

VeriLSM

Contents

1 Element

```
theory Element
imports
  Main
  HOL.Real
  HOL-Word.Word-Bitwise
begin
```

In this theory, we introduce the elementary datatype and data structure of Kernel

1.1 uidgid

```
type-synonym k--kernel-uid32-t = nat
type-synonym k--kernel-gid32-t = nat
type-synonym uid-t = k--kernel-uid32-t
type-synonym gid-t = k--kernel-gid32-t
typedecl uid-gid-map
record kuid-t = uval :: uid-t

record kgid-t = gval :: gid-t

type-synonym usnum = nat

record user-namespace = uid-map :: uid-gid-map
  gid-map :: uid-gid-map
  projid-map :: uid-gid-map
  count :: int
  ns-level :: int
  owner :: kuid-t
  group :: kgid-t
  u-flags :: nat
  ns-parent :: usnum
```

```

type-synonym ns = user-namespace

definition DEFAULT-OVERFLOWUID ≡ 65534
definition DEFAULT-OVERFLOWGID ≡ 65534

definition overflowuid ≡ DEFAULT-OVERFLOWUID
definition overflowgid ≡ DEFAULT-OVERFLOWGID

consts CONFIG-MULTIUSER :: bool

definition k--kuid-val :: kuid-t ⇒ uid-t
  where k--kuid-val uid' ≡ if CONFIG-MULTIUSER then (uval uid') else 0

definition k--kgid-val :: kgid-t ⇒ gid-t
  where k--kgid-val gid' ≡ if CONFIG-MULTIUSER then (gval gid') else 0

definition KUIDT-INIT value ≡ (uval = value )

definition KGIDT-INIT value ≡ (gval = value )

definition make-kuid :: user-namespace ⇒ uid-t ⇒ kuid-t
  where make-kuid from uid' ≡ KUIDT-INIT uid'

definition make-kgid :: user-namespace ⇒ gid-t ⇒ kgid-t
  where make-kgid from gid' ≡ KGIDT-INIT gid'

definition from-kuid :: ns ⇒ kuid-t ⇒ uid-t
  where from-kuid to kuid ≡ k--kuid-val kuid

definition from-kgid :: ns ⇒ kgid-t ⇒ gid-t
  where from-kgid to kgid ≡ k--kgid-val kgid

definition from-kuid-munged :: ns ⇒ kuid-t ⇒ uid-t
  where from-kuid-munged to kuid ≡
    let uid = from-kuid to kuid
    in
    if uid = 65535 - 1 then overflowuid
    else uid

definition from-kgid-munged :: ns ⇒ kgid-t ⇒ gid-t
  where from-kgid-munged to kgid ≡
    let gid = from-kgid to kgid
    in
    if gid = 65535 - 1 then overflowgid
    else gid

```

definition *kuid-has-mapping* :: *ns* \Rightarrow *kuid-t* \Rightarrow *bool*

where *kuid-has-mapping ns uid* \equiv *True*

definition *kgid-has-mapping* :: *ns* \Rightarrow *kgid-t* \Rightarrow *bool*

where *kgid-has-mapping ns gid* \equiv *True*

definition *uid-eq* :: *kuid-t* \Rightarrow *kuid-t* \Rightarrow *bool*

where *uid-eq left right* \equiv *k--kuid-val left = k--kuid-val right*

1.2 stat_h

definition *S-IFMT* \equiv 00170000

definition *S-IFSOCK* \equiv 0140000

definition *S-IFLNK* \equiv 0120000

definition *S-IFREG* \equiv 0100000

definition *S-IFBLK* \equiv 0060000

definition *S-IFDIR* \equiv 0040000

definition *S-IFCHR* \equiv 0020000

definition *S-IFIFO* \equiv 0010000

definition *S-ISUID* \equiv 0004000

definition *S-ISGID* \equiv 0002000

definition *S-ISVTX* \equiv 0001000

definition *S-ISLNK m* \equiv (((*m*) AND *S-IFMT*) = *S-IFLNK*)

definition *S-ISREG m* \equiv (((*m*) AND *S-IFMT*) = *S-IFREG*)

definition *S-ISDIR m* \equiv (((*m*) AND *S-IFMT*) = *S-IFDIR*)

definition *S-ISCHR m* \equiv (((*m*) AND *S-IFMT*) = *S-IFCHR*)

definition *S-ISBLK m* \equiv (((*m*) AND *S-IFMT*) = *S-IFBLK*)

definition *S-ISFIFO m* \equiv (((*m*) AND *S-IFMT*) = *S-IFIFO*)

definition *S-ISSOCK m* \equiv (((*m*) AND *S-IFMT*) = *S-IFSOCK*)

definition *S-IRWXU* \equiv 00700

definition *S-IRUSR* \equiv 00400

definition *S-IWUSR* \equiv 00200

definition *S-IXUSR* \equiv 00100

definition *S-IRWXG* \equiv 00070

definition *S-IRGRP* \equiv 00040

definition *S-IWGRP* \equiv 00020

definition *S-IXGRP* \equiv 00010

definition *S-IRWXO* \equiv 00007

definition *S-IROTH* \equiv 00004

definition *S-IWOTH* \equiv 00002

definition *S-IXOTH* \equiv 00001

definition *S-IRWXUGO* \equiv *bitOR (bitOR S-IRWXU S-IRWXG) S-IRWXO*

definition *S-IALLUGO* \equiv *bitOR*(*bitOR* (*bitOR* *S-ISUID* *S-ISGID*) *S-ISVTX*)
S-IRWXUGO

definition *S-IRUGO* \equiv *bitOR* (*bitOR* *S-IRUSR* *S-IRGRP*) *S-IROTH*
definition *S-IWUGO* \equiv *bitOR*(*bitOR* *S-IWUSR* *S-IWGRP*) *S-IWOTH*
definition *S-IXUGO* \equiv *bitOR* (*bitOR* *S-IXUSR* *S-IXGRP*) *S-IXOTH*

definition *STATX-TYPE* \equiv *0x00000001*
definition *STATX-MODE* \equiv *0x00000002*
definition *STATX-NLINK* \equiv *0x00000004*
definition *STATX-UID* \equiv *0x00000008*
definition *STATX-GID* \equiv *0x00000010*
definition *STATX-ATIME* \equiv *0x00000020*
definition *STATX-MTIME* \equiv *0x00000040*
definition *STATX-CTIME* \equiv *0x00000080*
definition *STATX-INO* \equiv *0x00000100*
definition *STATX-SIZE* \equiv *0x00000200*
definition *STATX-BLOCKS* \equiv *0x00000400*
definition *STATX-BASIC-STATS* \equiv *0x000007ff*
definition *STATX-BTIME* \equiv *0x00000800*
definition *STATX-ALL* \equiv *0x00000fff*
definition *STATX--RESERVED* \equiv *0x80000000*

definition *STATX-ATTR-COMPRESSED* \equiv *0x00000004*
definition *STATX-ATTR-IMMUTABLE* \equiv *0x00000010*
definition *STATX-ATTR-APPEND* \equiv *0x00000020*
definition *STATX-ATTR-NODUMP* \equiv *0x00000040*
definition *STATX-ATTR-ENCRYPTED* \equiv *0x00000800*

definition *STATX-ATTR-AUTOMOUNT* \equiv *0x00001000*

1.3 cred

type-synonym *kuid* = *nat*
type-synonym *kgid* = *nat*
record *kernel-cap-struct* = *kcap* :: *int list*

type-synonym *kernel-cap-t* = *kernel-cap-struct*

record *Cred* = *uid* :: *kuid-t*
 gid :: *kgid-t*
 suid :: *kgid-t*
 sgid :: *kgid*
 euid :: *kuid-t*
 egid :: *kgid-t*
 fsuid :: *kuid-t*
 fsgid :: *kgid-t*
 user-ns :: *ns*

cap-effective :: kernel-cap-t

1.4 fs_h

definition *ATTR-MODE* $\equiv (1 \ll 0)$
definition *ATTR-UID* $\equiv (1 \ll 1)$
definition *ATTR-GID* $\equiv (1 \ll 2)$
definition *ATTR-SIZE* $\equiv (1 \ll 3)$
definition *ATTR-ATIME* $\equiv (1 \ll 4)$
definition *ATTR-MTIME* $\equiv (1 \ll 5)$
definition *ATTR-CTIME* $\equiv (1 \ll 6)$
definition *ATTR-ATIME-SET* $\equiv (1 \ll 7)$
definition *ATTR-MTIME-SET* $\equiv (1 \ll 8)$
definition *ATTR-FORCE* $\equiv (1 \ll 9)$
definition *ATTR-KILL-SUID* $\equiv (1 \ll 11)$
definition *ATTR-KILL-SGID* $\equiv (1 \ll 12)$
definition *ATTR-FILE* $\equiv (1 \ll 13)$
definition *ATTR-KILL-PRIV* $\equiv (1 \ll 14)$
definition *ATTR-OPEN* $\equiv (1 \ll 15)$
definition *ATTR-TIMES-SET* $\equiv (1 \ll 16)$
definition *ATTR-TOUCH* $\equiv (1 \ll 17)$

type-synonym *dname* = *string*
record *ovl-fs* = *creator-cred* :: *Cred*

record *super-block* = *s-magic* :: *nat*
 s-id :: *string*
 s-root :: *dname*
 s-user-ns :: *user-namespace*
 s-fs-info :: *ovl-fs*
 s-flags :: *nat*
 s-iflags :: *nat*

record *file-lock* = *fl-flags* :: *nat*
 fl-type :: *char*

definition *SB-I-NOEXEC* $\equiv 0x00000002$
definition *O-ACCMODE* $\equiv 00000003$
definition *FMODE-NONOTIFY* $\equiv 0x4000000$
definition *OPEN-FMODE* *flag* $\equiv \text{bitOR } (\text{flag} + 1 \text{ AND } \text{O-ACCMODE}) (\text{flag} \text{ AND } \text{FMODE-NONOTIFY})$

1.5 fat_h

definition *VFAT-SFN-DISPLAY-LOWER* $\equiv 0x0001$
definition *VFAT-SFN-DISPLAY-WIN95* $\equiv 0x0002$
definition *VFAT-SFN-DISPLAY-WINNT* $\equiv 0x0004$
definition *VFAT-SFN-CREATE-WIN95* $\equiv 0x0100$
definition *VFAT-SFN-CREATE-WINNT* $\equiv 0x0200$

definition *FAT-ERRORS-CONT* $\equiv 1$
definition *FAT-ERRORS-PANIC* $\equiv 2$
definition *FAT-ERRORS-RO* $\equiv 3$

definition *FAT-NFS-STALE-RW* $\equiv 1$
definition *FAT-NFS-NOSTALE-RO* $\equiv 2$

type-synonym *umode-t* = *nat*
record *fat-mount-options* = *fs-uid* :: *kuid-t*
 fs-gid :: *kgid-t*
 fs-fmask :: *nat*
 fs-dmask :: *nat*
 rodir :: *nat*

record *msdos-sb-info* = *sbi-options* :: *fat-mount-options*

definition *ATTR-RO* $\equiv 1$
definition *ATTR-DIR* $\equiv 16$
type-synonym *u8* = *char*

definition *fat-make-mode* :: *msdos-sb-info* \Rightarrow *u8* \Rightarrow *umode-t* \Rightarrow *umode-t*
where *fat-make-mode* *sbi* *attrs* *m* \equiv
 let
 attrs' = *int*(*of-char* *attrs*);
 mode = *if* ((*attrs'* AND *ATTR-RO*) $\neq 0$) \wedge \neg ((*attrs'* AND *ATTR-DIR*)
 $\neq 0$) \wedge \neg (*rodir*(*sbi-options* *sbi*)) $\neq 0$)
 then ((*int* *m*) AND (*NOT* *S-IWUGO*))
 else (*int* *m*);
 ret = (*if* (*attrs'* AND *ATTR-DIR*) $\neq 0$ *then*
 bitOR (*mode* AND (*NOT* (*int*(*fs-dmask*(*sbi-options* *sbi*))))))
 S-IFDIR
 else
 bitOR (*mode* AND (*NOT* (*int*(*fs-fmask*(*sbi-options* *sbi*)))))) *S-IFREG*
)
 in (*nat* *ret*)

1.6 other kernel data structures

type-synonym *mode* = *int*
type-synonym *pages* = *int*
type-synonym *flags* = *nat*
type-synonym *kernel-ulong-t* = *nat*
typeddecl *spinlock-t*
typeddecl *security*
type-synonym *loff-t* = *int*
typeddecl *fown-struct*
typeddecl *kernel-load-data-id*
typeddecl *kernel-read-file-id*

```

type-synonym pid-t = int
typedecl siginfo
typedecl file-system-type

```

```

type-synonym process-id = nat
type-synonym inum = nat
type-synonym t-sb = nat
type-synonym fname = string
type-synonym pname = string
type-synonym msg-qid = int
type-synonym msg-mid = int
type-synonym keyid = int
type-synonym socketdesp = int

```

```

record vm-area-struct = vm-end :: nat
                        vm-start :: nat
                        vm-flags :: nat

```

```

record mm-struct = mmap :: vm-area-struct

```

```

record msg-msg = m-type :: int
                m-ts :: nat

```

```

datatype Process-flags = PF-IDLE | PF-EXITING | PF-EXITPIDONE | PF-VCPU |
PF-WQ-WORKER
| PF-FORKNOEXEC | PF-MCE-PROCESS | PF-SUPERPRIV | PF-DUMPCORE
| PF-SIGNALLED | PF-MEMALLOC | PF-NPROC-EXCEEDED | PF-USED-MATH
| PF-USED-ASYNC | PF-NOFREEZE | PF-FROZEN | PF-KSWAPD | PF-MEMALLOC-NOFS
| PF-MEMALLOC-NOIO
| PF-LESS-THROTTLE | PF-KTHREAD
| PF-RANDOMIZE | PF-SWAPWRITE | PF-NO-SETAFFINITY | PF-MCE-EARLY
| PF-MUTEX-TESTER
| PF-FREEZER-SKIP | PF-SUSPEND-TASK

```

```

record fs-struct = users :: int
                  umask :: int
                  in-exec :: int

```

```

record files-struct = count :: int

```

```

record Task = real-cred :: Cred
              cred :: Cred
              flags :: Process-flags
              comm :: string
              ptrace :: int
              parent :: process-id
              ptracer-cred :: Cred option

```

```

    mm :: mm-struct
    fs :: fs-struct
    files :: files-struct
    personality :: nat

record rlimit = rlim-cur :: kernel-ulong-t
               rlim-max :: kernel-ulong-t

record kern-ipc-perm = lock :: spinlock-t
                     deleted :: int
                     id :: int
                     key :: int
                     k-uid :: kuid
                     k-gid :: kgid
                     cuid :: kuid
                     cgid :: kgid
                     mode :: nat
                     seq :: nat

record msg-queue = q-perm :: kern-ipc-perm

record dentry = d-flags :: flags
               d-parent :: dname
               d-sb :: super-block
               d-inode :: inum
               d-name :: string

record ocfs2-security-xattr-info = enable :: int
                                   oname :: string
                                   vvalue :: string
                                   value-len :: nat

record reiserfs-security-handle = rsh-name :: string
                                   rsh-value :: string
                                   rsh-len :: nat

type-synonym initxattrs = int
type-synonym time64-t = int
type-synonym long = int

record timespec64 = tv-sec :: time64-t
                  tv-nsec :: long

type-synonym ts = timespec64
typedecl timezone
type-synonym tz = timezone

```



```

record iattr = ia-valid :: nat
    ia-mode :: mode
    ia-uid :: kuid
    ia-gid :: kgid
    ia-size :: loff-t
    ia-atime :: timespec64
    ia-mtime :: timespec64
    ia-ctime :: timespec64

typedefcl posix-acl
typedefcl inode-operations
typedefcl address-space

record nfs4-label = len :: nat
    label :: string

record inode = i-mode :: mode
    i-opflags :: flags
    i-uid :: kuid-t
    i-gid :: kgid-t
    i-flags :: flags
    i-sb :: super-block
    i-ino :: nat
    i-acl :: posix-acl
    i-default-acl :: posix-acl
    i-op :: inode-operations
    i-mapping :: address-space
    ii-size :: loff-t

record vfsmount = mnt-root :: dentry
    mnt-sb :: super-block
    mnt-flags :: int

record mount = mnt-mountpoint :: dentry
    mnt :: vfsmount

record path = p-mnt :: vfsmount
    p-dentry :: dentry

record binder-proc = tsk :: Task

record binder-thread = proc :: binder-proc
typedefcl flat-binder-object

record binder-transaction = to-proc :: binder-proc

datatype file-operations = fop-read | fop-write | fop-mmap-capabilities

record Files = f-inode :: inode

```

```

        f-mode :: mode
        f-path :: path
        f-cred :: Cred
        f-owner :: fown-struct
        private-data :: binder-proc
        f-op :: file-operations

record fd = fdfile :: Files
        fd-flags :: nat

record linux-binprm = called-set-creds :: int
        lfiles :: Files
        lcred :: Cred
        unsafe :: int
        per-clear :: nat

typedecl user-struct
typedecl ipc-namespace
typedecl ipc-params

record shm-kernel = shm-perm :: kern-ipc-perm
        shm-file :: Files
        shm-nattch :: nat
        shm-segsz :: nat
        shm-creator :: Task
        shm-cprid :: process-id
        shm-lprid :: process-id
        mlock-user :: user-struct

record sem-array = sem-perm :: kern-ipc-perm
        sem-nsems :: int
        complex-count :: int

typedecl delayed-call

record saved = saved-link :: path
        saved-done :: delayed-call
        saved-name :: string
        saved-seq :: nat

record nameidata = nd-path :: path
        nd-root :: path
        nd-last :: string
        nd-inode :: inode
        depth :: nat
        nd-saved :: saved
        link-inode :: inode
        root-seq :: nat
        nd-dfd :: int
        stack :: saved list

```

```

    nd-flags :: nat

typedecl Port
record in-addr = s-addr :: nat
typedecl in6-addr
typedecl kernel-sa-family-t

record sockaddr-in = sin-port :: Port
                     sin-addr :: in-addr
                     sin-family :: kernel-sa-family-t

type-synonym ushort = nat
record sockaddr-in6 = sin6-port :: Port
                     sin6-addr :: in6-addr
                     sin6-family :: ushort

typedecl sk
datatype Sk-Family = PF-INET | PF-INET6 | AF-INET | AF-INET6 | PF-UNSPEC
| PF-UNIX

record sock = sk-type :: nat
             sk-family :: Sk-Family
             sk-socket :: socketdesp

record sockaddr = sa-family :: ushort
                  sa-data :: string

typedecl socket-state
typedecl socket-wq

record proto-ops = proto-family :: int

record socket = skt-type :: int
               sk-flags :: nat
               sk :: sock option
               skt-state :: socket-state
               wq :: socket-wq
               skt-file :: Files
               skt-ops :: proto-ops

record socket-alloc = socket :: socket
                     skufs-inode :: inode

datatype Msghdr-name = Sockaddr-in sockaddr-in | Sockaddr-in6 sockaddr-in6

record iov-iter = iov-type :: int
                 iov-offset :: nat
                 iov-count :: nat

record msghdr = msg-name :: Msghdr-name option

```

```

    msg-iter :: iov-iter

typedef netlbl-lsm-secattr-catmap

record mls = lvl :: nat
    cat :: netlbl-lsm-secattr-catmap

record attr = mls :: mls
    secid :: nat

record netlbl-lsm-secattr = n-flags :: flags
    attr :: attr
type-synonym u32 = nat
record sk-buff = protocol :: int
    secmark :: u32
    skb-iif :: int
typedef short
record sembuf = sem-num :: ushort
    sem-op :: short
    sem-flg :: short

record request-sock = secid :: u32
    peer-secid :: u32

record ovl-cattr = mode :: mode
    link :: string
    hardlink :: dentry

typedef fscache-cache

record fscache-object = fsobj-cache :: fscache-cache

record cachefiles-object = fscache :: fscache-object
    co-dentry :: dentry
    backer :: dentry
    i-size :: loff-t
    co-type :: nat

record cachefiles-xattr = cx-len :: nat
    cx-type :: nat

record cachefiles-cache = cc-mnt :: vfsmount
    cache :: fscache-cache
    graveyard :: dentry
    cachefilesd :: Files
    cache-cred :: Cred

typedef work-struct

```

```

typedef xfrm-sec-ctx
typedef xfrm-user-sec-ctx
typedef xfrm-state

record bpf-map = work :: work-struct

typedef rcu-head

record bpf-prog-aux = rcu :: rcu-head

record bpf-prog = bpf-len :: u32
                  jited-len :: u32
                  aux :: bpf-prog-aux
typedef bpf-attr

typedef xfrm-policy

record audit-context-ipc = audit-context-ipc-osid :: u32

record audit-context = dummy :: int
                      in-syscall :: int
                      serial :: int
                      major :: int
                      ipc :: audit-context-ipc

type-synonym kct = kernel-cap-t
record key = usage :: int

record security-mnt-opts = mnt-opts :: string list
                          mnt-opts-flags :: int list
                          num-mnt-opts :: int
type-synonym opts = security-mnt-opts

record nfs-parsed-mount-data = lsm-opts :: opts

record nfs-clone-mount = nfsc-sb :: super-block

record nfs-mount-info = parsed :: nfs-parsed-mount-data
                      cloned :: nfs-clone-mount
typedef btrfs-fs-info
typedef gfp-t
typedef flowi

type-synonym key-ref-t = keyid

datatype enum-audit = Audit-equal | Audit-not-equal | Audit-bitmask | Audit-bittest
| Audit-lt

```

| *Audit-gt* | *Audit-le* | *Audit-ge* | *Audit-bad*

record *audit-field* = *atype* :: *nat*
 aop :: *enum-audit*
 lsm-rule :: *string*
 lsm-str :: *string*

record *audit-krule* = *field-count* :: *u32*
 afields :: *audit-field list*

record *kernfs-iattrs* =
 ia-iattr :: *iattr*
 ia-secddata :: *string*
 ia-secddata-len :: *nat*

record *ppid* = *level* :: *int*
 tid :: *process-id*

record *proc-inode* = *vfs-inode* :: *inode*
 proci-pid :: *ppid*

definition *EPERM* ≡ 1
definition *ENOENT* ≡ 2
definition *ESRCH* ≡ 3
definition *EINTR* ≡ 4
definition *EIO* ≡ 5
definition *ENXIO* ≡ 6
definition *E2BIG* ≡ 7
definition *ENOEXEC* ≡ 8
definition *EBADF* ≡ 9
definition *ECHILD* ≡ 10
definition *EAGAIN* ≡ 11
definition *ENOMEM* ≡ 12
definition *EACCES* ≡ 13
definition *EFAULT* ≡ 14
definition *ENOTBLK* ≡ 15
definition *EBUSY* ≡ 16
definition *EEXIST* ≡ 17
definition *EXDEV* ≡ 18
definition *ENODEV* ≡ 19
definition *ENOTDIR* ≡ 20
definition *EISDIR* ≡ 21
definition *EINVAL* ≡ 22
definition *ENFILE* ≡ 23
definition *EMFILE* ≡ 24
definition *ENOTTY* ≡ 25
definition *ETXTBSY* ≡ 26
definition *EFBIG* ≡ 27

definition *ENOSPC* \equiv 28
definition *ESPIPE* \equiv 29
definition *EROFS* \equiv 30
definition *EMLINK* \equiv 31
definition *EPIPE* \equiv 32
definition *EDOM* \equiv 33
definition *ERANGE* \equiv 34

1.7 *audit_h*

definition *AUDIT-GET* \equiv 1000
definition *AUDIT-SET* \equiv 1001
definition *AUDIT-LIST* \equiv 1002
definition *AUDIT-ADD* \equiv 1003
definition *AUDIT-DEL* \equiv 1004
definition *AUDIT-USER* \equiv 1005
definition *AUDIT-LOGIN* \equiv 1006
definition *AUDIT-WATCH-INS* \equiv 1007
definition *AUDIT-WATCH-REM* \equiv 1008
definition *AUDIT-WATCH-LIST* \equiv 1009
definition *AUDIT-SIGNAL-INFO* \equiv 1010
definition *AUDIT-ADD-RULE* \equiv 1011
definition *AUDIT-DEL-RULE* \equiv 1012
definition *AUDIT-LIST-RULES* \equiv 1013
definition *AUDIT-TRIM* \equiv 1014
definition *AUDIT-MAKE-EQUIV* \equiv 1015
definition *AUDIT-TTY-GET* \equiv 1016
definition *AUDIT-TTY-SET* \equiv 1017
definition *AUDIT-SET-FEATURE* \equiv 1018
definition *AUDIT-GET-FEATURE* \equiv 1019

consts *audit-sig-sid:: int*

definition *AUDIT-PID* \equiv 0
definition *AUDIT-UID* \equiv 1
definition *AUDIT-EUID* \equiv 2
definition *AUDIT-SUID* \equiv 3
definition *AUDIT-FSUID* \equiv 4
definition *AUDIT-GID* \equiv 5
definition *AUDIT-EGID* \equiv 6
definition *AUDIT-SGID* \equiv 7
definition *AUDIT-FSGID* \equiv 8
definition *AUDIT-LOGINUID* \equiv 9
definition *AUDIT-PERS* \equiv 10
definition *AUDIT-ARCH* \equiv 11
definition *AUDIT-MSGTYPE* \equiv 12
definition *AUDIT-SUBJ-USER* \equiv 13
definition *AUDIT-SUBJ-ROLE* \equiv 14
definition *AUDIT-SUBJ-TYPE* \equiv 15

```

definition AUDIT-SUBJ-SEN  $\equiv$  16
definition AUDIT-SUBJ-CLR  $\equiv$  17
definition AUDIT-PPID  $\equiv$  18
definition AUDIT-OBJ-USER  $\equiv$  19
definition AUDIT-OBJ-ROLE  $\equiv$  20
definition AUDIT-OBJ-TYPE  $\equiv$  21
definition AUDIT-OBJ-LEV-LOW  $\equiv$  22
definition AUDIT-OBJ-LEV-HIGH  $\equiv$  23
definition AUDIT-LOGINUID-SET  $\equiv$  24
definition AUDIT-SESSIONID  $\equiv$  25
definition AUDIT-FSTYPE  $\equiv$  26

type-synonym cap = int

type-synonym mm = mm-struct

typedef seq-file

type-synonym qstr = string

typedef dev-t

definition PTRACE-MODE-SET = {1,2,4,8,16}

type-synonym mask = int

datatype Void = String string | Int int

definition S-PRIVATE = 512

security define

definition LSM-SETID-ID = 1
definition LSM-SETID-RE = 2
definition LSM-SETID-RES = 4
definition LSM-SETID-FS = 8
definition LSM-PRLIMIT-READ = 1
definition LSM-PRLIMIT-WRITE = 2
definition LSM-UNSAFE-SHARE = 1
definition LSM-UNSAFE-PTRACE = 2
definition LSM-UNSAFE-NO-NEW-PRIVS = 4
definition ENOSYS = 78

definition FS-OPEN-PERM  $\equiv$  0x00010000
definition FS-ACCESS-PERM  $\equiv$  0x00020000

definition PTRACE-MODE-READ  $\equiv$  0x01
definition PTRACE-MODE-ATTACH  $\equiv$  0x02
definition PTRACE-MODE-NOAUDIT  $\equiv$  4

```


definition *PTRACE-MODE-FSCREDS* $\equiv 0x08$
definition *PTRACE-MODE-REALCREDS* $\equiv 0x10$

definition *MAY-EXEC* $\equiv 1$
definition *MAY-WRITE* $\equiv 2$
definition *MAY-READ* $\equiv 4$
definition *MAY-APPEND* $\equiv 8$
definition *MAY-ACCESS* $\equiv 0x00000010$
definition *MAY-OPEN* $\equiv 32$
definition *MAY-CHDIR* $\equiv 0x00000040$

definition *MAY-NOT-BLOCK* $\equiv 0x00000080$
definition *F-GETLK* $\equiv 7$
definition *F-SETLK* $\equiv 8$
definition *F-SETLKW* $\equiv 9$

definition *F-SETOWN* $\equiv 5$
definition *F-GETOWN* $\equiv 6$
definition *F-SETSIG* $\equiv 10$
definition *F-GETSIG* $\equiv 11$

definition *F-RDLCK* $\equiv 1$
definition *F-WRLCK* $\equiv 2$
definition *F-UNLCK* $\equiv 8$

definition *F-EXLCK* $\equiv 16$
definition *F-SHLCK* $\equiv 32$
definition *CAP-SYS-RAWIO* $\equiv 17$
definition *CAP-SYS-PTRACE* $\equiv 19$
definition *CAP-SYS-ADMIN* $\equiv 21$
definition *CAP-MAC-ADMIN* $\equiv 33$
definition *CAP-SETFCAP* $\equiv 31$
definition *CAP-MAC-OVERRIDE* $\equiv 32$
definition *SOCKFS-MAGIC* $\equiv 1397703499$
definition *EOPNOTSUPP* $\equiv 45$

definition *FMODE-READ* $= 1$
definition *FMODE-WRITE* $= 2$

definition *IS-PRIVATE* $:: \text{inode} \Rightarrow \text{int}$
where *IS-PRIVATE* $i \equiv i\text{-flags } i \text{ AND } S\text{-PRIVATE}$

definition *RENAME-EXCHANGE* $\equiv 2$

definition *unlikely exp* $\equiv \text{if } exp = 0 \text{ then False else True}$

datatype *xattr* = *XATTR-NAME-SMACK* | *XATTR-NAME-SMACKIPIN* | *XATTR-NAME-SMACKIPOU*
 | *XATTR-NAME-SMACKEXEC*
 | *XATTR-NAME-SMACKMMAP* | *XATTR-NAME-SMACKTRANSMUTE* |
XATTR-SMACK-SUFFIX | *XATTR-SMACK-IPIN*
 | *XATTR-SMACK-IPOUT* | *XATTR-SMACK-EXEC* | *XATTR-SMACK-TRANSMUTE*
 | *XATTR-SMACK-MMAP*
 | *XATTR-SECURITY-PREFIX* | *XATTR-NAME-CAPS*

datatype *IOC-DIR* = *IOC-NONE* | *IOC-READ* | *IOC-WRITE* | *IOC-READWRITE*

datatype *fcntl-cmd* = *F-DUPFD* | *F-GETFD* | *F-SETFD* | *F-GETFL*

definition *ETH-P-IP* \equiv 2048

definition *ETH-P-IPV6* \equiv 34525

definition *S-NOSEC* \equiv 4096

definition *IOP-XATTR* \equiv 8

definition *SECURITY-CAP-AUDIT* \equiv 1

definition *PAGE-SHIFT* \equiv 13

definition *PAGE-SIZE* \equiv 4096

definition *LOOKUP-FOLLOW* \equiv 0x0001

definition *LOOKUP-DIRECTORY* \equiv 0x0002

definition *LOOKUP-AUTOMOUNT* \equiv 0x0004

definition *LOOKUP-PARENT* \equiv 0x0010

definition *LOOKUP-REVAL* \equiv 0x0020

definition *LOOKUP-RCU* \equiv 0x0040

definition *LOOKUP-NO-REVAL* \equiv 0x0080

definition *LOOKUP-OPEN* \equiv 0x0100

definition *LOOKUP-CREATE* \equiv 0x0200

definition *LOOKUP-EXCL* \equiv 0x0400

definition *LOOKUP-RENAME-TARGET* \equiv 0x0800

definition *LOOKUP-JUMPED* \equiv 0x1000

definition *LOOKUP-ROOT* \equiv 0x2000

definition *LOOKUP-EMPTY* \equiv 0x4000

definition *LOOKUP-DOWN* \equiv 0x8000

record *audit-names* = *hidden* :: bool

an-dev :: dev-t

osid :: u32

record *ovl-copy-up-ctx* = *copy-parent* :: *dentry*
 copy-dentry :: *dentry*

definition *KREAD* ≡ 0

definition *KWRITE* ≡ 1

definition *SHM-RDONLY* ≡ 010000

definition *SHM-RND* ≡ 020000

definition *SHM-REMAP* ≡ 040000

definition *SHM-EXEC* ≡ 0100000

definition *SHM-LOCK* ≡ 11

definition *SHM-UNLOCK* ≡ 12

definition *SHM-STAT* ≡ 13

definition *SHM-INFO* ≡ 14

definition *SHM-STAT-ANY* ≡ 15

definition *PROT-READ* ≡ 0x1

definition *PROT-WRITE* ≡ 0x2

definition *PROT-EXEC* ≡ 0x4

definition *PROT-SEM* ≡ 0x8

definition *PROT-NONE* ≡ 0x0

definition *PROT-GROWSDOWN* ≡ 0x01000000

definition *PROT-GROWSUP* ≡ 0x02000000

definition *MAP-SHARED* ≡ 0x01

definition *MAP-PRIVATE* ≡ 0x02

definition *MAP-SHARED-VALIDATE* ≡ 0x03

definition *MAP-TYPE* ≡ 0x0f

definition *MAP-FIXED* ≡ 0x100

definition *MAP-ANONYMOUS* ≡ 0x10

definition *VM-NONE* ≡ 0x00000000

definition *VM-READ* ≡ 0x00000001

definition *VM-WRITE* ≡ 0x00000002

definition *VM-EXEC* ≡ 0x00000004

definition *VM-SHARED* ≡ 0x00000008

definition *VM-MAYREAD* ≡ 0x00000010

definition *VM-MAYWRITE* ≡ 0x00000020

definition *VM-MAYEXEC* ≡ 0x00000040

definition *VM-MAYSHARE* ≡ 0x00000080

definition *VM-GROWSDOWN* ≡ 0x00000100

definition *VM-UFFD-MISSING* $\equiv 0x00000200$
definition *VM-PFNMAP* $\equiv 0x00000400$
definition *VM-DENYWRITE* $\equiv 0x00000800$
definition *VM-UFFD-WP* $\equiv 0x00001000$

definition *VM-LOCKED* $\equiv 0x00002000$
definition *VM-IO* $\equiv 0x00004000$

definition *VM-SEQ-READ* $\equiv 0x00008000$
definition *VM-RAND-READ* $\equiv 0x00010000$

definition *VM-DONTCOPY* $\equiv 0x00020000$
definition *VM-DONTEXPAND* $\equiv 0x00040000$
definition *VM-LOCKONFAULT* $\equiv 0x00080000$
definition *VM-ACCOUNT* $\equiv 0x00100000$
definition *VM-NORESERVE* $\equiv 0x00200000$
definition *VM-HUGETLB* $\equiv 0x00400000$
definition *VM-SYNC* $\equiv 0x00800000$
definition *VM-ARCH-1* $\equiv 0x01000000$
definition *VM-WIPEONFORK* $\equiv 0x02000000$
definition *VM-DONTDUMP* $\equiv 0x04000000$

definition *UNAME26* $\equiv 0x00200000$
definition *ADDR-NO-RANDOMIZE* $\equiv 0x00400000$
definition *FDPIC-FUNCPTRS* $\equiv 0x00800000$

definition *MMAP-PAGE-ZERO* $\equiv 0x01000000$
definition *ADDR-COMPAT-LAYOUT* $\equiv 0x02000000$
definition *READ-IMPLIES-EXEC* $\equiv 0x04000000$
definition *ADDR-LIMIT-32BIT* $\equiv 0x08000000$
definition *SHORT-INODE* $\equiv 0x10000000$
definition *WHOLE-SECONDS* $\equiv 0x20000000$
definition *STICKY-TIMEOUTS* $\equiv 0x40000000$
definition *ADDR-LIMIT-3GB* $\equiv 0x80000000$

definition *FDPUT-FPUT* $\equiv 1$
definition *FDPUT-POS-UNLOCK* $\equiv 2$

definition *SOL-SOCKET* $\equiv 0xffff$
definition *SO-DEBUG* $\equiv 0x0001$
definition *SO-REUSEADDR* $\equiv 0x0004$
definition *SO-KEEPALIVE* $\equiv 0x0008$
definition *SO-DONTROUTE* $\equiv 0x0010$
definition *SO-BROADCAST* $\equiv 0x0020$
definition *SO-LINGER* $\equiv 0x0080$

definition *SO-OOBINLINE* $\equiv 0x0100$
definition *SO-REUSEPORT* $\equiv 0x0200$
definition *SO-TYPE* $\equiv 0x1008$
definition *SO-ERROR* $\equiv 0x1007$
definition *SO-SNDBUF* $\equiv 0x1001$
definition *SO-RCVBUF* $\equiv 0x1002$
definition *SO-SNDBUFFORCE* $\equiv 0x100a$
definition *SO-RCVBUFFORCE* $\equiv 0x100b$
definition *SO-RCVLOWAT* $\equiv 0x1010$
definition *SO-SNDLOWAT* $\equiv 0x1011$
definition *SO-RCVTIMEO* $\equiv 0x1012$
definition *SO-SNDTIMEO* $\equiv 0x1013$
definition *SO-ACCEPTCONN* $\equiv 0x1014$
definition *SO-PROTOCOL* $\equiv 0x1028$
definition *SO-DOMAIN* $\equiv 0x1029$
definition *SO-NO-CHECK* $\equiv 11$
definition *SO-PRIORITY* $\equiv 12$
definition *SO-BSDCOMPAT* $\equiv 14$
definition *SO-PASSCRED* $\equiv 17$
definition *SO-PEERCRED* $\equiv 18$
definition *SO-BINDTODEVICE* $\equiv 25$
definition *SO-ATTACH-FILTER* $\equiv 26$
definition *SO-DETACH-FILTER* $\equiv 27$
definition *SO-GET-FILTER* \equiv *SO-ATTACH-FILTER*
definition *SO-PEERNAME* $\equiv 28$
definition *SO-TIMESTAMP* $\equiv 29$
definition *SCM-TIMESTAMP* \equiv *SO-TIMESTAMP*
definition *SO-PEERSEC* $\equiv 30$
definition *SO-PASSSEC* $\equiv 34$
definition *SO-TIMESTAMPNS* $\equiv 35$
definition *SCM-TIMESTAMPNS* \equiv *SO-TIMESTAMPNS*
definition *SO-SECURITY-AUTHENTICATION* $\equiv 19$
definition *SO-SECURITY-ENCRYPTION-TRANSPORT* $\equiv 20$
definition *SO-SECURITY-ENCRYPTION-NETWORK* $\equiv 21$
definition *SO-MARK* $\equiv 36$
definition *SO-TIMESTAMPING* $\equiv 37$
definition *SCM-TIMESTAMPING* \equiv *SO-TIMESTAMPING*
definition *SO-RXQ-OVFL* $\equiv 40$
definition *SO-WIFI-STATUS* $\equiv 41$
definition *SCM-WIFI-STATUS* \equiv *SO-WIFI-STATUS*
definition *SO-PEEK-OFF* $\equiv 42$
definition *SO-NOFCS* $\equiv 43$
definition *SO-LOCK-FILTER* $\equiv 44$
definition *SO-SELECT-ERR-QUEUE* $\equiv 45$
definition *SO-BUSY-POLL* $\equiv 46$
definition *SO-MAX-PACING-RATE* $\equiv 47$
definition *SO-BPF-EXTENSIONS* $\equiv 48$
definition *SO-INCOMING-CPU* $\equiv 49$
definition *SO-ATTACH-BPF* $\equiv 50$

```

definition SO-DETACH-BPF  $\equiv$  SO-DETACH-FILTER
definition SO-ATTACH-REUSEPORT-CBPF  $\equiv$  51
definition SO-ATTACH-REUSEPORT-EBPF  $\equiv$  52
definition SO-CNX-ADVICE  $\equiv$  53
definition SCM-TIMESTAMPING-OPT-STATS  $\equiv$  54
definition SO-MEMINFO  $\equiv$  55
definition SO-INCOMING-NAPI-ID  $\equiv$  56
definition SO-COOKIE  $\equiv$  57
definition SCM-TIMESTAMPING-PKTINFO  $\equiv$  58
definition SO-PEERGROUPS  $\equiv$  59
definition SO-ZEROCOPY  $\equiv$  60
definition SO-TXTIME  $\equiv$  61
definition SCM-TXTIME  $\equiv$  SO-TXTIME

```

```

typedef kmem-cache
record proto = slab :: kmem-cache

```

```

record scm-cookie = scm-pid :: ppid
                   scm-secid :: u32

```

```

record sctp-ep-common = sctp-ep-sk :: sock

```

```

record sctp-endpoint = sctp-base :: sctp-ep-common

```

```

record sctp-chunk = sctp-skb :: sk-buff

```

```

definition SECMARK-MODE-SEL  $\equiv$  0x01
definition SECMARK-SECCTX-MAX  $\equiv$  256

```

```

record xt-secmark-target-info = xt-mode :: u8
                                xt-secid :: u32
                                xt-secctx :: string

```

```

consts xt-mode :: char

```

```

record tun-struct = numqueues :: nat
                   tun-flags :: nat
                   tun-owner :: kuid-t
                   tun-group :: kgid-t

```

```

typedef ifreq

```

```

record key-type = kname :: string

```

type-synonym *int32-t* = *int*
type-synonym *key-serial-t* = *int32-t*
type-synonym *key-perm-t* = *nat*

typedec1 *Nlmsg-type*
record *nlmsghdr* = *nlmsg-len* :: *nat*
 nlmsg-type :: *nat*

record *nf-conn* = *nf-secmark* :: *nat*

record *netlbl-audit* = *netlbl-audit-secid* :: *u32*
 loginuid :: *kuid-t*
 sessionid :: *nat*

record *kernfs-node* = *kn-iattr* :: *kernfs-iattrs*
 kn-mode :: *mode*
 kn-flags :: *nat*

record *gfs2-inode* = *i-inode* :: *inode*

record *svc-fh* = *fh-dentry* :: *dentry*

record *xdr-netobj* = *xdr-len* :: *nat*
 xdr-data :: *string*
typedec1 *nfs-fh*

definition *MNT-NOEXEC* \equiv *0x04*

definition *path-noexec* :: *path* \Rightarrow *bool*
 where *path-noexec p* \equiv ((*mnt-flags* (*p-mnt p*)) *AND* *MNT-NOEXEC*) \neq 0
 \vee ((*int*(*s-iflags* (*mnt-sb* (*p-mnt p*)))) *AND* *SB-I-NOEXEC*) \neq 0
consts *CONFIG-MMU*::*bool*

definition *NOMMU-MAP-EXEC* \equiv *VM-MAYEXEC*

record *xattrs* = *xattr-name* :: *string*
 xattr-value :: *string*
 xattr-value-len :: *nat*

datatype *IPC-CMD* = *IPC-STAT* | *MSG-STAT* | *MSG-STAT-ANY* | *IPC-SET*
 | *IPC-RMID* | *IPC-INFO* | *MSG-INFO* |
GETPID | *GETNCNT* | *GETZCNT* | *GETVAL* | *GETALL* | *SEM-STAT* | *SEM-STAT-ANY*

| *SETVAL* | *SETALL* | *SEM-INFO*
 | *SHM-STAT* | *SHM-STAT-ANY* | *SHM-LOCK* | *SHM-UNLOCK*

typedef *net*
typedef *audit-buffer*

1.8 dache_h

definition *DCACHE-OP-HASH* \equiv *0x00000001*
definition *DCACHE-OP-COMPARE* \equiv *0x00000002*
definition *DCACHE-OP-REVALIDATE* \equiv *0x00000004*
definition *DCACHE-OP-DELETE* \equiv *0x00000008*
definition *DCACHE-OP-PRUNE* \equiv *0x00000010*
definition *DCACHE-DISCONNECTED* \equiv *0x00000020*

definition *DCACHE-REFERENCED* \equiv *0x00000040*

definition *DCACHE-CANT-MOUNT* \equiv *0x00000100*
definition *DCACHE-GENOCIDE* \equiv *0x00000200*
definition *DCACHE-SHRINK-LIST* \equiv *0x00000400*
definition *DCACHE-OP-WEAK-REVALIDATE* \equiv *0x00000800*
definition *DCACHE-NFSFS-RENAMED* \equiv *0x00001000*
definition *DCACHE-COOKIE* \equiv *0x00002000*
definition *DCACHE-FSNOTIFY-PARENT-WATCHED* \equiv *0x00004000*
definition *DCACHE-DENTRY-KILLED* \equiv *0x00008000*
definition *DCACHE-MOUNTED* \equiv *0x00010000*
definition *DCACHE-NEED-AUTOMOUNT* \equiv *0x00020000*
definition *DCACHE-MANAGE-TRANSIT* \equiv *0x00040000*

definition *DCACHE-LRU-LIST* \equiv *0x00080000*

definition *DCACHE-ENTRY-TYPE* \equiv *0x00700000*
definition *DCACHE-MISS-TYPE* \equiv *0x00000000*
definition *DCACHE-WHITEOUT-TYPE* \equiv *0x00100000*
definition *DCACHE-DIRECTORY-TYPE* \equiv *0x00200000*
definition *DCACHE-AUTODIR-TYPE* \equiv *0x00300000*
definition *DCACHE-REGULAR-TYPE* \equiv *0x00400000*
definition *DCACHE-SPECIAL-TYPE* \equiv *0x00500000*
definition *DCACHE-SYMLINK-TYPE* \equiv *0x00600000*

definition *DCACHE-MAY-FREE* \equiv *0x00800000*
definition *DCACHE-FALLTHRU* \equiv *0x01000000*
definition *DCACHE-ENCRYPTED-WITH-KEY* \equiv *0x02000000*
definition *DCACHE-OP-REAL* \equiv *0x04000000*

definition *DCACHE-PAR-LOOKUP* \equiv *0x10000000*
definition *DCACHE-DENTRY-CURSOR* \equiv *0x20000000*
definition *DCACHE-NORCU* \equiv *0x40000000*

definition $d\text{-entry-type} :: \text{dentry} \Rightarrow \text{int}$
where $d\text{-entry-type } d \equiv d\text{-flags } d \text{ AND } \text{DCACHE-ENTRY-TYPE}$

definition $d\text{-entry-type}' :: \text{dentry} \Rightarrow \text{int}$
where $d\text{-entry-type}' \text{ dentry} \equiv (d\text{-flags } \text{dentry} \text{ AND } \text{DCACHE-ENTRY-TYPE})$

definition $d\text{-is-autodir} :: \text{dentry} \Rightarrow \text{bool}$
where $d\text{-is-autodir } \text{dentry} \equiv \text{if } (d\text{-entry-type}' \text{ dentry} = \text{DCACHE-AUTODIR-TYPE})$
 $\text{ then True else False}$

definition $d\text{-can-lookup} :: \text{dentry} \Rightarrow \text{bool}$
where $d\text{-can-lookup } \text{dentry} \equiv \text{if } (d\text{-entry-type}' \text{ dentry} = \text{DCACHE-DIRECTORY-TYPE})$
 $\text{ then True else False}$

definition $d\text{-is-dir} :: \text{dentry} \Rightarrow \text{bool}$
where $d\text{-is-dir } \text{dentry} \equiv d\text{-can-lookup } \text{dentry} \vee d\text{-is-autodir } \text{dentry}$

definition $d\text{-is-miss} :: \text{dentry} \Rightarrow \text{bool}$
where $d\text{-is-miss } \text{dentry} \equiv \text{if } (d\text{-entry-type}' \text{ dentry} = \text{DCACHE-MISS-TYPE})$
 $\text{ then True else False}$

definition $d\text{-is-negative} :: \text{dentry} \Rightarrow \text{bool}$
where $d\text{-is-negative } d \equiv d\text{-is-miss}(d)$

definition $d\text{-is-positive} :: \text{dentry} \Rightarrow \text{bool}$
where $d\text{-is-positive } d \equiv \neg(d\text{-is-negative } d)$

definition $d\text{-is-whiteout} :: \text{dentry} \Rightarrow \text{bool}$
where $d\text{-is-whiteout } \text{dentry} \equiv \text{if } (d\text{-entry-type}' \text{ dentry} = \text{DCACHE-WHITEOUT-TYPE})$
 $\text{ then True else False}$

definition $d\text{-is-symlink} :: \text{dentry} \Rightarrow \text{bool}$
where $d\text{-is-symlink } \text{dentry} \equiv \text{if } (d\text{-entry-type}' \text{ dentry} = \text{DCACHE-SYMLINK-TYPE})$
 $\text{ then True else False}$

definition $d\text{-is-reg} :: \text{dentry} \Rightarrow \text{bool}$
where $d\text{-is-reg } \text{dentry} \equiv \text{if } (d\text{-entry-type}' \text{ dentry} = \text{DCACHE-REGULAR-TYPE})$
 $\text{ then True else False}$

definition $d\text{-is-special} :: \text{dentry} \Rightarrow \text{bool}$
where $d\text{-is-special } \text{dentry} \equiv \text{if } (d\text{-entry-type}' \text{ dentry} = \text{DCACHE-SPECIAL-TYPE})$
 $\text{ then True else False}$

definition $d\text{-is-file} :: \text{dentry} \Rightarrow \text{bool}$
where $d\text{-is-file } \text{dentry} \equiv d\text{-is-reg } \text{dentry} \vee d\text{-is-special } \text{dentry}$

definition $d\text{-is-fallthru} :: \text{dentry} \Rightarrow \text{bool}$
where $d\text{-is-fallthru } \text{dentry} \equiv \text{if } (d\text{-flags } \text{dentry} \text{ AND } \text{DCACHE-FALLTHRU}) \neq$

0 then True else False

definition *d-inodeid* :: *dentry* \Rightarrow *inum*
where *d-inodeid dentry* \equiv (*d-inode dentry*)

1.9 fcntl_h

definition *F-LINUX-SPECIFIC-BASE* \equiv 1024

definition *F-SETLEASE* \equiv (*F-LINUX-SPECIFIC-BASE* + 0)

definition *F-GETLEASE* \equiv (*F-LINUX-SPECIFIC-BASE* + 1)

definition *F-CANCELLK* \equiv (*F-LINUX-SPECIFIC-BASE* + 5)

definition *F-DUPFD-CLOEXEC* \equiv (*F-LINUX-SPECIFIC-BASE* + 6)

definition *F-NOTIFY* \equiv (*F-LINUX-SPECIFIC-BASE* + 2)

definition *F-SETPPIPE-SZ* \equiv (*F-LINUX-SPECIFIC-BASE* + 7)

definition *F-GETPIPE-SZ* \equiv (*F-LINUX-SPECIFIC-BASE* + 8)

definition *F-ADD-SEALS* \equiv (*F-LINUX-SPECIFIC-BASE* + 9)

definition *F-GET-SEALS* \equiv (*F-LINUX-SPECIFIC-BASE* + 10)

definition *F-SEAL-SEAL* \equiv 0x0001

definition *F-SEAL-SHRINK* \equiv 0x0002

definition *F-SEAL-GROW* \equiv 0x0004

definition *F-SEAL-WRITE* \equiv 0x0008

definition *F-GET-RW-HINT* \equiv (*F-LINUX-SPECIFIC-BASE* + 11)

definition *F-SET-RW-HINT* \equiv (*F-LINUX-SPECIFIC-BASE* + 12)

definition *F-GET-FILE-RW-HINT* \equiv (*F-LINUX-SPECIFIC-BASE* + 13)

definition *F-SET-FILE-RW-HINT* \equiv (*F-LINUX-SPECIFIC-BASE* + 14)

definition *RWF-WRITE-LIFE-NOT-SET* \equiv 0

definition *RWH-WRITE-LIFE-NONE* \equiv 1

definition *RWH-WRITE-LIFE-SHORT* \equiv 2

definition *RWH-WRITE-LIFE-MEDIUM* \equiv 3

definition *RWH-WRITE-LIFE-LONG* \equiv 4

definition *RWH-WRITE-LIFE-EXTREME* \equiv 5

```

definition DN-ACCESS  $\equiv 0x00000001$ 
definition DN-MODIFY  $\equiv 0x00000002$ 
definition DN-CREATE  $\equiv 0x00000004$ 
definition DN-DELETE  $\equiv 0x00000008$ 
definition DN-RENAME  $\equiv 0x00000010$ 
definition DN-ATTRIB  $\equiv 0x00000020$ 
definition DN-MULTISHOT  $\equiv 0x80000000$ 

definition AT-FDCWD  $\equiv -100$ 
definition AT-SYMLINK-NOFOLLOW  $\equiv 0x100$ 
definition AT-REMOVEDIR  $\equiv 0x200$ 
definition AT-SYMLINK-FOLLOW  $\equiv 0x400$ 
definition AT-NO-AUTOMOUNT  $\equiv 0x800$ 
definition AT-EMPTY-PATH  $\equiv 0x1000$ 

definition AT-STATX-SYNC-TYPE  $\equiv 0x6000$ 
definition AT-STATX-SYNC-AS-STAT  $\equiv 0x0000$ 
definition AT-STATX-FORCE-SYNC  $\equiv 0x2000$ 
definition AT-STATX-DONT-SYNC  $\equiv 0x4000$ 
definition Q-SYNC  $\equiv 8388609$ 
end

```

2 The Core of the Subject-Object Access Control Policy For Smack

In this theory, we introduce subject-object access control policy. A subject is an active entity, usually a process (running program), that causes information to flow among objects or changes the system state. On Smack a subject is a task, which is in turn the basic unit of execution. An object is a passive entity that contains or receives data, such as a File, Inode, IPC, Sock. A process may be an object, such as when you use kill on a process. All subjects and objects in a system have labels. The label determines which information you can access.

```

theory
  SOAC
  imports
    Element
begin

```

2.1 Model of a AC configuration

```

datatype decision = allow | deny

```

```

datatype access = READ | WRITE | EXECUTE | APPEND | T | LOCK |
  Control | OWN

```

datatype *Request* = *MAY-WRITE'* | *MAY-READ'* | *MAY-EXECUTE'* | *MAY-APPEND'*
| *MAY-T'* | *MAY-LOCK'*

type-synonym ('*subj*, '*obj*) *policy-table* = '*subj* \Rightarrow ('*subj* \times '*obj*) \Rightarrow *access set*

Label: Data that identifies the Mandatory Access Control characteristics of a subject or an object. The format of an access rule is: *subject_llabelobject_llabelaccess*. Each rule must specify *Un*class for unclassified, *C* for classified, *S* for secret, and *TS* for top secret. Then, with a handful of rules, the traditional hierarchy of access is defined. Because of the Smack defaults, *Un*class will only be able to access data with that same label, whereas because of the rules above, *TS* can access *S*, *C* and *Un*class data. Note that there is no transitivity in Smack rules, just because *S* can access *C* and *TS* can access *S*, that does not mean that *TS* can access *C*.

datatype *Label* = *Normal string* | *Floor* | *Hat* | *Star* | *Huh* | *Web* | *UNDEFINED*

type-synonym *subject-label* = *Label*

type-synonym *object-label* = *Label*

type-synonym *Subj* = *process-id*

datatype *Obj* = *Sb super-block* | *Process process-id* | *File Files* | *IPC kern-ipc-perm*
| *Msg msg-msg*
| *ObjInode inode* | *ObjSock sock* | *ObjKey key*

definition *access-rl* :: *Request* \Rightarrow *access*
where *access-rl* *r* \equiv (case *r* of *MAY-WRITE'* \Rightarrow *WRITE* |
MAY-READ' \Rightarrow *READ* |
MAY-EXECUTE' \Rightarrow *EXECUTE* |
MAY-APPEND' \Rightarrow *APPEND* |
MAY-T' \Rightarrow *T* |
MAY-LOCK' \Rightarrow *LOCK*
)

locale *SOModel* =
fixes *subj-label* :: '*s* \Rightarrow *Subj* \Rightarrow *subject-label*
fixes *obj-label* :: '*s* \Rightarrow *Obj* \Rightarrow *object-label*
fixes *access-rules* :: *Label* \Rightarrow *Label* \Rightarrow *access set*
fixes *Subj* :: '*s* \Rightarrow *Subj set*
fixes *Obj* :: '*s* \Rightarrow *Obj set*
fixes *request* :: '*s* \Rightarrow *Subj* \Rightarrow *Obj* \Rightarrow *Request* \Rightarrow *decision*

begin

abbreviation *subjects-have-auth* :: *Subj* \Rightarrow *access* \Rightarrow *bool*
where *subjects-have-auth* *subj a* $\equiv \forall s$ *obj. subj* \in *Subj s* \longrightarrow *a* \in *access-rules*
(*subj-label s subj*) (*obj-label s obj*)

end

end

theory *Value-Abbreviation*

imports *Main*

keywords *value-abbreviation* :: *thy-decl*

begin

Computing values and saving as abbreviations.

Useful in program verification to handle some configuration constant (e.g. $n = 4$) which may change. This mechanism can be used to give names (abbreviations) to other related constants (e.g. 2^n , $2^n - 1$, $[1..n]$, $rev[1..n]$) which may appear repeatedly.

ML \langle

structure Value-Abbreviation = struct

fun value-and-abbreviation mode name expr int ctxt = let

val decl = (name, NONE, Mixfix.NoSyn)

val expr = Syntax.read-term ctxt expr

val eval-expr = Value-Command.value ctxt expr

val lhs = Free (Binding.name-of name, fastype-of expr)

val eq = Logic.mk-equals (lhs, eval-expr)

val ctxt = Specification.abbreviation mode (SOME decl) [] eq int ctxt

val pretty-eq = Syntax.pretty-term ctxt eq

in Pretty.writeln pretty-eq; ctxt end

val - =

Outer-Syntax.local-theory' @ {command-keyword value-abbreviation}

setup abbreviation for evaluated value

(Parse.syntax-mode -- Parse.binding -- Parse.term

>> (fn ((mode, name), expr) => value-and-abbreviation mode name expr));

end

)

Testing it out. Unfortunately locale/experiment/notepad all won't work here because the code equation setup is all global.

definition

value-abbreviation-test-config-constant-1 = (24 :: nat)

definition

value-abbreviation-test-config-constant-2 = (5 :: nat)

value-abbreviation (*input*)

value-abbreviation-test-important-magic-number

```

      ((2 :: int) ^ value-abbreviation-test-config-constant-1)
      - (2 ^ value-abbreviation-test-config-constant-2)

value-abbreviation (input)
  value-abbreviation-test-range-of-options
  rev [int value-abbreviation-test-config-constant-2
      .. int value-abbreviation-test-config-constant-1]

end

theory Match-Abbreviation

imports Main

keywords match-abbreviation :: thy-decl
and reassoc-thm :: thy-decl

begin

Splicing components of terms and saving as abbreviations. See the example
at the bottom for explanation/documentation.

ML <
structure Match-Abbreviation = struct

  fun app-cons-dummy cons x y
    = Const (cons, dummyT) $ x $ y

  fun lazy-lam x t = if Term.exists-subterm (fn t' => t' aconv x) t
    then lambda x t else t

  fun abs-dig-f ctxt lazy f (Abs (nm, T, t))
    = let
      val (nms, ctxt) = Variable.variant-fixes [nm] ctxt
      val x = Free (hd nms, T)
      val t = betapply (Abs (nm, T, t), x)
      val t' = f ctxt t
    in if lazy then lazy-lam x t' else lambda x t' end
    | abs-dig-f - - - t = raise TERM (abs-dig-f: not abs, [t])

  fun find-term1 ctxt get (f $ x)
    = (get ctxt (f $ x) handle Option => (find-term1 ctxt get f
      handle Option => find-term1 ctxt get x))
    | find-term1 ctxt get (a as Abs -)
    = abs-dig-f ctxt true (fn ctxt => find-term1 ctxt get) a
    | find-term1 ctxt get t = get ctxt t

  fun not-found pat t = raise TERM (pattern not found, [pat, t])

  fun find-term ctxt get pat t = find-term1 ctxt get t

```

```

handle Option => not-found pat t

fun lambda-frees-vars ctxt ord-t t = let
  fun is-free t = is-Free t andalso not (Variable.is-fixed ctxt (Term.term-name t))
  fun is-it t = is-free t orelse is-Var t
  val get = fold-aterms (fn t => if is-it t then insert (=) t else I)
  val all-vars = get ord-t []
  val vars = get t []
  val ord-vars = filter (member (=) vars) all-vars
in fold lambda ord-vars t end

fun parse-pat-fixes ctxt fixes pats = let
  val (-, ctxt') = Variable.add-fixes
    (map (fn (b, -, -) => Binding.name-of b) fixes) ctxt
  val read-pats = Syntax.read-terms ctxt' pats
in Variable.export-terms ctxt' ctxt read-pats end

fun add-reassoc name rhs fixes thms-info ctxt = let
  val thms = Attrib.eval-thms ctxt thms-info
  val rhs-pat = singleton (parse-pat-fixes ctxt fixes) rhs
  |> Thm.cterm-of ctxt
  val rew = Simplifier.rewrite (clear-simpset ctxt addsimps thms) rhs-pat
  |> Thm.symmetric
  val (-, ctxt) = Local-Theory.note ((name, []), [rew]) ctxt
  val pretty-decl = Pretty.block [Pretty.str (Binding.name-of name ^ :\n),
    Thm.pretty-thm ctxt rew]
in Pretty.writeln pretty-decl; ctxt end

fun dig-f ctxt repeat adj (f $ x) = (adj ctxt (f $ x)
  handle Option => (dig-f ctxt repeat adj f
    $ (if repeat then (dig-f ctxt repeat adj x
      handle Option => x) else x)
    handle Option => f $ dig-f ctxt repeat adj x))
| dig-f ctxt repeat adj (a as Abs -)
  = abs-dig-f ctxt false (fn ctxt => dig-f ctxt repeat adj) a
| dig-f ctxt - adj t = adj ctxt t

fun do-rewrite ctxt repeat rew-pair t = let
  val thy = Proof-Context.theory-of ctxt
  fun adj - t = case Pattern.match-rew thy t rew-pair
    of NONE => raise Option | SOME (t', -) => t'
in dig-f ctxt repeat adj t
  handle Option => not-found (fst rew-pair) t end

fun select-dig ctxt [] f t = f ctxt t
| select-dig ctxt (p :: ps) f t = let
  val thy = Proof-Context.theory-of ctxt
  fun do-rec ctxt t = if Pattern.matches thy (p, t)
    then select-dig ctxt ps f t else raise Option

```

```

in dig-f ctxt false do-rec t handle Option => not-found p t end

fun ext-dig-lazy ctxt f (a as Abs -)
  = abs-dig-f ctxt true (fn ctxt => ext-dig-lazy ctxt f) a
  | ext-dig-lazy ctxt f t = f ctxt t

fun report-adjust ctxt nm t = let
  val pretty-decl = Pretty.block [Pretty.str (nm ^ ", have:\n"),
    Syntax.pretty-term ctxt t]
in Pretty.writeln pretty-decl; t end

fun do-adjust ctxt (((select, []), [p]), fixes) t = let
  val p = singleton (parse-pat-fixes ctxt fixes) p
  val thy = Proof-Context.theory-of ctxt
  fun get - t = if Pattern.matches thy (p, t) then t else raise Option
  val t = find-term ctxt get p t
in report-adjust ctxt Selected t end
| do-adjust ctxt (((retype-consts, []), consts), []) t = let
  fun get-constname (Const (s, -)) = s
    | get-constname (Abs (-, -, t)) = get-constname t
    | get-constname (f $ -) = get-constname f
    | get-constname - = raise Option
  fun get-constname2 t = get-constname t
    handle Option => raise TERM (do-adjust: no constant, [t])
  val cnames = map (get-constname2 o Syntax.read-term ctxt) consts
    |> Symtab.make-set
  fun adj (Const (cn, T)) = if Symtab.defined cnames cn
    then Const (cn, dummyT) else Const (cn, T)
    | adj t = t
  val t = Syntax.check-term ctxt (Term.map-aterms adj t)
in report-adjust ctxt Adjusted types t end
| do-adjust ctxt (((r, in-selects), [from, to]), fixes) t = if
  r = rewrite1 orelse r = rewrite then let
    val repeat = r <> rewrite1
    val sel-pats = map (fn (p, fixes) => singleton (parse-pat-fixes ctxt fixes) p)
      in-selects
    val rewrite-pair = case parse-pat-fixes ctxt fixes [from, to]
      of [f, t] => (f, t) | - => error (do-adjust: unexpected length)
    val t = ext-dig-lazy ctxt (fn ctxt => select-dig ctxt sel-pats
      (fn ctxt => do-rewrite ctxt repeat rewrite-pair)) t
  in report-adjust ctxt (if repeat then Rewrote else Rewrote (repeated)) t end
else error (do-adjust: unexpected: ^ r)
| do-adjust - args - = error (do-adjust: unexpected: ^ @{make-string} args)

fun unvarify-types-same ty = ty
|> Term-Subst.map-atypsT-same
  (fn TVar ((a, i), S) => TFree (a ^ -var- ^ string-of-int i, S)
    | - => raise Same.SAME)

```



```

fun unvarify-types tm = tm
  |> Same.commit (Term-Subst.map-types-same unvarify-types-same)

fun match-abbreviation mode name init adjusts int ctxt = let
  val init-term = init ctxt
  val init-lambda = lambda-frees-vars ctxt init-term init-term
  |> unvarify-types
  |> Syntax.check-term ctxt
  val decl = (name, NONE, Mixfix.NoSyn)
  val result = fold (do-adjust ctxt) adjusts init-lambda
  val lhs = Free (Binding.name-of name, fastype-of result)
  val eq = Logic.mk-equals (lhs, result)
  val ctxt = Specification.abbreviation mode (SOME decl) [] eq int ctxt
  val pretty-eq = Syntax.pretty-term ctxt eq
in Pretty.writeln pretty-eq; ctxt end

fun from-thm f thm-info ctxt = let
  val thm = singleton (Attrib.eval-thms ctxt) thm-info
in f thm end

fun from-term term-str ctxt = Syntax.parse-term ctxt term-str

val init-term-parse = Parse.$$$ in |--
  ((Parse.reserved concl |-- Parse.thm >> from-thm Thm.concl-of)
   || (Parse.reserved thm-prop |-- Parse.thm >> from-thm Thm.prop-of)
   || (Parse.term >> from-term)
  )

val term-to-term = (Parse.term -- (Parse.reserved to |-- Parse.term))
  >> (fn (a, b) => [a, b])

val p-for-fixes = Scan.optional
  (Parse.$$$ ( |-- Parse.for-fixes --| Parse.$$$ )) []

val adjust-parser = Parse.and-list1
  ((Parse.reserved select -- Scan.succeed [] -- (Parse.term >> single) --
  p-for-fixes)
   || (Parse.reserved retype-consts -- Scan.succeed []
      -- Scan.repeat Parse.term -- Scan.succeed [])
   || ((Parse.reserved rewrite1 || Parse.reserved rewrite)
      -- Scan.repeat (Parse.$$$ in |-- Parse.term -- p-for-fixes)
      -- term-to-term -- p-for-fixes)
  )

(* install match-abbreviation. see below for examples/docs *)
val - =
  Outer-Syntax.local-theory' @ {command-keyword match-abbreviation}
  setup abbreviation for subterm of theorem
  (Parse.syntax-mode -- Parse.binding

```

```

-- init-term-parse -- adjust-parser
>> (fn (((mode, name), init), adjusts)
    => match-abbreviation mode name init adjusts));

val - =
  Outer-Syntax.local-theory @{command-keyword reassoc-thm}
    store a reassociate-theorem
    (Parse.binding -- Parse.term -- p-for-fixes -- Scan.repeat Parse.thm
    >> (fn (((name, rhs), fixes), thms)
        => add-reassoc name rhs fixes thms));
end

```

The match/abbreviate command. There are examples of all elements below, and an example involving monadic syntax in the theory Match-Abbreviation-Test.

