

11.7)

a)  $\frac{\frac{y:\text{int}}{\text{succ}(y):\text{int}} \quad (T\text{-succ}) \quad z:\text{int} \quad (T\text{-I})}{\text{if } x \text{ then } \text{succ}(y) \text{ else } z:\text{int}}$

$\Gamma := \{x:\text{Bool}, y:\text{int}, z:\text{int}\}$

b)  $\frac{\frac{x:\text{int}}{\Gamma \vdash \text{is zero } x:\text{Bool}} \quad (T\text{-is zero})}{\Gamma \vdash (\lambda x:\text{int} \text{ is zero } x):\text{int} \rightarrow \text{Bool}} \quad (T\text{-Abs})$

$= \text{int} \rightarrow \text{Bool}$

N.2)

$$\frac{(x: \text{Bool} \rightarrow \text{Bool}) \in \{x: \text{Bool} \rightarrow \text{Bool} \mid y: \text{Bool}\}}{(T\text{-Var})} \frac{(y: \text{Bool}) \in \{x: \text{Bool} \rightarrow \text{Bool} \mid y: \text{Bool}\}}{(T\text{-Var})}$$

$$\frac{x: \text{Bool} \rightarrow \text{Bool}, y: \text{Bool} \vdash x: \text{Bool} \rightarrow \text{Bool} \quad x: \text{Bool} \rightarrow \text{Bool}, y: \text{Bool} \vdash y: \text{Bool}}{(T\text{-App})}$$

$$\frac{x: \text{Bool} \rightarrow \text{Bool}, y: \text{Bool} \vdash xy: \text{Bool}}{(T\text{-Abs})}$$

$$\frac{x: \text{Bool} \rightarrow \text{Bool} \vdash \lambda y: \text{Bool} \ xy: \text{Bool} \rightarrow \text{Bool}}{(T\text{-Abs})}$$

$$\vdash \lambda x: \text{Bool} \rightarrow \text{Bool}, \lambda y: \text{Bool} \ xy: \text{Bool} \rightarrow \text{Bool} \rightarrow \text{Bool} \rightarrow \text{Bool}$$