

Fundamental  
Quantity

Length

Time

Mass

Temp.

Current

Derived  
Quantity

Force

Weight

Volume

(\*)

$10^{24}$  → Yotta

→ [Mid Question Must]

$10^{-24}$  → Xecto

(\*)

$$E = \frac{1}{2} mv^2$$

$$= [ML^2 T^{-2}]$$

$$E = mc^2$$

$$= [ML^2 T^{-2}]$$

(\*) Why current is not a vector?

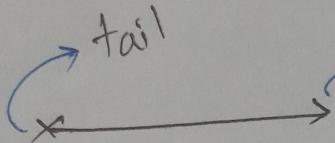
$$X = vt$$

Length

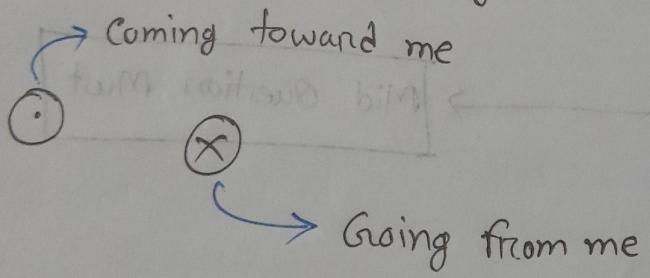
$$= [L T^{-1} \cdot T]$$

$$\Rightarrow [L]$$

Vector,



magnitude

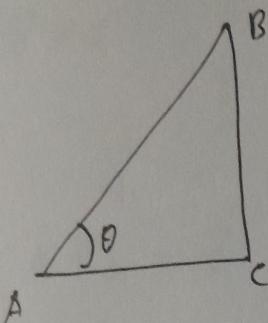


$$[L^2 T^{-1} M] =$$

$$[L^2 T^{-1} M] =$$

Newton's law of motion

⊗ Pythagorean Theorem:



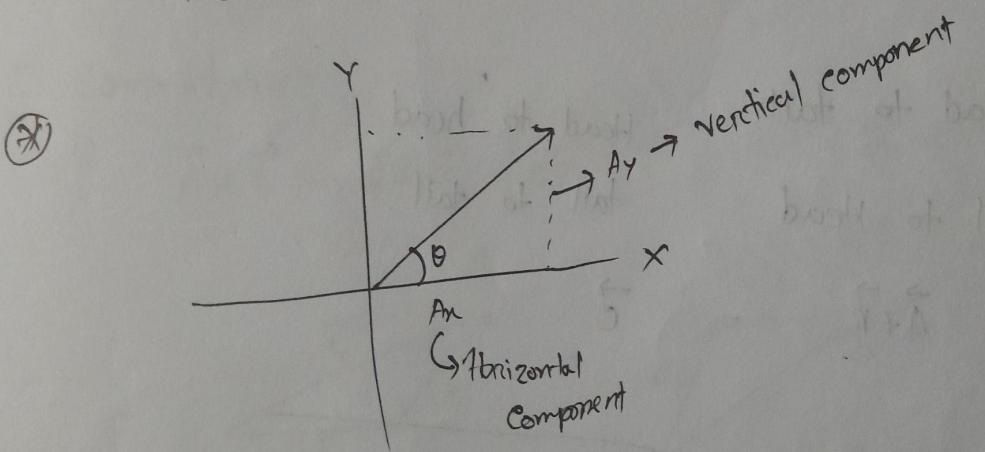
$$AB^2 = BC^2 + AC^2$$

- ① calculating unknown length
- ② Checking Right Triangle

$$\cos \theta = \frac{AC}{AB}$$

$$\sin \theta = \frac{BC}{AB}$$

$$\tan \theta = \frac{BC}{AC}$$



$$\cos \theta = \frac{Ax}{A}$$

$$Ax^2 + Ay^2 = A^2$$

$$\text{i) } Ax = A \cos \theta$$

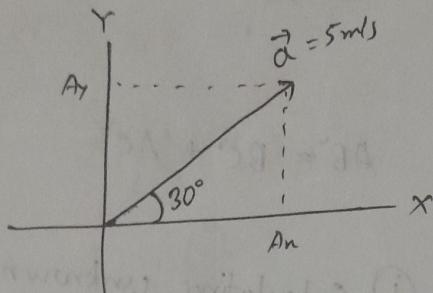
$$|A| = \sqrt{Ax^2 + Ay^2}$$

$$\text{ii) } Ay = A \sin \theta$$

$$\tan \theta = \frac{Ay}{Ax}$$

$$\text{iii) } \theta = \tan^{-1} \left( \frac{Ay}{Ax} \right)$$

(\*)



$$A_x = 5 \cos \theta$$

$$A_y = 5 \sin \theta$$

$$\frac{\partial A}{\partial t} = 0.203$$

$$\frac{\partial A}{\partial x} = 0.012$$

$$\frac{\partial A}{\partial y} = 0.005$$

(\*)

$$\vec{A} = \vec{B}$$

(\*)

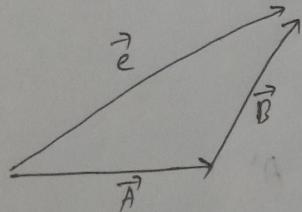
Head to tail

tail to Head

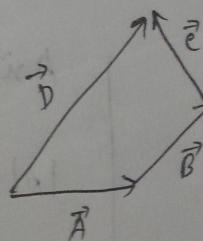
Head to head

tail to tail

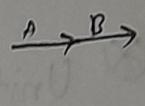
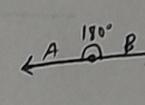
$$\vec{A} + \vec{B} = \vec{C}$$