Each invocation is match abbreviation, a syntax mode (e.g. (input)), an abbreviation name, a term specifier, and a list of adjustment specifiers.

A term specifier can be term syntax or the conclusion or proposition of some theorem. Examples below.

Each adjustment is a select, a rewrite, or a constant retype.

The select adjustment picks out the part of the term matching the pattern (examples below). It picks the first match point, ordered in term order with compound terms before their subterms and functions before their arguments.

The rewrite adjustment uses a pattern pair, and rewrites instances of the first pattern into the second. The match points are found in the same order as select. The "in" specifiers (examples below) limit the rewriting to within some matching subterm, specified with pattern in the same way as select. The rewrite1 variant only rewrites once, at the first matching site.

The rewrite mechanism can be used to replace terms with terms of different types. The retype adjustment can then be used to repair the term by resetting the types of all instances of the named constants. This is used below with list constructors, to assemble a new list with a different element type.

experiment begin

Fetching part of the statement of a theorem.

```

match-abbreviation (input) fixp-thm-bit
  in thm-prop fixp-induct-tailrec
  select  $X \equiv Y$  (for  $X$   $Y$ )

```

Ditto conclusion.

```

match-abbreviation (input) rev-simps-bit
  in concl rev.simps(2)
  select  $X$  (for  $X$ )

```

Selecting some conjuncts and reorienting an equality.

```

match-abbreviation (input) conjunct-test
  in ( $P \wedge Q \wedge P \wedge P \wedge P \wedge ((1 :: \text{nat}) = 2) \wedge Q \wedge Q, [\text{Suc } 0, 0]$ )
  select  $Q \wedge Z$  (for  $Z$ )
  and rewrite  $x = y$  to  $y = x$  (for  $x y$ )
  and rewrite in  $x = y \ \& \ Z$  (for  $x y Z$ )
   $A \wedge B$  to  $A$  (for  $A B$ )

```

The relevant reassociate theorem, that rearranges a conjunction like the above to group the elements selected.

```

reassoc-thm conjunct-test-reassoc
  conjunct-test  $P Q \wedge Z$  (for  $P Q Z$ )
  conj-assoc

```

Selecting some elements of a list, and then replacing tuples with equalities, and adjusting the type of the list constructors so the new term is type correct.

```

match-abbreviation (input) list-test
  in [ $(\text{Suc } 1, \text{Suc } 2), (4, 5), (6, 7), (8, 9), (10, 11), (x, y), (6, 7),$ 
     $(18, 19), a, a, a, a, a, a, a]$ 
  select  $(4, V) \# xs$  (for  $V xs$ )
  and rewrite  $(x, y)$  to  $(y, x)$  (for  $x y$ )
  and rewrite1 in  $(9, V) \# xs$  (for  $V xs$ ) in  $(7, V) \# xs$  (for  $V xs$ )
   $x \# xs$  to  $[x]$  (for  $x xs$ )
  and rewrite  $(x, y)$  to  $x = y$  (for  $x y$ )
  and retype-consts  $\text{Cons Nil}$ 

```

end

end

```

theory Subgoal-Methods
imports Main
begin
ML ⟨
  signature SUBGOAL-METHODS =
  sig
    val fold-subgoals: Proof.context -> bool -> thm -> thm
    val unfold-subgoals-tac: Proof.context -> tactic
    val distinct-subgoals: Proof.context -> thm -> thm
  end;

  structure Subgoal-Methods: SUBGOAL-METHODS =
  struct

    fun max-common-prefix eq (ls :: lss) =
      let

```

```

    val ls' = tag-list 0 ls;
    fun all-prefix (i,a) =
      forall (fn ls' => if length ls' > i then eq (a, nth ls' i) else false) lss
    val ls'' = take-prefix all-prefix ls'
    in map snd ls'' end
  | max-common-prefix - [] = [];

fun push-outer-params ctxt th =
  let
    val ctxt' = ctxt
    |> Simplifier.empty-simpset
    |> Simplifier.add-simp Drule.norm-hhf-eq;
  in
    Conv.fconv-rule
    (Raw-Simplifier.rewrite-cterm (true, false, false) (K (K NONE)) ctxt') th
  end;

fun fix-schematics ctxt raw-st =
  let
    val ((schematic-types, [st']), ctxt1) = Variable.importT [raw-st] ctxt;
    val ((-, inst), ctxt2) =
      Variable.import-inst true [Thm.prop-of st'] ctxt1;

    val schematic-terms = map (apsnd (Thm.cterm-of ctxt2)) inst;
    val schematics = (schematic-types, schematic-terms);

    in (Thm.instantiate schematics st', ctxt2) end

  val strip-params = Term.strip-all-vars;
  val strip-prems = Logic.strip-imp-prems o Term.strip-all-body;
  val strip-concl = Logic.strip-imp-concl o Term.strip-all-body;

fun fold-subgoals ctxt prefix raw-st =
  if Thm.nprems-of raw-st < 2 then raw-st
  else
    let
      val (st, inner-ctxt) = fix-schematics ctxt raw-st;

      val subgoals = Thm.prems-of st;
      val paramss = map strip-params subgoals;
      val common-params = max-common-prefix (eq-snd (op =)) paramss;

      fun strip-shift subgoal =
        let
          val params = strip-params subgoal;
          val diff = length common-params - length params;
          val prems = strip-prems subgoal;

```

```

    in map (Term.incr-boundvars diff) prems end;

val prems = map (strip-shift) subgoals;

val common-prems = max-common-prefix (op aconv) prems;

val common-params = if prefix then common-params else [];
val common-prems = if prefix then common-prems else [];

fun mk-concl subgoal =
  let
    val params = Term.strip-all-vars subgoal;
    val local-params = drop (length common-params) params;
    val prems = strip-prems subgoal;
    val local-prems = drop (length common-prems) prems;
    val concl = strip-concl subgoal;
  in Logic.list-all (local-params, Logic.list-implies (local-prems, concl)) end;

val goal =
  Logic.list-all (common-params,
    (Logic.list-implies (common-prems, Logic.mk-conjunction-list (map mk-concl
subgoals))));

val chyp = Thm.ctrm-of inner-ctxt goal;

val (common-params', inner-ctxt') =
  Variable.add-fixes (map fst common-params) inner-ctxt
|>> map2 (fn (-, T) => fn x => Thm.ctrm-of inner-ctxt (Free (x, T)))
common-params;

fun try-dest rule =
  try (fn () => (@{thm conjunctionD1} OF [rule], @{thm conjunctionD2}
OF [rule])) ();

fun solve-headgoal rule =
  let
    val rule' = rule
    |> Drule.forall-intr-list common-params'
    |> push-outer-params inner-ctxt';
  in
    (fn st => Thm.implies-elim st rule')
  end;

fun solve-subgoals rule' st =
  (case try-dest rule' of
    SOME (this, rest) => solve-subgoals rest (solve-headgoal this st)
  | NONE => solve-headgoal rule' st);

val rule = Drule.forall-elim-list common-params' (Thm.assume chyp);

```

```

in
  st
  |> push-outer-params inner-ctxt
  |> solve-subgoals rule
  |> Thm.implies-intr chyp
  |> singleton (Variable.export inner-ctxt' ctxt)
end;

fun distinct-subgoals ctxt raw-st =
  let
    val (st, inner-ctxt) = fix-schematics ctxt raw-st;
    val subgoals = Drule.cprems-of st;
    val atomize = Conv.fconv-rule (Object-Logic.atomize-prems inner-ctxt);

    val rules =
      map (atomize o Raw-Simplifier.norm-hhf inner-ctxt o Thm.assume) subgoals
      |> sort (int-ord o apply2 Thm.nprems-of);

    val st' = st
      |> ALLGOALS (fn i =>
        Object-Logic.atomize-prems-tac inner-ctxt i THEN solve-tac inner-ctxt rules
      i)
      |> Seq.hd;

    val subgoals' = subgoals
      |> inter (op aconv) (Thm.chyps-of st')
      |> distinct (op aconv);
  in
    Drule.implies-intr-list subgoals' st'
    |> singleton (Variable.export inner-ctxt ctxt)
  end;

(* Variant of filter-prems-tac that recovers premise order *)
fun filter-prems-tac' ctxt pred =
  let
    fun Then NONE tac = SOME tac
      | Then (SOME tac) tac' = SOME (tac THEN' tac');
    fun thins H (tac, n, i) =
      (if pred H then (tac, n + 1, i)
       else (Then tac (rotate-tac n THEN' eresolve-tac ctxt [thin-rl]), 0, i + n));
  in
    SUBGOAL (fn (goal, i) =>
      let val Hs = Logic.strip-assums-hyp goal in
        (case fold thins Hs (NONE, 0, 0) of
          (NONE, -, -) => no-tac
          | (SOME tac, -, n) => tac i THEN rotate-tac (~ n) i)
        end)
    end;
end;

```

```

fun trim-prems-tac ctxt rules =
let
  fun matches (prem,rule) =
  let
    val ((-,prem'),ctxt') = Variable.focus NONE prem ctxt;
    val rule-prop = Thm.prop-of rule;
  in Unify.matches-list (Context.Proof ctxt') [rule-prop] [prem'] end;

in filter-prems-tac' ctxt (not o member matches rules) end;

val adhoc-conjunction-tac = REPEAT-ALL-NEW
  (SUBGOAL (fn (goal, i) =>
    if can Logic.dest-conjunction (Logic.strip-imp-concl goal)
    then resolve0-tac [Conjunction.conjunctionI] i
    else no-tac));

fun unfold-subgoals-tac ctxt =
  TRY (adhoc-conjunction-tac 1)
  THEN (PRIMITIVE (Raw-Simplifier.norm-hhf ctxt));

val - =
  Theory.setup
    (Method.setup @{binding fold-subgoals}
      (Scan.lift (Args.mode prefix) >> (fn prefix => fn ctxt =>
        SIMPLE-METHOD (PRIMITIVE (fold-subgoals ctxt prefix))))
      lift all subgoals over common premises/params #>
    Method.setup @{binding unfold-subgoals}
      (Scan.succeed (fn ctxt => SIMPLE-METHOD (unfold-subgoals-tac ctxt)))
      recover subgoals after folding #>
    Method.setup @{binding distinct-subgoals}
      (Scan.succeed (fn ctxt => SIMPLE-METHOD (PRIMITIVE (distinct-subgoals
        ctxt)))))
    trim all subgoals to be (logically) distinct #>
  Method.setup @{binding trim}
    (Attrib.thms >> (fn thms => fn ctxt =>
      SIMPLE-METHOD (HEADGOAL (trim-prems-tac ctxt thms))))
    trim all premises that match the given rules);

end;
}

end

theory Rule-By-Method
imports
  Main
  HOL-Eisbach.Eisbach-Tools
begin

```

```

ML <
signature RULE-BY-METHOD =
sig
  val rule-by-tac: Proof.context -> {vars : bool, prop: bool} ->
    (Proof.context -> tactic) -> (Proof.context -> tactic) list -> Position.T
-> thm
end;

fun atomize ctxt = Conv.fconv-rule (Object-Logic.atomize ctxt);

fun fix-schematics ctxt raw-st =
  let
    val ((schematic-types, [st']), ctxt1) = Variable.importT [raw-st] ctxt;
    fun certify-inst ctxt inst = map (apsnd (Thm.ctrm-of ctxt)) (#2 inst)
    val (schematic-terms, ctxt2) =
      Variable.import-inst true [Thm.prop-of st'] ctxt1
    |>> certify-inst ctxt1;
    val schematics = (schematic-types, schematic-terms);
  in (Thm.instantiate schematics st', ctxt2) end

fun curry-asm ctxt st = if Thm.nprems-of st = 0 then Seq.empty else
  let
    val prems = Thm.cprem-of st 1 |> Thm.term-of |> Logic.strip-imp-prems;

    val (thesis :: xs, ctxt') = Variable.variant-fixes (thesis :: replicate (length prems)
P) ctxt;

    val rl =
      xs
      |> map (fn x => Thm.ctrm-of ctxt' (Free (x, propT)))
      |> Conjunction.mk-conjunction-balanced
      |> (fn xs => Thm.apply (Thm.apply @ {ctrm Pure.imp} xs) (Thm.ctrm-of
ctxt' (Free (thesis, propT))))
      |> Thm.assume
      |> Conjunction.curry-balanced (length prems)
      |> Drule.implies-intr-hyps

    val rl' = singleton (Variable.export ctxt' ctxt) rl;

    in Thm.bicompose (SOME ctxt) {flatten = false, match = false, incremented =
false}
      (false, rl', 1) 1 st end;

val drop-trivial-imp =
  let
    val asm =

```



```

    Thm.assume (Drule.protect @{cprop (PROP A ==> PROP A) ==> PROP A})
|> Goal.conclude;

in
  Thm.implies-elim asm (Thm.trivial @{cprop PROP A})
|> Drule.implies-intr-hyps
|> Thm.generalize ([], [A]) 1
|> Drule.zero-var-indices
end

val drop-trivial-imp' =
let
  val asm =
    Thm.assume (Drule.protect @{cprop (PROP P ==> A) ==> A})
|> Goal.conclude;

  val asm' = Thm.assume @{cprop PROP P == Trueprop A}

in
  Thm.implies-elim asm (asm' COMP Drule.equal-elim-rule1)
|> Thm.implies-elim (asm' COMP Drule.equal-elim-rule2)
|> Drule.implies-intr-hyps
|> Thm.permute-prems 0 ~ 1
|> Thm.generalize ([], [A, P]) 1
|> Drule.zero-var-indices
end

fun atomize-equiv-tac ctxt i =
  Object-Logic.full-atomize-tac ctxt i
  THEN PRIMITIVE (fn st' =>
    let val (-, [A, -]) = Drule.strip-comb (Thm.cprem-of st' i) in
    if Object-Logic.is-judgment ctxt (Thm.term-of A) then st'
    else error (Failed to fully atomize result:\n ^ (Syntax.string-of-term ctxt (Thm.term-of
A))) end)

structure Data = Proof-Data
(
  type T = thm list * bool;
  fun init - = ([], false);
);

val empty-rule-prems = Data.map (K ([], true));

fun add-rule-prem thm = Data.map (apfst (Thm.add-thm thm));

fun with-rule-prems enabled parse =
  Scan.state :| |-- (fn context =>
    let

```

```

    val context' = Context.proof-of context |> Data.map (K ([Drule.free-dummy-thm],enabled))
    |> Context.Proof
  in Scan.lift (Scan.pass context' parse) end

fun get-rule-prems ctxt =
  let
    val (thms,b) = Data.get ctxt
  in if (not b) then [] else thms end

fun zip-subgoal assume tac (ctxt,st : thm) = if Thm.nprems-of st = 0 then Seq.single (ctxt,st) else
  let
    fun bind-prems st' =
      let
        val prems = Drule.cprems-of st';
        val (asms, ctxt') = Assumption.add-assumes prems ctxt;
        val ctxt'' = fold add-rule-prem asms ctxt';
        val st'' = Goal.conclude (Drule.implies-elim-list st' (map Thm.assume prems));
      in (ctxt'',st'') end

    fun defer-prems st' =
      let
        val nprems = Thm.nprems-of st';
        val st'' = Thm.permute-prems 0 nprems (Goal.conclude st');
      in (ctxt,st'') end;
  in

in
  tac ctxt (Goal.protect 1 st)
  |> Seq.map (if assume then bind-prems else defer-prems) end

fun zip-subgoals assume tacs pos ctxt st =
  let
    val nprems = Thm.nprems-of st;
    val - = nprems < length tacs andalso error (More tactics than rule assumptions
    ^ Position.here pos);
    val tacs' = map (zip-subgoal assume) (tacs @ (replicate (nprems - length tacs)
    (K all-tac)));
    val ctxt' = empty-rule-prems ctxt;
  in Seq.EVERY tacs' (ctxt',st) end;

fun rule-by-tac' ctxt {vars,prop} tac asm-tacs pos raw-st =
  let
    val (st,ctxt1) = if vars then (raw-st,ctxt) else fix-schematics ctxt raw-st;

    val ([x],ctxt2) = Proof-Context.add-fixes [(Binding.name Auto-Bind.thesisN,NONE,

```

```

NoSyn)] ctxt1;

val thesis = if prop then Free (x,propT) else Object-Logic.fixed-judgment ctxt2
x;

val cthesis = Thm.ctrm-of ctxt thesis;

val revcut-rl' = Thm.instantiate' [] ([NONE,SOME cthesis]) @ {thm revcut-rl};

fun is-thesis t = Logic.strip-assums-concl t aconv thesis;

fun err thm str = error (str ^ Position.here pos ^ \n ^
(Pretty.string-of (Goal-Display.pretty-goal ctxt thm)));

fun pop-thesis st =
let
  val prems = Thm.prem-of st |> tag-list 0;
  val (i,-) = (case filter (is-thesis o snd) prems of
    [] => err st Lost thesis
    | [x] => x
    | - => err st More than one result obtained);
in st |> Thm.permute-prems 0 i end

val asm-st =
(revcut-rl' OF [st])
|> (fn st => Goal.protect (Thm.nprems-of st - 1) st)

val (ctxt3,concl-st) = case Seq.pull (zip-subgoals (not vars) asm-tacs pos ctxt2
asm-st) of
  SOME (x,-) => x
  | NONE => error (Failed to apply tactics to rule assumptions. ^ (Position.here
pos));

val concl-st-prepped =
  concl-st
  |> Goal.conclude
  |> (fn st => Goal.protect (Thm.nprems-of st) st |> Thm.permute-prems 0
~ 1 |> Goal.protect 1)

val concl-st-result = concl-st-prepped
  |> (tac ctxt3
    THEN (PRIMITIVE pop-thesis)
    THEN curry-asm ctxt
    THEN PRIMITIVE (Goal.conclude #> Thm.permute-prems 0 1 #>
Goal.conclude))

val result = (case Seq.pull concl-st-result of
  SOME (result,-) => singleton (Proof-Context.export ctxt3 ctxt) result

```

```

| NONE => err concl-st-prepped Failed to apply tactic to rule conclusion:)

val drop-rule = if prop then drop-trivial-imp else drop-trivial-imp'

val result' = ((Goal.protect (Thm.nprems-of result - 1) result) RS drop-rule)
|> (if prop then all-tac else
    (atomize-equiv-tac ctxt (Thm.nprems-of result)
     THEN resolve-tac ctxt @{thms Pure.reflexive} (Thm.nprems-of result)))
|> Seq.hd
|> Raw-Simplifier.norm-hhf ctxt

in Drule.zero-var-indexes result' end;

fun rule-by-tac is-closed ctxt args tac asm-tacs pos raw-st =
  let val f = rule-by-tac' ctxt args tac asm-tacs pos
  in
    if is-closed orelse Context-Position.is-really-visible ctxt then SOME (f raw-st)
    else try f raw-st
  end

fun pos-closure (scan : 'a context-parser) :
  (('a * (Position.T * bool)) context-parser) = (fn (context,toks) =>
    let
      val (((context',x),tr-toks),toks') = Scan.trace (Scan.pass context (Scan.state
-- scan)) toks;
      val pos = Token.range-of tr-toks;
      val is-closed = exists (fn t => is-some (Token.get-value t)) tr-toks
    in ((x,(Position.range-position pos, is-closed)),(context',toks')) end)

val parse-flags = Args.mode schematic -- Args.mode raw-prop >> (fn (b,b') =>
  {vars = b, prop = b'})

fun tac m ctxt =
  Method.NO-CONTEXT-TACTIC ctxt
  (Method.evaluate-runtime m ctxt []);

(* Declare as a mixed attribute to avoid any partial evaluation *)

fun handle-dummy f (context, thm) =
  case (f context thm) of SOME thm' => (NONE, SOME thm')
  | NONE => (SOME context, SOME Drule.free-dummy-thm)

val (rule-prems-by-method : attribute context-parser) = Scan.lift parse-flags :--
(fn flags =>
  pos-closure (Scan.repeat1
    (with-rule-prems (not (#vars flags)) Method.text-closure ||
      Scan.lift (Args.$$$ - >> (K Method.succeed-text)))) >>
    (fn (flags,(ms,(pos, is-closed))) => handle-dummy (fn context =>
      rule-by-tac is-closed (Context.proof-of context) flags (K all-tac) (map tac

```

```

ms) pos))

val (rule-concl-by-method : attribute context-parser) = Scan.lift parse-flags :--
(fn flags =>
  pos-closure (with-rule-prems (not (#vars flags)) Method.text-closure)) >>
  (fn (flags,(m,(pos, is-closed))) => handle-dummy (fn context =>
    rule-by-tac is-closed (Context.proof-of context) flags (tac m) [] pos))

val - = Theory.setup
  (Global-Theory.add-thms-dynamic (@{binding rule-prems},
    (fn context => get-rule-prems (Context.proof-of context))) #>
  Attrib.setup @{binding #} rule-prems-by-method
    transform rule premises with method #>
  Attrib.setup @{binding @} rule-concl-by-method
    transform rule conclusion with method #>
  Attrib.setup @{binding atomized}
    (Scan.succeed (Thm.rule-attribute []
      (fn context => fn thm =>
        Conv.fconv-rule (Object-Logic.atomize (Context.proof-of context)) thm
          |> Drule.zero-var-indexes)))
    atomize rule)
)

```

experiment begin

```

ML <
  val [att] = @{@erule thin-rl, cut-tac TrueI, fail}}
  val k = Attrib.attribute @{context} att
  val - = case (try k (Context.Proof @{context}, Drule.dummy-thm)) of
    SOME - => error Should fail
    | - => ()
)

```

lemmas baz = [[@{@erule thin-rl, rule revcut-rl[of $P \longrightarrow P \wedge P$], simp}]] **for** P

lemmas bazz[*THEN impE*] = TrueI[@{@erule thin-rl, rule revcut-rl[of $P \longrightarrow P \wedge P$], simp}] **for** P

lemma $Q \longrightarrow Q \wedge Q$ **by** (rule baz)

method silly-rule **for** $P :: \text{bool}$ **uses** rule =
 (rule [[@{@erule thin-rl, cut-tac rule, drule asm-rl[of P]}]])

lemma assumes A **shows** A **by** (silly-rule A rule: $\langle A \rangle$)

lemma assumes A [simp]: A **shows** A
apply (match **conclusion** in P **for** $P \Rightarrow$
 $\langle \text{rule } [[@{@erule thin-rl, rule revcut-rl[of P], simp}]] \rangle$)
done

end

end

```
theory Local-Method
imports Main
keywords supply-local-method :: prf-script % proof
begin
```

See documentation in `Local_Method_Tests.thy`.

ML <

```
  structure MethodData = Proof-Data(
    type T = Method.method Symtab.table
    val init = K Symtab.empty);
```

>

```
method-setup local-method = <
  Scan.lift Parse.liberal-name >>
  (fn name => fn - => fn facts => fn (ctxt, st) =>
    case (ctxt |> MethodData.get |> Symtab.lookup) name of
      SOME method => method facts (ctxt, st)
    | NONE => Seq.succeed (Seq.Error (K (Couldn't find method text named ^
quote name))))))
>
```

ML <

local

```
val parse-name-text-ranges =
  Scan.repeat1 (Parse.liberal-name --| Parse.!!! @ {keyword = } -- Method.parse)
```

```
fun supply-method-cmd name-text-ranges ctxt =
  let
    fun add-method ((name, (text, range)), ctxt) =
      let
        val - = Method.report (text, range)
        val method = Method.evaluate text ctxt
      in
        MethodData.map (Symtab.update (name, method)) ctxt
      end
  in
    List.foldr add-method ctxt name-text-ranges
  end
```

val - =

```
Outer-Syntax.command @ {command-keyword (supply-local-method)}
  Add a local method alias to the current proof context
```

```

    (parse-name-text-ranges >> (Toplevel.proof o Proof.map-context o supply-method-cmd))

in end
)

end

```

```

theory Eisbach-Methods
imports
  subgoal-focus/Subgoal-Methods
  HOL-Eisbach.Eisbach-Tools
  Rule-By-Method
  Local-Method
begin

```

3 Debugging methods

```

method print-concl = (match conclusion in P for P  $\Rightarrow$   $\langle$ print-term P $\rangle$ )

```

```

method-setup print-raw-goal =  $\langle$ Scan.succeed (fn ctxt  $\Rightarrow$  fn facts  $\Rightarrow$ 
  (fn (ctxt, st)  $\Rightarrow$  (Output.writeln (Thm.string-of-thm ctxt st);
    Seq.make-results (Seq.single (ctxt, st)))) $\rangle$ 

```

```

ML  $\langle$ fun method-evaluate text ctxt facts =
  Method.NO-CONTEXT-TACTIC ctxt
  (Method.evaluate-runtime text ctxt facts) $\rangle$ 

```

```

method-setup print-headgoal =
   $\langle$ Scan.succeed (fn ctxt  $\Rightarrow$ 
    fn -  $\Rightarrow$  fn (ctxt', thm)  $\Rightarrow$ 
      ((SUBGOAL (fn (t, -)  $\Rightarrow$ 
        (Output.writeln
          (Pretty.string-of (Syntax.pretty-term ctxt t)); all-tac)) 1 thm);
        Seq.make-results (Seq.single (ctxt', thm)))) $\rangle$ 

```

4 Simple Combinators

```

method-setup defer-tac =  $\langle$ Scan.succeed (fn -  $\Rightarrow$  SIMPLE-METHOD (defer-tac
  1)) $\rangle$ 

```

```

method-setup prefer-last =  $\langle$ Scan.succeed (fn -  $\Rightarrow$  SIMPLE-METHOD (PRIMITIVE
  (Thm.permute-prems 0  $\sim$  1))) $\rangle$ 

```

```

method-setup all =
   $\langle$ Method.text-closure >> (fn m  $\Rightarrow$  fn ctxt  $\Rightarrow$  fn facts  $\Rightarrow$ 

```

```

let
  fun tac i st' =
    Goal.restrict i 1 st'
    |> method-evaluate m ctxt facts
    |> Seq.map (Goal.unrestrict i)

in SIMPLE-METHOD (ALLGOALS tac) facts end)
)

method-setup determ =
  ⟨Method.text-closure >> (fn m => fn ctxt => fn facts =>
    let
      fun tac st' = method-evaluate m ctxt facts st'

in SIMPLE-METHOD (DETERM tac) facts end)
  ⟩ ⟨Run the given method, but only yield the first result⟩

ML ⟨
  fun require-determ (method : Method.method) facts st =
    case method facts st |> Seq.filter-results |> Seq.pull of
      NONE => Seq.empty
    | SOME (r1, rs) =>
      (case Seq.pull rs of
        NONE => Seq.single r1 |> Seq.make-results
      | - => Method.fail facts st);

  fun require-determ-method text ctxt =
    require-determ (Method.evaluate-runtime text ctxt);
  )

method-setup require-determ =
  ⟨Method.text-closure >> require-determ-method⟩
  ⟨Run the given method, but fail if it returns more than one result⟩

method-setup changed =
  ⟨Method.text-closure >> (fn m => fn ctxt => fn facts =>
    let
      fun tac st' = method-evaluate m ctxt facts st'

in SIMPLE-METHOD (CHANGED tac) facts end)
  ⟩

method-setup timeit =
  ⟨Method.text-closure >> (fn m => fn ctxt => fn facts =>
    let
      fun timed-tac st seq = Seq.make (fn () => Option.map (apsnd (timed-tac st))
        (timeit (fn () => (Seq.pull seq)))));

```



```

    fun tac st' =
      timed-tac st' (method-evaluate m ctxt facts st');

  in SIMPLE-METHOD tac [] end)
)

method-setup timeout =
  ⟨Scan.lift Parse.int -- Method.text-closure >> (fn (i,m) => fn ctxt => fn facts
=>
  let
    fun str-of-goal th = Pretty.string-of (Goal-Display.pretty-goal ctxt th);

    fun limit st f x = Timeout.apply (Time.fromSeconds i) f x
      handle Timeout.TIMEOUT - => error (Method timed out:\n ^ (str-of-goal
st));

    fun timed-tac st seq = Seq.make (limit st (fn () => Option.map (apsnd
(timed-tac st))
      (Seq.pull seq)));

    fun tac st' =
      timed-tac st' (method-evaluate m ctxt facts st');

  in SIMPLE-METHOD tac [] end)
)

```

```

method repeat-new methods m = (m ; (repeat-new ⟨m⟩)?)

```

The following *fails* and *succeeds* methods protect the goal from the effect of a method, instead simply determining whether or not it can be applied to the current goal. The *fails* method inverts success, only succeeding if the given method would fail.

```

method-setup fails =
  ⟨Method.text-closure >> (fn m => fn ctxt => fn facts =>
  let
    fun fail-tac st' =
      (case Seq.pull (method-evaluate m ctxt facts st') of
        SOME - => Seq.empty
        | NONE => Seq.single st')

    in SIMPLE-METHOD fail-tac facts end)
  )

```

```

method-setup succeeds =
  ⟨Method.text-closure >> (fn m => fn ctxt => fn facts =>
  let
    fun can-tac st' =
      (case Seq.pull (method-evaluate m ctxt facts st') of

```

```

    SOME (st'',-) => Seq.single st'
  | NONE => Seq.empty)

  in SIMPLE-METHOD can-tac facts end)
)

```

This method wraps up the "focus" mechanic of match without actually doing any matching. We need to consider whether or not there are any assumptions in the goal, as premise matching fails if there are none.

If the *fails* method is removed here, then backtracking will produce a set of invalid results, where only the conclusion is focused despite the presence of subgoal premises.

```

method focus-concl methods m =
  ((fails ⟨rule thin-rl⟩, match conclusion in - => ⟨m⟩)
  | match premises (local) in H:- (multi) => ⟨m⟩)

```

repeat applies a method a specific number of times, like a bounded version of the '+' combinator.

usage: apply (repeat n *text*)

- Applies the method *text* to the current proof state n times. - Fails if *text* can't be applied n times.

```

ML ⟨
  fun repeat-tac count tactic =
    if count = 0
    then all-tac
    else tactic THEN (repeat-tac (count - 1) tactic)
  ⟩

```

```

method-setup repeat = ⟨
  Scan.lift Parse.nat -- Method.text-closure >> (fn (count, text) => fn ctxt =>
  fn facts =>
    let val tactic = method-evaluate text ctxt facts
    in SIMPLE-METHOD (repeat-tac count tactic) facts end)
  ⟩

```

```

notepad begin
  fix A B C
  assume assms: A B C

```

repeat: simple repeated application.

```

have A ∧ B ∧ C ∧ True

```

repeat: fails if method can't be applied the specified number of times.

```

apply (fails ⟨repeat 4 ⟨rule conjI, rule assms⟩⟩)
apply (repeat 3 ⟨rule conjI, rule assms⟩)
by (rule TrueI)

```

repeat: application with subgoals.

```
have  $A \wedge A \ B \wedge B \ C \wedge C$ 
apply  $-$ 
```

We have three subgoals. This *repeat* call consumes two of them.

```
apply (repeat 2 (rule conjI, (rule assms) $+$ ))
```

One subgoal remaining...

```
apply (rule conjI, (rule assms) $+$ )
done
```

end

Literally a copy of the parser for *subgoal-tac* composed with an analogue of **prefer**.

Useful if you find yourself introducing many new facts via ‘*subgoal_tac*’, but *prefer* to prove them immediately.

```
setup (
  Method.setup binding (prop-tac)
  (Args.goal-spec  $--$  Scan.lift (Scan.repeat1 Args.embedded-inner-syntax  $--$ 
Parse.for-fixes)  $>>$ 
    (fn (quant, (props, fixes))  $=>$  fn ctxt  $=>$ 
      (SIMPLE-METHOD'' quant
        (EVERY' (map (fn prop  $=>$  Rule-Insts.subgoal-tac ctxt prop fixes) props)
          THEN'
            (K (prefer-tac 2))))))
    insert prop (dynamic instantiation), introducing prop subgoal first
)
```

```
notepad begin {
  fix xs
  assume assms: list-all even (xs :: nat list)

  from assms have even (sum-list xs)
  apply (induct xs)
  apply simp
```

Inserts the desired proposition as the current subgoal.

```
apply (prop-tac list-all even xs)
subgoal by simp
```

The prop *list-all even xs* is now available as an assumption. Let’s add another one.

```
apply (prop-tac even (sum-list xs))
subgoal by simp
```

Now that we’ve proven our introduced props, use them!

```
apply clarsimp
```

```

    done
  }
end

```

5 Advanced combinators

5.1 Protecting goal elements (assumptions or conclusion) from methods

```

context
begin

private definition protect-concl  $x \equiv \neg x$ 
private definition protect-false  $\equiv \text{False}$ 

private lemma protect-start:  $(\text{protect-concl } P \implies \text{protect-false}) \implies P$ 
  by (simp add: protect-concl-def protect-false-def) (rule ccontr)

private lemma protect-end:  $\text{protect-concl } P \implies P \implies \text{protect-false}$ 
  by (simp add: protect-concl-def protect-false-def)

method only-asm methods  $m =$ 
  (match premises in  $H[\text{thin}]$ :- (multi, cut)  $\Rightarrow$ 
    ⟨rule protect-start,
     match premises in  $H'[\text{thin}]$ :protect-concl -  $\Rightarrow$ 
     ⟨insert  $H, m$ ; rule protect-end[OF  $H' \rangle \rangle$ )

method only-concl methods  $m = (\text{focus-concl } \langle m \rangle)$ 

end

notepad begin
fix  $D C$ 
  assume  $DC:D \implies C$ 
  have  $D \wedge D \implies C \wedge C$ 
  apply (only-asm ⟨simp⟩) — stash conclusion before applying method
  apply (only-concl ⟨simp add: DC⟩) — hide premises from method
  by (rule DC)
end

```

5.2 Safe subgoal folding (avoids expanding meta-conjuncts)

Isabelle’s goal mechanism wants to aggressively expand meta-conjunctions if they are the top-level connective. This means that *fold-subgoals* will immediately be unfolded if there are no common assumptions to lift over.

To avoid this we simply wrap conjunction inside of *conjunction’* to hide it from the usual facilities.

context begin

definition

conjunction' :: *prop* \Rightarrow *prop* \Rightarrow *prop* (**infixr** & ^& 2) **where**
conjunction' *A B* \equiv (*PROP A* &&& *PROP B*)

In general the context antiquotation does not work in method definitions.

Here it is fine because `Conv.topsweepconvconvisjustover–specifiedtoneedaProof.contextwhenanything`

method *safe-meta-conjuncts* =

raw-tactic
 ⟨*REPEAT-DETERM*
 (*CHANGED-PROP*
 (*PRIMITIVE*
 (*Conv.gconv-rule* ((*Conv.top-sweep-conv* (*K* (*Conv.rewr-conv* @{*thm conjunction'-def*[*symmetric*]})) @{*context*}}) 1)))⟩

method *safe-fold-subgoals* = (*fold-subgoals* (*prefix*), *safe-meta-conjuncts*)

lemma *atomize-conj'* [*atomize*]: (*A* & ^& *B*) == *Trueprop* (*A* & *B*)
by (*simp add: conjunction'-def, rule atomize-conj*)

lemma *context-conjunction'I*:

PROP P \Longrightarrow (*PROP P* \Longrightarrow *PROP Q*) \Longrightarrow *PROP P* & ^& *PROP Q*
apply (*simp add: conjunction'-def*)
apply (*rule conjunctionI*)
apply *assumption*
apply (*erule meta-mp*)
apply *assumption*
done

lemma *conjunction'I*:

PROP P \Longrightarrow *PROP Q* \Longrightarrow *PROP P* & ^& *PROP Q*
by (*rule context-conjunction'I; simp*)

lemma *conjunction'E*:

assumes *PQ*: *PROP P* & ^& *PROP Q*
assumes *PQR*: *PROP P* \Longrightarrow *PROP Q* \Longrightarrow *PROP R*
shows
PROP R
apply (*rule PQR*)
apply (*rule PQ*[*simplified conjunction'-def, THEN conjunctionD1*])
by (*rule PQ*[*simplified conjunction'-def, THEN conjunctionD2*])

end

notepad begin

fix *D C E*

assume *DC*: *D* \wedge *C*

```

have  $D \ C \wedge C$ 
apply  $-$ 
apply (safe-fold-subgoals, simp, atomize (full))
apply (rule  $DC$ )
done

end

```

6 Utility methods

6.1 Finding a goal based on successful application of a method

context begin

```

method-setup find-goal =
   $\langle \text{Method.text-closure} \gg (fn \ m \Rightarrow fn \ ctxt \Rightarrow fn \ facts \Rightarrow$ 
    let
      fun prefer-first  $i = SELECT-GOAL$ 
        (fn  $st' \Rightarrow$ 
          (case  $Seq.pull \ (method-evaluate \ m \ ctxt \ facts \ st') \ of$ 
             $SOME \ (st'', -) \Rightarrow Seq.single \ st''$ 
             $| \ NONE \Rightarrow Seq.empty$ )  $i \ THEN \ prefer-tac \ i$ 
          )
        )
      in  $SIMPLE-METHOD \ (FIRSTGOAL \ prefer-first) \ facts \ end$ )
   $\rangle$ 

end

```

notepad begin

```

fix  $A \ B$ 
assume  $A: A \ \text{and} \ B: B$ 

have  $A \ A \ B$ 
  apply (find-goal  $\langle match \ conclusion \ in \ B \Rightarrow \langle - \rangle \rangle$ )
  apply (rule  $B$ )
  by (rule  $A$ ) $+$ 

have  $A \wedge A \ A \wedge A \ B$ 
  apply (find-goal  $\langle fails \ \langle simp \rangle \rangle$ ) — find the first goal which cannot be simplified
  apply (rule  $B$ )
  by (simp add:  $A$ ) $+$ 

have  $B \ A \ A \wedge A$ 
  apply (find-goal  $\langle succeeds \ \langle simp \rangle \rangle$ ) — find the first goal which can be simplified
  (without doing so)
  apply (rule conjI)
  by (rule  $A \ B$ ) $+$ 

end

```

6.2 Remove redundant subgoals

Tries to solve subgoals by assuming the others and then using the given method. Backtracks over all possible re-orderings of the subgoals.

context begin

definition *protect* (*PROP P*) $\equiv P$

lemma *protectE*: *PROP protect P* \implies (*PROP P* \implies *PROP R*) \implies *PROP R* **by** (*simp add: protect-def*)

private lemmas *protect-thin* = *thin-rl*[**where** *V=PROP protect P for P*]

private lemma *context-conjunction'I-protected*:

assumes *P: PROP P*

assumes *PQ: PROP protect (PROP P) \implies PROP Q*

shows

PROP P & \wedge *PROP Q*

apply (*simp add: conjunction'-def*)

apply (*rule P*)

apply (*rule PQ*)

apply (*simp add: protect-def*)

by (*rule P*)

private lemma *conjunction'-sym*: *PROP P* & \wedge *PROP Q* \implies *PROP Q* & \wedge *PROP P*

apply (*simp add: conjunction'-def*)

apply (*frule conjunctionD1*)

apply (*drule conjunctionD2*)

apply (*rule conjunctionI*)

by *assumption+*

private lemmas *context-conjuncts'I* =

context-conjunction'I-protected

context-conjunction'I-protected[*THEN conjunction'-sym*]

method *distinct-subgoals-strong* **methods** *m* =

(*safe-fold-subgoals*,

(*intro context-conjuncts'I*;

((*elim protectE conjunction'E*)?, *solves* $\langle m \rangle$)

| (*elim protect-thin*)?)))?

end

method *forward-solve* **methods** *fwd m* =

(*fwd*, *prefer-last*, *fold-subgoals*, *safe-meta-conjuncts*, *rule conjunction'I*,

defer-tac, ((*intro conjunction'I*)?, *solves* $\langle m \rangle$))[1]

method *frule-solve* **methods** *m* **uses** *rule* = (*forward-solve* $\langle \text{frule rule} \rangle \langle m \rangle$)
method *drule-solve* **methods** *m* **uses** *rule* = (*forward-solve* $\langle \text{drule rule} \rangle \langle m \rangle$)

notepad begin

```
{
fix A B C D E
assume ABCD: A  $\implies$  B  $\implies$  C  $\implies$  D
assume ACD: A  $\implies$  C  $\implies$  D
assume DE: D  $\implies$  E
assume B C

have A  $\implies$  D
apply (frule-solve (simp add:  $\langle B \rangle \langle C \rangle$ ) rule: ABCD)
apply (drule-solve (simp add:  $\langle B \rangle \langle C \rangle$ ) rule: ACD)
apply (match premises in A  $\Rightarrow$   $\langle \text{fail} \rangle$  | -  $\Rightarrow$   $\langle - \rangle$ )
apply assumption
done
}
end
```

notepad begin

```
{
fix A B C
assume A: A
have A B  $\implies$  A
apply -
apply (distinct-subgoals-strong  $\langle \text{assumption} \rangle$ )
by (rule A)

have B  $\implies$  A A
by (distinct-subgoals-strong  $\langle \text{assumption} \rangle$ , rule A) — backtracking required here
}

{
fix A B C

assume B: B
assume BC: B  $\implies$  C B  $\implies$  A
have A B  $\longrightarrow$  (A  $\wedge$  C) B
apply (distinct-subgoals-strong  $\langle \text{simp} \rangle$ , rule B) — backtracking required here
by (simp add: BC)

}
end
```


7 Attribute methods (for use with `rule_by_method_attributes`)

```

method prove-prop-raw for  $P :: prop$  methods  $m =$ 
  (erule thin-rl, rule revcut-rl[of PROP P],
   solves match conclusion in -  $\Rightarrow$   $\langle m \rangle$ )

method prove-prop for  $P :: prop = (prove-prop-raw PROP P \langle auto \rangle)$ 

experiment begin

lemma assumes  $A[simp]: A$  shows  $A$  by (rule [[@(prove-prop A)]])

end

```

8 Shortcuts for `prove_prop`. *Not these are less efficient than using the raw syntax proven every time.*

```

method ruleP for  $P :: prop = (catch \langle rule \text{ [[}@ (prove-prop PROP P) ] \rangle \langle fail \rangle$ 
method insertP for  $P :: prop = (catch \langle insert \text{ [[}@ (prove-prop PROP P) ] \rangle \langle fail \rangle$ )[1]

experiment begin

lemma assumes  $A[simp]: A$  shows  $A$  by (ruleP False | ruleP A)
lemma assumes  $A: A$  shows  $A$  by (ruleP  $\wedge P. P \Rightarrow P \Rightarrow P$ , rule A, rule A)

end

context begin

private definition bool-protect ( $b::bool$ )  $\equiv b$ 

lemma bool-protectD:
  bool-protect P  $\Rightarrow$  P
  unfolding bool-protect-def by simp

lemma bool-protectI:
  P  $\Rightarrow$  bool-protect P
  unfolding bool-protect-def by simp

```

When you want to apply a rule/tactic to transform a potentially complex goal into another one manually, but want to indicate that any fresh emerging goals are solved by a more brutal method. E.g. `apply (solves_ergingfrule $x=...$ in my-rulefastforce s)`

```

method solves-emerging methods  $m1\ m2 = (rule\ bool-protectD,\ (m1\ ;\ (rule\$ 
bool-protectI | ( $m2$ ; fail)))

end

end

```

theory *Try-Methods*

imports *Eisbach-Methods*

keywords *trym* :: *diag*
 and *add-try-method* :: *thy-decl*

begin

A collection of methods that can be "tried" against subgoals (similar to *try*, *try0* etc). It is easy to add new methods with "*add_ttry_mmethod*", *although the parser currently supports only one method*. Particular subgoals can be tried with "*trym 1*" etc. By default all subgoals are attempted unless they are coupled to others by shared schematic variables.

ML <

structure Try-Methods = struct

structure Methods = Theory-Data

(
 type T = Symtab.set;
 val empty = Symtab.empty;
 val extend = I;
 val merge = Symtab.merge (K true);
);

val get-methods-global = Methods.get #> Symtab.keys
val add-method = Methods.map o Symtab.insert-set

(* borrowed from *try0* implementation (of course) *)

fun parse-method-name keywords =
 enclose (
 #> Token.explode keywords Position.start
 #> filter Token.is-proper
 #> Scan.read Token.stopper Method.parse
 #> (fn SOME (Method.Source src, -) => src | - => raise Fail expected Source);

fun mk-method ctxt = parse-method-name (Thy-Header.get-keywords' ctxt)
 #> Method.method-cmd ctxt
 #> Method.Basic

fun get-methods ctxt = get-methods-global (Proof-Context.theory-of ctxt)
 |> map (mk-method ctxt)

fun try-one-method m ctxt n goal
 = can (Timeout.apply (Time.fromSeconds 5)
 (Goal.restrict n 1 #> Method.NO-CONTEXT-TACTIC ctxt
 (Method.evaluate-runtime m ctxt []))

```

    #> Seq.hd
  )) goal

fun msg m-nm n = writeln (method ^ m-nm ^ succeeded on goal ^ string-of-int
n)

fun times xs ys = maps (fn x => map (pair x) ys) xs

fun independent-subgoals goal verbose = let
  fun get-vars t = Term.fold-aterms
    (fn (Var v) => Termtab.insert-set (Var v) | - => I)
    t Termtab.empty
  val goals = Thm.premis-of goal
  val goal-vars = map get-vars goals
  val count-vars = fold (fn t1 => fn t2 => Termtab.join (K (+))
    (Termtab.map (K (K 1)) t1, t2)) goal-vars Termtab.empty
  val indep-vars = Termtab.forall (fst #> Termtab.lookup count-vars
    #> (fn n => n = SOME 1))
  val indep = (1 upto Thm.nprems-of goal) ~~ map indep-vars goal-vars
  val - = app (fst #> string-of-int
    #> prefix ignoring non-independent goal #> warning)
    (filter (fn x => verbose andalso not (snd x)) indep)
  in indep |> filter snd |> map fst end

fun try-methods opt-n ctxt goal = let
  val ms = get-methods-global (Proof-Context.theory-of ctxt)
    ~~ get-methods ctxt
  val ns = case opt-n of
    NONE => independent-subgoals goal true
  | SOME n => [n]
  fun apply ((m-nm, m), n) = if try-one-method m ctxt n goal
    then (msg m-nm n; SOME (m-nm, n)) else NONE
  val results = Par-List.map apply (times ms ns)
  in map-filter I results end

fun try-methods-command opt-n st = let
  val ctxt = #context (Proof.goal st)
  |> Try0.silence-methods false
  val goal = #goal (Proof.goal st)
  in try-methods opt-n ctxt goal; () end

val - = Outer-Syntax.command @{command-keyword trym}
  try methods from a library of specialised strategies
  (Scan.option Parse.int >> (fn opt-n =>
    Toplevel.keep-proof (try-methods-command opt-n o Toplevel.proof-of)))

fun local-check-add-method nm ctxt =
  (mk-method ctxt nm; Local-Theory.background-theory (add-method nm) ctxt)

```

```

val - = Outer-Syntax.command @{command-keyword add-try-method}
  add a method to a library of strategies tried by trym
  (Parse.name >> (Toplevel.local-theory NONE NONE o local-check-add-method))

end
)

add-try-method fastforce
add-try-method blast
add-try-method metis

method auto-metis = solves (auto; metis)
add-try-method auto-metis

end

theory Extract-Conjunct
imports
  Main
  Eisbach-Methods
begin

```

9 Extracting conjuncts in the conclusion

Methods for extracting a conjunct from a nest of conjuncts in the conclusion of a goal, typically by pattern matching.

When faced with a conclusion which is a big conjunction, it is often the case that a small number of conjuncts require special attention, while the rest can be solved easily by *clarsimp*, *auto* or similar. However, sometimes the method that would solve the bulk of the conjuncts would put some of the conjuncts into a more difficult or unsolvable state.

The higher-order methods defined here provide an efficient way to select a conjunct requiring special treatment, so that it can be dealt with first. Once all such conjuncts have been removed, the remaining conjuncts can all be solved together by some automated method.

Each method takes an inner method as an argument, and selects the left-most conjunct for which that inner method succeeds. The methods differ according to what they do with the selected conjunct. See below for more information and some simple examples.

context begin

9.1 Focused conjunct with context

We define a predicate which allows us to identify a particular sub-tree and its context within a nest of conjunctions. We express this sub-tree-with-context using a function which reconstructs the original nest of conjunctions. The context consists of a list of parent contexts, where each parent context consists of a sibling sub-tree, and a tag indicating whether the focused sub-tree is on the left or right. Rebuilding the original tree works from the focused sub-tree up towards the root of the original structure. This sub-tree-with-context is sometimes known as a zipper.

```
private fun focus-conj :: bool  $\Rightarrow$  bool list  $\Rightarrow$  bool where
  focus-conj current [] = current
| focus-conj current (sibling # parents) = focus-conj (current  $\wedge$  sibling) parents
```

```
private definition focus  $\equiv$  focus-conj
```

```
private definition tag t P  $\equiv$  P
private lemmas focus-defs = focus-def tag-def
```

```
private abbreviation left  $\equiv$  tag Left
private abbreviation right  $\equiv$  tag Right
```

```
private lemma focus-example:
  focus C [right B, left D, left E, right A]  $\longleftrightarrow$  A  $\wedge$  ((B  $\wedge$  C)  $\wedge$  D)  $\wedge$  E
unfolding focus-defs by auto
```

9.2 Moving the focus

We now prove some rules which allow us to switch between focused and unfocused structures, and to move the focus around. Some versions of these rules carry an extra conjunct E outside the structure. Once we find the conjunct we want, this E allows to keep track of it while we reassemble the rest of the original structure.

First, we have rules for going between focused and unfocused structures.

```
private lemma focus-top-iff: E  $\wedge$  focus P []  $\longleftrightarrow$  E  $\wedge$  P
unfolding focus-def by simp
```

```
private lemmas to-focus = focus-top-iff [where E=True, simplified, THEN iffD1]
private lemmas from-focusE = focus-top-iff [THEN iffD2]
private lemmas from-focus = from-focusE [where E=True, simplified]
```

Next, we have rules for moving the focus to and from the left conjunct.

```
private lemma focus-left-iff: E  $\wedge$  focus L (left R # P)  $\longleftrightarrow$  E  $\wedge$  focus (L  $\wedge$  R)
P
unfolding focus-defs by simp
```

private lemmas $\text{focus-left} = \text{focus-left-iff}$ [**where** $E = \text{True}$, *simplified*, *THEN* *iffD1*]
private lemmas $\text{unfocusE-left} = \text{focus-left-iff}$ [*THEN* *iffD2*]
private lemmas $\text{unfocus-left} = \text{unfocusE-left}$ [**where** $E = \text{True}$, *simplified*]

Next, we have rules for moving the focus to and from the right conjunct.

private lemma focus-right-iff : $E \wedge \text{focus } R \text{ (right } L \# P) \longleftrightarrow E \wedge \text{focus } (L \wedge R) \text{ } P$
unfolding *focus-defs* **using** *conj-commute* **by** *simp*

private lemmas $\text{focus-right} = \text{focus-right-iff}$ [**where** $E = \text{True}$, *simplified*, *THEN* *iffD1*]
private lemmas $\text{unfocusE-right} = \text{focus-right-iff}$ [*THEN* *iffD2*]
private lemmas $\text{unfocus-right} = \text{unfocusE-right}$ [**where** $E = \text{True}$, *simplified*]

Finally, we have rules for extracting the current focus. The sibling of the extracted focus becomes the new focus of the remaining structure.

private lemma extract-focus-iff : $\text{focus } C \text{ (tag } t \text{ } S \# P) \longleftrightarrow (C \wedge \text{focus } S \text{ } P)$
unfolding *focus-defs* **by** (*induct* P *arbitrary*: S) *auto*

private lemmas $\text{extract-focus} = \text{extract-focus-iff}$ [*THEN* *iffD2*]

9.3 Primitive methods for navigating a conjunction

Using these rules as transitions, we implement a machine which navigates a tree of conjunctions, searching from left to right for a conjunct for which a given method will succeed. Once a matching conjunct is found, it is extracted, and the remaining conjuncts are reassembled.

From the current focus, move to the leftmost sub-conjunct.

private method $\text{focus-leftmost} = (\text{intro } \text{focus-left})?$

Find the furthest ancestor for which the current focus is still on the right.

private method $\text{unfocus-rightmost} = (\text{intro } \text{unfocus-right})?$

Move to the immediate-right sibling.

private method $\text{focus-right-sibling} = (\text{rule } \text{unfocus-left}, \text{rule } \text{focus-right})$

Move to the next conjunct in right-to-left ordering.

private method $\text{focus-next-conjunct} = (\text{unfocus-rightmost}, \text{focus-right-sibling}, \text{focus-leftmost})$

Search from current focus toward the right until we find a matching conjunct.

private method find-match **methods** $m = (\text{rule } \text{extract-focus}, m \mid \text{focus-next-conjunct}, \text{find-match } m)$

Search within nest of conjuncts, leaving remaining structure focused.

private method extract-match **methods** $m = (\text{rule } \text{to-focus}, \text{focus-leftmost}, \text{find-match } m)$

Move all the way out of focus, keeping track of any extracted conjunct.

private method *unfocusE* = ((*intro unfocusE-right unfocusE-left*)?, *rule from-focusE*)
private method *unfocus* = ((*intro unfocus-right unfocus-left*)?, *rule from-focus*)

9.4 Methods for selecting the leftmost matching conjunct

See the introduction at the top of this theory for motivation, and below for some simple examples.

Assuming the conclusion of the goal is a nest of conjunctions, method *lift-conjunct* finds the leftmost conjunct for which the given method succeeds, and moves it to the front of the conjunction in the goal.

method *lift-conjunct* **methods** *m* = (*extract-match* ⟨*succeeds* ⟨*rule conjI*, *m*⟩⟩, *unfocusE*)

Method *extract-conjunct* finds the leftmost conjunct for which the given method succeeds, and splits it into a fresh subgoal, leaving the remaining conjuncts untouched in the second subgoal. It is equivalent to *lift-conjunct* followed by *rule* $\llbracket ?P; ?Q \rrbracket \Longrightarrow ?P \wedge ?Q$.

method *extract-conjunct* **methods** *m* = (*extract-match* ⟨*rule conjI*, *succeeds m*⟩; *unfocus?*)

Method *apply-conjunct* finds the leftmost conjunct for which the given method succeeds, leaving any subgoals created by the application of that method, and a subgoal containing the remaining conjuncts untouched. It is equivalent to *extract-conjunct* followed by the given method, but more efficient.

method *apply-conjunct* **methods** *m* = (*extract-match* ⟨*rule conjI*, *m*⟩; *unfocus?*)

9.5 Examples

Given an inner method based on *match*, which only succeeds on the desired conjunct *C*, *lift-conjunct* moves the conjunct *C* to the front. The body of the *match* here is irrelevant, since *lift-conjunct* always discards the effect of the method it is given.

lemma $\llbracket A; B; \llbracket A; B; D; E \rrbracket \Longrightarrow C; D; E \rrbracket \Longrightarrow A \wedge ((B \wedge C) \wedge D) \wedge E$
apply (*lift-conjunct* ⟨*match conclusion in C* $\Rightarrow \langle - \rangle$ ⟩)
— *C* as been moved to the front of the conclusion.
apply (*match conclusion in* ⟨*C* $\wedge A \wedge (B \wedge D) \wedge E \Rightarrow \langle - \rangle$ ⟩)
oops

Method *extract-conjunct* works similarly, but peels off the matched conjunct as a separate subgoal. As for *lift-conjunct*, the effect of the given method is discarded, so the body of the *match* is irrelevant.

lemma $\llbracket A; B; \llbracket A; B; D; E \rrbracket \Longrightarrow C; D; E \rrbracket \Longrightarrow A \wedge ((B \wedge C) \wedge D) \wedge E$
apply (*extract-conjunct* ⟨*match conclusion in C* $\Rightarrow \langle - \rangle$ ⟩)

— *extract-conjunct* gives us the matched conjunct C as a separate subgoal.

apply (*match conclusion in* $C \Rightarrow \langle - \rangle$)

apply *blast*

— The other subgoal contains the remaining conjuncts untouched.

apply (*match conclusion in* $\langle A \wedge (B \wedge D) \wedge E \rangle \Rightarrow \langle - \rangle$)

oops

Method *apply-conjunct* goes one step further, and applies the given method to the extracted subgoal.

lemma $\llbracket A; B; \llbracket A; B; D; E \rrbracket \Longrightarrow C; D; E \rrbracket \Longrightarrow A \wedge ((B \wedge C) \wedge D) \wedge E$

apply (*apply-conjunct* *match conclusion in* $C \Rightarrow \langle \text{match premises in } H: - \Rightarrow \langle \text{rule } H \rangle \rangle$)

— We get four subgoals from applying the given method to the matched conjunct C .

apply (*match premises in* $H: A \Rightarrow \langle \text{rule } H \rangle$)

apply (*match premises in* $H: B \Rightarrow \langle \text{rule } H \rangle$)

apply (*match premises in* $H: D \Rightarrow \langle \text{rule } H \rangle$)

apply (*match premises in* $H: E \Rightarrow \langle \text{rule } H \rangle$)

— The last subgoal contains the remaining conjuncts untouched.

apply (*match conclusion in* $\langle A \wedge (B \wedge D) \wedge E \rangle \Rightarrow \langle - \rangle$)

oops

end

end

theory *Eval-Bool*

imports *Try-Methods*

begin

The *eval_{bool}method/simproc* uses the code generator set up to reduce terms of boolean type to *True* or *False* equations.

Additional simprocs exist to reduce other types.

ML \langle

structure Eval-Simproc = struct

exception Failure

fun mk-constname-tab ts = fold Term.add-const-names ts []
|> Symtab.make-set

fun is-built-from tab t = case Term.strip-comb t of
(Const (cn, -), ts) => Symtab.defined tab cn
andalso forall (is-built-from tab) ts
| - => false


```

fun eval tab ctxt ct = let
  val t = Thm.term-of ct
  val - = Term.fold-aterms (fn Free - => raise Failure
    | Var - => raise Failure | - => ignore) t ()
  val - = not (is-built-from tab t) orelse raise Failure
  val ev = the (try (Code-Simp.dynamic-conv ctxt) ct)
  in if is-built-from tab (Thm.term-of (Thm.rhs-of ev))
    then SOME ev else NONE end
  handle Failure => NONE | Option => NONE

val eval-bool = eval (mk-constname-tab [@{term True}, @{term False}])
val eval-nat = eval (mk-constname-tab [@{term Suc 0}, @{term Suc 1},
  @{term Suc 9}])
val eval-int = eval (mk-constname-tab [@{term 0 :: int}, @{term 1 :: int},
  @{term 18 :: int}, @{term (-9) :: int}])

val eval-bool-simproc = Simplifier.make-simproc @context eval-bool
  { lhs = [@{term b :: bool}], proc = K eval-bool }
val eval-nat-simproc = Simplifier.make-simproc @context eval-nat
  { lhs = [@{term n :: nat}], proc = K eval-nat }
val eval-int-simproc = Simplifier.make-simproc @context eval-int
  { lhs = [@{term i :: int}], proc = K eval-int }

end
)

method-setup eval-bool = (Scan.succeed (fn ctxt => SIMPLE-METHOD'
  (CHANGED o full-simp-tac (clear-simpset ctxt
    addsimprocs [Eval-Simproc.eval-bool-simproc])))
  use code generator setup to simplify booleans in goals to True or False

method-setup eval-int-nat = (Scan.succeed (fn ctxt => SIMPLE-METHOD'
  (CHANGED o full-simp-tac (clear-simpset ctxt
    addsimprocs [Eval-Simproc.eval-nat-simproc, Eval-Simproc.eval-int-simproc])))
  use code generator setup to simplify nats and ints in goals to values

add-try-method eval-bool

Testing.

definition
  eval-bool-test-seq :: int list
where
  eval-bool-test-seq = [2, 3, 4, 5, 6, 7, 8]

lemma
  eval-bool-test-seq ! 4 = 6 ∧ (3 :: nat) < 4
  ∧ sorted eval-bool-test-seq
by eval-bool

```

A related gadget for installing constant definitions from locales as code equations. Useful where locales are being used to "hide" constants from the global state rather than to do anything tricky with interpretations.

Installing the global definitions in this way will allow `evalbool t cto` "seethrough" the hiding and decide equations.

