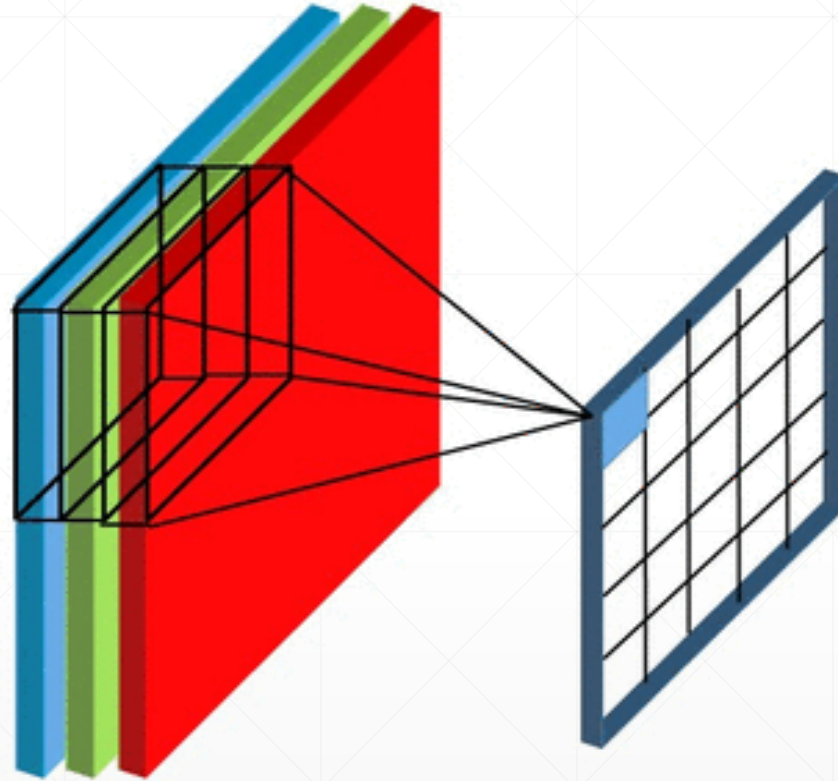


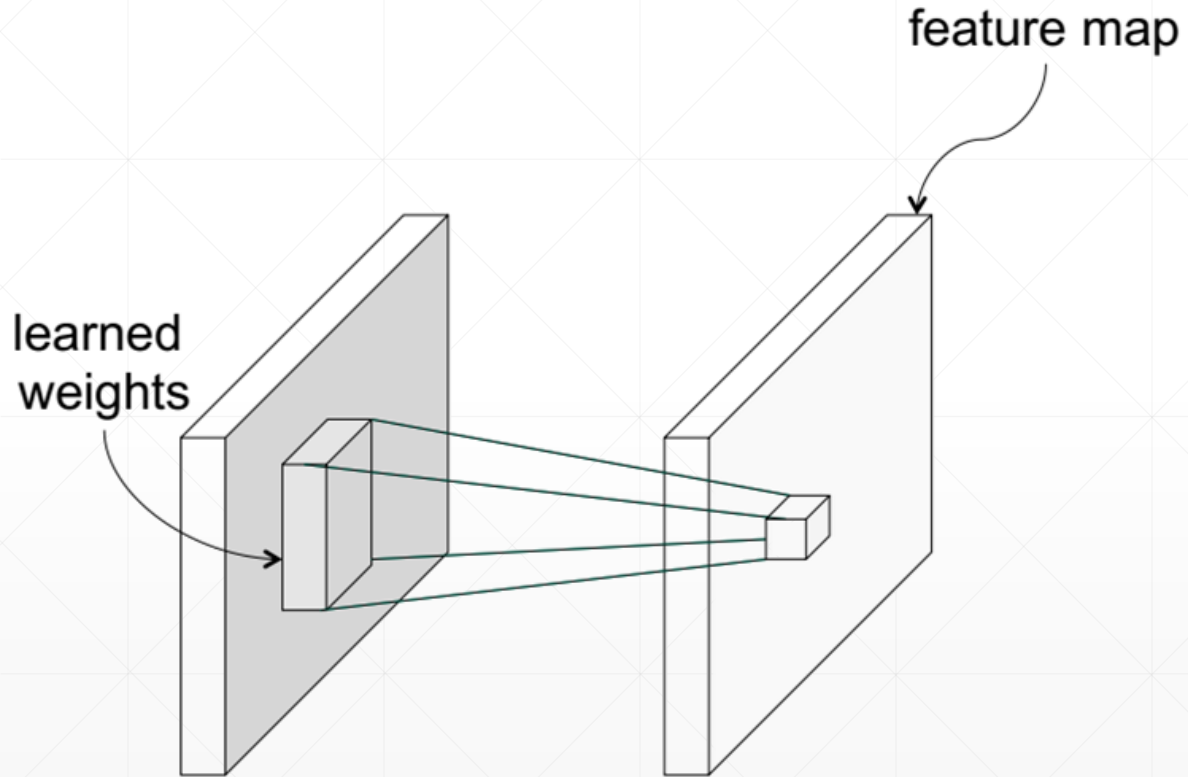
卷积神经网络

主讲：龙良曲

2D Convolution



Kernel size



1x1	1x0	1x1	0	0
0x0	1x1	1x0	1	0
0x1	0x0	1x1	1	1
0	0	1	1	0
