

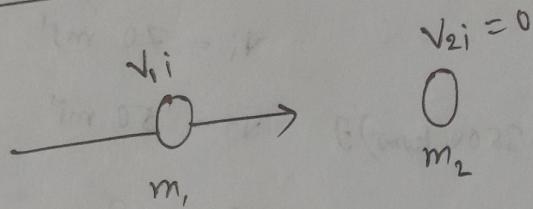
Collision

elastic collision

kinetic energy

$$k_i = k_f$$

Before collision



after, v_{1f} v_{2f}

$$m_1 v_{1i} = m_1 v_{1f} + m_2 v_{2f}$$

$$m_1 (v_{1i} - v_{1f}) = m_2 v_{2f} \quad \text{--- (i)}$$

Elastic collision:

$$\frac{1}{2} m_1 v_{1i}^2 = \frac{1}{2} m_1 v_{1f}^2 + \frac{1}{2} m_2 v_{2f}^2$$

$$m_1 (v_{1i}^2 - v_{1f}^2) = m_2 v_{2f}^2 \quad \text{--- (ii)}$$

(ii) \div (i),

(A) $v_{1f} = \frac{m_1 - m_2}{m_1 + m_2} v_{ii}$

(B) $v_{2f} = \frac{2m_1}{m_1 + m_2} v_{ii}$

Case-i :

$$m_1 = m_2$$

$$v_{1f} = 0$$

$$v_{2f} = v_{ii}$$

case-ii:

$$m_1 \ll m_2$$

$$v_{1f} \approx -v_{ii}$$

$$v_{2f} \approx 0$$

case-iii
 $m_1 \gg m_2$

$$v_{1f} \approx v_{ii}$$

$$v_{2f} \approx 2v_{ii}$$

Linear Motion

Position, x

Displacement, Δx

$$\Delta x = x_2 - x_1$$

Average Velocity, v_{avg}

$$v_{avg} = \frac{\Delta x}{\Delta t} = ms^{-1}$$

$$v = \lim_{\Delta t \rightarrow 0} \frac{\Delta x}{\Delta t} = \frac{dx}{dt}$$

Average Acceleration,

$$a_{avg} =$$

Rotational Motion

Angular position, $\theta \rightarrow rad$

Angular displacement, $\Delta \theta = \theta_2 - \theta_1$

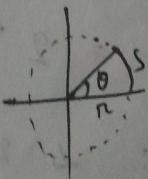
Average Angular velocity, ω_{avg}

$$\omega_{avg} = \frac{\Delta \theta}{\Delta t}$$

$$\omega = \lim_{\Delta t \rightarrow 0} \frac{\Delta \theta}{\Delta t} = \frac{d\theta}{dt}$$

Average angular acceleration,

$$a_{avg}$$



$$s = r\theta$$

$$x(t) = t^2 + 2t + 1$$

$$t = 2 \text{ sec}$$

$$v = \frac{dx}{dt} = 2t + 2$$

$$v = 2 \cdot 2 + 2$$

$$= 6$$

$$\theta(t) = t^2 + 2t + 1$$

$$\omega = \frac{d\theta}{dt} = 2t + 2$$

$$t = 2 \text{ sec}$$

$$\omega = 6 \text{ rad/sec}$$

$$a_{avg} = \frac{\Delta v}{\Delta t} = \frac{12}{2} = 6 \text{ m/s}^2$$

$$a = \frac{dv}{dt} = \frac{d^2x}{dt^2} = \ddot{x} \text{ m/s}^2$$

$$\Delta \omega = \omega_2 - \omega_1$$

$$\alpha_{avg} = \frac{\Delta \omega}{\Delta t} \quad \left| \begin{array}{l} \omega = \frac{d\theta}{dt} = \frac{d^2\theta}{dt^2} = \ddot{\theta} \text{ rad/sec}^2 \\ \text{initial position} \\ \text{final position} \end{array} \right.$$

$$\textcircled{*} \quad \theta(t) = t^2 + 2t + 1$$

$$\omega, d = 2 \text{ sec}$$

$$\omega = ?$$

$$\omega = \frac{d\theta}{dt} = 2t + 2$$

$$\alpha = \frac{d\omega}{dt} = 2 \rightarrow \text{time independent.}$$

$$t = 2 \text{ sec}; \quad \omega = 2 \text{ rad/sec}$$

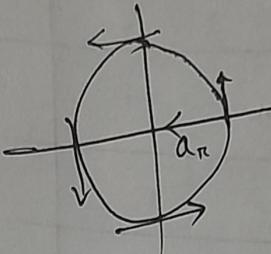
$$\textcircled{*} \quad s = \theta R \rightarrow \text{constant}$$

$$\frac{ds}{dt} = R \frac{d\theta}{dt}$$

$$v = R\omega$$

$$\frac{dv}{dt} = R \frac{d\omega}{dt}$$

$$a = R\alpha$$



$$a_n = \frac{v^2}{R}$$

$$a_n = \tilde{\omega}^2 R$$

$$\begin{aligned} s &= R\theta \\ v &= \omega R \\ a_s &= \omega^2 R \end{aligned}$$

if, $\omega = \text{constant}$

$$a_n = \tilde{\omega}^2 R$$

$$a_s = \omega R = R \cdot \frac{d\omega}{dt} = 0$$

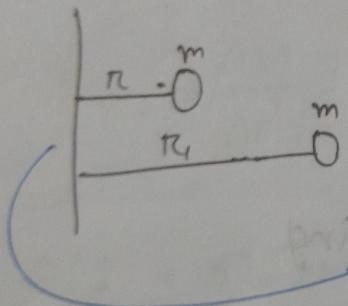
if, $\omega = \text{increasing or decreasing}$

$$a_n = \tilde{\omega}^2 R$$

$$a_s = \omega R$$

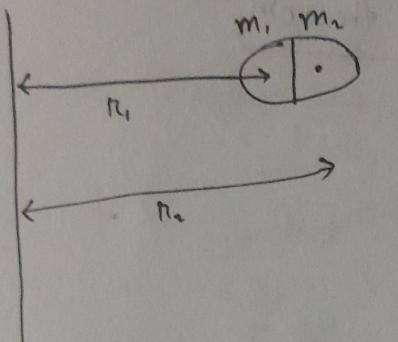
L-13 / 16. 11. 2022/

<u>Linear</u>	<u>Rotational</u>
α	θ
Δx	$\Delta \theta$
v	ω
a	α
F	τ
p	L
m	$I \rightarrow \text{Rotational mass} / \text{moment of Inertia}$