ML `(`

`structure Add-Locale-Code-Defs = struct`

`fun get-const-defs thy nm = Sign.consts-of thy`

`|> Consts.dest |> #constants`

`|> map fst`

`|> filter (fn s => case Long-Name.explode s of`

`[-, nm', -] => nm' = nm | - => false)`

`|> map-filter (try (suffix -def #> Global-Theory.get-thm thy))`

`|> filter (Thm.strip-shyps #> Thm.shyps-of #> null)`

`|> tap (fn xs => tracing (Installing ^ string-of-int (length xs) ^ code defs))`

`fun setup nm thy = fold (fn t => Code.add-eqn-global (t, true))`

`(get-const-defs thy nm) thy`

`end`

`)`

locale `eval-bool-test-locale` **begin**

definition

`x == (12 :: int)`

definition

`y == (13 :: int)`

definition

`z = (x * y) + x + y`

end

setup `(Add-Locale-Code-Defs.setup eval-bool-test-locale)`

setup `(Add-Locale-Code-Defs.setup eval-bool-test-locale)`

lemma `eval-bool-test-locale.z > 150`

by `eval-bool`

end

— MLUtils is a collection of 'basic' ML utilities (kind of like `~~/src/Pure/library.ML`, but maintained by Trustworthy Systems). If you find yourself implementing: - A simple data-structure-shuffling task, - Something that shows up in the standard

library of other functional languages, or - Something that's "missing" from the general pattern of an Isabelle ML library, consider adding it here.

```
theory MLUtils
imports Main
begin
ML-file StringExtras.ML
ML-file ListExtras.ML
ML-file MethodExtras.ML
ML-file OptionExtras.ML
ML-file ThmExtras.ML
ML-file Sum.ML
end
```

```
theory Apply-Trace
imports
  Main
  ml-helpers/MLUtils
begin
```

```
ML (
  signature APPLY-TRACE =
  sig
    val apply-results :
      {silent-fail : bool} ->
      (Proof.context -> thm -> ((string * int option) * term) list -> unit) ->
      Method.text-range -> Proof.state -> Proof.state Seq.result Seq.seq

    (* Lower level interface. *)
    val can-clear : theory -> bool
    val clear-deps : thm -> thm
    val join-deps : thm -> thm -> thm
    val used-facts : Proof.context -> thm -> ((string * int option) * term) list
    val pretty-deps : bool -> (string * Position.T) option -> Proof.context -> thm
  ->
    ((string * int option) * term) list -> Pretty.T
  end

  structure Apply-Trace : APPLY-TRACE =
  struct

    (*TODO: Add more robust oracle without hyp clearing *)
    fun thm-to-cterm keep-hyps thm =
    let

      val thy = Thm.theory-of-thm thm
```

```

    val pairs = Thm.tpairs-of thm
    val ceqs = map (Thm.global-cterm-of thy o Logic.mk-equals) pairs
    val hyps = Thm.chyps-of thm
    val prop = Thm.cprop-of thm
    val thm' = if keep-hyps then Drule.list-implies (hyps, prop) else prop

in
  Drule.list-implies (ceqs, thm') end

val (-, clear-thm-deps') =
  Context.>>> (Context.map-theory-result (Thm.add-oracle (Binding.name count-cheat,
    thm-to-cterm false)));

fun clear-deps thm =
  let

    val thm' = try clear-thm-deps' thm
    |> Option.map (fold (fn - => fn t => (@{thm Pure.reflexive} RS t)) (Thm.tpairs-of
    thm))

    in case thm' of SOME thm' => thm' | NONE => error Can't clear deps here end

  fun can-clear thy = Context.subthy(@{theory}, thy)

  fun join-deps pre-thm post-thm =
    let
      val pre-thm' = Thm.flexflex-rule NONE pre-thm |> Seq.hd
      |> Thm.adjust-maxidx-thm (Thm.maxidx-of post-thm + 1)
    in
      Conjunction.intr pre-thm' post-thm |> Conjunction.elim |> snd
    end

  fun get-ref-from-nm' nm =
    let
      val exploded = space-explode - nm;
      val base = List.take (exploded, (length exploded) - 1) |> space-implode -
      val idx = List.last exploded |> Int.fromString;
    in if is-some idx andalso base <> then SOME (base, the idx) else NONE end

  fun get-ref-from-nm nm = Option.join (try get-ref-from-nm' nm);

  fun maybe-nth l = try (curry List.nth l)

  fun fact-from-derivation ctxt xnm =
    let

      val facts = Proof-Context.facts-of ctxt;

```

```

(* TODO: Check that exported local fact is equivalent to external one *)

val idx-result =
  let
    val (name', idx) = get-ref-from-nm xnm |> the;
    val entry = try (Facts.retrieve (Context.Proof ctxt) facts) (name', Position.none) |> the;
    val thm = maybe-nth (#thms entry) (idx - 1) |> the;
    in SOME (xnm, thm) end handle Option => NONE;

fun non-idx-result () =
  let
    val entry = try (Facts.retrieve (Context.Proof ctxt) facts) (xnm, Position.none) |> the;
    val thm = try the-single (#thms entry) |> the;
    in SOME (#name entry, thm) end handle Option => NONE;

in
  case idx-result of
    SOME thm => SOME thm
  | NONE => non-idx-result ()
end

fun most-local-fact-of ctxt xnm =
  let
    val local-name = try (fn xnm => Long-Name.explode xnm |> tl |> tl |> Long-Name.implode) xnm |> the;
    in SOME (fact-from-derivation ctxt local-name |> the) end handle Option => fact-from-derivation ctxt xnm;

fun thms-of (PBody {thms,...}) = thms

fun proof-body-descend' f get-fact (ident, thm-node) deptab = let
  val nm = Proofterm.thm-node-name thm-node
  val body = Proofterm.thm-node-body thm-node
in
  (if not (f nm) then
    (Inttab.update-new (ident, SOME (nm, get-fact nm |> the)) deptab handle Inttab.DUP - => deptab)
  else raise Option) handle Option =>
    ((fold (proof-body-descend' f get-fact) (thms-of (Future.join body))
      (Inttab.update-new (ident, NONE) deptab)) handle Inttab.DUP - => deptab)
end

fun used-facts' f get-fact thm =
  let
    val body = thms-of (Thm.proof-body-of thm);
  in fold (proof-body-descend' f get-fact) body Inttab.empty end

```

```

fun used-pbody-facts ctxt thm =
  let
    val nm = Thm.get-name-hint thm;
    val get-fact = most-local-fact-of ctxt;
  in
    used-facts' (fn nm' => nm' = orelse nm' = nm) get-fact thm
    |> Inttab.dest |> map-filter snd |> map snd |> map (apsnd (Thm.prop-of))
  end

fun raw-primitive-text f = Method.Basic (fn - => ((K (fn (ctxt, thm) => Seq.
  make-results (Seq.single (ctxt, f thm)))))

(*Find local facts from new hyps*)
fun used-local-facts ctxt thm =
  let
    val hyps = Thm.hyps-of thm
    val facts = Proof-Context.facts-of ctxt |> Facts.dest-static true []

    fun match-hyp hyp =
      let
        fun get (nm, thms) =
          case (get-index (fn t => if (Thm.prop-of t) aconv hyp then SOME hyp else
            NONE) thms)
          of SOME t => SOME (nm, t)
            | NONE => NONE
      in
        get (nm, hyps)
      end

    in
      get-first get facts
    end

  in
    map-filter match-hyp hyps end

fun used-facts ctxt thm =
  let
    let
      val used-from-pbody = used-pbody-facts ctxt thm |> map (fn (nm, t) => ((nm, NONE), t))
      val used-from-hyps = used-local-facts ctxt thm |> map (fn (nm, (i, t)) =>
        ((nm, SOME i), t))
    in
      (used-from-hyps @ used-from-pbody)
    end
  end

(* Perform refinement step, and run the given stateful function
  against computed dependencies afterwards. *)
fun refine args f text state =
  let

```

```

val ctxt = Proof.context-of state

val thm = Proof.simple-goal state |> #goal

fun save-deps deps = f ctxt thm deps

in
  if (can-clear (Proof.theory-of state)) then
    Proof.refine (Method.Combinator (Method.no-combinator-info, Method.Then,
[raw-primitive-text (clear-deps), text,
  raw-primitive-text (fn thm' => (save-deps (used-facts ctxt thm'); join-deps thm
thm'))])) state
  else
    (if (#silent-fail args) then (save-deps []; Proof.refine text state) else error
Apply-Trace theory must be imported to trace applies)
  end

(* Boilerplate from Proof.ML *)

fun method-error kind pos state =
  Seq.single (Proof-Display.method-error kind pos (Proof.raw-goal state));

fun apply args f text = Proof.assert-backward #> refine args f text #>
  Seq.maps-results (Proof.apply ((raw-primitive-text I), (Position.none, Position.none)));

fun apply-results args f (text, range) =
  Seq.APPEND (apply args f text, method-error (Position.range-position range));

structure Filter-Thms = Named-Thms
(
  val name = @{binding no-trace}
  val description = thms to be ignored from tracing
)

(* Print out the found dependencies. *)
fun pretty-deps only-names query ctxt thm deps =
let
  (* Remove duplicates. *)
  val deps = sort-distinct (prod-ord (prod-ord string-ord (option-ord int-ord)) Term-Ord.term-ord)
  deps

  (* Fetch canonical names and theorems. *)
  val deps = map (fn (ident, term) => ThmExtras.adjust-thm-name ctxt ident
term) deps

```

```

(* Remove boring theorems. *)
val deps = subtract (fn (a, ThmExtras.FoundName (-, thm)) => Thm.eq-thm
(thm, a)
| - => false) (Filter-Thms.get ctxt) deps

val deps = case query of SOME (raw-query,pos) =>
let
val pos' = perhaps (try (Position.advance-offsets 1)) pos;
val q = Find-Theorems.read-query pos' raw-query;
val results = Find-Theorems.find-theorems-cmd ctxt (SOME thm) (SOME
1000000000) false q
|> snd
|> map ThmExtras.fact-ref-to-name;

(* Only consider theorems from our query. *)

val deps = inter (fn (ThmExtras.FoundName (nmidx,-), ThmExtras.FoundName
(nmidx',-)) => nmidx = nmidx'
| - => false) results deps
in deps end
| - => deps

in
if only-names then
Pretty.block
(Pretty.separate (map (ThmExtras.pretty-fact only-names ctxt) deps))
else
(* Pretty-print resulting theorems. *)
Pretty.big-list used theorems:
(map (Pretty.item o single o ThmExtras.pretty-fact only-names ctxt) deps)

end

val - = Context.>> (Context.map-theory Filter-Thms.setup)

end
)

end

theory Apply-Trace-Cmd
imports Apply-Trace
keywords apply-trace :: prf-script
begin

ML<

```



```

val - =
  Outer-Syntax.command @{command-keyword apply-trace} initial refinement step
  (unstructured)

  (Args.mode only-names -- (Scan.option (Parse.position Parse.cartouche)) --
  Method.parse >>
    (fn ((on,query),text) => Toplevel.proofs (Apply-Trace.apply-results {silent-fail
    = false}
      (Pretty.writeln ooo (Apply-Trace.pretty-deps on query)) text)));

  )

lemmas [no-trace] = protectI protectD TrueI Eq-TrueI eq-reflection

lemma (a ∧ b) = (b ∧ a)
  apply-trace auto
  oops

lemma (a ∧ b) = (b ∧ a)
  apply-trace <intro> auto
  oops

lemma
  assumes X: b = a
  assumes Y: b = a
  shows
  b = a
  apply-trace (rule Y)
  oops

locale Apply-Trace-foo = fixes b a
  assumes X: b = a
begin

  lemma shows b = a b = a
  apply -
  apply-trace (rule Apply-Trace-foo.X)
  prefer 2
  apply-trace (rule X)
  oops
end

experiment begin

```

Example of trace for grouped lemmas

definition *ex* :: *nat set* **where**

ex = {1,2,3,4}

lemma *v1*: 1 ∈ *ex* **by** (*simp add: ex-def*)

lemma *v2*: 2 ∈ *ex* **by** (*simp add: ex-def*)

lemma *v3*: 3 ∈ *ex* **by** (*simp add: ex-def*)

Group several lemmas in a single one

lemmas *vs* = *v1 v2 v3*

lemma 2 ∈ *ex*

apply-trace (*simp add: vs*)

oops

end

end

theory *Apply-Debug*

imports

Apply-Trace

HOL-Eisbach.Eisbach-Tools

keywords

apply-debug :: *prf-script* % *proof* **and**

continue :: *prf-script* % *proof* **and** *finish* :: *prf-script* % *proof*

begin

ML <

val start-max-threads = *Multithreading.max-threads* ();

>

context

begin

private method *put-prems* =

(*match premises in H:PROP - (multi) ⇒ (insert H)*)

ML <

fun get-match-prems ctxt =

let

val st = *Goal.init* @ {*cterm PROP P*}

fun get-wrapped () =

let

val ((-,st'),-) =

```

      Method-Closure.apply-method ctxt @{method put-prems} [] [] ctxt [] (ctxt,
st)
      |> Seq.first-result prems;

      val prems =
        Thm.prems-of st' |> hd |> Logic.strip-imp-prems;

      in prems end

      val match-prems = the-default [] (try get-wrapped ());

      val all-prems = Assumption.all-prems-of ctxt;

      in map-filter (fn t => find-first (fn thm => t aconv (Thm.prop-of thm))
all-prems) match-prems end

    }
  end

ML (
signature APPLY-DEBUG =
sig
type break-opts = { tags : string list, trace : (string * Position.T) option, show-running
: bool }

val break : Proof.context -> string option -> tactic;
val apply-debug : break-opts -> Method.text-range -> Proof.state -> Proof.state;
val continue : int option -> (context-state -> context-state option) option ->
Proof.state -> Proof.state;
val finish : Proof.state -> Proof.state;

val pretty-state: Toplevel.state -> Pretty.T option;

end

structure Apply-Debug : APPLY-DEBUG =
struct
type break-opts = { tags : string list, trace : (string * Position.T) option, show-running
: bool }

fun do-markup range m = Output.report [Markup.markup (Markup.properties (Position.properties-of-range
range) m) ];
fun do-markup-pos pos m = Output.report [Markup.markup (Markup.properties
(Position.properties-of pos) m) ];

type markup-queue = { cur : Position.range option, next : Position.range option,
clear-cur : bool }

fun map-cur f ({cur, next, clear-cur} : markup-queue) =

```

```

    ({cur = f cur, next = next, clear-cur = clear-cur} : markup-queue)

fun map-next f ({cur, next, clear-cur} : markup-queue) =
    ({cur = cur, next = f next, clear-cur = clear-cur} : markup-queue)

fun map-clear-cur f ({cur, next, clear-cur} : markup-queue) =
    ({cur = cur, next = next, clear-cur = f clear-cur} : markup-queue)

type markup-state =
    { running : markup-queue
    }

fun map-running f ({running} : markup-state) =
    {running = f running}

structure Markup-Data = Proof-Data
(
    type T = markup-state Synchronized.var option *
        Position.range option (* latest method location *) *
        Position.range option (* latest breakpoint location *)
    fun init - : T = (NONE, NONE, NONE)
);

val init-queue = ({cur = NONE, next = NONE, clear-cur = false} : markup-queue)
val init-markup-state = ({running = init-queue} : markup-state)

fun set-markup-state id = Markup-Data.map (@{apply 3 (1)} (K id));
fun get-markup-id ctxt = #1 (Markup-Data.get ctxt);

fun set-latest-range range = Markup-Data.map (@{apply 3 (2)} (K (SOME range)));
fun get-latest-range ctxt = #2 (Markup-Data.get ctxt);

fun set-breakpoint-range range = Markup-Data.map (@{apply 3 (3)} (K (SOME range)));
fun get-breakpoint-range ctxt = #3 (Markup-Data.get ctxt);

val clear-ranges = Markup-Data.map (@{apply 3 (3)} (K NONE) o @{apply 3 (2)} (K NONE));

fun swap-markup queue startm endm =
    if is-some (#next queue) andalso #next queue = #cur queue then SOME (map-next (K NONE) queue) else
    let
        fun clear-cur () =
            (case #cur queue of SOME crng =>
                do-markup crng endm
                | NONE => ())
    in

```

```

    case #next queue of SOME rng =>
      (clear-cur (); do-markup rng startm; SOME ((map-cur (K (SOME rng)) o
map-next (K NONE)) queue))
    | NONE => if #clear-cur queue then (clear-cur (); SOME ((map-cur (K
NONE) o map-clear-cur (K false)) queue))
      else NONE
end

fun markup-worker (SOME (id : markup-state Synchronized.var)) =
let
  fun main-loop () =
    let val - = Synchronized.guarded-access id (fn e =>
      case swap-markup (#running e) Markup.running Markup.finished of
        SOME queue' => SOME ((),map-running (fn - => queue') e)
      | NONE => NONE)
    in main-loop () end
  in main-loop () end
  | markup-worker NONE = (fn () => ())

fun set-gen get set (SOME id) rng =
let
  val - =
    Synchronized.guarded-access id (fn e =>
      if is-some (#next (get e)) orelse (#clear-cur (get e)) then NONE else
      if (#cur (get e)) = SOME rng then SOME ((), e)
      else (SOME ((),(set (map-next (fn - => SOME rng)) e))))

  val - = Synchronized.guarded-access id (fn e => if is-some (#next (get e))
then NONE else SOME ((),e))
  in () end
  | set-gen - - NONE - = ()

fun clear-gen get set (SOME id) =
  Synchronized.guarded-access id (fn e =>
    if (#clear-cur (get e)) then NONE
    else (SOME ((),(set (map-clear-cur (fn - => true)) e))))
  | clear-gen - - NONE = ()

val set-running = set-gen #running map-running
val clear-running = clear-gen #running map-running

fun traceify-method static-ctxt src =
let
  val range = Token.range-of src;
  val head-range = Token.range-of [hd src];
  val m = Method.method-cmd static-ctxt src;

```

```

in (fn eval-ctxt => fn facts =>
  let
    val eval-ctxt = set-latest-range head-range eval-ctxt;
    val markup-id = get-markup-id eval-ctxt;

    fun traceify seq = Seq.make (fn () =>
      let
        val - = set-running markup-id range;
        val r = Seq.pull seq;
        val - = clear-running markup-id;
        in Option.map (apsnd traceify) r end)

    fun tac (runtime-ctxt, thm) =
      let
        val runtime-ctxt' = set-latest-range head-range runtime-ctxt;
        val - = set-running markup-id range;
        in traceify (m eval-ctxt facts (runtime-ctxt', thm)) end

      in tac end)
end

fun add-debug ctxt (Method.Source src) = (Method.Basic (traceify-method ctxt src))
  | add-debug ctxt (Method.Combinator (x,y,txts)) = (Method.Combinator (x,y,
map (add-debug ctxt) txts))
  | add-debug - x = x

fun st-eq (ctxt : Proof.context, st) (ctxt', st') =
  pointer-eq (ctxt, ctxt') andalso Thm.eq-thm (st, st')

type result =
  { pre-state : thm,
    post-state : thm,
    context: Proof.context }

datatype final-state = RESULT of (Proof.context * thm) | ERR of (unit ->
string)

type debug-state =
  { results : result list, (* this execution, in order of appearance *)
    prev-results : thm list, (* continuations needed to get thread back to some state *)
    next-state : thm option, (* proof thread blocks waiting for this *)
    break-state : (Proof.context * thm) option, (* state of proof thread just before
blocking *)
    restart : (unit -> unit) * int, (* restart function (how many previous results to
keep), restart requested if non-zero *)
    final : final-state option, (* final result, maybe error *)
    trans-id : int, (* increment on every restart *)
    ignore-breaks: bool }

```

```

val init-state =
  ({results = [],
    prev-results = [],
    next-state = NONE, break-state = NONE,
    final = NONE, ignore-breaks = false, restart = (K (), ~1), trans-id = 0} :
  debug-state)

fun map-next-state f ({results, next-state, break-state, final, ignore-breaks, prev-results,
  restart, trans-id} : debug-state) =
  ({results = results, next-state = f next-state, break-state = break-state, final =
  final, prev-results = prev-results,
    restart = restart, ignore-breaks = ignore-breaks, trans-id = trans-id} : debug-state)

fun map-results f ({results, next-state, break-state, final, ignore-breaks, prev-results,
  restart, trans-id} : debug-state) =
  ({results = f results, next-state = next-state, break-state = break-state, final =
  final, prev-results = prev-results,
    restart = restart, ignore-breaks = ignore-breaks, trans-id = trans-id} : debug-state)

fun map-prev-results f ({results, next-state, break-state, final, ignore-breaks, prev-results,
  restart, trans-id} : debug-state) =
  ({results = results, next-state = next-state, break-state = break-state, final =
  final, prev-results = f prev-results,
    restart = restart, ignore-breaks = ignore-breaks, trans-id = trans-id} : debug-state)

fun map-ignore-breaks f ({results, next-state, break-state = break-state, final, ignore-breaks,
  prev-results, restart, trans-id} : debug-state) =
  ({results = results, next-state = next-state, break-state = break-state, final = final,
  prev-results = prev-results,
    restart = restart, ignore-breaks = f ignore-breaks, trans-id = trans-id} : debug-state)

fun map-final f ({results, next-state, break-state, final, ignore-breaks, prev-results,
  restart, trans-id} : debug-state) =
  ({results = results, next-state = next-state, break-state = break-state, final = f
  final, prev-results = prev-results,
    restart = restart, ignore-breaks = ignore-breaks, trans-id = trans-id} : debug-state)

fun map-restart f ({results, next-state, break-state, final, ignore-breaks, prev-results,
  restart, trans-id} : debug-state) =
  ({results = results, next-state = next-state, break-state = break-state, final =
  final, prev-results = prev-results,
    restart = f restart, ignore-breaks = ignore-breaks, trans-id = trans-id} : debug-state)

fun map-break-state f ({results, next-state, break-state, final, ignore-breaks, prev-results,
  restart, trans-id} : debug-state) =
  ({results = results, next-state = next-state, break-state = f break-state, final =
  final, prev-results = prev-results,
    restart = restart, ignore-breaks = ignore-breaks, trans-id = trans-id} : debug-state)

```

```

fun map-trans-id f ({results, next-state, break-state, final, ignore-breaks, prev-results,
restart, trans-id} : debug-state) =
  ({results = results, next-state = next-state, break-state = break-state, final =
final, prev-results = prev-results,
  restart = restart, ignore-breaks = ignore-breaks, trans-id = f trans-id} : debug-state)

fun is-restarting ({restart,...} : debug-state) = snd restart > ~1;
fun is-finished ({final,...} : debug-state) = is-some final;

val drop-states = map-break-state (K NONE) o map-next-state (K NONE);

fun add-result ctxt pre post = map-results (cons {pre-state = pre, post-state =
post, context = ctxt}) o drop-states;

fun get-trans-id (id : debug-state Synchronized.var) = #trans-id (Synchronized.value
id);

fun stale-transaction-err trans-id trans-id' =
  error (Stale transaction. Expected ^ Int.toString trans-id ^ but found ^ Int.
toString trans-id')

fun assert-trans-id trans-id (e : debug-state) =
  if trans-id = (#trans-id e) then ()
  else stale-transaction-err trans-id (#trans-id e)

fun guarded-access id f =
  let
    val trans-id = get-trans-id id;
  in
    Synchronized.guarded-access id
      (fn (e : debug-state) =>
        (assert-trans-id trans-id e;
         (case f e of
           NONE => NONE
           | SOME (e', g) => SOME (e', g e))))
  end

fun guarded-read id f =
  let
    val trans-id = get-trans-id id;
  in
    Synchronized.guarded-access id
      (fn (e : debug-state) =>
        (assert-trans-id trans-id e;
         (case f e of
           NONE => NONE
           | SOME e' => SOME (e', e))))
  end

```


(Immediate return if there are previous results available or we are ignoring break-points *)*

```
fun pop-state-no-block id ctxt pre = guarded-access id (fn e =>
  if is-finished e then error Attempted to pop state from finished proof else
  if (#ignore-breaks e) then SOME (SOME pre, add-result ctxt pre pre) else
  case #prev-results e of
    [] => SOME (NONE, I)
  | (st :: sts) => SOME (SOME st, add-result ctxt pre st o map-prev-results (fn
- => sts)))
```

```
fun pop-next-state id ctxt pre = guarded-access id (fn e =>
  if is-finished e then error Attempted to pop state from finished proof else
  if not (null (#prev-results e)) then error Attempted to pop state when previous
  results exist else
  if (#ignore-breaks e) then SOME (pre, add-result ctxt pre pre) else
  (case #next-state e of
    NONE => NONE
  | SOME st => SOME (st, add-result ctxt pre st)))
```

```
fun set-next-state id trans-id st = guarded-access id (fn e =>
  (assert-trans-id trans-id e;
  if is-none (#next-state e) andalso is-some (#break-state e) then
    SOME ((), map-next-state (fn - => SOME st) o map-break-state (fn - =>
  NONE))
  else error (Attempted to set next state in inconsistent state ^ (@{make-string}
  e))))))
```

```
fun set-break-state id st = guarded-access id (fn e =>
  if is-none (#next-state e) andalso is-none (#break-state e) then
    SOME ((), map-break-state (fn - => SOME st))
  else error (Attempted to set break state in inconsistent state ^ (@{make-string}
  e)))
```

```
fun pop-state id ctxt pre =
  case pop-state-no-block id ctxt pre of SOME st => st
  | NONE =>
  let
    val - = set-break-state id (ctxt, pre); (* wait for continue *)
  in pop-next-state id ctxt pre end
```

(block until a breakpoint is hit or method finishes *)*

```
fun wait-break-state id trans-id = guarded-read id
  (fn e =>
    (assert-trans-id trans-id e;
    (case (#final e) of SOME st => SOME (st, true) | NONE =>
```

```

      case (#break-state e) of SOME st => SOME (RESULT st, false)
    | NONE => NONE));

fun debug-print (id : debug-state Synchronized.var) =
  (@{print} (Synchronized.value id));

(* Trigger a restart if an existing nth entry differs from the given one *)
fun maybe-restart id n st =
  let
    val gen = guarded-read id (fn e => SOME (#trans-id e));

    val did-restart = guarded-access id (fn e =>
      if is-some (#next-state e) then NONE else
      if not (null (#prev-results e)) then NONE else
      if is-restarting e then NONE (* TODO, what to do if we're already restarting?
*)
      else if length (#results e) > n then
        (SOME (true, map-restart (apsnd (fn - => n))))
      else SOME (false, I))

    val trans-id = Synchronized.guarded-access id
      (fn e => if is-restarting e then NONE else
        if not did-restart orelse gen + 1 = #trans-id e then SOME (#trans-id
e,e) else
          stale-transaction-err (gen + 1) (#trans-id e));
    in trans-id end;

fun peek-all-results id = guarded-read id (fn e => SOME (#results e));

fun peek-final-result id =
  guarded-read id (fn e => #final e)

fun poke-error (RESULT st) = st
  | poke-error (ERR e) = error (e ())

fun context-state e = (#context e, #pre-state e);

fun nth-pre-result id i = guarded-read id
  (fn e =>
    if length (#results e) > i then SOME (RESULT (context-state (nth (rev
(#results e)) i)), false) else
    if not (null (#prev-results e)) then NONE else
    (if length (#results e) = i then
      (case #break-state e of SOME st => SOME (RESULT st, false) | NONE
=> NONE) else
      (case #final e of SOME st => SOME (st, true) | NONE => NONE)))

```

```

fun set-finished-result id trans-id st =
  guarded-access id (fn e =>
    (assert-trans-id trans-id e;
     SOME ((), map-final (K (SOME st)))));

fun is-finished-result id = guarded-read id (fn e => SOME (is-finished e));

fun get-finish id =
  if is-finished-result id then peek-final-result id else
  let
    val - = guarded-access id
      (fn - => SOME ((), (map-ignore-breaks (fn - => true))))
  in peek-final-result id end

val no-break-opts = ({tags = [], trace = NONE, show-running = false} : break-opts)

structure Debug-Data = Proof-Data
(
  type T = debug-state Synchronized.var option (* handle on active proof thread *) *
    int * (* continuation counter *)
    bool * (* currently interactive context *)
    break-opts * (* global break arguments *)
    string option (* latest breakpoint tag *)
    fun init - : T = (NONE, ~1, false, no-break-opts, NONE)
);

fun set-debug-ident ident = Debug-Data.map (@{apply 5 (1)} (fn - => SOME ident))
val get-debug-ident = #1 o Debug-Data.get;
val get-the-debug-ident = the o get-debug-ident;

fun set-break-opts opts = Debug-Data.map (@{apply 5 (4)} (fn - => opts))
val get-break-opts = #4 o Debug-Data.get;

fun set-last-tag tags = Debug-Data.map (@{apply 5 (5)} (fn - => tags))
val get-last-tag = #5 o Debug-Data.get;

val is-debug-ctxt = is-some o #1 o Debug-Data.get;

fun clear-debug ctxt = ctxt
|> Debug-Data.map (fn - => (NONE, ~1, false, no-break-opts, NONE))
|> clear-ranges

val get-continuation = #2 o Debug-Data.get;
val get-can-break = #3 o Debug-Data.get;

```

```

(* Maintain pointer equality if possible *)
fun set-continuation i ctxt = if get-continuation ctxt = i then ctxt else
  Debug-Data.map (@{apply 5 (2)} (fn - => i)) ctxt;

fun set-can-break b ctxt = if get-can-break ctxt = b then ctxt else
  Debug-Data.map (@{apply 5 (3)} (fn - => b)) ctxt;

fun has-break-tag (SOME tag) tags = member (=) tags tag
  | has-break-tag NONE - = true;

fun break ctxt tag = (fn thm =>
  if not (get-can-break ctxt)
  orelse Method.detect-closure-state thm
  orelse not (has-break-tag tag (#tags (get-break-opts ctxt)))
  then Seq.single thm else
  let
    val id = get-the-debug-ident ctxt;
    val ctxt' = set-last-tag tag ctxt;

    val st' = Seq.make (fn () =>
      SOME (pop-state id ctxt' thm, Seq.empty))

  in st' end)

fun init-interactive ctxt = ctxt
  |> set-can-break false
  |> Config.put Method.closure true;

type static-info =
  {private-dyn-facts : string list, local-facts : (string * thm list) list}

structure Data = Generic-Data
(
  type T = (morphism * Proof.context * static-info) option;
  val empty: T = NONE;
  val extend = K NONE;
  fun merge data : T = NONE;
);

(* Present Eisbach/Match variable binding context as normal context elements.
  Potentially shadows existing facts/binds *)

fun dest-local s =
  let
    val [local,s'] = Long-Name.explode s;
  in SOME s' end handle Bind => NONE

fun maybe-bind st (-,[tok]) ctxt =

```

```

if Method.detect-closure-state st then
  let
    val target = Local-Theory.target-of ctxt
    val local-facts = Proof-Context.facts-of ctxt;
    val global-facts = map (Global-Theory.facts-of) (Context.parents-of (Proof-Context.theory-of
ctxt));
    val raw-facts = Facts.dest-all (Context.Proof ctxt) true global-facts local-facts
|> map fst;

    fun can-retrieve s = can (Facts.retrieve (Context.Proof ctxt) local-facts) (s,
Position.none)

    val private-dyns = raw-facts |>
      (filter (fn s => Facts.is-concealed local-facts s andalso Facts.is-dynamic
local-facts s
        andalso can-retrieve (Long-Name.base-name s)
        andalso Facts.intern local-facts (Long-Name.base-name s) = s
        andalso not (can-retrieve s)) )

    val local-facts = Facts.dest-static true [(Proof-Context.facts-of target)] local-facts;

    val - = Token.assign (SOME (Token.Declaration (fn phi =>
      Data.put (SOME (phi,ctxt, {private-dyn-facts = private-dyns, local-facts =
local-facts})))))) tok;

  in ctxt end
else
  let
    val SOME (Token.Declaration decl) = Token.get-value tok;
    val dummy-ctxt = decl Morphism.identity (Context.Proof ctxt);
    val SOME (phi,static-ctxt,{private-dyn-facts, local-facts}) = Data.get dummy-ctxt;

    val old-facts = Proof-Context.facts-of static-ctxt;
    val cur-priv-facts = map (fn s =>
      Facts.retrieve (Context.Proof ctxt) old-facts (Long-Name.base-name
s,Position.none)) private-dyn-facts;

    val cur-local-facts =
      map (fn (s,fact) => (dest-local s, Morphism.fact phi fact)) local-facts
|> map-filter (fn (s,fact) => case s of SOME s => SOME (s,fact) | - =>
NONE)

    val old-fixes = (Variable.dest-fixes static-ctxt)

    val local-fixes =
      filter (fn (-,f) =>
        Variable.is-newly-fixed static-ctxt (Local-Theory.target-of static-ctxt) f)
old-fixes
|> map-filter (fn (n,f) => case Variable.default-type static-ctxt f of SOME

```

```

typ =>
  if typ = dummyT then NONE else SOME (n, Free (f, typ))
  | NONE => NONE)

val local-binds = (map (apsnd (Morphism.term phi)) local-fixes)

val ctxt' = ctxt
|> fold (fn (s,t) =>
  Variable.bind-term ((s,0),t)
  #> Variable.declare-constraints (Var ((s,0),Term.fastype-of t))) local-binds
|> fold (fn e =>
  Proof-Context.put-thms true (Long-Name.base-name (#name e), SOME
(#thms e))) cur-priv-facts
|> fold (fn (nm,fact) =>
  Proof-Context.put-thms true (nm, SOME fact)) cur-local-facts
|> Proof-Context.put-thms true (match-prems, SOME (get-match-prems ctxt));

  in ctxt' end
| maybe-bind - - ctxt = ctxt

val - = Context.>> (Context.map-theory (Method.setup @{binding #}
(Scan.lift (Scan.trace (Scan.trace (Args.$$$ break) -- (Scan.option Parse.string)))
>>
(fn ((b,tag),toks) => fn - => fn - =>
  fn (ctxt,thm) =>
    (let

      val range = Token.range-of toks;
      val ctxt' = ctxt
      |> maybe-bind thm b
      |> set-breakpoint-range range;

      in Seq.make-results (Seq.map (fn thm' => (ctxt',thm')) (break ctxt' tag thm))
    end))) ))

fun map-state f state =
  let
    val (r,-) = Seq.first-result map-state (Proof.apply
      (Method.Basic (fn - => fn - => fn st =>
        Seq.make-results (Seq.single (f st))),
        Position.no-range) state)
  in r end;

fun get-state state =
  let
    val {context,goal} = Proof.simple-goal state;
  in (context,goal) end

```

```

fun maybe-trace (SOME (tr, pos)) (ctxt, st) =
let
  val deps = Apply-Trace.used-facts ctxt st;
  val query = if tr = then NONE else SOME (tr, pos);
  val pr = Apply-Trace.pretty-deps false query ctxt st deps;
in Pretty.writeln pr end
| maybe-trace NONE (ctxt, st) = ()

val active-debug-threads = Synchronized.var active-debug-threads ([] : unit future
list);

fun update-max-threads extra =
let
  val n-active = Synchronized.change-result active-debug-threads (fn ts =>
let
  val ts' = List.filter (not o Future.is-finished) ts;
  in (length ts', ts') end)
  val - = Multithreading.max-threads-update (start-max-threads + ((n-active + ex-
tra) * 3));
in () end

fun continue i-opt m-opt =
(map-state (fn (ctxt, thm) =>
let
  val ctxt = set-can-break true ctxt

  val thm = Apply-Trace.clear-deps thm;

  val - = if is-none (get-debug-ident ctxt) then error Cannot continue in a
non-debug state else ();

  val id = get-the-debug-ident ctxt;

  val start-cont = get-continuation ctxt; (* how many breakpoints so far *)

  val trans-id = maybe-restart id start-cont (ctxt, thm);
  (* possibly restart if the thread has made too much progress.
trans-id is the current number of restarts, used to avoid manipulating
stale states *)

  val - = nth-pre-result id start-cont; (* block until we've hit the start of this
continuation *)

  fun get-final n (st as (ctxt, -)) =
case (i-opt, m-opt) of
  (SOME i, NONE) => if i < 1 then error Can only continue a positive
number of breakpoints else

```

```

    if n = start-cont + i then SOME st else NONE
  | (NONE, SOME m) => (m (apfst init-interactive st))
  | (-, -) => error Invalid continue arguments

val ex-results = peek-all-results id |> rev;

fun tick-up n (-,thm) =
  if n < length ex-results then error Unexpected number of existing results
    (*case get-final n (#pre-state (nth ex-results n)) of SOME st' => (st',
false, n)
  | NONE => tick-up (n + 1) st *)
  else
  let
    val - = if n > length ex-results then set-next-state id trans-id thm else ();
    val (n-r, b) = wait-break-state id trans-id;
    val st' = poke-error n-r;
  in if b then (st',b, n) else
    case get-final n st' of SOME st'' => (st'', false, n)
    | NONE => tick-up (n + 1) st' end

val - = if length ex-results < start-cont then
(debug-print id; @{print} (start-cont,start-cont); @{print} (trans-id,trans-id);
  error Unexpected number of existing results)
else ()

val (st',b, cont) = tick-up (start-cont + 1) (ctxt, thm)

val st'' = if b then (Output.writeln Final Result.; st' |> apfst clear-debug)
  else st' |> apfst (set-continuation cont) |> apfst (init-interactive);

(* markup for matching breakpoints to continues *)

val sr = serial ();

fun markup-def rng =
  (Output.report
    [Markup.markup (Markup.entity breakpoint
  |> Markup.properties (Position.entity-properties-of true sr
    (Position.range-position rng))) ]);

val - = Option.map markup-def (get-latest-range (fst st''));
val - = Option.map markup-def (get-breakpoint-range (fst st''));

val - =
  (Context-Position.report ctxt (Position.thread-data ())
    (Markup.entity breakpoint
  |> Markup.properties (Position.entity-properties-of false sr Position.none)))

```



```

    val - = maybe-trace (#trace (get-break-opts ctxt)) st'';

    in st'' end))

fun do-apply pos rng opts m =
let
  val {tags, trace, show-running} = opts;
  val batch-mode = is-some (Position.line-of (fst rng));
  val show-running = if batch-mode then false else show-running;

  val - = if batch-mode then () else update-max-threads 1;

in
  (fn st => map-state (fn (ctxt,thm) =>
    let
      val ident = Synchronized.var debug-state init-state;
      val markup-id = if show-running then SOME (Synchronized.var markup-state
init-markup-state)
      else NONE;
      fun maybe-markup m = if show-running then do-markup rng m else ();

      val - = if is-debug-ctxt ctxt then
        error Cannot use apply-debug while debugging else ();

      val m = apfst (fn f => f ctxt) m;

      val st = Proof.map-context
        (set-can-break true
         #> set-break-opts opts
         #> set-markup-state markup-id
         #> set-debug-ident ident
         #> set-continuation ~1) st
        |> map-state (apsnd Apply-Trace.clear-deps);

      fun do-cancel thread = (Future.cancel thread; Future.join-result thread; ());

      fun do-fork trans-id = Future.fork (fn () =>
        let
          val (ctxt,thm) = get-state st;

          val r = case Exn.interruptible-capture (fn st =>
            let val - = Seq.pull (break ctxt NONE thm) in
              (case (Seq.pull o Proof.apply m) st
                of (SOME (Seq.Result st', -)) => RESULT (get-state st')
                 | (SOME (Seq.Error e, -)) => ERR e
                 | - => ERR (fn - => No results)) end) st
                of Exn.Res (RESULT r) => RESULT r
                 | Exn.Res (ERR e) => ERR e

```

```

    | Exn.Exn e => ERR (fn - => Runtime.exn-message e)
  val - = set-finished-result ident trans-id r;

  val - = clear-running markup-id;

  in () end)

  val thread = do-fork 0;
  val - = Synchronized.change ident (map-restart (fn - => (fn () => do-cancel
thread, ~1)));

  val - = maybe-markup Markup.finished;

  val - = Future.fork (fn () => markup-worker markup-id ());

  val st' = get-state (continue (SOME 1) NONE (Proof.map-context (set-continuation
0) st))

  val - = maybe-markup Markup.joined;

  val main-thread = if batch-mode then Future.fork (fn () => ()) else Future.fork
(fn () =>
  let

    fun restart-state gls e = e
      |> map-prev-results (fn - => map #post-state (take gls (rev (#results
e))))
      |> map-results (fn - => [])
      |> map-final (fn - => NONE)
      |> map-ignore-breaks (fn - => false)
      |> map-restart (fn - => (K (), gls))
      |> map-break-state (fn - => NONE)
      |> map-next-state (fn - => NONE)
      |> map-trans-id (fn i => i + 1);

    fun main-loop () =
      let
        val r = Synchronized.timed-access ident (fn - => SOME (seconds 0.1))
      in (fn e as {restart,next-state,...} =>
        if is-restarting e andalso is-none next-state then
          SOME ((fst restart, #trans-id e), restart-state (snd restart) e) else
          NONE);
        val - = OS.Process.sleep (seconds 0.1);
        in case r of NONE => main-loop ()
        | SOME (f,trans-id) =>
          let
            val - = f ();

```

```

        val - = clear-running markup-id;
        val thread = do-fork (trans-id + 1);
        val - = Synchronized.change ident (map-restart (fn - => (fn () =>
do-cancel thread, ~1))))
        in main-loop () end
    end;
in main-loop () end);

val - = maybe-markup Markup.running;
val - = maybe-markup Markup.forked;

val - = Synchronized.change active-debug-threads (cons main-thread);

in st' end) st)
end

fun apply-debug opts (m', rng) =
let
    val - = Method.report (m', rng);

    val m'' = (fn ctxt => add-debug ctxt m')
    val m = (m'', rng)
    val pos = Position.thread-data ();

in do-apply pos rng opts m end;

fun quasi-keyword x = Scan.trace (Args.$$$ x) >>
    (fn (s,[tok]) => (Position.reports [(Token.pos-of tok, Markup.quasi-keyword)];
s))

val parse-tags = (Args.parens (quasi-keyword tags |-- Parse.enum1 , Parse.string));
val parse-trace = Scan.option (Args.parens (quasi-keyword trace |-- Scan.option
(Parse.position Parse.cartouche))) >>
    (fn SOME NONE => SOME (, Position.none) | SOME (SOME x) => SOME
x | - => NONE);

val parse-opts1 = (parse-tags -- parse-trace) >>
    (fn (tags,trace) => {tags = tags, trace = trace});

val parse-opts2 = (parse-trace -- (Scan.optional parse-tags [])) >>
    (fn (trace,tags) => {tags = tags, trace = trace});

fun mode s = Scan.optional (Args.parens (quasi-keyword s) >> (K true)) false

val parse-opts = ((parse-opts1 || parse-opts2) -- mode show-running) >>
    (fn ({tags, trace}, show-running) => {tags = tags, trace = trace, show-running
= show-running} : break-opts) ;

val - =

```

```

    Outer-Syntax.command @{command-keyword apply-debug} initial goal refinement
    step (unstructured)
      (Scan.trace
        (parse-opts -- Method.parse) >>
        (fn ((opts, (m,-)),toks) => Toplevel.proof (apply-debug opts (m,Token.range-of
toks))));

val finish = map-state (fn (ctxt,-) =>
  let
    val - = if is-none (get-debug-ident ctxt) then error Cannot finish in a
non-debug state else ();
    val f = get-finish (get-the-debug-ident ctxt);
    in f |> poke-error |> apfst clear-debug end)

fun continue-cmd i-opt m-opt state =
let
  val {context,...} = Proof.simple-goal state;
  val check = Method.map-source (Method.method-closure (init-interactive contex-
t))

  val m-opt' = Option.map (check o Method.check-text context o fst) m-opt;

  fun eval-method txt =
    (fn (ctxt,thm) => try (fst o Seq.first-result method) (Method.evaluate txt ctxt
[] (ctxt,thm)))

  val i-opt' = case (i-opt,m-opt) of (NONE,NONE) => SOME 1 | - => i-opt;

in continue i-opt' (Option.map eval-method m-opt') state end

val - =
  Outer-Syntax.command @{command-keyword continue} step to next breakpoint
  (Scan.option Parse.int -- Scan.option Method.parse >> (fn (i-opt,m-opt) =>
    (Toplevel.proof (continue-cmd i-opt m-opt))))

val - =
  Outer-Syntax.command @{command-keyword finish} finish debugging
  (Scan.succeed (Toplevel.proof (continue NONE (SOME (fn - => NONE)))))

fun pretty-hidden-goals ctxt0 thm =
let
  val ctxt = ctxt0
  |> Config.put show-types (Config.get ctxt0 show-types orelse Config.get ctxt0
show-sorts)
  |> Config.put show-sorts false;

```

```

val prt-term =
  singleton (Syntax.uncheck-terms ctxt) #>
  Type-Annotation.ignore-free-types #>
  Syntax.unparse-term ctxt;
val prt-subgoal = prt-term

fun pretty-subgoal s A =
  Pretty.markup (Markup.subgoal s) [Pretty.str ( ^ s ^ . ), prt-subgoal A];
fun pretty-subgoals n = map-index (fn (i, A) => pretty-subgoal (string-of-int
(i + n)) A);

fun collect-extras prop =
  case try Logic.unprotect prop of
  SOME prop' =>
    (if Logic.count-prems prop' > 0 then
      (case try Logic.strip-horn prop'
        of SOME (As, B) => As :: collect-extras B
         | NONE => [])
      else [])
  | NONE => []

val (As,B) = Logic.strip-horn (Thm.prop-of thm);
val extras' = collect-extras B;
val extra-goals-limit = Int.max (Config.get ctxt0 Goal-Display.goals-limit -
length As, 0);
val all-extras = flat (take (length extras' - 1) extras');
val extras = take extra-goals-limit all-extras;

val pretty = pretty-subgoals (length As + 1) extras @
  (if extra-goals-limit < length all-extras then
    [Pretty.str (A total of ^ (string-of-int (length all-extras)) ^ hidden
subgoals...)]
    else [])
in pretty end

fun pretty-state state =
  if Toplevel.is-proof state
  then
    let
      val st = Toplevel.proof-of state;
      val {goal, context, ...} = Proof.raw-goal st;
      val pretty = Toplevel.pretty-state state;
      val hidden = pretty-hidden-goals context goal;
      val out = pretty @
        (if length hidden > 0 then [Pretty.keyword1 hidden goals] @ hidden else []);
    in SOME (Pretty.chunks out) end
  else NONE

end

```

)

```
ML ⟨val - =  
  Query-Operation.register {name = print-state, pri = Task-Queue.urgent-pri}  
  (fn {state = st, output-result, ...} =>  
    case Apply-Debug.pretty-state st of  
      SOME prt => output-result (Markup.markup Markup.state (Pretty.string-of  
prt))  
    | NONE => ());⟩
```

end

```
theory Find-Names  
imports Pure  
keywords find-names :: diag  
begin
```

The **find-names** command, when given a theorem, finds other names the theorem appears under, via matching on the whole proposition. It will not identify unnamed theorems.

```
ML ⟨
```

```
  local  
  (* all-facts-of and pretty-ref taken verbatim from non-exposed version  
    in Find-Theorems.ML of official Isabelle/HOL distribution *)  
  fun all-facts-of ctxt =  
    let  
      val thy = Proof-Context.theory-of ctxt;  
      val transfer = Global-Theory.transfer-theories thy;  
      val local-facts = Proof-Context.facts-of ctxt;  
      val global-facts = Global-Theory.facts-of thy;  
    in  
      (Facts.dest-all (Context.Proof ctxt) false [global-facts] local-facts  
       @ Facts.dest-all (Context.Proof ctxt) false [] global-facts)  
      |> maps Facts.selections  
      |> map (apsnd transfer)  
    end;
```

```
  fun pretty-ref ctxt thmref =  
    let  
      val (name, sel) =  
        (case thmref of  
          Facts.Named ((name, -), sel) => (name, sel)  
        | Facts.Fact - => raise Fail Illegal literal fact);  
    in  
      [Pretty.marks-str (#1 (Proof-Context.markup-extern-fact ctxt name), name),  
       Pretty.str (Facts.string-of-selection sel)]  
    end;
```

```

in

fun find-names ctxt thm =
  let
    fun eq-filter body thmref = (body = Thm.full-prop-of (snd thmref));
  in
    (filter (eq-filter (Thm.full-prop-of thm))) (all-facts-of ctxt)
    |> map #1
  end;

fun pretty-find-names ctxt thm =
  let
    val results = find-names ctxt thm;
    val position-markup = Position.markup (Position.thread-data ()) Markup.position;
  in
    ((Pretty.mark position-markup (Pretty.keyword1 find-names)) ::
     Par-List.map (Pretty.item o (pretty-ref ctxt)) results)
    |> Pretty.fbreaks |> Pretty.block |> Pretty.writeln
  end

end

val - =
  Outer-Syntax.command @{command-keyword find-names}
  find other names of a named theorem
  (Parse.thms1 >> (fn srcs => Toplevel.keep (fn st =>
    pretty-find-names (Toplevel.context-of st)
    (hd (Attrib.eval-thms (Toplevel.context-of st) srcs))))));
)

end

theory TSubst
imports
  Main
begin

method-setup tsubst = ⟨
  Scan.lift (Args.mode asm --
    Scan.optional (Args.parens (Scan.repeat Parse.nat)) [0] --
    Parse.term)
  >> (fn ((asm,occs),t) => (fn ctxt =>
    Method.SIMPLE-METHOD (Subgoal.FOCUS-PARAMS (fn focus => (fn thm
=>
  let

```

```

(* This code used to use Thm.certify-inst in 2014, which was removed.
   The following is just a best guess for what it did. *)
fun certify-inst ctxt (typ-insts, term-insts) =
  (typ-insts
   |> map (fn (tvar, inst) =>
            (Thm.ctyp-of ctxt (TVar tvar),
             Thm.ctyp-of ctxt inst)),
   term-insts
   |> map (fn (var, inst) =>
            (Thm.cterm-of ctxt (Var var),
             Thm.cterm-of ctxt inst)))

val ctxt' = #context focus

val ((-, schematic-terms), ctxt2) =
  Variable.import-inst true [(#concl focus) |> Thm.term-of] ctxt'
|>> certify-inst ctxt'

val ctxt3 = fold (fn (t,t') => Variable.bind-term (Thm.term-of t |> Ter-
m.dest-Var |> fst, (t' |> Thm.term-of))) schematic-terms ctxt2

val athm = Syntax.read-term ctxt3 t
|> Object-Logic.ensure-propT ctxt'
|> Thm.cterm-of ctxt'
|> Thm.trivial

val thm' = Thm.instantiate ([], map (apfst (Thm.term-of #> dest-Var))
schematic-terms) thm

in
  (if asm then EqSubst.eqsubst-asm-tac else EqSubst.eqsubst-tac)
  ctxt3 occs [athm] 1 thm'
  |> Seq.map (singleton (Variable.export ctxt3 ctxt'))
  end)) ctxt 1)))
› subst, with term instead of theorem as equation

schematic-goal
assumes a:  $\bigwedge x y. P x \implies P y$ 
fixes x :: 'b
shows  $\bigwedge x :: 'a :: \text{type}. ?Q x \implies P x \wedge ?Q x$ 
apply (tsubst (asm) ?Q x = (P x  $\wedge$  P x))
apply (rule refl)
apply (tsubst P x = P y, simp add:a)+
apply (tsubst (2) P y = P x, simp add:a)
apply (clarsimp simp: a)
done

end

```



```
theory Time-Methods-Cmd imports
```

```
  Main
```

```
begin
```

```
ML (
```

```
  structure Time-Methods = struct
```

```
    (* Work around Isabelle running every apply method on a dummy proof state *)
```

```
    fun skip-dummy-state (method: Method.method) : Method.method =
```

```
      fn facts => fn (ctxt, st) =>
```

```
        case Thm.prop-of st of
```

```
          Const (Pure.prop, -) $ (Const (Pure.term, -) $ Const (Pure.dummy-pattern,
```

```
-)) =>
```

```
          Seq.succeed (Seq.Result (ctxt, st))
```

```
        | - => method facts (ctxt, st);
```

```
    (* ML interface. Takes a list of (possibly-named) methods, then calls the supplied
```

```
    * callback with the method index (starting from 1), supplied name and timing.
```

```
    * Also returns the list of timings at the end. *)
```

```
    fun time-methods
```

```
      (no-check: bool)
```

```
      (skip-fail: bool)
```

```
      (callback: (int * string option -> Timing.timing -> unit))
```

```
      (maybe-named-methods: (string option * Method.method) list)
```

```
      (* like Method.method but also returns timing list *)
```

```
      : thm list -> context-state -> (Timing.timing list * context-state Seq.result
```

```
Seq.seq)
```

```
    = fn facts => fn (ctxt, st) => let
```

```
      fun run method =
```

```
        Timing.timing (fn () =>
```

```
          case method facts (ctxt, st) |> Seq.pull of
```

```
            (* Peek at first result, then put it back *)
```

```
            NONE => (NONE, Seq.empty)
```

```
          | SOME (r as Seq.Result (-, st'), rs) => (SOME st', Seq.cons r rs)
```

```
          | SOME (r as Seq.Error -, rs) => (NONE, Seq.cons r rs)
```

```
        ) ()
```

```
    val results = tag-list 1 maybe-named-methods
```

```
    |> map (fn (idx1, (maybe-name, method)) =>
```

```
      let val (time, (st', results)) = run method
```

```
        val - =
```

```
          if Option.isSome st' orelse not skip-fail
```

```
            then callback (idx1, maybe-name) time
```

```
          else ()
```

```
        val name = Option.getOpt (maybe-name, [method ^ string-of-int
```

```
idx1 ^ ])
```

```

    in {name = name, state = st', results = results, time = time} end)

    val canonical-result = hd results
    val other-results = tl results
    val return-val = (map #time results, #results canonical-result)
    fun show-state NONE = @{thm FalseE[where P=METHOD-FAILED]}
      | show-state (SOME st) = st
  in
    if no-check then return-val else
    (* Compare the proof states that we peeked at *)
    case other-results
    |> filter (fn result =>
      (* It's tempting to use aconv, etc., here instead of (<>), but
       * minute differences such as bound names in Pure.all can
       * break a proof script later on. *)
      Option.map Thm.full-prop-of (#state result) <>
      Option.map Thm.full-prop-of (#state canonical-result)) of
    [] => return-val
    | (bad-result::-) =>
      raise THM (methods \ ^ #name canonical-result ^
        \ and \ ^ #name bad-result ^ \ have different results,
        1, map (show-state o #state) [canonical-result, bad-result])
  end
end
)

method-setup time-methods = (
  let
    fun scan-flag name = Scan.lift (Scan.optional (Args.parens (Parse.reserved name)
    >> K true) false)
    val parse-no-check = scan-flag no-check
    val parse-skip-fail = scan-flag skip-fail
    val parse-maybe-name = Scan.option (Scan.lift (Parse.liberal-name --| Parse.$$$
    :))
    fun auto-name (idx1, maybe-name) =
      Option.getOpt (maybe-name, [method ^ string-of-int idx1 ^ ])
  in
    parse-no-check -- parse-skip-fail --
    Scan.repeat1 (parse-maybe-name -- Method.text-closure) >>
    (fn ((no-check, skip-fail), maybe-named-methods-text) => fn ctxt =>
      let
        val max-length = tag-list 1 (map fst maybe-named-methods-text)
          |> map (String.size o auto-name)
          |> (fn ls => fold (curry Int.max) ls 0)
      fun pad-name s =
        let val pad-length = max-length + String.size : - String.size s
        in s ^ replicate-string pad-length end
      fun timing-callback id time = warning (pad-name (auto-name id ^ : ) ^
Timing.message time)

```

```

      val maybe-named-methods = maybe-named-methods-text
      |> map (apsnd (fn method-text => Method.evaluate method-text ctxt))
      val timed-method = Time-Methods.time-methods no-check skip-fail timing-callback
maybe-named-methods
      fun method-discard-times facts st = snd (timed-method facts st)
      in
        method-discard-times
      |> Time-Methods.skip-dummy-state
      end)
end
) Compare running time of several methods on the current proof state

end

```

```

theory Try-Attribute
imports Main
begin

```

```

ML (
  local

```

```

    val parse-warn = Scan.lift (Scan.optional (Args.parens (Parse.reserved warn) >>
      K true) false)

```

```

    val attribute-generic = Context.cases Attrib.attribute-global Attrib.attribute

```

```

    fun try-attribute-cmd (warn, attr-srcs) (ctxt, thm) =
      let
        val attrs = map (attribute-generic ctxt) attr-srcs
        val (th', context') =
          fold (uncurry o Thm.apply-attribute) attrs (thm, ctxt)
        handle e =>
          (if Exn.is-interrupt e then Exn.reraise e
           else if warn then warning (TRY: ignoring exception: ^ (@{make-string}
e))
           else ();
          (thm, ctxt))
      in (SOME context', SOME th') end

```

```

  in

```

```

    val - = Theory.setup
      (Attrib.setup @{binding TRY}
        (parse-warn -- Attrib.attrs >> try-attribute-cmd)
        higher order attribute combinator to try other attributes, ignoring failure)

```

```

  end
)

```

The *TRY* attribute is an attribute combinator that applies other attributes, ignoring any failures by returning the original state. Note that since attributes are applied separately to each theorem in a theorem list, *TRY* will leave failing theorems unchanged while modifying the rest.

Accepts a "warn" flag to print any errors encountered.

Usage: `thm foo[TRY [iattributesi]]`

`thm foo[TRY (warn) [iattributesi]]`

10 Examples

experiment begin

lemma *eq1*: $(1 :: \text{nat}) = 1 + 0$ **by** *simp*

lemma *eq2*: $(2 :: \text{nat}) = 1 + 1$ **by** *simp*

lemmas *eqs* = *eq1 TrueI eq2*

'eqs[symmetric]' would fail because there are no unifiers with *True*, but *TRY* ignores that.

lemma

$1 + 0 = (1 :: \text{nat})$

True

$1 + 1 = (2 :: \text{nat})$

by (*rule eqs[TRY [symmetric]]*)+

You can chain calls to *TRY* at the top level, to apply different attributes to different theorems.

lemma *ineq*: $(1 :: \text{nat}) < 2$ **by** *simp*

lemmas *ineqs* = *eq1 ineq*

lemma

$1 + 0 = (1 :: \text{nat})$

$(1 :: \text{nat}) \leq 2$

by (*rule ineqs[TRY [symmetric], TRY [THEN order.strict-implies-order]]*)+

You can chain calls to *TRY* within each other, to chain more attributes onto particular theorems.

lemmas *more-eqs* = *eq1 eq2*

lemma

$1 = (1 :: \text{nat})$

$1 + 1 = (2 :: \text{nat})$

by (*rule more-eqs[TRY [symmetric], TRY [simplified add-0-right]]*)+

The 'warn' flag will print out any exceptions encountered. Since *symmetric* doesn't apply to *True* or $1 < 2$, this will log two errors.

lemmas *yet-another-group* = *eq1 TrueI eq2 ineq*

thm *yet-another-group*[*TRY (warn) [symmetric]*]

TRY should handle pretty much anything it might encounter.

```

thm eq1[TRY (warn) [where x=5]]
thm eq1[TRY (warn) [OF refl]]
end

```

end

term_pat : ML antiquotation for pattern matching on terms.

See TermPatternAntiquoteTests for examples and tests.

theory TermPatternAntiquote **imports**

Pure

begin

ML \langle

structure Term-Pattern-Antiquote = struct

val quote-string = quote

(typ matching; doesn't support matching on named TVars.*

** This is because each TVar is likely to appear many times in the pattern. *)*

```

fun gen-typ-pattern (TVar -) = -
  | gen-typ-pattern (TFree (v, sort)) =
    Term.TFree ( ^ quote-string v ^ , [ ^ commas (map quote-string sort) ^ ])
  | gen-typ-pattern (Type (typ-head, args)) =
    Term.Type ( ^ quote-string typ-head ^ , [ ^ commas (map gen-typ-pattern
args) ^ ])

```

(term matching; does support matching on named (non-dummy) Vars.*

** The ML var generated will be identical to the Var name except in*

** indexed names like ?v1.2, which creates the var v12. *)*

```

fun gen-term-pattern (Var ((-dummy-, -), -)) = -
  | gen-term-pattern (Var ((v, 0), -)) = v
  | gen-term-pattern (Var ((v, n), -)) = v ^ string-of-int n
  | gen-term-pattern (Const (n, typ)) =
    Term.Const ( ^ quote-string n ^ , ^ gen-typ-pattern typ ^ )
  | gen-term-pattern (Free (n, typ)) =
    Term.Free ( ^ quote-string n ^ , ^ gen-typ-pattern typ ^ )
  | gen-term-pattern (t as f $ x) =
    (* (read-term-pattern -) helpfully generates a dummy var that is
    * applied to all bound vars in scope. We go back and remove them. *)
    let fun default () = ( ^ gen-term-pattern f ^ $ ^ gen-term-pattern x ^ );
    in case strip-comb t of
      (h as Var ((-dummy-, -), -), bs) =>
        if forall is-Bound bs then gen-term-pattern h else default ()
    | - => default () end
  | gen-term-pattern (Abs (-, typ, t)) =
    Term.Abs (-, ^ gen-typ-pattern typ ^ , ^ gen-term-pattern t ^ )
  | gen-term-pattern (Bound n) = Bound ^ string-of-int n

```

```

(* Create term pattern. All Var names must be distinct in order to generate ML
variables. *)
fun term-pattern-antiquote ctxt s =
  let val pat = Proof-Context.read-term-pattern ctxt s
      val add-var-names' = fold-aterms (fn Var (v, -) => curry (v | - => I);
      val vars = add-var-names' pat [] |> filter (fn (n, -) => n <> -dummy-)
      val - = if vars = distinct (vars) then () else
                raise TERM (Pattern contains duplicate vars, [pat])
  in ( ^ gen-term-pattern pat ^ ) end

end;
val - = Context.>> (Context.map-theory (
  ML-Antiquotation.inline @{binding term-pat}
  ((Args.context -- Scan.lift Args.embedded-inner-syntax)
   >> uncurry Term-Pattern-Antiquote.term-pattern-antiquote)))
)

end

```

```

theory Trace-Schematic-Insts
imports
  Main
  ml-helpers/MLUtils
  ml-helpers/TermPatternAntiquote
begin

```

See `TraceSchematicInstsTest` for tests and examples.

```

locale data-stash
begin

```

We use this to stash a list of the schematics in the conclusion of the proof state. After running a method, we can read off the schematic instantiations (if any) from this list, then restore the original conclusion. Schematic types are added as "undefined :: ?'a" (for now, we don't worry about types that don't have sort "type").

TODO: there ought to be some standard way of stashing things into the proof state. Find out what that is and refactor

```

definition container :: 'a => bool => bool
where
  container a b ≡ True

```

```

lemma proof-state-add:
  Pure.prop PROP P ≡ PROP Pure.prop (container True xs ==> PROP P)
by (simp add: container-def)

```

```

lemma proof-state-remove:
  PROP Pure.prop (container True xs ==> PROP P) ≡ Pure.prop (PROP P)

```

```

by (simp add: container-def)

lemma rule-add:
   $PROP\ P \equiv (container\ True\ xs \implies PROP\ P)$ 
by (simp add: container-def)

lemma rule-remove:
   $(container\ True\ xs \implies PROP\ P) \equiv PROP\ P$ 
by (simp add: container-def)

lemma elim:
  container a b
by (simp add: container-def)

ML (
signature TRACE-SCHEMATIC-INSTS = sig
  type instantiations = (term * (int * term)) list * (typ * typ) list

  val trace-schematic-insts:
    Method.method -> (instantiations -> unit) -> Method.method
  val default-report:
    Proof.context -> string -> instantiations -> unit

  val trace-schematic-insts-tac:
    Proof.context ->
      (instantiations -> instantiations -> unit) ->
      (thm -> int -> tactic) ->
      thm -> int -> tactic
  val default-rule-report:
    Proof.context -> string -> instantiations -> instantiations -> unit

  val skip-dummy-state: Method.method -> Method.method
  val make-term-container: term list -> term
  val dest-term-container: term -> term list

  val attach-proof-annotations: Proof.context -> term list -> thm -> thm
  val detach-proof-annotations: Proof.context -> thm -> (int * term) list * thm

  val attach-rule-annotations: Proof.context -> term list -> thm -> thm
  val detach-rule-result-annotations: Proof.context -> thm -> (int * term) list *
thm
end

structure Trace-Schematic-Insts: TRACE-SCHEMATIC-INSTS = struct

```

— Each pair is a (schematic, instantiation) pair.

The int in the term instantiations is the number of binders which are due to subgoal bounds.

