



NORTH SOUTH UNIVERSITY

Department of Electrical and Computer Engineering

Homework – 02

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Ans. to the ques.no.01Lexemes:

Lexemes is a string of characters that are the lowest syntactical unit. Includes numerical literals, identifiers, reserve words.

Token:

Token is a group or collection of lexemes given a name. Sometimes, a single lexemes can also form a token.

Example:

Source Code:

while ($x \geq 5$):

$x = x - 6$;

<u>Lexemes</u>	<u>Tokens</u>
while	KEYWORDS
(LPAREN
x	ID
≥	OP
5	NUMBER
)	RPAREN
:	COLONE
x	ID
=	EQ
x	ID
-	OP
6	NUMBER
;	SEMICOLONE

Reserved Words:

Some words are kept reserved as an identifier for various operations, these words can't be used as user defined identifier.

Example: do, while, if, etc.

do, if, individually they are reserved words, but if we write together "doif" then it will be a valid identifier.

Metalinguage:

Metalinguage is a symbolic language that is used to define other language.

| \Rightarrow OR
 \rightarrow \Rightarrow defined as
 $::$ \Rightarrow defined as
 etc.

Content Free Grammar (CFG):

CFG is a formal grammar that describes the syntax of a PL. This grammar defines how tokens can be combined to form valid statements in the PL.

Example of CFG using Metalanguage:

$$\begin{aligned} \langle \text{number} \rangle &\rightarrow \langle \text{number} \rangle \langle \text{digit} \rangle \mid \langle \text{digit} \rangle \\ \langle \text{digit} \rangle &\rightarrow 0 \mid 1 \mid 2 \mid 3 \mid 4 \mid 5 \mid 6 \mid 7 \mid 8 \mid 9 \end{aligned}$$

Derivation:

Derivation is a process where we replace non-terminal with terminals word one by one. There are two types of derivation:

- (i) Left most derivation: left non-terminal replaced first
- (ii) Right most derivation: Right non-terminal replaced first

Production Rule:

Some rules defined in CFG that specify how symbols can be replaced by other symbols to form a valid statement in PL.

Example of Derivation:

Grammar:

$$\langle \text{number} \rangle \rightarrow \langle \text{number} \rangle \langle \text{digit} \rangle \mid \langle \text{digit} \rangle$$

$$\langle \text{digit} \rangle \rightarrow 0 \mid 1 \mid 2 \mid 3 \mid 4 \mid 5 \mid 6 \mid 7 \mid 8 \mid 9$$

Source/String: 234

Metalinguage derivation, left most:

$$\langle \text{number} \rangle \rightarrow \langle \text{number} \rangle \langle \text{digit} \rangle$$

$$\rightarrow \langle \text{number} \rangle \langle \text{digit} \rangle \langle \text{digit} \rangle$$

$$\rightarrow \langle \text{digit} \rangle \langle \text{digit} \rangle \langle \text{digit} \rangle$$

$$\rightarrow 2 \langle \text{digit} \rangle \langle \text{digit} \rangle$$

$$\rightarrow 2 \ 3 \langle \text{digit} \rangle$$

$$\rightarrow 2 \ 3 \ 4$$

Ans. to the ques. no. 02

Backw - Naur Form (BNF) is a context free grammar form, used to define grammar of a PL. And

EBNF is an extended version of BNF, proposed for convenience and reduce the lines on grammar.

In EBNF:

$\{ \dots \} \Rightarrow 0$ or any number of repetition

$(\dots) \Rightarrow$ options.

Example:

$\langle \text{number} \rangle \rightarrow \langle \text{number} \rangle \langle \text{digit} \rangle$

$\rightarrow \langle \text{number} \rangle \langle \text{digit} \rangle \langle \text{digit} \rangle$

$\rightarrow \langle \text{digit} \rangle \langle \text{digit} \rangle \langle \text{digit} \rangle \dots$

EBNF

$\langle \text{number} \rangle \rightarrow \langle \text{digit} \rangle \{ \langle \text{digit} \rangle \}$

Combined Example:

BNF:

$\langle \text{expr} \rangle \rightarrow \langle \text{expr} \rangle + \langle \text{term} \rangle \mid$

$\langle \text{expr} \rangle - \langle \text{term} \rangle \mid$

$\langle \text{term} \rangle \mid$

$\langle \text{term} \rangle \rightarrow \langle \text{term} \rangle * \langle \text{factor} \rangle \mid$

$\langle \text{term} \rangle / \langle \text{factor} \rangle \mid$

$\langle \text{factor} \rangle$

$\langle \text{factor} \rangle \rightarrow \langle \text{exp} \rangle ** \langle \text{factor} \rangle \mid$