$$\vec{A} + \vec{B} + \vec{C} = \vec{D}$$

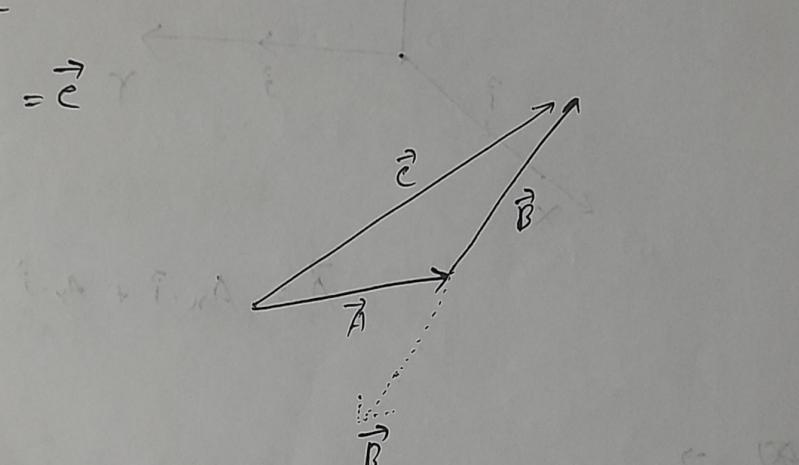


④  $\vec{A} = 5$        $\vec{B} = 6$        $\vec{C} = ?$

Maximum = 11  $\rightarrow$    
 Minimum = 1  $\rightarrow$  

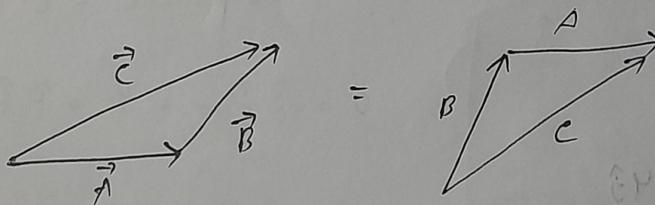
⑤  $\vec{A} - \vec{B} = \vec{C}$

$\vec{A} + (-\vec{B}) = \vec{C}$

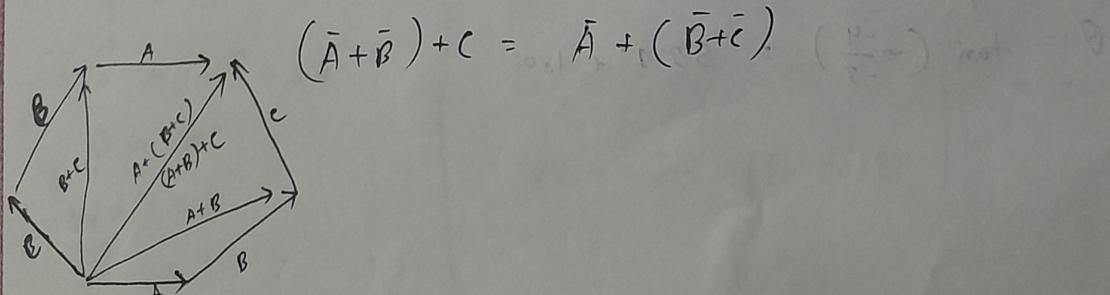


⑥ Commutative:

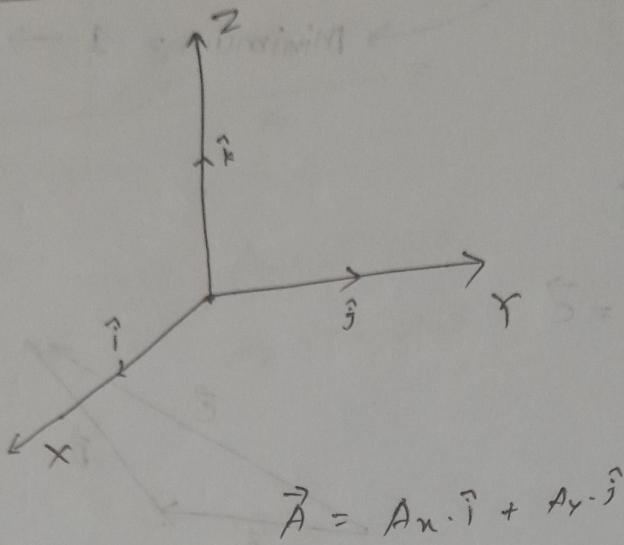
$$\vec{A} + \vec{B} = \vec{B} + \vec{A} = \vec{C}$$



⑦ Associative Rule:



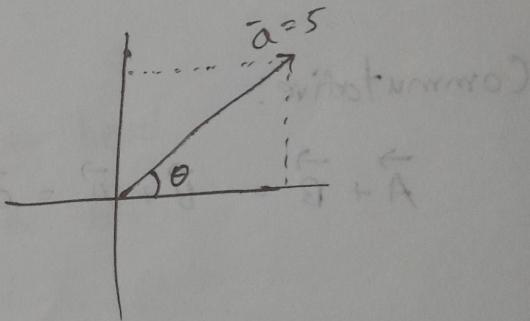
⊗ Unit vector



⊗  $\vec{A} = 3\hat{i} + 4\hat{j}$

$$|\vec{A}| = \sqrt{3^2 + 4^2} = 5$$

$$\theta = \tan^{-1}\left(\frac{4}{3}\right) = 53.1^\circ$$



$$A = -3\hat{i} - 4\hat{j}$$

$$|\vec{A}| = \sqrt{3^2 + 4^2} = 5$$

$$\theta = \tan^{-1}\left(-\frac{4}{3}\right) = 53.1^\circ + 180^\circ$$



L-3 / 12-10-2022

(\*)

No relation with  $(A, B)$

$$\text{i) } \bar{A} \cdot \bar{B} = c \rightarrow \vec{F} \cdot \vec{d} = w \quad | \quad \vec{F} \cdot \vec{v} = p$$

$$\text{ii) } \bar{A} \times \bar{B} = \vec{c} \rightarrow \vec{R} \times \vec{F} = \vec{\gamma}$$

(\*)

$$\text{i) } \bar{A} \cdot \bar{B} = |\bar{A}| \cdot |\bar{B}| \cdot \cos\theta$$

$$= A_x B_x + A_y B_y + A_z B_z$$

$$\bar{A} = A_x \hat{i} + A_y \hat{j} + A_z \hat{k}$$

$$\bar{B} = B_x \hat{i} + B_y \hat{j} + B_z \hat{k}$$

$$\text{i) } \hat{i} \cdot \hat{j} = 1 \cdot 1 \cos 90^\circ = 0$$

$$\hat{i} \cdot \hat{j} = \hat{j} \cdot \hat{k} = \hat{k} \cdot \hat{i} = 0$$

$$\text{ii) } \hat{i} \cdot \hat{i} = \hat{j} \cdot \hat{j} = \hat{k} \cdot \hat{k} = 1$$

$$\text{i) } \vec{F} = 3\hat{i} + 3\hat{j} + \hat{k}$$

$$\vec{d} = -\hat{j} + 5\hat{k}$$

$$\theta = 30^\circ$$

$$w = ?$$

$$|\vec{F}| = \sqrt{3^2 + 3^2 + 1^2} = \sqrt{19}$$

$$|\vec{d}| = \sqrt{1 + 5^2} = \sqrt{26}$$

$$w = \sqrt{19} \cdot \sqrt{26} \cos 30^\circ$$

$$w = -3 + 5 = 2$$

$$\Theta = \cos^{-1} \frac{|\bar{A} \cdot \bar{B}|}{|\bar{A}| \cdot |\bar{B}|}$$

⊗ Cross Product

$$\bar{A} \times \bar{B} = |A| |B| \sin \theta$$

$$\text{i) } \hat{i} \times \hat{i} = |x| \times \sin 0$$

$$= 0$$

$$\hat{i} \times \hat{i} = \hat{j} \times \hat{j} = \hat{k} \times \hat{k} = 0$$

$$\text{ii) } \hat{i} \times \hat{j} = |x| \times \sin 90^\circ$$

$$= 1 \hat{k}$$

$$\hat{j} \times \hat{i} = -\hat{k}$$

$$\bar{A} = A_x \hat{i} + A_y \hat{j} + A_z \hat{k}$$

$$\bar{B} = B_x \hat{i} + B_y \hat{j} + B_z \hat{k}$$

$$\bar{A} \times \bar{B} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ A_x & A_y & A_z \\ B_x & B_y & B_z \end{vmatrix}$$

$$= \hat{i}(A_y B_z - A_z B_y) - \hat{j}(A_x B_z - A_z B_x) + \hat{k}(A_x B_y - A_y B_x)$$

$$\vec{R} = \hat{i} + \hat{j} + 3\hat{k}$$

$$\vec{F} = 2\hat{i} + \hat{k}$$

$$\vec{\gamma} = \vec{R} \times \vec{F}$$

$$\theta = \sin^{-1} \frac{|\vec{A} \times \vec{B}|}{|\vec{A}| |\vec{B}|}$$

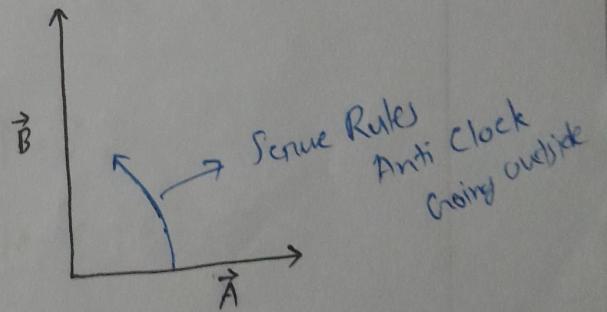
$$\vec{\gamma} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 1 & 1 & 3 \\ 2 & 0 & 1 \end{vmatrix}$$

$$= \hat{i}(1-0) - \hat{j}(1-6) + \hat{k}(0-2)$$

$$= \hat{i} + 5\hat{j} - 2\hat{k}$$

$$|\gamma| = \sqrt{1+5^2+2^2} = \sqrt{30}$$

$$\theta = \sin^{-1} \frac{\sqrt{30}}{\sqrt{11} \cdot \sqrt{5}}$$



$\vec{A} \times \vec{B} = \odot \rightarrow$  Coming Towards me.