An explanation: if we instantiate some schematic ‘?P’ within a subgoal like $\bigwedge x\ y.$

Q , it might be instantiated to $\lambda a. R\ a\ x$. We need to capture ‘ x ’ when reporting the instantiation, so we report that ‘ $?P$ ’ has been instantiated to $\lambda x\ y\ a. R\ a\ x$. In order to distinguish between the bound ‘ x ’, ‘ y ’, and ‘ a ’, we record that the two outermost binders are actually due to the subgoal bounds.

type instantiations = (term * (int * term)) list * (typ * typ) list

— Work around Isabelle running every apply method on a dummy proof state

```
fun skip-dummy-state method =
  fn facts => fn (ctxt, st) =>
    case Thm.prop-of st of
      Const (@{const-name Pure.prop}, -) $
        (Const (@{const-name Pure.term}, -) $ Const (@{const-name Pure.dummy-pattern},
-)) =>
        Seq.succeed (Seq.Result (ctxt, st))
    | - => method facts (ctxt, st);
```

— Utils

```
fun rewrite-state-concl eqn st =
  Conv.fconv-rule (Conv.concl-conv (Thm.nprems-of st) (K eqn)) st
```

— Strip the *Pure.prop* that wraps proof state conclusions

```
fun strip-prop ct =
  case Thm.term-of ct of
    Const (@{const-name Pure.prop}, @ {typ prop => prop}) $ - => Thm.dest-arg
  ct
  | - => raise CTERM (strip-prop: head is not Pure.prop, [ct])
```

```
fun cconcl-of st =
  funpow (Thm.nprems-of st) Thm.dest-arg (Thm.cprop-of st)
  |> strip-prop
```

```
fun vars-of-term t =
  Term.add-vars t []
  |> sort-distinct Term-Ord.var-ord
```

```
fun type-vars-of-term t =
  Term.add-tvars t []
  |> sort-distinct Term-Ord.tvar-ord
```

— Create annotation list

```
fun make-term-container ts =
  fold (fn t => fn container =>
    Const (@{const-name container},
      fastype-of t --> @ {typ bool => bool}) $
      t $ container)
    (rev ts) @ {term True}
```

— Retrieve annotation list

```
fun dest-term-container
```



```

    (Const (@{const-name container}, -) $ x $ list) =
      x :: dest-term-container list
| dest-term-container - = []

```

— Attach some terms to a proof state, by "hiding" them in the protected goal.

```

fun attach-proof-annotations ctxt terms st =
  let
    val container = make-term-container terms
    (* FIXME: this might affect st's maxidx *)
    val add-eqn =
      Thm.instantiate
        ([],
         [(((P, 0), @{typ prop}), concl-of st),
          (((xs, 0), @{typ bool}), Thm.ctrm-of ctxt container)])
        @ {thm proof-state-add}
  in
    rewrite-state-concl add-eqn st
  end

```

— Retrieve attached terms from a proof state

```

fun detach-proof-annotations ctxt st =
  let
    val st-concl = concl-of st
    val (ccontainer', real-concl) = Thm.dest-implies st-concl
    val ccontainer =
      ccontainer'
      |> Thm.dest-arg (* strip Trueprop *)
      |> Thm.dest-arg — strip outer container True
    val terms =
      ccontainer
      |> Thm.term-of
      |> dest-term-container
    val remove-eqn =
      Thm.instantiate
        ([],
         [(((P, 0), @{typ prop}), real-concl),
          (((xs, 0), @{typ bool}), ccontainer)])
        @ {thm proof-state-remove}
  in
    (map (pair 0) terms, rewrite-state-concl remove-eqn st)
  end

```

— Attaches the given terms to the given thm by stashing them as a new *container* premise, *after* all the existing premises (this minimises disruption when the rule is used with things like 'erule').

```

fun attach-rule-annotations ctxt terms thm =
  let
    val container = make-term-container terms
    (* FIXME: this might affect thm's maxidx *)

```

```

val add-eqn =
  Thm.instantiate
    ([],
      [(((P, 0), @{typ prop}), Thm.cconcl-of thm),
        (((xs, 0), @{typ bool}), Thm.cterm-of ctxt container)]]
      @{thm rule-add})
in
  rewrite-state-concl add-eqn thm
end

```

— Finds all the variables and type variables in the given thm, then uses ‘attach’ to stash them in a *container* within the thm.

Returns a tuple containing the variables and type variables which were attached this way.

```

fun annotate-with-vars-using (attach: Proof.context -> term list -> thm -> thm) ctxt thm =
  let
    val tvars = type-vars-of-term (Thm.prop-of thm) |> map TVar
    val tvar-carriers = map (fn tvar => Const (@{const-name undefined}, tvar))
  tvars
    val vars = vars-of-term (Thm.prop-of thm) |> map Var
    val annotated-rule = attach ctxt (vars @ tvar-carriers) thm
  in ((vars, tvars), annotated-rule) end

```

```

val annotate-rule = annotate-with-vars-using attach-rule-annotations
val annotate-proof-state = annotate-with-vars-using attach-proof-annotations

```

```

fun split-and-zip-instantiations (vars, tvars) insts =
  let val (var-insts, tvar-insts) = chop (length vars) insts
  in (vars ~~ var-insts, tvars ~~ map (snd #> fastype-of) tvar-insts) end

```

— Term version of **Thm.dest_arg**.

```

val dest-arg = Term.dest-comb #> snd

```

— Cousin of **Term.strip_abs**.

```

fun strip-all t = (Term.strip-all-vars t, Term.strip-all-body t)

```

— Matches subgoals of the form:

$\bigwedge A B C. \llbracket X; Y; Z \rrbracket \Longrightarrow \text{container True data}$

Extracts the instantiation variables from ‘?data’, and re-applies the surrounding meta abstractions (in this case ‘ $\bigwedge A B C$ ’).

```

fun dest-instantiation-container-subgoal t =

```

```

  let
    val (vars, goal) = t |> strip-all
    val goal = goal |> Logic.strip-imp-concl
  in
    case goal of
      @{term-pat Trueprop (container True ?data)} =>
        dest-term-container data

```

```

|> map (fn t => (length vars, Logic.rlist-abs (rev vars, t))) (* reapply
variables *)
|> SOME
| - => NONE
end

```

— Finds the first subgoal with a *container* conclusion. Extracts the data from the container and removes the subgoal.

fun detach-rule-result-annotations ctxt st =

```

let
  val (idx, data) =
    st
    |> Thm.premis-of
    |> Library.get-index dest-instantiation-container-subgoal
    |> OptionExtras.get-or-else (fn () => error No container subgoal!)
  val st' =
    st
    |> resolve-tac ctxt @ { thms elim } (idx + 1)
    |> Seq.hd
in
  (data, st')
end

```

— ‘*abs_all n t wrap the first n lambda abstractions in t with interleaved Pure.all constructors. For example, ‘abs_aab.lambda > c.P’.* The resulting term is usually not well-typed.

Used to disambiguate schematic instantiations where the instantiation is a lambda.

```

fun abs-all 0 t = t
| abs-all n (t as (Abs (v, typ, body))) =
  if n < 0 then error Number of lambdas to wrap should be positive. else
  Const (@ { const-name Pure.all }, dummyT)
  $ Abs (v, typ, abs-all (n - 1) body)
| abs-all n - = error (Expected at least ^ Int.toString n ^ more lambdas.)

```

fun filtered-instantiation-lines ctxt (var-insts, tvar-insts) =

```

let
  val vars-lines =
    map (fn (var, (abs, inst)) =>
      if var = inst then (* don't show unchanged *) else
      ^ Syntax.string-of-term ctxt var ^ => ^
      Syntax.string-of-term ctxt (abs-all abs inst) ^ \n)
    var-insts
  val tvars-lines =
    map (fn (tvar, inst) =>
      if tvar = inst then (* don't show unchanged *) else
      ^ Syntax.string-of-typ ctxt tvar ^ => ^
      Syntax.string-of-typ ctxt inst ^ \n)
    tvar-insts
in
  vars-lines @ tvars-lines
end

```

end

— Default callback for black-box method tracing. Prints nontrivial instantiations to tracing output with the given title line.

```
fun default-report ctxt title insts =
  let
    val all-insts = String.concat (filtered-instantiation-lines ctxt insts)
    (* TODO: add a quiet flag, to suppress output when nothing was instantiated *)
    in title ^ \n ^ (if all-insts = then (no instantiations)\n else all-insts)
      |> tracing
    end
```

— Default callback for tracing rule applications. Prints nontrivial instantiations to tracing output with the given title line. Separates instantiations of rule variables and goal variables.

```
fun default-rule-report ctxt title rule-insts proof-insts =
  let
    val rule-lines = String.concat (filtered-instantiation-lines ctxt rule-insts)
    val rule-lines =
      if rule-lines =
      then (no rule instantiations)\n
      else rule instantiations:\n ^ rule-lines;
    val proof-lines = String.concat (filtered-instantiation-lines ctxt proof-insts)
    val proof-lines =
      if proof-lines =
      then (no goal instantiations)\n
      else goal instantiations:\n ^ proof-lines;
    in title ^ \n ^ rule-lines ^ \n ^ proof-lines |> tracing end
```

— ‘trace_{schematic_iinsts_tac}ctxtcallbacktacticthmidx’ does the following :

- Produce a *container*-annotated version of ‘thm’. - Runs ‘tactic’ on subgoal ‘idx’, using the annotated version of ‘thm’. - If the tactic succeeds, call ‘callback’ with the rule instantiations and the goal instantiations, in that order.

```
fun trace-schematic-insts-tac
  ctxt
  (callback: instantiations -> instantiations -> unit)
  (tactic: thm -> int -> tactic)
  thm idx st =
  let
    val (rule-vars, annotated-rule) = annotate-rule ctxt thm
    val (proof-vars, annotated-proof-state) = annotate-proof-state ctxt st
    val st = tactic annotated-rule idx annotated-proof-state
  in
    st |> Seq.map (fn st =>
      let
        val (rule-terms, st) = detach-rule-result-annotations ctxt st
        val (proof-terms, st) = detach-proof-annotations ctxt st
        val rule-insts = split-and-zip-instantiations rule-vars rule-terms
        val proof-insts = split-and-zip-instantiations proof-vars proof-terms
```

```

    val () = callback rule-insts proof-insts
  in
    st
  end
)
end

```

— ML interface, calls the supplied function with schematic unifications (will be given all variables, including those that haven't been instantiated).

```

fun trace-schematic-insts (method: Method.method) callback
= fn facts => fn (ctxt, st) =>
  let
    val (vars, annotated-st) = annotate-proof-state ctxt st
  in (* Run the method *)
    method facts (ctxt, annotated-st)
  |> Seq.map-result (fn (ctxt', annotated-st') => let
    (* Retrieve the stashed list, now with unifications *)
    val (annotations, st') = detach-proof-annotations ctxt' annotated-st'
    val insts = split-and-zip-instantiations vars annotations
    (* Report the list *)
    val - = callback insts
  in (ctxt', st') end)
  end
end
end
)
end

```

```

method-setup trace-schematic-insts = (
  let
    open Trace-Schematic-Insts
  in
    (Scan.option (Scan.lift Parse.liberal-name) -- Method.text-closure) >>
    (fn (maybe-title, method-text) => fn ctxt =>
      trace-schematic-insts
        (Method.evaluate method-text ctxt)
        (default-report ctxt
          (Option.getOpt (maybe-title, trace-schematic-insts:)))
    )
  end
)
) Method combinator to trace schematic variable and type instantiations
end

```

theory *Insulin*

imports

Pure

keywords

desugar-term desugar-thm desugar-goal :: diag

begin

ML (

structure Insulin = struct

val desugar-random-tag = dsfjdssdfs

fun fresh-substring s = let

fun next [] = [#a]

| next (#z :: n) = #a :: next n

| next (c :: n) = Char.succ c :: n

fun fresh n = let

val ns = String.implode n

in if String.isSubstring ns s then fresh (next n) else ns end

in fresh [#a] end

(Encode a (possibly qualified) constant name as an (expected-to-be-)unused name.*

** The encoded name will be treated as a free variable. *)*

fun escape-const c = let

val delim = fresh-substring c

in desugar-random-tag ^ delim ^ - ^

String.concat (case Long-Name.explode c of

(a :: b :: xs) => a :: map (fn x => delim ^ x) (b :: xs)

| xs => xs)

end

(Decode; if it fails, return input string *)*

fun unescape-const s =

if not (String.isPrefix desugar-random-tag s) then s else

let val cs = String.extract (s, String.size desugar-random-tag, NONE) |> String.explode

fun readDelim d (#- :: cs) = (d, cs)

| readDelim d (c :: cs) = readDelim (d @ [c]) cs

val (delim, cs) = readDelim [] cs

val delimlen = length delim

fun splitDelim name cs =

if take delimlen cs = delim then name :: splitDelim [] (drop delimlen cs)

else case cs of [] => if null name then [] else [name]

| (c::cs) => splitDelim (name @ [c]) cs

val names = splitDelim [] cs

in Long-Name.implode (map String.implode names) end

handle Match => s

fun dropQuotes s = if String.isPrefix \ s andalso String.isSuffix \ s
then String.substring (s, 1, String.size s - 2) else s

```

(* Translate markup from consts-encoded-as-free-variables to actual consts *)
fun desugar-reconst ctxt (tr as XML.Elem ((tag, attrs), children))
= if tag = fixed orelse tag = intensify then
  let val s = XML.content-of [tr]
      val name = unescape-const s
      fun get-entity-attrs (XML.Elem ((entity, attrs), -)) = SOME attrs
        | get-entity-attrs (XML.Elem (-, body)) =
            find-first (K true) (List.mapPartial get-entity-attrs body)
        | get-entity-attrs (XML.Text -) = NONE
  in
    if name = s then tr else
      (* try to look up the const's info *)
      case Syntax.read-term ctxt name
      |> Thm.ctrm-of ctxt
      |> Proof-Display.pp-ctrm (fn - => Proof-Context.theory-of ctxt)
      |> Pretty.string-of
      |> dropQuotes
      |> YXML.parse
      |> get-entity-attrs of
        SOME attrs =>
          XML.Elem ((entity, attrs), [XML.Text name])
        | - =>
          XML.Elem ((entity, [(name, name), (kind, constant)]),
                    [XML.Text name]) end
      else XML.Elem ((tag, attrs), map (desugar-reconst ctxt) children)
  | desugar-reconst - (t as XML.Text -) = t

fun term-to-string ctxt no-markup =
  Syntax.pretty-term ctxt
  #> Pretty.string-of
  #> YXML.parse-body
  #> map (desugar-reconst ctxt)
  #> (if no-markup then XML.content-of else YXML.string-of-body)
  #> dropQuotes

(* Strip constant names from a term.
 * A term is split to a term-unconst and a string list of the
 * const names in tree preorder. *)
datatype term-unconst =
  UCCnst of typ |
  UCAbs of string * typ * term-unconst |
  UCApp of term-unconst * term-unconst |
  UCVar of term

fun is-ident-char c = Char.isAlphaNum c orelse c = #- orelse c = #. orelse c =
  #'

fun term-to-unconst (Const (name, typ)) =

```

```

(* some magical constants have strange names, such as ==>; ignore them *)
if forall is-ident-char (String.explode name) then (UCCConst typ, [name])
else (UCVar (Const (name, typ)), [])
| term-to-unconst (Abs (var, typ, body)) = let
  val (body', consts) = term-to-unconst body
  in (UCAbs (var, typ, body'), consts) end
| term-to-unconst (f $ x) = let
  val (f', consts1) = term-to-unconst f
  val (x', consts2) = term-to-unconst x
  in (UCApp (f', x'), consts1 @ consts2) end
| term-to-unconst t = (UCVar t, [])

fun term-from-unconst (UCCConst typ) (name :: consts) =
  ((if unescape-const name = name then Const else Free) (name, typ), consts)
| term-from-unconst (UCAbs (var, typ, body)) consts = let
  val (body', consts) = term-from-unconst body consts
  in (Abs (var, typ, body'), consts) end
| term-from-unconst (UCApp (f, x)) consts = let
  val (f', consts) = term-from-unconst f consts
  val (x', consts) = term-from-unconst x consts
  in (f' $ x', consts) end
| term-from-unconst (UCVar v) consts = (v, consts)

(* Count occurrences of bad strings.
* Bad strings are allowed to overlap, but for each string, non-overlapping occurrences are counted.
* Note that we search on string lists, to deal with symbols correctly. *)
fun count-matches (haystack: 'a list) (needles: 'a list list): int list =
  let (* Naive algorithm. Probably ok, given that we're calling the term printer a
  lot elsewhere. *)
    fun try-match xs [] = SOME xs
      | try-match (x::xs) (y::ys) = if x = y then try-match xs ys else NONE
      | try-match _ _ = NONE
    fun count [] = 0
      | count needle = let
        fun f [] occs = occs
          | f haystack' occs = case try-match haystack' needle of
            NONE => f (tl haystack') occs
            | SOME tail => f tail (occs + 1)
        in f haystack 0 end
    in map count needles end

fun focus-list (xs: 'a list): ('a list * 'a * 'a list) list =
  let fun f head x [] = [(head, x, [])]
      | f head x (tail as x'::tail') = (head, x, tail) :: f (head @ [x]) x' tail'
    in case xs of [] => []
      | (x::xs) => f [] x xs end

(* Do one rewrite pass: try every constant in sequence, then collect the ones which

```



```

* reduced the occurrences of bad strings *)
fun rewrite-pass ctxt (t: term) (improved: term -> bool) (escape-const: string ->
string): term =
  let val (ucterm, consts) = term-to-unconst t
  fun rewrite-one (prev, const, rest) =
    let val (t', []) = term-from-unconst ucterm (prev @ [escape-const const]
@ rest)
    in improved t' end
  val consts-to-rewrite = focus-list consts |> map rewrite-one
  val consts' = map2 (fn rewr => fn const => if rewr then escape-const const
else const) consts-to-rewrite consts
  val (t', []) = term-from-unconst ucterm consts'
  in t' end

(* Do rewrite passes until bad strings are gone or no more rewrites are possible *)
fun desugar ctxt (t0: term) (bads: string list): term =
  let fun count t = count-matches (Symbol.explode (term-to-string ctxt true t))
  (map Symbol.explode bads)
  val - = if null bads then error Nothing to desugar else ()
  fun rewrite t = let
    val counts0 = count t
    fun improved t' = exists (<) (count t' ~~ counts0)
    val t' = rewrite-pass ctxt t improved escape-const
    in if forall (fn c => c = 0) (count t') (* bad strings gone *)
    then t'
    else if t = t' (* no more rewrites *)
    then let
      val bads' = filter (fn (c, -) => c > 0) (counts0 ~~ bads) |> map snd
      val - = warning (Sorry, failed to desugar ^ commas-quote bads')
      in t end
    else rewrite t'
  end
  in rewrite t0 end

fun span - [] = ([], [])
| span p (a::s) =
  if p a then let val (y, n) = span p s in (a::y, n) end else ([], a::s)

fun check-desugar s = let
  fun replace [] = []
  | replace xs =
    if take (String.size desugar-random-tag) xs = String.explode desugar-random-tag
    then case span is-ident-char xs of
      (v, xs) => String.explode (unescape-const (String.implode v)) @
replace xs
    else hd xs :: replace (tl xs)
  val desugar-string = String.implode o replace o String.explode
  in if not (String.isSubstring desugar-random-tag s) then s
  else desugar-string s end

```

```

fun desugar-term ctxt t s =
  desugar ctxt t s |> term-to-string ctxt false |> check-desugar

fun desugar-thm ctxt thm s = desugar-term ctxt (Thm.prop-of thm) s

fun desugar-goal ctxt goal n s = let
  val subgoals = goal |> Thm.premis-of
  val subgoals = if n = 0 then subgoals else
    if n < 1 orelse n > length subgoals then
      (* trigger error *) [Logic.get-goal (Thm.term-of (Thm.cprop-of
goal)) n]
    else [nth subgoals (n - 1)]
  val results = map (fn t => (NONE, desugar-term ctxt t s)
    handle ex as TERM - => (SOME ex, term-to-string ctxt
false t))
    subgoals
  in if null results
    then error No subgoals to desugar
    else if forall (Option.isSome o fst) results
      then raise the (fst (hd results))
      else map snd results
  end

end

)

ML <
Outer-Syntax.command @{command-keyword desugar-term}
term str str2... -> desugar str in term
(Parse.term -- Scan.repeat1 Parse.string >> (fn (t, s) =>
  Toplevel.keep (fn state => let val ctxt = Toplevel.context-of state in
    Insulin.desugar-term ctxt (Syntax.read-term ctxt t) s
    |> writeln end))))
)

ML <
Outer-Syntax.command @{command-keyword desugar-thm}
thm str str2... -> desugar str in thm
(Parse.thm -- Scan.repeat1 Parse.string >> (fn (t, s) =>
  Toplevel.keep (fn state => let val ctxt = Toplevel.context-of state in
    Insulin.desugar-thm ctxt (Attrib.eval-thms ctxt [t] |> hd) s |> writeln end))))
)

ML <
fun print-subgoals (x::xs) n = (writeln (Int.toString n ^ . ^ x); print-subgoals xs
(n+1))
| print-subgoals [] - = ();
Outer-Syntax.command @{command-keyword desugar-goal}

```

```

goal-num str str2... -> desugar str in goal
(Scan.option Parse.int -- Scan.repeat1 Parse.string >> (fn (n, s) =>
  Toplevel.keep (fn state => let val ctxt = Toplevel.context-of state in
    Insulin.desugar-goal ctxt (Toplevel.proof-of state |> Proof.raw-goal |> #goal)
  (Option.getOpt (n, 0)) s
    |> (fn xs => case xs of
      [x] => writeln x
      | - => print-subgoals xs 1) end))))
)

```

end

theory ShowTypes imports

Main

keywords *term-show-types thm-show-types goal-show-types :: diag*

begin

ML (

structure Show-Types = struct

fun pretty-markup-to-string no-markup =

Pretty.string-of

#> YXML.parse-body

#> (if no-markup then XML.content-of else YXML.string-of-body)

fun term-show-types no-markup ctxt term =

let val keywords = Thy-Header.get-keywords' ctxt

val ctxt' = ctxt

|> Config.put show-markup false

|> Config.put Printer.show-type-emphasis false

(FIXME: the sledgehammer code also sets these,*

** but do we always want to force them on the user? *)*

*(**

|> Config.put show-types false

|> Config.put show-sorts false

|> Config.put show-consts false

**)*

|> Variable.auto-fixes term

in

singleton (Syntax.uncheck-terms ctxt') term

|> Sledgehammer-Isar-Annotate.annotate-types-in-term ctxt'

|> Syntax.unparse-term ctxt'

|> pretty-markup-to-string no-markup

end

```

fun goal-show-types no-markup ctxt goal n = let
  val subgoals = goal |> Thm.premsof
  val subgoals = if n = 0 then subgoals else
    if n < 1 orelse n > length subgoals then
      (* trigger error *) [Logic.get-goal (Thm.term-of (Thm.cprop-of
goal)) n]
    else [nth subgoals (n - 1)]
  val results = map (fn t => (NONE, term-show-types no-markup ctxt t)
    handle ex as TERM - => (SOME ex, term-show-types
no-markup ctxt t))
    subgoals
  in if null results
    then error No subgoals to show
    else if forall (Option.isSome o fst) results
      then raise the (fst (hd results))
      else map snd results
  end

end;

Outer-Syntax.command @{command-keyword term-show-types}
term-show-types TERM -> show TERM with type annotations
(Parse.term >> (fn t =>
  Toplevel.keep (fn state =>
    let val ctxt = Toplevel.context-of state in
      Show-Types.term-show-types false ctxt (Syntax.read-term ctxt t)
    |> writeln end)));

Outer-Syntax.command @{command-keyword thm-show-types}
thm-show-types THM1 THM2 ... -> show theorems with type annotations
(Parse.thms1 >> (fn ts =>
  Toplevel.keep (fn state =>
    let val ctxt = Toplevel.context-of state in
      Attrib.eval-thms ctxt ts
    |> app (Thm.prop-of #> Show-Types.term-show-types false ctxt #> writeln)
end)));

let
  fun print-subgoals (x::xs) n = (writeln (Int.toString n ^ . ^ x); print-subgoals xs
(n+1))
  | print-subgoals [] - = ();
in
  Outer-Syntax.command @{command-keyword goal-show-types}
goal-show-types [N] -> show subgoals (or Nth goal) with type annotations
(Scan.option Parse.int >> (fn n =>
  Toplevel.keep (fn state =>
    let val ctxt = Toplevel.context-of state
      val goal = Toplevel.proof-of state |> Proof.raw-goal |> #goal
    in Show-Types.goal-show-types false ctxt goal (Option.getOpt (n, 0))
    end
  end
end

```

```

|> (fn xs => case xs of
      [x] => writeln x
    | - => print-subgoals xs 1) end)))
end;

```

end

```

theory AutoLevity-Base
imports Main Apply-Trace
keywords levity-tag :: thy-decl
begin

```

```

ML ⟨
  fun is-simp (·: Proof.context) (·: thm) = true
  ⟩

```

```

ML ⟨
  val is-simp-installed = is-some (
    try (ML-Context.eval ML-Compiler.flags @{here})
    (ML-Lex.read-text (val is-simp = Raw-Simplifier.is-simp, @{here} )));
  ⟩

```

```

ML⟨
  (* Describing a ordering on Position.T. Optionally we compare absolute document
  position, or
  just line numbers. Somewhat complicated by the fact that jEdit positions don't
  have line or
  file identifiers. *)

```

```

  fun pos-ord use-offset (pos1, pos2) =
    let
      fun get-offset pos = if use-offset then Position.offset-of pos else SOME 0;

```

```

      fun get-props pos =
        (SOME (Position.file-of pos |> the,
          (Position.line-of pos |> the,
            get-offset pos |> the)), NONE)
      handle Option => (NONE, Position.parse-id pos)

```

```

      val props1 = get-props pos1;
      val props2 = get-props pos2;

```

```

    in prod-ord
      (option-ord (prod-ord string-ord (prod-ord int-ord int-ord)))
      (option-ord (int-ord))
      (props1, props2) end

```

```
structure Postab = Table(type key = Position.T val ord = (pos-ord false));
structure Postab-strict = Table(type key = Position.T val ord = (pos-ord true));
```

```
signature AUTOLEVITY-BASE =
sig
  type extras = {levity-tag : string option, subgoals : int}
```

```
val get-transactions : unit -> ((string * extras) Postab-strict.table * string list
  Postab-strict.table) Symtab.table;
```

```
val get-applys : unit -> ((string * string list) list) Postab-strict.table Symtab.table;
```

```
val add-attribute-test: string -> (Proof.context -> thm -> bool) -> theory ->
  theory;
```

```
val attribs-of: Proof.context -> thm -> string list;
```

```
val used-facts: Proof.context option -> thm -> (string * thm) list;
val used-facts-attribs: Proof.context -> thm -> (string * string list) list;
```

```
(*
  Returns the proof body form of the prop proved by a theorem.
```

Unfortunately, proof bodies don't contain terms in the same form as what you'd get from things like 'Thm.full-prop-of': the proof body terms have sort constraints pulled out as separate assumptions, rather than as annotations on the types of terms.

It's easier for our dependency-tracking purposes to treat this transformed term as the 'canonical' form of a theorem, since it's always available as the top-level prop of a theorem's proof body.

```
*)
val proof-body-prop-of: thm -> term;
```

```
(*
  Get every (named) term that was proved in the proof body of the given thm.
```

The returned terms are in proof body form.

```
*)
val used-named-props-of: thm -> (string * term) list;
```

```
(*
  Distinguish whether the thm name foo-3 refers to foo(3) or foo-3 by comparing
  against the given term. Assumes the term is in proof body form.
```

```

    The provided context should match the context used to extract the (name, prop)
    pair
    (that is, it should match the context used to extract the thm passed into
    'proof-body-prop-of' or 'used-named-props-of').

    Returns SOME (foo, SOME 3) if the answer is 'it refers to foo(3)'.
    Returns SOME (foo-3, NONE) if the answer is 'it refers to foo-3'.
    Returns NONE if the answer is 'it doesn't seem to refer to anything.'
*)
val disambiguate-indices: Proof.context -> string * term -> (string * int option)
option;

(* Install toplevel hook for tracking command positions. *)

val setup-command-hook: {trace-apply : bool} -> theory -> theory;

(* Used to trace the dependencies of all apply statements.
   They are set up by setup-command-hook if the appropriate hooks in the Proof
   module exist. *)

val pre-apply-hook: Proof.context -> Method.text -> thm -> thm;
val post-apply-hook: Proof.context -> Method.text -> thm -> thm -> thm;

end;

structure AutoLevity-Base : AUTOLEVITY-BASE =
struct

val applys = Synchronized.var applys
  (Symtab.empty : ((string * string list) list) Postab-strict.table) Symtab.table)

fun get-applys () = Synchronized.value applys;

type extras = {levity-tag : string option, subgoals : int}

val transactions = Synchronized.var hook
  (Symtab.empty : ((string * extras) Postab-strict.table * ((string list) Postab-strict.table))
  Symtab.table);

fun get-transactions () =
  Synchronized.value transactions;

```

```

structure Data = Theory-Data
(
  type T = (bool *
    string option *
    (Proof.context -> thm -> bool) Symtab.table); (* command-hook * levity
tag * attribute tests *)
  val empty = (false, NONE, Symtab.empty);
  val extend = I;
  fun merge (((b1, -, tab), (b2, -, tab')) : T * T) = (b1 orelse b2, NONE,
Symtab.merge (fn - => true) (tab, tab'));
);

val set-command-hook-flag = Data.map (@{apply 3(1)} (fn - => true));
val get-command-hook-flag = #1 o Data.get

fun set-levity-tag tag = Data.map (@{apply 3(2)} (fn - => tag));
val get-levity-tag = #2 o Data.get

fun update-attrib-tab f = Data.map (@{apply 3(3)} f);

fun add-attribute-test nm f =
let
  val f' = (fn ctxt => fn thm => the-default false (try (f ctxt) thm))
in update-attrib-tab (Symtab.update-new (nm,f')) end;

val get-attribute-tests = Symtab.dest o #3 o Data.get;

(* Internal fact names get the naming scheme foo-3 to indicate the third
member of the multi-thm foo. We need to do some work to guess if
such a fact refers to an indexed multi-thm or a real fact named foo-3 *)

fun base-and-index nm =
let
  val exploded = space-explode - nm;
  val base =
    (exploded, (length exploded) - 1)
    |> try (List.take #> space-implode -)
    |> Option.mapPartial (Option.filter (fn nm => nm <> ))
  val idx = exploded |> try (List.last #> Int.fromString) |> Option.join;
in
  case (base, idx) of
    (SOME base, SOME idx) => SOME (base, idx)
  | - => NONE
end

fun maybe-nth idx xs = idx |> try (curry List.nth xs)

fun fact-from-derivation ctxt prop xnm =

```



```

let
  val facts = Proof-Context.facts-of ctxt;
  (* TODO: Check that exported local fact is equivalent to external one *)
  fun check-prop thm = Thm.full-prop-of thm = prop

  fun entry (name, idx) =
    (name, Position.none)
    |> try (Facts.retrieve (Context.Proof ctxt) facts)
    |> Option.mapPartial (#thms #> maybe-nth (idx - 1))
    |> Option.mapPartial (Option.filter check-prop)
    |> Option.map (pair name)

  val idx-result = (base-and-index xnm) |> Option.mapPartial entry
  val non-idx-result = (xnm, 1) |> entry

  val - =
    if is-some idx-result andalso is-some non-idx-result
    then warning (
      Levity: found two possible results for name ^ quote xnm ^ with the same
prop:\n ^
      (@{make-string} (the idx-result)) ^ ,\nand\n ^
      (@{make-string} (the non-idx-result)) ^ .\nUsing the first one.)
    else ()
  in
    merge-options (idx-result, non-idx-result)
  end

(* Local facts (from locales) aren't marked in proof bodies, we only
see their external variants. We guess the local name from the external one
(i.e. Theory-Name.Locale-Name.foo -> foo)

This is needed to perform localized attribute tests (e.g.. is this locale assumption
marked as simp?) *)

(* TODO: extend-locale breaks this naming scheme by adding the chunk qualifier.
This can
probably just be handled as a special case *)

fun most-local-fact-of ctxt xnm prop =
let
  val local-name = xnm |> try (Long-Name.explode #> tl #> tl #> Long-Name.implode)
  val local-result = local-name |> Option.mapPartial (fact-from-derivation ctxt
prop)
  fun global-result () = fact-from-derivation ctxt prop xnm
  in
    if is-some local-result then local-result else global-result ()
  end
end

```

```

fun thms-of (PBody {thms,...}) = thms

(* We recursively descend into the proof body to find dependent facts.
   We skip over empty derivations or facts that we fail to find, but recurse
   into their dependents. This ensures that an attempt to re-build the proof dependencies
   graph will result in a connected graph. *)

fun proof-body-deps
  (filter-name: string -> bool)
  (get-fact: string -> term -> (string * thm) option)
  (thm-ident, thm-node)
  (tab: (string * thm) option Inttab.table) =
let
  val name = Proofterm.thm-node-name thm-node
  val body = Proofterm.thm-node-body thm-node
  val prop = Proofterm.thm-node-prop thm-node
  val result = if filter-name name then NONE else get-fact name prop
  val is-new-result = not (Inttab.defined tab thm-ident)
  val insert = if is-new-result then Inttab.update (thm-ident, result) else I
  val descend =
    if is-new-result andalso is-none result
    then fold (proof-body-deps filter-name get-fact) (thms-of (Future.join body))
    else I
in
  tab |> insert |> descend
end

fun used-facts opt-ctxt thm =
let
  val nm = Thm.get-name-hint thm;
  val get-fact =
    case opt-ctxt of
      SOME ctxt => most-local-fact-of ctxt
    | NONE => fn name => fn - => (SOME (name, Drule.dummy-thm));
  val body = thms-of (Thm.proof-body-of thm);
  fun filter-name nm' = nm' = orelse nm' = nm;
in
  fold (proof-body-deps filter-name get-fact) body Inttab.empty
  |> Inttab.dest |> map-filter snd
end

fun attribs-of ctxt =
let
  val tests = get-attribute-tests (Proof-Context.theory-of ctxt)
  |> map (apsnd (fn test => test ctxt));
in
  (fn t => map-filter (fn (testnm, test) => if test t then SOME testnm else
    NONE) tests) end;

```

```

fun used-facts-attrs txt thm =
let
  val fact-nms = used-facts (SOME txt) thm;

  val attrs-of = attrs-of txt;

in map (apsnd attrs-of) fact-nms end

local
  fun app3 f g h x = (f x, g x, h x);

  datatype ('a, 'b) Either =
    Left of 'a
    | Right of 'b;

  local
    fun partition-map-foldr f (x, (ls, rs)) =
      case f x of
        Left l => (l :: ls, rs)
      | Right r => (ls, r :: rs);
  in
    fun partition-map f = List.foldr (partition-map-foldr f) ([], []);
  end

  (*
    Extracts the bits we care about from a thm-node: the name, the prop,
    and (the next steps of) the proof.
  *)
  val thm-node-dest =
    app3
      Profterm.thm-node-name
      Profterm.thm-node-prop
      (Profterm.thm-node-body #> Future.join);

  (*
    Partitioning function for thm-node data. We want to insert any named props,
    then recursively find the named props used by any unnamed intermediate/anonymous
    props.
  *)
  fun insert-or-descend (name, prop, proof) =
    if name = then Right proof else Left (name, prop);

  (*
    Extracts the next layer of proof data from a proof step.
  *)
  val next-level = thms-of #> List.map (snd #> thm-node-dest);

  (*
    Secretly used as a set, using '()' as the values.
  *)

```

```

*)
structure NamePropTab = Table(
  type key = string * term;
  val ord = prod-ord fast-string-ord Term-Ord.fast-term-ord);

val insert-all = List.foldr (fn (k, tab) => NamePropTab.update (k, ()) tab)

(*
  Proofterm.fold-body-thms unconditionally recursively descends into the proof
  body,
  so instead of only getting the topmost named props we'd get -all- of them. Here
  we do a more controlled recursion.
*)
fun used-props-foldr (proof, named-props) =
  let
    val (to-insert, child-proofs) =
      proof |> next-level |> partition-map insert-or-descend;
    val thms = insert-all named-props to-insert;
  in
    List.foldr used-props-foldr thms child-proofs
  end;

(*
  Extracts the outermost proof step of a thm (which is just the proof of the prop
  of the thm).
*)
val initial-proof =
  Thm.proof-body-of
  #> thms-of
  #> List.hd
  #> snd
  #> Proofterm.thm-node-body
  #> Future.join;

in
  fun used-named-props-of thm =
    let val used-props = used-props-foldr (initial-proof thm, NamePropTab.empty);
    in used-props |> NamePropTab.keys
    end;
end

val proof-body-prop-of =
  Thm.proof-body-of
  #> thms-of
  #> List.hd
  #> snd
  #> Proofterm.thm-node-prop

local

```

```

fun thm-matches prop thm = proof-body-prop-of thm = prop

fun entry ctxt prop (name, idx) =
  name
  |> try (Proof-Context.get-thms ctxt)
  |> Option.mapPartial (maybe-nth (idx - 1))
  |> Option.mapPartial (Option.filter (thm-matches prop))
  |> Option.map (K (name, SOME idx))

fun warn-if-ambiguous
  name
  (idx-result: (string * int option) option)
  (non-idx-result: (string * int option) option) =
  if is-some idx-result andalso is-some non-idx-result
  then warning (
    Levity: found two possible results for name ^ quote name ^ with the same
prop:\n ^
    (@{make-string} (the idx-result)) ^ ,\nand\n ^
    (@{make-string} (the non-idx-result)) ^ .\nUsing the first one.)
  else ()

in
  fun disambiguate-indices ctxt (name, prop) =
    let
      val entry = entry ctxt prop
      val idx-result = (base-and-index name) |> Option.mapPartial entry
      val non-idx-result = (name, 1) |> entry |> Option.map (apsnd (K NONE))
      val - = warn-if-ambiguous name idx-result non-idx-result
    in
      merge-options (idx-result, non-idx-result)
    end
end

(* We identify apply applications by the document position of their corresponding
method.
We can only get a document position out of real methods, so internal methods
(i.e. Method.Basic) won't have a position.*)

fun get-pos-of-text' (Method.Source src) = SOME (snd (Token.name-of-src src))
  | get-pos-of-text' (Method.Combinator (-, -, texts)) = get-first get-pos-of-text'
texts
  | get-pos-of-text' - = NONE

(* We only want to apply our hooks in batch mode, so we test if our position has a
line number
(in jEdit it will only have an id number) *)

fun get-pos-of-text text = case get-pos-of-text' text of
  SOME pos => if is-some (Position.line-of pos) then SOME pos else NONE

```

```

| NONE => NONE

(* Clear the theorem dependencies using the apply-trace oracle, then
   pick up the new ones after the apply step is finished. *)

fun pre-apply-hook ctxt text thm =
  case get-pos-of-text text of NONE => thm
  | SOME pos =>
    if Apply-Trace.can-clear (Proof-Context.theory-of ctxt)
    then Apply-Trace.clear-deps thm
    else thm;

val post-apply-hook = (fn ctxt => fn text => fn pre-thm => fn post-thm =>
  case get-pos-of-text text of NONE => post-thm
  | SOME pos => if Apply-Trace.can-clear (Proof-Context.theory-of ctxt) then
    (let
      val thy-nm = Context.theory-name (Thm.theory-of-thm post-thm);

      val used-facts = the-default [] (try (used-facts-attribs ctxt) post-thm);
      val - =
        Synchronized.change applies
        (Symtab.map-default
         (thy-nm, Postab-strict.empty) (Postab-strict.update (pos, used-facts)))

      (* We want to keep our old theorem dependencies around, so we put them back
         into
         the goal thm when we are done *)

      val post-thm' = post-thm
      |> Apply-Trace.join-deps pre-thm

      in post-thm' end)
    else post-thm)

(* The Proof hooks need to be patched in to track apply dependencies, but the rest
   of levity
   can work without them. Here we graciously fail if the hook interface is missing
   *)

fun setup-pre-apply-hook () =
  try (ML-Context.eval ML-Compiler.flags @{here})
  (ML-Lex.read-text (Proof.set-pre-apply-hook AutoLevity-Base.pre-apply-hook, @{here}));

fun setup-post-apply-hook () =
  try (ML-Context.eval ML-Compiler.flags @{here})
  (ML-Lex.read-text (Proof.set-post-apply-hook AutoLevity-Base.post-apply-hook,
    @{here}));

```

(This command is treated specially by AutoLevity-Theory-Report. The command executed directly*

*after this one will be tagged with the given tag *)*

val - =

*Outer-Syntax.command @{command-keyword levity-tag} tag for levity
 (Parse.string >> (fn str =>
 Toplevel.local-theory NONE NONE
 (Local-Theory.raw-theory (set-levity-tag (SOME str)))))*

fun get-subgoals' state =

let

*val proof-state = Toplevel.proof-of state;
 val {goal, ...} = Proof.raw-goal proof-state;*

in Thm.nprems-of goal end

fun get-subgoals state = the-default ~1 (try get-subgoals' state);

fun setup-toplevel-command-hook () =

Toplevel.add-hook (fn transition => fn start-state => fn end-state =>

*let val name = Toplevel.name-of transition
 val pos = Toplevel.pos-of transition;
 val thy = Toplevel.theory-of start-state;
 val thynm = Context.theory-name thy;
 val end-thy = Toplevel.theory-of end-state;*

in

*if name = clear-deps orelse name = dummy-apply orelse Position.line-of pos =
 NONE then () else*

(let

val levity-input = if name = levity-tag then get-levity-tag end-thy else NONE;

val subgoals = get-subgoals start-state;

val entry = {levity-tag = levity-input, subgoals = subgoals}

val - =

Synchronized.change transactions

*(Symtab.map-default (thynm, (Postab-strict.empty, Postab-strict.empty))
 (apfst (Postab-strict.update (pos, (name, entry)))))*

in () end) handle e => if Exn.is-interrupt e then Exn.reraise e else

Synchronized.change transactions

*(Symtab.map-default (thynm, (Postab-strict.empty, Postab-strict.empty))
 (apsnd (Postab-strict.map-default (pos, []) (cons (@{make-string}*

e))))

end)

fun setup-attrib-tests theory = if not (is-simp-installed) then

error Missing interface into Raw-Simplifier. Can't trace apply statements with un-

```

patched isabelle.
else
let
  fun is-first-cong ctxt thm =
    let
      val simpset = Raw-Simplifier.internal-ss (Raw-Simplifier.simpset-of ctxt);
      val (congs, -) = #congs simpset;
      val cong-thm = #mk-cong (#mk-rews simpset) ctxt thm;
    in
      case (find-first (fn (-, thm') => Thm.eq-thm-prop (cong-thm, thm')) congs)
    of
      SOME (nm, -) =>
        Thm.eq-thm-prop (find-first (fn (nm', -) => nm' = nm) congs |> the |>
snd, cong-thm)
      | NONE => false
    end

  fun is-classical proj ctxt thm =
    let
      val intros = proj (Classical.claset-of ctxt |> Classical.rep-cs);
      val results = Item-Net.retrieve intros (Thm.full-prop-of thm);
      in exists (fn (thm', -, -) => Thm.eq-thm-prop (thm', thm)) results end
    in
      theory
      |> add-attribute-test simp is-simp
      |> add-attribute-test cong is-first-cong
      |> add-attribute-test intro (is-classical #unsafeIs)
      |> add-attribute-test intro! (is-classical #safeIs)
      |> add-attribute-test elim (is-classical #unsafeEs)
      |> add-attribute-test elim! (is-classical #safeEs)
      |> add-attribute-test dest (fn ctxt => fn thm => is-classical #unsafeEs ctxt
(Tactic.make-elim thm))
      |> add-attribute-test dest! (fn ctxt => fn thm => is-classical #safeEs ctxt (Tactic.make-elim
thm))
    end

  fun setup-command-hook {trace-apply, ...} theory =
    if get-command-hook-flag theory then theory else
    let
      val - = if trace-apply then
        (the (setup-pre-apply-hook ());
         the (setup-post-apply-hook ()))
        handle Option => error Missing interface into Proof module. Can't trace
apply statements with unpatched isabelle
      else ()

      val - = setup-toplevel-command-hook ();
    end

```



```

    val theory' = theory
      |> trace-apply ? setup-attrb-tests
      |> set-command-hook-flag

in theory' end;

end
>

end

theory AutoLevity-Theory-Report
imports AutoLevity-Base
begin

ML <
(* An antiquotation for creating json-like serializers for
   simple records. Serializers for primitive types are automatically used,
   while serializers for complex types are given as parameters. *)
val JSON-string-encode: string -> string =
  String.translate (
    fn #\\ => \\\\
    | #\n => \\n
    | x => if Char.isPrint x then String.str x else
          \\u ^ align-right 0 4 (Int.fmt StringCvt.HEX (Char.ord x)))
  #> quote;

fun JSON-int-encode (i: int): string =
  if i < 0 then - ^ Int.toString (~i) else Int.toString i

val - = Theory.setup(
  ML-Antiquotation.inline @{binding string-record}
  (Scan.lift
    (Parse.name --|
      Parse.$$$ = --
      Parse.position Parse.string) >>
    (fn (name,(source,pos)) =>

  let

    val entries =
    let
      val chars = String.explode source
      |> filter-out (fn #\n => true | - => false)

    val trim =
      String.explode

```

```

#> chop-prefix (fn # => true | - => false)
#> snd
#> chop-suffix (fn # => true | - => false)
#> fst
#> String.implode

val str = String.implode chars
  |> String.fields (fn #, => true | #: => true | - => false)
  |> map trim

fun pairify [] = []
  | pairify (a::b::l) = ((a,b) :: pairify l)
  | pairify - = error (Record syntax error ^ Position.here pos)

in
  pairify str
end

val typedecl =
  type ^ name ^ = {
    ^ (map (fn (nm,typ) => nm ^ : ^ typ) entries |> String.concatWith .)
    ^ };

val base-typs = [string,int,bool, string list]

val encodes = map snd entries |> distinct (op =)
  |> filter-out (member (op =) base-typs)

val sanitize = String.explode
#> map (fn # => #-
  | #- => #-
  | #* => #P
  | #( => #B
  | #) => #R
  | x => x)
#> String.implode

fun mk-encode typ =
  if typ = string
  then JSON-string-encode
  else if typ = int
  then JSON-int-encode
  else if typ = bool
  then Bool.toString
  else if typ = string list
  then (fn xs => (enclose \"\ \"\ (String.concatWith \"\ \"\ (map JSON-string-encode
xs))))

```

```

else (sanitize typ) ^ -encode

fun mk-elem nm - value =
  (ML-Syntax.print-string (JSON-string-encode nm) ^ ^ \ : \ ) ^ ^ ( ^ value
^ )

fun mk-head body =
  (\ ^ {\ ^ String.concatWith \, \ ( ^ body ^ ) ^ }\)

val global-head = if (null encodes) then else
fn ( ^ (map mk-encode encodes |> String.concatWith ,) ^ ) =>

val encode-body =
  fn { ^ (map fst entries |> String.concatWith ,) ^ } : ^ name ^ => ^
  mk-head
  (ML-Syntax.print-list (fn (field,typ) => mk-elem field typ (mk-encode typ ^
^ field)) entries)

val val-expr =
val ( ^ name ^ -encode) = (
  ^ global-head ^ ( ^ encode-body ^ ))

val - = @{print} val-expr

in
  typedecl ^ val-expr
end)))

```

ML <

```

@{string-record deps = consts : string list, types: string list}
@{string-record lemma-deps = consts: string list, types: string list, lemmas: string
list}
@{string-record location = file : string, start-line : int, end-line : int}
@{string-record levity-tag = tag : string, location : location}
@{string-record apply-dep = name : string, attribs : string list}

@{string-record proof-command =
  command-name : string, location : location, subgoals : int, depth : int,
  apply-deps : apply-dep list }

@{string-record lemma-entry =
  name : string, command-name : string, levity-tag : levity-tag option, location :
location,

```

```

    proof-commands : proof-command list,
    deps : lemma-deps}

@{string-record dep-entry =
  name : string, command-name : string, levity-tag : levity-tag option, location:
location,
  deps : deps}

@{string-record theory-entry =
  name : string, file : string}

@{string-record log-entry =
  errors : string list, location : location}

fun encode-list enc x = [ ^ (String.concatWith , (map enc x)) ^ ]

fun encode-option enc (SOME x) = enc x
  | encode-option - NONE = {}

val opt-levity-tag-encode = encode-option (levity-tag-encode location-encode);

val proof-command-encode = proof-command-encode (location-encode, encode-list
apply-dep-encode);

val lemma-entry-encode = lemma-entry-encode
  (opt-levity-tag-encode, location-encode, encode-list proof-command-encode, lemma-deps-encode)

val dep-entry-encode = dep-entry-encode
  (opt-levity-tag-encode, location-encode, deps-encode)

val log-entry-encode = log-entry-encode (location-encode)

}

ML (

signature AUTOLEVITY-THEORY-REPORT =
sig
val get-reports-for-thy: theory ->
  string * log-entry list * theory-entry list * lemma-entry list * dep-entry list *
  dep-entry list

val string-reports-of:
  string * log-entry list * theory-entry list * lemma-entry list * dep-entry list *
  dep-entry list
  -> string list

end;

```

```

structure AutoLevity-Theory-Report : AUTOLEVITY-THEORY-REPORT =
struct

fun map-pos-line f pos =
let
  val line = Position.line-of pos |> the;
  val file = Position.file-of pos |> the;

  val line' = f line;

  val - = if line' < 1 then raise Option else ();

in SOME (Position.line-file-only line' file) end handle Option => NONE

(* A Position.T table based on offsets (Postab-strict) can be collapsed into a line-based
one
with lists of entries on for each line. This function searches such a table
for the closest entry, either backwards (LESS) or forwards (GREATER) from
the given position. *)

(* TODO: If everything is sane then the search depth shouldn't be necessary. In
practice
entries won't be more than one or two lines apart, but if something has gone
wrong in the
collection phase we might end up wasting a lot of time looking for an entry that
doesn't exist. *)

fun search-by-lines depth ord-kind f h pos = if depth = 0 then NONE else
let
  val line-change = case ord-kind of LESS => ~1 | GREATER => 1 | - =>
raise Fail Bad relation
  val idx-change = case ord-kind of GREATER => 1 | - => 0;
in
  case f pos of
    SOME x =>
      let
        val i = find-index (fn e => h (pos, e) = ord-kind) x;
      in if i > ~1 then SOME (List.nth(x, i + idx-change)) else SOME (hd x) end
    | NONE =>
      (case (map-pos-line (fn i => i + line-change) pos) of
        SOME pos' => search-by-lines (depth - 1) ord-kind f h pos'
        | NONE => NONE)
      end
end

fun location-from-range (start-pos, end-pos) =
let
  val start-file = Position.file-of start-pos |> the;

```

```

    val end-file = Position.file-of end-pos |> the;
    val - = if start-file = end-file then () else raise Option;
    val start-line = Position.line-of start-pos |> the;
    val end-line = Position.line-of end-pos |> the;
  in
    SOME ({file = start-file, start-line = start-line, end-line = end-line} : location)
  end
  handle Option => NONE

(* Here we collapse our proofs (lemma foo .. done) into single entries with start/end
positions. *)

fun get-command-ranges-of keywords thy-nm =
let
  fun is-ignored nm' = nm' = <ignored>
  fun is-levity-tag nm' = nm' = levity-tag

  fun is-proof-cmd nm' = nm' = apply orelse nm' = by orelse nm' = proof

(* All top-level transactions for the given theory *)

  val (transactions, log) =
    Symtab.lookup (AutoLevity-Base.get-transactions ()) thy-nm
    |> the-default (Postab-strict.empty, Postab-strict.empty)
    ||> Postab-strict.dest
    |>> Postab-strict.dest

(* Line-based position table of all apply statements for the given theory *)

  val applytab =
    Symtab.lookup (AutoLevity-Base.get-applys ()) thy-nm
    |> the-default Postab-strict.empty
    |> Postab-strict.dest
    |> map (fn (pos,e) => (pos, (pos,e)))
    |> Postab.make-list
    |> Postab.map (fn - => sort (fn ((pos,-),(pos',-)) => pos-ord true (pos, pos'))))

(* A special ignored command lets us find the real end of commands which span
multiple lines. After finding a real command, we assume the last ignored one
was part of the syntax for that command *)

fun find-cmd-end last-pos ((pos', (nm', ext)) :: rest) =
  if is-ignored nm' then
    find-cmd-end pos' rest
  else (last-pos, ((pos', (nm', ext)) :: rest))
  | find-cmd-end last-pos [] = (last-pos, [])

fun change-level nm level =

```

```

    if Keyword.is-proof-open keywords nm then level + 1
    else if Keyword.is-proof-close keywords nm then level - 1
    else if Keyword.is-qed-global keywords nm then ~1
    else level

fun make-apply-deps lemma-deps =
  map (fn (nm, atts) => {name = nm, attribs = atts} : apply-dep) lemma-deps

(* For a given apply statement, search forward in the document for the closest
method to retrieve
its lemma dependencies *)

fun find-apply pos = if Postab.is-empty applytab then [] else
  search-by-lines 5 GREATER (Postab.lookup applytab) (fn (pos, (pos', -)) =>
pos-ord true (pos, pos')) pos
|> Option.map snd |> the-default [] |> make-apply-deps

fun find-proof-end level ((pos', (nm', ext)) :: rest) =
  let val level' = change-level nm' level in
  if level' > ~1 then
    let
      val (cmd-end, rest') = find-cmd-end pos' rest;
      val ((prf-cmds, prf-end), rest'') = find-proof-end level' rest'
    in (({command-name = nm', location = location-from-range (pos', cmd-end)
|> the,
      depth = level, apply-deps = if is-proof-cmd nm' then find-apply pos' else [],
      subgoals = #subgoals ext} :: prf-cmds, prf-end), rest'') end
    else
      let
        val (cmd-end, rest') = find-cmd-end pos' rest;
        in (({command-name = nm', location = location-from-range (pos', cmd-end)
|> the,
          apply-deps = if is-proof-cmd nm' then find-apply pos' else [],
          depth = level, subgoals = #subgoals ext}], cmd-end), rest') end
      end
  | find-proof-end - - = (([], Position.none), [])

fun find-ends tab tag ((pos,(nm, ext)) :: rest) =
  let
    val (cmd-end, rest') = find-cmd-end pos rest;

    val ((prf-cmds, pos'), rest'') =
      if Keyword.is-theory-goal keywords nm
      then find-proof-end 0 rest'
      else (([],cmd-end),rest'');
  end

```

```

    val tab' = Postab.cons-list (pos, (pos, (nm, pos', tag, prf-cmds))) tab;

    val tag' =
      if is-levity-tag nm then Option.map (rpair (pos,pos')) (#levity-tag ext) else
      NONE;

    in find-ends tab' tag' rest'' end
      | find-ends tab - [] = tab

    val command-ranges = find-ends Postab.empty NONE transactions
      |> Postab.map (fn - => sort (fn ((pos,-),(pos',-)) => pos-ord true (pos, pos'))))

    in (command-ranges, log) end

fun make-deps (const-deps, type-deps): deps =
  {consts = distinct (op =) const-deps, types = distinct (op =) type-deps}

fun make-lemma-deps (const-deps, type-deps, lemma-deps): lemma-deps =
  {
    consts = distinct (op =) const-deps,
    types = distinct (op =) type-deps,
    lemmas = distinct (op =) lemma-deps
  }

fun make-tag (SOME (tag, range)) = (case location-from-range range
  of SOME rng => SOME ({tag = tag, location = rng} : levity-tag)
  | NONE => NONE)
  | make-tag NONE = NONE

fun add-deps (((Defs.Const, nm), -) :: rest) =
  let val (consts, types) = add-deps rest in
    (nm :: consts, types) end
  | add-deps (((Defs.Type, nm), -) :: rest) =
  let val (consts, types) = add-deps rest in
    (consts, nm :: types) end
  | add-deps - = ([], [])

fun get-deps ({rhs, ...} : Defs.spec) = add-deps rhs

fun typs-of-typ (Type (nm, Ts)) = nm :: (map typs-of-typ Ts |> flat)
  | typs-of-typ - = []

fun typs-of-term t = Term.fold-types (append o typs-of-typ) t []

fun deps-of-thm thm =

```



```

let
  val consts = Term.add-const-names (Thm.prop-of thm) [];
  val types = typs-of-term (Thm.prop-of thm);
in (consts, types) end

fun file-of-thy thy =
  let
    val path = Resources.master-directory thy;
    val name = Context.theory-name thy;
    val path' = Path.append path (Path.basic (name ^ ".thy"))
  in Path.smart-implode path' end;

fun entry-of-thy thy = ({name = Context.theory-name thy, file = file-of-thy thy}
: theory-entry)

fun used-facts thy thm =
  AutoLevity-Base.used-named-props-of thm
  |> map-filter (AutoLevity-Base.disambiguate-indices (Proof-Context.init-global
thy))
  |> List.map fst;

fun get-reports-for-thy thy =
  let
    val thy-nm = Context.theory-name thy;
    val all-facts = Global-Theory.facts-of thy;
    val fact-space = Facts.space-of all-facts;

    val (tab, log) = get-command-ranges-of (Thy-Header.get-keywords thy) thy-nm;

    val parent-facts = map Global-Theory.facts-of (Theory.parents-of thy);

    val search-backwards = search-by-lines 5 LESS (Postab.lookup tab)
      (fn (pos, (pos', -)) => pos-ord true (pos, pos'))
      #> the

    val lemmas = Facts.dest-static false parent-facts (Global-Theory.facts-of thy)
  |> map-filter (fn (xnm, thms) =>
    let
      val {pos, theory-name, ...} = Name-Space.the-entry fact-space xnm;
    in
      if theory-name = thy-nm then
        let
          val thms' = map (Thm.transfer thy) thms;

          val (real-start, (cmd-name, end-pos, tag, prf-cmds)) = search-backwards
pos

          val lemma-deps =
            if cmd-name = datatype

```

```

      then []
      else map (used-facts thy) thms' |> flat |> distinct (op =);

flat
val (consts, types) = map deps-of-thm thms' |> ListPair.unzip |> apply2

val deps = make-lemma-deps (consts, types, lemma-deps)

val location = location-from-range (real-start, end-pos) |> the;

tag,
val (lemma-entry : lemma-entry) =
  {name = xnm, command-name = cmd-name, levity-tag = make-tag

    location = location, proof-commands = prf-cmds, deps = deps}

    in SOME (pos, lemma-entry) end
    else NONE end handle Option => NONE)
|> Postab-strict.make-list
|> Postab-strict.dest |> map snd |> flat

val defs = Theory.defs-of thy;

fun get-deps-of kind space xnms = xnms
|> map-filter (fn xnm =>
  let
    val {pos, theory-name, ...} = Name-Space.the-entry space xnm;
  in
    if theory-name = thy-nm then
      let
        val specs = Defs.specifications-of defs (kind, xnm);

        val deps =
          map get-deps specs
        |> ListPair.unzip
        |> (apply2 flat #> make-deps);

        val (real-start, (cmd-name, end-pos, tag, -)) = search-backwards pos

        val loc = location-from-range (real-start, end-pos) |> the;

        val entry =
          ({name = xnm, command-name = cmd-name, levity-tag = make-tag

            location = loc, deps = deps} : dep-entry)

          in SOME (pos, entry) end
          else NONE end handle Option => NONE)
|> Postab-strict.make-list
|> Postab-strict.dest |> map snd |> flat

```

```

    val {const-space, constants, ...} = Consts.dest (Sign.consts-of thy);

    val consts = get-deps-of Defs.Const const-space (map fst constants);

    val {types, ...} = Type.rep-tsig (Sign.tsig-of thy);

    val type-space = Name-Space.space-of-table types;
    val type-names = Name-Space.fold-table (fn (xnm, -) => cons xnm) types [];

    val types = get-deps-of Defs.Type type-space type-names;

    val thy-parents = map entry-of-thy (Theory.parents-of thy);

    val logs = log |>
      map (fn (pos, errs) => {errors = errs, location = location-from-range (pos,
pos) |> the} : log-entry)

    in (thy-nm, logs, thy-parents, lemmas, consts, types) end

fun add-commas (s :: s' :: ss) = s ^ , :: (add-commas (s' :: ss))
  | add-commas [s] = [s]
  | add-commas - = []

fun string-reports-of (thy-nm, logs, thy-parents, lemmas, consts, types) =
  [{theory-name\ : ^ JSON-string-encode thy-nm ^ ,] @
  [\logs\ : [] @
  add-commas (map (log-entry-encode) logs) @
  [,,\theory-imports\ : [] @
  add-commas (map (theory-entry-encode) thy-parents) @
  [,,\lemmas\ : [] @
  add-commas (map (lemma-entry-encode) lemmas) @
  [,,\consts\ : [] @
  add-commas (map (dep-entry-encode) consts) @
  [,,\types\ : [] @
  add-commas (map (dep-entry-encode) types) @
  []}]
  |> map (fn s => s ^ \n)

end
}

end

theory AutoLevity-Hooks
imports
  AutoLevity-Base
  AutoLevity-Theory-Report

```

begin

end

theory *Locale-Abbrev*

imports *Main*

keywords *revert-abbrev* :: *thy-decl* **and** *locale-abbrev* :: *thy-decl*
begin

ML \langle

local

fun *revert-abbrev* (*mode*,*name*) *lthy* =

let

val *the-const* = (*fst* *o* *dest-Const*) *oo* *Proof-Context.read-const* {*proper* = *true*,
strict = *false*};

in

Local-Theory.raw-theory (*Sign.revert-abbrev* (*fst* *mode*) (*the-const* *lthy* *name*))

lthy

end

fun *name-of spec lthy* = *Local-Defs.abs-def* (*Syntax.read-term lthy spec*) |> #1 |>
#1

in

val - =

Outer-Syntax.local-theory @{*command-keyword* *revert-abbrev*}

make an abbreviation available for output

(*Parse.syntax-mode* -- *Parse.const* >> *revert-abbrev*)

val - =

Outer-Syntax.local-theory' @{*command-keyword* *locale-abbrev*}

constant abbreviation that provides also provides printing in locales

(*Parse.syntax-mode* -- *Scan.option Parse-Spec.constdecl* -- *Parse.prop* --

Parse.for-fixes

>> (*fn* (((*mode*, *decl*), *spec*), *params*) => *fn* *restricted* => *fn* *lthy* =>

lthy

|> *Local-Theory.open-target* |> *snd*

|> *Specification.abbreviation-cmd* *mode* *decl* *params* *spec* *restricted*

|> *Local-Theory.close-target* (* *commit new abbrev. name* *)

|> *revert-abbrev* (*mode*, *name-of spec lthy*));

end

\rangle

end

```
theory NICTATools
imports
  Apply-Trace-Cmd
  Apply-Debug
  Find-Names

  Rule-By-Method
  Eisbach-Methods
  TSubst
  Time-Methods-Cmd
  Try-Attribute
  Trace-Schematic-Insts
  Insulin
  ShowTypes
  AutoLevity-Hooks
  Locale-Abbrev
begin
```

11 Detect unused meta-forall

ML <

```
(* Return a list of meta-forall variable names that appear
 * to be unused in the input term. *)
fun find-unused-metaall (Const (@{const-name Pure.all}, -) $ Abs (n, -, t)) =
  (if not (Term.is-dependent t) then [n] else []) @ find-unused-metaall t
| find-unused-metaall (Abs (-, -, t)) =
  find-unused-metaall t
| find-unused-metaall (a $ b) =
  find-unused-metaall a @ find-unused-metaall b
| find-unused-metaall - = []

(* Given a proof state, analyse its assumptions for unused
 * meta-foralls. *)
fun detect-unused-meta-forall - (state : Proof.state) =
let
  (* Fetch all assumptions and the main goal, and analyse them. *)
  val {context = lthy, goal = goal, ...} = Proof.goal state
  val checked-terms =
    [Thm.concl-of goal] @ map Thm.term-of (Assumption.all-assms-of lthy)
  val results = List.concat (map find-unused-metaall checked-terms)

  (* Produce a message. *)
  fun message results =
    Pretty.paragraph [
```

```

    Pretty.str Unused meta-forall(s): ,
    Pretty.commas
      (map (fn b => Pretty.mark-str (Markup.bound, b)) results)
    |> Pretty.paragraph,
    Pretty.str .
  ]

(* We use a warning instead of the standard mechanisms so that
   * we can produce a warning icon in Isabelle/jEdit. *)
val - =
  if length results > 0 then
    warning (message results |> Pretty.string-of)
  else ()
in
  (false, (, []))
end

(* Setup the tool, stealing the auto-solve-direct option. *)
val - = Try.tool-setup (unused-meta-forall,
  (1, @{system-option auto-solve-direct}, detect-unused-meta-forall))
)

lemma test-unused-meta-forall:  $\bigwedge x. y \vee \neg y$ 
oops

end
Library theory Lib
imports
  Value-Abbreviation
  Match-Abbreviation
  Try-Methods
  Extract-Conjunct
  Eval-Bool
  NICTATools
  HOL-Library.Prefix-Order
  HOL-Word.Word
begin

abbreviation (input)
  split :: ('a  $\Rightarrow$  'b  $\Rightarrow$  'c)  $\Rightarrow$  'a  $\times$  'b  $\Rightarrow$  'c
where
  split == case-prod

lemma hd-map-simp:
  b  $\neq [] \implies \text{hd} (\text{map } a \ b) = a \ (\text{hd } b)$ 
by (rule hd-map)

