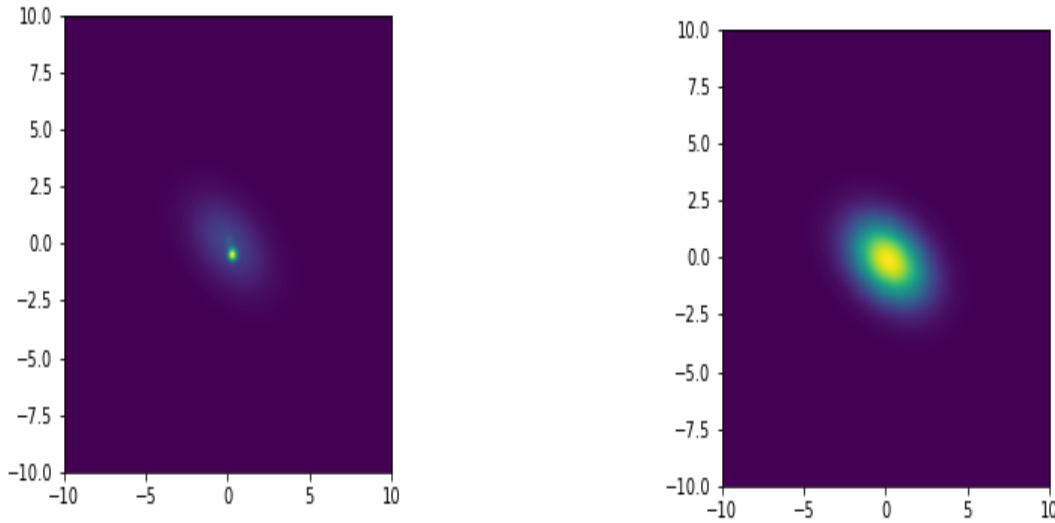
In order to save some computation time, we queried the first three years of the observation which yields 263 observation epochs. We also selected LSST-like OM10 mock lensed systems by querying with magnitude cut of 22.5.

## III. DATA PREPARATION

### A. Toy Source Catalog

Using the data from IIA, we were able to make an each entry of catalog describing how each lensed system would look like on a particular night. While doing this, we assumed that all the sources in the lensed system have Gaussian point spread functions. Also, we realized the systems with a null-deblender, meaning that we assumed that all the lensed images and the lens were observed as one big source.

In order to do so, we used Galsim package in Python. For each lensed system, we drew a Gaussian that has an effective radius of a galaxy as well as adding the rotation angle and shears to the values. We also drew the Gaussians



(a) Before null-deblending, the whole system looks like this image. The brightest source is the lensing galaxy, and there are two dimmer quasar images near the galaxy. There is only one quasar images that are obvious that makes the image more elliptical.

(b) After null-deblending, the whole system looks like this image. All the sources look like one big source observed at once. The color scheme used in matplotlib could be a little misleading here, but overall luminosity has not changed.

FIG. 1: Example null-deblending. The number on the axis corresponds to arcseconds, (0,0) being the center of the lensed system. We used a lensed system with ID 4898214 to demonstrate the above figure.

that have an effective radius of zero in the position for the quasar images. Then, we convolved the Gaussians with the Gaussian point spread functions. After then, we added all the convolved Gaussian onto the two-dimensional grid that has the same degree-to-pixel ratio (0.2 arcseconds per pixels) as LSST, realizing the total sum as one Gaussian. After the realization, we could get ellipticity, zeroth moment, the first moment, and the second moment per one big convolved Gaussian.

The toy catalog is in III A.

### B. Toy Object Catalog

After generating the source catalog, we computed the object table whose entree describes average properties of each lensed system per filter. In order to do so, we queried each lensed system in the source catalog. Then, for each lensed system, we computed the average properties for each filter.

The toy catalog is in IV B.

### C. Feature Selection

For now, we focused on classifying the lensed systems from the SDSS galaxies. We expect the lensed images to appear near the bright, massive galaxies. Thus, if we can differentiate the galaxies with lensed images with the galaxies without them, it would be really helpful.

