MAGNETIC RECONNECTION IN SPACE AND LABORATORY PLASMAS AND ITS IMPLICATION IN TOKAMAK PLASMA CONFINEMENT

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December 10, 2014

Abstract

Magnetic reconnection is the topological restructuring of magnetic field lines in high temperature plasmas. The aim of this paper will be to describe the fundamental physics of magnetic reconnection and discuss the various MHD models to describe magnetic reconnection. Magnetic reconnection as observed in both space plasmas and laboratory plasmas results in significant changes in kinetic and thermal properties of the plasma. This inherently deteriorates the ability to confine plasma in the laboratory. The second part of this paper will describe the fundamentals of sawtooth instabilities triggering magnetic reconnection in tokamak plasma devices. Due to the undesirable effects of magnetic reconnection in laboratory plasmas, several techniques have been developed to control sawtooth instabilities. The efficacy of these techniques to include current drive schemes and ion population control will be discussed.

1 Reconnection Defined

Reconnection is the rearranging of the magnetic topology where magnetic field lines are broken and then recombine and is shown in Figure 1. Priest,Yamada98,Yamada10 This is an important process to understand in astrophysics, laboratory plasma science, and others due to it's disruptive effects. The process of reconnection changes the macroscopic quantities of plasmas through: Priest

- conversion of magnetic energy into heat
- accelerate plasma by converting magnetic energy into kinetic energy
- create shockwaves, current filamentation, and turbulence
- affect fluxes of fast particles and heat due to changes in global magnetic field lines

The first two effects are especially important for stability of confined plasmas due to causing major and minor disruptions in tokomak discharges that will be discussed in this paper. $Y^{amada10}$

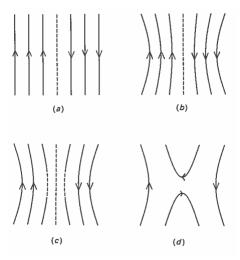


Figure 1: An intial perturbation generates magnetic pressure to counter. However, magnetic field diffusion occurs rapidly in locations of strong flux gradient. As magnetic field diffuses, perturbation is allowed to grow and alter topology. Hood

1.1 Reconnection in Space Plasmas

Magnetic reconnection is seen directly in many aspects of space plasmas. Solar flares and coronal mass ejections were one of the first events studied to understand magnetic reconnection. Yamada10 Coronal mass ejections and solar flares result form converting magnetic energy into heat and particle energy during a magnetic reconnection event. Priest Additionally, a small scale reconnection model is thought to be responsible for the higher density slow solar wind originating from the Sun's equatorial region. Priest Reconnection between solar wind magnetic field lines and the Earth's magnetoshpere field lines is also thought to be responsible for the penetration of solar particles to penetrate the magnetosphere (Figure 2). $^{Frey, Priest}$

Understanding reconnection in space plasma is vitally important to protecting space satellites, astronauts, and even terrestrial utilities from the damaging effects of highly energized charged particles from solar plasma.

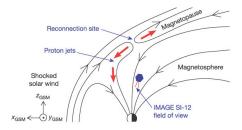


Figure 2: Reconnection at magnetopause Frey

1.2 Reconnection in Laboratory Plasmas

Reconnection is believed to be responsible for various anomalies in tokomak, reverse pinch, and spheromak devies. In tokomak devices, magnetic reconnection manifests in a periodic reorganization of core plasma density and temperature (Figure 3).

