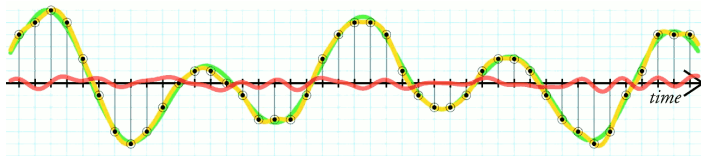


COMS20011 – Data-Driven Computer Science



February 2021

Majid Mirmehdi, Rui Ponte Costa & Dima Damen

Lecture Video #3

This lecture



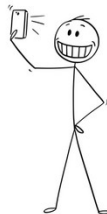
Analog Signal



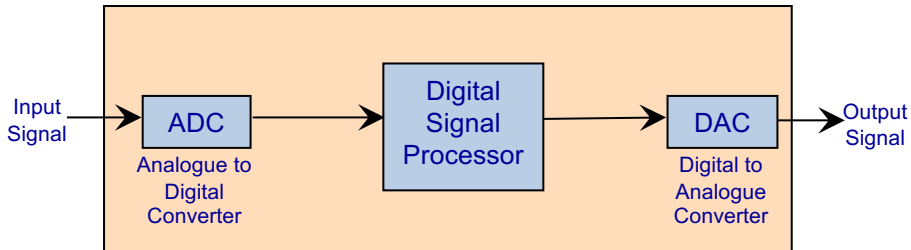
Digital Signal

- **Data acquisition**
- Data characteristics: distance measures
- Data characteristics: summary statistics [*reminder*]
- Data normalisation and outliers

Data Acquisition – Example data journey



<https://www.vectortock.com/>



Data Acquisition - Analogue to Digital Conversion

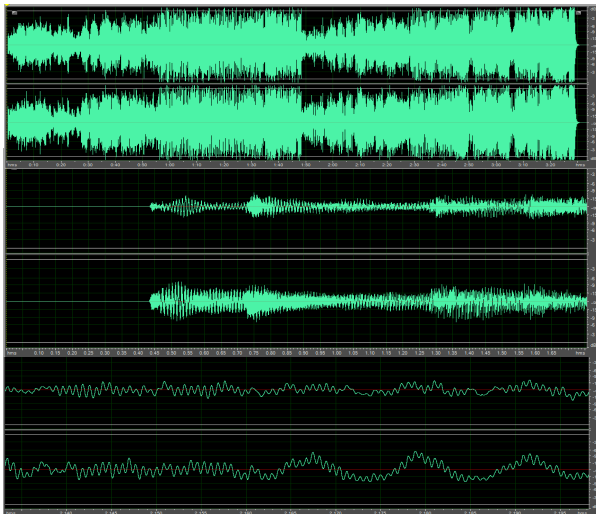
Analogue to Digital conversion involves *Sampling & Quantisation*

e.g. a 1D Audio Signal

low zoom

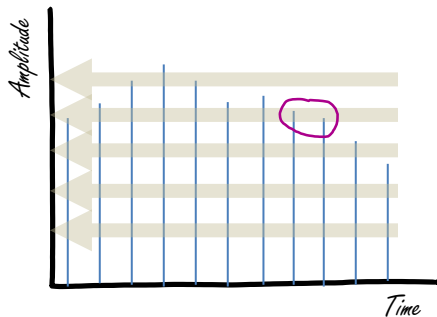
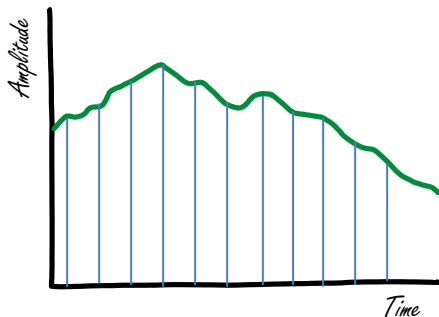
medium zoom

large zoom



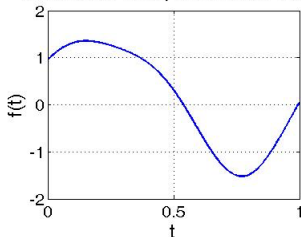
Data Acquisition - Analogue to Digital Conversion