$$I = mr^2 \rightarrow \text{kgm}^2$$

$$I_{\text{total}} > I$$



$$K = \frac{1}{2} m_1 v_1^2 + \frac{1}{2} m_2 v_2^2$$

$$= \sum_{i=1}^n \frac{1}{2} m_i v_i^2$$

$$= \sum \frac{1}{2} m_i \tilde{v}_i^2$$

$$= \sum \frac{1}{2} (m_i r_i^2) \omega^2$$

$$K = \sum \frac{1}{2} I \omega^2$$



$$\omega = 2 \text{ rad/sec}$$

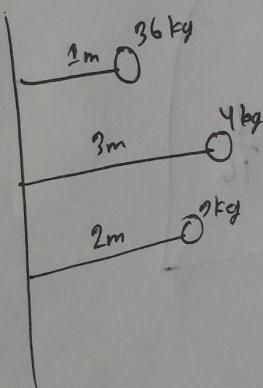
$$K = 10 \text{ J}$$

$$I = ?$$

$$I = \frac{2K}{\omega}$$

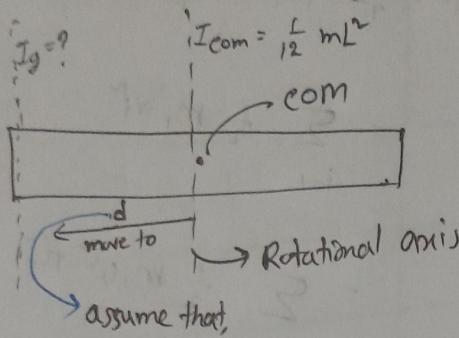
~~$$I = \frac{1}{2} I_{\text{tot}}$$~~

$$\begin{aligned} \omega &= \frac{d\theta}{dt} \\ v &= \omega r \end{aligned}$$



$$I_1 = I_2 = I_3 = 36$$

Parallel axis theorem



assume that,

$$d = \frac{L}{2}$$

$$\therefore I_g = I_{\text{com}} + m d^2$$

$$= \frac{1}{2} m L^2 + m \frac{L^2}{4}$$

$$= \frac{m L^2 + 3 m L^2}{12}$$

$$= \frac{4 m L^2}{12}$$

$$\frac{m L^2}{3}$$

$m = 1 \text{ kg}$
$L = 2 \text{ m}$
$I_g = ?$

if, $d = \frac{wL}{4}$

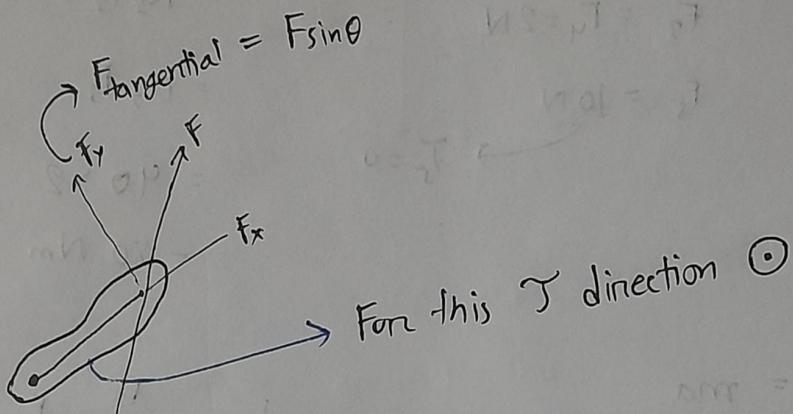
then, $I_g = \frac{1}{12} m L^2 + m \frac{L^2}{16}$

Midterm

L-15/23.11.2022/

$$k = \frac{I}{m} \cdot \omega$$

$\tau \rightarrow$ Torque \rightarrow rotational force.



$$\vec{\tau} = \tau \vec{F}_{\text{tan}} = (\tau) |\vec{F}| \sin \theta$$

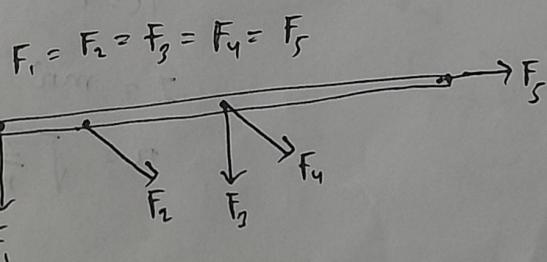
$$= \vec{r} \times \vec{F}$$

① $F \neq 0$

i) $\tau = 0, \tau = 0$

ii) $\tau = 0, \theta = 0$

$\vec{\tau} = \vec{r} \times \vec{F}$



$\tau_3 > \tau_4 > \tau_2 > \tau_1 = \tau_5$

If,

$$F_1 = 3 \text{ N} \quad \rightarrow \quad T_1 = 0$$

$$F_2 = 3 \text{ N}$$

$$T_3 = R_3 \times F_3$$

$$F_3 = F_4 = 2 \text{ N}$$

$$= R_3 F_3 \sin 90^\circ$$

$$F_5 = 10 \text{ N}$$

$$= R_3 F_3$$

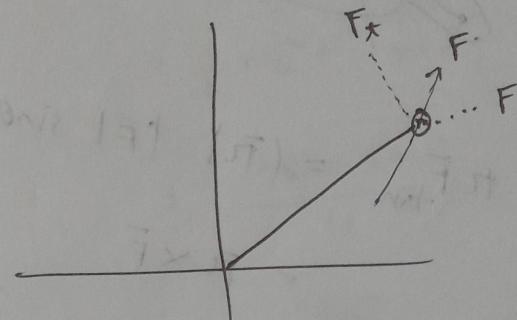
$$\rightarrow T_5 = 0$$

$$= 40 \times 2$$

$$= 80 \text{ Nm}$$

$$F_x = ma$$

$$T = I\alpha$$



$$F_x = m a_x$$

$$\textcircled{*} \quad T = 20 \text{ Nm}$$

$$T = R F_x$$

$$\alpha = 2 \text{ rad/sec}^2$$

$$= R m \alpha R$$

$$\therefore I = \frac{T}{\alpha} = \frac{20}{2} = 10 \text{ kgm}^2$$

$$= m R^2 \alpha$$

$$T = I \alpha$$

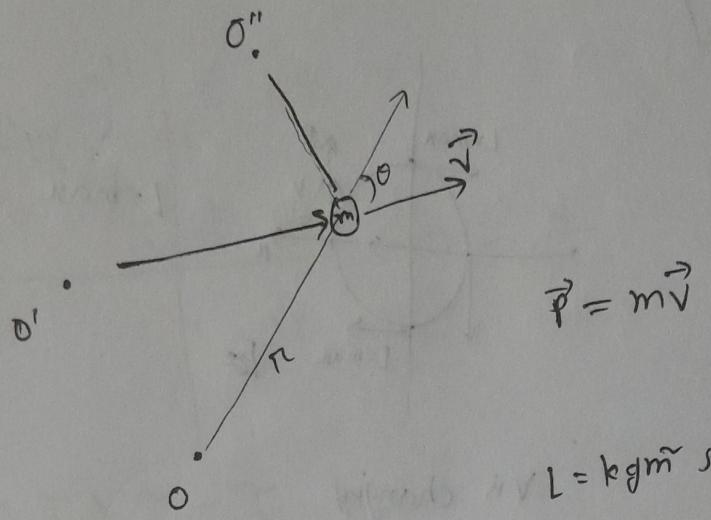
$$\textcircled{*} \quad m = 500 \text{ gm}$$