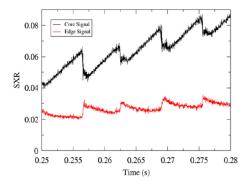


Figure 3: Soft X-ray emissions give core temperature indications. This shows the core plasma temperature periodically dropping associated with an increase in edge plasma temperature. Chapman11

In reverse pinch and spheromak device, magnetic reconnection plays a role in the magnetic relaxation. Magnetic relaxation is a self-organization of confined plasma that is thought to be a preferred state of minimal helicity. Garcia,Yamada10 Magnetic reconnection events are believed to be a driving factor in changes of helicity and therefore a driving factor for confined plasma self-organization. Garcia Understanding these phenomena is important and is a driving factor in the development of new confinement techniques in the field of plasma fusion. Champan11,Aymar,Wagner

1.3 Fundamental Physics of Reconnection

Davidson, Priest, and Garcia all present very good introductions to the relevant magnetohydrodynamics of magnetic reconnection, in particular Chapter

6 of Eric Priests textbook. For this paper we will focus on the derivation of magnetic diffusion and how this plays a role in magnetic reconnection.

Beginning with the differential forms of Ampere's Circuit Law and Gauss' Magnetic Law:

$$\nabla \times \vec{H} = \vec{J} + \frac{\partial \vec{D}}{\partial t} \text{ or } \nabla \times \vec{B} = \mu \vec{J} + \frac{1}{c^2} \frac{\partial \vec{E}}{\partial t}$$
$$\nabla \cdot \vec{B} = 0$$

And combining them with Ohm's Law:

$$\vec{J} = \sigma \left(\vec{E} + \vec{v} \times \vec{B} \right)$$

We arrive at the result,

$$\frac{\partial \vec{B}}{\partial t} = - \nabla \times \left(-\vec{v} \times \vec{B} + \frac{\vec{J}}{\sigma} \right)$$

or

$$\frac{\partial \vec{B}}{\partial t} = \bigtriangledown \times \left(\vec{v} \times \vec{B} \right) - \bigtriangledown \times \left(\eta \bigtriangledown \times \vec{B} \right) \text{ where } \eta \equiv \frac{1}{\mu \sigma}$$

To simplify further we can use $\nabla \times (\nabla \times \vec{a}) = \nabla (\nabla \cdot \vec{a}) - \nabla^2 \vec{a}$,

$$\frac{\partial \vec{B}}{\partial t} = \nabla \times \left(\vec{v} \times \vec{B} \right) - \eta \, \nabla^2 \, \vec{B}$$

We can introduce a new non-dimensional number called the magnetic Reynold's number, R_m

$$R_m = \frac{\left| \bigtriangledown \times \vec{v} \times \vec{B} \right|}{\left| \eta \bigtriangledown^2 \vec{B} \right|} \sim \frac{u_0 L}{\eta}$$

Typically velocity and length scales are much larger than η and this results in $R_m \gg 1$ and diffusivity can be neglected (this is considered idealized)^{Garcia};

$$\frac{\partial \vec{B}}{\partial t} = \nabla \times \left(\vec{v} \times \vec{B} \right)$$

In this case, the magnetic field lines are similar to elastic bands frozen in the vector field. Davidson, Garcia This means that any flux line through a closed loop will be conserved and the magnetic flux lines provide a restoring force to a disturbance. If, however, the gradient of the magnetic field is very large, diffusion can no longer be neglected.

Now we can revisit Figure 1 and discuss the evolution of this process further. In Figure 1a, normal magnetic flux lines exist in anti-parallel directions. In Figure 1b, a perturbation pushes outward (not shown) and the ideal magnetic flux lines respond with a restoring force. As the perturbation grows and the restoring force

grows, the magnetic flux lines become closer and closer. This increases the gradient of the magnetic field and diffusion sets in. In Figure 1d, magnetic flux lines diffuse and reconnect. In the Sun this perturbation is a manifestation of differential rotation rates that tend to twist the magnetic field lines. In tokomaks, this perturbation is caused from a kink in the magnetic field due to poloidal and toroidal magnetic interactions. Yamada10, Hastie, Champan11, Yun, Yamda94 This will be discussed in the next section.