(\*)  $\vec{A} \times \vec{B} = \vec{C}$

$$\begin{matrix} \downarrow & \downarrow & \downarrow \\ -z & \boxed{-x} & y \end{matrix}$$

$$\vec{B} \times \vec{A} = \odot$$

(\*)  $\vec{C} = \vec{A} \times \vec{B}$

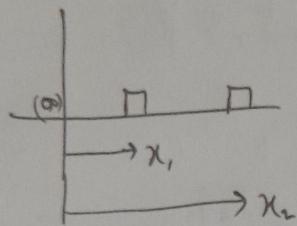
$$\begin{matrix} \downarrow & \downarrow & \downarrow \\ -z & x & \boxed{-y} \end{matrix}$$

L-4 / 17. 10. 2022 /

kinetics

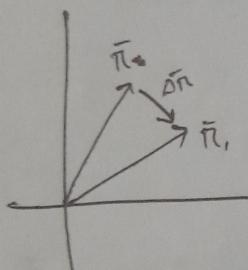
↳ kinema

↳ motion



$$\Delta \bar{x} = \bar{x}_2 - \bar{x}_1$$

$$\Delta t = t_2 - t_1$$



$$r = x\hat{i} + y\hat{j} = 2\hat{i} + 3\hat{j}$$

$$r_1 = x_1\hat{i} + y_1\hat{j} = 4\hat{i} + 5\hat{j}$$

$$\bar{r} + \Delta \bar{r} = \bar{r}_2$$

$$\Delta \bar{r} = \bar{r}_2 - \bar{r}_1$$

$$= (x_2\hat{i} + y_2\hat{j}) - (x_1\hat{i} + y_1\hat{j})$$

$$= (x_2 - x_1)\hat{i} + (y_2 - y_1)\hat{j}$$

$$= 2\hat{i} + 2\hat{j}$$

$$\otimes = 5 \times 5$$

$$5 = 5 \times 5$$

$$5 \times 5 = 5$$

$$\textcircled{1} \quad x(t) = t^2 + 2t + 1$$

$$y(t) = t + 5$$

$$t = 5 \text{ sec} \Rightarrow x(5) = 36$$

$$y(5) = 10$$

$$\vec{r} = x\hat{i} + y\hat{j}$$

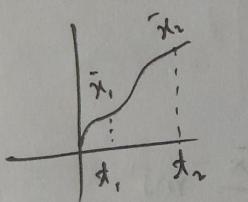
$$= 36\hat{i} + 10\hat{j}$$

$$|\vec{r}| = \sqrt{36 + 10}$$

$$\theta = \tan^{-1} \frac{y}{x} = \tan^{-1} \left( \frac{10}{36} \right) =$$

$$v_{avg} = \frac{\Delta \bar{x}}{\Delta t} \text{ m/s}$$

\textcircled{2}



$$\Delta t = t_2 - t_1$$

$$\textcircled{3} \quad x_1 = 2\hat{i} + 3\hat{j}$$

$$\Delta \bar{x} = \hat{i} + \hat{j}$$

$$x_2 = 3\hat{i} + 4\hat{j}$$

$$\Delta t = 10 - 5 = 5$$

$$t_1 = 5 \text{ sec}$$

$$t_2 = 10 \text{ sec}$$

$$v_{avg} = \frac{\Delta \bar{x}}{\Delta t} = \left( \frac{1}{5} \hat{i} + \frac{1}{5} \hat{j} \right) \text{ m/s}$$

$$v = \lim_{\Delta t \rightarrow 0} \frac{\Delta \bar{x}}{\Delta t} = \frac{dx}{dt} = \dot{x} \quad \rightarrow \frac{d}{dt}$$

$$\textcircled{X} \quad x(t) = t^2 + 2t + 1$$

$$\frac{dx}{dt} = 2t+2, \quad t=2 \text{ sec}$$

$$v = 2 \cdot 2 + 2 = 6 \text{ ms}^{-1}$$

$$\textcircled{X} \quad x(t) = t^2 + 2t + 5$$

$$y(t) = t + 10$$

$$t = 2 \text{ sec}$$

$$v = ?$$

$$v_x = \frac{dx}{dt} = 2t+2 = 6 \text{ ms}^{-1}$$

$$v_y = \frac{dy}{dt} = 1 \text{ ms}^{-1}$$

$$\vec{v} = v_x \hat{i} + v_y \hat{j}$$

$$= (6\hat{i} + \hat{j}) \text{ ms}^{-1}$$

$$|\vec{v}| = \sqrt{c^2 + r^2} \text{ ms}^{-1}$$

$$\approx \sqrt{37} \text{ ms}^{-1}$$

$$\theta = \tan^{-1}\left(\frac{1}{6}\right) =$$

$$v_{avg} = \frac{\Delta x}{\Delta t} \text{ ms}^{-1}$$

$$a_{avg} = \frac{\Delta \vec{v}}{\Delta t} \text{ ms}^{-1}$$

$$a = \lim_{\Delta t \rightarrow 0} \frac{\Delta \vec{v}}{\Delta t} = \frac{d\vec{v}}{dt} = \frac{d}{dt} \left( \frac{dx}{dt} \right)$$

$$= \frac{d^2x}{dt^2} = \ddot{x}$$

$$\textcircled{8} \quad x(t) = t^2 + 2t + 5$$

$$y(t) = t^3 + 3t + 6$$

$$t = 2 \text{ sec}$$

$$a = ?$$

$$v_x = \frac{dx}{dt} = 2t + 1$$

$$a_x = 2 \text{ m/s}^2 \rightarrow \text{time independent}$$

$$v_y = 3t^2 + 3$$

$$a_y = 6t \rightarrow \text{time dependent}$$

$$\vec{a} = a_x \hat{i} + a_y \hat{j}$$

$$= (2\hat{i} + 12\hat{j}) \text{ m/s}^2$$

$$|\vec{a}| = \sqrt{2^2 + 12^2} = \sqrt{148} \text{ m/s}^2$$

$$v = v_0 + at$$

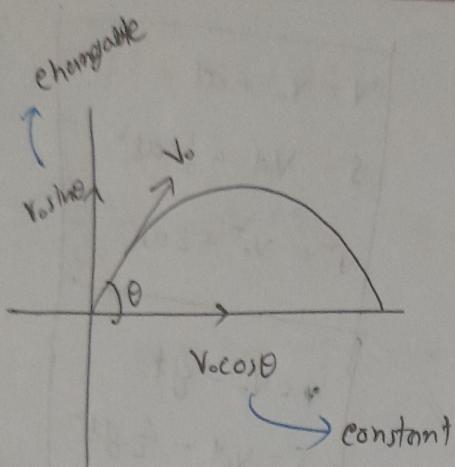
$$s = v_0 t + \frac{1}{2} a t^2$$

$$\tilde{v} = \tilde{v}_0 + 2at$$

$$v = v_0 - gt$$

$$s = v_0 t - \frac{1}{2} g t^2$$

$$\tilde{v} = \tilde{v}_0 - 2gt$$



$$s = v_0 t - \frac{1}{2} g t^2$$

Vertical

$$y - y_0 = (v_0 \sin \theta)t - \frac{1}{2} g t^2$$

$$y = (v_0 \sin \theta)t - \frac{1}{2} g t^2$$

$$y = v_0 \sin \theta \frac{x}{v_0 \cos \theta} - \frac{1}{2} g \left( \frac{x}{v_0 \cos \theta} \right)^2$$

