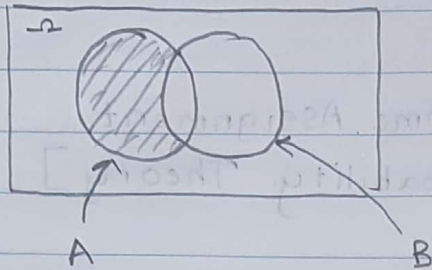
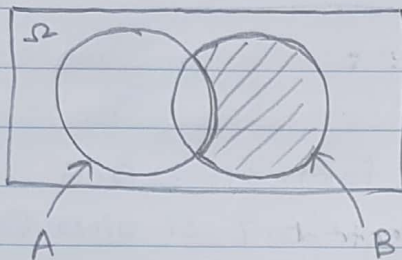


c) knows C/C++ but not ^{fortran} ~~C/C++~~?



$$\begin{aligned} A \text{ not } B &= P(A) - P(A \cap B) \\ &= 0.7 - 0.5 \\ &= 0.2 // \end{aligned}$$

D) knows fortran but not C/C++?



$$\begin{aligned} B \text{ not } A &= P(B) - P(A \cap B) \\ &= 0.6 - 0.5 \\ &= 0.1 // \end{aligned}$$

e) If someone knows fortran, what is the probability that he/she knows C/C++ too?

$$P(A|B) = \frac{P(A \cap B)}{P(B)} = \frac{0.5}{0.6} = 0.83333 //$$

f) If someone knows C/C++, what is the probability that he/she knows fortran too?

$$P(B|A) = \frac{P(A \cap B)}{P(A)} = \frac{0.5}{0.7} = 0.7142857 //$$

- 2) Among 10 laptop computers, five are good and five have defects. Unaware of this, a customer buys 6 laptops.
- a) What is the probability of exactly 2 defective laptops among them?

$P(G)$ = good laptops = 5

$P(D)$ = defects laptops = 5

No of ways to select 6 laptops

n = Total Objects to Select

k = No of Objects that Selected

$${}^n C_k = \frac{n!}{k!(n-k)!} = \frac{10!}{6! \cdot 4!} = \frac{1 \times 2 \times 3 \times 4 \times 5 \times 6 \times 7 \times 8 \times 9 \times 10}{1 \times 2 \times 3 \times 4 \times 5 \times 6 \times 1 \times 2 \times 3 \times 4} = 210$$

No of chances exactly 2 defective laptops are patches among them?

$$\begin{aligned} \left. \begin{array}{l} n = \text{Total defective laptops} \\ k = \text{No. of selection} \end{array} \right\} \Rightarrow 1^{\text{st}} \text{ selection} &= {}^n C_k = \frac{n!}{k!(n-k)!} \\ &= \frac{5!}{2! \cdot 3!} \\ &= \frac{1 \times 2 \times 3 \times 4 \times 5}{1 \times 2 \times 1 \times 2 \times 3} \\ &= 10 // \end{aligned}$$

2nd selection (Because here outputs are not replacing and without considering the order) $\Rightarrow {}^n C_k$

$${}^n C_k = \frac{n!}{k!(n-k)!} = \frac{5!}{4! \cdot 1!} = 5$$

→ 2 a) given 2 purchased laptops are defective →

$$50 * 10 = 500$$

probability of exactly 2 are defective = $\frac{50}{210}$

$$= \frac{5}{21} //$$

$$0.23809 //$$

2 b) Given that atleast 2 purchased laptops are defective,
What is the probability of that exactly 2 are defective

For one defective laptop = ${}^5C_1 * {}^5C_5 / {}^{10}C_6$

$$= \frac{5!}{1!(5-1)!} * \frac{5!}{5!} / \frac{10!}{6!(10-6)!}$$

$$\frac{1 \times 2 \times 3 \times 4 \times 5}{1 \times 1 \times 2 \times 3 \times 4} * 1 / \frac{210}{210} = \frac{55}{210} = 0.2619$$

Atleast 2 laptops defective = $0.23809 + 0.023809$

$$= 0.262 //$$

3. A problem on a multiple-choice quiz is answered correctly with probability 0.9 if a student is prepared. An unprepared student guesses between 4 possible answers, so the probability of choosing the right answer is $1/4$. Seventy-five percent of students prepare for the quiz. If Mr. X gives a correct answer to this problem, what is the chance that he did not prepare for the quiz?