2 Sawtooth Instabilities in Tokomak Devices

Tokomak plasmas are generally susceptible to two types of instabilities, microscopic and macroscopic. Microscopic instabilities generally dictate transport properties of a confined plasma, but in general do not cause significant disruption of confinement. Macroscopic instabilities however, can and often do result in total loss of plasma confinement. Sawtooth instabilities are unique in that they are macroscopic instabilities but do not result in a termination of discharge. They can however trigger other instabilities. In this section, we will discuss the characteristics of sawtooth instabilities in tokomak devices to include; cycle characteristics, energy transport, and problems associated with sawtooth instabilities. We will then discuss the current theories on causes of sawtooth instabilities and the methods of controlling them.

2.1 Sawtooth Characteristics

Sawtooth characteristics were discovered in 1974 and have now been verified on all tokomak devices. Hastie Sawtooth instabilities are periodic redistributions of core plasma and exist in three phases (Figure 4); Chapman 11

- an approximately linear increase in both plasma temperature and density
- an oscillatory precursor phase
- a final rapid drop in both temperature and plasma density.

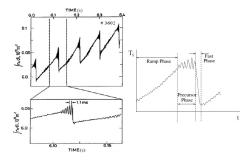


Figure 4: Sawtooth characteristic from JET showing all three phases Chapman11

When a sawtooth crash occurs, high energy electrons diffuse to cooler portions of the plasma resulting in a flattening T_e profile. This characteristic can be seen in both Figures 5 and 6.

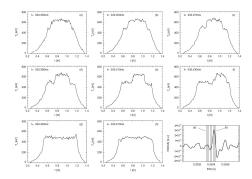


Figure 5: Electron temperature profile every $20\mu s$. In f, the temperature flattens out more on the interior where the higher magnetic field exists. The crash occurs between frames f and g. $^{Chapman 10}$

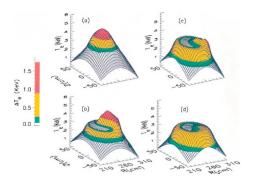


Figure 6: Two dimensional profile of electron temperature duing sawtooth crash. Similar flattening characteristics on the interior side can be seen. Yamada94

2.2 Tokamak Plasma Stability

Before we can discuss the theories for sawtooth instabilities, we need to qualitatively discuss confined plasma stability. To do this we will discuss the safety factor, $q = \frac{m}{n}$ where m is the poloidal number and n is the toroidal number. Essentially the safety factor is the ratio to the number of times a field line will go around toroidally for one poloidal circuit. O'Brien A more in depth review of MHD stability theory than is provided here will show that low rational numbers for q are least stable and tend to develop helical perturbations that can lead to kinks. O'Brien An interesting result of MHD stability analysis is that if an

m=n=1 kink instability exists(Figure 7), the central safety factor, q_0 , must be greater than one to diminish the perturbation. Hopcraft The large gradient of magnetic field can cause a transition from ideal to diffusion MHD where magnetic reconnection can occur. Priest This is where Kadomtsev comes in.

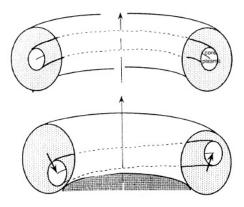


Figure 7: View of normal and m = n = 1 kink instability in a tokomak. Hastie

2.3 Sawtooth Theories

The initial theory for the cause of sawtooth instabilities was by Boris Kadomtsev who postulated that the cycle begins with an m=n=1 kink instability where the central saftey factor $q_0 < 1$. Yamada94, Hastie, Chapman11 Kadomtsev postulated that the kink instability would drive magnetic reconnection to restore a stable reconfiguration causing a transient the re-established a $q_0 > 1$ condition in the plasma. This is postulated to occur due to the kink mode createes a crowding of flux surfaces on one side triggering separation and the formation of a magnetic island. As the magnetic island grows, surfaces with equal helical flux will touch and reconnect (See Figure 8). Chapman11 Ohmic heating was then thought to be responsible for driving T_e up and forcing $q_0 < 0$ to restart the cycle. Hastie Kadomtsev's model has been the standard driving much of the research in sawtooth oscillations.