$\langle \text{exp} \rangle \rightarrow \langle \text{exp} \rangle$

$(\langle \text{exp} \rangle) \mid \text{id}$

EBNF:

$\langle \text{expr} \rangle \rightarrow \langle \text{term} \rangle \{ (+|-) \langle \text{term} \rangle \}$

$\langle \text{term} \rangle \rightarrow \langle \text{factor} \rangle \{ (*|/) \langle \text{factor} \rangle \}$

$\langle \text{factor} \rangle \rightarrow \langle \text{exp} \rangle \{ ** \langle \text{factor} \rangle \}$

$\langle \text{exp} \rangle \rightarrow (\langle \text{exp} \rangle) \mid \text{id}$

Ans. to the ques. no. 03

Given grammar:

$$\langle S \rangle \rightarrow \langle A \rangle a \langle B \rangle b$$

$$\langle A \rangle \rightarrow \langle A \rangle b \mid b$$

$$\langle B \rangle \rightarrow b$$

For string: babb

$$S \rightarrow \langle A \rangle a \langle B \rangle b$$

$$\rightarrow b a \langle B \rangle b \quad [\langle A \rangle = b]$$

$$\rightarrow b a b b \quad [\langle B \rangle = b]$$

\therefore babb is derivable.

For string: bbbabb

$$S \rightarrow \langle A \rangle a \langle B \rangle b$$

$$\rightarrow \langle A \rangle b a \langle B \rangle b \quad [\langle A \rangle = \langle A \rangle b]$$

$$\rightarrow \langle A \rangle b b a \langle B \rangle b \quad [\langle A \rangle = \langle A \rangle b]$$

$$\rightarrow b b b a \langle B \rangle b \quad [\langle A \rangle = b]$$

$$\rightarrow b b b a b b \quad [\langle B \rangle = b]$$

\therefore bbbabb is derivable.

For string: bbaaaaabc

As we can see that there is a terminal "c" which is not defined in the grammar.

Therefore, the string is not derivable.

For string: aaaaaa

"a" is not available as a single terminal in the grammar. As a result, whatever we choose it will produce b. Therefore, the string aaaaaa is not derivable by this grammar.

Ans. to the que. no. 04

The grammar will be,

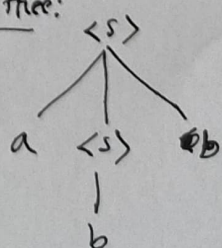
$a \langle S \rangle b$

$\langle S \rangle \rightarrow a \langle S \rangle b$
 $\langle S \rangle \rightarrow b$

For string: abb

$\langle S \rangle \rightarrow a \langle S \rangle b$
 $\rightarrow abb \quad [\langle S \rangle = b]$

Parse tree:



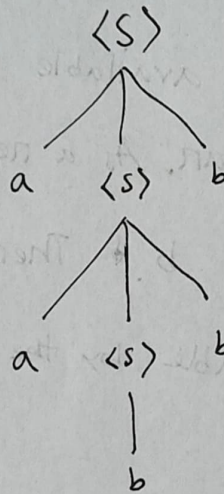
For string: aabb

$$\langle s \rangle \rightarrow a \langle s \rangle b$$

$$\rightarrow a a \langle s \rangle b b [\langle s \rangle = a \langle s \rangle b]$$

$$\rightarrow a a b b b [\langle s \rangle = b]$$

Parse tree:



Ans. to the ques. no. 05

Definition of Identifier:

$$\langle \text{identifier} \rangle \rightarrow \langle \text{letter} \rangle \langle \text{nest} \rangle$$

$$\langle \text{nest} \rangle \rightarrow \langle \text{letter} \rangle \langle \text{nest} \rangle / \langle \text{digit} \rangle \langle \text{nest} \rangle / \epsilon$$

$$\langle \text{letter} \rangle \rightarrow a|b|\dots|y|z|A|B|\dots|Z|_2$$

$$\langle \text{digit} \rangle \rightarrow 0|1|2|3|\dots|8|9$$

Ans. to the ques. no. 06

If a designed grammar has more than one left-most derivation or right-most derivation, then the grammar is ambiguous.

