

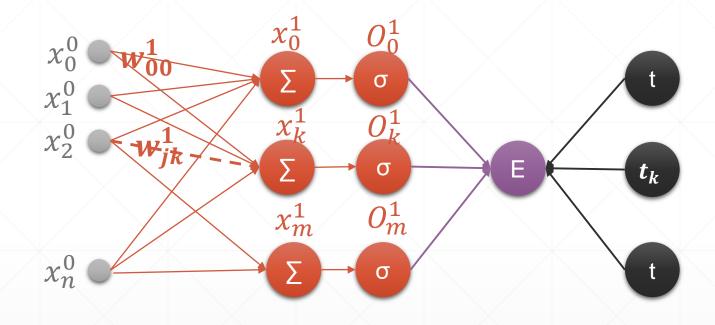
多层感知机梯度

主讲: 龙良曲

Chain rule

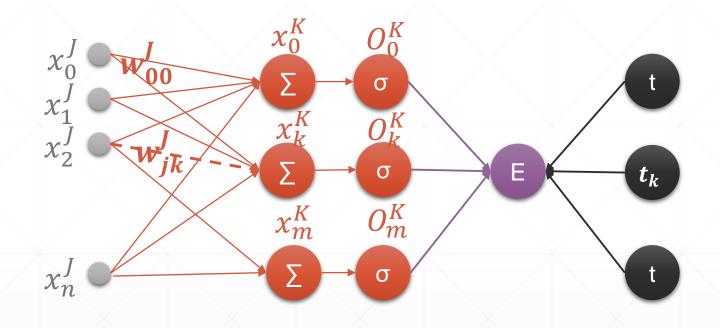
$$\begin{array}{c|c}
 & O_k^1 & O_k^2 \\
\hline
 & W_{jk}^1 & \Sigma & \Sigma \\
\hline
 & \frac{\partial E}{\partial W_{jk}^1} = \frac{\partial E}{\partial O_k^1} \frac{\partial O_k^1}{\partial x} = \frac{\partial E}{\partial O_k^2} \frac{\partial O_k^2}{\partial O_k^1} \frac{\partial O_k^1}{\partial x}
\end{array}$$

Multi-output Perceptron

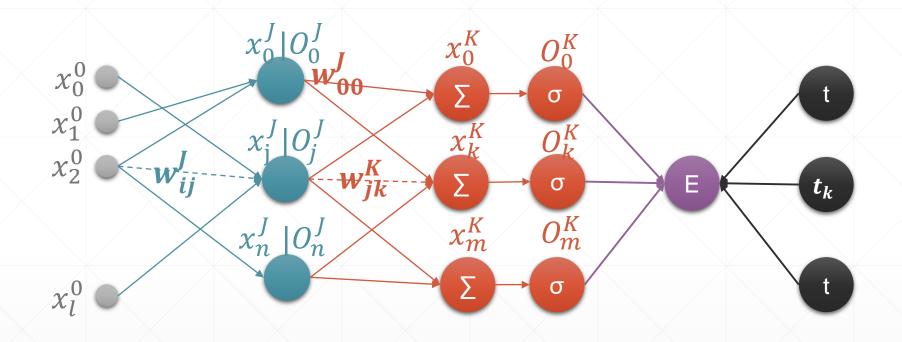


$$\frac{\partial E}{\partial w_{jk}} = \left(O_k - t_k\right) O_k \left(1 - O_k\right) x_j^0$$

