

Erroneous Non blocking Atomic Commitment Protocol (ACP-NB)

The mistake is to deliver a broadcast message locally *before* it has been forwarded to other participants.

This protocol does not satisfy the consistency property *AC1*

EXTENDS *ACP-SB*

Participants type is extended with a “forward” variable.

Coordinator type is unchanged.

$$\begin{aligned} \text{TypeInvParticipantNB} &\triangleq \text{participant} \in [\\ &\quad \text{participants} \rightarrow [\\ &\quad \quad \text{vote} : \{\text{yes, no}\}, \\ &\quad \quad \text{alive} : \text{BOOLEAN}, \\ &\quad \quad \text{decision} : \{\text{undecided, commit, abort}\}, \\ &\quad \quad \text{faulty} : \text{BOOLEAN}, \\ &\quad \quad \text{voteSent} : \text{BOOLEAN}, \\ &\quad \quad \text{forward} : [\text{participants} \rightarrow \{\text{notsent, commit, abort}\}] \\ &\quad] \\ &] \end{aligned}$$

$$\text{TypeInvNB} \triangleq \text{TypeInvParticipantNB} \wedge \text{TypeInvCoordinator}$$

Initially, participants have not forwarded anything yet

$$\begin{aligned} \text{InitParticipantNB} &\triangleq \text{participant} \in [\\ &\quad \text{participants} \rightarrow [\\ &\quad \quad \text{vote} : \{\text{yes, no}\}, \\ &\quad \quad \text{alive} : \{\text{TRUE}\}, \\ &\quad \quad \text{decision} : \{\text{undecided}\}, \\ &\quad \quad \text{faulty} : \{\text{FALSE}\}, \\ &\quad \quad \text{voteSent} : \{\text{FALSE}\}, \\ &\quad \quad \text{forward} : [\text{participants} \rightarrow \{\text{notsent}\}] \\ &\quad] \\ &] \end{aligned}$$

$$\text{InitNB} \triangleq \text{InitParticipantNB} \wedge \text{InitCoordinator}$$

Participant statements that realize a better broadcast

forward(*i, j*): forwarding of the predecision from participant *i* to participant *j*

IF

participant *i* is alive

participant *i* has received a decision and has decided (it shouldn't have decided yet)

participant *i* has not yet forwarded this decision to participant *j*

THEN

participant *i* forwards the decision to participant *j*

$$\begin{aligned} \text{forward}(i, j) &\triangleq \wedge i \neq j \\ &\quad \wedge \text{participant}[i].\text{alive} \\ &\quad \wedge \text{participant}[i].\text{decision} \neq \text{notsent} \\ &\quad \wedge \text{participant}[i].\text{forward}[j] = \text{notsent} \\ &\quad \wedge \text{participant}' = [\text{participant EXCEPT } !i = \\ &\quad \quad [\text{@ EXCEPT } !.\text{forward} = \\ &\quad \quad \quad [\text{@ EXCEPT } !j = \text{participant}[i].\text{decision}] \\ &\quad \quad] \\ &\quad] \end{aligned}$$

\wedge UNCHANGED $\langle \text{coordinator} \rangle$

$\text{decideOnForward}(i, j)$: participant i receives decision from participant j

IF

participant i is alive

participant i has yet to receive a decision

participant j has forwarded its decision to participant i

THEN

participant i decides in accordance with participant j 's decision (it should only predecide)

$$\begin{aligned} \text{decideOnForward}(i, j) \triangleq & \quad \wedge i \neq j \\ & \wedge \text{participant}[i].\text{alive} \\ & \wedge \text{participant}[i].\text{decision} = \text{undecided} \\ & \wedge \text{participant}[j].\text{forward}[i] \neq \text{notsent} \\ & \wedge \text{participant}' = [\text{participant EXCEPT } !i = \\ & \quad @ \text{EXCEPT } !.\text{decision} = \text{participant}[j].\text{forward}[i]] \\ & \quad] \\ & \wedge \text{UNCHANGED } \langle \text{coordinator} \rangle \end{aligned}$$

$\text{abortOnTimeout}(i)$: conditions for a timeout are simulated

IF

participant is alive and undecided and coordinator is not alive

coordinator died before sending decision to all participants who are alive

all dead participants died before forwarding decision to a participant who is alive

THEN

decide abort

$$\begin{aligned} \text{abortOnTimeout}(i) \triangleq & \quad \wedge \text{participant}[i].\text{alive} \\ & \wedge \text{participant}[i].\text{decision} = \text{undecided} \\ & \wedge \neg \text{coordinator}. \text{alive} \\ & \wedge \forall j \in \text{participants} : \text{participant}[j].\text{alive} \Rightarrow \text{coordinator}. \text{broadcast}[j] = \text{notsent} \\ & \wedge \forall j, k \in \text{participants} : \neg \text{participant}[j].\text{alive} \wedge \text{participant}[k].\text{alive} \Rightarrow \text{participant}[j].\text{forward}[k] = \text{notsent} \\ & \wedge \text{participant}' = [\text{participant EXCEPT } !i = @ \text{EXCEPT } !.\text{decision} = \text{abort}]] \\ & \wedge \text{UNCHANGED } \langle \text{coordinator} \rangle \end{aligned}$$

FOR N PARTICIPANTS

$$\begin{aligned} \text{parProgNB}(i, j) \triangleq & \quad \vee \text{parProg}(i) \\ & \vee \text{forward}(i, j) \\ & \vee \text{decideOnForward}(i, j) \\ & \vee \text{abortOnTimeout}(i) \end{aligned}$$

$$\text{parProgNNB} \triangleq \exists i, j \in \text{participants} : \text{parDie}(i) \vee \text{parProgNB}(i, j)$$

$$\text{progNNB} \triangleq \text{parProgNNB} \vee \text{coordProgN}$$

$$\begin{aligned} \text{fairnessNB} \triangleq & \quad \wedge \forall i \in \text{participants} : \text{WF}_{\langle \text{coordinator}, \text{participant} \rangle}(\exists j \in \text{participants} : \text{parProgNB}(i, j)) \\ & \wedge \text{WF}_{\langle \text{coordinator}, \text{participant} \rangle}(\text{coordProgB}) \end{aligned}$$

$$\text{SpecNB} \triangleq \text{InitNB} \wedge \square[\text{progNNB}]_{\langle \text{coordinator}, \text{participant} \rangle} \wedge \text{fairnessNB}$$