$$R = ?$$

$$I = m R^2$$

$$R^2 = \sqrt{\frac{I}{m}}$$

$L \rightarrow$ Angular momentum



$$\vec{\gamma} = \vec{r} \times \vec{F}$$

$$\vec{L} = \vec{r} \times \vec{p}$$

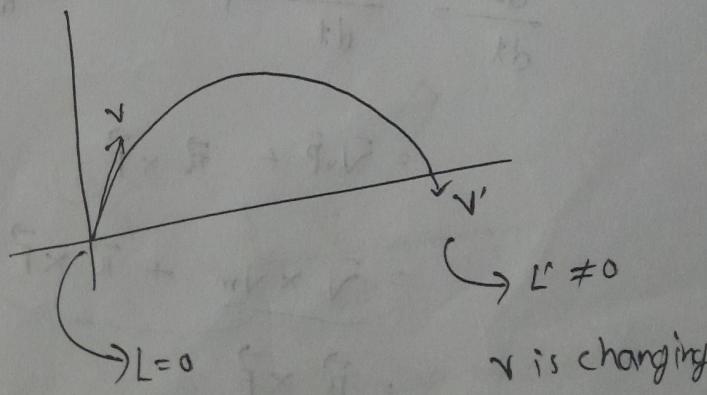
$$\vec{L} = \vec{r} \times \vec{p} = 0$$

$$L'' = \vec{r} \times \vec{p} = m a r$$

$$\textcircled{i} L=0, r=0$$

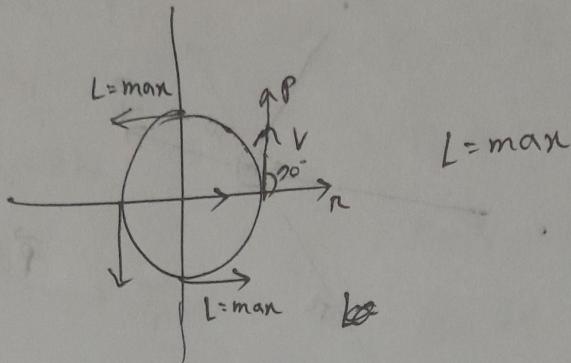
$$\textcircled{ii} L=0, \theta=0$$

~~(*)~~
case-1/



L is also changing

case-2/



v is changing

but, L is ~~no~~ constant.



$$\left. \begin{array}{l} F = ma \\ \tau = I\alpha \end{array} \right| \quad \begin{array}{l} \vec{F}_T = \frac{d\vec{p}}{dt} \\ \tau = \frac{d\vec{L}}{dt} \end{array}$$

$$\vec{L} = \vec{r} \times \vec{p}$$

$$\frac{d\vec{L}}{dt} = \frac{d\vec{r}}{dt} \times \vec{p} + \vec{r} \times \frac{d\vec{p}}{dt}$$

$$= \vec{v} \times \vec{p} + \vec{r} \times \vec{F}$$

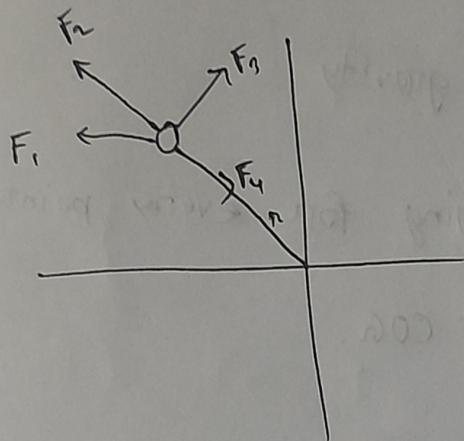
$$= \vec{v} \times \vec{v}_m + \vec{r} \times \vec{F}$$

$$= \vec{r} \times \vec{F}$$

$$= \tau$$

$$\therefore \tau = \frac{d\vec{L}}{dt}$$

(*)



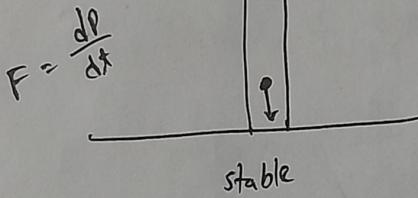
$$\gamma = \frac{dL}{dx}$$

$$T_3 > T_1 > T_2 = T_4$$

$$L_3 > L_1 > L_2 = L_4$$

(*)

i)



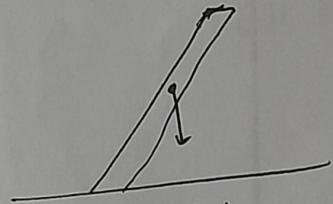
$$F = \frac{dp}{dt}$$

stable

$$\gamma = 0$$

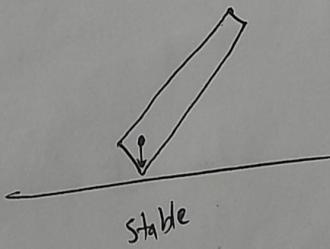
$L \rightarrow \text{constant}$

ii)



unstable

iii)



stable

(*) if the net torque is zero the angular momentum is constant.

→ conservation of Angular momentum.

- ④ COG \rightarrow center of gravity
- ⑤ If g is not changing for every point of an object then $\text{COM} = \text{COG}$.

$F = F < T < P$

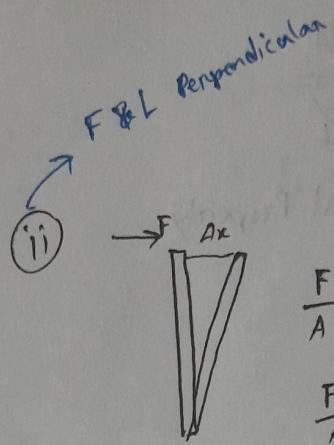
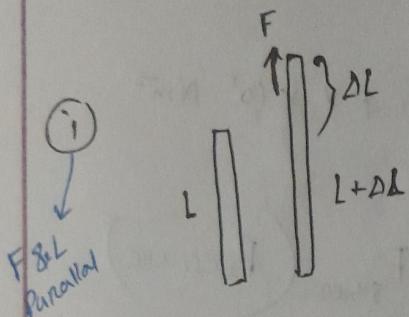
$w = w < d < d$



Centroid is arithmetic average of areas of support the with 1/3 of maximum value of the minimum

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Elasticity



$$\frac{F}{A} \propto \frac{\Delta x}{L}$$

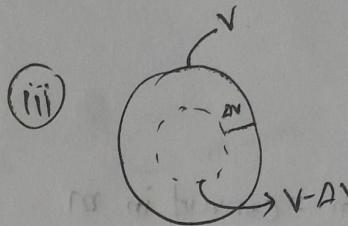
S. Modulus

$$\frac{F}{A} = G = \frac{\Delta x}{L}$$

$$\frac{F}{A} \propto \frac{\Delta L}{L}$$

Elastic Modulus

$$\frac{F}{A} = E \frac{\Delta L}{L}$$



$$\frac{F}{A} \propto \frac{\Delta V}{V}$$

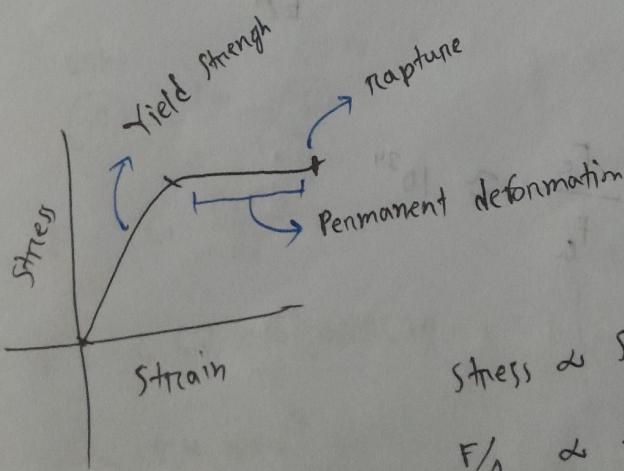
$$\frac{F}{A} = B = \frac{\Delta V}{V}$$

Bulk Modulus

$$\text{Stress : } \frac{F}{A} = \text{N m}^{-2}$$

$$\text{Strain : } \frac{\Delta L}{L} \text{ (Unitless)}$$

Identify which formula will apply.