Initial experiments indeed supported the Kadomtsev model Sykes , but as devices got larger and data collection became more accurate, discrepancies were noted. One discrepancy is that expected central safety factors, q_0 , should be restored to a value greater than one after a sawtooth crash. However increased precision yield experimental measurements showing q_0 never reaches 1.0 post crash (See Figures 9 and 10). This is indicative that full Kadomtsev reconnection is not occurring and has led to a theory that Kadomtsev reconnection is interrupted due to rapid heat diffusion through the reconnection region. Yamada10

Additional data has been collected that deviates from the Kadomtsev model.

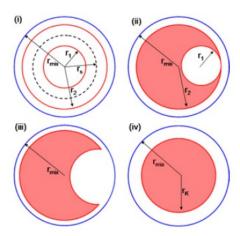


Figure 8: (i)Magnetic flux surfaces prior to reconnection (ii)Reconnection of flux surfaces (iii)Deformation of magnetic island (iv)Complete reconnection. Chapman11

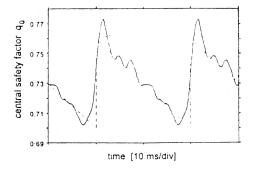


Figure 9: q_0 for TEXTOR. Hastie

Reconnection times are significantly faster than those predicted by the Kadomtsev model, since the Kadomtsev model incorporates the Sweet-Parker model for reconnection. Reconnective theory predicts sawtooth crash times of $\tau_K \approx 340 \mu s$ while actual sawtooth crashes occur on timescales $\leq 20 \mu s.^{Yamada94,Chapman10,Chapman11}$ As Chapman explains, this is not surprising since the Sweet-Parker model of reconnection is only applicable to collisional plasmas, while tokamak plasmas have a collisionless behavior.

These contradictions have led to many additional theories on the cause of sawtooth crashes and the current widely accepted theory is a modified Kadomtsev model with interrupted reconnection. Chapman 11 The partial reconnection model is initialized with a kink instability and begins reconnection per the Kadomtsev model. However, full reconnection is interrupted due to the faster heat diffusion

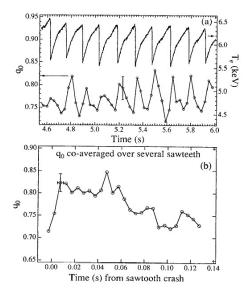


Figure 10: q_0 measurements on the TFTR. $Y^{amada94}$

than magnetic diffusion. This heat conduction minimizes the pressure gradient driving the kink mode. Yamada10 This causes the magnetic island to reach a critical width and creates two regions undergoing different relaxation processes, the core and the magnetic island. This creates a complex diffusion event of two current sheets during a subsequent sawtooth ramp. Chapman11 Even this theory isn't complete because it relies still on having a kink instability precursor. There is evidence of precursor-less sawteeth and could imply that the kink mode instability is a consequence of some other factor rather than the cause of the collapse. Hastie

2.4 Controlling Sawtooth Oscillations

There are two main techniques for controlling sawtooth oscillations; stabilizing the oscillations to lengthen the time between crashes and destabilizing the oscillations to minimize the amplitude of crashes. Chapman11 Stabilization of sawtooth oscillations will lengthen the period between sawtooth crashes and recent studies have shown that long period sawtooth oscillations can go on to cause other instabilities such as neo-classical tearing modes(NTMs) and edge localized modes(ELMs). Chapman11 Additionally, helium ash from fusion reactions is thought to further destabilize so most efforts are aimed at destabilizing the sawtooth oscillations. Chapmain07 Techniques to destabilize sawtooth oscillations aim to shorten the period by creating conditions conducing to sawtooth crashes. This minimizes the amplitude and shortens the period to reduce the potential for causing NTMs and ELMs. An added benefit is that small amplitude sawtooth oscillations can aid in preventing an accumulation of helium ash in tokomak

fusion devices. Chapman11

3 References

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