0	1	1	0	0

4		

1x1	1x0	1x1	0	0
0x0	1x1	1x0	1	0
0x1	0x0	1x1	1	1
0	0	1	1	0
0	1	1	0	0

4		

1x1	1x0	1x1	0	0
0x0	1x1	1x0	1	0
0x1	0x0	1x1	1	1
0	0	1	1	0
0	1	1	0	0

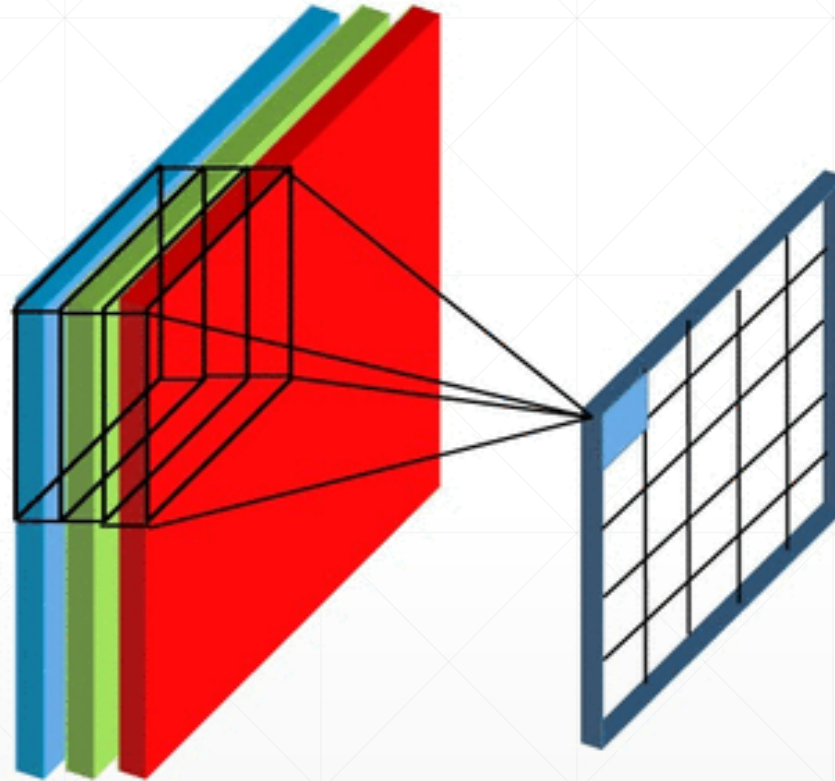