```

lemma *tl-map-simp*:
 $tl (map\ a\ b) = map\ a\ (tl\ b)$
by (*induct b, auto*)

lemma *Collect-eq*:
 $\{x. P\ x\} = \{x. Q\ x\} \longleftrightarrow (\forall x. P\ x = Q\ x)$
by (*rule iffI*) *auto*

lemma *iff-impI*: $\llbracket P \implies Q = R \rrbracket \implies (P \longrightarrow Q) = (P \longrightarrow R)$ **by** *blast*

definition
 $fun\text{-}app :: ('a \Rightarrow 'b) \Rightarrow 'a \Rightarrow 'b$ (**infixr** \$ 10) **where**
 $f\ \$\ x \equiv f\ x$

declare *fun-app-def* [*iff*]

lemma *fun-app-cong*[*fundef-cong*]:
 $\llbracket f\ x = f'\ x' \rrbracket \implies (f\ \$\ x) = (f'\ \$\ x')$
by *simp*

lemma *fun-app-apply-cong*[*fundef-cong*]:
 $f\ x\ y = f'\ x'\ y' \implies (f\ \$\ x)\ y = (f'\ \$\ x')\ y'$
by *simp*

lemma *if-apply-cong*[*fundef-cong*]:
 $\llbracket P = P'; x = x'; P' \implies f\ x' = f'\ x'; \neg P' \implies g\ x' = g'\ x' \rrbracket$
 $\implies (if\ P\ then\ f\ else\ g)\ x = (if\ P'\ then\ f'\ else\ g')\ x'$
by *simp*

lemma *case-prod-apply-cong*[*fundef-cong*]:
 $\llbracket f\ (fst\ p)\ (snd\ p)\ s = f'\ (fst\ p')\ (snd\ p')\ s' \rrbracket \implies case\text{-}prod\ f\ p\ s = case\text{-}prod\ f'\ p'\ s'$
by (*simp add: split-def*)

lemma *prod-injects*:
 $(x,y) = p \implies x = fst\ p \wedge y = snd\ p$
 $p = (x,y) \implies x = fst\ p \wedge y = snd\ p$
by *auto*

definition
 $pred\text{-}conj :: ('a \Rightarrow bool) \Rightarrow ('a \Rightarrow bool) \Rightarrow ('a \Rightarrow bool)$ (**infixl** and 35)
where
 $pred\text{-}conj\ P\ Q \equiv \lambda x. P\ x \wedge Q\ x$

definition

pred-disj :: ('a \Rightarrow bool) \Rightarrow ('a \Rightarrow bool) \Rightarrow ('a \Rightarrow bool) (**infixl** or 30)
where
pred-disj P Q $\equiv \lambda x. P\ x \vee Q\ x$

definition
pred-neg :: ('a \Rightarrow bool) \Rightarrow ('a \Rightarrow bool) (*not* - [40] 40)
where
pred-neg P $\equiv \lambda x. \neg P\ x$

definition K $\equiv \lambda x\ y. x$

definition
zipWith :: ('a \Rightarrow 'b \Rightarrow 'c) \Rightarrow 'a list \Rightarrow 'b list \Rightarrow 'c list **where**
zipWith f xs ys $\equiv \text{map } (\text{case-prod } f) (\text{zip } xs\ ys)$

primrec
delete :: 'a \Rightarrow 'a list \Rightarrow 'a list
where
delete y [] = []
| *delete* y (x#xs) = (if y=x then xs else x # *delete* y xs)

definition
swp f $\equiv \lambda x\ y. f\ y\ x$

lemma *swp-apply[simp]*: *swp* f y x = f x y
by (*simp add: swp-def*)

primrec (*nonexhaustive*)
theRight :: 'a + 'b \Rightarrow 'b **where**
theRight (Inr x) = x

primrec (*nonexhaustive*)
theLeft :: 'a + 'b \Rightarrow 'a **where**
theLeft (Inl x) = x

definition
isLeft x $\equiv (\exists y. x = \text{Inl } y)$

definition
isRight x $\equiv (\exists y. x = \text{Inr } y)$

definition
const x $\equiv \lambda y. x$

primrec
opt-rel :: ('a \Rightarrow 'b \Rightarrow bool) \Rightarrow 'a option \Rightarrow 'b option \Rightarrow bool
where
opt-rel f None y = (y = None)
| *opt-rel* f (Some x) y = ($\exists y'. y = \text{Some } y' \wedge f\ x\ y'$)

lemma *opt-rel-None-rhs*[simp]:
 $\text{opt-rel } f \ x \ \text{None} = (x = \text{None})$
by (*cases x, simp-all*)

lemma *opt-rel-Some-rhs*[simp]:
 $\text{opt-rel } f \ x \ (\text{Some } y) = (\exists x'. x = \text{Some } x' \wedge f \ x' \ y)$
by (*cases x, simp-all*)

lemma *trancld2*:
 $(x, y) \in R^+ \implies \exists z. (x, z) \in R^* \wedge (z, y) \in R$
by (*erule trancldE*) *auto*

lemma *linorder-min-same1* [simp]:
 $(\min y \ x = y) = (y \leq (x::'a::\text{linorder}))$
by (*auto simp: min-def linorder-not-less*)

lemma *linorder-min-same2* [simp]:
 $(\min x \ y = y) = (y \leq (x::'a::\text{linorder}))$
by (*auto simp: min-def linorder-not-le*)

A combinator for pairing up well-formed relations. The divisor function splits the population in halves, with the True half greater than the False half, and the supplied relations control the order within the halves.

definition

$\text{wf-sum} :: ('a \Rightarrow \text{bool}) \Rightarrow ('a \times 'a) \text{ set} \Rightarrow ('a \times 'a) \text{ set} \Rightarrow ('a \times 'a) \text{ set}$

where

$\text{wf-sum divisor } r \ r' \equiv$
 $(\{(x, y). \neg \text{divisor } x \wedge \neg \text{divisor } y\} \cap r')$
 $\cup \{(x, y). \neg \text{divisor } x \wedge \text{divisor } y\}$
 $\cup (\{(x, y). \text{divisor } x \wedge \text{divisor } y\} \cap r)$

lemma *wf-sum-wf*:

$\llbracket \text{wf } r; \text{wf } r' \rrbracket \implies \text{wf } (\text{wf-sum divisor } r \ r')$

apply (*simp add: wf-sum-def*)

apply (*rule wf-Un*)**+**

apply (*erule wf-Int2*)

apply (*rule wf-subset*)

[where $r = \text{measure } (\lambda x. \text{If } (\text{divisor } x) \ 1 \ 0)$ **])**

apply *simp*

apply *clarsimp*

apply *blast*

apply (*erule wf-Int2*)

apply *blast*

done

abbreviation(*input*)

$\text{option-map} == \text{map-option}$

lemmas *option-map-def* = *map-option-case*

lemma *False-implies-equals* [*simp*]:
 $((False \implies P) \implies PROP\ Q) \equiv PROP\ Q$
apply (*rule equal-intr-rule*)
apply (*erule meta-mp*)
apply *simp*
apply *simp*
done

lemma *split-paired-Ball*:
 $(\forall x \in A. P\ x) = (\forall x\ y. (x,y) \in A \longrightarrow P\ (x,y))$
by *auto*

lemma *split-paired-Bex*:
 $(\exists x \in A. P\ x) = (\exists x\ y. (x,y) \in A \wedge P\ (x,y))$
by *auto*

lemma *delete-remove1*:
 $delete\ x\ xs = remove1\ x\ xs$
by (*induct xs, auto*)

lemma *ignore-if*:
 $(y\ and\ z)\ s \implies (if\ x\ then\ y\ else\ z)\ s$
by (*clarsimp simp: pred-conj-def*)

lemma *zipWith-Nil2* :
 $zipWith\ f\ xs\ [] = []$
unfolding *zipWith-def* **by** *simp*

lemma *isRight-right-map*:
 $isRight\ (case-sum\ Inl\ (Inr\ o\ f)\ v) = isRight\ v$
by (*simp add: isRight-def split: sum.split*)

lemma *zipWith-nth*:
 $\llbracket n < \min\ (length\ xs)\ (length\ ys) \rrbracket \implies zipWith\ f\ xs\ ys\ !\ n = f\ (xs\ !\ n)\ (ys\ !\ n)$
unfolding *zipWith-def* **by** *simp*

lemma *length-zipWith* [*simp*]:
 $length\ (zipWith\ f\ xs\ ys) = \min\ (length\ xs)\ (length\ ys)$
unfolding *zipWith-def* **by** *simp*

lemma *first-in-uptoD*:
 $a \leq b \implies (a::'a::order) \in \{a..b\}$
by *simp*

lemma *construct-singleton*:

$\llbracket S \neq \{\}; \forall s \in S. \forall s'. s \neq s' \longrightarrow s' \notin S \rrbracket \Longrightarrow \exists x. S = \{x\}$
by *blast*

lemmas *insort-com* = *insort-left-comm*

lemma *bleeding-obvious*:
 $(P \Longrightarrow \text{True}) \equiv (\text{Trueprop } \text{True})$
by (*rule*, *simp-all*)

lemma *Some-helper*:
 $x = \text{Some } y \Longrightarrow x \neq \text{None}$
by *simp*

lemma *in-empty-interE*:
 $\llbracket A \cap B = \{\}; x \in A; x \in B \rrbracket \Longrightarrow \text{False}$
by *blast*

lemma *None-upd-eq*:
 $g \ x = \text{None} \Longrightarrow g(x := \text{None}) = g$
by (*rule ext*) *simp*

lemma *exx [iff]*: $\exists x. x$ **by** *blast*
lemma *ExNot [iff]*: $Ex \text{ Not}$ **by** *blast*

lemma *cases-simp2 [simp]*:
 $((\neg P \longrightarrow Q) \wedge (P \longrightarrow Q)) = Q$
by *blast*

lemma *a-imp-b-imp-b*:
 $((a \longrightarrow b) \longrightarrow b) = (a \vee b)$
by *blast*

lemma *length-neq*:
 $\text{length } as \neq \text{length } bs \Longrightarrow as \neq bs$ **by** *auto*

lemma *take-neq-length*:
 $\llbracket x \neq y; x \leq \text{length } as; y \leq \text{length } bs \rrbracket \Longrightarrow \text{take } x \ as \neq \text{take } y \ bs$
by (*rule length-neq*, *simp*)

lemma *eq-concat-lenD*:
 $xs = ys @ zs \Longrightarrow \text{length } xs = \text{length } ys + \text{length } zs$
by *simp*

lemma *map-upt-reindex'*: $\text{map } f \ [a \ ..< b] = \text{map } (\lambda n. f \ (n + a - x)) \ [x \ ..< x + b - a]$
by (*rule nth-equalityI*; *clarsimp simp: add commute*)

lemma *map-upt-reindex*: $\text{map } f \ [a \ ..< b] = \text{map } (\lambda n. f \ (n + a)) \ [0 \ ..< b - a]$
by (*subst map-upt-reindex'* [**where** $x=0$]) *clarsimp*

lemma *notemptyI*:
 $x \in S \implies S \neq \{\}$
by *clarsimp*

lemma *setcomp-Max-has-prop*:
assumes $a: P\ x$
shows $P\ (\text{Max}\ \{(x::'a::\{\text{finite}, \text{linorder}\})\}. P\ x)$
proof $-$
from a **have** $\text{Max}\ \{x. P\ x\} \in \{x. P\ x\}$
by $-(\text{rule Max-in, auto intro: notemptyI})$
thus *?thesis* **by** *auto*
qed

lemma *cons-set-intro*:
 $\text{lst} = x \# xs \implies x \in \text{set lst}$
by *fastforce*

lemma *list-all2-conj-nth*:
assumes $\text{lall}: \text{list-all2}\ P\ \text{as}\ \text{cs}$
and $\text{rl}: \bigwedge n. \llbracket P\ (\text{as}!\ n)\ (\text{cs}!\ n); n < \text{length as} \rrbracket \implies Q\ (\text{as}!\ n)\ (\text{cs}!\ n)$
shows $\text{list-all2}\ (\lambda a\ b. P\ a\ b \wedge Q\ a\ b)\ \text{as}\ \text{cs}$
proof $(\text{rule list-all2-all-nthI})$
from lall **show** $\text{length as} = \text{length cs} ..$
next
fix n
assume $n < \text{length as}$

show $P\ (\text{as}!\ n)\ (\text{cs}!\ n) \wedge Q\ (\text{as}!\ n)\ (\text{cs}!\ n)$
proof
from lall **show** $P\ (\text{as}!\ n)\ (\text{cs}!\ n)$ **by** $(\text{rule list-all2-nthD})\ \text{fact}$
thus $Q\ (\text{as}!\ n)\ (\text{cs}!\ n)$ **by** $(\text{rule rl})\ \text{fact}$
qed
qed

lemma *list-all2-conj*:
assumes $\text{lall1}: \text{list-all2}\ P\ \text{as}\ \text{cs}$
and $\text{lall2}: \text{list-all2}\ Q\ \text{as}\ \text{cs}$
shows $\text{list-all2}\ (\lambda a\ b. P\ a\ b \wedge Q\ a\ b)\ \text{as}\ \text{cs}$
proof $(\text{rule list-all2-all-nthI})$
from lall1 **show** $\text{length as} = \text{length cs} ..$
next
fix n
assume $n < \text{length as}$

show $P\ (\text{as}!\ n)\ (\text{cs}!\ n) \wedge Q\ (\text{as}!\ n)\ (\text{cs}!\ n)$
proof
from lall1 **show** $P\ (\text{as}!\ n)\ (\text{cs}!\ n)$ **by** $(\text{rule list-all2-nthD})\ \text{fact}$
from lall2 **show** $Q\ (\text{as}!\ n)\ (\text{cs}!\ n)$ **by** $(\text{rule list-all2-nthD})\ \text{fact}$

qed
qed

lemma *all-set-into-list-all2*:
 assumes *lall*: $\forall x \in \text{set } ls. P x$
 and $\text{length } ls = \text{length } ls'$
 shows *list-all2* $(\lambda a b. P a)$ *ls* *ls'*
proof (*rule list-all2-all-nthI*)
 fix *n*
 assume $n < \text{length } ls$
 from *lall* show $P (ls ! n)$
 by (*rule bspec [OF - nth-mem]*) *fact*
 qed *fact*

lemma *GREATEST-lessE*:
 fixes *x* :: '*a* :: order
 assumes *gts*: $(\text{GREATEST } x. P x) < X$
 and *px*: $P x$
 and *gtst*: $\exists \text{max}. P \text{max} \wedge (\forall z. P z \longrightarrow (z \leq \text{max}))$
 shows $x < X$
proof –
 from *gtst* obtain *max* where *pm*: $P \text{max}$ and *g'*: $\bigwedge z. P z \implies z \leq \text{max}$
 by *auto*

 hence $(\text{GREATEST } x. P x) = \text{max}$
 by (*auto intro: Greatest-equality*)

 moreover have $x \leq \text{max}$ using *px* by (*rule g'*)

 ultimately show *?thesis* using *gts* by *simp*
 qed

lemma *set-has-max*:
 fixes *ls* :: ('*a* :: linorder) list
 assumes *ls*: $ls \neq []$
 shows $\exists \text{max} \in \text{set } ls. \forall z \in \text{set } ls. z \leq \text{max}$
 using *ls*
proof (*induct ls*)
 case *Nil* thus *?case* by *simp*
 next
 case (*Cons l ls*)

 show *?case*
proof (*cases ls = []*)
 case *True*
 thus *?thesis* by *simp*
 next
 case *False*
 then obtain *max* where *mv*: $\text{max} \in \text{set } ls$ and *mm*: $\forall z \in \text{set } ls. z \leq \text{max}$

```

using Cons.hyps
  by auto
show ?thesis
proof (cases max ≤ l)
  case True
  have  $l \in \text{set } (l \# ls)$  by simp
  thus ?thesis
proof
  from mm show  $\forall z \in \text{set } (l \# ls). z \leq l$  using True by auto
qed
next
  case False
  from mv have  $max \in \text{set } (l \# ls)$  by simp
  thus ?thesis
proof
  from mm show  $\forall z \in \text{set } (l \# ls). z \leq max$  using False by auto
qed
qed
qed
qed

```

lemma *True-notin-set-replicate-conv*:
 $True \notin \text{set } ls = (ls = \text{replicate } (\text{length } ls) \text{ False})$
by (*induct ls*) *simp+*

lemma *Collect-singleton-eqI*:
 $(\bigwedge x. P x = (x = v)) \implies \{x. P x\} = \{v\}$
by *auto*

lemma *exEI*:
 $\llbracket \exists y. P y; \bigwedge x. P x \implies Q x \rrbracket \implies \exists z. Q z$
by (*rule ex-forward*)

lemma *allEI*:
assumes $\forall x. P x$
assumes $\bigwedge x. P x \implies Q x$
shows $\forall x. Q x$
using *assms* **by** (*rule all-forward*)

General lemmas that should be in the library

lemma *dom-ran*:
 $x \in \text{dom } f \implies \text{the } (f x) \in \text{ran } f$
by (*simp add: dom-def ran-def, erule exE, simp, rule exI, simp*)

lemma *orthD1*:
 $\llbracket S \cap S' = \{\}; x \in S \rrbracket \implies x \notin S'$ **by** *auto*

lemma *orthD2*:
 $\llbracket S \cap S' = \{\}; x \in S' \rrbracket \implies x \notin S$ **by** *auto*

lemma *distinct-element*:
 $\llbracket b \cap d = \{\}; a \in b; c \in d \rrbracket \Longrightarrow a \neq c$
by *auto*

lemma *ball-reorder*:
 $(\forall x \in A. \forall y \in B. P\ x\ y) = (\forall y \in B. \forall x \in A. P\ x\ y)$
by *auto*

lemma *hd-map*: $ls \neq [] \Longrightarrow \text{hd}\ (\text{map}\ f\ ls) = f\ (\text{hd}\ ls)$
by (*cases* *ls*) *auto*

lemma *tl-map*: $\text{tl}\ (\text{map}\ f\ ls) = \text{map}\ f\ (\text{tl}\ ls)$
by (*cases* *ls*) *auto*

lemma *not-NilE*:
 $\llbracket xs \neq []; \bigwedge x\ xs'. xs = x \# xs' \Longrightarrow R \rrbracket \Longrightarrow R$
by (*cases* *xs*) *auto*

lemma *length-SucE*:
 $\llbracket \text{length}\ xs = \text{Suc}\ n; \bigwedge x\ xs'. xs = x \# xs' \Longrightarrow R \rrbracket \Longrightarrow R$
by (*cases* *xs*) *auto*

lemma *map-upt-unfold*:
assumes *ab*: $a < b$
shows $\text{map}\ f\ [a ..< b] = f\ a \# \text{map}\ f\ [\text{Suc}\ a ..< b]$
using *assms* *upt-conv-Cons* **by** *auto*

lemma *tl-nat-list-simp*:
 $\text{tl}\ [a..<b] = [a + 1 ..<b]$
by (*induct* *b*, *auto*)

lemma *image-Collect2*:
 $\text{case-prod}\ f\ ' \{x. P\ (\text{fst}\ x)\ (\text{snd}\ x)\} = \{f\ x\ y\ | x\ y. P\ x\ y\}$
by (*subst* *image-Collect*) *simp*

lemma *image-id'*:
 $\text{id}\ ' Y = Y$
by *clarsimp*

lemma *image-invert*:
assumes *r*: $f \circ g = \text{id}$
and $g: B = g\ ' A$
shows $A = f\ ' B$
by (*simp* *add*: *g* *image-comp* *r*)

lemma *Collect-image-fun-cong*:
assumes *rl*: $\bigwedge a. P\ a \Longrightarrow f\ a = g\ a$
shows $\{f\ x\ | x. P\ x\} = \{g\ x\ | x. P\ x\}$

```

using rl by force

lemma inj-on-take:
  shows inj-on (take n) {x. drop n x = k}
proof (rule inj-onI)
  fix x y
  assume xv: x ∈ {x. drop n x = k}
    and yv: y ∈ {x. drop n x = k}
    and tk: take n x = take n y

  from xv have take n x @ k = x
    using append-take-drop-id mem-Collect-eq by auto
  moreover from yv tk
  have take n x @ k = y
    using append-take-drop-id mem-Collect-eq by auto
  ultimately show x = y by simp
qed

lemma foldr-upd-dom:
  dom (foldr (λp ps. ps (p ↦ f p)) as g) = dom g ∪ set as
proof (induct as)
  case Nil thus ?case by simp
next
  case (Cons a as)
  show ?case
  proof (cases a ∈ set as ∨ a ∈ dom g)
    case True
    hence ain: a ∈ dom g ∪ set as by auto
    hence dom g ∪ set (a # as) = dom g ∪ set as by auto
    thus ?thesis using Cons by fastforce
  next
    case False
    hence a ∉ (dom g ∪ set as) by simp
    hence dom g ∪ set (a # as) = insert a (dom g ∪ set as) by simp
    thus ?thesis using Cons by fastforce
  qed
qed

lemma foldr-upd-app:
  assumes xin: x ∈ set as
  shows (foldr (λp ps. ps (p ↦ f p)) as g) x = Some (f x)
  (is (?f as g) x = Some (f x))
  using xin
proof (induct as arbitrary: x)
  case Nil thus ?case by simp
next
  case (Cons a as)
  from Cons.premis show ?case by (subst foldr.simps) (auto intro: Cons.hyps)
qed

```



```

lemma foldr-upd-app-other:
  assumes xin:  $x \notin \text{set } as$ 
  shows  $(\text{foldr } (\lambda p \ ps. \ ps \ (p \mapsto f \ p)) \ as \ g) \ x = g \ x$ 
  (is  $(?f \ as \ g) \ x = g \ x$ )
  using xin
proof (induct as arbitrary: x)
  case Nil thus ?case by simp
next
  case (Cons a as)
  from Cons.prems show ?case
    by (subst foldr.simps) (auto intro: Cons.hyps)
qed

lemma foldr-upd-app-if:
   $\text{foldr } (\lambda p \ ps. \ ps \ (p \mapsto f \ p)) \ as \ g = (\lambda x. \ \text{if } x \in \text{set } as \ \text{then } Some \ (f \ x) \ \text{else } g \ x)$ 
  by (auto simp: foldr-upd-app foldr-upd-app-other)

lemma foldl-fun-upd-value:
   $\bigwedge Y. \ \text{foldl } (\lambda f \ p. \ f(p := X \ p)) \ Y \ e \ p = (\text{if } p \in \text{set } e \ \text{then } X \ p \ \text{else } Y \ p)$ 
  by (induct e) simp-all

lemma foldr-fun-upd-value:
   $\bigwedge Y. \ \text{foldr } (\lambda p \ f. \ f(p := X \ p)) \ e \ Y \ p = (\text{if } p \in \text{set } e \ \text{then } X \ p \ \text{else } Y \ p)$ 
  by (induct e) simp-all

lemma foldl-fun-upd-eq-foldr:
   $!!m. \ \text{foldl } (\lambda f \ p. \ f(p := g \ p)) \ m \ xs = \text{foldr } (\lambda p \ f. \ f(p := g \ p)) \ xs \ m$ 
  by (rule ext) (simp add: foldl-fun-upd-value foldr-fun-upd-value)

lemma Cons-eq-neq:
   $\llbracket y = x; x \# xs \neq y \# ys \rrbracket \implies xs \neq ys$ 
  by simp

lemma map-upt-append:
  assumes lt:  $x \leq y$ 
  and lt2:  $a \leq x$ 
  shows  $\text{map } f \ [a \ ..< y] = \text{map } f \ [a \ ..< x] @ \text{map } f \ [x \ ..< y]$ 
proof (subst map-append [symmetric], rule arg-cong [where f = map f])
  from lt obtain k where ky:  $x + k = y$ 
  by (auto simp: le-iff-add)

  thus  $[a \ ..< y] = [a \ ..< x] @ [x \ ..< y]$ 
  using lt2
  by (auto intro: upt-add-eq-append)
qed

lemma Min-image-distrib:
  assumes minf:  $\bigwedge x \ y. \ \llbracket x \in A; y \in A \rrbracket \implies \min \ (f \ x) \ (f \ y) = f \ (\min \ x \ y)$ 

```

```

and      fa: finite A
and      ane: A ≠ {}
shows Min (f ` A) = f (Min A)
proof -
have rl:  $\bigwedge F. \llbracket F \subseteq A; F \neq \{\} \rrbracket \implies \text{Min } (f ` F) = f (\text{Min } F)$ 
proof -
fix F
assume fa:  $F \subseteq A$  and fne:  $F \neq \{\}$ 
have finite F by (rule finite-subset) fact+

thus ?thesis F
  unfolding min-def using fa fne fa
proof (induct rule: finite-subset-induct)
case empty
thus ?case by simp
next
case (insert x F)
thus ?case
  by (cases F = {}) (auto dest: Min-in intro: minf)
qed
qed

show ?thesis by (rule rl [OF order-refl]) fact+
qed

lemma min-of-mono':
assumes (f a ≤ f c) = (a ≤ c)
shows min (f a) (f c) = f (min a c)
unfolding min-def
by (subst if-distrib [where f = f, symmetric], rule arg-cong [where f = f], rule
if-cong [OF - refl refl]) fact+

lemma nat-diff-less:
fixes x :: nat
shows  $\llbracket x < y + z; z \leq x \rrbracket \implies x - z < y$ 
using less-diff-conv2 by blast

lemma take-map-Not:
(take n (map Not xs) = take n xs) = (n = 0 ∨ xs = [])
by (cases n; simp) (cases xs; simp)

lemma union-trans:
assumes SR:  $\bigwedge x y z. \llbracket (x,y) \in S; (y,z) \in R \rrbracket \implies (x,z) \in S^*$ 
shows  $(R \cup S)^* = R^* \cup R^* \circ S^*$ 
apply (rule set-eqI)
apply clarsimp
apply (rule iffI)
apply (erule rtrancl-induct; simp)

```

```

apply (erule disjE)
apply (erule disjE)
  apply (drule (1) rtrancl-into-rtrancl)
  apply blast
apply clarsimp
apply (drule rtranclD [where  $R=S$ ])
apply (erule disjE)
  apply simp
apply (erule conjE)
apply (drule tranclD2)
apply (elim exE conjE)
apply (drule (1) SR)
apply (drule (1) rtrancl-trans)
apply blast
apply (rule disjI2)
apply (erule disjE)
  apply (blast intro: in-rtrancl-UnI)
apply clarsimp
apply (drule (1) rtrancl-into-rtrancl)
apply (erule (1) relcompI)
apply (erule disjE)
  apply (blast intro: in-rtrancl-UnI)
apply clarsimp
apply (blast intro: in-rtrancl-UnI rtrancl-trans)
done

```

lemma *trancl-trancl*:

$$(R^+)^+ = R^+$$

by *auto*

Some rules for showing that the reflexive transitive closure of a relation/predicate doesn't add much if it was already transitively closed.

lemma *rtrancl-eq-reflc-trans*:

assumes *trans: trans X*

shows $rtrancl\ X = X \cup Id$

by (*simp only: rtrancl-trancl-reflcl trancl-id[OF trans]*)

lemma *rtrancl-id*:

assumes *refl: Id \subseteq X*

assumes *trans: trans X*

shows $rtrancl\ X = X$

using *refl rtrancl-eq-reflc-trans[OF trans]*

by *blast*

lemma *rtranclp-eq-reflcp-transp*:

assumes *trans: transp X*

shows $rtranclp\ X = (\lambda x\ y. X\ x\ y \vee x = y)$

by (*simp add: Enum.rtranclp-rtrancl-eq fun-eq-iff
rtrancl-eq-reflc-trans trans[unfolded transp-trans]*)

```

lemma rtrancpl-id:
  shows  $\text{reflp } X \implies \text{transp } X \implies \text{rtrancpl } X = X$ 
  apply (simp add: rtrancpl-eq-reflcp-transp)
  apply (auto simp: fun-eq-iff elim: reflpD)
  done

lemmas rtrancpl-id2 = rtrancpl-id[unfolded reflp-def transp-relcompp le-fun-def]

lemma if-1-0-0:
   $((\text{if } P \text{ then } 1 \text{ else } 0) = (0 :: ('a :: \text{zero-neq-one}))) = (\neg P)$ 
  by (simp split: if-split)

lemma neq-Nil-lengthI:
   $\text{Suc } 0 \leq \text{length } xs \implies xs \neq []$ 
  by (cases xs, auto)

lemmas ex-with-length = Ex-list-of-length

lemma in-singleton:
   $S = \{x\} \implies x \in S$ 
  by simp

lemma singleton-set:
   $x \in \text{set } [a] \implies x = a$ 
  by auto

lemma take-drop-eqI:
  assumes t:  $\text{take } n \text{ } xs = \text{take } n \text{ } ys$ 
  assumes d:  $\text{drop } n \text{ } xs = \text{drop } n \text{ } ys$ 
  shows  $xs = ys$ 
proof –
  have  $xs = \text{take } n \text{ } xs @ \text{drop } n \text{ } xs$  by simp
  with t d
  have  $xs = \text{take } n \text{ } ys @ \text{drop } n \text{ } ys$  by simp
  moreover
  have  $ys = \text{take } n \text{ } ys @ \text{drop } n \text{ } ys$  by simp
  ultimately
  show ?thesis by simp
qed

lemma append-len2:
   $zs = xs @ ys \implies \text{length } xs = \text{length } zs - \text{length } ys$ 
  by auto

lemma if-flip:
   $(\text{if } \neg P \text{ then } T \text{ else } F) = (\text{if } P \text{ then } F \text{ else } T)$ 
  by simp

```

lemma *not-in-domIff*: $f\ x = \text{None} = (x \notin \text{dom } f)$
by *blast*

lemma *not-in-domD*:
 $x \notin \text{dom } f \implies f\ x = \text{None}$
by (*simp add: not-in-domIff*)

definition
 $\text{graph-of } f \equiv \{(x,y). f\ x = \text{Some } y\}$

lemma *graph-of-None-update*:
 $\text{graph-of } (f\ (p := \text{None})) = \text{graph-of } f - \{p\} \times \text{UNIV}$
by (*auto simp: graph-of-def split: if-split-asm*)

lemma *graph-of-Some-update*:
 $\text{graph-of } (f\ (p \mapsto v)) = (\text{graph-of } f - \{p\} \times \text{UNIV}) \cup \{(p,v)\}$
by (*auto simp: graph-of-def split: if-split-asm*)

lemma *graph-of-restrict-map*:
 $\text{graph-of } (m \upharpoonright S) \subseteq \text{graph-of } m$
by (*simp add: graph-of-def restrict-map-def subset-iff*)

lemma *graph-ofD*:
 $(x,y) \in \text{graph-of } f \implies f\ x = \text{Some } y$
by (*simp add: graph-of-def*)

lemma *graph-ofI*:
 $m\ x = \text{Some } y \implies (x, y) \in \text{graph-of } m$
by (*simp add: graph-of-def*)

lemma *graph-of-empty* :
 $\text{graph-of } \text{Map.empty} = \{\}$
by (*simp add: graph-of-def*)

lemma *graph-of-in-ranD*: $\forall y \in \text{ran } f. P\ y \implies (x,y) \in \text{graph-of } f \implies P\ x$
by (*auto simp: graph-of-def ran-def*)

lemma *graph-of-SomeD*:
 $\llbracket \text{graph-of } f \subseteq \text{graph-of } g; f\ x = \text{Some } y \rrbracket \implies g\ x = \text{Some } y$
unfolding *graph-of-def*
by *auto*

lemma *in-set-zip-refl* :
 $(x,y) \in \text{set } (\text{zip } xs\ xs) = (y = x \wedge x \in \text{set } xs)$
by (*induct xs*) *auto*

lemma *map-conv-upd*:
 $m\ v = \text{None} \implies m\ o\ (f\ (x := v)) = (m\ o\ f)\ (x := \text{None})$
by (*rule ext*) (*clarsimp simp: o-def*)

lemma *sum-all-ex* [*simp*]:
 $(\forall a. x \neq \text{Inl } a) = (\exists a. x = \text{Inr } a)$
 $(\forall a. x \neq \text{Inr } a) = (\exists a. x = \text{Inl } a)$
by (*metis Inr-not-Inl sum.exhaust*)+

lemma *split-distrib*: $\text{case-prod } (\lambda a b. T (f a b)) = (\lambda x. T (\text{case-prod } (\lambda a b. f a b) x))$
by (*clarsimp simp: split-def*)

lemma *case-sum-triv* [*simp*]:
 $(\text{case } x \text{ of } \text{Inl } x \Rightarrow \text{Inl } x \mid \text{Inr } x \Rightarrow \text{Inr } x) = x$
by (*clarsimp split: sum.splits*)

lemma *set-eq-UNIV*: $(\{a. P a\} = \text{UNIV}) = (\forall a. P a)$
by *force*

lemma *allE2*:
 $\llbracket \forall x y. P x y; P x y \implies R \rrbracket \implies R$
by *blast*

lemma *allE3*: $\llbracket \forall x y z. P x y z; P x y z \implies R \rrbracket \implies R$
by *auto*

lemma *my-BallE*: $\llbracket \forall x \in A. P x; y \in A; P y \implies Q \rrbracket \implies Q$
by (*simp add: Ball-def*)

lemma *unit-Inl-or-Inr* [*simp*]:
 $\bigwedge a. (a \neq \text{Inl } ()) = (a = \text{Inr } ())$
 $\bigwedge a. (a \neq \text{Inr } ()) = (a = \text{Inl } ())$
by (*case-tac a; clarsimp*)+

lemma *disjE-L*: $\llbracket a \vee b; a \implies R; \llbracket \neg a; b \rrbracket \implies R \rrbracket \implies R$
by *blast*

lemma *disjE-R*: $\llbracket a \vee b; \llbracket \neg b; a \rrbracket \implies R; \llbracket b \rrbracket \implies R \rrbracket \implies R$
by *blast*

lemma *int-max-thms*:
 $(a :: \text{int}) \leq \max a b$
 $(b :: \text{int}) \leq \max a b$
by (*auto simp: max-def*)

lemma *sgn-negation* [*simp*]:
 $\text{sgn } (\neg(x :: \text{int})) = - \text{sgn } x$
by (*clarsimp simp: sgn-if*)

lemma *sgn-sgn-nonneg* [*simp*]:
 $\text{sgn } (a :: \text{int}) * \text{sgn } a \neq -1$

by (*clarsimp simp: sgn-if*)

lemma *inj-inj-on*:

inj f \implies *inj-on f A*

by (*metis injD inj-onI*)

lemma *ex-eqI*:

$\llbracket \bigwedge x. f\ x = g\ x \rrbracket \implies (\exists x. f\ x) = (\exists x. g\ x)$

by *simp*

lemma *pre-post-ex*:

$\llbracket \exists x. P\ x; \bigwedge x. P\ x \implies Q\ x \rrbracket \implies \exists x. Q\ x$

by *auto*

lemma *ex-conj-increase*:

$((\exists x. P\ x) \wedge Q) = (\exists x. P\ x \wedge Q)$

$(R \wedge (\exists x. S\ x)) = (\exists x. R \wedge S\ x)$

by *simp+*

lemma *all-conj-increase*:

$((\forall x. P\ x) \wedge Q) = (\forall x. P\ x \wedge Q)$

$(R \wedge (\forall x. S\ x)) = (\forall x. R \wedge S\ x)$

by *simp+*

lemma *Ball-conj-increase*:

$xs \neq \{\} \implies ((\forall x \in xs. P\ x) \wedge Q) = (\forall x \in xs. P\ x \wedge Q)$

$xs \neq \{\} \implies (R \wedge (\forall x \in xs. S\ x)) = (\forall x \in xs. R \wedge S\ x)$

by *auto*

lemma *disjoint-subset*:

assumes $A' \subseteq A$ **and** $A \cap B = \{\}$

shows $A' \cap B = \{\}$

using *assms* **by** *auto*

lemma *disjoint-subset2*:

assumes $B' \subseteq B$ **and** $A \cap B = \{\}$

shows $A \cap B' = \{\}$

using *assms* **by** *auto*

lemma *UN-nth-mem*:

$i < \text{length}\ xs \implies f\ (xs\ !\ i) \subseteq (\bigcup x \in \text{set}\ xs. f\ x)$

by (*metis UN-upper nth-mem*)

lemma *Union-equal*:

$f\ ` A = f\ ` B \implies (\bigcup x \in A. f\ x) = (\bigcup x \in B. f\ x)$

by *blast*

lemma *UN-Diff-disjoint*:

$i < \text{length } xs \implies (A - (\bigcup_{x \in \text{set } xs} f x)) \cap f (xs ! i) = \{\}$
by (*metis Diff-disjoint Int-commute UN-nth-mem disjoint-subset*)

lemma *image-list-update*:

$f a = f (xs ! i)$
 $\implies f ' \text{set } (xs [i := a]) = f ' \text{set } xs$
by (*metis list-update-id map-update set-map*)

lemma *Union-list-update-id*:

$f a = f (xs ! i) \implies (\bigcup_{x \in \text{set } (xs [i := a])} f x) = (\bigcup_{x \in \text{set } xs} f x)$
by (*rule Union-equal*) (*erule image-list-update*)

lemma *Union-list-update-id'*:

$\llbracket i < \text{length } xs; \bigwedge x. g (f x) = g x \rrbracket$
 $\implies (\bigcup_{x \in \text{set } (xs [i := f (xs ! i)])} g x) = (\bigcup_{x \in \text{set } xs} g x)$
by (*metis Union-list-update-id*)

lemma *Union-subset*:

$\llbracket \bigwedge x. x \in A \implies (f x) \subseteq (g x) \rrbracket \implies (\bigcup_{x \in A} f x) \subseteq (\bigcup_{x \in A} g x)$
by (*metis UN-mono order-refl*)

lemma *UN-sub-empty*:

$\llbracket \text{list-all } P \text{ } xs; \bigwedge x. P x \implies f x = g x \rrbracket \implies (\bigcup_{x \in \text{set } xs} f x) - (\bigcup_{x \in \text{set } xs} g x) = \{\}$
by (*simp add: Ball-set-list-all[symmetric] Union-subset*)

lemma *bij-betw-fun-updI*:

$\llbracket x \notin A; y \notin B; \text{bij-betw } f \text{ } A \text{ } B \rrbracket \implies \text{bij-betw } (f(x := y)) (insert x A) (insert y B)$
by (*clarsimp simp: bij-betw-def fun-upd-image inj-on-fun-updI split: if-split-asm; blast*)

definition

$\text{bij-betw-map } f \text{ } A \text{ } B \equiv \text{bij-betw } f \text{ } A \text{ } (\text{Some } ' B)$

lemma *bij-betw-map-fun-updI*:

$\llbracket x \notin A; y \notin B; \text{bij-betw-map } f \text{ } A \text{ } B \rrbracket$
 $\implies \text{bij-betw-map } (f(x \mapsto y)) (insert x A) (insert y B)$
unfolding *bij-betw-map-def* **by** *clarsimp* (*erule bij-betw-fun-updI; clarsimp*)

lemma *bij-betw-map-imp-inj-on*:

$\text{bij-betw-map } f \text{ } A \text{ } B \implies \text{inj-on } f \text{ } A$
by (*simp add: bij-betw-map-def bij-betw-imp-inj-on*)

lemma *bij-betw-empty-dom-exists*:

$r = \{\} \implies \exists t. \text{bij-betw } t \text{ } \{\} \text{ } r$


```

by (clarsimp simp: bij-betw-def)

lemma bij-betw-map-empty-dom-exists:
   $r = \{\} \implies \exists t. \text{bij-betw-map } t \ \{\} \ r$ 
by (clarsimp simp: bij-betw-map-def bij-betw-empty-dom-exists)

lemma funpow-add [simp]:
  fixes  $f :: 'a \Rightarrow 'a$ 
  shows  $(f \ ^\wedge \ a) ((f \ ^\wedge \ b) \ s) = (f \ ^\wedge \ (a + b)) \ s$ 
by (metis comp-apply funpow-add)

lemma funpow-unfold:
  fixes  $f :: 'a \Rightarrow 'a$ 
  assumes  $n > 0$ 
  shows  $f \ ^\wedge \ n = (f \ ^\wedge \ (n - 1)) \circ f$ 
by (metis Suc-diff-1 assms funpow-Suc-right)

lemma relpow-unfold:  $n > 0 \implies S \ ^\wedge \ n = (S \ ^\wedge \ (n - 1)) \ O \ S$ 
by (cases n, auto)

definition
  equiv-of ::  $('s \Rightarrow 't) \Rightarrow ('s \times 's) \text{ set}$ 
where
  equiv-of proj  $\equiv \{(a, b). \text{proj } a = \text{proj } b\}$ 

lemma equiv-of-is-equiv-relation [simp]:
  equiv UNIV (equiv-of proj)
by (auto simp: equiv-of-def intro!: equivI refl-onI symI transI)

lemma in-equiv-of [simp]:
   $((a, b) \in \text{equiv-of } f) \longleftrightarrow (f \ a = f \ b)$ 
by (clarsimp simp: equiv-of-def)

lemma equiv-relation-to-projection:
  fixes  $R :: ('a \times 'a) \text{ set}$ 
  assumes equiv: equiv UNIV R
  shows  $\exists f :: 'a \Rightarrow 'a \text{ set}. \forall x \ y. f \ x = f \ y \longleftrightarrow (x, y) \in R$ 
  apply (rule exI [of -  $\lambda x. \{y. (x, y) \in R\}$ ])
  apply clarsimp
  apply (case-tac  $(x, y) \in R$ )
  apply clarsimp
  apply (rule set-eqI)

```

```

apply clarsimp
apply (metis equivE sym-def trans-def equiv)
apply (clarsimp)
apply (metis UNIV-I equiv equivE mem-Collect-eq refl-on-def)
done

lemma range-constant [simp]:
  range ( $\lambda\cdot. k$ ) =  $\{k\}$ 
by (clarsimp simp: image-def)

lemma dom-unpack:
  dom (map-of (map ( $\lambda x. (f\ x, g\ x)$ ) xs)) = set (map ( $\lambda x. f\ x$ ) xs)
by (simp add: dom-map-of-conv-image-fst image-image)

lemma fold-to-disj:
  fold (++) ms a x = Some y  $\implies (\exists b \in \text{set } ms. b\ x = \text{Some } y) \vee a\ x = \text{Some } y$ 
by (induct ms arbitrary:a x y; clarsimp) blast

lemma fold-ignore1:
  a x = Some y  $\implies \text{fold } (++)\ ms\ a\ x = \text{Some } y$ 
by (induct ms arbitrary:a x y; clarsimp)

lemma fold-ignore2:
  fold (++) ms a x = None  $\implies a\ x = \text{None}$ 
by (metis fold-ignore1 option.collapse)

lemma fold-ignore3:
  fold (++) ms a x = None  $\implies (\forall b \in \text{set } ms. b\ x = \text{None})$ 
by (induct ms arbitrary:a x; clarsimp) (meson fold-ignore2 map-add-None)

lemma fold-ignore4:
  b  $\in \text{set } ms \implies b\ x = \text{Some } y \implies \exists y. \text{fold } (++)\ ms\ a\ x = \text{Some } y$ 
using fold-ignore3 by fastforce

lemma dom-unpack2:
  dom (fold (++) ms Map.empty) =  $\bigcup (\text{set } (\text{map } \text{dom } ms))$ 
apply (induct ms; clarsimp simp:dom-def)
apply (rule equalityI; clarsimp)
apply (drule fold-to-disj)
apply (erule disjE)
apply clarsimp
apply (rename-tac b)
apply (erule-tac x=b in ballE; clarsimp)
apply clarsimp
apply (rule conjI)
apply clarsimp
apply (rule-tac x=y in exI)
apply (erule fold-ignore1)
apply clarsimp

```

```

apply (rename-tac y)
apply (erule-tac y=y in fold-ignore4; clarsimp)
done

lemma fold-ignore5: fold (++) ms a x = Some y  $\implies$  a x = Some y  $\vee$  ( $\exists b \in \text{set}$ 
ms. b x = Some y)
  by (induct ms arbitrary: a x y; clarsimp) blast

lemma dom-inter-nothing: dom f  $\cap$  dom g = {}  $\implies$   $\forall x. f\ x = \text{None} \vee g\ x =$ 
None
  by auto

lemma fold-ignore6:
  f x = None  $\implies$  fold (++) ms f x = fold (++) ms Map.empty x
  apply (induct ms arbitrary: f x; clarsimp simp: map-add-def)
  by (metis (no-types, lifting) fold-ignore1 option.collapse option.simps(4))

lemma fold-ignore7:
  m x = m' x  $\implies$  fold (++) ms m x = fold (++) ms m' x
  apply (case-tac m x)
  apply (frule-tac ms=ms in fold-ignore6)
  apply (cut-tac f=m' and ms=ms and x=x in fold-ignore6)
  apply clarsimp+
  apply (rename-tac a)
  apply (cut-tac ms=ms and a=m and x=x and y=a in fold-ignore1, clarsimp)
  apply (cut-tac ms=ms and a=m' and x=x and y=a in fold-ignore1; clarsimp)
  done

lemma fold-ignore8:
  fold (++) ms [x  $\mapsto$  y] = (fold (++) ms Map.empty)(x  $\mapsto$  y)
  apply (rule ext)
  apply (rename-tac xa)
  apply (case-tac xa = x)
  apply clarsimp
  apply (rule fold-ignore1)
  apply clarsimp
  apply (subst fold-ignore6; clarsimp)
  done

lemma fold-ignore9:
   $\llbracket \text{fold (++) ms } [x \mapsto y] \ x' = \text{Some } z; x = x' \rrbracket \implies y = z$ 
  by (subst (asm) fold-ignore8) clarsimp

lemma fold-to-map-of:
  fold (++) (map ( $\lambda x. [f\ x \mapsto g\ x]$ ) xs) Map.empty = map-of (map ( $\lambda x. (f\ x, g$ 
x)) xs)
  apply (rule ext)
  apply (rename-tac x)
  apply (case-tac fold (++) (map ( $\lambda x. [f\ x \mapsto g\ x]$ ) xs) Map.empty x)

```

```

apply clarsimp
apply (drule fold-ignore3)
apply (clarsimp split:if-split-asm)
apply (rule sym)
apply (subst map-of-eq-None-iff)
apply clarsimp
apply (rename-tac xa)
apply (erule-tac x=xa in ballE; clarsimp)
apply clarsimp
apply (frule fold-ignore5; clarsimp split:if-split-asm)
apply (subst map-add-map-of-foldr[where m=Map.empty, simplified])
apply (induct xs arbitrary:f g; clarsimp split:if-split)
apply (rule conjI; clarsimp)
apply (drule fold-ignore9; clarsimp)
apply (cut-tac ms=map (λx. [f x ↦ g x]) xs and f=[f a ↦ g a] and x=f b in
fold-ignore6, clarsimp)
apply auto
done

```

```

lemma if-n-0-0:
  ((if P then n else 0) ≠ 0) = (P ∧ n ≠ 0)
by (simp split: if-split)

```

```

lemma insert-dom:
  assumes fx: f x = Some y
  shows insert x (dom f) = dom f
  unfolding dom-def using fx by auto

```

```

lemma map-comp-subset-dom:
  dom (prj ∘m f) ⊆ dom f
  unfolding dom-def
  by (auto simp: map-comp-Some-iff)

```

```

lemmas map-comp-subset-domD = subsetD [OF map-comp-subset-dom]

```

```

lemma dom-map-comp:
  x ∈ dom (prj ∘m f) = (∃ y z. f x = Some y ∧ prj y = Some z)
  by (fastforce simp: dom-def map-comp-Some-iff)

```

```

lemma map-option-Some-eq2:
  (Some y = map-option f x) = (∃ z. x = Some z ∧ f z = y)
  by (metis map-option-eq-Some)

```

```

lemma map-option-eq-dom-eq:
  assumes ome: map-option f ∘ g = map-option f ∘ g'
  shows dom g = dom g'
proof (rule set-eqI)
  fix x
  {

```

```

    assume  $x \in \text{dom } g$ 
    hence  $\text{Some } (f \text{ (the } (g \ x))) = (\text{map-option } f \circ g) \ x$ 
      by (auto simp: map-option-case split: option.splits)
    also have  $\dots = (\text{map-option } f \circ g') \ x$  by (simp add: ome)
    finally have  $x \in \text{dom } g'$ 
      by (auto simp: map-option-case split: option.splits)
  } moreover
  {
    assume  $x \in \text{dom } g'$ 
    hence  $\text{Some } (f \text{ (the } (g' \ x))) = (\text{map-option } f \circ g') \ x$ 
      by (auto simp: map-option-case split: option.splits)
    also have  $\dots = (\text{map-option } f \circ g) \ x$  by (simp add: ome)
    finally have  $x \in \text{dom } g$ 
      by (auto simp: map-option-case split: option.splits)
  } ultimately show  $(x \in \text{dom } g) = (x \in \text{dom } g')$  by auto
qed

```

lemma *cart-singleton-image*:
 $S \times \{s\} = (\lambda v. (v, s)) \text{ ` } S$
 by *auto*

lemma *singleton-eq-o2s*:
 $(\{x\} = \text{set-option } v) = (v = \text{Some } x)$
 by (cases v , *auto*)

lemma *option-set-singleton-eq*:
 $(\text{set-option } \text{opt} = \{v\}) = (\text{opt} = \text{Some } v)$
 by (cases opt , *simp-all*)

lemmas *option-set-singleton-eqs*
 = *option-set-singleton-eq*
 trans[*OF eq-commute option-set-singleton-eq*]

lemma *map-option-comp2*:
 $\text{map-option } (f \circ g) = \text{map-option } f \circ \text{map-option } g$
 by (simp add: option.map-comp fun-eq-iff)

lemma *compD*:
 $\llbracket f \circ g = f \circ g'; g \ x = v \rrbracket \implies f \ (g' \ x) = f \ v$
 by (*metis comp-apply*)

lemma *map-option-comp-eqE*:
 assumes *om*: $\text{map-option } f \circ \text{mp} = \text{map-option } f \circ \text{mp}'$
 and $p1: \llbracket \text{mp } x = \text{None}; \text{mp}' \ x = \text{None} \rrbracket \implies P$
 and $p2: \bigwedge v \ v'. \llbracket \text{mp } x = \text{Some } v; \text{mp}' \ x = \text{Some } v'; f \ v = f \ v' \rrbracket \implies P$
 shows P
proof (cases $\text{mp } x$)
 case *None*

hence $x \notin \text{dom } mp$ **by** (*simp add: domIff*)
 hence $mp' x = \text{None}$ **by** (*simp add: map-option-eq-dom-eq [OF om] domIff*)
 with None **show** *?thesis* **by** (*rule p1*)
next
 case (*Some v*)
 hence $x \in \text{dom } mp$ **by** *clarsimp*
 then obtain v' where Some' : $mp' x = \text{Some } v'$ **by** (*clarsimp simp add: map-option-eq-dom-eq [OF om]*)
 with Some **show** *?thesis*
proof (*rule p2*)
 show $f v = f v'$ **using** Some' *compD [OF om, OF Some]* **by** *simp*
qed
qed

lemma *Some-the*:
 $x \in \text{dom } f \implies f x = \text{Some } (the (f x))$
by *clarsimp*

lemma *map-comp-update*:
 $f \circ_m (g(x \mapsto v)) = (f \circ_m g)(x := f v)$
by (*rule ext, rename-tac y*) (*case-tac g y; simp*)

lemma *restrict-map-eqI*:
 assumes $req: A \mid 'S = B \mid 'S$
 and $mem: x \in S$
 shows $A x = B x$
proof –
 from mem have $A x = (A \mid 'S) x$ **by** *simp*
 also have $\dots = (B \mid 'S) x$ **using** req **by** *simp*
 also have $\dots = B x$ **using** mem **by** *simp*
 finally **show** *?thesis* .
qed

lemma *map-comp-eqI*:
 assumes $dm: \text{dom } g = \text{dom } g'$
 and $fg: \bigwedge x. x \in \text{dom } g' \implies f (the (g' x)) = f (the (g x))$
 shows $f \circ_m g = f \circ_m g'$
apply (*rule ext*)
apply (*case-tac x \in dom g*)
apply (*frule subst [OF dm]*)
apply (*clarsimp split: option.splits*)
apply (*frule domI [where m = g']*)
apply (*drule fg*)
apply *simp*
apply (*frule subst [OF dm]*)
apply *clarsimp*
apply (*drule not-sym*)
apply (*clarsimp simp: map-comp-Some-iff*)
done

definition

$$\text{modify-map } m \ p \ f \equiv m \ (p := \text{map-option } f \ (m \ p))$$
lemma *modify-map-id:*

$$\text{modify-map } m \ p \ \text{id} = m$$

$$\text{by } (\text{auto simp add: modify-map-def map-option-case split: option.splits})$$
lemma *modify-map-addr-com:*

$$\text{assumes } com: x \neq y$$

$$\text{shows } \text{modify-map } (\text{modify-map } m \ x \ g) \ y \ f = \text{modify-map } (\text{modify-map } m \ y \ f)$$

$$x \ g$$

$$\text{by } (\text{rule ext}) (\text{simp add: modify-map-def map-option-case com split: option.splits})$$
lemma *modify-map-dom :*

$$\text{dom } (\text{modify-map } m \ p \ f) = \text{dom } m$$

$$\text{unfolding modify-map-def by } (\text{auto simp: dom-def})$$
lemma *modify-map-None:*

$$m \ x = \text{None} \implies \text{modify-map } m \ x \ f = m$$

$$\text{by } (\text{rule ext}) (\text{simp add: modify-map-def})$$
lemma *modify-map-ndom :*

$$x \notin \text{dom } m \implies \text{modify-map } m \ x \ f = m$$

$$\text{by } (\text{rule modify-map-None}) \text{ clarsimp}$$
lemma *modify-map-app:*

$$(\text{modify-map } m \ p \ f) \ q = (\text{if } p = q \text{ then } \text{map-option } f \ (m \ p) \text{ else } m \ q)$$

$$\text{unfolding modify-map-def by simp}$$
lemma *modify-map-apply:*

$$m \ p = \text{Some } x \implies \text{modify-map } m \ p \ f = m \ (p \mapsto f \ x)$$

$$\text{by } (\text{simp add: modify-map-def})$$
lemma *modify-map-com:*

$$\text{assumes } com: \bigwedge x. f \ (g \ x) = g \ (f \ x)$$

$$\text{shows } \text{modify-map } (\text{modify-map } m \ x \ g) \ y \ f = \text{modify-map } (\text{modify-map } m \ y \ f)$$

$$x \ g$$

$$\text{using assms by } (\text{auto simp: modify-map-def map-option-case split: option.splits})$$
lemma *modify-map-comp:*

$$\text{modify-map } m \ x \ (f \circ g) = \text{modify-map } (\text{modify-map } m \ x \ g) \ x \ f$$

$$\text{by } (\text{rule ext}) (\text{simp add: modify-map-def option.map-comp})$$
lemma *modify-map-exists-eq:*

$$(\exists \text{cte. } \text{modify-map } m \ p' \ f \ p = \text{Some cte}) = (\exists \text{cte. } m \ p = \text{Some cte})$$

$$\text{by } (\text{auto simp: modify-map-def split: if-splits})$$

lemma *modify-map-other*:
 $p \neq q \implies (\text{modify-map } m \ p \ f) \ q = (m \ q)$
by (*simp add: modify-map-app*)

lemma *modify-map-same*:
 $\text{modify-map } m \ p \ f \ p = \text{map-option } f \ (m \ p)$
by (*simp add: modify-map-app*)

lemma *next-update-is-modify*:
 $\llbracket m \ p = \text{Some } \text{cte}'; \text{cte} = f \ \text{cte}' \rrbracket \implies (m(p \mapsto \text{cte})) = \text{modify-map } m \ p \ f$
unfolding *modify-map-def* **by** *simp*

lemma *nat-power-minus-less*:
 $a < 2^x \wedge (x - n) \implies (a :: \text{nat}) < 2^{x-n}$
by (*erule order-less-le-trans*) *simp*

lemma *neg-rtranclI*:
 $\llbracket x \neq y; (x, y) \notin R^+ \rrbracket \implies (x, y) \notin R^*$
by (*meson rtranclD*)

lemma *neg-rtrancl-into-trancl*:
 $\neg (x, y) \in R^* \implies \neg (x, y) \in R^+$
by (*erule contrapos-nn, erule trancl-into-rtrancl*)

lemma *set-neqI*:
 $\llbracket x \in S; x \notin S' \rrbracket \implies S \neq S'$
by *clarsimp*

lemma *set-pair-UN*:
 $\{x. P \ x\} = \text{UNION } \{xa. \exists xb. P \ (xa, xb)\} \ (\lambda xa. \{xa\} \times \{xb. P \ (xa, xb)\})$
by *fastforce*

lemma *singleton-elemD*: $S = \{x\} \implies x \in S$
by *simp*

lemma *singleton-eqD*: $A = \{x\} \implies x \in A$
by *blast*

lemma *ball-ran-fun-updI*:
 $\llbracket \forall v \in \text{ran } m. P \ v; \forall v. y = \text{Some } v \longrightarrow P \ v \rrbracket \implies \forall v \in \text{ran } (m \ (x := y)). P \ v$
by (*auto simp add: ran-def*)

lemma *ball-ran-eq*:
 $(\forall y \in \text{ran } m. P \ y) = (\forall x \ y. m \ x = \text{Some } y \longrightarrow P \ y)$
by (*auto simp add: ran-def*)

lemma *cart-helper*:
 $(\{\} = \{x\} \times S) = (S = \{\})$
by *blast*

lemmas *converse-trancl-induct'* = *converse-trancl-induct* [*consumes 1*, *case-names base step*]

lemma *disjCI2*: $(\neg P \implies Q) \implies P \vee Q$ **by** *blast*

lemma *insert-UNIV* :
 $\text{insert } x \text{ UNIV} = \text{UNIV}$
by *blast*

lemma *not-singletonE*:
 $\llbracket \forall p. S \neq \{p\}; S \neq \{\}; \bigwedge p p'. \llbracket p \neq p'; p \in S; p' \in S \rrbracket \implies R \rrbracket \implies R$
by *blast*

lemma *not-singleton-oneE*:
 $\llbracket \forall p. S \neq \{p\}; p \in S; \bigwedge p'. \llbracket p \neq p'; p' \in S \rrbracket \implies R \rrbracket \implies R$
using *not-singletonE* **by** *fastforce*

lemma *ball-ran-modify-map-eq*:
 $\llbracket \forall v. m \ x = \text{Some } v \longrightarrow P \ (f \ v) = P \ v \rrbracket$
 $\implies (\forall v \in \text{ran } (\text{modify-map } m \ x \ f). P \ v) = (\forall v \in \text{ran } m. P \ v)$
by (*auto simp: modify-map-def ball-ran-eq*)

lemma *disj-imp*: $(P \vee Q) = (\neg P \longrightarrow Q)$ **by** *blast*

lemma *eq-singleton-reduce*:
 $\llbracket S = \{x\} \rrbracket \implies x \in S$
by *simp*

lemma *if-eq-elem-helperE*:
 $\llbracket x \in (\text{if } P \text{ then } S \text{ else } S'); \llbracket P; x \in S \rrbracket \implies a = b; \llbracket \neg P; x \in S' \rrbracket \implies a = c \rrbracket$
 $\implies a = (\text{if } P \text{ then } b \text{ else } c)$
by *fastforce*

lemma *if-option-Some*:
 $((\text{if } P \text{ then } \text{None} \text{ else } \text{Some } x) = \text{Some } y) = (\neg P \wedge x = y)$
by *simp*

lemma *insert-minus-eq*:
 $x \notin A \implies A - S = (A - (S - \{x\}))$
by *auto*

lemma *modify-map-K-D*:
 $\text{modify-map } m \ p \ (\lambda x. y) \ p' = \text{Some } v \implies (m \ (p \mapsto y)) \ p' = \text{Some } v$
by (*simp add: modify-map-def split: if-split-asm*)

lemma *tranclE2*:
assumes *trancl*: $(a, b) \in r^+$

```

and      base:  $(a, b) \in r \implies P$ 
and      step:  $\bigwedge c. \llbracket (a, c) \in r; (c, b) \in r^+ \rrbracket \implies P$ 
shows  $P$ 
using tranc1 base step
proof -
  note rl = converse-tranc1-induct [where  $P = \lambda x. x = a \longrightarrow P$ ]
  from tranc1 have  $a = a \longrightarrow P$ 
    by (rule rl, (iprover intro: base step)+)
  thus ?thesis by simp
qed

lemmas tranc1E2' = tranc1E2 [consumes 1, case-names base tranc1]

lemma weak-imp-cong:
   $\llbracket P = R; Q = S \rrbracket \implies (P \longrightarrow Q) = (R \longrightarrow S)$ 
  by simp

lemma Collect-Diff-restrict-simp:
   $T - \{x \in T. Q\ x\} = T - \{x. Q\ x\}$ 
  by (auto intro: Collect-cong)

lemma Collect-Int-pred-eq:
   $\{x \in S. P\ x\} \cap \{x \in T. P\ x\} = \{x \in (S \cap T). P\ x\}$ 
  by (simp add: Collect-conj-eq [symmetric] conj-comms)

lemma Collect-restrict-predR:
   $\{x. P\ x\} \cap T = \{\} \implies \{x. P\ x\} \cap \{x \in T. Q\ x\} = \{\}$ 
  by (fastforce simp: disjoint-iff-not-equal)

lemma Diff-Un2:
  assumes emptyad:  $A \cap D = \{\}$ 
  and      emptybc:  $B \cap C = \{\}$ 
  shows     $(A \cup B) - (C \cup D) = (A - C) \cup (B - D)$ 
proof -
  have  $(A \cup B) - (C \cup D) = (A \cup B - C) \cap (A \cup B - D)$ 
    by (rule Diff-Un)
  also have  $\dots = ((A - C) \cup B) \cap (A \cup (B - D))$  using emptyad emptybc
    by (simp add: Un-Diff Diff-triv)
  also have  $\dots = (A - C) \cup (B - D)$ 
  proof -
    have  $(A - C) \cap (A \cup (B - D)) = A - C$  using emptyad emptybc
      by (metis Diff-Int2 Diff-Int-distrib2 inf-sup-absorb)
    moreover
      have  $B \cap (A \cup (B - D)) = B - D$  using emptyad emptybc
      by (metis Int-Diff Un-Diff Un-Diff-Int Un-commute Un-empty-left inf-sup-absorb)
    ultimately show ?thesis
      by (simp add: Int-Un-distrib2)
  qed
  finally show ?thesis .