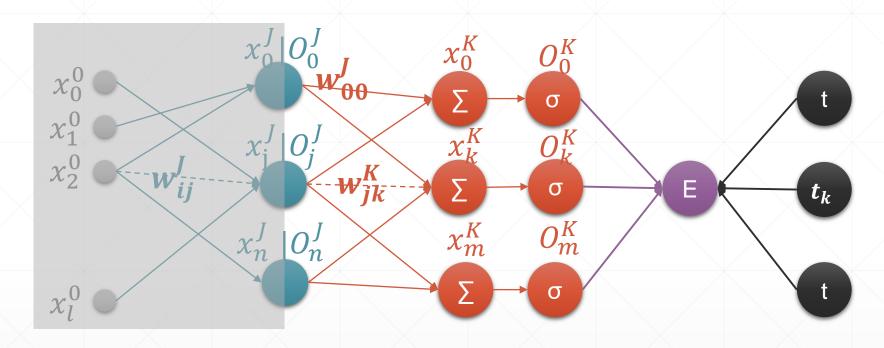
Multi-Layer Perceptron



Multi-Layer Perceptron



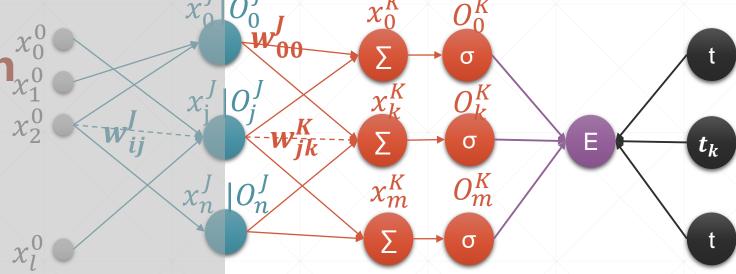
Multi-Layer Perceptron



$$\frac{\partial E}{\partial w_{jk}} = (O_k - t_k) O_k (1 - O_k) x_j^0$$

$$\frac{\partial E}{\partial w_{jk}} = (O_k - t_k) O_k (1 - O_k) O_j^J$$

Multi-Layer Perceptron $\chi_1^{\alpha_0}$

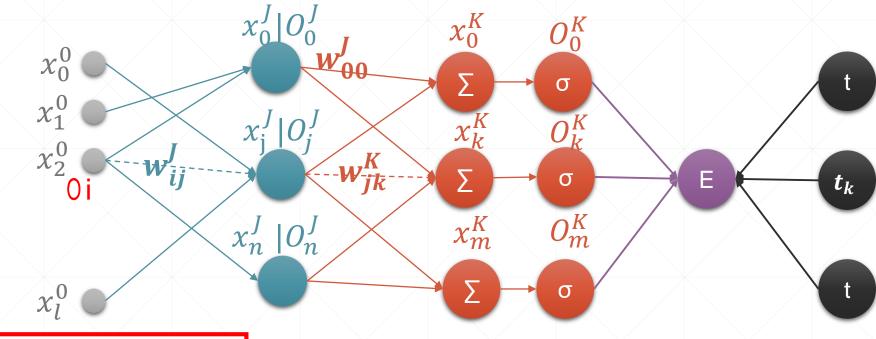


$$\frac{\partial E}{\partial w_{jk}} = (O_k - t_k) O_k (1 - O_k) O_j^J$$

$$\frac{\partial E}{\partial w_{jk}} = \delta_k^K$$

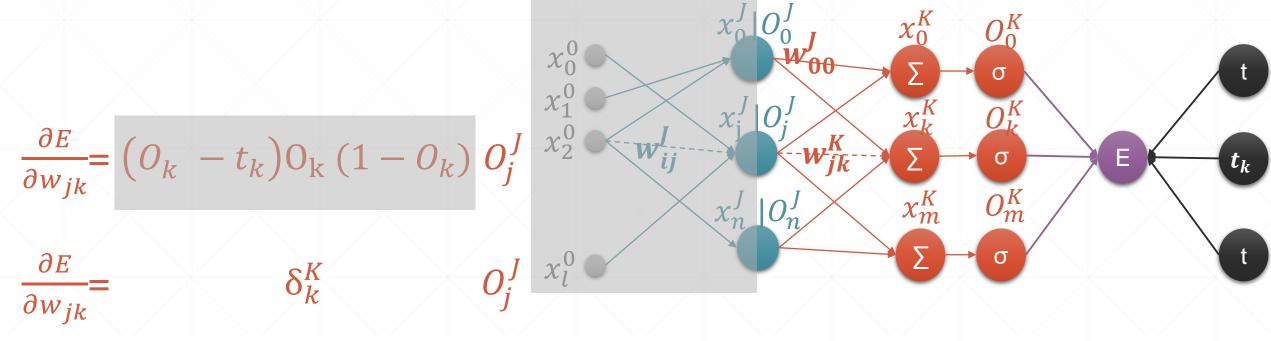
$$O_j^J$$

$$\frac{\partial E}{\partial W_{ij}} = \frac{\partial}{\partial W_{ij}} \frac{1}{2} \sum_{k \in K} (\mathcal{O}_k - t_k)^2 \qquad x_0^0 | \mathcal{O}_0^J \int_{\mathcal{W}_0} x_0^K | \mathcal{O}_0^K |$$



$$\frac{\partial E}{\partial W_{ij}} = \mathcal{O}_j(1 - \mathcal{O}_j)\mathcal{O}_i \sum_{k \in K} (\mathcal{O}_k - t_k)\mathcal{O}_k(1 - \mathcal{O}_k)W_{jk}$$