4		

4+4+4	3+3+3	4+4+4
6	12	9
6	9	12

1x1	1x0	1x1	0	0
0x0	1x1	1x0	1	0
0x1	0x0	1x1	1	1
0	0	1	1	0
0	1	1	0	0

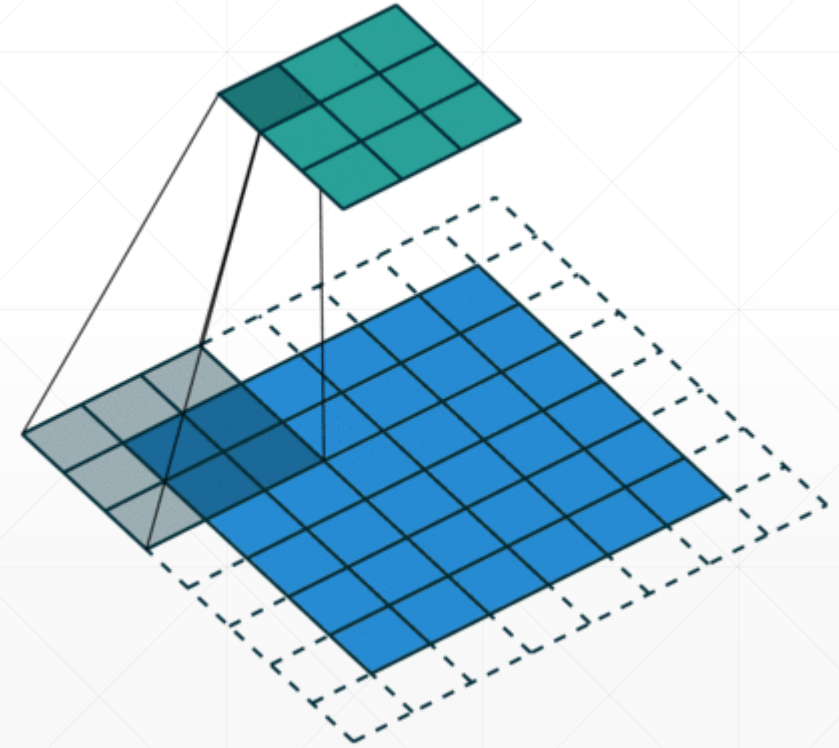
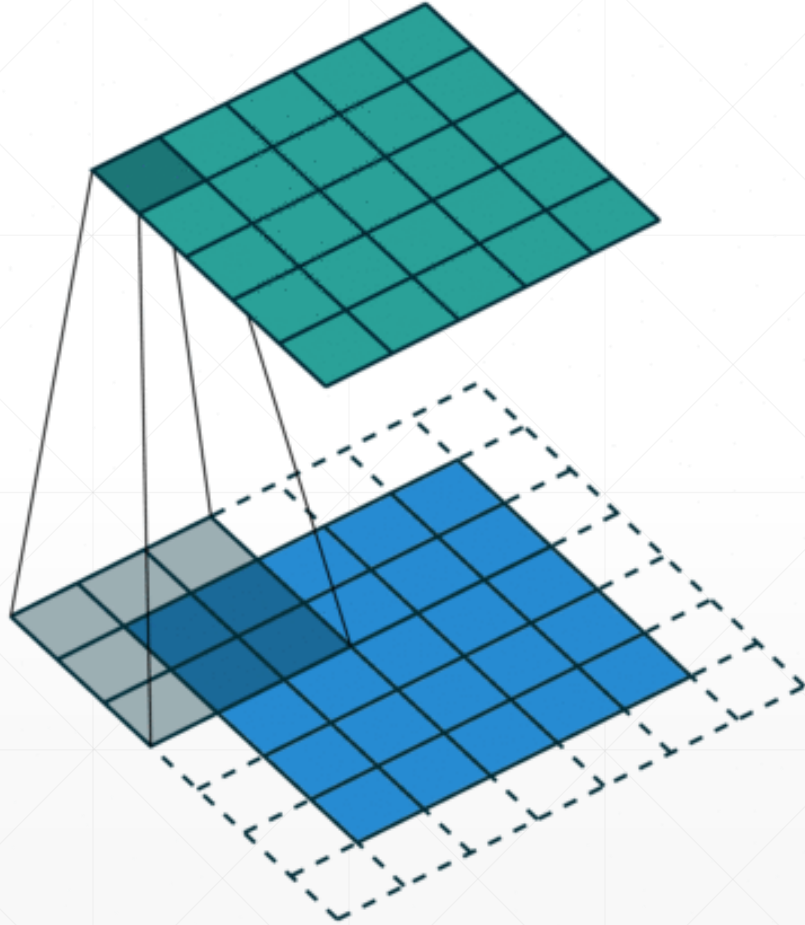
4		