We expect that the quasar images will be brighter in the shorter wavelength filters. The galaxies will be brighter in the longer wavelength filters. Thus, when we observe a lensed system through a  $u$  filter (the shortest wavelength filter that OM10 has), we will see the more stretched object because of the contribution from the quasar images. However, in the  $z$  band, we will see a round object because of the contribution from the lens. By comparing the features in the  $u$  filter and the  $z$  filter, we will thus be able to see bigger changes in the properties for the lensed systems than SDSS galaxies.

The features that we could get from the object table is changes in the first moment along the x-axis (reference to the  $r$  filter), changes in the first moment along the y-axis (reference to the  $r$  filter), changes in the position (reference to the  $r$  filter), ellipticities, rotation angles, fluxes, and sizes.

The catalog of SDSS galaxies also provides the same features. Magnitude systems are the same in both SDSS and OM10, and the units are scaled to be the same. However, the only difference was in the sizes. SDSS's definition of size was  $I_{xx} + I_{yy}$ . Galsim calculates the size of OM10 systems by calculating the determinant of the second moment ( $M = I_{xx} * I_{yy} - I_{xy} * I_{xy}$ ) and applying the fourth root on it ( $\sqrt[4]{M}$ ). In order to solve the problem by scaling the SDSS sizes, we multiplied the power of pixel-to-arcsec ratio to change the unit to arcseconds, multiplied two to convert the half size to the full size, and applied the square root to the value to get a right dimension.

Using these values, we computed various additional features. We plotted SDSS galaxies and OM10 lensed systems onto the corner plot III C, and chose the features that differentiated OM10 lensed systems from SDSS galaxies the most.

#### D. Classification

We have 2323 OM10 lensed systems and 16000 SDSS galaxies. In order to make the balanced test data set, we randomly selected 2323 SDSS galaxies. We mixed the order of those two samples so that there will be a roughly same number of each OM10 and SDSS samples in both the test and the training data. Then, using the scikit train\_test\_split method, we selected 75% of the data to be the training set and performed the test on the remaining 25%.

According to the scikit's choosing the right estimator, we were able to choose three different algorithms for the classification purposes. We did have more than 50 samples, we were predicting a category, we did have a labeled data, and we had less than 100K samples in a text data. This yields Linear SVC, KNeighbors Classifier, and Ensemble classifiers such as Random Forest.

Detailed results are in IV D.

### IV. RESULTS

#### A. Toy Source Catalog

lensid	MJD	filter	RA	RA_err	DEC	DEC_err	x	x_com_err	y	y_com_err
710960	59823.286523	g	0	0	0	0	2.1350	0	1.2151	0
17432684	59823.286523	g	0	0	0	0	0.1226	0	0.7593	0
50310149	59823.286523	g	0	0	0	0	0.2527	0	0.4665	0
52812164	59823.286523	g	0	0	0	0	0.3874	0	-0.3413	0
flux	flux_err	size	size_err	e1	e2	e	phi	psf_sigma	sky	
21.9127	0.03549	1.4501	0	0.2386	0.3360	0.4121	0.4766	1.093153	24.377204	
18.2072	0.03549	1.1802	0	-0.0550	-0.004712	0.05525	0.04270	1.093153	24.377204	
5.9831	0.03549	1.2253	0	-0.05931	0.02588	0.06471	-0.2057	1.093153	24.377204	
6.2727	0.03549	1.2102	0	-0.03114	-0.05654	0.06455	0.5336	1.093153	24.377204	

TABLE II: Few sample entrees of the toy source catalog. The full toy object catalog can be viewed here

The above is the toy source catalog that we generated. For now, we haven't added error terms and calculated the positions (RA and DEC).

#### B. Toy Object Catalog

III is the toy object catalog that we generated.