Analogue to Digital conversion involves *Sampling* & *Quantisation*

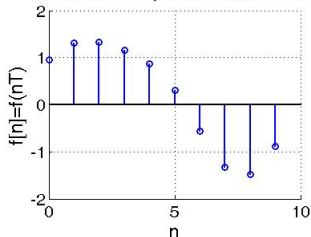


Sample and Quantise

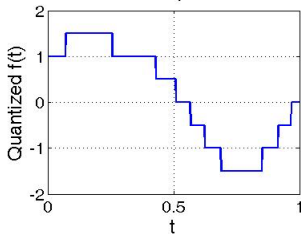
Continuous Time, Continuous Value



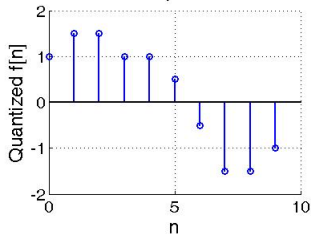
Discrete Time, Continuous Value



Continuous Time, Discrete Value

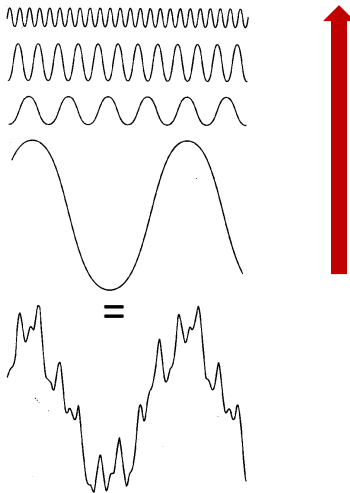


Discrete Time, Discrete Value



Nyquist-Shannon Sampling Theory

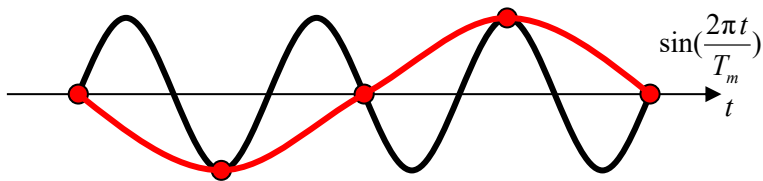
"An analogue signal containing components up to some maximum frequency u (Hz) may be completely reconstructed by regularly spread samples, provided the sampling rate is at least $2u$ samples per second"



Nyquist-Shannon Sampling Theory

"An analogue signal containing components up to some maximum frequency u (Hz) may be completely reconstructed by regularly spread samples, provided the sampling rate is at least $2u$ samples per second"

Also referred to as the Nyquist-Shannon criterion: sampling rate s should be at least twice the highest spatial frequency u .



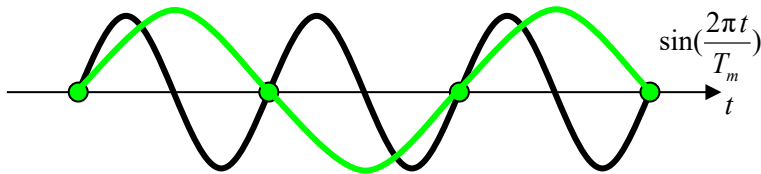
$$\text{sampling period } T_m \leq \frac{1}{2u}$$

$$\text{equivalent to sampling rate } s \geq 2u$$

Nyquist-Shannon Sampling Theory

"An analogue signal containing components up to some maximum frequency u (Hz) may be completely reconstructed by regularly spread samples, provided the sampling rate is at least $2u$ samples per second"

Also referred to as the Nyquist-Shannon criterion: sampling rate s should be at least twice the highest spatial frequency u .



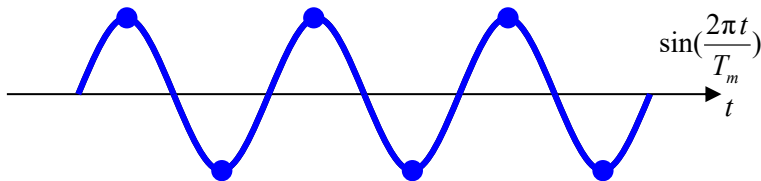
$$\text{sampling period } T_m \leq \frac{1}{2u}$$

$$\text{equivalent to sampling rate } s \geq 2u$$

Nyquist-Shannon Sampling Theory

"An analogue signal containing components up to some maximum frequency u (Hz) may be completely reconstructed by regularly spread samples, provided the sampling rate is at least $2u$ samples per second"

Also referred to as the Nyquist-Shannon criterion: sampling rate s should be at least twice the highest spatial frequency u .



$$\text{sampling period } T_m \leq \frac{1}{2u}$$

$$\text{equivalent to sampling rate } s \geq 2u$$

Data Acquisition - Analogue to Digital Conversion

Examples of sampling and quantisation of standard audio formats:

- Speech (e.g. phone call)
 - Sampling: 8 KHz samples
 - Quantisation: 8 bits / sample
- Audio CD
 - Sampling: 44 KHz samples
 - Quantisation: 16 bits / sample
 - Stereo (2 channels)

Higher sampling and quantisation levels achieves better signal quality, but at the expense of larger memory and storage.

Data Acquisition - Analogue to Digital Conversion

Examples of sampling and quantisation of Images - Multi-Dimensional:

- Sampling: Resolution in digital photography
- Quantisation: Representation of each pixel in the image
 - 8 Mega Pixel Camera: 3264 x 2448 pixels
 - Colour images: 3 channels: Red, Green, Blue (8 bits per colour)
 - Greyscale images: 1 channel: intensity = $aR+bG+cB$ where $a+b+c=1.0$
 - Binary images: Black/White 1 bit per pixel

Sampling – visual example

The effect of sparser sampling...is **ALIASING**



256x256



64x64



32x32

Anti-aliasing is achieved by filtering to remove frequencies above the Nyquist limit.

Quantisation – visual example

This results from representing a continuously varying function $f(x)$ with a discrete one using quantisation levels



16 levels



6 levels



2 levels

Next lecture video



Analog Signal



Digital Signal

- Data acquisition
- **Data characteristics: distance measures**
- Data characteristics: summary statistics [*reminder*]
- Data normalisation and outliers