2D Convolution

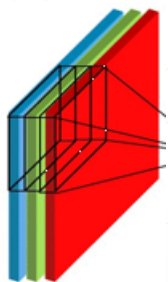


$4+4+4$	$3+3+3$	$4+4+4$
6	12	9
6	9	12

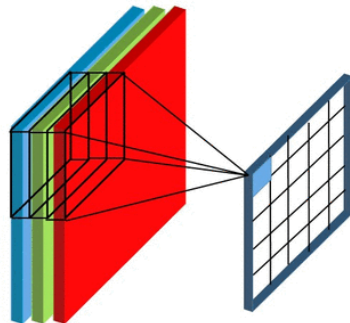
Padding & Stride



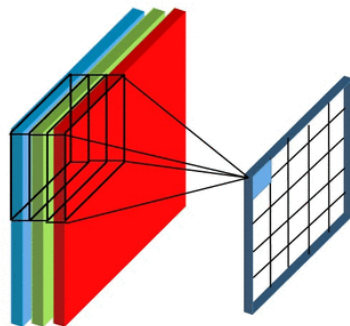
Channels



[1,32,32,3]

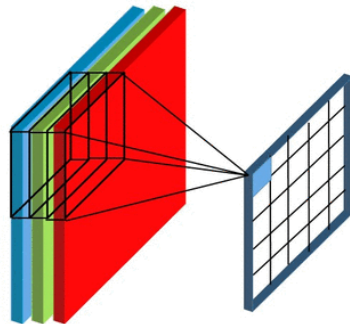


b_0 [4]

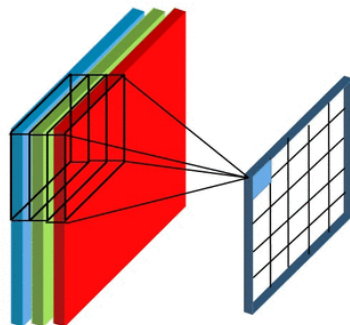


[4, 3, 5, 5]