$$P(C) = \text{choosing correct answer} = 0.25$$

$$P(C|P) = \text{choosing an wrong answer} = 0.25$$

$$P(P) = \text{prepared student} = 0.75$$

$$P(P') = \text{unprepared student} = 0.25$$

$$P(C|P) = 0.9$$

$$P(P'|C) = ?$$

$$P(C|P') = 0.25$$

By using total probability theorem

$$\begin{aligned} P(C) &= P(C \cap P) + P(C \cap P') \\ &= P(C|P) \cdot P(P) + P(C|P') \cdot P(P') \\ &= 0.9 \cdot 0.75 + 0.25 \cdot 0.25 \\ &= 0.675 + 0.0625 \\ &= 0.7375 // \end{aligned}$$

$$P(C|P') = \frac{P(P'|C) \cdot P(C)}{P(P')} \quad \left. \vphantom{\frac{P(P'|C) \cdot P(C)}{P(P')}} \right\} \text{by Bayes theorem}$$

$$\frac{P(C|P') \cdot P(P')}{P(C)} = P(P'|C)$$

$$\frac{0.25 \cdot 0.25}{0.7375} = P(P'|C)$$

$$P(P'|C) = 0.0847 //$$

- 4) Successful implementation of a new system is based on 3 independent modules. Module 1 works properly with probability 0.96. For modules 2 and 3, these probabilities equal 0.95 and 0.90. Compute the probability that at least one of these 03 modules fails to work properly

Module 1 works properly $P(M_1) = 0.96$

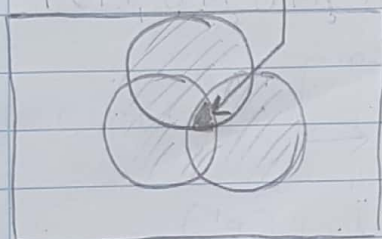
Module 2 works properly $P(M_2) = 0.95$

Module 3 works properly $P(M_3) = 0.90$

All 03 components work properly $\rightarrow 0.96 \times 0.95 \times 0.90$

Module 3 does not work properly $P(M_3') = 1 - \text{components are independent}$

$$P(M_1 \cap M_2 \cap M_3) = 0.96 \cdot 0.95 \cdot 0.90 \\ = 0.8208$$



Compliment of $P(M_1 \cap M_2 \cap M_3)$ is the probability that at least one of these 03 modules fails to work properly \Rightarrow

$$\therefore P(M_1 \cap M_2 \cap M_3)' = 1 - P(M_1 \cap M_2 \cap M_3) \\ = 1 - 0.8208 \\ = 0.1792 //$$

- 5) At a plant, 20% of all the produced parts are subject to a special electronic inspection. It is known that any produced part which was inspected electronically has no defects with probability 0.95. for a part that was not inspected electronically this probability is only 0.7. A customer receives a part and find defects in it. What is the probability that this part went through an electronic inspection

All produced parts of a plant go through electronic inspection $\Rightarrow P(I) = 0.2$

Produced part which was inspection has no defects $\Rightarrow P(N) = \underline{\hspace{2cm}}$

All $P(N|I) = 0.95$ $P(N|I') = 0.7$ $P(I|N') = ?$

From 2nd Axiom \Rightarrow

$$P(N'|I) = 1 - 0.95 = 0.05$$

$$P(N'|I') = 1 - 0.7 = 0.30$$

$$P(I) = P(I \cap N) + P(I \cap N')$$

$$P(N'|I) = \frac{P(I|N')P(N')}{P(I)}$$

We have to find N'

$$\begin{aligned} P(N') &= P(N' \cap I) + P(N' \cap I') \\ &= P(N|I) \cdot P(I) + P(N'|I') \cdot P(I') \\ &= 0.05 \times 0.2 + 0.3 \times 0.8 \\ &= 0.01 + 0.24 = 0.25 // \end{aligned}$$

$$\rightarrow \frac{P(N'|I) \times P(I)}{P(N')} = P(I|N')$$

$$\rightarrow \frac{0.05 \times 0.2}{0.25} = P(I|N')$$

$$\frac{0.01}{0.25} = 0.04 // \Rightarrow P(I|N') = 0.04 //$$

- 6) Among 18 computers in some store, six have defects. 5 randomly selected computers are bought for the university lab. Compute the probability that all five computers have no defects.