$$y = x \tan \theta - \left[ \frac{1}{2} g \frac{x^2}{v_0^2 \cos^2 \theta} \right]$$

$$y = ax - bx^2$$

horizontal

$$x - x_0 = (v_0 \cos \theta)t$$

$$x = (v_0 \cos \theta)t + x_0$$

$$t = \frac{x - x_0}{v_0 \cos \theta}$$

Q

$$t = \frac{R}{v_0 \cos \theta}$$

$$Y - Y_0 = (V_0 \sin \theta) t - \frac{1}{2} g t^2$$

$$0 = V_0 \sin \theta \frac{R}{V_0 \cos \theta} - \frac{1}{2} g \left( \frac{R}{V_0 \cos \theta} \right)^2$$

$$R = \frac{2 V_0^2 \sin \theta \cos \theta}{g}$$

$$R = \frac{V_0^2 \sin 2\theta}{g}$$

Earth  
 $v = 460 \text{ m/s}$

$$R = 6371 \times 1000 \text{ m}$$

$$a = \frac{v^2}{R} = 0.03 \text{ m/s}^2 < 2.8$$

### Uniform circular motion



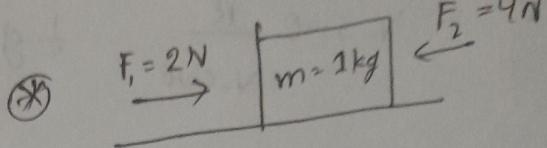
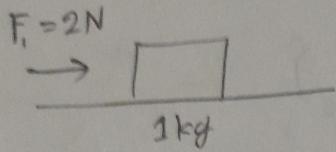
$$|v| = 10 \text{ m/s}$$

$$a = \frac{v^2}{R}$$

Newton 2nd Law

$$F = ma$$

L-6 / 24.10.2022 /



$$\bar{F}_{\text{net}} = m\bar{a}$$

$$F_1 = ma$$

$$a = \frac{F_1}{m} = 2 \text{ m/s}^2$$

$\rightarrow x \text{ axis}$

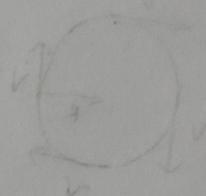
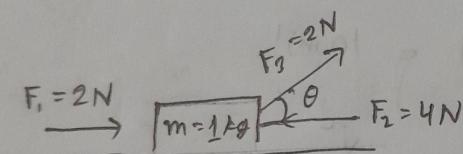
$$\bar{F}_{\text{net}} = m\bar{a}$$

$$F_1 - F_2 = m\bar{a}$$

$$2 - 4 = ma$$

$$a = \frac{2 - 4}{1} = -2 \text{ m/s}^2$$

$\rightarrow -x \text{ axis}$



$$\bar{F}_{\text{net}} = m\bar{a}$$

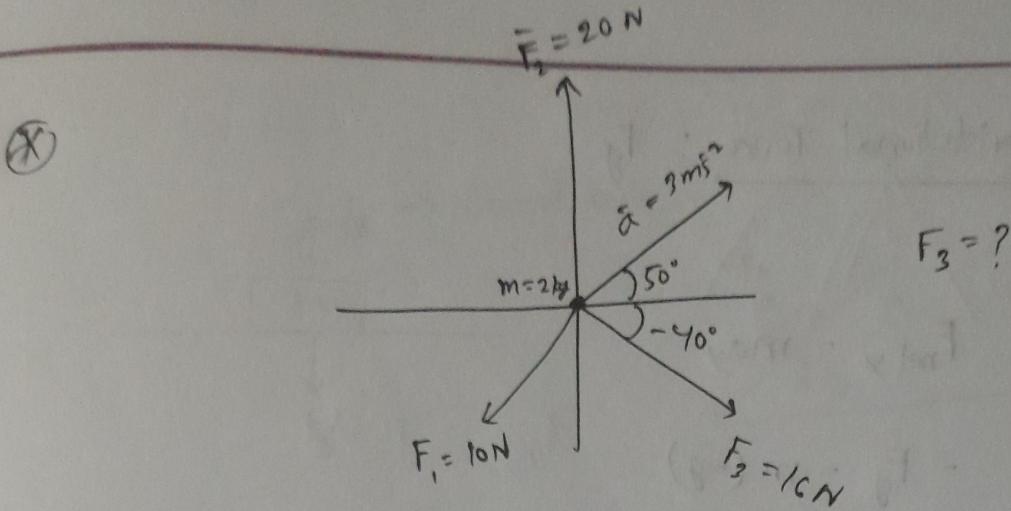
$$F_1 - F_2 + F_3 \cos\theta = ma$$

$$a = \frac{F_1 - F_2 + F_3 \cos\theta}{m}$$

$$= \frac{2 - 4 + 2 \cos 30^\circ}{1} \text{ m/s}^2$$

$$= -0.267 \text{ m/s}^2$$

$\rightarrow -x \text{ axis}$



$$\bar{F}_{\text{net}} = m\ddot{a}$$

$$\bar{F}_1 + \bar{F}_2 + \bar{F}_3 = m\ddot{a}$$

$$\bar{F}_3 = m\ddot{a} - \bar{F}_1 - \bar{F}_2$$

X-component:

$$F_{3x} = m\ddot{a}_x - F_{1x} - F_{2x}$$

$$= m\ddot{a} \cos 50^\circ - F_1 \cos 210^\circ - F_2 \cos 90^\circ$$

$$= 12.5 \text{ N}$$

Y-component:

$$F_{3y} = m\ddot{a}_y - F_{1y} - F_{2y}$$

$$= m\ddot{a} \sin 50^\circ - F_1 \sin 210^\circ - F_2 \sin 90^\circ$$

$$= -10.4 \text{ N}$$

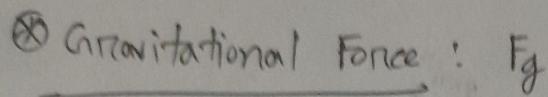
$$\therefore F_3 = 12.5 \hat{i} - 10.4 \hat{j}$$

$$F_3 = \sqrt{(12.5)^2 + (10.4)^2}$$

$$= 16 \text{ N}$$

$$\theta = \tan^{-1}\left(\frac{F_1}{F_2}\right)$$

$$= -40$$

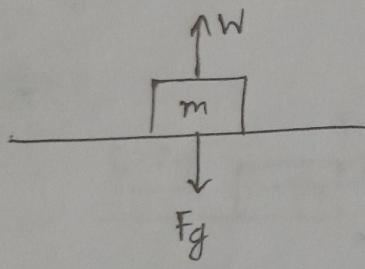
  $\otimes$  Gravitational Force :  $F_g$

$$F_{net\ y} = m a_y$$

$$- F_g = m (-g)$$

$$\boxed{F_g = mg}$$

Weight:



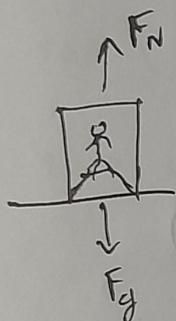
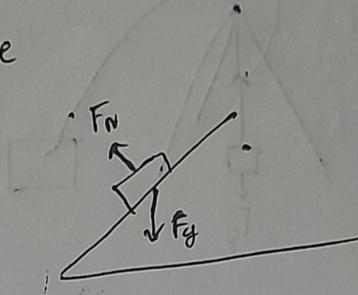
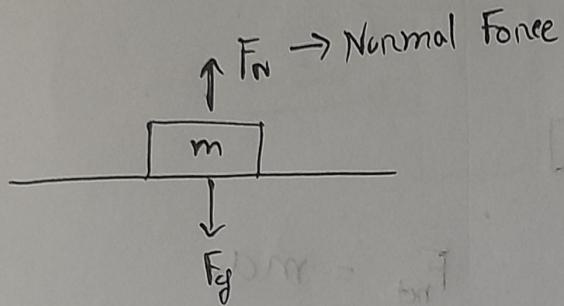
$$\vec{F}_{net} = m \vec{a} = 0$$

$$\bar{W} - \bar{F}_g = 0$$

$$\bar{W} = \bar{F}_g = m \bar{g}$$

$$\boxed{W = mg}$$

L-7 / 26.10.2022/



$$F_{net} = m a_y$$

$$F_N = F_g = m a_y$$

$$F_N = F_g + m a_y$$

For Free Fall

$$\Rightarrow F_N = m(g - g) \\ = 0$$

►  $F_N = m(g + a_y)$  → For moving

For stationary,

$$a_y = 0$$

$$F_N = F_g = m g$$

$\uparrow \Rightarrow a_y = \text{positive}$

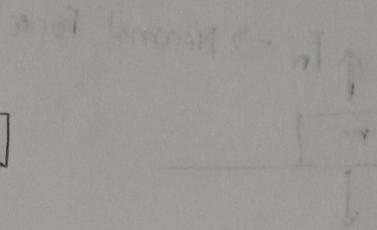
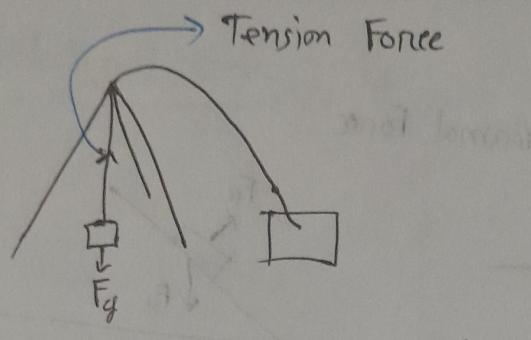
$$\Rightarrow F_N = m(9.8 + 2)$$

$$\bullet F_N > F_g$$

$\downarrow \Rightarrow F_N = m(9.8 - a_y);$

$$a_y = -v$$

$$F_N < F_g$$



$$F_{net} = m\alpha_y$$

① Stationary:

$$T = m(g + \alpha_y)$$

$$T = F_g = mg$$

$$T - F_g = m\alpha_y$$

$$T = F_g + m\alpha_y$$

$$T = m(g + \alpha_y)$$

②  $\downarrow \alpha_y = 1 m/s^2$

$$T = m(g - 1)$$

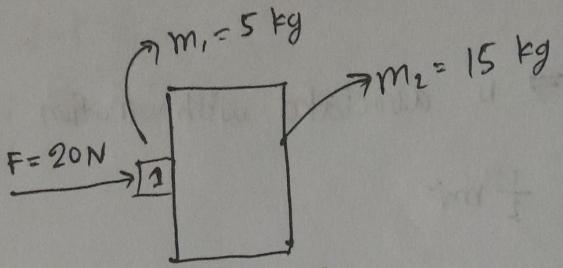
$$T < F_g$$

③  $\uparrow \alpha_y = 1 m/s^2$

$$T = m(g + 1)$$

$$T > F_g$$

⊗ For Newton's third law, we need at least two objects.



$$F_{\text{net}} = ma$$

$$20 = (m_1 + m_2)a$$

$$20 = (5+15)a$$

$$20 = 20a$$

$$a = 1 \text{ m/s}^2$$

$\rightarrow +x$  axis

$$\vec{F}_{12} = ?$$

$$F_{\text{net}} = ma$$

$$F_{12} = 15 \times 1$$

$$F_{12} = 15 \text{ N}$$

$$\vec{F}_{21} = ma$$

$$= 5 \times 1$$

$$= 5 \text{ N?}$$

$$F_{21} = ma$$

$$F - F_{21} = ma$$

$$F_{21} = F - ma$$

$$= 20 - 5 \times 1$$

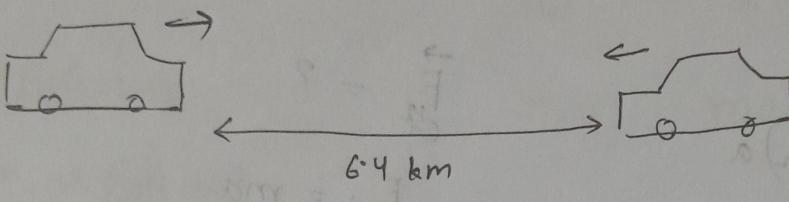
$$= 15 \text{ N}$$

$$\boxed{\therefore F_{12} = F_{21}}$$

L-8 / 31.10.2022 /

K.E  $\Rightarrow$  is associated with motion

$$K.E = \frac{1}{2} m v^2$$



$$K.E = \frac{1}{2} m v^2$$

$$v^2 = v_0^2 + 2as$$

$$= 0 + 2 \times 0.26 \times 3.2 \times 10^9 \text{ m}$$

$$v = 40.8 \text{ m/s}$$

$$W = 1.2 \times 10^6 \text{ N}$$

$$a = 0.26 \text{ m/s}^2$$

$$m = \frac{W}{g} = 1.22 \times 10^5 \text{ kg}$$

$$K.E = 2 \times \frac{1}{2} m v^2$$

$$= m v^2 = 2 \times 10^8 \text{ J}$$

For two cars

- \* Energy transfer by a force, then there will be work done.