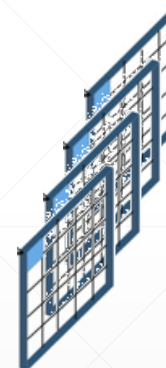
b_1



b_2

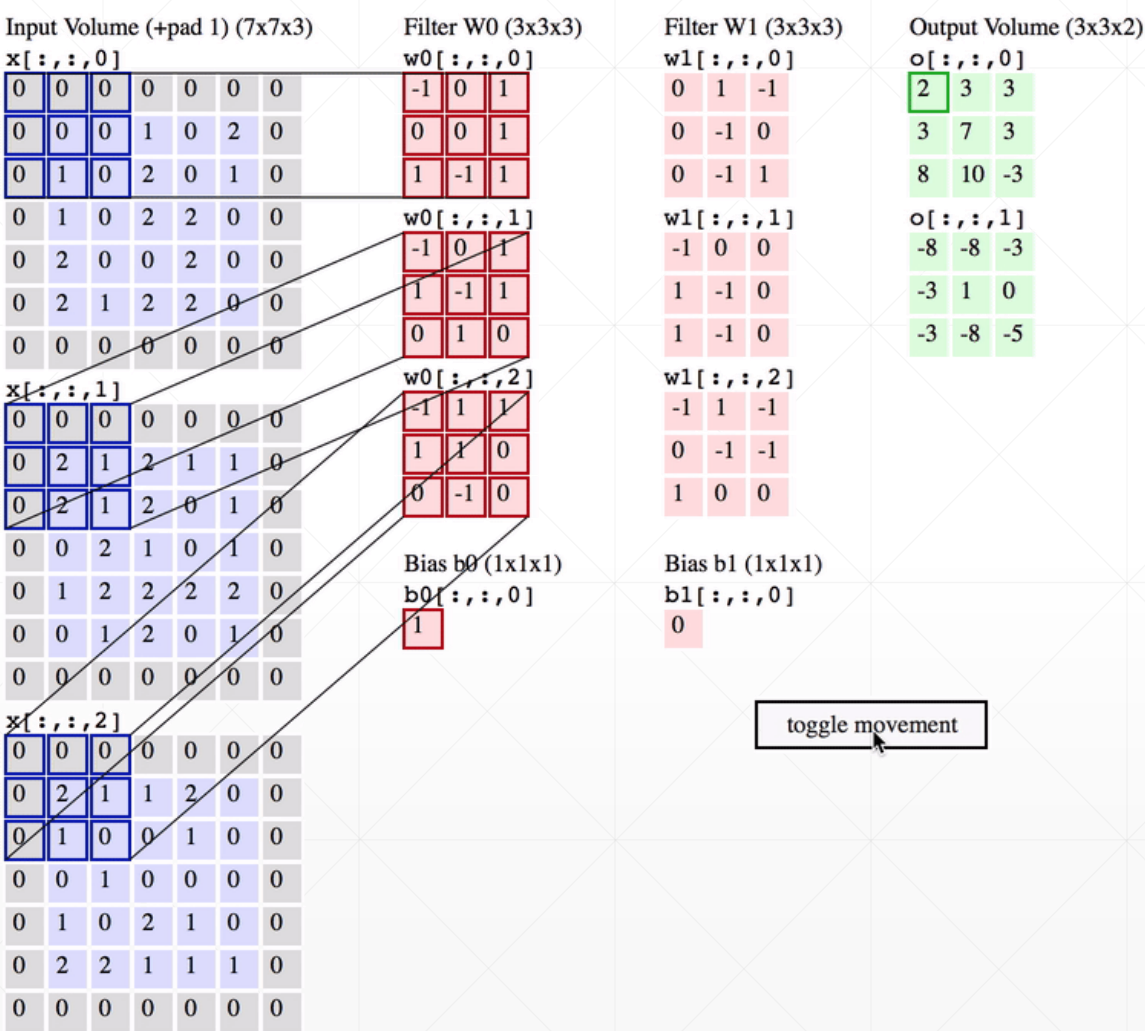


b_3



[1,30,30,4]

For instance



x: [b, 28, 28, 3]

one k: [3, 3, 3]

multi-k: [16, 3, 3, 3]