Stress \propto Strain } within Elastic Limit
 $F/A \propto \frac{\Delta L}{L}$ only

$$E = \frac{F/A}{\Delta L}$$

Material Property

$$E_{\text{Steel}} = 2.8 \times 10^8 \text{ Nm}^{-2}$$

$$E_{\text{Silver}} = 1.7 \times 10^8 \text{ Nm}^{-2}$$

$$E_{\text{Steel}} > E_{\text{Silver}} \quad (\text{Pressure})$$



$$L = 10 \text{ m}$$

$$F = 2 \text{ N}$$

$$r = 0.5 \text{ cm} = \text{convert in m}$$

$$E = 2.8 \times 10^8 \text{ Nm}^{-2}$$

$$\text{Stress} = ?$$

$$\text{Strain} = ?$$

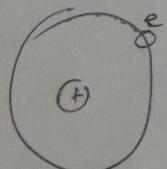
$$\Delta L = ?$$

$$\text{Stress} = \frac{F}{A} = \frac{2}{\pi r^2}$$

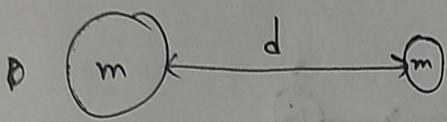
$$\text{Strain} = \frac{F}{EA}$$

$$E = \frac{F/A}{\Delta L/L}$$

$$\Delta L = \frac{FL}{EA}$$



$$\frac{F_e}{F_a} \approx 10^{34}$$



$\oplus \text{---} \ominus$

$$F_c = k \frac{q_1 q_2}{d^2}$$

$F \propto m_1 m_2$

$$F \propto \frac{1}{d^2}$$

$$F \propto \frac{m_1 m_2}{d^2}$$

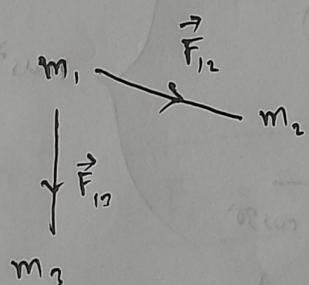
$$F = G \frac{m_1 m_2}{d^2}$$

[Limitation: only applicable with two objects]

Vector Form:

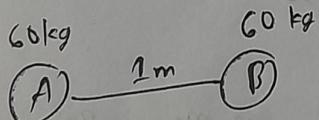
$$\vec{F}_{12} = G \frac{m_1 m_2}{d^2} \vec{R}_{12} \quad \vec{R}_{12} \text{ from } m_1 \text{ to } m_2$$

\otimes



$$\vec{F}_{\text{net}} = \vec{F}_{12} + \vec{F}_{23}$$

\otimes



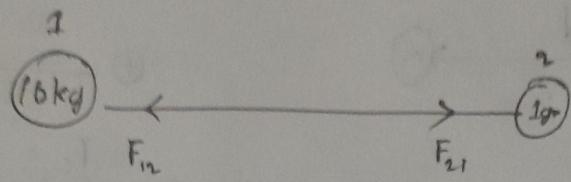
$$F = G \frac{m_1 m_2}{d^2}$$

$$G = 6.67 \times 10^{-11} \text{ Nm}^2/\text{kg}^2$$

$$F = 6.67 \times 10^{-11} \times 3600$$

$$= 2.4 \times 10^{-7} \text{ N}$$

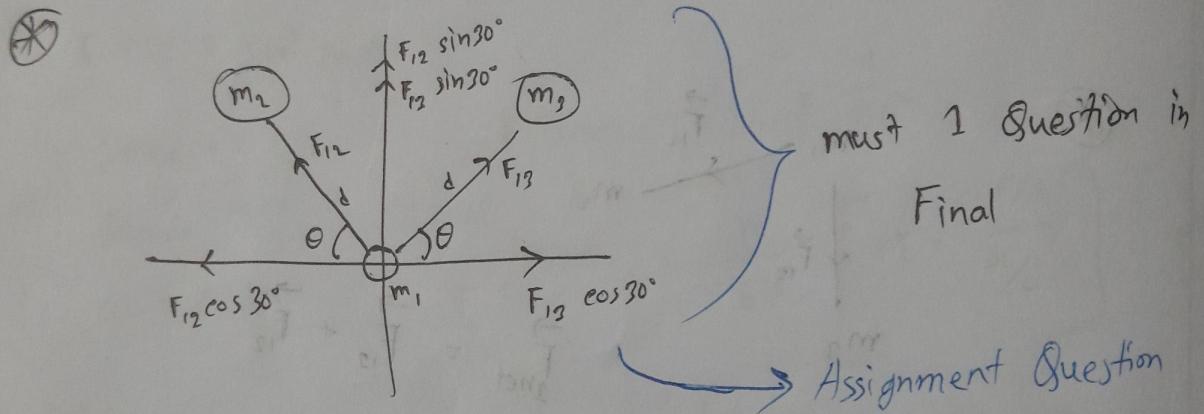
$$= 0.24 \times 10^{-6} \text{ N} = 0.24 \mu\text{N}$$



$$F_{12} = G \frac{m_1 m_2}{d^2} \quad F_{21} = G \frac{m_1 m_2}{d^2}$$

$F_{12} = F_{21}$

⊗ World moves towards me $\approx 10^{24} \text{ m s}^{-2}$



$$F_{1\text{net}} = F_{12} \sin 30^\circ + F_{13} \sin 30^\circ$$

$$= G \frac{m_1 m_2}{d^2} \times \sin 30^\circ + G \frac{m_1 m_3}{d^2} \sin 30^\circ$$

$$F_{1x} = F_{13} \cos 30^\circ - F_{12} \cos 30^\circ = 10 \text{ N}$$

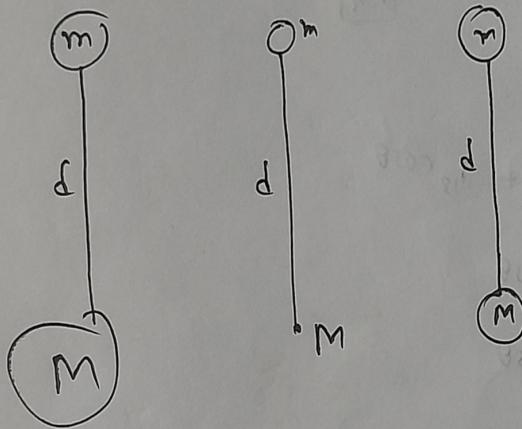
$$F_{1y} = F_{13} \sin 30^\circ + F_{12} \sin 30^\circ = 12 \text{ N}$$