#### C. Feature Selection

Full corner plots can be viewed in the SLRealizer's GitHub repository's notebook folder.

lensid	u_flux	u_x	u_y	u_size	u_flux_err	u_x_com_err	u_y_com_err	u_size_err	u_e1	u_e2	u_e	u_phi
710960.0	37.0846	2.2817	1.2996	1.4151	0.2511	0.0	0.0	0.0	0.1399	0.205	0.2496	0.4574
17432684.0	26.7018	0.1211	0.7633	0.971	0.2516	0.0	0.0	0.0	-0.0968	-0.0092	0.0972	0.0497
	g_flux	g_x	g_y	g_size	g_flux_err	g_x_com_err	g_y_com_err	g_size_err	g_e1	g_e2	g_e	g_phi
	19.9485	2.1555	1.2328	1.4608	0.1244	0.0	0.0	0.0	0.1967	0.2768	0.3395	0.4765
	17.5991	0.1221	0.7518	1.2413	0.1244	0.0	0.0	0.0	-0.0532	-0.0045	0.0534	0.0425
	r_flux	r_x	r_y	r_size	r_flux_err	r_x_com_err	r_y_com_err	r_size_err	r_e1	r_e2	r_e	r_phi
	31.0886	2.27	1.2928	1.2608	0.0923	0.0	0.0	0.0	0.1693	0.2395	0.2933	0.4779
	25.2258	0.1215	0.7617	0.9958	0.0923	0.0	0.0	0.0	-0.0867	-0.0078	0.087	0.0457
	i_flux	i_x	i_y	i_size	i_flux_err	i_x_com_err	i_y_com_err	i_size_err	i_e1	i_e2	i_e	i_phi
	26.2547	2.3012	1.3075	1.2154	0.0433	0.0	0.0	0.0	0.1521	0.2146	0.263	0.4773
	22.747	0.1217	0.7612	1.0063	0.0433	0.0	0.0	0.0	-0.0813	-0.0071	0.0816	0.0436
	z_flux	z_x	z_y	z_size	z_flux_err	z_x_com_err	z_y_com_err	z_size_err	z_e1	z_e2	z_e	z_phi
	19.7955	2.264	1.2879	1.2545	0.0322	0.0	0.0	0.0	0.1595	0.2247	0.2755	0.4767
	18.0387	0.1216	0.7587	1.0622	0.0315	0.0	0.0	0.0	-0.0751	-0.0064	0.0754	0.0426

TABLE III: Few sample enrees of the toy object catalog. The full toy object catalog can be viewed [here](#)

As mentioned in III C, we thought comparing features between  $u$  and  $z$  filter will be discriminatory. We chose six main features that we thought would change dramatically between the filters for OM10 lenses – sizes, ellipticities ( $e$ ), rotation angles of galaxies ( $\phi$ ), magnitudes, positions( $\Delta x$ ), and the angle between ellipticity vector and the rotation vector ( $\omega = \frac{e \cdot \phi}{|e||\phi|}$ ).

Here, the centroid of the yellow points(SDSS galaxies) and the purple points(OM10 systems) differed the most for size. Still, we could quantify the importance of the features by putting all the data into the Random Forest Algorithms. The results were as follows.

#### D. Classification

As mentioned in IIID, we used three different algorithms: linear SVC, KNeighbors (Nearest Neighbors), and Random Forest. 4a is the results that we got for each algorithm.

Random forest showed the best performance among the three different algorithms. If we look into the top left corner where all the curves are overlapped, we can see this more obviously. The best classifiers were Random Forest, and the more the number of estimators were, the better the algorithm performed. For the best algorithm, we were able to achieve 98% of the true positive rate(TPR) and 0.04% of the false positive rate(FPR).

### V. CONCLUSIONS

The results suggest that random forest algorithms would be able to differentiate lensed systems from galaxies. Still, even though we have high accuracy, because we expect to have much more non-lensed systems than the lensed systems, we will have more contaminants in the truly-classified lensed systems than the actual lensed systems. For instance, we expect to find 10,000 times more non-lensed systems than the lensed ones. Thus, with 98% of the TPR and 0.042% of the FPR, we will have 430 contaminants per truly classified lensed systems. Thus, it would also be helpful to have a more rigorous model that actually fits physical models to the systems after rejecting all the non lensed-systems using SLRealizer.

