

11.7)

a) $\frac{y: \text{int} \quad (\Gamma - \text{succ})}{\text{succ}(y): \text{int} \quad z: \text{int} \quad (\Gamma - \text{if})} (+1)$
if x then $\text{succ}(y)$ else $z: \text{int}$

$\Gamma := \{x: \text{Bool}, y: \text{int}, z: \text{int}\}$

b) $\frac{x: \text{int} \quad (\Gamma - \text{is zero})}{\frac{x: \text{int} \vdash \text{is zero } x: \text{Bool}}{\vdash (\lambda x: \text{int} \text{ is zero } x): \text{int} \rightarrow \text{Bool}}} (\Gamma - \text{Abs})$

$= \text{int} \rightarrow \text{Bool}$

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N.2)

$$\frac{(x: \text{Bool} \rightarrow \text{Bool}) \in \{x: \text{Bool} \rightarrow \text{Bool} \mid y: \text{Bool}\}}{(T\text{-Var})} \frac{(y: \text{Bool}) \in \{x: \text{Bool} \rightarrow \text{Bool} \mid y: \text{Bool}\}}{(T\text{-Var})}$$

$$\frac{x: \text{Bool} \rightarrow \text{Bool}, y: \text{Bool} \vdash x: \text{Bool} \rightarrow \text{Bool} \quad x: \text{Bool} \rightarrow \text{Bool}, y: \text{Bool} \vdash y: \text{Bool}}{(T\text{-App})}$$

$$\frac{x: \text{Bool} \rightarrow \text{Bool}, y: \text{Bool} \vdash xy: \text{Bool}}{(T\text{-Abs})}$$

$$\frac{x: \text{Bool} \rightarrow \text{Bool} \vdash \lambda y: \text{Bool}. xy: \text{Bool} \rightarrow \text{Bool}}{(T\text{-Abs})}$$

$$\vdash \lambda x: \text{Bool} \rightarrow \text{Bool}, \lambda y: \text{Bool}. xy: (\text{Bool} \rightarrow \text{Bool}) \rightarrow \text{Bool} \rightarrow \text{Bool} \quad -1$$

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