$$\vec{d} \quad \vec{F}$$

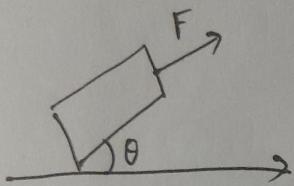
$W = \vec{F} \cdot \vec{d}$

$W \rightarrow +ve$

$$\vec{d} \quad 180^\circ \quad \vec{F}$$

$W = Fd \cos 180^\circ$

$= -ve$



$$F_x = m a_x$$

$$\tilde{v} = \tilde{v}_0 + 2ad$$

$$a_x = \frac{\tilde{v} - \tilde{v}_0}{2d}$$

$$F_x = m \left( \frac{\tilde{v} - \tilde{v}_0}{2d} \right)$$

$$F_x d = \frac{1}{2} m \tilde{v}^2 - \frac{1}{2} m \tilde{v}_0^2 = k_f - k_i = \Delta k$$

$$x_1 = 35$$

$$x_2 = 29$$

$$\Delta x = x_2 - x_1 \\ = 29 - 35$$

$= -6 \text{ cm} \rightarrow$  Losing energy

$$Fd \cos \theta = \Delta k$$

$$W = \vec{F} \cdot \vec{d} = \Delta k$$

| if,  $k_f < k_i$

$W \rightarrow -ve$

$$W = \vec{F} \cdot \vec{d} = k_f - k_i = \Delta k$$

$$\textcircled{i} \quad v_i = 3 \text{ ms}^{-1}$$

$$v_f = -2 \text{ ms}^{-1}$$

$$\frac{1}{2} m v_f^2 + \frac{1}{2} m v_i^2 = W$$

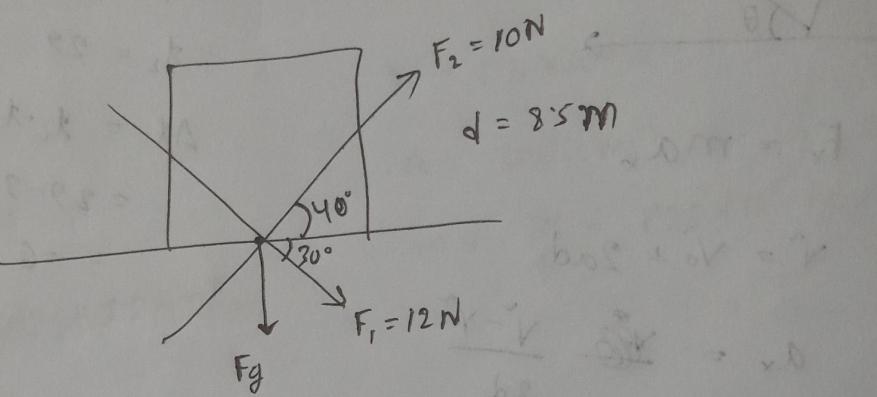
$$\frac{1}{2} m (4 - 9) = -W$$

$$\textcircled{ii} \quad v_i = 5 \text{ ms}^{-1}$$

$$v_f = 2 \text{ ms}^{-1}$$

$$\frac{1}{2} m (2^2 - 5^2)$$

$$= 0$$



$$W = \vec{F} \cdot \vec{d}$$

$$W_1 = \vec{F}_1 \cdot \vec{d}$$

$$= F_1 d \cos 30^\circ$$

$$= 12 \times 8.5 \times \cos 30^\circ$$

$$= 88.3 \text{ J}$$

$$W_2 = \vec{F}_2 \cdot \vec{d}$$

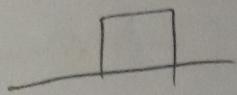
$$= F_2 d \cos 40^\circ = 6.7$$

$$= 65.12 \text{ J}$$

$$W = W_1 + W_2 = 88.3 + 6.7 = W$$

$$= 153.4 \text{ J}$$

$$\bar{A} \cdot \bar{B} = A_x B_x + A_y B_y + A_z B_z$$



$$\vec{d} = -3m\hat{i}$$

$$\vec{F} = 2N\hat{i} - 6N\hat{j}$$

$$k_i = 10j$$

$$w = -6j$$

$$k_f = ?$$

$$w = k_f - k_i$$

$$k_f = w + k_i$$

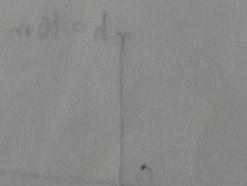
$$w = \vec{F} \cdot \vec{d}$$

$$= -6 + 10$$

$$\therefore k_f = 4j$$

$$deg(d) = w$$

$$0.1 \times 3.8 \times 10^{-3}$$



$$(8C - 2)$$

$$0.1 \times 10^{-3}$$

length (m) width (m)

$$1.0 \times 10^{-3}$$

CHW

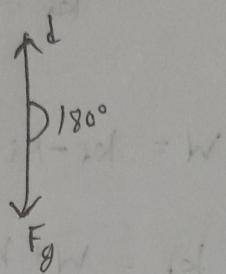
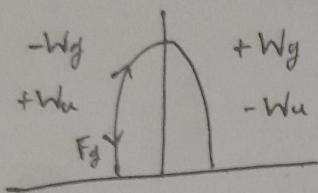
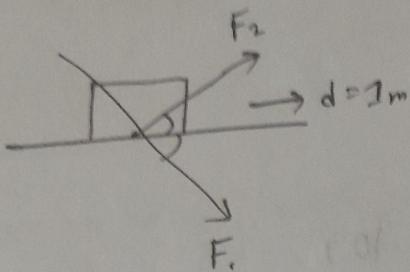
$$1.0 \times 10^{-3}$$

CHW

$$1.0 \times 10^{-3} \times \frac{1}{10} \times \frac{1}{10} = 10^{-6}$$

$$10^{-6}$$

L-9 | 02. 11. 2022 /

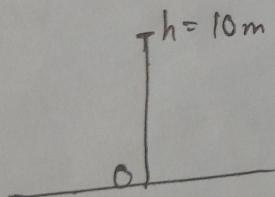


$$\begin{aligned}\downarrow W_g &= \bar{F}_g \cdot \bar{d} \\ &= \bar{F}_g d \cos 180^\circ \\ &= -mgd\end{aligned}$$

$$\uparrow W_g = -mgh$$

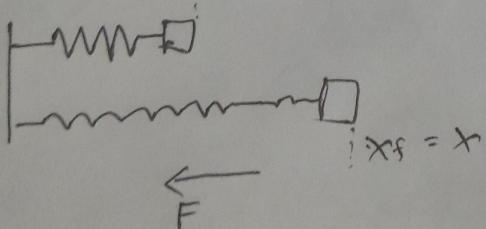
$$\begin{aligned}\downarrow W_g &= \bar{F}_g \cdot \bar{d} \\ &= \bar{F}_g d \cos 0^\circ\end{aligned}$$

$$\downarrow W_g = mgh$$

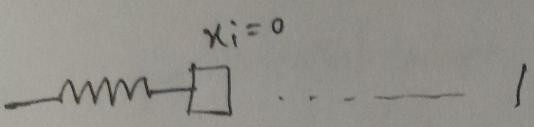


$$\begin{aligned}W_g &= -mgh \\ &= -9.8 \times 1.0 \times 10 \\ &= -98 j\end{aligned}$$

$$x_1 = 0$$



$$\begin{aligned}F &\propto -x \quad \text{Spring Constant} \\ F &= -kx \\ k &= \frac{F}{x} = \frac{N}{m} = N\text{m}^{-1}\end{aligned}$$

