## Length of the union of segments

Given n segments on a line, each described by a pair of coordinates  $(a_{i1}, a_{i2})$ . We have to find the length of their union.

The following algorithm was proposed by Klee in 1977. It works in  $O(n \log n)$  and has been proven to be the asymptotically optimal.

## Solution

We store in an array x the endpoints of all the segments sorted by their values. And additionally we store whether it is a left end or a right end of a segment. Now we iterate over the array, keeping a counter c of currently opened segments. Whenever the current element is a left end, we increase this counter, and otherwise we decrease it. To compute the answer, we take the length between the last to x values  $x_i - x_{i-1}$ , whenever we come to a new coordinate, and there is currently at least one segment is open.

## **Implementation**

```
int length_union(const vector<pair<int, int>> &a) {
int n = a.size();
vector<pair<int, bool>> x(n*2);
for (int i = 0; i < n; i++) {
    x[i*2] = \{a[i].first, false\};
    x[i*2+1] = \{a[i].second, true\};
sort(x.begin(), x.end());
int result = 0;
int c = 0;
 for (int i = 0; i < n * 2; i++) {
     if (i > 0 \&\& x[i].first > x[i-1].first \&\& c > 0)
        result += x[i].first - x[i-1].first;
    if (x[i].second)
        C--;
    else
        C++;
 return result;
```

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