In addition, we only compared the features between OM10 lensed systems and SDSS galaxies. It will also be useful to overlap star-star pairs, star-galaxy pairs, quasar-quasar pairs, or quasar-galaxy pairs to see how different the other samples could be from the lensed system.

There are few ways to further improve the classifiers. If we could implement the working deblender that resembles LSSTs deblender, that will increase the performance of the classifiers. We could also add more features such as time-variabilities of quasar images. While making the source and the object catalog, rather than giving equal weights to all the observations, we could weight by how good the seeing was for each night.

In addition, while studying cosmology, gravitationally lensed systems with four images (quads) are generally more useful than the systems with two images (doubles). Thus, comparing how many quads were classified as true out of the testing samples quads should also give useful statistics.

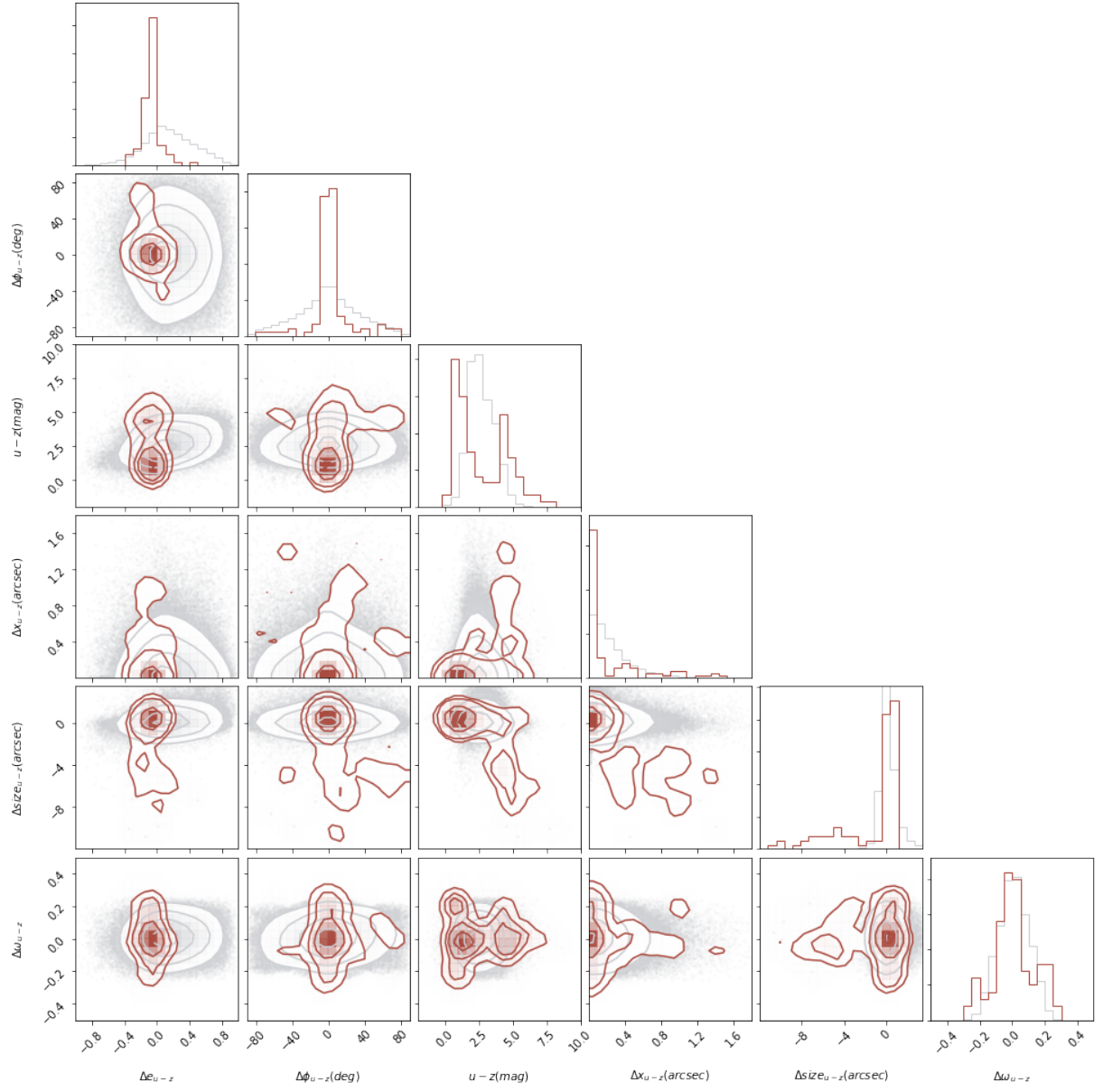


FIG. 2: The cornerplot with six features.

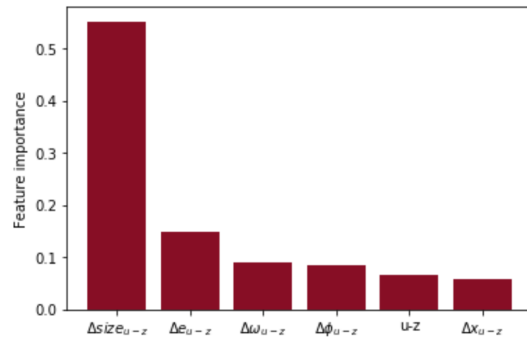


FIG. 3: Feature importance calculated with the Random Forest algorithm.

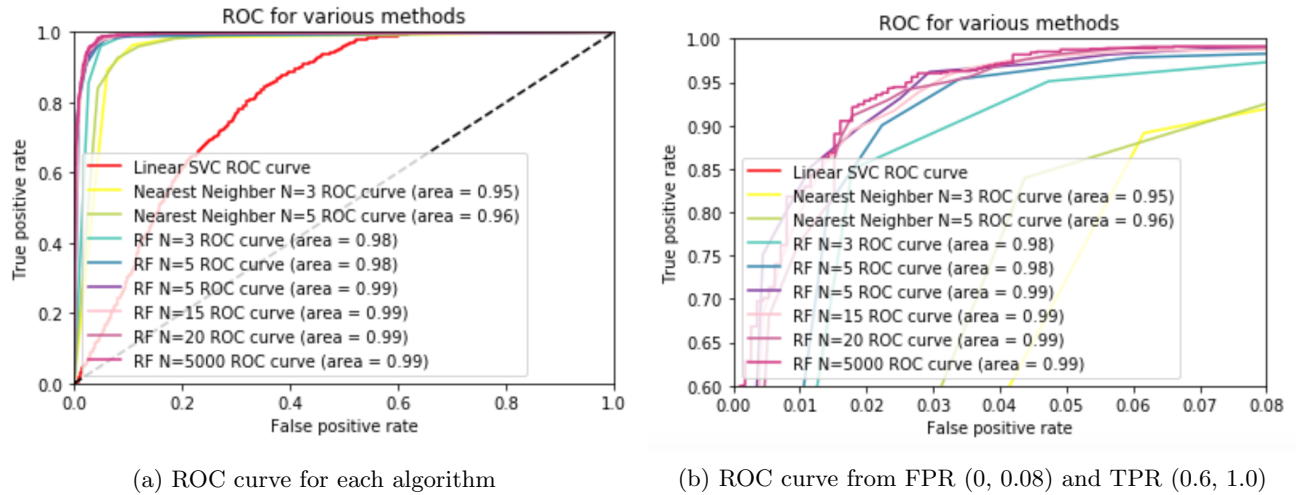


FIG. 4: Example null-deblending.

### Acknowledgments

Here is where you should add your specific acknowledgments, remembering that some standard thanks will be added via the `acknowledgments.tex` and `contributions.tex` files.

This is the text imported from `acknowledgments.tex`, and will be replaced by some standard LSST DESC boilerplate at some point.

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