$$\vec{F} = F_{ix} \hat{i} + F_{iy} \hat{j}$$

$$= 10N \hat{i} + 12N \hat{j}$$

$$|\vec{F}| = \sqrt{10^2 + 12^2} = \dots N$$

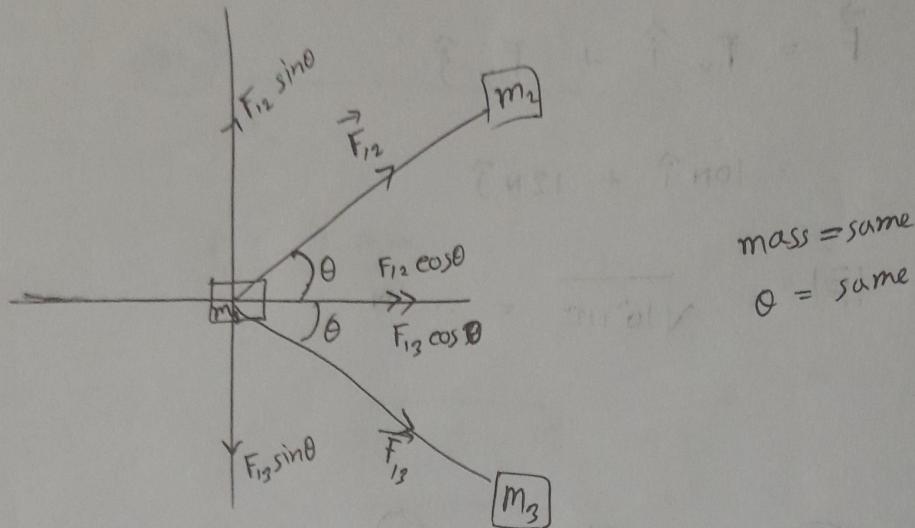
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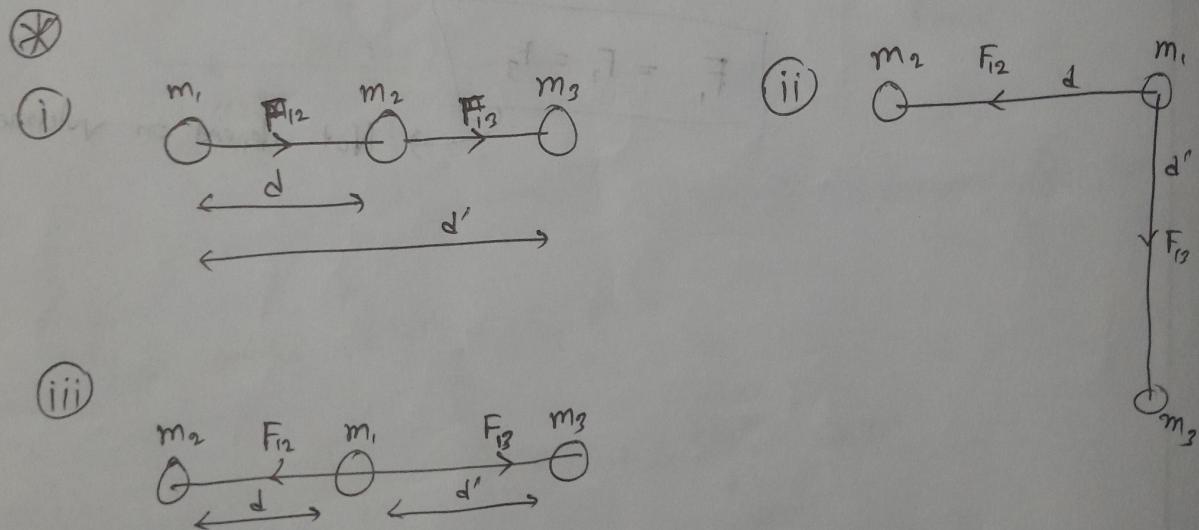
$$F_1 = F_2 = F_3$$

Not depend on volume

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$$\begin{aligned}
 F_{1\text{net}} &= F_{12} \cos \theta + F_{13} \cos \theta \\
 &= 2 F_{12} \cos \theta \\
 &= 2 F_{13} \cos \theta
 \end{aligned}$$

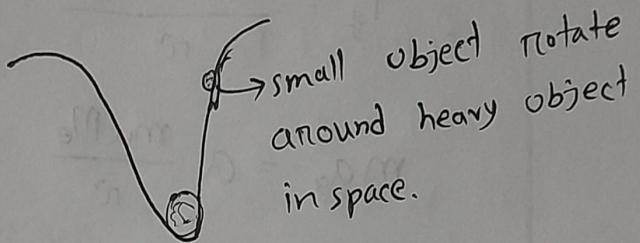
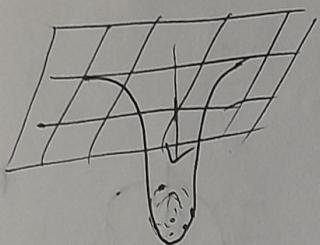


$$F_{1\text{net}} \quad 1 > 2 > 3$$

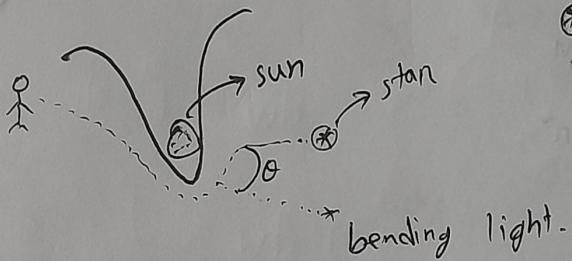
Q in which arrangement m_1 will get maximum gravitational force?

⊗ Space and time is co-related.

⊗ Heavy object in space distorted space more.



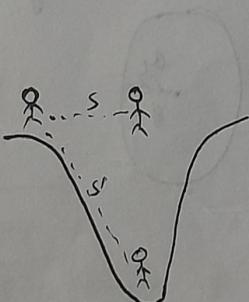
⊗



⊗ experiment only applicable
in solar eclipses

Heavy object makes time and space more distorted.

⊗



$$s = \sqrt{t}$$

$$v = 3 \times 10^8 \text{ m/s}$$

$$t = \frac{s}{v}$$

$$s' = \sqrt{t'}$$

$$t' = \frac{s'}{v}$$

∴ distortion & time



$$F = mg$$

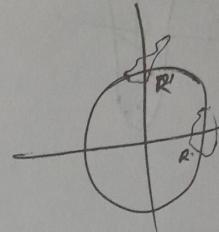
$$g = \alpha g$$

$$= m \alpha g$$

$$F_g = \frac{G M_{\text{Earth}} M}{r^2}$$

$$m \alpha g = G \frac{m M_e}{r^2}$$

$$\alpha g = \frac{G M}{r^2}$$



$\therefore \alpha g$ depends on M and r^2

when, R is bigger

g is smaller.

$$g \approx M$$

$$g \approx r^{-2}$$

④ To calculate original weight.