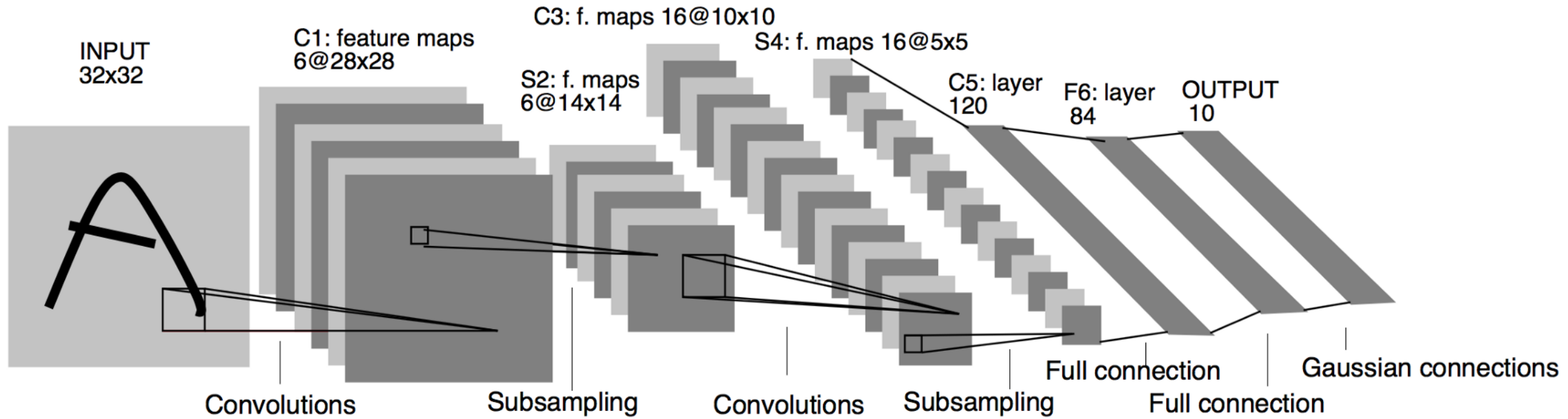
stride: 1

padding: [1,1,1,1]

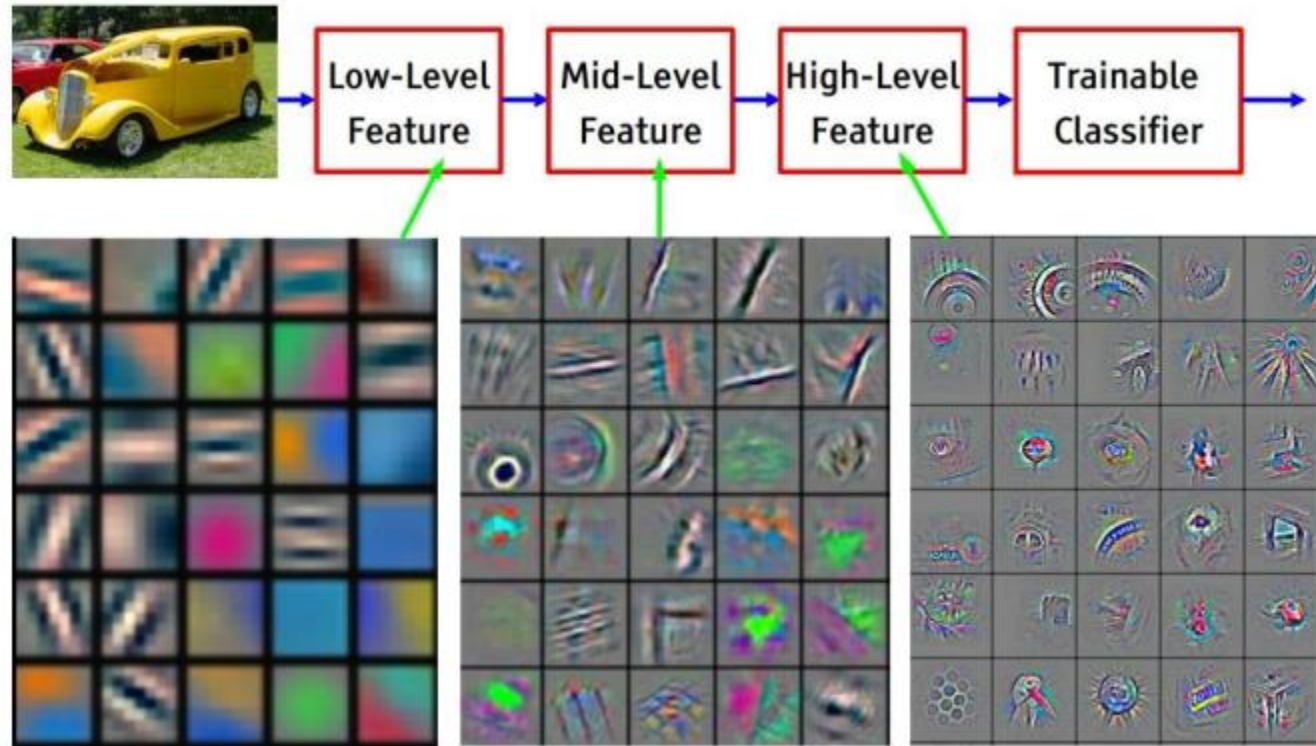
bias: [16]

out: [b, 28, 28, 16]