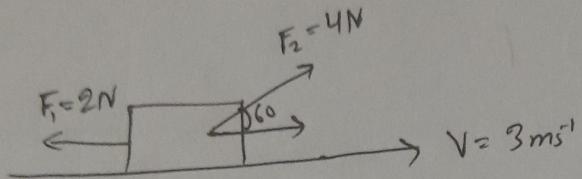


$$\begin{aligned}
 \int dw &= \int_{x_i}^{x_f} \vec{F} \cdot d\vec{x} = \int_{x_i}^{x_f} -F dx = - \int_{x_i}^{x_f} kx dx \\
 &= -k \int_{x_i}^{x_f} x dx = -k \left[ \frac{x^2}{2} \right]_{x_i}^{x_f} \\
 &= -k \left[ \frac{x_f^2}{2} - \frac{x_i^2}{2} \right] \\
 &= -k \frac{x_f^2}{2} \\
 \boxed{\uparrow W_g = -mgh} \quad w_s &= -\frac{1}{2} k x_i^2
 \end{aligned}$$

$$P = \frac{w}{t} = \frac{j}{rec} = \text{watt}$$

$$\begin{aligned}
 P &= \frac{dw}{dt} = \frac{\vec{F} \cdot d\vec{x}}{dt} = \frac{F dx \cos\theta}{dt} \\
 &= F \cos\theta \frac{dx}{dt} \\
 &= F \cos\theta V
 \end{aligned}$$

$$P = \vec{F} \cdot \vec{v}$$



$$P_1 = \vec{F}_1 \cdot \vec{V} = F \cdot V \cos 180^\circ$$

$$= 2 \cdot 3 \cdot (-1) = -6 \text{ W}$$

System is loosing energy per unit second

$$P_2 = \vec{F}_2 \cdot \vec{V} = F \cdot V \cos 60^\circ$$

$$= 4 \cdot 3 \cdot \frac{1}{2}$$

$$= 6 \text{ W}$$

$$P = P_1 + P_2 = -6 + 6 = 0 \text{ W}$$

$$\text{Heat} = \frac{C}{m} = \frac{W}{k} = 9$$

$$\frac{8.603 \times kT}{h} = \frac{3kT}{h} = \frac{W}{k} = 9$$

$$\frac{8.603}{h} \times kT =$$

$$V \times kT =$$

$$V \cdot T = 9$$

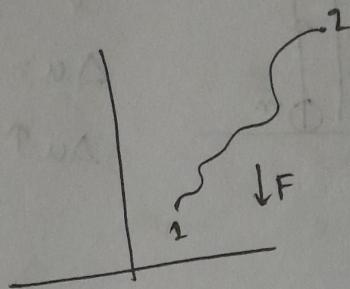
↪ Potential Energy

$$\Delta U = -W$$

$$W = \Delta k$$

$$E = k + U$$

↪ Mechanical Energy



$$W = \int_1^2 dw$$

$$= \int_1^2 \vec{F} \cdot \vec{dy}$$

$$= \int_1^2 F dy \cos 180^\circ$$

$$= - \int_1^2 F dy$$

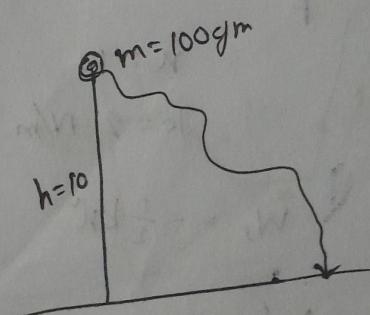
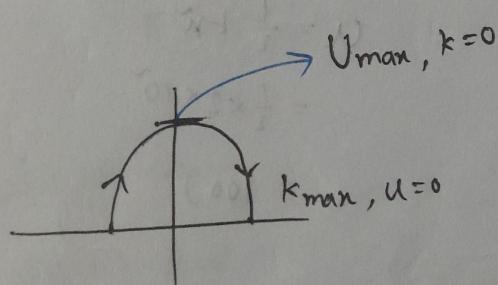
$$= -mg \int_1^2 dy$$

$$= -mgh$$

$$= -mg[y_2 - y_1]$$

$$k_1 + U_1 = k_2 + U_2$$

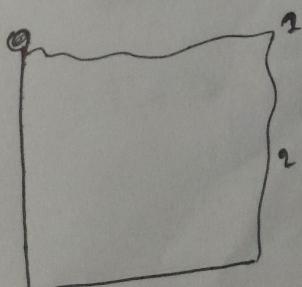
$$E_1 = E_2$$



$$W_g = mgh$$

$$= 0.1 \times 9.8 \times 10$$

$$= 9.8 J$$

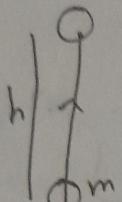


$$W_{g1} = \vec{F} \cdot \vec{d} = F \cdot d \cos 90^\circ = 0$$

$$W_{g2} = \vec{F} \cdot \vec{d} = F_g d \cos 0^\circ = 9.8 J$$

$$\therefore W_g = W_{g1} + W_{g2} = 9.8 J$$

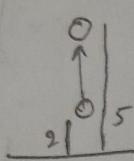
(\*)



$$Wg = mgh$$

$$\Delta u = -W$$

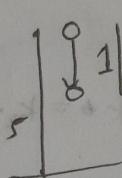
$$\begin{aligned}\Delta u \uparrow &= -(-mgh) \\ &= mgh\end{aligned}$$



$$u = mgh$$

$$= 0.5 \times 9.8 \times 2$$

$$= \dots$$



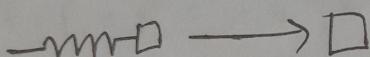
$$u = -mgh$$

$$\begin{aligned}u &= -0.5 \times 9.8 \times 1 \\ &= -4.7 i\end{aligned}$$

$\boxed{u_{initial} = , u_{final}}$

$\boxed{u_i = , f}$

(\*)



$$k = 10$$

$$F = 2 \text{ N/m}$$

$$W_s = -\frac{1}{2} k \tilde{x}$$

$$u = \frac{1}{2} k \tilde{x}$$

$$= \frac{1}{2} \times 2 \times 10$$

$$= 100 j$$

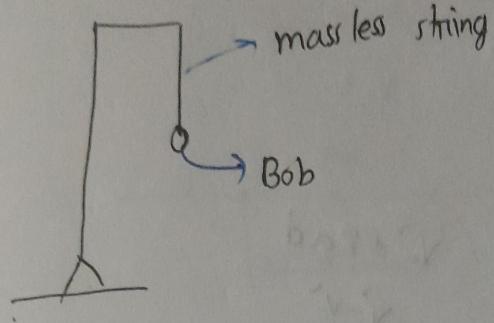
$$\Delta u = -W$$

$$= -\left(-\frac{1}{2} k \tilde{x}\right)$$

$$\Delta u = \frac{1}{2} k \tilde{x}$$

$$(100 \times 0.5) = 50 \text{ J} = W$$

$i \cdot s \cdot e = m \cdot v^2 + m \cdot g \cdot h = \frac{1}{2} m v^2 + m g h$



$$E = u + k = 5 \text{ J ul}$$

$$k = 0$$

$$h_{\text{man}} =$$

$$u = mgh = 5$$

$$\begin{aligned} h &= 0 \\ k &= mgh = 5 \\ u &= 0 \\ \text{calculate } v' \\ E &= k = \frac{1}{2} mv'^2 \end{aligned}$$