Example:

Grammar:

$$S \rightarrow AS \mid \epsilon$$

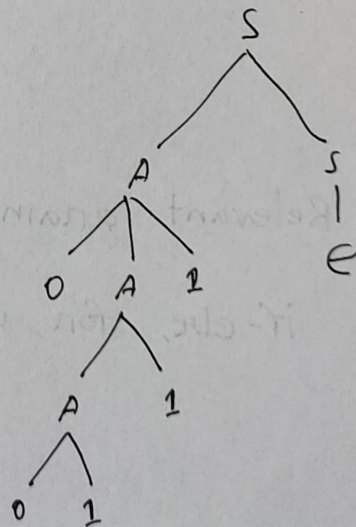
$$A \rightarrow A1 \mid 0A1 \mid 01$$

String: 00111

Left-most derivation:

$$\begin{aligned} S &\rightarrow AS \\ &\rightarrow 0A1S \quad [A = 0A1] \\ &\rightarrow 0A11S \quad [A = A1] \\ &\rightarrow 00111S \quad [A = 01] \\ &\rightarrow 00111 \quad [S = \epsilon] \end{aligned}$$

Parse tree:



Another left-most derivation:

$$S \rightarrow AS$$

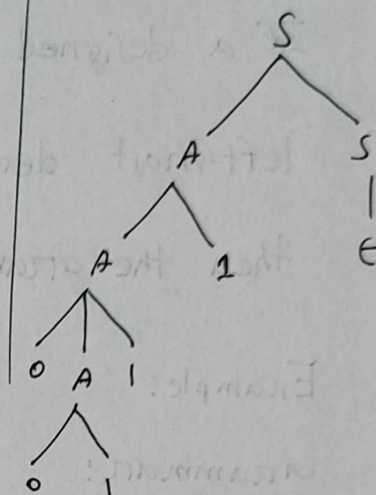
$$\rightarrow AIS [A = AI]$$

$$\rightarrow 0A11S [A = 0AI]$$

$$\rightarrow 00111S [A = 01]$$

$$\rightarrow 00111 [S = \epsilon]$$

Parse tree:



This grammar has two left-most derivation for the string "00111".

Therefore, the grammar is ~~any~~ ambiguous.

Ans. to the ques. no.07

Relevant grammars of three control statements if-else, for, while are given below:

Grammar for "if-else" statement:

$\langle \text{If Stmt} \rangle \rightarrow \text{if} (\langle \text{condition} \rangle) \langle \text{statement} \rangle \langle \text{else} \rangle$

$\langle \text{else} \rangle \rightarrow \text{else } \langle \text{statement} \rangle \mid \epsilon \mid \text{else } \langle \text{If Stmt} \rangle$

$\langle \text{condition} \rangle \rightarrow \langle \text{expr} \rangle$

$\langle \text{statement} \rangle \rightarrow \langle \text{expr} \rangle ; \mid \{ \langle \text{block} \rangle \}$

$\langle \text{block} \rangle \rightarrow \{ \langle \text{If Stmt} \rangle \mid \langle \text{For Stmt} \rangle \mid \langle \text{While Stmt} \rangle \mid \langle \text{stmt list} \rangle$

$\langle \text{stmt list} \rangle \rightarrow \langle \text{statement} \rangle \langle \text{stmt list} \rangle \mid \epsilon$

Grammar for "for" statement:

$\langle \text{For Stmt} \rangle \rightarrow \text{for} (\langle \text{init} \rangle ; \langle \text{condition} \rangle ; \langle \text{update} \rangle) \langle \text{statement} \rangle$

$\langle \text{init} \rangle \rightarrow \langle \text{assignment} \rangle \mid \langle \text{expr} \rangle \mid \epsilon$

$\langle \text{condition} \rangle \rightarrow \langle \text{expr} \rangle \mid \epsilon$

$\langle \text{update} \rangle \rightarrow \langle \text{expr} \rangle \mid \epsilon$

$\langle \text{statement} \rangle \rightarrow \langle \text{expr} \rangle ; \mid \{ \langle \text{block} \rangle \}$

$\langle \text{block} \rangle \rightarrow \langle \text{If Stmt} \rangle \mid \langle \text{For Stmt} \rangle \mid \langle \text{While Stmt} \rangle \mid \langle \text{stmt list} \rangle$

$\langle \text{stmt list} \rangle \rightarrow \langle \text{statement} \rangle \langle \text{stmt list} \rangle \mid \epsilon$

Grammar for while statement:

$\langle \text{While Stmt} \rangle \rightarrow \text{while} (\langle \text{condition} \rangle) \langle \text{statement} \rangle$

$\langle \text{condition} \rangle \rightarrow \langle \text{expr} \rangle$

$\langle \text{statement} \rangle \rightarrow \langle \text{expr} \rangle ; \mid \{ \langle \text{block} \rangle \}$

$\langle \text{block} \rangle \rightarrow \langle \text{If Stmt} \rangle \mid \langle \text{For Stmt} \rangle \mid \langle \text{While Stmt} \rangle \mid \langle \text{stmtlist} \rangle$

$\langle \text{stmtlist} \rangle \rightarrow \langle \text{statement} \rangle \langle \text{stmtlist} \rangle \mid \epsilon$

~~Grammar~~

Ref.:

- Class Notes
- Handouts provided by ~~MSK1~~ Dr. Md Shahriar Karim [MSK1]
- ChatGPT - for the last question.