```

qed

lemma *ballEI*:

$\llbracket \forall x \in S. Q\ x; \bigwedge x. \llbracket x \in S; Q\ x \rrbracket \implies P\ x \rrbracket \implies \forall x \in S. P\ x$
by *auto*

lemma *dom-if-None*:

$\text{dom } (\lambda x. \text{if } P\ x \text{ then None else } f\ x) = \text{dom } f - \{x. P\ x\}$
by (*simp add: dom-def*) *fastforce*

lemma *restrict-map-Some-iff*:

$((m \mid S)\ x = \text{Some } y) = (m\ x = \text{Some } y \wedge x \in S)$
by (*cases x \in S, simp-all*)

lemma *context-case-bools*:

$\llbracket \bigwedge v. P\ v \implies R\ v; \llbracket \neg P\ v; \bigwedge v. P\ v \implies R\ v \rrbracket \implies R\ v \rrbracket \implies R\ v$
by (*cases P v, simp-all*)

lemma *inj-on-fun-upd-strongerI*:

$\llbracket \text{inj-on } f\ A; y \notin f\ ' (A - \{x\}) \rrbracket \implies \text{inj-on } (f(x := y))\ A$
by (*fastforce simp: inj-on-def*)

lemma *less-handly-casesE*:

$\llbracket m < n; m = 0 \implies R; \bigwedge m' n'. \llbracket n = \text{Suc } n'; m = \text{Suc } m'; m < n \rrbracket \implies R \rrbracket$
 $\implies R$
by (*case-tac n; simp*) (*case-tac m; simp*)

lemma *subset-drop-Diff-strg*:

$(A \subseteq C) \longrightarrow (A - B \subseteq C)$
by *blast*

lemma *inj-case-bool*:

$\text{inj } (\text{case-bool } a\ b) = (a \neq b)$
by (*auto dest: inj-onD[where x=True and y=False] intro: inj-onI split: bool.split-asm*)

lemma *foldl-fun-upd*:

$\text{foldl } (\lambda s\ r. s\ (r := g\ r))\ f\ rs = (\lambda x. \text{if } x \in \text{set } rs \text{ then } g\ x \text{ else } f\ x)$
by (*induct rs arbitrary: f*) (*auto simp: fun-eq-iff*)

lemma *all-rv-choice-fn-eq-pred*:

$\llbracket \bigwedge rv. P\ rv \implies \exists fn. f\ rv = g\ fn \rrbracket \implies \exists fn. \forall rv. P\ rv \longrightarrow f\ rv = g\ (fn\ rv)$
apply (*rule-tac x=\lambda rv. SOME h. f rv = g h in exI*)
apply (*clarsimp split: if-split*)
by (*meson someI-ex*)

lemma *ex-const-function*:

$\exists f. \forall s. f\ (f'\ s) = v$
by *force*

lemma *if-Const-helper*:

If P (*Con* x) (*Con* y) = *Con* (*If* P x y)

by (*simp split: if-split*)

lemmas *if-Some-helper* = *if-Const-helper*[**where** *Con*=*Some*]

lemma *expand-restrict-map-eq*:

$(m \mid 'S = m' \mid 'S) = (\forall x. x \in S \longrightarrow m\ x = m'\ x)$

by (*simp add: fun-eq-iff restrict-map-def split: if-split*)

lemma *disj-imp-rhs*:

$(P \Longrightarrow Q) \Longrightarrow (P \vee Q) = Q$

by *blast*

lemma *remove1-filter*:

distinct $xs \Longrightarrow \text{remove1 } x\ xs = \text{filter } (\lambda y. x \neq y)\ xs$

by (*induct xs*) (*auto intro!: filter-True [symmetric]*)

lemma *Int-Union-empty*:

$(\bigwedge x. x \in S \Longrightarrow A \cap P\ x = \{\}) \Longrightarrow A \cap (\bigcup x \in S. P\ x) = \{\}$

by *auto*

lemma *UN-Int-empty*:

$(\bigwedge x. x \in S \Longrightarrow P\ x \cap T = \{\}) \Longrightarrow (\bigcup x \in S. P\ x) \cap T = \{\}$

by *auto*

lemma *disjointI*:

$\llbracket \bigwedge x\ y. \llbracket x \in A; y \in B \rrbracket \Longrightarrow x \neq y \rrbracket \Longrightarrow A \cap B = \{\}$

by *auto*

lemma *UN-disjointI*:

assumes *rl*: $\bigwedge x\ y. \llbracket x \in A; y \in B \rrbracket \Longrightarrow P\ x \cap Q\ y = \{\}$

shows $(\bigcup x \in A. P\ x) \cap (\bigcup x \in B. Q\ x) = \{\}$

by (*auto dest: rl*)

lemma *UN-set-member*:

assumes *sub*: $A \subseteq (\bigcup x \in S. P\ x)$

and *nz*: $A \neq \{\}$

shows $\exists x \in S. P\ x \cap A \neq \{\}$

proof –

from *nz* **obtain** z **where** zA : $z \in A$ **by** *fastforce*

with *sub* **obtain** x **where** $x \in S$ **and** $z \in P\ x$ **by** *auto*

hence $P\ x \cap A \neq \{\}$ **using** zA **by** *auto*

thus *?thesis* **using** *sub nz* **by** *auto*

qed

lemma *append-Cons-cases* [*consumes 1, case-names pre mid post*]:

$\llbracket (x, y) \in \text{set } (as @ b \# bs) \rrbracket;$

$(x, y) \in \text{set } as \Longrightarrow R;$

$\llbracket (x, y) \notin \text{set } as; (x, y) \notin \text{set } bs; (x, y) = b \rrbracket \Longrightarrow R;$
 $(x, y) \in \text{set } bs \Longrightarrow R \rrbracket \Longrightarrow R$
by *auto*

lemma *cart-singletons*:
 $\{a\} \times \{b\} = \{(a, b)\}$
by *blast*

lemma *disjoint-subset-neg1*:
 $\llbracket B \cap C = \{\}; A \subseteq B; A \neq \{\} \rrbracket \Longrightarrow \neg A \subseteq C$
by *auto*

lemma *disjoint-subset-neg2*:
 $\llbracket B \cap C = \{\}; A \subseteq C; A \neq \{\} \rrbracket \Longrightarrow \neg A \subseteq B$
by *auto*

lemma *iffE2*:
 $\llbracket P = Q; \llbracket P; Q \rrbracket \Longrightarrow R; \llbracket \neg P; \neg Q \rrbracket \Longrightarrow R \rrbracket \Longrightarrow R$
by *blast*

lemma *list-case-If*:
 $(\text{case } xs \text{ of } [] \Rightarrow P \mid - \Rightarrow Q) = (\text{if } xs = [] \text{ then } P \text{ else } Q)$
by (*rule list.case-eq-if*)

lemma *remove1-Nil-in-set*:
 $\llbracket \text{remove1 } x \text{ } xs = []; xs \neq [] \rrbracket \Longrightarrow x \in \text{set } xs$
by (*induct xs*) (*auto split: if-split-asm*)

lemma *remove1-empty*:
 $(\text{remove1 } v \text{ } xs = []) = (xs = [v] \vee xs = [])$
by (*cases xs; simp*)

lemma *set-remove1*:
 $x \in \text{set } (\text{remove1 } y \text{ } xs) \Longrightarrow x \in \text{set } xs$
by (*induct xs*) (*auto split: if-split-asm*)

lemma *If-rearrange*:
 $(\text{if } P \text{ then if } Q \text{ then } x \text{ else } y \text{ else } z) = (\text{if } P \wedge Q \text{ then } x \text{ else if } P \text{ then } y \text{ else } z)$
by *simp*

lemma *disjI2-strg*:
 $Q \longrightarrow (P \vee Q)$
by *simp*

lemma *eq-imp-strg*:
 $P \text{ } t \longrightarrow (t = s \longrightarrow P \text{ } s)$
by *clarsimp*

lemma *if-both-strengthen*:

$P \wedge Q \longrightarrow (\text{if } G \text{ then } P \text{ else } Q)$
by *simp*

lemma *if-both-strengthen2*:
 $P \ s \wedge Q \ s \longrightarrow (\text{if } G \text{ then } P \text{ else } Q) \ s$
by *simp*

lemma *if-swap*:
 $(\text{if } P \text{ then } Q \text{ else } R) = (\text{if } \neg P \text{ then } R \text{ else } Q)$ **by** *simp*

lemma *imp-consequent*:
 $P \longrightarrow Q \longrightarrow P$ **by** *simp*

lemma *list-case-helper*:
 $xs \neq [] \implies \text{case-list } f \ g \ xs = g \ (\text{hd } xs) \ (\text{tl } xs)$
by (*cases xs, simp-all*)

lemma *list-cons-rewrite*:
 $(\forall x \ xs. L = x \# xs \longrightarrow P \ x \ xs) = (L \neq [] \longrightarrow P \ (\text{hd } L) \ (\text{tl } L))$
by (*auto simp: neq-Nil-conv*)

lemma *list-not-Nil-manip*:
 $\llbracket xs = y \# ys; \text{case } xs \text{ of } [] \Rightarrow \text{False} \mid (y \# ys) \Rightarrow P \ y \ ys \rrbracket \implies P \ y \ ys$
by *simp*

lemma *ran-ball-triv*:
 $\bigwedge P \ m \ S. \llbracket \forall x \in (\text{ran } S). P \ x ; m \in (\text{ran } S) \rrbracket \implies P \ m$
by *blast*

lemma *singleton-tuple-cartesian*:
 $(\{(a, b)\} = S \times T) = (\{a\} = S \wedge \{b\} = T)$
 $(S \times T = \{(a, b)\}) = (\{a\} = S \wedge \{b\} = T)$
by *blast+*

lemma *strengthen-ignore-if*:
 $A \ s \wedge B \ s \longrightarrow (\text{if } P \text{ then } A \text{ else } B) \ s$
by *clarsimp*

lemma *case-sum-True* :
 $(\text{case } r \text{ of } \text{Inl } a \Rightarrow \text{True} \mid \text{Inr } b \Rightarrow f \ b) = (\forall b. r = \text{Inr } b \longrightarrow f \ b)$
by (*cases r*) *auto*

lemma *sym-ex-elim*:
 $F \ x = y \implies \exists x. y = F \ x$
by *auto*

lemma *tl-drop-1* :
 $\text{tl } xs = \text{drop } 1 \ xs$
by (*simp add: drop-Suc*)

lemma *upt-lhs-sub-map*:
 $[x \text{ ..< } y] = \text{map } ((+) x) [0 \text{ ..< } y - x]$
by (*induct y*) (*auto simp: Suc-diff-le*)

lemma *upto-0-to-4*:
 $[0 \text{ ..< } 4] = 0 \# [1 \text{ ..< } 4]$
by (*subst upt-rec*) *simp*

lemma *disjEI*:
 $\llbracket P \vee Q; P \implies R; Q \implies S \rrbracket$
 $\implies R \vee S$
by *fastforce*

lemma *dom-fun-upd2*:
 $s \ x = \text{Some } z \implies \text{dom } (s \ (x \mapsto y)) = \text{dom } s$
by (*simp add: insert-absorb domI*)

lemma *foldl-True* :
 $\text{foldl } (\vee) \ \text{True } bs$
by (*induct bs*) *auto*

lemma *image-set-comp*:
 $f \text{ ‘ } \{g \ x \mid x. Q \ x\} = (f \circ g) \text{ ‘ } \{x. Q \ x\}$
by *fastforce*

lemma *mutual-exE*:
 $\llbracket \exists x. P \ x; \bigwedge x. P \ x \implies Q \ x \rrbracket \implies \exists x. Q \ x$
by *blast*

lemma *nat-diff-eq*:
fixes $x :: \text{nat}$
shows $\llbracket x - y = x - z; y < x \rrbracket \implies y = z$
by *arith*

lemma *comp-upd-simp*:
 $(f \circ (g \ (x := y))) = ((f \circ g) \ (x := f \ y))$
by (*rule fun-upd-comp*)

lemma *dom-option-map*:
 $\text{dom } (\text{map-option } f \ o \ m) = \text{dom } m$
by (*rule dom-map-option-comp*)

lemma *drop-imp*:
 $P \implies (A \longrightarrow P) \wedge (B \longrightarrow P)$ **by** *blast*

lemma *inj-on-fun-updI2*:
 $\llbracket \text{inj-on } f \ A; y \notin f \text{ ‘ } (A - \{x\}) \rrbracket \implies \text{inj-on } (f(x := y)) \ A$
by (*rule inj-on-fun-upd-strongerI*)

lemma *inj-on-fun-upd-elsewhere*:

$x \notin S \implies \text{inj-on } (f \ (x := y)) \ S = \text{inj-on } f \ S$
by (*simp add: inj-on-def*) *blast*

lemma *not-Some-eq-tuple*:

$(\forall y \ z. x \neq \text{Some } (y, z)) = (x = \text{None})$
by (*cases x, simp-all*)

lemma *ran-option-map*:

$\text{ran } (\text{map-option } f \ o \ m) = f \ ^\circ \ \text{ran } m$
by (*auto simp add: ran-def*)

lemma *All-less-Ball*:

$(\forall x < n. P \ x) = (\forall x \in \{..< n\}. P \ x)$
by *fastforce*

lemma *Int-image-empty*:

$\llbracket \bigwedge x \ y. f \ x \neq g \ y \rrbracket$
 $\implies f \ ^\circ \ S \cap g \ ^\circ \ T = \{\}$
by *auto*

lemma *Max-prop*:

$\llbracket \text{Max } S \in S \implies P \ (\text{Max } S); (S :: ('a :: \{\text{finite}, \text{linorder}\}) \ \text{set}) \neq \{\} \rrbracket \implies P$
 $(\text{Max } S)$
by *auto*

lemma *Min-prop*:

$\llbracket \text{Min } S \in S \implies P \ (\text{Min } S); (S :: ('a :: \{\text{finite}, \text{linorder}\}) \ \text{set}) \neq \{\} \rrbracket \implies P$
 $(\text{Min } S)$
by *auto*

lemma *findSomeD*:

$\text{find } P \ xs = \text{Some } x \implies P \ x \wedge x \in \text{set } xs$
by (*induct xs*) (*auto split: if-split-asm*)

lemma *findNoneD*:

$\text{find } P \ xs = \text{None} \implies \forall x \in \text{set } xs. \neg P \ x$
by (*induct xs*) (*auto split: if-split-asm*)

lemma *dom-upd*:

$\text{dom } (\lambda x. \text{if } x = y \text{ then } \text{None} \text{ else } f \ x) = \text{dom } f - \{y\}$
by (*rule set-eqI*) (*auto split: if-split-asm*)

definition

$\text{is-inv} :: ('a \multimap 'b) \Rightarrow ('b \multimap 'a) \Rightarrow \text{bool}$ **where**
 $\text{is-inv } f \ g \equiv \text{ran } f = \text{dom } g \wedge (\forall x \ y. f \ x = \text{Some } y \longrightarrow g \ y = \text{Some } x)$


```

lemma is-inv-NoneD:
  assumes  $g\ x = \text{None}$ 
  assumes is-inv  $f\ g$ 
  shows  $x \notin \text{ran } f$ 
proof -
  from assms
  have  $x \notin \text{dom } g$  by (auto simp: ran-def)
  moreover
  from assms
  have  $\text{ran } f = \text{dom } g$ 
    by (simp add: is-inv-def)
  ultimately
  show ?thesis by simp
qed

lemma is-inv-SomeD:
   $\llbracket f\ x = \text{Some } y; \text{is-inv } f\ g \rrbracket \implies g\ y = \text{Some } x$ 
  by (simp add: is-inv-def)

lemma is-inv-com:
   $\text{is-inv } f\ g \implies \text{is-inv } g\ f$ 
  apply (unfold is-inv-def)
  apply safe
    apply (clarsimp simp: ran-def dom-def set-eq-iff)
    apply (erule-tac x=a in allE)
    apply clarsimp
    apply (clarsimp simp: ran-def dom-def set-eq-iff)
    apply blast
    apply (clarsimp simp: ran-def dom-def set-eq-iff)
    apply (erule-tac x=x in allE)
    apply clarsimp
  done

lemma is-inv-inj:
   $\text{is-inv } f\ g \implies \text{inj-on } f\ (\text{dom } f)$ 
  apply (frule is-inv-com)
  apply (clarsimp simp: inj-on-def)
  apply (drule (1) is-inv-SomeD)
  apply (auto dest: is-inv-SomeD)
  done

lemma ran-upd':
   $\llbracket \text{inj-on } f\ (\text{dom } f); f\ y = \text{Some } z \rrbracket \implies \text{ran } (f\ (y := \text{None})) = \text{ran } f - \{z\}$ 
  by (force simp: ran-def inj-on-def dom-def intro!: set-eqI)

lemma is-inv-None-upd:
   $\llbracket \text{is-inv } f\ g; g\ x = \text{Some } y \rrbracket \implies \text{is-inv } (f\ (y := \text{None}))\ (g\ (x := \text{None}))$ 
  apply (subst is-inv-def)
  apply (clarsimp simp: dom-upd)

```

```

apply (drule is-inv-SomeD, erule is-inv-com)
apply (frule is-inv-inj)
apply (auto simp: ran-upd' is-inv-def dest: is-inv-SomeD is-inv-inj)
done

lemma is-inv-inj2:
  is-inv f g  $\implies$  inj-on g (dom g)
using is-inv-com is-inv-inj by blast

lemma range-convergence1:
   $\llbracket \forall z. x < z \wedge z \leq y \longrightarrow P\ z; \forall z > y. P\ (z :: 'a :: \text{linorder}) \rrbracket \implies \forall z > x. P\ z$ 
using not-le by blast

lemma range-convergence2:
   $\llbracket \forall z. x < z \wedge z \leq y \longrightarrow P\ z; \forall z. z > y \wedge z < w \longrightarrow P\ (z :: 'a :: \text{linorder}) \rrbracket$ 
 $\implies \forall z. z > x \wedge z < w \longrightarrow P\ z$ 
using range-convergence1 [where P= $\lambda z. z < w \longrightarrow P\ z$  and  $x=x$  and  $y=y$ ]
by auto

lemma zip-upt-Cons:
   $a < b \implies \text{zip}\ [a ..< b]\ (x \# xs) = (a, x) \# \text{zip}\ [\text{Suc}\ a ..< b]\ xs$ 
by (simp add: upt-conv-Cons)

lemma map-comp-eq:
   $f \circ_m g = \text{case-option}\ \text{None}\ f \circ g$ 
apply (rule ext)
apply (case-tac g x)
by auto

lemma dom-If-Some:
   $\text{dom}\ (\lambda x. \text{if } x \in S \text{ then Some } v \text{ else } f\ x) = (S \cup \text{dom}\ f)$ 
by (auto split: if-split)

lemma foldl-fun-upd-const:
   $\text{foldl}\ (\lambda s\ x. s(f\ x := v))\ s\ xs$ 
 $= (\lambda x. \text{if } x \in f\ \text{'set } xs \text{ then } v \text{ else } s\ x)$ 
by (induct xs arbitrary: s) auto

lemma foldl-id:
   $\text{foldl}\ (\lambda s\ x. s)\ s\ xs = s$ 
by (induct xs) auto

lemma SucSucMinus:  $2 \leq n \implies \text{Suc}\ (\text{Suc}\ (n - 2)) = n$  by arith

lemma ball-to-all:
   $(\bigwedge x. (x \in A) = (P\ x)) \implies (\forall x \in A. B\ x) = (\forall x. P\ x \longrightarrow B\ x)$ 
by blast

lemma case-option-If:

```

```

case-option P (λx. Q) v = (if v = None then P else Q)
by clarsimp

lemma case-option-If2:
  case-option P Q v = If (v ≠ None) (Q (the v)) P
  by (simp split: option.split)

lemma if3-fold:
  (if P then x else if Q then y else x) = (if P ∨ ¬ Q then x else y)
  by simp

lemma rtrancl-insert:
  assumes x-new:  $\bigwedge y. (x,y) \notin R$ 
  shows  $R^* \text{ ``insert } x \ S = \text{insert } x \ (R^* \text{ `` } S)$ 
proof -
  have  $R^* \text{ ``insert } x \ S = R^* \text{ `` } (\{x\} \cup S)$  by simp
  also
  have  $R^* \text{ `` } (\{x\} \cup S) = R^* \text{ `` } \{x\} \cup R^* \text{ `` } S$ 
    by (subst Image-Un) simp
  also
  have  $R^* \text{ `` } \{x\} = \{x\}$ 
    by (meson Image-closed-trancl Image-singleton-iff subsetI x-new)
  finally
  show ?thesis by simp
qed

lemma ran-del-subset:
   $y \in \text{ran } (f \ (x := \text{None})) \implies y \in \text{ran } f$ 
  by (auto simp: ran-def split: if-split-asm)

lemma trancl-sub-lift:
  assumes sub:  $\bigwedge p \ p'. (p,p') \in r \implies (p,p') \in r'$ 
  shows  $(p,p') \in r^+ \implies (p,p') \in r'^+$ 
  by (fastforce intro: trancl-mono sub)

lemma trancl-step-lift:
  assumes x-step:  $\bigwedge p \ p'. (p,p') \in r' \implies (p,p') \in r \vee (p = x \wedge p' = y)$ 
  assumes y-new:  $\bigwedge p'. \neg (y,p') \in r$ 
  shows  $(p,p') \in r'^+ \implies (p,p') \in r^+ \vee ((p,x) \in r^+ \wedge p' = y) \vee (p = x \wedge p' = y)$ 
  = y)
  apply (erule trancl-induct)
  apply (drule x-step)
  apply fastforce
  apply (erule disjE)
  apply (drule x-step)
  apply (erule disjE)
  apply (drule trancl-trans, drule r-into-trancl, assumption)
  apply blast
  apply fastforce

```

apply (*fastforce simp: y-new dest: x-step*)
done

lemma *rtrancl-simulate-weak*:

assumes $r: (x,z) \in R^*$
assumes $s: \bigwedge y. (x,y) \in R \implies (y,z) \in R^* \implies (x,y) \in R' \wedge (y,z) \in R'^*$
shows $(x,z) \in R'^*$
apply (*rule converse-rtranclE[OF r]*)
apply *simp*
apply (*frule (1) s*)
apply *clarsimp*
by (*rule converse-rtrancl-into-rtrancl*)

lemma *list-case-If2*:

case-list f g xs = If (xs = []) f (g (hd xs) (tl xs))
by (*simp split: list.split*)

lemma *length-ineq-not-Nil*:

$length\ xs > n \implies xs \neq []$
 $length\ xs \geq n \implies n \neq 0 \longrightarrow xs \neq []$
 $\neg length\ xs < n \implies n \neq 0 \longrightarrow xs \neq []$
 $\neg length\ xs \leq n \implies xs \neq []$
by *auto*

lemma *numeral-egs*:

$2 = Suc\ (Suc\ 0)$
 $3 = Suc\ (Suc\ (Suc\ 0))$
 $4 = Suc\ (Suc\ (Suc\ (Suc\ 0)))$
 $5 = Suc\ (Suc\ (Suc\ (Suc\ (Suc\ 0))))$
 $6 = Suc\ (Suc\ (Suc\ (Suc\ (Suc\ (Suc\ 0))))))$
by *simp+*

lemma *psubset-singleton*:

$(S \subset \{x\}) = (S = \{x\})$
by *blast*

lemma *length-takeWhile-ge*:

$length\ (takeWhile\ f\ xs) = n \implies length\ xs = n \vee (length\ xs > n \wedge \neg f\ (xs\ !\ n))$
by (*induct xs arbitrary: n*) (*auto split: if-split-asm*)

lemma *length-takeWhile-le*:

$\neg f\ (xs\ !\ n) \implies length\ (takeWhile\ f\ xs) \leq n$
by (*induct xs arbitrary: n; simp*) (*case-tac n; simp*)

lemma *length-takeWhile-gt*:

$n < length\ (takeWhile\ f\ xs)$
 $\implies (\exists\ ys\ zs. length\ ys = Suc\ n \wedge xs = ys\ @\ zs \wedge takeWhile\ f\ xs = ys\ @\ takeWhile\ f\ zs)$
apply (*induct xs arbitrary: n; simp split: if-split-asm*)

```

apply (case-tac n; simp)
apply (rule-tac x=[a] in exI)
apply simp
apply (erule meta-allE, drule(1) meta-mp)
apply clarsimp
apply (rule-tac x=a # ys in exI)
apply simp
done

```

lemma *hd-drop-conv-nth2*:
 $n < \text{length } xs \implies \text{hd } (\text{drop } n \text{ } xs) = xs ! n$
by (rule hd-drop-conv-nth) clarsimp

lemma *map-upt-eq-vals-D*:
 $\llbracket \text{map } f \text{ } [0 \dots n] = ys; m < \text{length } ys \rrbracket \implies f \text{ } m = ys ! m$
by clarsimp

lemma *length-le-helper*:
 $\llbracket n \leq \text{length } xs; n \neq 0 \rrbracket \implies xs \neq [] \wedge n - 1 \leq \text{length } (\text{tl } xs)$
by (cases xs, simp-all)

lemma *all-ex-eq-helper*:
 $(\forall v. (\exists v'. v = f \text{ } v' \wedge P \text{ } v \text{ } v') \longrightarrow Q \text{ } v)$
 $= (\forall v'. P \text{ } (f \text{ } v') \text{ } v' \longrightarrow Q \text{ } (f \text{ } v'))$
by auto

lemma *nat-less-cases'*:
 $(x::\text{nat}) < y \implies x = y - 1 \vee x < y - 1$
by auto

lemma *filter-to-shorter-upto*:
 $n \leq m \implies \text{filter } (\lambda x. x < n) [0 \dots m] = [0 \dots n]$
by (induct m) (auto elim: le-SucE)

lemma *in-emptyE*: $\llbracket A = \{\}; x \in A \rrbracket \implies P$ **by** blast

lemma *Ball-emptyI*:
 $S = \{\} \implies (\forall x \in S. P \text{ } x)$
by simp

lemma *allfEI*:
 $\llbracket \forall x. P \text{ } x; \bigwedge x. P \text{ } (f \text{ } x) \implies Q \text{ } x \rrbracket \implies \forall x. Q \text{ } x$
by fastforce

lemma *cart-singleton-empty2*:
 $(\{x\} \times S = \{\}) = (S = \{\})$
 $(\{\} = S \times \{e\}) = (S = \{\})$
by auto

lemma *cases-simp-conj*:

$((P \longrightarrow Q) \wedge (\neg P \longrightarrow Q) \wedge R) = (Q \wedge R)$

by *fastforce*

lemma *domE* :

$\llbracket x \in \text{dom } m; \bigwedge r. \llbracket m \ x = \text{Some } r \rrbracket \Longrightarrow P \rrbracket \Longrightarrow P$

by *clarsimp*

lemma *dom-eqD*:

$\llbracket f \ x = \text{Some } v; \text{dom } f = S \rrbracket \Longrightarrow x \in S$

by *clarsimp*

lemma *exception-set-finite-1*:

$\text{finite } \{x. P \ x\} \Longrightarrow \text{finite } \{x. (x = y \longrightarrow Q \ x) \wedge P \ x\}$

by (*simp add: Collect-conj-eq*)

lemma *exception-set-finite-2*:

$\text{finite } \{x. P \ x\} \Longrightarrow \text{finite } \{x. x \neq y \longrightarrow P \ x\}$

by (*simp add: imp-conv-disj*)

lemmas *exception-set-finite* = *exception-set-finite-1 exception-set-finite-2*

lemma *exfEI*:

$\llbracket \exists x. P \ x; \bigwedge x. P \ x \Longrightarrow Q \ (f \ x) \rrbracket \Longrightarrow \exists x. Q \ x$

by *fastforce*

lemma *Collect-int-vars*:

$\{s. P \ r \ v \ s\} \cap \{s. r \ v = x \ f \ s\} = \{s. P \ (x \ f \ s) \ s\} \cap \{s. r \ v = x \ f \ s\}$

by *auto*

lemma *if-0-1-eq*:

$((\text{if } P \text{ then } 1 \text{ else } 0) = (\text{case } Q \text{ of True} \Rightarrow \text{of-nat } 1 \mid \text{False} \Rightarrow \text{of-nat } 0)) = (P = Q)$

by (*simp split: if-split bool.split*)

lemma *modify-map-exists-cte* :

$(\exists \text{cte. modify-map } m \ p \ f \ p' = \text{Some cte}) = (\exists \text{cte. } m \ p' = \text{Some cte})$

by (*simp add: modify-map-def*)

lemma *dom-eqI*:

assumes *c1*: $\bigwedge x \ y. P \ x = \text{Some } y \Longrightarrow \exists y. Q \ x = \text{Some } y$

and *c2*: $\bigwedge x \ y. Q \ x = \text{Some } y \Longrightarrow \exists y. P \ x = \text{Some } y$

shows $\text{dom } P = \text{dom } Q$

unfolding *dom-def* **by** (*auto simp: c1 c2*)

lemma *dvd-reduce-multiple*:

fixes *k* :: *nat*

shows $(k \ \text{dvd} \ k * m + n) = (k \ \text{dvd} \ n)$

by (*induct m*) (*auto simp: add-ac*)

lemma *image-iff2*:

$\text{inj } f \implies f\ x \in f\ 'S = (x \in S)$
by (*rule inj-image-mem-iff*)

lemma *map-comp-restrict-map-Some-iff*:

$((g \circ_m (m \mid 'S))\ x = \text{Some } y) = ((g \circ_m m)\ x = \text{Some } y \wedge x \in S)$
by (*auto simp add: map-comp-Some-iff restrict-map-Some-iff*)

lemma *range-subsetD*:

fixes $a :: 'a :: \text{order}$
shows $\llbracket \{a..b\} \subseteq \{c..d\}; a \leq b \rrbracket \implies c \leq a \wedge b \leq d$
by *simp*

lemma *case-option-dom*:

$(\text{case } f\ x \text{ of } \text{None} \Rightarrow a \mid \text{Some } v \Rightarrow b\ v) = (\text{if } x \in \text{dom } f \text{ then } b\ (\text{the } (f\ x)) \text{ else } a)$
by (*auto split: option.split*)

lemma *contrapos-imp*:

$P \longrightarrow Q \implies \neg Q \longrightarrow \neg P$
by *clarsimp*

lemma *filter-eq-If*:

$\text{distinct } xs \implies \text{filter } (\lambda v. v = x)\ xs = (\text{if } x \in \text{set } xs \text{ then } [x] \text{ else } [])$
by (*induct xs auto*)

lemma (*in semigroup-add*) *foldl-assoc*:

shows $\text{foldl } (+) (x+y)\ zs = x + (\text{foldl } (+)\ y\ zs)$
by (*induct zs arbitrary: y (simp-all add: add.assoc)*)

lemma (*in monoid-add*) *foldl-absorb0*:

shows $x + (\text{foldl } (+)\ 0\ zs) = \text{foldl } (+)\ x\ zs$
by (*induct zs (simp-all add: foldl-assoc)*)

lemma *foldl-conv-concat*:

$\text{foldl } (@)\ xs\ xss = xs @ \text{concat } xss$
proof (*induct xss arbitrary: xs*)
case *Nil* **show** ?case **by** *simp*
next
interpret *monoid-add* (@) **proof** *qed simp-all*
case *Cons* **then show** ?case **by** (*simp add: foldl-absorb0*)
qed

lemma *foldl-concat-concat*:

$\text{foldl } (@)\ []\ (xs @ ys) = \text{foldl } (@)\ []\ xs @ \text{foldl } (@)\ []\ ys$
by (*simp add: foldl-conv-concat*)

lemma *foldl-does-nothing*:

$\llbracket \bigwedge x. x \in \text{set } xs \implies f\ s\ x = s \rrbracket \implies \text{foldl } f\ s\ xs = s$

by (*induct xs*) *auto*

lemma *foldl-use-filter*:

$$\llbracket \bigwedge v x. \llbracket \neg g x; x \in \text{set } xs \rrbracket \implies f v x = v \rrbracket \implies \text{foldl } f v xs = \text{foldl } f v (\text{filter } g xs)$$
by (*induct xs arbitrary: v*) *auto*

lemma *map-comp-update-lift*:
assumes *fv*: $f v = \text{Some } v'$
shows $(f \circ_m (g(\text{ptr} \mapsto v))) = ((f \circ_m g)(\text{ptr} \mapsto v'))$
by (*simp add: fv map-comp-update*)

lemma *restrict-map-cong*:
assumes *sv*: $S = S'$
and *rl*: $\bigwedge p. p \in S' \implies mp p = mp' p$
shows $mp \mid 'S = mp' \mid 'S'$
using *expand-restrict-map-eq rl sv* **by** *auto*

lemma *case-option-over-if*:

$$\begin{aligned} \text{case-option } P Q (\text{if } G \text{ then None else Some } v) &= (\text{if } G \text{ then } P \text{ else } Q v) \\ \text{case-option } P Q (\text{if } G \text{ then Some } v \text{ else None}) &= (\text{if } G \text{ then } Q v \text{ else } P) \end{aligned}$$
by (*simp split: if-split*)**+**

lemma *map-length-cong*:

$$\llbracket \text{length } xs = \text{length } ys; \bigwedge x y. (x, y) \in \text{set } (\text{zip } xs ys) \implies f x = g y \rrbracket \implies \text{map } f xs = \text{map } g ys$$
apply *atomize*
apply (*erule rev-mp, erule list-induct2*)
apply *auto*
done

lemma *take-min-len*:

$$\text{take } (\text{min } (\text{length } xs) n) xs = \text{take } n xs$$
by (*simp add: min-def*)

lemmas *interval-empty = atLeastatMost-empty-iff*

lemma *fold-and-false*[*simp*]:

$$\neg(\text{fold } (\wedge) xs \text{ False})$$
apply *clarsimp*
apply (*induct xs*)
apply *simp*
apply *simp*
done

lemma *fold-and-true*:

$$\text{fold } (\wedge) xs \text{ True} \implies \forall i < \text{length } xs. xs ! i$$


```

apply clarsimp
apply (induct xs)
  apply simp
apply (case-tac i = 0; simp)
  apply (case-tac a; simp)
apply (case-tac a; simp)
done

```

```

lemma fold-or-true[simp]:
  fold ( $\vee$ ) xs True
  by (induct xs, simp+)

```

```

lemma fold-or-false:
   $\neg(\text{fold } (\vee) \text{ } xs \text{ } False) \implies \forall i < \text{length } xs. \neg(xs ! i)$ 
  apply (induct xs, simp+)
  apply (case-tac a, simp+)
  apply (rule allI, case-tac i = 0, simp+)
done

```

12 Take, drop, zip, list_alletcrules

```

method two-induct for xs ys =
  ((induct xs arbitrary: ys; simp?), (case-tac ys; simp?))

```

```

lemma map-fst-zip-prefix:
  map fst (zip xs ys) ≤ xs
  by (two-induct xs ys)

```

```

lemma map-snd-zip-prefix:
  map snd (zip xs ys) ≤ ys
  by (two-induct xs ys)

```

```

lemma nth-upt-0 [simp]:
   $i < \text{length } xs \implies [0..<\text{length } xs] ! i = i$ 
  by simp

```

```

lemma take-insert-nth:
   $i < \text{length } xs \implies \text{insert } (xs ! i) (\text{set } (\text{take } i \text{ } xs)) = \text{set } (\text{take } (Suc \ i) \ xs)$ 
  by (subst take-Suc-conv-app-nth, assumption, fastforce)

```

```

lemma zip-take-drop:
   $\llbracket n < \text{length } xs; \text{length } ys = \text{length } xs \rrbracket \implies$ 
   $\text{zip } xs \ (\text{take } n \text{ } ys \ @ \ a \ \# \ \text{drop } (Suc \ n) \ ys) =$ 
   $\text{zip } (\text{take } n \text{ } xs) \ (\text{take } n \text{ } ys) \ @ \ (xs ! n, a) \ \# \ \text{zip } (\text{drop } (Suc \ n) \ xs) \ (\text{drop } (Suc$ 
   $n) \ ys)$ 
  by (subst id-take-nth-drop, assumption, simp)

```

```

lemma take-nth-distinct:
   $\llbracket \text{distinct } xs; n < \text{length } xs; xs ! n \in \text{set } (\text{take } n \text{ } xs) \rrbracket \implies False$ 

```

by (fastforce simp: distinct-conv-nth in-set-conv-nth)

lemma take-drop-append:
 $drop\ a\ xs = take\ b\ (drop\ a\ xs) @ drop\ (a + b)\ xs$
 by (metis append-take-drop-id drop-drop add commute)

lemma drop-take-drop:
 $drop\ a\ (take\ (b + a)\ xs) @ drop\ (b + a)\ xs = drop\ a\ xs$
 by (metis add commute take-drop take-drop-append)

lemma not-prefixI:
 $\llbracket xs \neq ys; length\ xs = length\ ys \rrbracket \implies \neg xs \leq ys$
 by (auto elim: prefixE)

lemma map-fst-zip':
 $length\ xs \leq length\ ys \implies map\ fst\ (zip\ xs\ ys) = xs$
 by (metis length-map length-zip map-fst-zip-prefix min-absorb1 not-prefixI)

lemma zip-take-triv:
 $n \geq length\ bs \implies zip\ (take\ n\ as)\ bs = zip\ as\ bs$
 apply (induct bs arbitrary: n as; simp)
 apply (case-tac n; simp)
 apply (case-tac as; simp)
 done

lemma zip-take-triv2:
 $length\ as \leq n \implies zip\ as\ (take\ n\ bs) = zip\ as\ bs$
 apply (induct as arbitrary: n bs; simp)
 apply (case-tac n; simp)
 apply (case-tac bs; simp)
 done

lemma zip-take-length:
 $zip\ xs\ (take\ (length\ xs)\ ys) = zip\ xs\ ys$
 by (metis order-refl zip-take-triv2)

lemma zip-singleton:
 $ys \neq [] \implies zip\ [a]\ ys = [(a, ys ! 0)]$
 by (case-tac ys, simp-all)

lemma zip-append-singleton:
 $\llbracket i = length\ xs; length\ xs < length\ ys \rrbracket \implies zip\ (xs @ [a])\ ys = (zip\ xs\ ys) @ [(a, ys ! i)]$
 by (induct xs; case-tac ys; simp)
 (clarsimp simp: zip-append1 zip-take-length zip-singleton)

lemma ran-map-of-zip:
 $\llbracket length\ xs = length\ ys; distinct\ xs \rrbracket \implies ran\ (map-of\ (zip\ xs\ ys)) = set\ ys$
 by (induct rule: list-induct2) auto

```

lemma ranE:
   $\llbracket v \in \text{ran } f; \bigwedge x. f\ x = \text{Some } v \implies R \rrbracket \implies R$ 
  by (auto simp: ran-def)

lemma ran-map-option-restrict-eq:
   $\llbracket x \in \text{ran } (\text{map-option } f \circ g); x \notin \text{ran } (\text{map-option } f \circ (g \mid '(- \{y\}))) \rrbracket$ 
     $\implies \exists v. g\ y = \text{Some } v \wedge f\ v = x$ 
  apply (clarsimp simp: elim!: ranE)
  apply (rename-tac w z)
  apply (case-tac w = y)
  apply clarsimp
  apply (erule notE, rule-tac a=w in ranI)
  apply (simp add: restrict-map-def)
  done

lemma map-of-zip-range:
   $\llbracket \text{length } xs = \text{length } ys; \text{distinct } xs \rrbracket \implies (\lambda x. (\text{the } (\text{map-of } (\text{zip } xs\ ys)\ x))) \text{ ' set}$ 
   $xs = \text{set } ys$ 
  apply (clarsimp simp: image-def)
  apply (subst ran-map-of-zip [symmetric, where xs=xs and ys=ys]; simp?)
  apply (clarsimp simp: ran-def)
  apply (rule equalityI)
  apply clarsimp
  apply (rename-tac x)
  apply (frule-tac x=x in map-of-zip-is-Some; fastforce)
  apply (clarsimp simp: set-zip)
  by (metis domI dom-map-of-zip nth-mem ranE ran-map-of-zip option.sel)

lemma map-zip-fst:
   $\text{length } xs = \text{length } ys \implies \text{map } (\lambda(x, y). f\ x) (\text{zip } xs\ ys) = \text{map } f\ xs$ 
  by (two-induct xs ys)

lemma map-zip-fst':
   $\text{length } xs \leq \text{length } ys \implies \text{map } (\lambda(x, y). f\ x) (\text{zip } xs\ ys) = \text{map } f\ xs$ 
  by (metis length-map map-fst-zip' map-zip-fst zip-map-fst-snd)

lemma map-zip-snd:
   $\text{length } xs = \text{length } ys \implies \text{map } (\lambda(x, y). f\ y) (\text{zip } xs\ ys) = \text{map } f\ ys$ 
  by (two-induct xs ys)

lemma map-zip-snd':
   $\text{length } ys \leq \text{length } xs \implies \text{map } (\lambda(x, y). f\ y) (\text{zip } xs\ ys) = \text{map } f\ ys$ 
  by (two-induct xs ys)

lemma map-of-zip-tuple-in:
   $\llbracket (x, y) \in \text{set } (\text{zip } xs\ ys); \text{distinct } xs \rrbracket \implies \text{map-of } (\text{zip } xs\ ys)\ x = \text{Some } y$ 
  by (two-induct xs ys) (auto intro: in-set-zipE)

```

lemma *in-set-zip1*:

$(x, y) \in \text{set } (\text{zip } xs \ ys) \implies x \in \text{set } xs$
by (*erule in-set-zipE*)

lemma *in-set-zip2*:

$(x, y) \in \text{set } (\text{zip } xs \ ys) \implies y \in \text{set } ys$
by (*erule in-set-zipE*)

lemma *map-zip-snd-take*:

$\text{map } (\lambda(x, y). f \ y) (\text{zip } xs \ ys) = \text{map } f (\text{take } (\text{length } xs) \ ys)$
apply (*subst map-zip-snd' [symmetric, where xs=xs and ys=take (length xs) ys], simp*)
apply (*subst zip-take-length [symmetric], simp*)
done

lemma *map-of-zip-is-index*:

$\llbracket \text{length } xs = \text{length } ys; x \in \text{set } xs \rrbracket \implies \exists i. (\text{map-of } (\text{zip } xs \ ys)) \ x = \text{Some } (ys \ ! \ i)$
apply (*induct rule: list-induct2; simp*)
apply (*rule conjI; clarsimp*)
apply (*metis nth-Cons-0*)
apply (*metis nth-Cons-Suc*)
done

lemma *map-of-zip-take-update*:

$\llbracket i < \text{length } xs; \text{length } xs \leq \text{length } ys; \text{distinct } xs \rrbracket$
 $\implies \text{map-of } (\text{zip } (\text{take } i \ xs) \ ys) (xs \ ! \ i \mapsto (ys \ ! \ i)) = \text{map-of } (\text{zip } (\text{take } (\text{Suc } i) \ xs) \ ys)$
apply (*rule ext, rename-tac x*)
apply (*case-tac x=xs ! i; clarsimp*)
apply (*rule map-of-is-SomeI[symmetric]*)
apply (*simp add: map-fst-zip'*)
apply (*force simp add: set-zip*)
apply (*clarsimp simp: take-Suc-conv-app-nth zip-append-singleton map-add-def split: option.splits*)
done

lemma *map-of-zip-is-Some'*:

$\text{length } xs \leq \text{length } ys \implies (x \in \text{set } xs) = (\exists y. \text{map-of } (\text{zip } xs \ ys) \ x = \text{Some } y)$
apply (*subst zip-take-length[symmetric]*)
apply (*rule map-of-zip-is-Some*)
by (*metis length-take min-absorb2*)

lemma *map-of-zip-inj*:

$\llbracket \text{distinct } xs; \text{distinct } ys; \text{length } xs = \text{length } ys \rrbracket$
 $\implies \text{inj-on } (\lambda x. (\text{the } (\text{map-of } (\text{zip } xs \ ys) \ x))) (\text{set } xs)$
apply (*clarsimp simp: inj-on-def*)
apply (*subst (asm) map-of-zip-is-Some, assumption*) +

apply *clarsimp*
apply (*clarsimp simp: set-zip*)
by (*metis nth-eq-iff-index-eq*)

lemma *map-of-zip-inj'*:
 $\llbracket \text{distinct } xs; \text{distinct } ys; \text{length } xs \leq \text{length } ys \rrbracket$
 $\implies \text{inj-on } (\lambda x. (\text{the } (\text{map-of } (\text{zip } xs \text{ } ys) \text{ } x))) (\text{set } xs)$
apply (*subst zip-take-length[symmetric]*)
apply (*erule map-of-zip-inj, simp*)
by (*metis length-take min-absorb2*)

lemma *list-all-nth*:
 $\llbracket \text{list-all } P \text{ } xs; i < \text{length } xs \rrbracket \implies P (xs ! i)$
by (*metis list-all-length*)

lemma *list-all-update*:
 $\llbracket \text{list-all } P \text{ } xs; i < \text{length } xs; \bigwedge x. P \text{ } x \implies P (f \text{ } x) \rrbracket$
 $\implies \text{list-all } P (xs [i := f (xs ! i)])$
by (*metis length-list-update list-all-length nth-list-update*)

lemma *list-allI*:
 $\llbracket \text{list-all } P \text{ } xs; \bigwedge x. P \text{ } x \implies P' \text{ } x \rrbracket \implies \text{list-all } P' \text{ } xs$
by (*metis list-all-length*)

lemma *list-all-imp-filter*:
 $\text{list-all } (\lambda x. f \text{ } x \longrightarrow g \text{ } x) \text{ } xs = \text{list-all } (\lambda x. g \text{ } x) [x \leftarrow xs . f \text{ } x]$
by (*fastforce simp: Ball-set-list-all[symmetric]*)

lemma *list-all-imp-filter2*:
 $\text{list-all } (\lambda x. f \text{ } x \longrightarrow g \text{ } x) \text{ } xs = \text{list-all } (\lambda x. \neg f \text{ } x) [x \leftarrow xs . (\lambda x. \neg g \text{ } x) \text{ } x]$
by (*fastforce simp: Ball-set-list-all[symmetric]*)

lemma *list-all-imp-chain*:
 $\llbracket \text{list-all } (\lambda x. f \text{ } x \longrightarrow g \text{ } x) \text{ } xs; \text{list-all } (\lambda x. f' \text{ } x \longrightarrow f \text{ } x) \text{ } xs \rrbracket$
 $\implies \text{list-all } (\lambda x. f' \text{ } x \longrightarrow g \text{ } x) \text{ } xs$
by (*clarsimp simp: Ball-set-list-all [symmetric]*)

lemma *inj-Pair*:
 $\text{inj-on } (\text{Pair } x) \text{ } S$
by (*rule inj-onI, simp*)

lemma *inj-on-split*:
 $\text{inj-on } f \text{ } S \implies \text{inj-on } (\lambda x. (z, f \text{ } x)) \text{ } S$
by (*auto simp: inj-on-def*)

lemma *split-state-strg*:

$(\exists x. f\ s = x \wedge P\ x\ s) \longrightarrow P\ (f\ s)\ s$ **by** *clarsimp*

lemma *theD*:

$\llbracket the\ (f\ x) = y;\ x \in dom\ f \rrbracket \Longrightarrow f\ x = Some\ y$
by *(auto simp add: dom-def)*

lemma *bspec-split*:

$\llbracket \forall (a, b) \in S. P\ a\ b;\ (a, b) \in S \rrbracket \Longrightarrow P\ a\ b$
by *fastforce*

lemma *set-zip-same*:

$set\ (zip\ xs\ xs) = Id \cap (set\ xs \times set\ xs)$
by *(induct xs) auto*

lemma *ball-ran-updI*:

$(\forall x \in ran\ m. P\ x) \Longrightarrow P\ v \Longrightarrow (\forall x \in ran\ (m\ (y \mapsto v)). P\ x)$
by *(auto simp add: ran-def)*

lemma *not-psubset-eq*:

$\llbracket \neg A \subset B;\ A \subseteq B \rrbracket \Longrightarrow A = B$
by *blast*

lemma *in-image-op-plus*:

$(x + y \in (+)\ x\ 'S) = ((y :: 'a :: ring) \in S)$
by *(simp add: image-def)*

lemma *insert-subtract-new*:

$x \notin S \Longrightarrow (insert\ x\ S - S) = \{x\}$
by *auto*

lemma *zip-is-empty*:

$(zip\ xs\ ys = []) = (xs = [] \vee ys = [])$
by *(cases xs; simp) (cases ys; simp)*

lemma *minus-Suc-0-lt*:

$a \neq 0 \Longrightarrow a - Suc\ 0 < a$
by *simp*

lemma *fst-last-zip-upt*:

$zip\ [0 ..< m]\ xs \neq [] \Longrightarrow$
 $fst\ (last\ (zip\ [0 ..< m]\ xs)) = (if\ length\ xs < m\ then\ length\ xs - 1\ else\ m - 1)$
apply *(subst last-conv-nth, assumption)*
apply *(simp only: One-nat-def)*
apply *(subst nth-zip)*
apply *(rule order-less-le-trans[OF minus-Suc-0-lt])*
apply *(simp add: zip-is-empty)*
apply *simp*

```

apply (rule order-less-le-trans[OF minus-Suc-0-lt])
apply (simp add: zip-is-empty)
apply simp
apply (simp add: min-def zip-is-empty)
done

lemma neq-into-nprefix:
   $\llbracket x \neq \text{take } (\text{length } x) \ y \rrbracket \implies \neg x \leq y$ 
by (clarsimp simp: prefix-def less-eq-list-def)

lemma suffix-eqI:
   $\llbracket \text{suffix } xs \ as; \text{suffix } xs \ bs; \text{length } as = \text{length } bs; \\ \text{take } (\text{length } as - \text{length } xs) \ as \leq \text{take } (\text{length } bs - \text{length } xs) \ bs \rrbracket \implies as = bs$ 
by (clarsimp elim!: prefixE suffixE)

lemma suffix-Cons-mem:
   $\text{suffix } (x \# xs) \ as \implies x \in \text{set } as$ 
by (metis in-set-conv-decomp suffix-def)

lemma distinct-imply-not-in-tail:
   $\llbracket \text{distinct } list; \text{suffix } (y \# ys) \ list \rrbracket \implies y \notin \text{set } ys$ 
by (clarsimp simp: suffix-def)

lemma list-induct-suffix [case-names Nil Cons]:
  assumes nilr:  $P \llbracket$ 
  and consr:  $\bigwedge x \ xs. \llbracket P \ xs; \text{suffix } (x \# xs) \ as \rrbracket \implies P \ (x \# xs)$ 
  shows  $P \ as$ 
proof –
  define  $as'$  where  $as' == as$ 

  have  $\text{suffix } as \ as'$  unfolding  $as'$ -def by simp
  then show ?thesis
  proof (induct as)
    case Nil show ?case by fact
  next
    case (Cons x xs)

    show ?case
    proof (rule consr)
      from Cons.prem1 show  $\text{suffix } (x \# xs) \ as$  unfolding  $as'$ -def .
      then have  $\text{suffix } xs \ as'$  by (auto dest: suffix-ConsD simp:  $as'$ -def)
      then show  $P \ xs$  using Cons.hyps by simp
    qed
  qed
qed

```

Parallel etc. and lemmas for list prefix

```

lemma prefix-induct [consumes 1, case-names Nil Cons]:
  fixes prefix

```

```

    assumes np:  $\text{prefix} \leq \text{lst}$ 
    and base:  $\bigwedge xs. P [] xs$ 
    and rl:  $\bigwedge x xs y ys. [x = y; xs \leq ys; P xs ys] \implies P (x \# xs) (y \# ys)$ 
    shows  $P \text{ prefix } \text{lst}$ 
    using np
  proof (induct prefix arbitrary: lst)
    case Nil show ?case by fact
  next
    case (Cons x xs)

    have prem:  $(x \# xs) \leq \text{lst}$  by fact
    then obtain y ys where lv:  $\text{lst} = y \# ys$ 
      by (rule prefixE, auto)

    have ih:  $\bigwedge \text{lst}. xs \leq \text{lst} \implies P xs \text{lst}$  by fact

    show ?case using prem
      by (auto simp: lv intro!: rl ih)
  qed

lemma not-prefix-cases:
  fixes prefix
  assumes pfx:  $\neg \text{prefix} \leq \text{lst}$ 
  and c1:  $[ \text{prefix} \neq []; \text{lst} = [] ] \implies R$ 
  and c2:  $\bigwedge a as x xs. [ \text{prefix} = a \# as; \text{lst} = x \# xs; x = a; \neg as \leq xs ] \implies R$ 
  and c3:  $\bigwedge a as x xs. [ \text{prefix} = a \# as; \text{lst} = x \# xs; x \neq a ] \implies R$ 
  shows R
proof (cases prefix)
  case Nil then show ?thesis using pfx by simp
next
  case (Cons a as)

  have c:  $\text{prefix} = a \# as$  by fact

  show ?thesis
  proof (cases lst)
    case Nil then show ?thesis
      by (intro c1, simp add: Cons)
  next
    case (Cons x xs)
    show ?thesis
    proof (cases x = a)
      case True
      show ?thesis
      proof (intro c2)
        show  $\neg as \leq xs$  using pfx c Cons True
          by simp
      qed fact+
    next

```



```

    case False
    show ?thesis by (rule c3) fact+
  qed
qed
qed

lemma not-prefix-induct [consumes 1, case-names Nil Neq Eq]:
  fixes prefix
  assumes np:  $\neg \text{prefix} \leq \text{lst}$ 
  and base:  $\bigwedge x \text{ xs}. P (x \# \text{xs})$ 
  and r1:  $\bigwedge x \text{ xs } y \text{ ys}. x \neq y \implies P (x \# \text{xs}) (y \# \text{ys})$ 
  and r2:  $\bigwedge x \text{ xs } y \text{ ys}. \llbracket x = y; \neg \text{xs} \leq \text{ys}; P \text{ xs } \text{ys} \rrbracket \implies P (x \# \text{xs}) (y \# \text{ys})$ 
  shows  $P \text{ prefix } \text{lst}$ 
  using np
proof (induct lst arbitrary: prefix)
  case Nil then show ?case
    by (auto simp: neq-Nil-conv elim!: not-prefix-cases intro!: base)
  next
    case (Cons y ys)

    have npfx:  $\neg \text{prefix} \leq (y \# \text{ys})$  by fact
    then obtain x xs where pv:  $\text{prefix} = x \# \text{xs}$ 
      by (rule not-prefix-cases) auto

    have ih:  $\bigwedge \text{prefix}. \neg \text{prefix} \leq \text{ys} \implies P \text{ prefix } \text{ys}$  by fact

    show ?case using npfx
      by (simp only: pv) (erule not-prefix-cases, auto intro: r1 r2 ih)
  qed

lemma rsubst:
   $\llbracket P s; s = t \rrbracket \implies P t$ 
  by simp

lemma ex-impE:  $((\exists x. P x) \longrightarrow Q) \implies P x \implies Q$ 
  by blast

lemma option-Some-value-independent:
   $\llbracket f x = \text{Some } v; \bigwedge v'. f x = \text{Some } v' \rrbracket \implies f y = \text{Some } v$ 
  by blast

Some int bitwise lemmas. Helpers for proofs about NatBitwise.thy

lemma int-2p-eq-shiffl:
   $(2::\text{int})^x = 1 << x$ 
  by (simp add: shiffl-int-def)

lemma nat-int-mul:
   $\text{nat } (\text{int } a * b) = a * \text{nat } b$ 
  by (simp add: nat-mult-distrib)

```

lemma *int-shiffl-less-cancel*:

```

   $n \leq m \implies ((x :: \text{int}) << n < y << m) = (x < y << (m - n))$ 
  apply (drule le-Suc-ex)
  apply (clarsimp simp: shiffl-int-def power-add)
  done

```

lemma *int-shiffl-lt-2p-bits*:

```

   $0 \leq (x :: \text{int}) \implies x < 1 << n \implies \forall i \geq n. \neg x !! i$ 
  apply (clarsimp simp: shiffl-int-def)
  apply (clarsimp simp: bin-nth-eq-mod even-iff-mod-2-eq-zero)
  apply (drule-tac z=2^i in less-le-trans)
  apply simp
  apply simp
  done

```

— TODO: The converse should be true as well, but seems hard to prove.

lemma *int-eq-test-bit*:

```

   $((x :: \text{int}) = y) = (\forall i. \text{test-bit } x \ i = \text{test-bit } y \ i)$ 
  apply simp
  apply (metis bin-eqI)
  done

```

lemmas *int-eq-test-bitI* = *int-eq-test-bit*[*THEN iffD2, rule-format*]

lemma *le-nat-shrink-left*:

```

   $y \leq z \implies y = \text{Suc } x \implies x < z$ 
  by simp

```

lemma *length-ge-split*:

```

   $n < \text{length } xs \implies \exists x \ xs'. \ xs = x \# xs' \wedge n \leq \text{length } xs'$ 
  by (cases xs) auto

```

end

Nondeterministic State Monad with Failure **theory** *NonDetMonad*

imports *../Lib*

begin

State monads are used extensively in the seL4 specification. They are defined below.

13 The Monad

The basic type of the nondeterministic state monad with failure is very similar to the normal state monad. Instead of a pair consisting of result and new state, we return a set of these pairs coupled with a failure flag. Each element in the set is a potential result of the computation. The flag is *True* if there is an execution path in the computation that may have failed.

Conversely, if the flag is *False*, none of the computations resulting in the returned set can have failed.

type-synonym (*'s, 'a*) *nondet-monad* = *'s* \Rightarrow (*'a* \times *'s*) *set* \times *bool*

Print the type (*'s, 'a*) *nondet-monad* instead of its unwieldy expansion. Needs an AST translation in code, because it needs to check that the state variable *'s* occurs twice. This comparison is not guaranteed to always work as expected (AST instances might have different decoration), but it does seem to work here.

print-ast-translation (

```

let
  fun monad-tr - [t1, Ast.Appl [Ast.Constant @{type-syntax prod},
                                Ast.Appl [Ast.Constant @{type-syntax set},
                                            Ast.Appl [Ast.Constant @{type-syntax prod}, t2, t3]],
                                Ast.Constant @{type-syntax bool}]] =
    if t3 = t1
    then Ast.Appl [Ast.Constant @{type-syntax nondet-monad}, t1, t2]
    else raise Match
in [(@{type-syntax fun}, monad-tr)] end
)
```

The definition of fundamental monad functions *return* and *bind*. The monad function *return* *x* does not change the state, does not fail, and returns *x*.

definition

```

return :: 'a  $\Rightarrow$  ('s, 'a) nondet-monad where
return a  $\equiv$   $\lambda s.$  ({(a,s)}, False)

```

The monad function *bind* *f g*, also written *f* $>>=$ *g*, is the execution of *f* followed by the execution of *g*. The function *g* takes the result value *and* the result state of *f* as parameter. The definition says that the result of the combined operation is the union of the set of sets that is created by *g* applied to the result sets of *f*. The combined operation may have failed, if *f* may have failed or *g* may have failed on any of the results of *f*.

definition

```

bind :: ('s, 'a) nondet-monad  $\Rightarrow$  ('a  $\Rightarrow$  ('s, 'b) nondet-monad)  $\Rightarrow$ 
      ('s, 'b) nondet-monad (infixl  $>>=$  60)
where
bind f g  $\equiv$   $\lambda s.$  ( $\bigcup$  (fst ' case-prod g ' fst (f s)),
                  True  $\in$  snd ' case-prod g ' fst (f s)  $\vee$  snd (f s))

```

Sometimes it is convenient to write *bind* in reverse order.

abbreviation(*input*)

```

bind-rev :: ('c  $\Rightarrow$  ('a, 'b) nondet-monad)  $\Rightarrow$  ('a, 'c) nondet-monad  $\Rightarrow$ 
          ('a, 'b) nondet-monad (infixl  $=<<$  60) where
g  $=<<$  f  $\equiv$  f  $>>=$  g

```

The basic accessor functions of the state monad. *get* returns the current state as result, does not fail, and does not change the state. *put s* returns nothing (*unit*), changes the current state to *s* and does not fail.

definition

$get :: ('s, 's) \text{ nondet-monad } \mathbf{where}$
 $get \equiv \lambda s. (\{(s, s)\}, \text{False})$

definition

$put :: 's \Rightarrow ('s, \text{unit}) \text{ nondet-monad } \mathbf{where}$
 $put\ s \equiv \lambda -. (\{(() , s)\}, \text{False})$

13.1 Nondeterminism

Basic nondeterministic functions. *select A* chooses an element of the set *A*, does not change the state, and does not fail (even if the set is empty). *f OR g* executes *f* or executes *g*. It returns the union of results of *f* and *g*, and may have failed if either may have failed.

definition

$select :: 'a \text{ set} \Rightarrow ('s, 'a) \text{ nondet-monad } \mathbf{where}$
 $select\ A \equiv \lambda s. (A \times \{s\}, \text{False})$

definition

$alternative :: ('s, 'a) \text{ nondet-monad} \Rightarrow ('s, 'a) \text{ nondet-monad} \Rightarrow$
 $('s, 'a) \text{ nondet-monad}$
 $(\mathbf{infixl}\ OR\ 20)$

where

$f\ OR\ g \equiv \lambda s. (fst\ (f\ s) \cup fst\ (g\ s), snd\ (f\ s) \vee snd\ (g\ s))$

Alternative notation for *OR*

notation (*xsymbols*) *alternative* (**infixl** $\sqcap\ 20$)

A variant of *select* that takes a pair. The first component is a set as in normal *select*, the second component indicates whether the execution failed. This is useful to lift monads between different state spaces.

definition

$select\text{-}f :: 'a \text{ set} \times \text{bool} \Rightarrow ('s, 'a) \text{ nondet-monad } \mathbf{where}$
 $select\text{-}f\ S \equiv \lambda s. (fst\ S \times \{s\}, snd\ S)$

select-state takes a relationship between states, and outputs nondeterministically a state related to the input state.

definition

$state\text{-}select :: ('s \times 's) \text{ set} \Rightarrow ('s, \text{unit}) \text{ nondet-monad}$

where

$state\text{-}select\ r \equiv \lambda s. ((\lambda x. (() , x))\ ' \{s'. (s, s') \in r\}, \neg (\exists s'. (s, s') \in r))$

13.2 Failure

The monad function that always fails. Returns an empty set of results and sets the failure flag.

definition

$fail :: ('s, 'a) \text{ nondet-monad } \mathbf{where}$
 $fail \equiv \lambda s. (\{\}, True)$

Assertions: fail if the property P is not true

definition

$assert :: bool \Rightarrow ('a, unit) \text{ nondet-monad } \mathbf{where}$
 $assert P \equiv \text{if } P \text{ then return } () \text{ else fail}$

Fail if the value is $None$, return result v for $Some v$

definition

$assert-opt :: 'a \text{ option} \Rightarrow ('b, 'a) \text{ nondet-monad } \mathbf{where}$
 $assert-opt v \equiv \text{case } v \text{ of } None \Rightarrow fail \mid Some v \Rightarrow return v$

An assertion that also can introspect the current state.

definition

$state-assert :: ('s \Rightarrow bool) \Rightarrow ('s, unit) \text{ nondet-monad}$
 \mathbf{where}
 $state-assert P \equiv get \gg= (\lambda s. assert (P s))$

13.3 Generic functions on top of the state monad

Apply a function to the current state and return the result without changing the state.

definition

$gets :: ('s \Rightarrow 'a) \Rightarrow ('s, 'a) \text{ nondet-monad } \mathbf{where}$
 $gets f \equiv get \gg= (\lambda s. return (f s))$

Modify the current state using the function passed in.

definition

$modify :: ('s \Rightarrow 's) \Rightarrow ('s, unit) \text{ nondet-monad } \mathbf{where}$
 $modify f \equiv get \gg= (\lambda s. put (f s))$

lemma *simpler-gets-def*: $gets f = (\lambda s. (\{f s, s\}, False))$
apply (*simpl add: gets-def return-def bind-def get-def*)
done

lemma *simpler-modify-def*:

$modify f = (\lambda s. (\{(), f s\}, False))$
by (*simpl add: modify-def bind-def get-def put-def*)

Execute the given monad when the condition is true, return $()$ otherwise.

definition

$when :: bool \Rightarrow ('s, unit) \text{ nondet-monad} \Rightarrow$
 $('s, unit) \text{ nondet-monad} \textbf{ where}$
 $when P m \equiv if P then m else return ()$

Execute the given monad unless the condition is true, return $()$ otherwise.

definition

$unless :: bool \Rightarrow ('s, unit) \text{ nondet-monad} \Rightarrow$
 $('s, unit) \text{ nondet-monad} \textbf{ where}$
 $unless P m \equiv when (\neg P) m$

Perform a test on the current state, performing the left monad if the result is true or the right monad if the result is false.

definition

$condition :: ('s \Rightarrow bool) \Rightarrow ('s, 'r) \text{ nondet-monad} \Rightarrow ('s, 'r) \text{ nondet-monad} \Rightarrow$
 $('s, 'r) \text{ nondet-monad}$
where
 $condition P L R \equiv \lambda s. if (P s) then (L s) else (R s)$

notation (output)

$condition ((condition (-)// (-)// (-)) [1000,1000,1000] 1000)$

Apply an option valued function to the current state, fail if it returns *None*, return *v* if it returns *Some v*.

definition

$gets-the :: ('s \Rightarrow 'a \text{ option}) \Rightarrow ('s, 'a) \text{ nondet-monad} \textbf{ where}$
 $gets-the f \equiv gets f >>= assert-opt$

Get a map (such as a heap) from the current state and apply an argument to the map. Fail if the map returns *None*, otherwise return the value.

definition

$gets-map :: ('s \Rightarrow 'a \Rightarrow 'b \text{ option}) \Rightarrow 'a \Rightarrow ('s, 'b) \text{ nondet-monad} \textbf{ where}$
 $gets-map f p \equiv gets f >>= (\lambda m. assert-opt (m p))$

13.4 The Monad Laws

A more expanded definition of *bind*

lemma *bind-def'*:

$(f >>= g) \equiv$
 $\lambda s. (\{ (r'', s''). \exists (r', s') \in fst (f s). (r'', s'') \in fst (g r' s') \},$
 $snd (f s) \vee (\exists (r', s') \in fst (f s). snd (g r' s')))$
apply (*rule eq-reflection*)
apply (*auto simp add: bind-def split-def Let-def*)
done

Each monad satisfies at least the following three laws.

return is absorbed at the left of a $(>>=)$, applying the return value directly:

lemma *return-bind* [simp]: (return x $>>=$ f) = f x
by (simp add: return-def bind-def)

return is absorbed on the right of a ($>>=$)

lemma *bind-return* [simp]: (m $>>=$ return) = m
apply (rule ext)
apply (simp add: bind-def return-def split-def)
done

($>>=$) is associative

lemma *bind-assoc*:
fixes $m :: ('a, 'b)$ nondet-monad
fixes $f :: 'b \Rightarrow ('a, 'c)$ nondet-monad
fixes $g :: 'c \Rightarrow ('a, 'd)$ nondet-monad
shows (m $>>=$ f) $>>=$ g = m $>>=$ ($\lambda x. f$ x $>>=$ g)
apply (unfold bind-def Let-def split-def)
apply (rule ext)
apply clarsimp
apply (auto intro: rev-image-eqI)
done

14 Adding Exceptions

The type ($'s, 'a$) *nondet-monad* gives us nondeterminism and failure. We now extend this monad with exceptional return values that abort normal execution, but can be handled explicitly. We use the sum type to indicate exceptions.