$$k = u = 5 \text{ J ul}$$

①  $E = 5 \text{ J}$

$$m = 100 \text{ g}$$

$$E = k = \frac{1}{2} mv^2$$

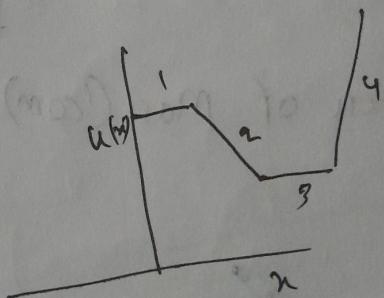
②  $\Delta u = -W$

$$du = -dW$$

$$du = -F dx$$

$$F = -\frac{du}{dx}$$

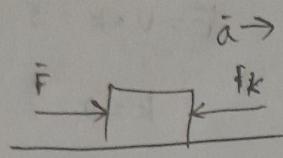
Slope



$$F_4 > F_2 > F_1 = F_3$$

L-11 / 09.11.2022 /

$$E_{mec} = U + K$$



$$v^2 = v_0^2 + 2ad$$

$$a = \frac{v^2 - v_0^2}{2d}$$

$$F_{net} = ma$$

$$F - f_k = ma$$

$$F - f_k = m \left( \frac{v^2 - v_0^2}{2d} \right)$$

$$Fd - f_k d = \frac{1}{2} mv^2 - \frac{1}{2} mv_0^2$$

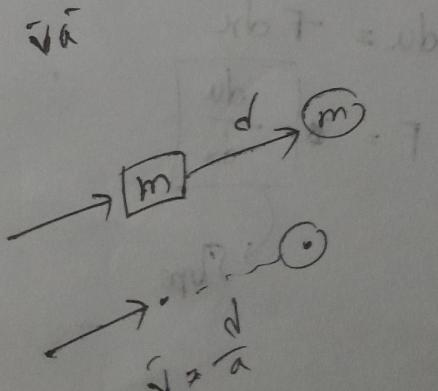
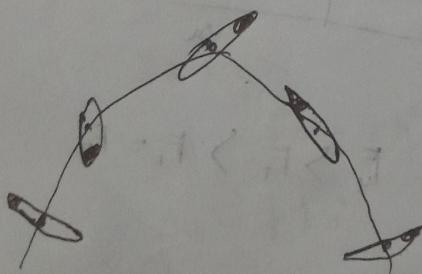
$$Fd - f_k d = E_{mec}$$

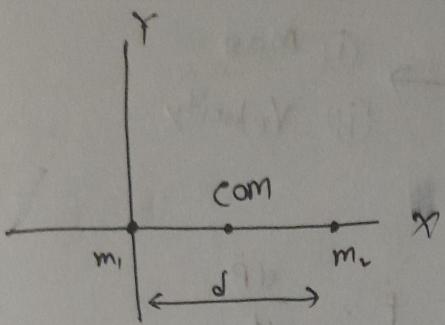
$v_0$   $v$   $\rightarrow$   
 $U + K$

$$Fd = f_k d + E_{mec}$$

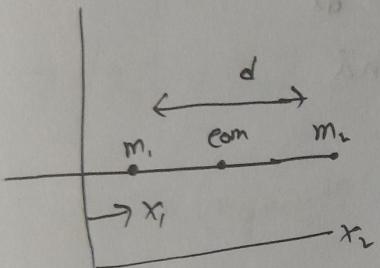
$$E = E_{th} + E_{mec} + E_{int}$$

### \* Center of Mass (com)





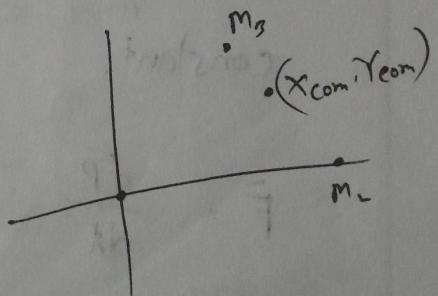
$$x_{\text{com}} = \frac{m_2 d}{m_1 + m_2}$$



$$x_{\text{com}} = \frac{m_1 x_1 + m_2 x_2}{m_1 + m_2}$$

$$\sum x_{\text{com}} = \frac{1}{m} \sum_{i=1}^{i=n} m_i x_i$$

Particle	Mass	$x_{\text{com}}$	$y_{\text{com}}$
1	1.2	0	0
2	2.5	140	0
3	3.4	70	12



$$x_{\text{com}} = \frac{m_1 x_1 + m_2 x_2 + m_3 x_3}{m_1 + m_2 + m_3} = \frac{0 + 2.5 \times 140 + 3.4 \times 70}{1.2 + 2.5 + 3.4} = 83 \text{ cm}$$

$$y_{\text{com}} = \frac{m_1 y_1 + m_2 y_2 + m_3 y_3}{m_1 + m_2 + m_3} = \frac{0 + 0 + 3.4 \times 120}{1.2 + 2.5 + 3.4} = 58 \text{ cm}$$

$$\therefore \text{COM} = (83, 58)$$

⊗ Linear momentum,  $\bar{P}$  → ① Mass  
② Velocity

$$\bar{P} = m\bar{v}$$

Force

$$F = \boxed{\frac{d\bar{P}}{dt}} \rightarrow \text{slope}$$

$$\bar{F} = \frac{d\bar{P}}{dt}$$

$$= \frac{d(m\bar{v})}{dt}$$

$$= m \frac{d\bar{v}}{dt}$$

$$F_{\text{net}} = 0$$

$$\bar{F} = ma$$

$$\boxed{\frac{d\bar{P}}{dt} = 0}$$

$\bar{P} = \text{constant}$

$$P_i = P_f$$

∴ If there is no net force, the momentum will be constant.

$$\bar{F} = \frac{d\bar{P}}{dt}$$

$$d\bar{P} = \bar{F} dt$$

$$\int_{P_i}^{P_f} d\bar{P} = \int_{t_1}^{t_2} \bar{F} dt$$

$$\boxed{\Delta \bar{P} = \bar{J}}$$

Linear momentum impulse theorem

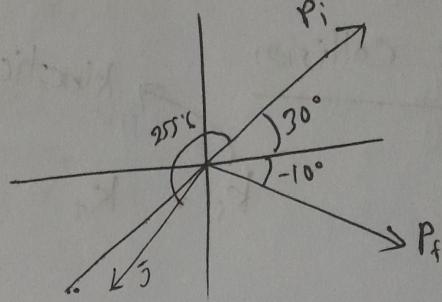
impulse

impulse

$$\vec{J} = \int_{\text{st}}^{\text{st}} \vec{F} \cdot dt$$

$$\Delta P = \vec{J}$$

$$\vec{P}_f - \vec{P}_i = \vec{J}$$



$$m = 80 \text{ kg}$$

$$\vec{J} = J_x \hat{i} + J_y \hat{j}$$

$$v_i = 70 \text{ ms}^{-1}$$

$$= -910 \text{ (kgms}^{-1}\text{)} \hat{i} - 3500 \text{ (kgms}^{-1}\text{)} \hat{j} \quad v_f = 50 \text{ ms}^{-1}$$

$$J_x = P_{fx} - P_{ix}$$

$$|J_x| = \sqrt{J_x^2 + J_y^2}$$

$$= mv_{fx} - mv_{ix}$$

$$= 3600 \text{ kgms}^{-1}$$

$$= mv_f \cos(-10) - mv_i \cos 30^\circ$$

$$\theta = \tan^{-1} \left( \frac{J_y}{J_x} \right)$$

$$= -910 \text{ kgms}^{-1}$$

$$= 75^\circ \text{ C}$$

$$J_y = P_{fy} - P_{iy}$$

$$\theta = 180^\circ + 75^\circ \text{ C}$$

$$= mv_{fy} - mv_{iy}$$

$$= 255^\circ \text{ C}$$

$$= mv_f \sin(-10) - mv_i \sin 30^\circ$$

⊗  $J : F_{\text{avg}} \Delta t$

$$= -3500 \text{ kgms}^{-1}$$

$$\Delta t = 16 \text{ ms}$$

$$\therefore F_{\text{avg}} = \frac{J}{\Delta t}$$