$$mg = \cancel{m \alpha g} - \frac{mv^2}{r}$$

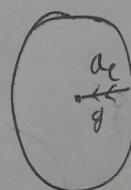
$$\cancel{= m \alpha g}$$

$$= m \alpha g - m \omega^2 r$$

$$g = \alpha g - \omega^2 r$$

$$\alpha_c = 0.3 \text{ m/s}^2$$

$$g = 9.8 \text{ m/s}^2$$



$$\alpha_c = \frac{v^2}{r}$$

$$F = ma$$

$$V = \omega r$$

Q

$$\pi = 5.98 \times 10^6 \text{ m}$$

R
earth
 M

$$g = \frac{GM}{r^2}$$

$$g_{\text{near}} = \frac{GM}{r^2}$$

$$g_{\text{near}} = \frac{GM}{(R+h)^2}$$

we can't use 1.8 m like that,
so, we have use another method

$$d_g = -14.5 \text{ m/s}^2$$

$$\frac{dg}{r} = -2 \frac{GM}{r^3}$$

$$d_g = -2 \frac{GM}{r^3} dr$$

$$d_g = -2 \frac{GM}{r^3} dr$$

$$= -4.37 \times 10^{-6} \text{ m/s}^2$$

$$-d_g = -14.5 \text{ m/s}^2$$

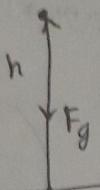
$$g = \frac{GM}{R'^2}$$

R' = digging height

R = earth surface length

m = mass

(X)



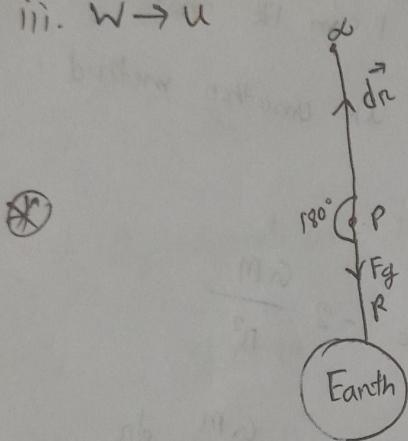
$$W_g = -mgh$$

$$\Delta u = -W \\ = -(-mgh) \\ = mgh$$

i. Reference Point

ii. Work done

iii. $W \rightarrow u$



$$U_f - U_i = mg^0$$

$$U_f = mgh$$

$$dw = \vec{F} \cdot d\vec{r}$$

$$F_g = \frac{GM_m}{r^2}$$

$$\int dw = \int_R^\alpha \vec{F} \cdot d\vec{r}$$

$$= - \int_R^\alpha F dr$$

$$= - \int_R^\alpha \frac{GM_m}{r^2} dr$$

$$= - GM_m \int_R^\alpha r^{-2} dr$$

$$= - GM_m \left[-\frac{1}{r} \right]_R^\alpha$$

$$= - GM_m \left[0 + \frac{1}{R} \right]$$

$$W = -GMm \frac{1}{R}$$

$$= -\frac{GMm}{R}$$



$$\Delta u = -W$$

$$U_{\infty} - U_i = -\frac{GMm}{R}$$

0, in infinity

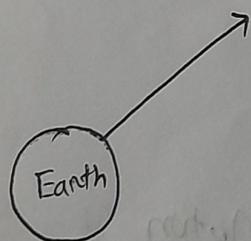
$$U_p = -\frac{GMm}{R}$$

work done positive. So,
Potential energy will decrease
and become negative.

$$U = -\frac{GMm}{R}$$

Assignment Question

Escape Speed:



$$-\frac{GMm}{R} + \frac{1}{2}mv^2 = 0$$

$$\frac{1}{2}mv^2 = \frac{GMm}{R}$$

$$v_{es} = \sqrt{\frac{2GM}{R}}$$

Escape Speed

$$v_{es} = 11.2 \text{ km/s}$$

$$v_{es} = 2.38 \text{ km/s}$$

$$v_{es} = 618 \text{ km/s}$$

$$v_{es} = 2 \times 10^5 \text{ km/s}$$

④ Simple Harmonic Motion (SHM)

$$F \propto -x$$

$$F = -kx$$

Spring Constant $\Rightarrow \text{Nm}^{-1}$

⊗ Hook's Law only works within Elastic Limit.



$$F = -kx$$

$$ma = -kx$$

$$ma + kx = 0$$

$$a + \frac{k}{m}x = 0$$

$$\omega = \sqrt{\frac{k}{m}}$$

Angular Frequency

$$a + \tilde{\omega}^2 x = 0$$

$$a(t) = -\tilde{\omega}^2 x$$

$$a \propto -x$$

SHM: Simple Harmonic Motion

$$\frac{d^2x}{dt^2} + \omega^2 x = 0$$

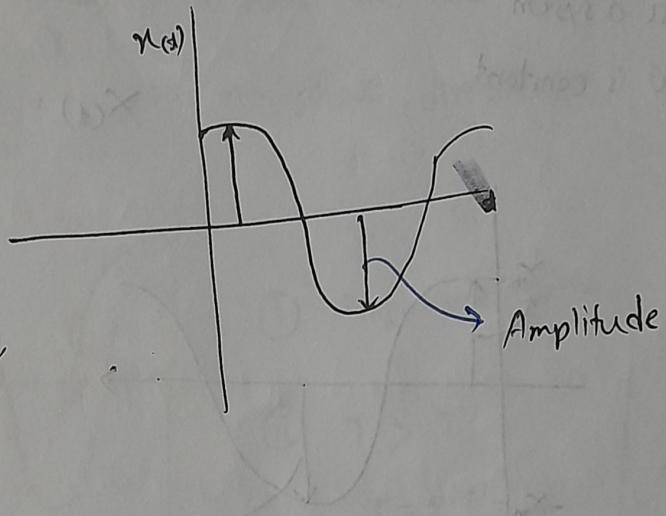
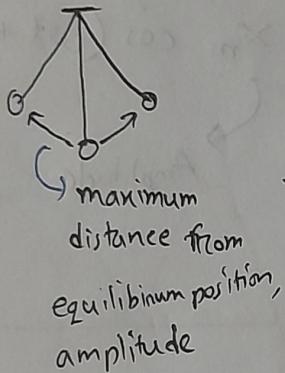
$$\Rightarrow x(t) = x_m \cos(\omega t + \theta)$$

Amplitude

Angular Frequency
Phase angle

$$v = \frac{dx}{dt}$$

$$a = \frac{d^2x}{dt^2}$$



T = time Period

$$T \text{ sec} \dots \text{ circle} \quad \frac{1}{T}$$

frequency

$$f = \frac{1}{T} \text{ sec}^{-1}/\text{Hz}$$

$$T \dots 2\pi$$

$$1 \dots \frac{2\pi}{T} = \omega$$

Angular frequency

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SHM \rightarrow Angular frequency