LeNet-5



Pyramid Architecture



Feature visualization of convolutional net trained on ImageNet from [Zeiler & Fergus 2013]

layers.Conv2D



```
In [1]: import tensorflow as tf
In [2]: from tensorflow.keras import layers

In [6]: layer=layers.Conv2D(4, kernel_size=5, strides=1, padding='valid')
In [8]: out=layer(x)
Out[9]: TensorShape([1, 28, 28, 4])

In [10]: layer=layers.Conv2D(4, kernel_size=5, strides=1, padding='same')
In [11]: out=layer(x)
Out[12]: TensorShape([1, 32, 32, 4])

In [13]: layer=layers.Conv2D(4, kernel_size=5, strides=2, padding='same')
In [14]: out=layer(x)
Out[15]: TensorShape([1, 16, 16, 4])

In [16]: layer.call(x).shape
Out[16]: TensorShape([1, 16, 16, 4])
```

kernel 个数 (不padding)

weight & bias



```
In [13]: layer=layers.Conv2D(4, kernel_size=5, strides=2, padding='same')
```

```
In [14]: out=layer(x)
```

```
Out[15]: TensorShape([1, 16, 16, 4])
```

```
In [17]: layer.kernel
```

```
<tf.Variable 'conv2d_3/kernel:0' shape=(5, 5, 3, 4) dtype=float32, numpy=
array([[[[-0.16160963,  0.04107726, -0.09828208, -0.00601757],
          [-0.02003701,  0.01415607, -0.07604317, -0.12557343],
          [-0.11157566,  0.1328298 ,  0.14624669, -0.04775226]], ...
```

```
In [18]: layer.bias
```

```
Out[18]: <tf.Variable 'conv2d_3/bias:0' shape=(4,) dtype=float32, numpy=array([0.,
0., 0., 0.], dtype=float32)>
```

nn.conv2d



```
In [21]: w=tf.random.normal([5,5,3,4])
In [22]: b=tf.zeros([4])
In [23]: x.shape
Out[23]: TensorShape([1, 32, 32, 3])

In [29]: out=tf.nn.conv2d(x, w, strides=1, padding='VALID')
Out[30]: TensorShape([1, 28, 28, 4])

In [31]: out = out + b
Out[32]: TensorShape([1, 28, 28, 4])

In [33]: out=tf.nn.conv2d(x,w,strides=2,padding='VALID')
Out[34]: TensorShape([1, 14, 14, 4])
```

One more thing

The Gradient

Gradient?

■ $\frac{\partial Loss}{\partial w}$

1x1	1x0	1x1	0	0
0x0	1x1	1x0	1	0
0x1	0x0	1x1	1	1
0	0	1	1	0
0	1	1	0	0

4		

For instance

x_{00}	x_{01}	x_{02}
x_{10}	x_{11}	x_{12}
x_{20}	x_{21}	x_{22}

w_{00}	w_{01}
w_{10}	w_{11}

O_{00}	O_{01}
O_{10}	O_{11}

0
1
0
0



$$O_{00} = x_{00} * w_{00} + x_{01} * w_{01} + x_{10} * w_{10} + x_{11} * w_{11} + b$$

$$O_{01} = x_{01} * w_{00} + x_{02} * w_{01} + x_{11} * w_{10} + x_{12} * w_{11} + b$$

$$O_{10} = x_{10} * w_{00} + x_{11} * w_{01} + x_{20} * w_{10} + x_{21} * w_{11} + b$$

$$O_{11} = x_{11} * w_{00} + x_{12} * w_{01} + x_{21} * w_{10} + x_{22} * w_{11} + b$$

$$\frac{\partial Loss}{\partial w_{00}} = \sum_{i \in \{00,01,10,11\}} \frac{\partial Loss}{\partial O_i} \frac{\partial O_i}{\partial w_{00}}$$

$$\begin{aligned} \frac{\partial O_{00}}{\partial w_{00}} &= \frac{\partial (x_{00} * w_{00} + x_{01} * w_{01} + x_{10} * w_{10} + x_{11} * w_{11} + b)}{\partial w_{00}} \\ &= x_{00} \end{aligned}$$

下一课时

池化与采样

Thank You.