$$\frac{\partial E}{\partial W_{ij}} = \mathcal{O}_i \mathcal{O}_j (1 - \mathcal{O}_j) \sum_{k \in K} \delta_k W_{jk}$$



$$\frac{\partial E}{\partial W_{ij}} = \mathcal{O}_j(1 - \mathcal{O}_j)\mathcal{O}_i \sum_{k \in K} (\mathcal{O}_k - t_k)\mathcal{O}_k(1 - \mathcal{O}_k)W_{jk}$$

$$\frac{\partial E}{\partial W_{ij}} = \mathcal{O}_i \mathcal{O}_j (1 - \mathcal{O}_j) \sum_{k \in K} \delta_k W_{jk}$$

For an output layer node $k \in K$

$$\frac{\partial E}{\partial W_{jk}} = \mathcal{O}_j \delta_k$$

呼呼

where

$$\delta_k = \frac{\mathcal{O}_k(1 - \mathcal{O}_k)(\mathcal{O}_k - t_k)}{$$
若最后一层无激活函数,则没有这一部分

For a hidden layer node $j \in J$

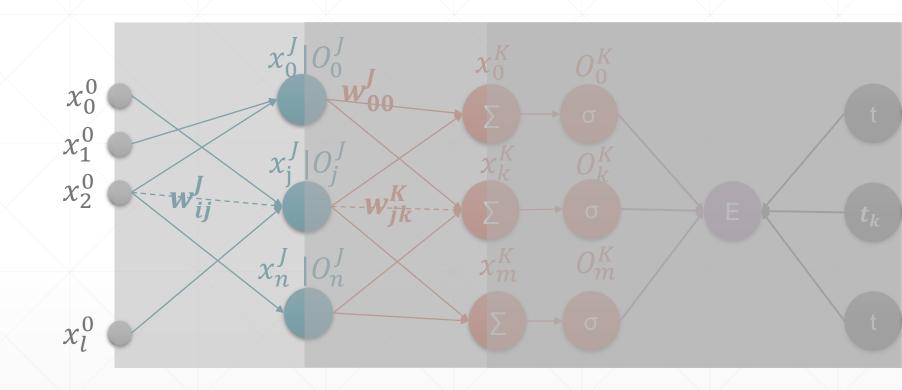
$$\frac{\partial E}{\partial W_{ij}} = \mathcal{O}_i \delta_j$$
 此处的参数矩阵与Ng课程中的互为转置,因为Ng中每层为列向量,而此处为行向量

where

$$\delta_j = \mathcal{O}_j(1 - \mathcal{O}_j) \sum_{k \in K} \delta_k W_{jk}$$



- δ_k^K $\frac{\partial E}{\partial w_{jk}}$
- $\frac{\partial E}{\partial w_{ij}}$
- δ_i^I



Congratulations!



下一课时

优化与训练

Thank You.