$$a_{(g)} = -\omega^2 x(t)$$

$\omega = \sqrt{\frac{k}{m}}$ \rightarrow Spring Constant
mass

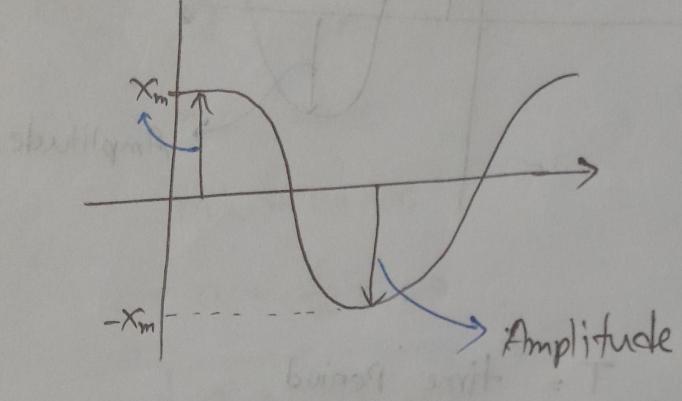
for a system

ω is constant

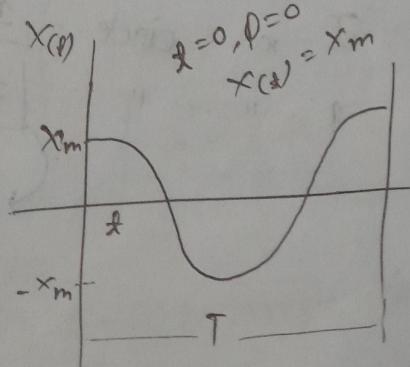
$$\text{Frequency} \\ \omega = \frac{2\pi}{T} \\ = \text{rad/sec}$$

$$x(t) = x_m \cos(\omega t + \phi)$$

Amplitude Phase angle



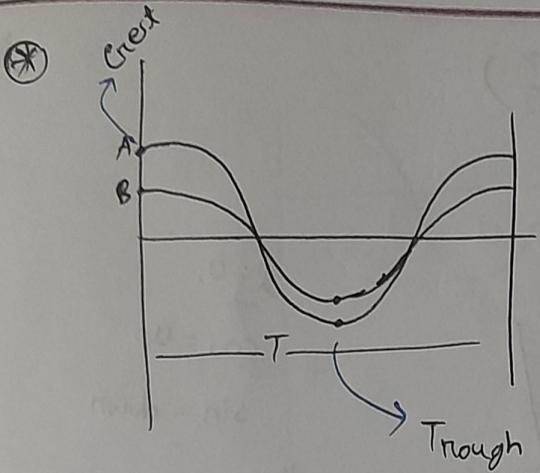
$$t=0, \phi=0 \\ x(t)=x_m$$



1 circle

$$\Rightarrow \text{Only frequency} = f = \frac{1}{T} \\ = \text{Hz}$$

$$\omega = \frac{2\pi}{T}$$

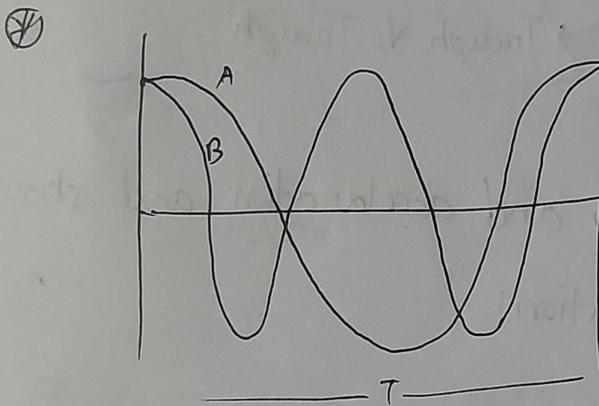


i) Amplitude (Difference)

ii) T, f, ω (same)

in x-axis they are at the same point.

So, no phase difference.



i) Amplitude same

ii) $T > T'$

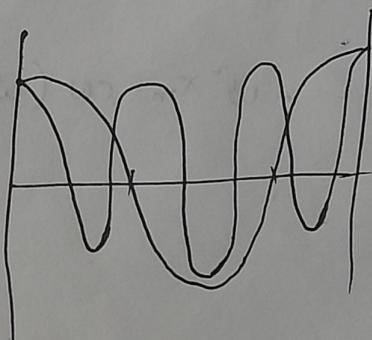
$$T = 2T'$$

$$\begin{array}{l} T = A \\ T' = B \end{array}$$

iii) $f_B > f_A$

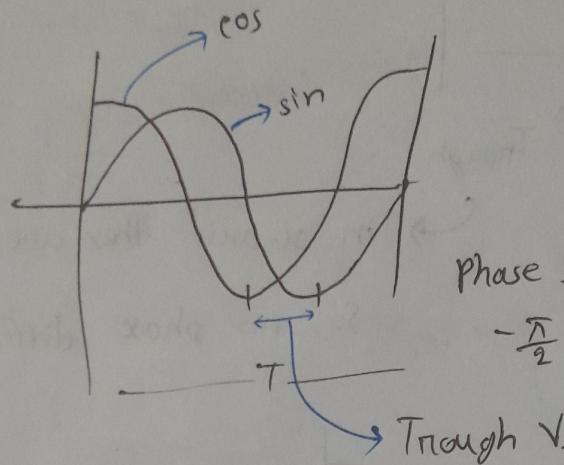
$$f_B = 2f_A$$

(*) Can you draw, same amplitude, one has 3 times higher frequency.



$$\textcircled{X} \quad X(t) = X_m \cos(\omega t - \frac{\pi}{2})$$

$$= X_m \sin(\omega t)$$



$$t=0,$$

$\cos = \text{up}$

$\sin = \text{down}$

then, \cos leading the graph

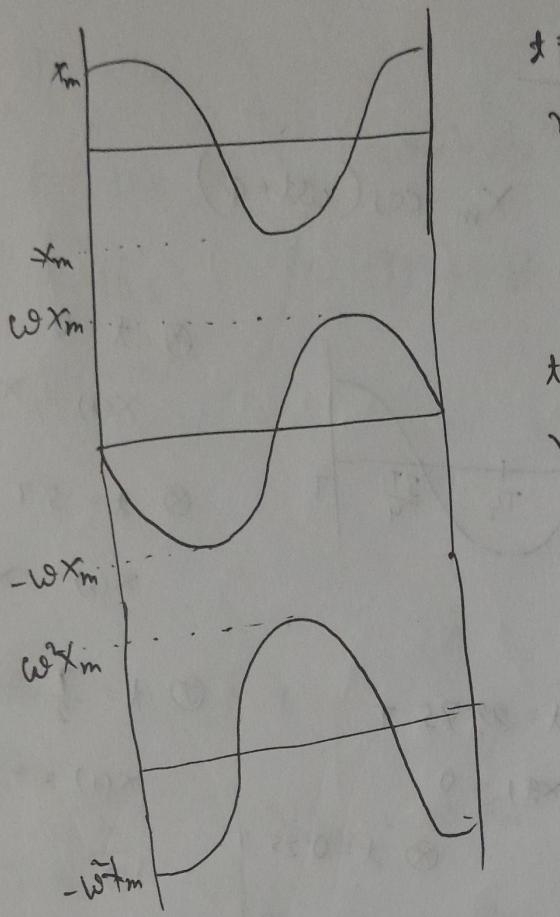
- \textcircled{Q} Can you find velocity and acceleration and show graphical representation.

