

Chapter 1: The Role of Algorithms in Computing

《算法分析与设计》课程组
重庆大学计算机学院

Algorithm Design & Analysis Introduction to Algorithm

《算法分析与设计》 课程介绍

- **教材** 《Introduction to Algorithms》
- **作者**: Thomas H. Cormen, Charles E. Leiserson, Ronald L. Rivest, Clifford Stein.
- **出版社**: MIT Press
- **版本**: Third Edition, 2009
- **学习目标**: 掌握经典算法的基本原理, 懂得如何寻求解决问题的方法
- **学习方法**: 多读、多练习、勤思考、勤动手

《算法分析与设计》课程成绩评价方式

- **平时成绩 占总成绩45%**

PTA在线答题

纸质版作业

课堂小测试

- **期末考试（闭卷） 占总成绩55%**

The Role of Algorithms in Computing

OUTLINE

- **1.1 What are algorithms?**
- **1.2 Why is the study of algorithms worthwhile?**
- **1.3 Algorithms as a technology: How?**
- **1.4 Textbook selected: What & Why?**
- **1.5 Exercise & Mark**

1.1 What are algorithm

- **What are algorithm?**
 - Definition{ computational procedure, computational problem, Input, Output }
 - Examples with instance — sorting problem
 - Requirement: correct, precise description

Definition of algorithm

- Definition:
 - An *algorithm* is any **well-defined computational procedure** that
 - takes some value, or set of values, as *input* and
 - produces some value, or set of values, as *output*.
- An algorithm is thus a **sequence of computational steps** that transform the input into the output.

Relationship: algorithm and problem

- Problem:
 - The statement of the problem specifies the desired **input/output relationship**.
- Algorithm:
 - The algorithm describes a **specific computational procedure** for achieving that input/output relationship.
- Relationship:
 - We can also view an algorithm as a tool for solving a **well-specified computational problem**

Problem description: sorting problem

- Sorting problem:
 - **Input:** A sequence of n numbers a_1, a_2, \dots, a_n
 - **Output:** A permutation (reordering) a'_1, a'_2, \dots, a'_n of the input sequence such that
$$a'_1 \leq a'_2 \leq \dots \leq a'_n$$
- An **instance** of the sorting problem
 - Input: 31, 41, 59, 26, 41, 58 or $\langle 8 \ 2 \ 4 \ 9 \ 3 \ 6 \rangle$
 - Output: 26, 31, 41, 41, 58, 59
- Notation:
 - Sorting is a fundamental operation in CS
 - A large number of good sorting algorithms have been D&R

Algorithm description

- Specification:
 - Natural language, computer program, hardware design
 - An algorithm can be specified in English | Chinese, as a computer program, or even as a hardware design.
- Requirement
 - Precise description
 - The only requirement is that the specification must provide a **precise description** of the computational procedure to be followed.

Correctness of algorithm

- Correctness:
 - An algorithm is said to be *correct* if, **for every input instance**, it **halts with the correct output**.
- Incorrect algorithm
 - An incorrect algorithm might **not halt at all on some input instances**, or it **might halt** with an answer other than the desired one.
 - Incorrect algorithms can sometimes be useful, if their error rate can be controlled.
 - Example ?

1.2 Why is the study of algorithms w...?

- **Why is the study of algorithms worthwhile?**
 - **What is the role of algorithms?**
 - **What kinds of problems are solved by algorithms?**
 - The Human Genome Project: 100,000 genes in human DNA, sequences of the 3 billion chemical base pairs
 - Internet: finding good routes.
 - Electronic commerce: Public-key cryptography
 - Road map: shortest path
 - Product of a sequence of n matrices $A_1 A_2 A_n$
 - Equation $ax \equiv b \pmod{n}$: integers
 - n points in the plane: find the convex hull
- Know the strengths and limitations of *data structures*
- Hard problems: NP-complete, efficient algorithm, good | best

1.3 Algorithms as a technology

- **Algorithms as a technology**
 - infinitely fast: Terminates, with the correct answer
 - not infinitely fast: **Computing time** is therefore a bounded resource, algorithms that are efficient in terms of time or space
- **Efficiency:** algorithms-T, hardware-v, Software-c
 - Algorithms for sorting: Insertion sort, Merge sort
 - $c_1=2, c_2=50;$ $T_A=c_1n^2,$ $T_B=c_2n\log n$
 - Computer: $A-v=1G,$ $B-v=1M$
 - $n=1M:$ $t_A=?$ $t_B=?$
 - $n=100M:$ $t_A=?$ $t_B=?$

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 - Computer: $A-v=1G,$ $B-v=1M$
 - $n=1M:$ $t_A=?2000s$ $t_B=?1000s$
 - $n=100M:$ $t_A=?23d$ $t_B=?1.5d$

Problem: Comparison of running times

- **Determine the largest size n** : For each function $f(n)$ and time t in the following table, determine the largest size n of a problem that can be solved in time t , assuming that the algorithm to solve the problem takes $f(n)$ microseconds

	1	1	1	1	1	1	1
	second	minute	hour	day	month	year	century
$\lg n$							
\sqrt{n}							
n							
$n \lg n$							
n^2							
n^3							
2^n							
$n!$							

1.4 Textbook selected: What & Why?

- **Textbook**

- Thomas H. [Cormen](#), Charles E. Leiserson, Ronald L. Rivest, Clifford Stein.
- [Introduction to Algorithms](#).
- 3rd Edition, the MIT Press, 2009.

- **Famous people with Classical Book in CS**

- Donald Ervin [Knuth](#), 1938.1.10-
- Donald E. Knuth. [The Art of Computer Programming](#), Volumes 1-4A, 1st edition. Addison-Wesley Professional, March 13, 2011.

1.5 Exercise & Mark

- See 《算法分析与设计》课程介绍与要求.ppt

Exercises for Chapter 1

- Exercises: 1.2-3: Find the smallest value of n ...
- Problems 1-1: Comparison of running times...


Exercises for Chapter 1

- 1. 1-3. Select a data structure that you have seen previously, and discuss its **strengths and limitations**.
- 1.1-4 How are the shortest-path and traveling-salesman problems given above **similar**? How are they **different**?
- 1.1-5 Come up with a real-world problem in which only the best solution will do. Then come up with one in which a solution that is "approximately" the best is good enough.


Exercises

- Exercises 1.2-3 What is **the smallest value of n** such that an algorithm whose running time is $100n^2$ runs faster than an algorithm whose running time is 2^n on the same machine?
- Problems 1-1: **Comparison of running times**
 - For each function $f(n)$ and time determine the largest size n of solved in time t , assuming solve the problem takes $f(n)$

	1	1	1	1	1	1	1
	second	minute	hour	day	month	year	century
$\lg n$							
\sqrt{n}							
n							
$n \lg n$							
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End of Chapter