No. of computers (n) = 18

picking computer with defects = $\frac{6}{18} = \frac{1}{3}$

picking a computer without defects = $\frac{12}{18} = \frac{2}{3}$

picking up 5 non-defected computers are done with a order and without replacement. So,

No. of objects gonna select (k) = 5

probability that all 5 computers have no defects = $\left(\frac{2}{3}\right)^5$

$$= \frac{2}{3} \times \frac{2}{3} \times \frac{2}{3} \times \frac{2}{3} \times \frac{2}{3} = \frac{32}{243}$$

$$= 0.1316872 //$$

7. A computer maker receives parts from 3 suppliers, S_1 , S_2 and S_3 . ~~50%~~ 50% come from S_1 , 20% from S_2 , and 30% from S_3 . Among all the parts supplied by S_1 , 5% are defective. For S_2 and S_3 , the portion of defective parts is 3% and 6%, respectively.

a) What portion of all the parts are defective?

$$\text{parts supply by } S_1 = P(S_1) = 0.5$$

$$\text{parts supply by } S_2 = P(S_2) = 0.2$$

$$\text{parts supply by } S_3 = P(S_3) = 0.3$$

All Defective parts (D)

$$\text{parts defected by } S_1 \Rightarrow P(D|S_1) = 0.05$$

$$\text{parts defected by } S_2 \Rightarrow P(D|S_2) = 0.03$$

$$\text{parts defected by } S_3 \Rightarrow P(D|S_3) = 0.06$$

From Total probability theorem \rightarrow

$$\begin{aligned} P(D) &= P(S_1)P(D|S_1) + P(S_2)P(D|S_2) + P(S_3)P(D|S_3) \\ &= 0.5 * 0.05 + 0.2 * 0.03 + 0.3 * 0.06 \\ &= 0.025 + 0.006 + 0.018 \\ &= 0.049 // \end{aligned}$$

b) A customer complains that a certain part in her recently purchased computer is defective. What is the probability that it was supplied by S_1 ?

Apply Bayes theorem

$$(S_1|D) =$$

$$(S_1|D) = \frac{(D|S_1) \cdot S_1}{D} = \frac{0.05 * 0.5}{0.049}$$

$$= 0.51020 //$$

Atlas

8) A computer program consists of 2 blocks written independently by 2 different programmers. The first block has an error with probability 0.2. The 2nd block has an error with probability 0.3. If the program returns an error, what is the probability that there is an error in both blocks?

error returns by block 01 (E_1) = 0.2

error returns by block 02 (E_2) = 0.3

because these two programs are independent

$$P(E_1 \cap E_2) = P(E_1) \times P(E_2)$$

$$= 0.2 \times 0.3$$

$$= 0.06 //$$

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Group - 15

Name = L.V.A. kumarage

IT3011 TPSM - Take home Assignment
[Probability Theory]

01. Among employees of a certain firm, 70% know C/C++, 60% know fortran and 50% know both languages. What portion of programmers

a) does not know fortran?

$P(B)$ = employees who know fortran = 0.6

$P(A)$ = employees who know C/C++ = 0.7

$P(A')$ = employees who does not know C/C++ = ?

$P(B')$ = employees who does not know fortran = ?

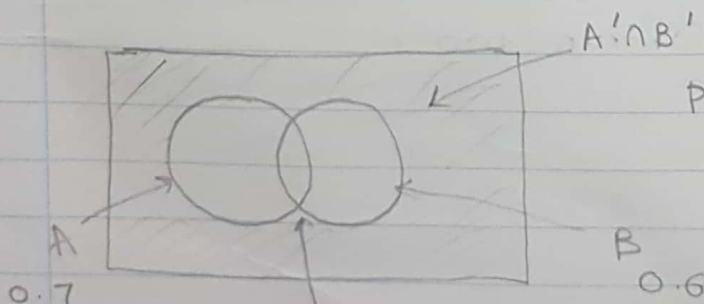
With 2nd probability axiom $\rightarrow P(B) + P(B') = 1$

$$0.6 + P(B') = 1$$

$$P(B') = 1 - 0.6$$

$$= 0.4 //$$

b) does not know fortran and does not know C/C++?



$$P(A \cup B) = P(A) + P(B) - P(A \cap B)$$

$$= 0.7 + 0.6 - 0.5$$

$$= 1.3 - 0.5$$

$$= 0.8$$

$$P(A' \cap B') = 1 - P(A \cup B)$$

$$= 1 - 0.8$$

$$= 0.2 //$$