$$X(t) = X_m \cos(\omega t + \phi)$$

derivative,

$$V(t) = -\omega X_m \sin(\omega t + \phi)$$

$$a(t) = -\omega^2 X_m \cos(\omega t + \phi)$$



$$t=0, \phi=0$$

$$x(t) = x_m$$

$$t=0, \phi=0$$

$$v(t) = 0$$

$$t=0, \phi=0$$

$$a(t) = -\tilde{\omega} x_m$$

⑧

$$x(t) = 2 \cos(2t + \phi)$$

maximum velocity

$$|v(t)| = |-\omega x_m|$$

$$= 2 \times 2 = 4 \text{ m/s}$$

$$v(t) = -4 \sin(2t + \phi)$$

$$a(t) = -8 \cos(2t + \phi)$$

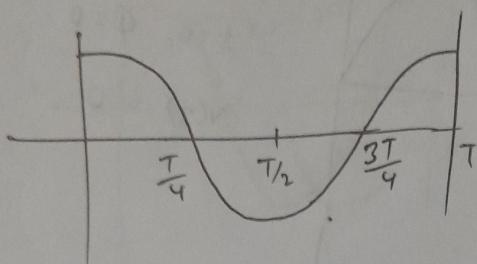
maximum acceleration

$$|a(t)| = |-\tilde{\omega} x_m|$$

$$= 4 \times 2 = 8 \text{ m/s}^2$$

~~(*)~~ Must in Final

$$x(t) = X_m \cos(\omega t + \phi)$$



$$\textcircled{2} \quad t = 0$$

$$x(t) = X_m$$

$$\textcircled{3} \quad t = 5T$$

$$x(t) = X_m$$

$$\textcircled{4} \quad t = 99.75T$$

$$x(t) = 0$$

$$\textcircled{5} \quad t = \frac{T}{2} = 5.5T$$

$$x(t) = -X_m$$

$$\textcircled{6} \quad t = 0.25T$$

$$x(t) = 0$$

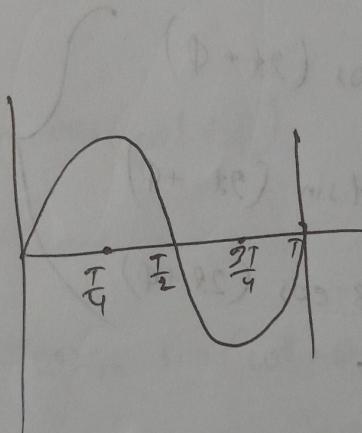
~~(*)~~ Given
 $t = 0$

$$x(t) \approx 0$$

$$\therefore t = 9.75T$$

$$x(t) = ?$$

$$= -X_m$$



marks = 3 points
must in final

(*)

$$\text{i) } F = -10x$$

$$\text{ii) } F = 10x$$

$$\text{iii) } F = 10\tilde{x}$$

$$\text{iv) } F = -10\tilde{x}$$

which is SHM?

i) \rightarrow Because similar to Hooke's Law

$$F = -kx$$

(*)

m = defined

k = defined

$$\omega = ? = \sqrt{\frac{k}{m}}$$

$$\omega = 2\pi f$$

$$T = \frac{1}{f}$$

$$v_{\max} = \omega x_m$$

$$a_{\max} = \omega^2 x_m$$

$$k = \frac{1}{2} m \tilde{v}^2$$

$$U = \frac{1}{2} k \tilde{x}^2$$

$$F = k + u$$

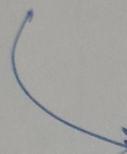
$$= \frac{1}{2} m \tilde{v}^2 + \frac{1}{2} k \tilde{x}^2$$

$$= \frac{1}{2} m \omega^2 x_m^2 \sin^2(\omega t + \phi) + \frac{1}{2} k x_m^2 \cos^2(\omega t + \phi)$$

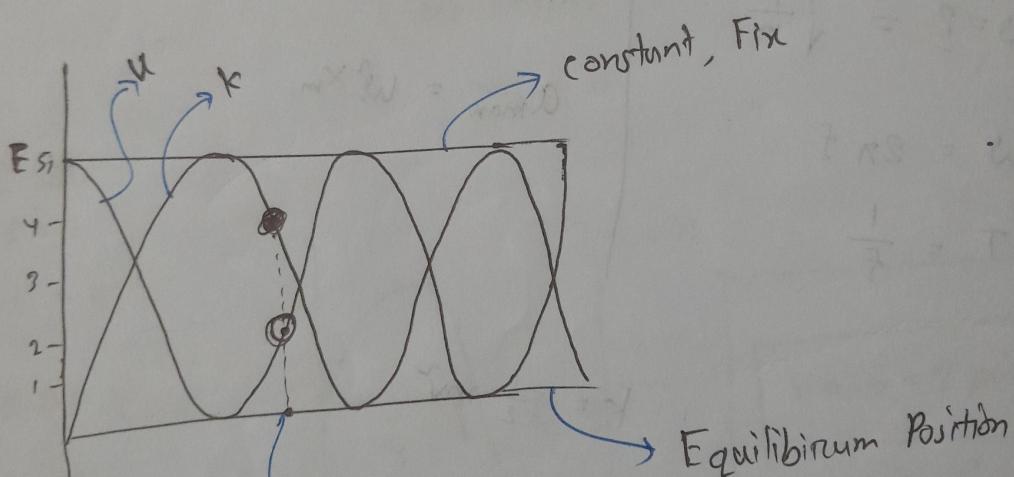
$$= \frac{1}{2} m \frac{k}{m} \tilde{x_m} \sin(\omega t + \phi) + \frac{1}{2} k \tilde{x_m} \cos(\omega t + \phi)$$

$$= \frac{1}{2} k \tilde{x_m} (\sin(\omega t + \phi) + \cos(\omega t + \phi))$$

$E = \frac{1}{2} k \tilde{x_m}$ \rightarrow Total energy time independent.



$$\left. \begin{aligned} k &= 2 \text{ N/m} \\ x_m &= 10 \text{ cm} \\ &= 0.1 \text{ m} \end{aligned} \right\} E = ?$$



$$\left. \begin{aligned} U &= 2j \\ k &= 3j \end{aligned} \right\} E = 5j$$

if intersected point, then,

$$\left. \begin{aligned} U &= 2.5j \\ k &= 2.5j \end{aligned} \right\} E = 5j$$

(*)

i) $\uparrow \vec{r}$
 $\uparrow \vec{F}$

ii) $\uparrow \vec{r}$
 $\downarrow \vec{F}$

iii) \vec{r} at 30°
 \vec{F}

iv) \vec{r} at 45°
 \vec{F}

$$\gamma_4 > \gamma_3 > \gamma_1 = \gamma_2$$

show below ←

(*) Wave is a disturbance that's carries energy.

i) Mechanical Wave

⇒ it requires medium

⇒ it follows Newton's Law

⇒ water wave, sound wave

ii) Electro magnetic Wave

⇒ No medium required

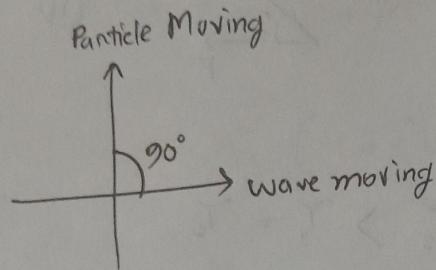
⇒ Doesn't follows Newton's Law

⇒ Light

iii) Matter Wave

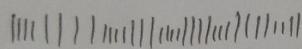
⇒ Electron & Proton

⊗ Transverse Wave \Rightarrow



\Rightarrow water wave

⊗ Longitudinal Wave:



$\rightarrow \rightarrow$

Sound Wave

⊗

$$x_{(t)} = x_m \cos(\omega t + \phi)$$

Amplitude Angular frequency Phase Difference

