

CSE 373 / L-16 / 16.04.2024 /

### \* Huffman Running time analysis:

⇒ initiation of  $Q$  using BUZLD-HEAP ⇒  $O(n)$

⇒  $\left. \begin{array}{l} \text{EXTRACT-MIN} \\ \text{INSERT} \end{array} \right\} O(\lg n) \text{ on } Q \text{ with } (n-1) \text{ objects}$

$$\begin{aligned} \therefore T(n) &= \sum_{i=1}^{n-1} \lg n \\ &= O(n \lg n) \end{aligned}$$

### \* Coin Change Problem (Cashier's Problem)

Algorithm:

CASHIER( $K, S$ )  $\xrightarrow{\text{amount need to change}}$   $\xrightarrow{\text{List of coin}}$

$n = S.length$

$\star = 0$

for  $i = n$  down to 1

while  $K \geq S[i]$

$\star = \star + 1$

$K = K - S[i]$

if  $K = 0$

break

return  $\star$

⊗ Does this algorithm always give the minimum amount of coins?

⇒ For common money systems, like euro, dollar  
⇒ Yes

For a general coin set or custom set  
⇒ No

⇒  $S = 1, 5, 8, 10$   
 $K = 13$

From greedy algorithm ⇒ 4 coins ⇒  $10 + 1 + 1 + 1$

But minimum coin is 2 ⇒  $8 + 5$

⊗ Run time:

for  $K = \text{constant}$

$$T(n) = O(n)$$

Midterm 28 April
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