In ($'s, 'e + 'a$) *nondet-monad*, $'s$ is the state, $'e$ is an exception, and $'a$ is a normal return value.

This new type itself forms a monad again. Since type classes in Isabelle are not powerful enough to express the class of monads, we provide new names for the *return* and ($>>=$) functions in this monad. We call them *returnOk* (for normal return values) and *bindE* (for composition). We also define *throwError* to return an exceptional value.

definition

returnOk :: $'a \Rightarrow ('s, 'e + 'a)$ nondet-monad **where**
returnOk \equiv return o Inr

definition

throwError :: $'e \Rightarrow ('s, 'e + 'a)$ nondet-monad **where**
throwError \equiv return o Inl

Lifting a function over the exception type: if the input is an exception, return that exception; otherwise continue execution.

definition

$lift :: ('a \Rightarrow ('s, 'e + 'b) nondet-monad) \Rightarrow$
 $'e + 'a \Rightarrow ('s, 'e + 'b) nondet-monad$

where

$lift\ f\ v \equiv case\ v\ of\ Inl\ e \Rightarrow throwError\ e$
 $\quad\quad\quad | Inr\ v' \Rightarrow f\ v'$

The definition of ($>>=$) in the exception monad (new name *bindE*): the same as normal ($>>=$), but the right-hand side is skipped if the left-hand side produced an exception.

definition

$bindE :: ('s, 'e + 'a) nondet-monad \Rightarrow$
 $'a \Rightarrow ('s, 'e + 'b) nondet-monad \Rightarrow$
 $('s, 'e + 'b) nondet-monad\ (infixl\ >>=E\ 60)$

where

$bindE\ f\ g \equiv bind\ f\ (lift\ g)$

Lifting a normal nondeterministic monad into the exception monad is achieved by always returning its result as normal result and never throwing an exception.

definition

$liftE :: ('s, 'a) nondet-monad \Rightarrow ('s, 'e + 'a) nondet-monad$

where

$liftE\ f \equiv f\ >>= (\lambda r. return\ (Inr\ r))$

Since the underlying type and *return* function changed, we need new definitions for *when* and *unless*:

definition

$whenE :: bool \Rightarrow ('s, 'e + unit) nondet-monad \Rightarrow$
 $('s, 'e + unit) nondet-monad$

where

$whenE\ P\ f \equiv if\ P\ then\ f\ else\ returnOk\ ()$

definition

$unlessE :: bool \Rightarrow ('s, 'e + unit) nondet-monad \Rightarrow$
 $('s, 'e + unit) nondet-monad$

where

$unlessE\ P\ f \equiv if\ P\ then\ returnOk\ ()\ else\ f$

Throwing an exception when the parameter is *None*, otherwise returning *v* for *Some v*.

definition

$throw-opt :: 'e \Rightarrow 'a\ option \Rightarrow ('s, 'e + 'a) nondet-monad\ \mathbf{where}$
 $throw-opt\ ex\ x \equiv$
 $case\ x\ of\ None \Rightarrow throwError\ ex\ | Some\ v \Rightarrow returnOk\ v$

Failure in the exception monad is redefined in the same way as *whenE* and *unlessE*, with *returnOk* instead of *return*.

definition

$\text{assert}E :: \text{bool} \Rightarrow ('a, 'e + \text{unit}) \text{ nondet-monad}$ **where**
 $\text{assert}E P \equiv \text{if } P \text{ then } \text{returnOk } () \text{ else fail}$

14.1 Monad Laws for the Exception Monad

More direct definition of $\text{lift}E$:

lemma liftE-def2 :

$\text{lift}E f = (\lambda s. ((\lambda(v,s'). (\text{Inr } v, s')) ' \text{fst } (f s), \text{snd } (f s))))$
by (*auto simp: liftE-def return-def split-def bind-def*)

Left returnOk absorption over $(>>=E)$:

lemma returnOk-bindE [*simp*]: $(\text{returnOk } x >>=E f) = f x$
apply (*unfold bindE-def returnOk-def*)
apply (*clarsimp simp: lift-def*)
done

lemma lift-return [*simp*]:

$\text{lift } (\text{return} \circ \text{Inr}) = \text{return}$
by (*rule ext*)
(simp add: lift-def throwError-def split: sum.splits)

Right returnOk absorption over $(>>=E)$:

lemma bindE-returnOk [*simp*]: $(m >>=E \text{returnOk}) = m$
by (*simp add: bindE-def returnOk-def*)

Associativity of $(>>=E)$:

lemma bindE-assoc :

$(m >>=E f) >>=E g = m >>=E (\lambda x. f x >>=E g)$
apply (*simp add: bindE-def bind-assoc*)
apply (*rule arg-cong [where f= $\lambda x. m >>=E x$]*)
apply (*rule ext*)
apply (*case-tac x, simp-all add: lift-def throwError-def*)
done

returnOk could also be defined via $\text{lift}E$:

lemma returnOk-liftE :

$\text{returnOk } x = \text{lift}E (\text{return } x)$
by (*simp add: liftE-def returnOk-def*)

Execution after throwing an exception is skipped:

lemma throwError-bindE [*simp*]:

$(\text{throwError } E >>=E f) = \text{throwError } E$
by (*simp add: bindE-def bind-def throwError-def lift-def return-def*)

15 Syntax

This section defines traditional Haskell-like do-syntax for the state monad in Isabelle.

15.1 Syntax for the Nondeterministic State Monad

We use *K-bind* to syntactically indicate the case where the return argument of the left side of a ($>>=$) is ignored

definition

K-bind-def [iff]: $K\text{-bind} \equiv \lambda x y. x$

nonterminal

dobinds and *dobind* and *nobind*

syntax

$\text{-dobind} \quad :: [pttrn, 'a] \Rightarrow \text{dobind} \quad ((- \leftarrow / -) 10)$
 $\quad \quad \quad :: \text{dobind} \Rightarrow \text{dobinds} \quad (-)$
 $\text{-nobind} \quad :: 'a \Rightarrow \text{dobind} \quad (-)$
 $\text{-dobinds} \quad :: [\text{dobind}, \text{dobinds}] \Rightarrow \text{dobinds} \quad ((-);/(-))$

 $\text{-do} \quad \quad :: [\text{dobinds}, 'a] \Rightarrow 'a \quad ((\text{do } ((-);/(-))/\text{od}) 100)$
syntax (*xsymbols*)
 $\text{-dobind} \quad :: [pttrn, 'a] \Rightarrow \text{dobind} \quad ((- \leftarrow / -) 10)$

translations

$\text{-do } (\text{-dobinds } b \text{ bs}) \text{ } e \quad == \text{-do } b \text{ } (\text{-do } bs \text{ } e)$
 $\text{-do } (\text{-nobind } b) \text{ } e \quad == b >>= (\text{CONST } K\text{-bind } e)$
 $\text{do } x \leftarrow a; e \text{ od} \quad == a >>= (\lambda x. e)$

Syntax examples:

lemma $\text{do } x \leftarrow \text{return } 1;$
 $\quad \text{return } (2::\text{nat});$
 $\quad \text{return } x$
 $\text{od} =$
 $\text{return } 1 >>=$
 $(\lambda x. \text{return } (2::\text{nat}) >>=$
 $\quad K\text{-bind } (\text{return } x))$
by (*rule refl*)

lemma $\text{do } x \leftarrow \text{return } 1;$
 $\quad \text{return } 2;$
 $\quad \text{return } x$
 $\text{od} = \text{return } 1$
by *simp*

15.2 Syntax for the Exception Monad

Since the exception monad is a different type, we need to syntactically distinguish it in the syntax. We use *doE*/*odE* for this, but can re-use most of the productions from *do*/*od* above.

syntax

-doE :: [*dobinds*, 'a] => 'a ((*doE* ((-);/(-))/odE) 100)

translations

-doE (*-dobinds* b bs) e == *-doE* b (*-doE* bs e)
-doE (*-nobind* b) e == b >>=E (CONST *K-bind* e)
doE x <- a; e *odE* == a >>=E (λx. e)

Syntax examples:

lemma *doE* x ← *returnOk* 1;
 returnOk (2::nat);
 returnOk x
odE =
returnOk 1 >>=E
(λx. *returnOk* (2::nat) >>=E
 K-bind (*returnOk* x))
by (*rule refl*)

lemma *doE* x ← *returnOk* 1;
 returnOk 2;
 returnOk x
odE = *returnOk* 1
by *simp*

16 Library of Monadic Functions and Combinators

Lifting a normal function into the monad type:

definition

liftM :: ('a ⇒ 'b) ⇒ ('s, 'a) *nondet-monad* ⇒ ('s, 'b) *nondet-monad*

where

liftM f m ≡ *do* x ← m; *return* (f x) *od*

The same for the exception monad:

definition

liftME :: ('a ⇒ 'b) ⇒ ('s, 'e+'a) *nondet-monad* ⇒ ('s, 'e+'b) *nondet-monad*

where

liftME f m ≡ *doE* x ← m; *returnOk* (f x) *odE*

Run a sequence of monads from left to right, ignoring return values.

definition

sequence-x :: ('s, 'a) nondet-monad list ⇒ ('s, unit) nondet-monad
where
sequence-x xs ≡ foldr (λx y. x >>= (λ-. y)) xs (return ())

Map a monadic function over a list by applying it to each element of the list from left to right, ignoring return values.

definition

mapM-x :: ('a ⇒ ('s, 'b) nondet-monad) ⇒ 'a list ⇒ ('s, unit) nondet-monad
where
mapM-x f xs ≡ *sequence-x* (map f xs)

Map a monadic function with two parameters over two lists, going through both lists simultaneously, left to right, ignoring return values.

definition

zipWithM-x :: ('a ⇒ 'b ⇒ ('s, 'c) nondet-monad) ⇒
'a list ⇒ 'b list ⇒ ('s, unit) nondet-monad
where
zipWithM-x f xs ys ≡ *sequence-x* (zipWith f xs ys)

The same three functions as above, but returning a list of return values instead of *unit*

definition

sequence :: ('s, 'a) nondet-monad list ⇒ ('s, 'a list) nondet-monad
where
sequence xs ≡ let mcons = (λp q. p >>= (λx. q >>= (λy. return (x#y))))
in foldr mcons xs (return [])

definition

mapM :: ('a ⇒ ('s, 'b) nondet-monad) ⇒ 'a list ⇒ ('s, 'b list) nondet-monad
where
mapM f xs ≡ *sequence* (map f xs)

definition

zipWithM :: ('a ⇒ 'b ⇒ ('s, 'c) nondet-monad) ⇒
'a list ⇒ 'b list ⇒ ('s, 'c list) nondet-monad
where
zipWithM f xs ys ≡ *sequence* (zipWith f xs ys)

definition

foldM :: ('b ⇒ 'a ⇒ ('s, 'a) nondet-monad) ⇒ 'b list ⇒ 'a ⇒ ('s, 'a) nondet-monad
where
foldM m xs a ≡ foldr (λp q. q >>= m p) xs (return a)

definition

foldME :: ('b ⇒ 'a ⇒ ('s, ('e + 'b)) nondet-monad) ⇒ 'b ⇒ 'a list ⇒ ('s, ('e + 'b)) nondet-monad
where *foldME* m a xs ≡ foldr (λp q. q >>=E swp m p) xs (returnOk a)

The sequence and map functions above for the exception monad, with and without lists of return value

definition

$sequenceE\text{-}x :: ('s, 'e + 'a) \text{ nondet-monad list} \Rightarrow ('s, 'e + \text{unit}) \text{ nondet-monad}$

where

$sequenceE\text{-}x \text{ xs} \equiv \text{foldr } (\lambda x \ y. \text{doE } - <- x; y \text{ odE}) \text{ xs } (\text{returnOk } ())$

definition

$mapME\text{-}x :: ('a \Rightarrow ('s, 'e + 'b) \text{ nondet-monad}) \Rightarrow 'a \text{ list} \Rightarrow ('s, 'e + \text{unit}) \text{ nondet-monad}$

where

$mapME\text{-}x \ f \ \text{xs} \equiv sequenceE\text{-}x \ (\text{map } f \ \text{xs})$

definition

$sequenceE :: ('s, 'e + 'a) \text{ nondet-monad list} \Rightarrow ('s, 'e + 'a \text{ list}) \text{ nondet-monad}$

where

$sequenceE \ \text{xs} \equiv \text{let } mcons = (\lambda p \ q. \ p >>=E \ (\lambda x. \ q >>=E \ (\lambda y. \ \text{returnOk } (x \# y))))$
 $\text{in foldr } mcons \ \text{xs } (\text{returnOk } [])$

definition

$mapME :: ('a \Rightarrow ('s, 'e + 'b) \text{ nondet-monad}) \Rightarrow 'a \text{ list} \Rightarrow ('s, 'e + 'b \text{ list}) \text{ nondet-monad}$

where

$mapME \ f \ \text{xs} \equiv sequenceE \ (\text{map } f \ \text{xs})$

Filtering a list using a monadic function as predicate:

primrec

$filterM :: ('a \Rightarrow ('s, \text{bool}) \text{ nondet-monad}) \Rightarrow 'a \text{ list} \Rightarrow ('s, 'a \text{ list}) \text{ nondet-monad}$

where

$filterM \ P \ [] = \text{return } []$
 $| \ filterM \ P \ (x \# \text{xs}) = \text{do}$
 $\quad b <- P \ x;$
 $\quad ys <- filterM \ P \ \text{xs};$
 $\quad \text{return } (\text{if } b \text{ then } (x \# ys) \text{ else } ys)$
 od

17 Catching and Handling Exceptions

Turning an exception monad into a normal state monad by catching and handling any potential exceptions:

definition

$catch :: ('s, 'e + 'a) \text{ nondet-monad} \Rightarrow$
 $\quad ('e \Rightarrow ('s, 'a) \text{ nondet-monad}) \Rightarrow$
 $\quad ('s, 'a) \text{ nondet-monad } (\text{infix } <catch> \ 10)$

where

$f <catch> \ \text{handler} \equiv$

```

do x ← f;
  case x of
    Inr b ⇒ return b
  | Inl e ⇒ handler e
od

```

Handling exceptions, but staying in the exception monad. The handler may throw a type of exceptions different from the left side.

definition

$$\begin{aligned} \text{handleE}' :: ('s, 'e1 + 'a) \text{ nondet-monad} \Rightarrow \\ ('e1 \Rightarrow ('s, 'e2 + 'a) \text{ nondet-monad}) \Rightarrow \\ ('s, 'e2 + 'a) \text{ nondet-monad} \text{ (infix } <\text{handle2}> \text{ } 10) \end{aligned}$$

where

```

f <handle2> handler ≡
do
  v ← f;
  case v of
    Inl e ⇒ handler e
  | Inr v' ⇒ return (Inr v')
od

```

A type restriction of the above that is used more commonly in practice: the exception handle (potentially) throws exception of the same type as the left-hand side.

definition

$$\begin{aligned} \text{handleE} :: ('s, 'x + 'a) \text{ nondet-monad} \Rightarrow \\ ('x \Rightarrow ('s, 'x + 'a) \text{ nondet-monad}) \Rightarrow \\ ('s, 'x + 'a) \text{ nondet-monad} \text{ (infix } <\text{handle}> \text{ } 10) \end{aligned}$$

where

$$\text{handleE} \equiv \text{handleE}'$$

Handling exceptions, and additionally providing a continuation if the left-hand side throws no exception:

definition

$$\begin{aligned} \text{handle-elseE} :: ('s, 'e + 'a) \text{ nondet-monad} \Rightarrow \\ ('e \Rightarrow ('s, 'ee + 'b) \text{ nondet-monad}) \Rightarrow \\ ('a \Rightarrow ('s, 'ee + 'b) \text{ nondet-monad}) \Rightarrow \\ ('s, 'ee + 'b) \text{ nondet-monad} \\ (- <\text{handle}> - <\text{else}> - 10) \end{aligned}$$

where

```

f <handle> handler <else> continue ≡
do v ← f;
  case v of Inl e ⇒ handler e
  | Inr v' ⇒ continue v'
od

```

17.1 Loops

Loops are handled using the following inductive predicate; non-termination is represented using the failure flag of the monad.

inductive-set

$whileLoop\text{-}results :: ('r \Rightarrow 's \Rightarrow bool) \Rightarrow ('r \Rightarrow ('s, 'r) \text{ nondet-monad}) \Rightarrow (((('r \times 's) \text{ option}) \times (('r \times 's) \text{ option})) \text{ set}$

for $C B$

where

$\llbracket \neg C r s \rrbracket \Longrightarrow (Some (r, s), Some (r, s)) \in whileLoop\text{-}results C B$
 $\mid \llbracket C r s; snd (B r s) \rrbracket \Longrightarrow (Some (r, s), None) \in whileLoop\text{-}results C B$
 $\mid \llbracket C r s; (r', s') \in fst (B r s); (Some (r', s'), z) \in whileLoop\text{-}results C B \rrbracket$
 $\Longrightarrow (Some (r, s), z) \in whileLoop\text{-}results C B$

inductive-cases $whileLoop\text{-}results\text{-}cases\text{-}valid: (Some x, Some y) \in whileLoop\text{-}results C B$

inductive-cases $whileLoop\text{-}results\text{-}cases\text{-}fail: (Some x, None) \in whileLoop\text{-}results C B$

inductive-simps $whileLoop\text{-}results\text{-}simps: (Some x, y) \in whileLoop\text{-}results C B$

inductive-simps $whileLoop\text{-}results\text{-}simps\text{-}valid: (Some x, Some y) \in whileLoop\text{-}results C B$

inductive-simps $whileLoop\text{-}results\text{-}simps\text{-}start\text{-}fail [simp]: (None, x) \in whileLoop\text{-}results C B$

inductive

$whileLoop\text{-}terminates :: ('r \Rightarrow 's \Rightarrow bool) \Rightarrow ('r \Rightarrow ('s, 'r) \text{ nondet-monad}) \Rightarrow 'r \Rightarrow 's \Rightarrow bool$

for $C B$

where

$\neg C r s \Longrightarrow whileLoop\text{-}terminates C B r s$
 $\mid \llbracket C r s; \forall (r', s') \in fst (B r s). whileLoop\text{-}terminates C B r' s' \rrbracket$
 $\Longrightarrow whileLoop\text{-}terminates C B r s$

inductive-cases $whileLoop\text{-}terminates\text{-}cases: whileLoop\text{-}terminates C B r s$

inductive-simps $whileLoop\text{-}terminates\text{-}simps: whileLoop\text{-}terminates C B r s$

definition

$whileLoop C B \equiv (\lambda r s.$
 $\{ (r', s'). (Some (r, s), Some (r', s')) \in whileLoop\text{-}results C B \},$
 $(Some (r, s), None) \in whileLoop\text{-}results C B \vee (\neg whileLoop\text{-}terminates C B r s)))$

notation (output)

$whileLoop ((whileLoop (-) // (-)) [1000, 1000] 1000)$

definition

$whileLoopE :: ('r \Rightarrow 's \Rightarrow bool) \Rightarrow ('r \Rightarrow ('s, 'e + 'r) \text{ nondet-monad})$
 $\Rightarrow 'r \Rightarrow 's \Rightarrow (('e + 'r) \times 's) \text{ set} \times bool$

where

$whileLoopE\ C\ body \equiv$
 $\lambda r. whileLoop\ (\lambda r\ s. (case\ r\ of\ Inr\ v \Rightarrow C\ v\ s\ |\ - \Rightarrow False))\ (lift\ body)\ (Inr\ r)$

notation (output)

$whileLoopE\ ((whileLoopE\ (-)//\ (-))\ [1000,\ 1000]\ 1000)$

18 Hoare Logic

18.1 Validity

This section defines a Hoare logic for partial correctness for the nondeterministic state monad as well as the exception monad. The logic talks only about the behaviour part of the monad and ignores the failure flag.

The logic is defined semantically. Rules work directly on the validity predicate.

In the nondeterministic state monad, validity is a triple of precondition, monad, and postcondition. The precondition is a function from state to bool (a state predicate), the postcondition is a function from return value to state to bool. A triple is valid if for all states that satisfy the precondition, all result values and result states that are returned by the monad satisfy the postcondition. Note that if the computation returns the empty set, the triple is trivially valid. This means *assert P* does not require us to prove that *P* holds, but rather allows us to assume *P*! Proving non-failure is done via separate predicate and calculus (see below).

definition

$valid :: ('s \Rightarrow bool) \Rightarrow ('s, 'a)\ nondet-monad \Rightarrow ('a \Rightarrow 's \Rightarrow bool) \Rightarrow bool$
 $(\{\!\{-}\!\} / - / \{\!\{-}\!\})$

where

$\{\!\{P}\!\}\ f\ \{\!\{Q}\!\} \equiv \forall s. P\ s \longrightarrow (\forall (r, s') \in fst\ (f\ s). Q\ r\ s')$

We often reason about invariant predicates. The following provides shorthand syntax that avoids repeating potentially long predicates.

abbreviation (input)

$invariant :: ('s, 'a)\ nondet-monad \Rightarrow ('s \Rightarrow bool) \Rightarrow bool\ (-\ \{\!\{-}\!\}\ [59,0]\ 60)$

where

$invariant\ f\ P \equiv \{\!\{P}\!\}\ f\ \{\!\{\lambda -. P\}\!\}$

Validity for the exception monad is similar and build on the standard validity above. Instead of one postcondition, we have two: one for normal and one for exceptional results.

definition

$validE :: ('s \Rightarrow bool) \Rightarrow ('s, 'a + 'b)\ nondet-monad \Rightarrow$
 $('b \Rightarrow 's \Rightarrow bool) \Rightarrow$
 $('a \Rightarrow 's \Rightarrow bool) \Rightarrow bool$
 $(\{\!\{-}\!\} / - / (\{\!\{-}\!\} / \{\!\{-}\!\}))$

where

$$\{P\} f \{Q\}, \{E\} \equiv \{P\} f \{ \lambda v s. \text{case } v \text{ of } \text{Inr } r \Rightarrow Q \ r \ s \mid \text{Inl } e \Rightarrow E \ e \ s \}$$

The following two instantiations are convenient to separate reasoning for exceptional and normal case.

definition

$$\begin{aligned} \text{validE-R} &:: ('s \Rightarrow \text{bool}) \Rightarrow ('s, 'e + 'a) \text{ nondet-monad} \Rightarrow \\ &\quad ('a \Rightarrow 's \Rightarrow \text{bool}) \Rightarrow \text{bool} \\ &\quad (\{ \cdot \} / - / \{ \cdot \}, -) \end{aligned}$$

where

$$\{P\} f \{Q\}, - \equiv \text{validE } P f Q (\lambda x y. \text{True})$$

definition

$$\begin{aligned} \text{validE-E} &:: ('s \Rightarrow \text{bool}) \Rightarrow ('s, 'e + 'a) \text{ nondet-monad} \Rightarrow \\ &\quad ('e \Rightarrow 's \Rightarrow \text{bool}) \Rightarrow \text{bool} \\ &\quad (\{ \cdot \} / - / -, \{ \cdot \}) \end{aligned}$$

where

$$\{P\} f -, \{Q\} \equiv \text{validE } P f (\lambda x y. \text{True}) Q$$

Abbreviations for trivial preconditions:

abbreviation(*input*)

$$\text{top} :: 'a \Rightarrow \text{bool} \ (\top)$$

where

$$\top \equiv \lambda -. \text{True}$$

abbreviation(*input*)

$$\text{bottom} :: 'a \Rightarrow \text{bool} \ (\perp)$$

where

$$\perp \equiv \lambda -. \text{False}$$

Abbreviations for trivial postconditions (taking two arguments):

abbreviation(*input*)

$$\text{toptop} :: 'a \Rightarrow 'b \Rightarrow \text{bool} \ (\top\top)$$

where

$$\top\top \equiv \lambda - -. \text{True}$$

abbreviation(*input*)

$$\text{botbot} :: 'a \Rightarrow 'b \Rightarrow \text{bool} \ (\perp\perp)$$

where

$$\perp\perp \equiv \lambda - -. \text{False}$$

Lifting \wedge and \vee over two arguments. Lifting \wedge and \vee over one argument is already defined (written *and* and *or*).

definition

$$\begin{aligned} \text{bipred-conj} &:: ('a \Rightarrow 'b \Rightarrow \text{bool}) \Rightarrow ('a \Rightarrow 'b \Rightarrow \text{bool}) \Rightarrow ('a \Rightarrow 'b \Rightarrow \text{bool}) \\ &\quad (\text{infixl } \text{And } 96) \end{aligned}$$

where

$$\text{bipred-conj } P Q \equiv \lambda x y. P \ x \ y \wedge Q \ x \ y$$

bipred-disj :: (*'a* \Rightarrow *'b* \Rightarrow *bool*) \Rightarrow (*'a* \Rightarrow *'b* \Rightarrow *bool*) \Rightarrow (*'a* \Rightarrow *'b* \Rightarrow *bool*)
(infixl Or 91)

$$\text{bipred-disj } P \ Q \equiv \lambda x \ y. \ P \ x \ y \vee Q \ x \ y$$

A monad of type *nondet-monad* is deterministic iff it returns exactly one state and result and does not fail

$$det :: ('a, 's) \text{ nondet-monad} \Rightarrow bool$$
$$\det f \equiv \forall s. \exists r. f s = (\{r\}, False)$$
$$the-run-state :: ('s, 'a) nondet-monad \Rightarrow 's \Rightarrow 'a \times 's$$

the-run-state $M \equiv \lambda s. \text{THE } s'. \text{fst } (M \ s) = \{s'\}$

With the failure flag, we can formulate non-failure separately from validity. A monad m does not fail under precondition P , if for no start state in that precondition it sets the failure flag.

$$no\text{-}fail :: ('s \Rightarrow bool) \Rightarrow ('s, 'a) \text{ nondet-monad} \Rightarrow bool$$
$$no\text{-}fail\ P\ m \equiv \forall s. P\ s \longrightarrow \neg (snd\ (m\ s))$$

It is often desired to prove non-failure and a Hoare triple simultaneously, as the reasoning is often similar. The following definitions allow such reasoning to take place.

$$\text{validNF} :: ('s \Rightarrow \text{bool}) \Rightarrow ('s, 'a) \text{ nondet-monad} \Rightarrow ('a \Rightarrow 's \Rightarrow \text{bool}) \Rightarrow \text{bool}$$

$$(\{\!\!\{-\}\!\!\} / - / \{\!\!\{-\}\!\!\} !)$$
$$validNF\ P\ f\ Q \equiv valid\ P\ f\ Q \wedge no-fail\ P\ f$$
$$\begin{aligned} \text{validE-NF} :: (& s \Rightarrow \text{bool}) \Rightarrow (& 's, 'a + 'b) \text{ nondet-monad} \Rightarrow \\ & ('b \Rightarrow 's \Rightarrow \text{bool}) \Rightarrow \\ & ('a \Rightarrow 's \Rightarrow \text{bool}) \Rightarrow \text{bool} \\ (& \{\!\!-\!\!\} / - / (\{\!\!-\!\!\}, / \{\!\!-\!\!\}!) \end{aligned}$$

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$$\text{validE-NF } P \text{ f } Q \text{ E} \equiv \text{validE } P \text{ f } Q \text{ E} \wedge \text{no-fail } P \text{ f}$$

lemma *validE-NF-alt-def*:

$$\llbracket P \rrbracket B \llbracket Q \rrbracket, \llbracket E \rrbracket! = \llbracket P \rrbracket B \llbracket \lambda v \text{ s. case } v \text{ of } \text{Inl } e \Rightarrow E \text{ e } s \mid \text{Inr } r \Rightarrow Q \text{ r } s \rrbracket!$$

by (*clarsimp simp: validE-NF-def validE-def validNF-def*)

Usually, well-formed monads constructed from the primitives above will have the following property: if they return an empty set of results, they will have the failure flag set.

definition

$$\text{empty-fail} :: ('s, 'a) \text{ nondet-monad} \Rightarrow \text{bool}$$

where

$$\text{empty-fail } m \equiv \forall s. \text{fst } (m \text{ s}) = \{\} \longrightarrow \text{snd } (m \text{ s})$$

Useful in forcing otherwise unknown executions to have the *empty-fail* property.

definition

$$\text{mk-ef} :: 'a \text{ set} \times \text{bool} \Rightarrow 'a \text{ set} \times \text{bool}$$

where

$$\text{mk-ef } S \equiv (\text{fst } S, \text{fst } S = \{\} \vee \text{snd } S)$$

19 Basic exception reasoning

The following predicates *no-throw* and *no-return* allow reasoning that functions in the exception monad either do no throw an exception or never return normally.

definition *no-throw* $P \text{ A} \equiv \llbracket P \rrbracket A \llbracket \lambda \text{ - } \text{True} \rrbracket, \llbracket \lambda \text{ - } \text{False} \rrbracket$

definition *no-return* $P \text{ A} \equiv \llbracket P \rrbracket A \llbracket \lambda \text{ - } \text{False} \rrbracket, \llbracket \lambda \text{ - } \text{True} \rrbracket$

end

theory *NonDetMonadLemmas*

imports *NonDetMonad*

begin

20 General Lemmas Regarding the Nondeterministic State Monad

20.1 Congruence Rules for the Function Package

lemma *bind-cong[fundef-cong]*:

$$\llbracket f = f'; \bigwedge v \text{ s } s'. (v, s') \in \text{fst } (f' \text{ s}) \Longrightarrow g \text{ v } s' = g' \text{ v } s' \rrbracket \Longrightarrow f >>= g = f' >>= g'$$

apply (*rule ext*)
apply (*auto simp: bind-def Let-def split-def intro: rev-image-eqI*)
done

lemma *bind-apply-cong [fundef-cong]*:
 $\llbracket f\ s = f'\ s'; \bigwedge rv\ st. (rv, st) \in fst\ (f'\ s') \implies g\ rv\ st = g'\ rv\ st \rrbracket$
 $\implies (f\ >>= g)\ s = (f'\ >>= g')\ s'$
apply (*simp add: bind-def*)
apply (*auto simp: split-def intro: SUP-cong [OF refl] intro: rev-image-eqI*)
done

lemma *bindE-cong [fundef-cong]*:
 $\llbracket M = M'; \bigwedge v\ s\ s'. (Inr\ v, s') \in fst\ (M'\ s) \implies N\ v\ s' = N'\ v\ s' \rrbracket \implies bindE$
 $M\ N = bindE\ M'\ N'$
apply (*simp add: bindE-def*)
apply (*rule bind-cong*)
apply (*rule refl*)
apply (*unfold lift-def*)
apply (*case-tac v, simp-all*)
done

lemma *bindE-apply-cong [fundef-cong]*:
 $\llbracket f\ s = f'\ s'; \bigwedge rv\ st. (Inr\ rv, st) \in fst\ (f'\ s') \implies g\ rv\ st = g'\ rv\ st \rrbracket$
 $\implies (f\ >>=E\ g)\ s = (f'\ >>=E\ g')\ s'$
apply (*simp add: bindE-def*)
apply (*rule bind-apply-cong*)
apply *assumption*
apply (*case-tac rv, simp-all add: lift-def*)
done

lemma *K-bind-apply-cong [fundef-cong]*:
 $\llbracket f\ st = f'\ st' \rrbracket \implies K\ bind\ f\ arg\ st = K\ bind\ f'\ arg'\ st'$
by *simp*

lemma *when-apply-cong [fundef-cong]*:
 $\llbracket C = C'; s = s'; C' \implies m\ s' = m'\ s' \rrbracket \implies whenE\ C\ m\ s = whenE\ C'\ m'\ s'$
by (*simp add: whenE-def*)

lemma *unless-apply-cong [fundef-cong]*:
 $\llbracket C = C'; s = s'; \neg C' \implies m\ s' = m'\ s' \rrbracket \implies unlessE\ C\ m\ s = unlessE\ C'\ m'\ s'$
by (*simp add: unlessE-def*)

lemma *whenE-apply-cong [fundef-cong]*:
 $\llbracket C = C'; s = s'; C' \implies m\ s' = m'\ s' \rrbracket \implies whenE\ C\ m\ s = whenE\ C'\ m'\ s'$
by (*simp add: whenE-def*)

lemma *unlessE-apply-cong [fundef-cong]*:
 $\llbracket C = C'; s = s'; \neg C' \implies m\ s' = m'\ s' \rrbracket \implies unlessE\ C\ m\ s = unlessE\ C'\ m'$

s'
by (*simp add: unlessE-def*)

20.2 Simplifying Monads

lemma *nested-bind* [*simp*]:
do x <- do y <- f; return (g y) od; h x od =
do y <- f; h (g y) od
apply (*clarsimp simp add: bind-def*)
apply (*rule ext*)
apply (*clarsimp simp add: Let-def split-def return-def*)
done

lemma *fail-bind* [*simp*]:
fail >>= f = fail
by (*simp add: bind-def fail-def*)

lemma *fail-bindE* [*simp*]:
fail >>=E f = fail
by (*simp add: bindE-def bind-def fail-def*)

lemma *assert-False* [*simp*]:
assert False >>= f = fail
by (*simp add: assert-def*)

lemma *assert-True* [*simp*]:
assert True >>= f = f ()
by (*simp add: assert-def*)

lemma *assertE-False* [*simp*]:
assertE False >>=E f = fail
by (*simp add: assertE-def*)

lemma *assertE-True* [*simp*]:
assertE True >>=E f = f ()
by (*simp add: assertE-def*)

lemma *when-False-bind* [*simp*]:
when False g >>= f = f ()
by (*rule ext*) (*simp add: when-def bind-def return-def*)

lemma *when-True-bind* [*simp*]:
when True g >>= f = g >>= f
by (*simp add: when-def bind-def return-def*)

lemma *whenE-False-bind* [*simp*]:
whenE False g >>=E f = f ()
by (*simp add: whenE-def bindE-def returnOk-def lift-def*)

lemma *whenE-True-bind* [simp]:
whenE True g >>=E f = g >>=E f
by (simp add: whenE-def bindE-def returnOk-def lift-def)

lemma *when-True* [simp]: *when True X = X*
by (clarsimp simp: when-def)

lemma *when-False* [simp]: *when False X = return ()*
by (clarsimp simp: when-def)

lemma *unless-False* [simp]: *unless False X = X*
by (clarsimp simp: unless-def)

lemma *unlessE-False* [simp]: *unlessE False f = f*
unfolding unlessE-def **by** fastforce

lemma *unless-True* [simp]: *unless True X = return ()*
by (clarsimp simp: unless-def)

lemma *unlessE-True* [simp]: *unlessE True f = returnOk ()*
unfolding unlessE-def **by** fastforce

lemma *unlessE-whenE*:
unlessE P = whenE (~P)
by (rule ext)+ (simp add: unlessE-def whenE-def)

lemma *unless-when*:
unless P = when (~P)
by (rule ext)+ (simp add: unless-def when-def)

lemma *gets-to-return* [simp]: *gets (λs. v) = return v*
by (clarsimp simp: gets-def put-def get-def bind-def return-def)

lemma *assert-opt-Some*:
assert-opt (Some x) = return x
by (simp add: assert-opt-def)

lemma *assertE-liftE*:
assertE P = liftE (assert P)
by (simp add: assertE-def assert-def liftE-def returnOk-def)

lemma *liftE-handleE'* [simp]: *((liftE a) <handle2> b) = liftE a*
apply (clarsimp simp: liftE-def handleE'-def)
done

lemma *liftE-handleE* [simp]: *((liftE a) <handle> b) = liftE a*
apply (unfold handleE-def)
apply simp
done

lemma *condition-split*:
 $P \text{ (condition } C \ a \ b \ s) = (((C \ s) \longrightarrow P \ (a \ s)) \wedge (\neg (C \ s) \longrightarrow P \ (b \ s)))$
apply (*clarsimp simp: condition-def*)
done

lemma *condition-split-asm*:
 $P \text{ (condition } C \ a \ b \ s) = (\neg (C \ s \wedge \neg P \ (a \ s)) \vee \neg C \ s \wedge \neg P \ (b \ s))$
apply (*clarsimp simp: condition-def*)
done

lemmas *condition-splits* = *condition-split condition-split-asm*

lemma *condition-true-triv* [*simp*]:
 $\text{condition } (\lambda_. \text{True}) \ A \ B = A$
apply (*rule ext*)
apply (*clarsimp split: condition-splits*)
done

lemma *condition-false-triv* [*simp*]:
 $\text{condition } (\lambda_. \text{False}) \ A \ B = B$
apply (*rule ext*)
apply (*clarsimp split: condition-splits*)
done

lemma *condition-true*: $\llbracket P \ s \rrbracket \Longrightarrow \text{condition } P \ A \ B \ s = A \ s$
apply (*clarsimp simp: condition-def*)
done

lemma *condition-false*: $\llbracket \neg P \ s \rrbracket \Longrightarrow \text{condition } P \ A \ B \ s = B \ s$
apply (*clarsimp simp: condition-def*)
done

lemmas *arg-cong-bind* = *arg-cong2*[**where** *f=bind*]
lemmas *arg-cong-bind1* = *arg-cong-bind*[*OF refl ext*]

21 Low-level monadic reasoning

lemma *monad-eqI* [*intro*]:
 $\llbracket \bigwedge r \ t \ s. (r, t) \in \text{fst } (A \ s) \Longrightarrow (r, t) \in \text{fst } (B \ s);$
 $\bigwedge r \ t \ s. (r, t) \in \text{fst } (B \ s) \Longrightarrow (r, t) \in \text{fst } (A \ s);$
 $\bigwedge x. \text{snd } (A \ x) = \text{snd } (B \ x) \rrbracket$
 $\Longrightarrow (A :: ('s, 'a) \text{ nondet-monad}) = B$
apply (*fastforce intro!: set-eqI prod-eqI*)
done

lemma *monad-state-eqI* [*intro*]:
 $\llbracket \bigwedge r \ t. (r, t) \in \text{fst } (A \ s) \Longrightarrow (r, t) \in \text{fst } (B \ s');$
 $\bigwedge r \ t. (r, t) \in \text{fst } (B \ s') \Longrightarrow (r, t) \in \text{fst } (A \ s);$
done

```

    snd (A s) = snd (B s') ]
 $\implies$  (A :: ('s, 'a) nondet-monad) s = B s'
apply (fastforce intro!: set-eqI prod-eqI)
done

```

21.1 General whileLoop reasoning

definition

```

whileLoop-terminatesE C B  $\equiv$  ( $\lambda r$ .
  whileLoop-terminates ( $\lambda r$  s. case r of Inr v  $\Rightarrow$  C v s | -  $\Rightarrow$  False) (lift B) (Inr
  r))

```

lemma whileLoop-cond-fail:

```

[  $\neg$  C x s ]  $\implies$  (whileLoop C B x s) = (return x s)
apply (auto simp: return-def whileLoop-def
  intro: whileLoop-results.intros
  whileLoop-terminates.intros
  elim!: whileLoop-results.cases)
done

```

lemma whileLoopE-cond-fail:

```

[  $\neg$  C x s ]  $\implies$  (whileLoopE C B x s) = (returnOk x s)
apply (clarsimp simp: whileLoopE-def returnOk-def)
apply (auto intro: whileLoop-cond-fail)
done

```

lemma whileLoop-results-simps-no-move [simp]:

```

shows ((Some x, Some x)  $\in$  whileLoop-results C B) = ( $\neg$  C (fst x) (snd x))
  (is ?LHS x = ?RHS x)
proof (rule iffI)
  assume ?LHS x
  then have ( $\exists a$ . Some x = Some a)  $\longrightarrow$  ?RHS (the (Some x))
  by (induct rule: whileLoop-results.induct, auto)
  thus ?RHS x
  by clarsimp
next
  assume ?RHS x
  thus ?LHS x
  by (metis surjective-pairing whileLoop-results.intros(1))
qed

```

lemma whileLoop-unroll:

```

(whileLoop C B r) = ((condition (C r) (B r  $\geq$  (whileLoop C B)) (return r)))
  (is ?LHS r = ?RHS r)
proof -
  have cond-fail:  $\bigwedge r$  s.  $\neg$  C r s  $\implies$  ?LHS r s = ?RHS r s
  apply (subst whileLoop-cond-fail, simp)
  apply (clarsimp simp: condition-def bind-def return-def)
  done

```



```

have cond-pass:  $\bigwedge r\ s. C\ r\ s \implies \text{whileLoop}\ C\ B\ r\ s = (B\ r\ >>= (\text{whileLoop}\ C\ B))\ s$ 
  apply (rule monad-state-eqI)
  apply (clarsimp simp: whileLoop-def bind-def split-def)
  apply (subst (asm) whileLoop-results-simps-valid)
  apply fastforce
  apply (clarsimp simp: whileLoop-def bind-def split-def)
  apply (subst whileLoop-results.simps)
  apply fastforce
  apply (clarsimp simp: whileLoop-def bind-def split-def)
  apply (subst whileLoop-results.simps)
  apply (subst whileLoop-terminates.simps)
  apply fastforce
  done

show ?thesis
  apply (rule ext)
  apply (metis cond-fail cond-pass condition-def)
  done
qed

```

```

lemma whileLoop-unroll':
   $(\text{whileLoop}\ C\ B\ r) = ((\text{condition}\ (C\ r)\ (B\ r)\ (\text{return}\ r))\ >>= (\text{whileLoop}\ C\ B))$ 
  apply (rule ext)
  apply (subst whileLoop-unroll)
  apply (clarsimp simp: condition-def bind-def return-def split-def)
  apply (subst whileLoop-cond-fail, simp)
  apply (clarsimp simp: return-def)
  done

```

```

lemma whileLoopE-unroll:
   $(\text{whileLoopE}\ C\ B\ r) = ((\text{condition}\ (C\ r)\ (B\ r\ >>=E\ (\text{whileLoopE}\ C\ B))\ (\text{returnOk}\ r)))$ 
  apply (rule ext)
  apply (unfold whileLoopE-def)
  apply (subst whileLoop-unroll)
  apply (clarsimp simp: whileLoopE-def bindE-def returnOk-def split: condition-splits)
  apply (clarsimp simp: lift-def)
  apply (rule-tac f= $\lambda a. (B\ r\ >>= a)\ x$  in arg-cong)
  apply (rule ext)+
  apply (clarsimp simp: lift-def split: sum.splits)
  apply (subst whileLoop-unroll)
  apply (subst condition-false)
  apply fastforce
  apply (clarsimp simp: throwError-def)
  done

```

```

lemma whileLoopE-unroll':
  (whileLoopE C B r) = ((condition (C r) (B r) (returnOk r)) >>= E (whileLoopE
C B))
  apply (rule ext)
  apply (subst whileLoopE-unroll)
  apply (clarsimp simp: condition-def bindE-def bind-def returnOk-def return-def
lift-def split-def)
  apply (subst whileLoopE-cond-fail, simp)
  apply (clarsimp simp: returnOk-def return-def)
  done

```

```

lemma valid-make-schematic-post:
  ( $\forall s0. \llbracket \lambda s. P\ s0\ s \rrbracket f \llbracket \lambda rv\ s. Q\ s0\ rv\ s \rrbracket$ )  $\implies$ 
   $\llbracket \lambda s. \exists s0. P\ s0\ s \wedge (\forall rv\ s'. Q\ s0\ rv\ s' \longrightarrow Q'\ rv\ s') \rrbracket f \llbracket Q' \rrbracket$ 
  by (auto simp add: valid-def no-fail-def split: prod.splits)

```

```

lemma validNF-make-schematic-post:
  ( $\forall s0. \llbracket \lambda s. P\ s0\ s \rrbracket f \llbracket \lambda rv\ s. Q\ s0\ rv\ s \rrbracket!$ )  $\implies$ 
   $\llbracket \lambda s. \exists s0. P\ s0\ s \wedge (\forall rv\ s'. Q\ s0\ rv\ s' \longrightarrow Q'\ rv\ s') \rrbracket f \llbracket Q' \rrbracket!$ 
  by (auto simp add: valid-def validNF-def no-fail-def split: prod.splits)

```

```

lemma validE-make-schematic-post:
  ( $\forall s0. \llbracket \lambda s. P\ s0\ s \rrbracket f \llbracket \lambda rv\ s. Q\ s0\ rv\ s \rrbracket, \llbracket \lambda rv\ s. E\ s0\ rv\ s \rrbracket$ )  $\implies$ 
   $\llbracket \lambda s. \exists s0. P\ s0\ s \wedge (\forall rv\ s'. Q\ s0\ rv\ s' \longrightarrow Q'\ rv\ s') \rrbracket f \llbracket Q' \rrbracket, \llbracket E' \rrbracket$ 
   $\wedge (\forall rv\ s'. E\ s0\ rv\ s' \longrightarrow E'\ rv\ s') \rrbracket f \llbracket Q' \rrbracket, \llbracket E' \rrbracket$ 
  by (auto simp add: validE-def valid-def no-fail-def split: prod.splits sum.splits)

```

```

lemma validE-NF-make-schematic-post:
  ( $\forall s0. \llbracket \lambda s. P\ s0\ s \rrbracket f \llbracket \lambda rv\ s. Q\ s0\ rv\ s \rrbracket, \llbracket \lambda rv\ s. E\ s0\ rv\ s \rrbracket!$ )  $\implies$ 
   $\llbracket \lambda s. \exists s0. P\ s0\ s \wedge (\forall rv\ s'. Q\ s0\ rv\ s' \longrightarrow Q'\ rv\ s') \rrbracket f \llbracket Q' \rrbracket, \llbracket E' \rrbracket!$ 
   $\wedge (\forall rv\ s'. E\ s0\ rv\ s' \longrightarrow E'\ rv\ s') \rrbracket f \llbracket Q' \rrbracket, \llbracket E' \rrbracket!$ 
  by (auto simp add: validE-NF-def validE-def valid-def no-fail-def split: prod.splits
sum.splits)

```

```

lemma validNF-conjD1:  $\llbracket P \rrbracket f \llbracket \lambda rv\ s. Q\ rv\ s \wedge Q'\ rv\ s \rrbracket! \implies \llbracket P \rrbracket f \llbracket Q \rrbracket!$ 
  by (fastforce simp: validNF-def valid-def no-fail-def)

```

```

lemma validNF-conjD2:  $\llbracket P \rrbracket f \llbracket \lambda rv\ s. Q\ rv\ s \wedge Q'\ rv\ s \rrbracket! \implies \llbracket P \rrbracket f \llbracket Q' \rrbracket!$ 
  by (fastforce simp: validNF-def valid-def no-fail-def)

```

end

```

theory WP-Pre
imports
  Main
  HOL-Eisbach.Eisbach-Tools

```

begin

named-theorems *wp-pre*

ML \langle

structure WP-Pre = struct

fun append-used-thm thm used-thms = used-thms := !used-thms @ [thm]

fun pre-tac ctxt pre-rules used-ref-option i t = let

fun append-thm used-thm thm =

if Option.isSome used-ref-option

then Seq.map (fn thm => (append-used-thm used-thm (Option.valOf used-ref-option);
thm)) thm

else thm;

fun apply-rule t thm = append-thm t (resolve-tac ctxt [t] i thm)

val t2 = FIRST (map apply-rule pre-rules) t |> Seq.hd

val etac = TRY o eresolve-tac ctxt [@{thm FalseE}]

fun dummy-t2 - - = Seq.single t2

val t3 = (dummy-t2 THEN-ALL-NEW etac) i t |> Seq.hd

in if Thm.nprems-of t3 <> Thm.nprems-of t2

then Seq.empty else Seq.single t2 end

handle Option => Seq.empty

fun tac used-ref-option ctxt = let

val pres = Named-Theorems.get ctxt @{named-theorems wp-pre}

in pre-tac ctxt pres used-ref-option end

val method

= Args.context >> (fn - => fn ctxt => Method.SIMPLE-METHOD' (tac
NONE ctxt));

end

\rangle

method-setup *wp-pre0* = \langle *WP-Pre.method* \rangle

method *wp-pre* = *wp-pre0*?

definition

test-wp-pre :: *bool* \Rightarrow *bool* \Rightarrow *bool*

where

test-wp-pre *P Q* = (*P* \longrightarrow *Q*)

lemma *test-wp-pre-pre*[*wp-pre*]:

test-wp-pre *P' Q* \Longrightarrow (*P* \Longrightarrow *P'*)

\Longrightarrow *test-wp-pre* *P Q*

by (*simp add: test-wp-pre-def*)

lemma *demo*:

test-wp-pre *P P*

```

apply wp-pre0+
  apply (simp add: test-wp-pre-def, rule imp-refl)
apply simp
done

```

end

theory *Datatype-Schematic*

imports

```

  ../ml-helpers/MLUtils
  ../ml-helpers/TermPatternAntiquote

```

begin

Introduces a method for improving unification outcomes for schematics with datatype expressions as parameters.

There are two variants: 1. In cases where a schematic is applied to a constant like *True*, we wrap the constant to avoid some undesirable unification candidates.

2. In cases where a schematic is applied to a constructor expression like *Some x* or *(x, y)*, we supply selector expressions like *the* or *fst* to provide more unification candidates. This is only done if parameter that would be selected (e.g. *x* in *Some x*) contains bound variables which the schematic does not have as parameters.

In the "constructor expression" case, we let users supply additional constructor handlers via the 'datatype_schematic' attribute. The method uses rules of the following form :

$$\bigwedge x1\ x2\ x3. \text{getter}(\text{constructor } x1\ x2\ x3) = x2$$

These are essentially simp rules for simple "accessor" primrec functions, which are used to turn schematics like

$$?P(\text{constructor } x1\ x2\ x3)$$

into

$$?P'x2(\text{constructor } x1\ x2\ x3).$$

ML (

— Anchor used to link error messages back to the documentation above.

```

  val usage-pos = @{here};

```

)

definition

$$ds-id :: 'a \Rightarrow 'a$$

where

$$ds-id = (\lambda x. x)$$

lemma *wrap-ds-id*:

$$x = ds-id\ x$$

```

by (simp add: ds-id-def)

ML <
structure Datatype-Schematic = struct

fun eq ((idx1, name1, thm1), (idx2, name2, thm2)) =
  idx1 = idx2 andalso
  name1 = name2 andalso
  (Thm.full-prop-of thm1) aconv (Thm.full-prop-of thm2);

structure Datatype-Schematic-Data = Generic-Data
(
  — Keys are names of datatype constructors (like (#)), values are '(index, functionname, thm)'.
  - 'functionname' is the name of an "accessor" function that accesses part of the constructor specified by the key (so the
  - 'thm' is a theorem showing that the function accesses one of the arguments to the
  constructor (like hd (?x21.0 # ?x22.0) = ?x21.0).
  - 'idx' is the index of the constructor argument that the accessor accesses. (eg. since
  'hd' accesses the first argument, 'idx = 0'; since 'tl' accesses the second argument,
  'idx = 1').
  type T = ((int * string * thm) list) Symtab.table;
  val empty = Symtab.empty;
  val extend = I;
  val merge = Symtab.merge-list eq;
);

fun gen-att m =
  Thm.declaration-attribute (fn thm => fn context =>
    Datatype-Schematic-Data.map (m (Context.proof-of context) thm) context);

(* gathers schematic applications from the goal. no effort is made
   to normalise bound variables here, since we'll always be comparing
   elements within a compound application which will be at the same
   level as regards lambdas. *)
fun gather-schem-apps (f $ x) insts = let
  val (f, xs) = strip-comb (f $ x)
  val insts = fold (gather-schem-apps) (f :: xs) insts
in if is-Var f then (f, xs) :: insts else insts end
| gather-schem-apps (Abs (-, -, t)) insts
  = gather-schem-apps t insts
| gather-schem-apps - insts = insts

fun sfirst xs f = get-first f xs

fun get-action ctxt prop = let
  val schem-insts = gather-schem-apps prop [];
  val actions = Datatype-Schematic-Data.get (Context.Proof ctxt);
  fun mk-sel selname T i = let
    val (argTs, resT) = strip-type T
  in Const (selname, resT --> nth argTs i) end

```

```

in
  sfirst schem-insts
  (fn (var, xs) => sfirst (Library.tag-list 0 xs)
    (try (fn (idx, x) => let
      val (c, ys) = strip-comb x
      val (fname, T) = dest-Const c
      val acts = Syntab.lookup-list actions fname
      fun interesting arg = not (member Term.aconv-untyped xs arg)
      andalso exists (fn i => not (member (=) xs (Bound i)))
      (Term.loose-bnos arg)
      in the (sfirst acts (fn (i, selname, thms) => if interesting (nth ys i)
        then SOME (var, idx, mk-sel selname T i, thms) else NONE))
      end)))
  end
end

fun get-bound-tac ctxt = SUBGOAL (fn (t, i) => case get-action ctxt t of
  SOME (Var ((nm, ix), T), idx, sel, thm) => (fn t => let
    val (argTs, -) = strip-type T
    val ix2 = Thm.maxidx-of t + 1
    val xs = map (fn (i, T) => Free (x ^ string-of-int i, T))
      (Library.tag-list 1 argTs)
    val nx = sel $ nth xs idx
    val v' = Var ((nm, ix2), fastype-of nx --> T)
    val inst-v = fold lambda (rev xs) (betapplys (v' $ nx, xs))
    val t' = Drule.infer-instantiate ctxt
      [((nm, ix), Thm.cterm-of ctxt inst-v)] t
    val t'' = Conv.fconv-rule (Thm.beta-conversion true) t'
  in safe-full-simp-tac (clear-simpset ctxt addsimps [thm]) i t'' end)
  | - => no-tac)

fun id-applicable (f $ x) = let
  val (f, xs) = strip-comb (f $ x)
  val here = is-Var f andalso exists is-Const xs
  in here orelse exists id-applicable (f :: xs) end
  | id-applicable (Abs (-, -, t)) = id-applicable t
  | id-applicable - = false

fun combination-conv cv1 cv2 ct =
  let
    val (ct1, ct2) = Thm.dest-comb ct
    val r1 = SOME (cv1 ct1) handle Option => NONE
    val r2 = SOME (cv2 ct2) handle Option => NONE
    fun mk - (SOME res) = res
      | mk ct NONE = Thm.reflexive ct
  in case (r1, r2) of
    (NONE, NONE) => raise Option
    | - => Thm.combination (mk ct1 r1) (mk ct2 r2)
  end
end

```

```

val wrap = mk-meta-eq @{thm wrap-ds-id}

fun wrap-const-conv - ct = if is-Const (Thm.term-of ct)
    andalso fastype-of (Thm.term-of ct) <> @{typ unit}
    then Conv.rewr-conv wrap ct
    else raise Option

fun combs-conv conv ctxt ct = case Thm.term-of ct of
    - $ - => combination-conv (combs-conv conv ctxt) (conv ctxt) ct
  | - => conv ctxt ct

fun wrap-conv ctxt ct = case Thm.term-of ct of
    Abs - => Conv.sub-conv wrap-conv ctxt ct
  | f $ x => if is-Var (head-of f) then combs-conv wrap-const-conv ctxt ct
    else if not (id-applicable (f $ x)) then raise Option
    else combs-conv wrap-conv ctxt ct
  | - => raise Option

fun CONVERSION-opt conv i t = CONVERSION conv i t
    handle Option => no-tac t

exception Datatype-Schematic-Error of Pretty.T;

fun apply-pos-markup pos text =
    let
        val props = Position.def-properties-of pos;
        val markup = Markup.properties props (Markup.entity );
    in Pretty.mark-str (markup, text) end;

fun invalid-accessor ctxt thm : exn =
    Datatype-Schematic-Error ([
        Pretty.str Bad input theorem ',
        Syntax.pretty-term ctxt (Thm.full-prop-of thm),
        Pretty.str '. Click ',
        apply-pos-markup usage-pos *here*,
        Pretty.str for info on the required rule format. ] |> Pretty.paragraph);

local
    fun dest-accessor' thm =
        case (thm |> Thm.full-prop-of |> HOLogic.dest-Trueprop) of
            @{term-pat ?fun-name ?data-pat = ?rhs} =>
                let
                    val fun-name = Term.dest-Const fun-name |> fst;
                    val (data-const, data-args) = Term.strip-comb data-pat;
                    val data-vars = data-args |> map (Term.dest-Var #> fst);
                    val rhs-var = rhs |> Term.dest-Var |> fst;
                    val data-name = Term.dest-Const data-const |> fst;
                    val rhs-idx = ListExtras.find-index (curry op = rhs-var) data-vars |> the;
                in (fun-name, data-name, rhs-idx) end;
end

```

```

in
  fun dest-accessor ctxt thm =
    case try dest-accessor' thm of
      SOME x => x
    | NONE => raise invalid-accessor ctxt thm;
end

fun add-rule ctxt thm data =
  let
    val (fun-name, data-name, idx) = dest-accessor ctxt thm;
    val entry = (data-name, (idx, fun-name, thm));
  in Symtab.insert-list eq entry data end;

fun del-rule ctxt thm data =
  let
    val (fun-name, data-name, idx) = dest-accessor ctxt thm;
    val entry = (data-name, (idx, fun-name, thm));
  in Symtab.remove-list eq entry data end;

val add = gen-att add-rule;
val del = gen-att del-rule;

fun wrap-tac ctxt = CONVERSION-opt (wrap-conv ctxt)

fun tac1 ctxt = REPEAT-ALL-NEW (get-bound-tac ctxt) THEN' (TRY o wrap-tac
  ctxt)

fun tac ctxt = tac1 ctxt ORELSE' wrap-tac ctxt

val add-section =
  Args.add -- Args.colon >> K (Method.modifier add @ {here});

val method =
  Method.sections [add-section] >> (fn - => fn ctxt => Method.SIMPLE-METHOD'
    (tac ctxt));

end
)

setup (
  Attrib.setup
    @ {binding datatype-schematic}
    (Attrib.add-del Datatype-Schematic.add Datatype-Schematic.del)
    Accessor rules to fix datatypes in schematics
)

method-setup datatype-schem = (
  Datatype-Schematic.method
)

```



```

declare prod.sel[datatype-schematic]
declare option.sel[datatype-schematic]
declare list.sel(1,3)[datatype-schematic]

locale datatype-schem-demo begin

lemma handles-nested-constructors:
   $\exists f. \forall y. f \text{ True } (\text{Some } [x, (y, z)]) = y$ 
  apply (rule exI, rule allI)
  apply datatype-schem
  apply (rule refl)
  done

datatype foo =
  basic nat int
  | another nat

primrec get-basic-0 where
  get-basic-0 (basic x0 x1) = x0

primrec get-nat where
  get-nat (basic x -) = x
  | get-nat (another z) = z

lemma selectively-exposing-datatype-arugments:
  notes get-basic-0.simps[datatype-schematic]
  shows  $\exists x. \forall a b. x \text{ (basic } a \text{ b)} = a$ 
  apply (rule exI, (rule allI)+)
  apply datatype-schem — Only exposes ‘a’ to the schematic.
  by (rule refl)

lemma method-handles-primrecs-with-two-constructors:
  shows  $\exists x. \forall a b. x \text{ (basic } a \text{ b)} = a$ 
  apply (rule exI, (rule allI)+)
  apply (datatype-schem add: get-nat.simps)
  by (rule refl)

end

end

theory Strengthen
imports Main
begin

```

Implementation of the *strengthen* tool and the *mk-strg* attribute. See the theory *Strengthen-Demo* for a demonstration.

locale *strengthen-implementation* **begin**

definition $st\ P\ rel\ x\ y = (x = y \vee (P \wedge rel\ x\ y) \vee (\neg P \wedge rel\ y\ x))$

definition

$st-prop1 :: prop \Rightarrow prop \Rightarrow prop$

where

$st-prop1\ (PROP\ P)\ (PROP\ Q) \equiv (PROP\ Q \Longrightarrow PROP\ P)$

definition

$st-prop2 :: prop \Rightarrow prop \Rightarrow prop$

where

$st-prop2\ (PROP\ P)\ (PROP\ Q) \equiv (PROP\ P \Longrightarrow PROP\ Q)$

definition $failed == True$

definition $elim :: prop \Rightarrow prop$

where

$elim\ (P :: prop) == P$

definition $oblig\ (P :: prop) == P$

end

notation *strengthen-implementation.elim* ($\{elim\} - \{|\}$)

notation *strengthen-implementation.oblig* ($\{oblig\} - \{|\}$)

notation *strengthen-implementation.failed* ($\langle strg-failed \rangle$)

syntax

$-ap-strg-bool :: ['a, 'a] \Rightarrow 'a\ (- =strg<--| \Rightarrow -)$

$-ap-wkn-bool :: ['a, 'a] \Rightarrow 'a\ (- =strg-->| \Rightarrow -)$

$-ap-ge-bool :: ['a, 'a] \Rightarrow 'a\ (- =strg<=| \Rightarrow -)$

$-ap-le-bool :: ['a, 'a] \Rightarrow 'a\ (- =strg>=| \Rightarrow -)$

syntax(*xsymbols*)

$-ap-strg-bool :: ['a, 'a] \Rightarrow 'a\ (- =strg\longleftarrow| \Rightarrow -)$

$-ap-wkn-bool :: ['a, 'a] \Rightarrow 'a\ (- =strg\longrightarrow| \Rightarrow -)$

$-ap-ge-bool :: ['a, 'a] \Rightarrow 'a\ (- =strg\leq| \Rightarrow -)$

$-ap-le-bool :: ['a, 'a] \Rightarrow 'a\ (- =strg\geq| \Rightarrow -)$

translations

$P =strg\longleftarrow| \Rightarrow Q == CONST\ strengthen-implementation.st\ (CONST\ False)$
 $(CONST\ HOL.implies)\ P\ Q$

$P =strg\longrightarrow| \Rightarrow Q == CONST\ strengthen-implementation.st\ (CONST\ True)$
 $(CONST\ HOL.implies)\ P\ Q$

$P =strg\leq| \Rightarrow Q == CONST\ strengthen-implementation.st\ (CONST\ False)$
 $(CONST\ Orderings.less-eq)\ P\ Q$

$P =strg\geq| \Rightarrow Q == CONST\ strengthen-implementation.st\ (CONST\ True)\ (CONST\ Orderings.less-eq)\ P\ Q$

context *strengthen-implementation* **begin**

lemma *failedI*:

<strg-failed>

by (*simp add: failed-def*)

lemma *strengthen-refl*:

st P rel x x

by (*simp add: st-def*)

lemma *st-prop-refl*:

PROP (st-prop1 (PROP P) (PROP P))

PROP (st-prop2 (PROP P) (PROP P))

unfolding *st-prop1-def st-prop2-def*

by *safe*

lemma *strengthenI*:

rel x y \implies st True rel x y

rel y x \implies st False rel x y

by (*simp-all add: st-def*)

lemmas *imp-to-strengthen* = *strengthenI*(2)[**where** *rel*=(\longrightarrow)]

lemmas *rev-imp-to-strengthen* = *strengthenI*(1)[**where** *rel*=(\longrightarrow)]

lemmas *ord-to-strengthen* = *strengthenI*[**where** *rel*=(\leq)]

lemma *use-strengthen-imp*:

st False (\longrightarrow) Q P \implies P \implies Q

by (*simp add: st-def*)

lemma *use-strengthen-prop-elim*:

PROP P \implies PROP (st-prop2 (PROP P) (PROP Q))

\implies (PROP Q \implies PROP R) \implies PROP R

unfolding *st-prop2-def*

apply (*drule*(1) *meta-mp*)+

apply *assumption*

done

lemma *strengthen-Not*:

st False rel x y \implies st (\neg True) rel x y

st True rel x y \implies st (\neg False) rel x y

by *auto*

lemmas *gather* =

swap-prems-eq[**where** *A*=*PROP (Trueprop P)* **and** *B*=*PROP (elim Q)* **for** *P*
Q]

swap-prems-eq[**where** *A*=*PROP (Trueprop P)* **and** *B*=*PROP (oblig Q)* **for** *P*
Q]

lemma *mk-True-imp*:

$P \equiv \text{True} \longrightarrow P$

by *simp*

lemma *narrow-quant*:

$(\bigwedge x. \text{PROP } P \Longrightarrow \text{PROP } (Q \ x)) \equiv (\text{PROP } P \Longrightarrow (\bigwedge x. \text{PROP } (Q \ x)))$

$(\bigwedge x. (R \longrightarrow S \ x)) \equiv \text{PROP } (\text{Trueprop } (R \longrightarrow (\forall x. S \ x)))$

$(\bigwedge x. (S \ x \longrightarrow R)) \equiv \text{PROP } (\text{Trueprop } ((\exists x. S \ x) \longrightarrow R))$

apply (*simp-all add: atomize-all*)

apply *rule*

apply *assumption*

apply *assumption*

done

ML <

structure Make-Strengthen-Rule = struct

fun binop-conv' cv1 cv2 = Conv.combination-conv (Conv.arg-conv cv1) cv2;

val mk-elim = Conv.rewr-conv @{thm elim-def[symmetric]}

val mk-oblig = Conv.rewr-conv @{thm oblig-def[symmetric]}

fun count-vars t = Term.fold-aterms

(fn (Var v) => Termtab.map-default (Var v, 0) (fn x => x + 1)
| - => I) t Termtab.empty

fun gather-to-imp ctxt drule pattern = let

val pattern = (if drule then D :: pattern else pattern)

fun inner pat ct = case (head-of (Thm.term-of ct), pat) of

(@{term Pure.imp}, (E :: pat)) => binop-conv' mk-elim (inner pat) ct

| (@{term Pure.imp}, (A :: pat)) => binop-conv' mk-elim (inner pat) ct

| (@{term Pure.imp}, (O :: pat)) => binop-conv' mk-oblig (inner pat) ct

| (@{term Pure.imp}, -) => binop-conv' (Object-Logic.atomize ctxt) (inner

(drop 1 pat)) ct

| (-, []) => Object-Logic.atomize ctxt ct

| (-, pat) => raise THM (gather-to-imp: leftover pattern: ^ commas pat, 1,

[])

fun simp thms = Raw-Simplifier.rewrite ctxt false thms

fun ensure-imp ct = case strip-comb (Thm.term-of ct) |> apsnd (map head-of)

of

(@{term Pure.imp}, -) => Conv.arg-conv ensure-imp ct

| (@{term HOL.Trueprop}, [@{term HOL.implies}]) => Conv.all-conv ct

| (@{term HOL.Trueprop}, -) => Conv.arg-conv (Conv.rewr-conv @{thm

mk-True-imp}) ct

| - => raise CTERM (gather-to-imp, [ct])

val gather = simp @{thms gather}

then-conv (if drule then Conv.all-conv else simp @{thms atomize-conjL})

then-conv simp @{thms atomize-imp}

then-conv ensure-imp

```

in Conv.fconv-rule (inner pattern then-conv gather) end

fun imp-list t = let
  val (x, y) = Logic.dest-implies t
in x :: imp-list y end handle TERM - => [t]

fun mk-ex (xnm, T) t = HOLLogic.exists-const T $ Term.lambda (Var (xnm, T))
t
fun mk-all (xnm, T) t = HOLLogic.all-const T $ Term.lambda (Var (xnm, T)) t

fun quantify-vars ctxt drule thm = let
  val (lhs, rhs) = Thm.concl-of thm |> HOLLogic.dest-Trueprop
  |> HOLLogic.dest-imp
  val all-vars = count-vars (Thm.prop-of thm)
  val new-vars = count-vars (if drule then rhs else lhs)
  val quant = filter (fn v => Termtab.lookup new-vars v = Termtab.lookup
all-vars v)
  (Termtab.keys new-vars)
  |> map (Thm.ctrm-of ctxt)
in fold Thm.forall-intr quant thm
  |> Conv.fconv-rule (Raw-Simplifier.rewrite ctxt false @ {thms narrow-quant})
end

fun mk-strg (typ, pat) ctxt thm = let
  val drule = typ = D orelse typ = D'
  val imp = gather-to-imp ctxt drule pat thm
  |> (if typ = I' orelse typ = D'
    then quantify-vars ctxt drule else I)
in if typ = I orelse typ = I'
  then imp RS @ {thm imp-to-strengthen}
  else if drule then imp RS @ {thm rev-imp-to-strengthen}
  else if typ = lhs then imp RS @ {thm ord-to-strengthen(1)}
  else if typ = rhs then imp RS @ {thm ord-to-strengthen(2)}
  else raise THM (mk-strg: unknown type: ^ typ, 1, [thm])
end

fun auto-mk ctxt thm = let
  val concl-C = try (fst o dest-Const o head-of
    o HOLLogic.dest-Trueprop) (Thm.concl-of thm)
in case (Thm.nprems-of thm, concl-C) of
  (_, SOME @ {const-name failed}) => thm
| (_, SOME @ {const-name st}) => thm
| (0, SOME @ {const-name HOL.implies}) => (thm RS @ {thm imp-to-strengthen}
  handle THM - => @ {thm failedI})
| - => mk-strg (I', []) ctxt thm
end

fun mk-strg-args (SOME (typ, pat)) ctxt thm = mk-strg (typ, pat) ctxt thm
| mk-strg-args NONE ctxt thm = auto-mk ctxt thm

```

```

val arg-pars = Scan.option (Scan.first (map Args.$$$ [I, I', D, D', lhs, rhs])
  -- Scan.repeat (Args.$$$ A || Args.$$$ E || Args.$$$ O || Args.$$$ -))

val attr-pars : attribute context-parser
  = (Scan.lift arg-pars -- Args.context)
    >> (fn (args, ctxt) => Thm.rule-attribute [] (K (mk-strg-args args ctxt)))

end
)

end

attribute-setup mk-strg = ⟨Make-Strengthen-Rule.attr-pars⟩
  put rule in 'strengthen' form (see theory Strengthen-Demo)

Quick test.

lemmas foo = nat.induct[mk-strg I O O]
  nat.induct[mk-strg D O]
  nat.induct[mk-strg I' E]
  exI[mk-strg I] exI[mk-strg I]

context strengthen-implementation begin

lemma do-elim:
  PROP P ⇒ PROP elim (PROP P)
  by (simp add: elim-def)

lemma intro-oblig:
  PROP P ⇒ PROP oblig (PROP P)
  by (simp add: oblig-def)

ML ⟨

structure Strengthen = struct

structure Congs = Theory-Data
(struct
  type T = thm list
  val empty = []
  val extend = I
  val merge = Thm.merge-thms;
end);

val tracing = Attrib.config-bool @{binding strengthen-trace} (K false)

fun map-context-total f (Context.Theory t) = (Context.Theory (f t))
  | map-context-total f (Context.Proof p)

```

```

= (Context.Proof (Context.raw-transfer (f (Proof-Context.theory-of p)) p))

val strg-add = Thm.declaration-attribute
  (fn thm => map-context-total (Congs.map (Thm.add-thm thm)));

val strg-del = Thm.declaration-attribute
  (fn thm => map-context-total (Congs.map (Thm.del-thm thm)));

val setup =
  Attrib.setup @{binding strg} (Attrib.add-del strg-add strg-del)
  strengthening congruence rules
  #> snd tracing;

fun goal-predicate t = let
  val gl = Logic.strip-assums-concl t
  val cn = head-of #> dest-Const #> fst
  in if cn gl = @{const-name oblig} then oblig
    else if cn gl = @{const-name elim} then elim
    else if cn gl = @{const-name st-prop1} then st-prop1
    else if cn gl = @{const-name st-prop2} then st-prop2
    else if cn (HOLogic.dest-Trueprop gl) = @{const-name st} then st
    else
  end handle TERM - =>

fun do-elim ctxt = SUBGOAL (fn (t, i) => if goal-predicate t = elim
  then eresolve-tac ctxt @{thms do-elim} i else all-tac)

fun final-oblig-strengthen ctxt = SUBGOAL (fn (t, i) => case goal-predicate t of
  oblig => resolve-tac ctxt @{thms intro-oblig} i
  | st => resolve-tac ctxt @{thms strengthen-refl} i
  | st-prop1 => resolve-tac ctxt @{thms st-prop-refl} i
  | st-prop2 => resolve-tac ctxt @{thms st-prop-refl} i
  | - => all-tac)

infix 1 THEN-TRY-ALL-NEW;

(* Like THEN-ALL-NEW but allows failure, although at least one subsequent
   method must succeed. *)
fun (tac1 THEN-TRY-ALL-NEW tac2) i st = let
  fun inner b j st = if i > j then (if b then all-tac else no-tac) st
    else ((tac2 j THEN inner true (j - 1)) ORELSE inner b (j - 1)) st
  in st |> (tac1 i THEN (fn st' =>
    inner false (i + Thm.nprems-of st' - Thm.nprems-of st) st')) end

fun maybe-trace-tac false - - = K all-tac
  | maybe-trace-tac true ctxt msg = SUBGOAL (fn (t, -) => let
    val tr = Pretty.big-list msg [Syntax.pretty-term ctxt t]
  in
    Pretty.writeln tr;

```

```

    all-tac
  end)

fun maybe-trace-rule false - - rl = rl
| maybe-trace-rule true ctxt msg rl = let
  val tr = Pretty.big-list msg [Syntax.pretty-term ctxt (Thm.prop-of rl)]
in
  Pretty.writeln tr;
  rl
end

type params = {trace : bool, once : bool}

fun params once ctxt = {trace = Config.get ctxt (fst tracing), once = once}

fun apply-tac-as-strg ctxt (params : params) (tac : tactic)
= SUBGOAL (fn (t, i) => case Logic.strip-assums-concl t of
  @ {term Trueprop} $ (@ {term st False (⟶)}) $ x $ -)
=> let
  val triv = Thm.trivial (Thm.cterm-of ctxt (HOLogic.mk-Trueprop x))
  val trace = #trace params
in
  fn thm => tac triv
  |> Seq.map (maybe-trace-rule trace ctxt apply-tac-as-strg: making strg)
  |> Seq.maps (Seq.try (Make-Strengthen-Rule.auto-mk ctxt))
  |> Seq.maps (fn str-rl => resolve-tac ctxt [str-rl] i thm)
end | - => no-tac)

fun opt-tac f (SOME v) = f v
| opt-tac - NONE = K no-tac

fun apply-strg ctxt (params : params) congs rules tac = EVERY' [
  maybe-trace-tac (#trace params) ctxt apply-strg,
  DETERM o TRY o resolve-tac ctxt @ {thms strengthen-Not},
  DETERM o ((resolve-tac ctxt rules THEN-ALL-NEW do-elim ctxt)
    OR ELSE' (opt-tac (apply-tac-as-strg ctxt params) tac)
    OR ELSE' (resolve-tac ctxt congs THEN-TRY-ALL-NEW
      (fn i => apply-strg ctxt params congs rules tac i)))
]

fun setup-strg ctxt params thms meths = let
  val congs = Congs.get (Proof-Context.theory-of ctxt)
  val rules = map (Make-Strengthen-Rule.auto-mk ctxt) thms
  val tac = case meths of [] => NONE
  | - => SOME (FIRST (map (fn meth => Method.NO-CONTEXT-TACTIC
    ctxt
    (Method.evaluate meth ctxt [])) meths))
in apply-strg ctxt params congs rules tac
  THEN-ALL-NEW final-oblig-strengthen ctxt end

```



```

fun strengthen ctxt asm concl thms meths = let
  val strg = setup-strg ctxt (params false ctxt) thms meths
in
  (if not concl then K no-tac
   else resolve-tac ctxt @ {thms use-strengthen-imp} THEN' strg)
  ORELSE' (if not asm then K no-tac
   else eresolve-tac ctxt @ {thms use-strengthen-prop-elim} THEN' strg)
end

fun default-strengthen ctxt thms = strengthen ctxt false true thms []

val strengthen-args =
  Attrib.thms >> curry (fn (rules, ctxt) =>
    Method.CONTEXT-METHOD (fn - =>
      Method.RUNTIME (Method.CONTEXT-TACTIC
        (strengthen ctxt false true rules [] 1))
      )
    );

val strengthen-asm-args =
  Attrib.thms >> curry (fn (rules, ctxt) =>
    Method.CONTEXT-METHOD (fn - =>
      Method.RUNTIME (Method.CONTEXT-TACTIC
        (strengthen ctxt true false rules [] 1))
      )
    );

val strengthen-method-args =
  Method.text-closure >> curry (fn (meth, ctxt) =>
    Method.CONTEXT-METHOD (fn - =>
      Method.RUNTIME (Method.CONTEXT-TACTIC
        (strengthen ctxt true true [] [meth] 1))
      )
    );

end

)

end

setup Strengthen.setup

method-setup strengthen = ⟨Strengthen.strengthen-args⟩
  strengthen the goal (see theory Strengthen-Demo)

method-setup strengthen-asm = ⟨Strengthen.strengthen-asm-args⟩
  apply "strengthen" to weaken an assumption

```

method-setup *strengthen-method* = $\langle \text{Strengthen.strengthen-method-args} \rangle$
use an argument method in "strengthen" sites

Important strengthen congruence rules.

context *strengthen-implementation* **begin**

lemma *strengthen-imp-imp*[*simp*]:
 $st\ True\ (\longrightarrow)\ A\ B = (A \longrightarrow B)$
 $st\ False\ (\longrightarrow)\ A\ B = (B \longrightarrow A)$
by (*simp-all add: st-def*)

abbreviation(*input*)
 $st\text{-}ord\ t \equiv st\ t\ ((\leq) :: ('a :: preorder) \Rightarrow -)$

lemma *strengthen-imp-ord*[*simp*]:
 $st\text{-}ord\ True\ A\ B = (A \leq B)$
 $st\text{-}ord\ False\ A\ B = (B \leq A)$
by (*auto simp add: st-def*)

lemma *strengthen-imp-conj* [*strg*]:
 $\llbracket A' \Longrightarrow st\ F\ (\longrightarrow)\ B\ B'; B \Longrightarrow st\ F\ (\longrightarrow)\ A\ A' \rrbracket$
 $\Longrightarrow st\ F\ (\longrightarrow)\ (A \wedge B)\ (A' \wedge B')$
by (*cases F, auto*)

lemma *strengthen-imp-disj* [*strg*]:
 $\llbracket \neg A' \Longrightarrow st\ F\ (\longrightarrow)\ B\ B'; \neg B \Longrightarrow st\ F\ (\longrightarrow)\ A\ A' \rrbracket$
 $\Longrightarrow st\ F\ (\longrightarrow)\ (A \vee B)\ (A' \vee B')$
by (*cases F, auto*)

lemma *strengthen-imp-implies* [*strg*]:
 $\llbracket st\ (\neg F)\ (\longrightarrow)\ X\ X'; X \Longrightarrow st\ F\ (\longrightarrow)\ Y\ Y' \rrbracket$
 $\Longrightarrow st\ F\ (\longrightarrow)\ (X \longrightarrow Y)\ (X' \longrightarrow Y')$
by (*cases F, auto*)

lemma *strengthen-all*[*strg*]:
 $\llbracket \bigwedge x. st\ F\ (\longrightarrow)\ (P\ x)\ (Q\ x) \rrbracket$
 $\Longrightarrow st\ F\ (\longrightarrow)\ (\forall x. P\ x)\ (\forall x. Q\ x)$
by (*cases F, auto*)

lemma *strengthen-ex*[*strg*]:
 $\llbracket \bigwedge x. st\ F\ (\longrightarrow)\ (P\ x)\ (Q\ x) \rrbracket$
 $\Longrightarrow st\ F\ (\longrightarrow)\ (\exists x. P\ x)\ (\exists x. Q\ x)$
by (*cases F, auto*)

lemma *strengthen-Ball*[*strg*]:
 $\llbracket st\text{-}ord\ (Not\ F)\ S\ S';$
 $\bigwedge x. x \in S \Longrightarrow st\ F\ (\longrightarrow)\ (P\ x)\ (Q\ x) \rrbracket$
 $\Longrightarrow st\ F\ (\longrightarrow)\ (\forall x \in S. P\ x)\ (\forall x \in S'. Q\ x)$

by (*cases F, auto*)

lemma *strengthen-Bex*[*strg*]:

$\llbracket st\text{-}ord\ F\ S\ S' ;$
 $\quad \bigwedge x. x \in S \implies st\ F\ (\longrightarrow)\ (P\ x)\ (Q\ x) \rrbracket$
 $\implies st\ F\ (\longrightarrow)\ (\exists x \in S. P\ x)\ (\exists x \in S'. Q\ x)$
by (*cases F, auto*)

lemma *strengthen-Collect*[*strg*]:

$\llbracket \bigwedge x. st\ F\ (\longrightarrow)\ (P\ x)\ (P'\ x) \rrbracket$
 $\implies st\text{-}ord\ F\ \{x. P\ x\}\ \{x. P'\ x\}$
by (*cases F, auto*)

lemma *strengthen-mem*[*strg*]:

$\llbracket st\text{-}ord\ F\ S\ S' \rrbracket$
 $\implies st\ F\ (\longrightarrow)\ (x \in S)\ (x \in S')$
by (*cases F, auto*)

lemma *strengthen-ord*[*strg*]:

$st\text{-}ord\ (\neg F)\ x\ x' \implies st\text{-}ord\ F\ y\ y'$
 $\implies st\ F\ (\longrightarrow)\ (x \leq y)\ (x' \leq y')$
by (*cases F, simp-all, (metis order-trans)+*)

lemma *strengthen-strict-ord*[*strg*]:

$st\text{-}ord\ (\neg F)\ x\ x' \implies st\text{-}ord\ F\ y\ y'$
 $\implies st\ F\ (\longrightarrow)\ (x < y)\ (x' < y')$
by (*cases F, simp-all, (metis order-le-less-trans order-less-le-trans)+*)

lemma *strengthen-image*[*strg*]:

$st\text{-}ord\ F\ S\ S' \implies st\text{-}ord\ F\ (f\ ' S)\ (f\ ' S')$
by (*cases F, auto*)

lemma *strengthen-vimage*[*strg*]:

$st\text{-}ord\ F\ S\ S' \implies st\text{-}ord\ F\ (f\ -' S)\ (f\ -' S')$
by (*cases F, auto*)

lemma *strengthen-Int*[*strg*]:

$st\text{-}ord\ F\ A\ A' \implies st\text{-}ord\ F\ B\ B' \implies st\text{-}ord\ F\ (A \cap B)\ (A' \cap B')$
by (*cases F, auto*)

lemma *strengthen-Un*[*strg*]:

$st\text{-}ord\ F\ A\ A' \implies st\text{-}ord\ F\ B\ B' \implies st\text{-}ord\ F\ (A \cup B)\ (A' \cup B')$
by (*cases F, auto*)

lemma *strengthen-UN*[*strg*]:

$st\text{-}ord\ F\ A\ A' \implies (\bigwedge x. x \in A \implies st\text{-}ord\ F\ (B\ x)\ (B'\ x))$
 $\implies st\text{-}ord\ F\ (\bigcup x \in A. B\ x)\ (\bigcup x \in A'. B'\ x)$
by (*cases F, auto*)

```

lemma strengthen-INT[strg]:
  st-ord ( $\neg F$ ) A A'  $\implies (\bigwedge x. x \in A \implies \textit{st-ord } F (B\ x) (B'\ x))$ 
     $\implies \textit{st-ord } F (\bigcap x \in A. B\ x) (\bigcap x \in A'. B'\ x)$ 
  by (cases F, auto)

lemma strengthen-imp-strengthen-prop[strg]:
  st False ( $\longrightarrow$ ) P Q  $\implies \textit{PROP (st-prop1 (Trueprop P) (Trueprop Q))}$ 
  st True ( $\longrightarrow$ ) P Q  $\implies \textit{PROP (st-prop2 (Trueprop P) (Trueprop Q))}$ 
  unfolding st-prop1-def st-prop2-def
  by auto

lemma st-prop-meta-imp[strg]:
  PROP (st-prop2 (PROP X) (PROP X'))
     $\implies \textit{PROP (st-prop1 (PROP Y) (PROP Y'))}$ 
     $\implies \textit{PROP (st-prop1 (PROP X \implies PROP Y) (PROP X' \implies PROP Y'))}$ 
  PROP (st-prop1 (PROP X) (PROP X'))
     $\implies \textit{PROP (st-prop2 (PROP Y) (PROP Y'))}$ 
     $\implies \textit{PROP (st-prop2 (PROP X \implies PROP Y) (PROP X' \implies PROP Y'))}$ 
  unfolding st-prop1-def st-prop2-def
  by (erule meta-mp | assumption)+

lemma st-prop-meta-all[strg]:
  ( $\bigwedge x. \textit{PROP (st-prop1 (PROP (X\ x)) (PROP (X'\ x)))}$ )
     $\implies \textit{PROP (st-prop1 (\bigwedge x. PROP (X\ x)) (\bigwedge x. PROP (X'\ x)))}$ 
  ( $\bigwedge x. \textit{PROP (st-prop2 (PROP (X\ x)) (PROP (X'\ x)))}$ )
     $\implies \textit{PROP (st-prop2 (\bigwedge x. PROP (X\ x)) (\bigwedge x. PROP (X'\ x)))}$ 
  unfolding st-prop1-def st-prop2-def
  apply (rule Pure.asm-rl)
  apply (erule meta-allE, erule meta-mp)
  apply assumption
  apply (rule Pure.asm-rl)
  apply (erule meta-allE, erule meta-mp)
  apply assumption
  done

```

end

```

lemma imp-consequent:
  P  $\longrightarrow$  Q  $\longrightarrow$  P by simp

```

Test cases.

```

lemma
  assumes x:  $\bigwedge x. P\ x \longrightarrow Q\ x$ 
  shows  $\{x. x \neq \textit{None} \wedge P\ (\textit{the } x)\} \subseteq \{y. \forall x. y = \textit{Some } x \longrightarrow Q\ x\}$ 
  apply (strengthen x)
  apply clarsimp
  done

```

```

locale strengthen-silly-test begin

definition
  silly :: nat  $\Rightarrow$  nat  $\Rightarrow$  bool
where
  silly x y = (x  $\leq$  y)

lemma silly-trans:
  silly x y  $\Longrightarrow$  silly y z  $\Longrightarrow$  silly x z
  by (simp add: silly-def)

lemma silly-refl:
  silly x x
  by (simp add: silly-def)

lemma foo:
  silly x y  $\Longrightarrow$  silly a b  $\Longrightarrow$  silly b c
     $\Longrightarrow$  silly x y  $\wedge$  ( $\forall$  x :: nat. silly a c )
  using [[strengthen-trace = true]]
  apply (strengthen silly-trans [mk-strg I E]) +
  apply (strengthen silly-refl)
  apply simp
  done

lemma foo-asm:
  silly x y  $\Longrightarrow$  silly y z
     $\Longrightarrow$  (silly x z  $\Longrightarrow$  silly a b)  $\Longrightarrow$  silly z z  $\Longrightarrow$  silly a b
  apply (strengthen-asm silly-trans [mk-strg I A])
  apply (strengthen-asm silly-trans [mk-strg I A])
  apply simp
  done

lemma foo-method:
  silly x y  $\Longrightarrow$  silly a b  $\Longrightarrow$  silly b c
     $\Longrightarrow$  silly x y  $\wedge$  ( $\forall$  x :: nat. z  $\longrightarrow$  silly a c )
  using [[strengthen-trace = true]]
  apply simp
  apply (strengthen-method (rule silly-trans))
  apply (strengthen-method (rule exI [where x=b]))
  apply simp
  done

end
end

theory WPFix

imports

```

```

../Datatype-Schematic
../Strengthen

```

begin

WPFix handles four issues which are annoying with precondition schematics: 1. Schematics in obligation (postcondition) positions which remain unset after goals are solved. They should be instantiated to *True*. 2. Schematics which appear in multiple precondition positions. They should be instantiated to a conjunction and then separated. 3/4. Schematics applied to datatype expressions such as *True* or *Some x*. for details.

lemma *use-strengthen-prop-intro*:

```

PROP P  $\implies$  PROP (strengthen-implementation.st-prop1 (PROP Q) (PROP P))
 $\implies$  PROP Q
unfolding strengthen-implementation.st-prop1-def
apply (drule(1) meta-mp)+
apply assumption
done

```

definition

```

target-var :: int  $\Rightarrow$  'a  $\Rightarrow$  'a

```

where

```

target-var n x = x

```

lemma *strengthen-to-conjunct1-target*:

```

strengthen-implementation.st True ( $\longrightarrow$ )
(target-var n (P  $\wedge$  Q)) (target-var n P)
by (simp add: strengthen-implementation.st-def target-var-def)

```

lemma *strengthen-to-conjunct2-target-trans*:

```

strengthen-implementation.st True ( $\longrightarrow$ )
(target-var n Q) R
 $\implies$  strengthen-implementation.st True ( $\longrightarrow$ )
(target-var n (P  $\wedge$  Q)) R
by (simp add: strengthen-implementation.st-def target-var-def)

```

lemma *target-var-drop-func*:

```

target-var n f = ( $\lambda x$ . target-var n (f x))
by (simp add: target-var-def)

```

named-theorems *wp-fix-strgs*

lemma *strg-target-to-true*:

```

strengthen-implementation.st F ( $\longrightarrow$ ) (target-var n True) True
by (simp add: target-var-def strengthen-implementation.strengthen-refl)

```

ML \langle

```

structure WPFix = struct

```

```

val st-refl = @{thm strengthen-implementation.strengthen-refl}
val st-refl-True = @{thm strengthen-implementation.strengthen-refl[where x=True]}
val st-refl-target-True = @{thm strg-target-to-true}
val st-refl-non-target
  = @{thm strengthen-implementation.strengthen-refl[where x=target-var (-1) v
for v]}

val conv-to-target = mk-meta-eq @{thm target-var-def[symmetric]}

val tord = Term-Ord.fast-term-ord
fun has-var vars t = not (null (Ord-List.inter tord vars
  (Ord-List.make tord (map Var (Term.add-vars t [])))))

fun get-vars prop = map Var (Term.add-vars prop [])
  |> Ord-List.make tord
  |> filter (fn v => snd (strip-type (fastype-of v)) = HLogic.boolT)

val st-intro = @{thm use-strengthen-prop-intro}
val st-not = @{thms strengthen-implementation.strengthen-Not}
val st-conj2-trans = @{thm strengthen-to-conjunct2-target-trans}
val st-conj1 = @{thm strengthen-to-conjunct1-target}

(* assumes Strengthen.goal-predicate g is st *)
fun dest-strg g = case Strengthen.goal-predicate g of
  st => (case HLogic.dest-Trueprop (Logic.strip-assums-concl g) of
    (Const - $ mode $ rel $ lhs $ rhs) => (st, SOME (mode, rel, lhs, rhs))
    | - => error (dest-strg ^ @{make-string} g)
  )
  | nm => (nm, NONE)

fun get-target (Const (@{const-name target-var}, -) $ n $ -)
  = (try (HLogic.dest-number #> snd) n)
  | get-target - = NONE

fun is-target P t = case get-target t of NONE => false
  | SOME v => P v

fun is-target-head P (f $ v) = is-target P (f $ v) orelse is-target-head P f
  | is-target-head - = false

fun has-target P (f $ v) = is-target P (f $ v)
  orelse has-target P f orelse has-target P v
  | has-target P (Abs (-, -, t)) = has-target P t
  | has-target - = false

fun apply-strgs congs ctxt = SUBGOAL (fn (t, i) => case
  dest-strg t of
  (st-prop1, -) => resolve-tac ctxt congs i

```

```

| (st-prop2, -) => resolve-tac ctxt congs i
| (st, SOME (-, -, lhs, -)) => resolve-tac ctxt st-not i
  ORELSE eresolve-tac ctxt [thin-rl] i
  ORELSE resolve-tac ctxt [st-refl-non-target] i
  ORELSE (if is-target-head (fn v => v >= 0) lhs
    then no-tac
    else if not (has-target (fn v => v >= 0) lhs)
      then resolve-tac ctxt [st-refl] i
      else if is-Const (head-of lhs)
        then (resolve-tac ctxt congs i ORELSE resolve-tac ctxt [st-refl] i)
        else resolve-tac ctxt [st-refl] i
  )
| - => no-tac
)

fun strg-proc ctxt = let
  val congs1 = Named-Theorems.get ctxt @ {named-theorems wp-fix-strgs}
  val thy = Proof-Context.theory-of ctxt
  val congs2 = Strengthen.Congs.get thy
  val strg = apply-strgs (congs1 @ congs2) ctxt
in REPEAT-ALL-NEW strg end

fun target-var-conv vars ctxt ct = case Thm.term-of ct of
  Abs - => Conv.sub-conv (target-var-conv vars) ctxt ct
| Var v => Conv.rewr-conv (Drule.infer-instantiate ctxt
  [((n, 1), Thm.cterm-of ctxt (HOLogic.mk-number @ {typ int}
    (find-index (fn v2 => v2 = Var v) vars)))] conv-to-target) ct
| - $ - => Datatype-Schematic.combs-conv (target-var-conv vars) ctxt ct
| - => raise Option

fun st-intro-tac ctxt = CSUBGOAL (fn (ct, i) => fn thm => let
  val intro = Drule.infer-instantiate ctxt [((Q, 0), ct)]
  (Thm.incr-indexes (Thm.maxidx-of thm + 1) st-intro)
in compose-tac ctxt (false, intro, 2) i
end thm)

fun intro-tac ctxt vs = SUBGOAL (fn (t, i) => if has-var vs t
  then CONVERSION (target-var-conv vs ctxt) i
  THEN CONVERSION (Simplifier.full-rewrite (clear-simpset ctxt
    addsimps @ {thms target-var-drop-func}
  )) i
  THEN st-intro-tac ctxt i
  else all-tac)

fun classify v thm = let
  val has-t = has-target (fn v' => v' = v)
  val relevant = filter (has-t o fst)
  (Thm.premis-of thm ~ (1 upto Thm.nprems-of thm))
|> map (apfst (Logic.strip-assums-concl #> Envir.beta-eta-contract))

```



```

fun class t = case dest-strg t of
  (st, SOME (@{term True}, @{|term (-->)}, lhs, -))
    => if has-t lhs then SOME true else NONE
  | (st, SOME (@{|term False}, @{|term (-->)}, lhs, -))
    => if has-t lhs then SOME false else NONE
  | - => NONE
val classn = map (apfst class) relevant
fun get k = map snd (filter (fn (k', -) => k' = k) classn)
in if (null relevant) then NONE
  else if not (null (get NONE))
  then NONE
  else if null (get (SOME true))
  then SOME (to-true, map snd relevant)
  else if length (get (SOME true)) > 1
  then SOME (to-conj, get (SOME true))
  else NONE
end

fun ONGOALS tac is = let
  val is = rev (sort int-ord is)
in EVERY (map tac is) end

fun act-on ctxt (to-true, is)
  = ONGOALS (resolve-tac ctxt [st-refl-target-True]) is
  | act-on ctxt (to-conj, is)
  = ONGOALS (resolve-tac ctxt [st-conj2-trans]) (drop 1 is)
    THEN (if length is > 2 then act-on ctxt (to-conj, drop 1 is)
      else ONGOALS (resolve-tac ctxt [st-refl]) (drop 1 is))
    THEN ONGOALS (resolve-tac ctxt [st-conj1]) (take 1 is)
  | act-on - (s, -) = error (act-on: ^ s)

fun act ctxt check vs thm = let
  val acts = map-filter (fn v => classify v thm) vs
in if null acts
  then (if check then no-tac else all-tac) thm
  else (act-on ctxt (hd acts) THEN act ctxt false vs) thm end

fun cleanup ctxt = SUBGOAL (fn (t, i) => case Strengthen.goal-predicate t of
  st => resolve-tac ctxt [st-refl] i
  | - => all-tac)

fun tac ctxt = SUBGOAL (fn (t, -) => let
  val vs = get-vars t
in if null vs then no-tac else ALLGOALS (intro-tac ctxt vs)
  THEN ALLGOALS (TRY o strg-proc ctxt)
  THEN act ctxt true (0 upto (length vs - 1))
  THEN ALLGOALS (cleanup ctxt)
  THEN Local-Defs.unfold-tac ctxt @{|thms target-var-def}
end)

```

```

fun both-tac ctxt = (Datatype-Schematic.tac ctxt THEN' (TRY o tac ctxt))
  OR ELSE' tac ctxt

val method =
  Method.sections [Datatype-Schematic.add-section] >>
  (fn - => fn ctxt => Method.SIMPLE-METHOD' (both-tac ctxt));

end

```

```

method-setup wpfix = ⟨WPFix.method⟩

```

```

lemma demo1:
  (∃ Ia Ib Ic Id Ra.
    (Ia (Suc 0) ⟶ Qa)
    ∧ (Ib ⟶ Qb)
    ∧ (Ic ⟶ Ra)
    ∧ (Id ⟶ Qc)
    ∧ (Id ⟶ Qd)
    ∧ (Qa ∧ Qb ∧ Qc ∧ Qd ⟶ Ia v ∧ Ib ∧ Ic ∧ Id))
  apply (intro exI conjI impI)

  apply (wpfix | assumption)+
  apply auto
done

```

```

lemma demo2:
  assumes P: ∧x. P (x + Suc x) ⟶ R (Inl x)
    ∧x. P ((x * 2) - 1) ⟶ R (Inr x)
  assumes P17: P 17
  shows ∃ I. I (Some 9)
    ∧ (∀ x. I x ⟶ (case x of None ⇒ R (Inl 8) | Some y ⇒ R (Inr y)))
    ∧ (∀ x. I x ⟶ (case x of None ⇒ R (Inr 9) | Some y ⇒ R (Inl (y - 1))))
  apply (intro exI conjI[rotated] allI)
  apply (case-tac x; simp)
  apply wpfix
  apply (rule P)
  apply wpfix
  apply (rule P)
  apply (case-tac x; simp)
  apply wpfix
  apply (rule P)
  apply wpfix
  apply (rule P)
  apply (simp add: P17)
done

```

— Shows how to use *datatype-schematic* rules as "accessors".

```

lemma (in datatype-schem-demo) demo3:
   $\exists x. \forall a\ b. x\ (basic\ a\ b) = a$ 
  apply (rule exI, (rule allI)+)
  apply (wpfix add: get-basic-0.simps) — Only exposes ‘a’ to the schematic.
  by (rule refl)

end

```

```

theory WP
imports
  WP-Pre
  WPFix
  ../.. / Apply-Debug
  ../.. / ml-helpers / MLUtils
begin

```

```

definition
  triple-judgement :: ('a  $\Rightarrow$  bool)  $\Rightarrow$  'b  $\Rightarrow$  ('a  $\Rightarrow$  'b  $\Rightarrow$  bool)  $\Rightarrow$  bool
where
  triple-judgement pre body property = ( $\forall s. pre\ s \longrightarrow property\ s\ body$ )

```

```

definition
  postcondition :: ('r  $\Rightarrow$  's  $\Rightarrow$  bool)  $\Rightarrow$  ('a  $\Rightarrow$  'b  $\Rightarrow$  ('r  $\times$  's) set)
                $\Rightarrow$  'a  $\Rightarrow$  'b  $\Rightarrow$  bool

```

```

where
  postcondition P f = ( $\lambda a\ b. \forall (rv, s) \in f\ a\ b. P\ rv\ s$ )

```

```

definition
  postconditions :: ('a  $\Rightarrow$  'b  $\Rightarrow$  bool)  $\Rightarrow$  ('a  $\Rightarrow$  'b  $\Rightarrow$  bool)  $\Rightarrow$  ('a  $\Rightarrow$  'b  $\Rightarrow$  bool)
where
  postconditions P Q = ( $\lambda a\ b. P\ a\ b \wedge Q\ a\ b$ )

```

```

lemma conj-TrueI:  $P \Longrightarrow True \wedge P$  by simp
lemma conj-TrueI2:  $P \Longrightarrow P \wedge True$  by simp

```

```

ML-file WP-method.ML

```

```

declare [wp-trace = false]

```

```

setup WeakestPre.setup

```

```

method-setup wp =  $\langle WeakestPre.apply-wp-args \rangle$ 
  applies weakest precondition rules

```

```

end

```

```

theory WPC

```

imports *WP-Pre*
keywords *wpc-setup* :: *thy-decl*

begin

definition

wpc-helper :: $((a \Rightarrow \text{bool}) \times b \text{ set}) \Rightarrow ((a \Rightarrow \text{bool}) \times b \text{ set}) \Rightarrow \text{bool} \Rightarrow \text{bool}$ **where**
wpc-helper $\equiv \lambda(P, P') (Q, Q') R. ((\forall s. P s \longrightarrow Q s) \wedge P' \subseteq Q') \longrightarrow R$

lemma *wpc-conj-process*:

$\llbracket \text{wpc-helper } (P, P') (A, A') C; \text{wpc-helper } (P, P') (B, B') D \rrbracket$
 $\impl \text{wpc-helper } (P, P') (\lambda s. A s \wedge B s, A' \cap B') (C \wedge D)$
by (*clarsimp simp add: wpc-helper-def*)

lemma *wpc-all-process*:

$\llbracket \bigwedge x. \text{wpc-helper } (P, P') (Q x, Q' x) (R x) \rrbracket$
 $\impl \text{wpc-helper } (P, P') (\lambda s. \forall x. Q x s, \{s. \forall x. s \in Q' x\}) (\forall x. R x)$
by (*clarsimp simp: wpc-helper-def subset-iff*)

lemma *wpc-all-process-very-weak*:

$\llbracket \bigwedge x. \text{wpc-helper } (P, P') (Q, Q') (R x) \rrbracket \impl \text{wpc-helper } (P, P') (Q, Q') (\forall x. R x)$
by (*clarsimp simp: wpc-helper-def*)

lemma *wpc-imp-process*:

$\llbracket Q \impl \text{wpc-helper } (P, P') (R, R') S \rrbracket$
 $\impl \text{wpc-helper } (P, P') (\lambda s. Q \longrightarrow R s, \{s. Q \longrightarrow s \in R'\}) (Q \longrightarrow S)$
by (*clarsimp simp add: wpc-helper-def subset-iff*)

lemma *wpc-imp-process-weak*:

$\llbracket \text{wpc-helper } (P, P') (R, R') S \rrbracket \impl \text{wpc-helper } (P, P') (R, R') (Q \longrightarrow S)$
by (*clarsimp simp add: wpc-helper-def*)

lemmas *wpc-processors*

= *wpc-conj-process wpc-all-process wpc-imp-process*

lemmas *wpc-weak-processors*

= *wpc-conj-process wpc-all-process wpc-imp-process-weak*

lemmas *wpc-vweak-processors*

= *wpc-conj-process wpc-all-process-very-weak wpc-imp-process-weak*

lemma *wpc-helperI*:

wpc-helper $(P, P') (P, P') Q \impl Q$
by (*simp add: wpc-helper-def*)

lemma *wpc-foo*: $\llbracket \text{undefined } x; \text{False} \rrbracket \impl P x$

by *simp*

lemma *foo*:

```

assumes foo-elim:  $\bigwedge P Q h. [\![\text{foo } Q h; \bigwedge s. P s \implies Q s]\!] \implies \text{foo } P h$ 
shows
   $[\![\bigwedge x. \text{foo } (Q x) (f x); \text{foo } R g]\!] \implies$ 
     $\text{foo } (\lambda s. (\forall x. Q x s) \wedge (y = \text{None} \longrightarrow R s))$ 
     $(\text{case } y \text{ of } \text{Some } x \Rightarrow f x \mid \text{None} \Rightarrow g)$ 
by (auto split: option.split intro: foo-elim)

ML (
signature WPC = sig
  exception WPCFailed of string * term list * thm list;

  val foo-thm: thm;
  val iff2-thm: thm;
  val wpc-helperI: thm;

  val instantiate-concl-pred: Proof.context -> cterm -> thm -> thm;

  val detect-term: Proof.context -> int -> thm -> cterm -> (cterm * term)
list;
  val detect-terms: Proof.context -> (term -> cterm -> thm -> int -> tactic)
-> int -> tactic;

  val split-term: thm list -> Proof.context -> term -> cterm -> thm -> int
-> tactic;

  val wp-cases-tac: thm list -> Proof.context -> int -> tactic;
  val wp-debug-tac: thm list -> Proof.context -> int -> tactic;
  val wp-cases-method: thm list -> (Proof.context -> Method.method) context-parser;

end;

structure WPCPredicateAndFinals = Theory-Data
(struct
  type T = (cterm * thm) list
  val empty = []
  val extend = I
  fun merge (xs, ys) =
    (* Order of predicates is important, so we can't reorder *)
    let val tms = map (Thm.term-of o fst) xs
        fun inxs x = exists (fn y => x aconv y) tms
        val ys' = filter (not o inxs o Thm.term-of o fst) ys
    in
      xs @ ys'
    end
end);

structure WeakestPreCases : WPC =
struct

```

```

exception WPCFailed of string * term list * thm list;

val iffD2-thm = @{thm iffD2};
val wpc-helperI = @{thm wpc-helperI};
val foo-thm = @{thm wpc-foo};

(* it looks like cterm-instantiate would do the job better,
   but this handles the case where ?'a must be instantiated
   to ?'a × ?'b *)
fun instantiate-concl-pred ctxt pred thm =
  let
    val get-concl-pred = (fst o strip-comb o HOLogic.dest-Trueprop o Thm.concl-of);
    val get-concl-predC = (Thm.cterm-of ctxt o get-concl-pred);

    val get-pred-tvar = domain-type o Thm.typ-of o Thm.ctyp-of-cterm;
    val thm-pred = get-concl-predC thm;
    val thm-pred-tvar = Term.dest-TVar (get-pred-tvar thm-pred);
    val pred-tvar = Thm.ctyp-of ctxt (get-pred-tvar pred);

    val thm2 = Thm.instantiate ([ (thm-pred-tvar, pred-tvar) ], []) thm;

    val thm2-pred = Term.dest-Var (get-concl-pred thm2);
  in
    Thm.instantiate ([], [(thm2-pred, pred)]) thm2
  end;

fun detect-term ctxt n thm tm =
  let
    val foo-thm-tm = instantiate-concl-pred ctxt tm foo-thm;
    val matches = resolve-tac ctxt [foo-thm-tm] n thm;
    val outcomes = Seq.list-of matches;
    val get-goalterm = (HOLogic.dest-Trueprop o Logic.strip-assums-concl
      o Envir.beta-eta-contract o hd o Thm.prem-of);
    val get-argument = hd o snd o strip-comb;
  in
    map (pair tm o get-argument o get-goalterm) outcomes
  end;

fun detect-terms ctxt tactic2 n thm =
  let
    val pfs = WPCPredicateAndFinals.get (Proof-Context.theory-of ctxt);
    val detects = map (fn (tm, rl) => (detect-term ctxt n thm tm, rl)) pfs;
    val detects2 = filter (not o null o fst) detects;
    val ((pred, arg), fin) = case detects2 of
      [] => raise WPCFailed (detect-terms: no match, [], [thm])
    | ((d3, fin) :: _) => (hd d3, fin)
  in
    tactic2 arg pred fin n thm
  end

```

```

end;

(* give each rule in the list one possible resolution outcome *)
fun resolve-each-once-tac ctxt thms i
  = fold (curry (APPEND'))
    (map (DETERM oo resolve-tac ctxt o single) thms)
    (K no-tac) i

fun resolve-single-tac ctxt rules n thm =
  case Seq.chop 2 (resolve-each-once-tac ctxt rules n thm)
  of ([], -) => raise WPCFailed
    (resolve-single-tac: no rules could apply,
     [], thm :: rules)
  | (- :: - :: -, -) => raise WPCFailed
    (resolve-single-tac: multiple rules applied,
     [], thm :: rules)
  | ([x], -) => Seq.single x;

fun split-term processors ctxt target pred fin =
  let
    val hdTarget      = head-of target;
    val (constNm, -) = dest-Const hdTarget handle TERM (-, tms)
      => raise WPCFailed (split-term: couldn't dest-Const, tms, []);
    val split = case (Ctr-Sugar.ctr-sugar-of-case ctxt constNm) of
      SOME sugar => #split sugar
    | - => raise WPCFailed (split-term: not a case, [hdTarget], []);
    val subst      = split RS iff2-thm;
    val subst2     = instantiate-concl-pred ctxt pred subst;
  in
    (resolve-tac ctxt [subst2])
    THEN'
    (resolve-tac ctxt [wpc-helperI])
    THEN'
    (REPEAT-ALL-NEW (resolve-tac ctxt processors)
     THEN-ALL-NEW
     resolve-single-tac ctxt [fin])
  end;

(* n.b. need to concretise the lazy sequence via a list to ensure exceptions
   have been raised already and catch them *)
fun wp-cases-tac processors ctxt n thm =
  detect-terms ctxt (split-term processors ctxt) n thm
  |> Seq.list-of |> Seq.of-list
  handle WPCFailed - => no-tac thm;

fun wp-debug-tac processors ctxt n thm =
  detect-terms ctxt (split-term processors ctxt) n thm
  |> Seq.list-of |> Seq.of-list
  handle WPCFailed e => (warning (@{make-string} (WPCFailed e)); no-tac

```

```

    thm);

    fun wp-cases-method processors = Scan.succeed (fn ctxt =>
      Method.SIMPLE-METHOD' (wp-cases-tac processors ctxt));

    local structure P = Parse and K = Keyword in

      fun add-wpc tm thm lthy = let
        val ctxt = Local-Theory.target-of lthy
        val tm' = (Syntax.read-term ctxt tm) |> Thm.ctrm-of ctxt o Logic.verify-global
        val thm' = Proof-Context.get-thm ctxt tm
      in
        Local-Theory.background-theory (WPCPredicateAndFinals.map (fn xs => (tm',
          thm') :: xs)) lthy
      end;

      val - =
        Outer-Syntax.command
          @{command-keyword wpc-setup}
          Add wpc stuff
          (P.term -- P.name >> (fn (tm, thm) => Toplevel.local-theory NONE
            NONE (add-wpc tm thm)))

    end;
  end;

}

ML <

val wp-cases-tactic-weak = WeakestPreCases.wp-cases-tac @{thms wpc-weak-processors};
val wp-cases-method-strong = WeakestPreCases.wp-cases-method @{thms wpc-processors};
val wp-cases-method-weak = WeakestPreCases.wp-cases-method @{thms wpc-weak-processors};
val wp-cases-method-vweak = WeakestPreCases.wp-cases-method @{thms wpc-vweak-processors};

}

method-setup wpc0 = <wp-cases-method-strong>
  case splitter for weakest-precondition proofs

method-setup wpcw0 = <wp-cases-method-weak>
  weak-form case splitter for weakest-precondition proofs

method wpc = (wp-pre, wpc0)
method wpcw = (wp-pre, wpcw0)

definition
  wpc-test :: 'a set => ('a × 'b) set => 'b set => bool
  where

```


$wpc\text{-}test\ P\ R\ S \equiv (R \text{ “ } P) \subseteq S$

lemma *wpc-test-weaken*:

$\llbracket wpc\text{-}test\ Q\ R\ S; P \subseteq Q \rrbracket \implies wpc\text{-}test\ P\ R\ S$
by (*simp add: wpc-test-def, blast*)

lemma *wpc-helper-validF*:

$wpc\text{-}test\ Q'\ R\ S \implies wpc\text{-}helper\ (P, P')\ (Q, Q')\ (wpc\text{-}test\ P'\ R\ S)$
by (*simp add: wpc-test-def wpc-helper-def, blast*)

setup \langle

let

$val\ tm = Thm.ctrm\text{-}of\ @\{context\}\ (Logic.varify\text{-}global\ @\{term\ \lambda R. wpc\text{-}test\ P\ R\ S\});$

$val\ thm = @\{thm\ wpc\text{-}helper\text{-}validF\};$

in

$WP\text{CPredicateAndFinals}.map\ (fn\ xs \Rightarrow (tm, thm) :: xs)$

end

\rangle

lemma *set-conj-Int-simp*:

$\{s \in S. P\ s\} = S \cap \{s. P\ s\}$
by *auto*

lemma *case-options-weak-wp*:

$\llbracket wpc\text{-}test\ P\ R\ S; \bigwedge x. wpc\text{-}test\ P'\ (R'\ x)\ S \rrbracket$
 $\implies wpc\text{-}test\ (P \cap P')\ (case\ opt\ of\ None \Rightarrow R \mid Some\ x \Rightarrow R'\ x)\ S$

apply (*rule wpc-test-weaken*)

apply *wpcw*

apply *assumption*

apply *assumption*

apply *simp*

done

end

theory *Simp-No-Conditional*

imports *Main*

begin

Simplification without conditional rewriting. Setting the simplifier depth limit to zero prevents attempts at conditional rewriting. This should make the simplifier faster and more predictable on average. It may be particularly useful in derived tactics and methods to avoid situations where the simplifier repeatedly attempts and fails a conditional rewrite.

As always, there are caveats. Failing to perform a simple conditional rewrite may open the door to expensive alternatives. Various simprocs which are conditional in nature will not be deactivated.

ML \langle

```

structure Simp-No-Conditional = struct

val set-no-cond = Config.put Raw-Simplifier.simp-depth-limit 0

val simp-tac = Simplifier.simp-tac o set-no-cond
val asm-simp-tac = Simplifier.asm-simp-tac o set-no-cond
val full-simp-tac = Simplifier.full-simp-tac o set-no-cond
val asm-full-simp-tac = Simplifier.asm-full-simp-tac o set-no-cond

val clarsimp-tac = Clarsimp.clarsimp-tac o set-no-cond
val auto-tac = Clarsimp.auto-tac o set-no-cond

fun mk-method secs tac
  = Method.sections secs >> K (SIMPLE-METHOD' o tac)
val mk-clarsimp-method = mk-method Clarsimp.clarsimp-modifiers

fun mk-clarsimp-all-method tac =
  Method.sections Clarsimp.clarsimp-modifiers >> K (SIMPLE-METHOD o tac)

val simp-method = mk-method Simplifier.simp-modifiers
  (CHANGED-PROP oo asm-full-simp-tac)
val clarsimp-method = mk-clarsimp-method (CHANGED-PROP oo clarsimp-tac)
val auto-method = mk-clarsimp-all-method (CHANGED-PROP o auto-tac)

end

)

method-setup simp-no-cond =  $\langle$ Simp-No-Conditional.simp-method $\rangle$ 
  Simplification with no conditional simplification.

method-setup clarsimp-no-cond =  $\langle$ Simp-No-Conditional.clarsimp-method $\rangle$ 
  Clarsimp with no conditional simplification.

method-setup auto-no-cond =  $\langle$ Simp-No-Conditional.auto-method $\rangle$ 
  Auto with no conditional simplification.

end

```

```

theory WPSimp
imports
  WP
  WPC

```

```

    WPFix
    ../Simp-No-Conditional
begin

method wpsimp uses wp wp-del simp simp-del split split-del cong comb comb-del
=
  ((determ (wpfix | wp add: wp del: wp-del comb: comb comb del: comb-del | wpc |
    clarsimp-no-cond simp: simp simp del: simp-del split: split split del:
split-del cong: cong |
    clarsimp simp: simp simp del: simp-del split: split split del: split-del cong:
cong) +) [1]

end

theory NonDetMonadVCG
imports
  NonDetMonadLemmas
  wp / WPSimp
  Strengthen
begin

declare K-def [simp]

```

22 Satisfiability

The dual to validity: an existential instead of a universal quantifier for the post condition. In refinement, it is often sufficient to know that there is one state that satisfies a condition.

definition

$$\begin{aligned}
\text{exs-valid} &:: ('a \Rightarrow \text{bool}) \Rightarrow ('a, 'b) \text{ nondet-monad} \Rightarrow \\
&('b \Rightarrow 'a \Rightarrow \text{bool}) \Rightarrow \text{bool} \\
&(\{\!\!-\!\!\} - \exists \{\!\!-\!\!\})
\end{aligned}$$

where

$$\text{exs-valid } P \text{ } f \text{ } Q \equiv (\forall s. P \text{ } s \longrightarrow (\exists (rv, s') \in \text{fst } (f \text{ } s). Q \text{ } rv \text{ } s'))$$

The above for the exception monad

definition

$$\begin{aligned}
\text{ex-exs-validE} &:: ('a \Rightarrow \text{bool}) \Rightarrow ('a, 'e + 'b) \text{ nondet-monad} \Rightarrow \\
&('b \Rightarrow 'a \Rightarrow \text{bool}) \Rightarrow ('e \Rightarrow 'a \Rightarrow \text{bool}) \Rightarrow \text{bool} \\
&(\{\!\!-\!\!\} - \exists \{\!\!-\!\!\}, \{\!\!-\!\!\})
\end{aligned}$$

where

$$\begin{aligned}
\text{ex-exs-validE } P \text{ } f \text{ } Q \text{ } E &\equiv \\
\text{exs-valid } P \text{ } f \text{ } (\lambda rv. \text{ case } rv \text{ of } \text{Inl } e \Rightarrow E \text{ } e \mid \text{Inr } v \Rightarrow Q \text{ } v)
\end{aligned}$$

23 Lemmas

23.1 Determinism

lemma *det-set-iff*:

$det\ f \implies (r \in fst\ (f\ s)) = (fst\ (f\ s) = \{r\})$
apply (*simp add: det-def*)
apply (*rule iffI*)
apply (*erule-tac x=s in allE*)
apply *auto*
done

lemma *return-det [iff]*:

$det\ (return\ x)$
by (*simp add: det-def return-def*)

lemma *put-det [iff]*:

$det\ (put\ s)$
by (*simp add: det-def put-def*)

lemma *get-det [iff]*:

$det\ get$
by (*simp add: det-def get-def*)

lemma *det-gets [iff]*:

$det\ (gets\ f)$
by (*auto simp add: gets-def det-def get-def return-def bind-def*)

lemma *det-UN*:

$det\ f \implies (\bigcup x \in fst\ (f\ s). g\ x) = (g\ (THE\ x. x \in fst\ (f\ s)))$
unfolding *det-def*
apply *simp*
apply (*drule spec [of - s]*)
apply *clarsimp*
done

lemma *bind-detI [simp, intro!]*:

$\llbracket det\ f; \forall x. det\ (g\ x) \rrbracket \implies det\ (f\ >>= g)$
apply (*simp add: bind-def det-def split-def*)
apply *clarsimp*
apply (*erule-tac x=s in allE*)
apply *clarsimp*
apply (*erule-tac x=a in allE*)
apply (*erule-tac x=b in allE*)
apply *clarsimp*
done

lemma *the-run-stateI*:

$fst\ (M\ s) = \{s'\} \implies the-run-state\ M\ s = s'$
by (*simp add: the-run-state-def*)

lemma *the-run-state-det*:
 $\llbracket s' \in \text{fst } (M \ s); \text{det } M \rrbracket \implies \text{the-run-state } M \ s = s'$
by (*simp add: the-run-stateI det-set-iff*)

23.2 Lifting and Alternative Basic Definitions

lemma *liftE-liftM*: $\text{liftE} = \text{liftM } \text{Inr}$
apply (*rule ext*)
apply (*simp add: liftE-def liftM-def*)
done

lemma *liftME-liftM*: $\text{liftME } f = \text{liftM } (\text{case-sum } \text{Inl } (\text{Inr} \circ f))$
apply (*rule ext*)
apply (*simp add: liftME-def liftM-def bindE-def returnOk-def lift-def*)
apply (*rule-tac f=bind x in arg-cong*)
apply (*rule ext*)
apply (*case-tac xa*)
apply (*simp-all add: lift-def throwError-def*)
done

lemma *liftE-bindE*:
 $(\text{liftE } a) >>= \text{E } b = a >>= b$
apply (*simp add: liftE-def bindE-def lift-def bind-assoc*)
done

lemma *liftM-id[simp]*: $\text{liftM } \text{id} = \text{id}$
apply (*rule ext*)
apply (*simp add: liftM-def*)
done

lemma *liftM-bind*:
 $(\text{liftM } t \ f \ >>= \ g) = (f \ >>= (\lambda x. \ g \ (t \ x)))$
by (*simp add: liftM-def bind-assoc*)

lemma *gets-bind-ign*: $\text{gets } f \ >>= (\lambda x. \ m) = m$
apply (*rule ext*)
apply (*simp add: bind-def simpler-gets-def*)
done

lemma *get-bind-apply*: $(\text{get } >>= f) \ x = f \ x \ x$
by (*simp add: get-def bind-def*)

lemma *exec-gets*:
 $(\text{gets } f \ >>= \ m) \ s = m \ (f \ s) \ s$
by (*simp add: simpler-gets-def bind-def*)

lemma *exec-get*:
 $(\text{get } >>= \ m) \ s = m \ s \ s$

by (*simp add: get-def bind-def*)

lemma *bind-eqI*:

$\llbracket f = f'; \bigwedge x. g\ x = g'\ x \rrbracket \Longrightarrow f >>= g = f' >>= g'$

apply (*rule ext*)

apply (*simp add: bind-def*)

apply (*auto simp: split-def*)

done

23.3 Simplification Rules for Lifted And/Or

lemma *pred-andE[elim!]*: $\llbracket (A\ \text{and}\ B)\ x; \llbracket A\ x; B\ x \rrbracket \Longrightarrow R \rrbracket \Longrightarrow R$

by (*simp add: pred-conj-def*)

lemma *pred-andI[intro!]*: $\llbracket A\ x; B\ x \rrbracket \Longrightarrow (A\ \text{and}\ B)\ x$

by (*simp add: pred-conj-def*)

lemma *pred-conj-app[simp]*: $(P\ \text{and}\ Q)\ x = (P\ x \wedge Q\ x)$

by (*simp add: pred-conj-def*)

lemma *bipred-andE[elim!]*: $\llbracket (A\ \text{And}\ B)\ x\ y; \llbracket A\ x\ y; B\ x\ y \rrbracket \Longrightarrow R \rrbracket \Longrightarrow R$

by (*simp add: bipred-conj-def*)

lemma *bipred-andI[intro!]*: $\llbracket A\ x\ y; B\ x\ y \rrbracket \Longrightarrow (A\ \text{And}\ B)\ x\ y$

by (*simp add: bipred-conj-def*)

lemma *bipred-conj-app[simp]*: $(P\ \text{And}\ Q)\ x = (P\ x\ \text{and}\ Q\ x)$

by (*simp add: pred-conj-def bipred-conj-def*)

lemma *pred-disjE[elim!]*: $\llbracket (P\ \text{or}\ Q)\ x; P\ x \Longrightarrow R; Q\ x \Longrightarrow R \rrbracket \Longrightarrow R$

by (*fastforce simp: pred-disj-def*)

lemma *pred-disjI1[intro]*: $P\ x \Longrightarrow (P\ \text{or}\ Q)\ x$

by (*simp add: pred-disj-def*)

lemma *pred-disjI2[intro]*: $Q\ x \Longrightarrow (P\ \text{or}\ Q)\ x$

by (*simp add: pred-disj-def*)

lemma *pred-disj-app[simp]*: $(P\ \text{or}\ Q)\ x = (P\ x \vee Q\ x)$

by *auto*

lemma *bipred-disjI1[intro]*: $P\ x\ y \Longrightarrow (P\ \text{Or}\ Q)\ x\ y$

by (*simp add: bipred-disj-def*)

lemma *bipred-disjI2[intro]*: $Q\ x\ y \Longrightarrow (P\ \text{Or}\ Q)\ x\ y$

by (*simp add: bipred-disj-def*)

lemma *bipred-disj-app[simp]*: $(P\ \text{Or}\ Q)\ x = (P\ x\ \text{or}\ Q\ x)$

by (*simp add: pred-disj-def bipred-disj-def*)

lemma *pred-notnotD[simp]*: $(\text{not not } P) = P$
by(*simp add:pred-neg-def*)

lemma *pred-and-true[simp]*: $(P \text{ and } \top) = P$
by(*simp add:pred-conj-def*)

lemma *pred-and-true-var[simp]*: $(\top \text{ and } P) = P$
by(*simp add:pred-conj-def*)

lemma *pred-and-false[simp]*: $(P \text{ and } \perp) = \perp$
by(*simp add:pred-conj-def*)

lemma *pred-and-false-var[simp]*: $(\perp \text{ and } P) = \perp$
by(*simp add:pred-conj-def*)

lemma *pred-conj-assoc*:
 $(P \text{ and } Q \text{ and } R) = (P \text{ and } (Q \text{ and } R))$
unfolding *pred-conj-def* **by** *simp*

23.4 Hoare Logic Rules

lemma *validE-def2*:
 $\{P\} f \{Q\}, \{R\} \equiv \forall s. P s \longrightarrow (\forall (r, s') \in \text{fst } (f s). \text{case } r \text{ of } \text{Inr } b \Rightarrow Q b s' \mid \text{Inl } a \Rightarrow R a s')$
by (*unfold valid-def validE-def*)

lemma *seq'*:
 $\llbracket \{A\} f \{B\}; \forall x. P x \longrightarrow \{C\} g x \{D\}; \forall x s. B x s \longrightarrow P x \wedge C s \rrbracket \Longrightarrow \{A\} \text{ do } x \leftarrow f; g x \text{ od } \{D\}$
apply (*clarsimp simp: valid-def bind-def*)
apply *fastforce*
done

lemma *seq*:
assumes *f-valid*: $\{A\} f \{B\}$
assumes *g-valid*: $\bigwedge x. P x \Longrightarrow \{C\} g x \{D\}$
assumes *bind*: $\bigwedge x s. B x s \Longrightarrow P x \wedge C s$
shows $\{A\} \text{ do } x \leftarrow f; g x \text{ od } \{D\}$
apply (*insert f-valid g-valid bind*)
apply (*blast intro: seq'*)
done

lemma *seq-ext'*:
 $\llbracket \{A\} f \{B\}; \forall x. \{B x\} g x \{C\} \rrbracket \Longrightarrow \{A\} \text{ do } x \leftarrow f; g x \text{ od } \{C\}$

by (*fastforce simp: valid-def bind-def Let-def split-def*)

lemma *seq-ext*:

assumes *f-valid*: $\{A\} f \{B\}$
assumes *g-valid*: $\bigwedge x. \{B\ x\} g\ x \{C\}$
shows $\{A\} \text{do } x \leftarrow f; g\ x \text{od} \{C\}$
apply(*insert f-valid g-valid*)
apply(*blast intro: seq-ext*)
done

lemma *seqE'*:

$\llbracket \{A\} f \{B\}, \{E\};$
 $\forall x. \{B\ x\} g\ x \{C\}, \{E\} \rrbracket \implies$
 $\{A\} \text{doE } x \leftarrow f; g\ x \text{odE } \{C\}, \{E\}$
apply(*simp add: bindE-def lift-def bind-def Let-def split-def*)
apply(*clarsimp simp: validE-def2*)
apply (*fastforce simp add: throwError-def return-def lift-def*
split: sum.splits)
done

lemma *seqE*:

assumes *f-valid*: $\{A\} f \{B\}, \{E\}$
assumes *g-valid*: $\bigwedge x. \{B\ x\} g\ x \{C\}, \{E\}$
shows $\{A\} \text{doE } x \leftarrow f; g\ x \text{odE } \{C\}, \{E\}$
apply(*insert f-valid g-valid*)
apply(*blast intro: seqE*)
done

lemma *hoare-TrueI*: $\{P\} f \{\lambda-. \top\}$

by (*simp add: valid-def*)

lemma *hoareE-TrueI*: $\{P\} f \{\lambda-. \top\}, \{\lambda r. \top\}$

by (*simp add: validE-def valid-def*)

lemma *hoare-True-E-R* [*simp*]:

$\{P\} f \{\lambda r\ s. \text{True}\}, -$
by (*auto simp add: validE-R-def validE-def valid-def split: sum.splits*)

lemma *hoare-post-conj* [*intro*]:

$\llbracket \{P\} a \{Q\}; \{P\} a \{R\} \rrbracket \implies \{P\} a \{Q \text{ And } R\}$
by (*fastforce simp: valid-def split-def bipred-conj-def*)

lemma *hoare-pre-disj* [*intro*]:

$\llbracket \{P\} a \{R\}; \{Q\} a \{R\} \rrbracket \implies \{P \text{ or } Q\} a \{R\}$
by (*simp add: valid-def pred-disj-def*)

lemma *hoare-conj*:

$\llbracket \{P\} f \{Q\}; \{P'\} f \{Q'\} \rrbracket \implies \{P \text{ and } P'\} f \{Q \text{ And } Q'\}$
unfolding *valid-def* **by** *auto*

lemma *hoare-post-taut*: $\{ P \} a \{ \top \top \}$
by (*simp add:valid-def*)

lemma *wp-post-taut*: $\{ \lambda r. \text{True} \} f \{ \lambda r s. \text{True} \}$
by (*rule hoare-post-taut*)

lemma *wp-post-tautE*: $\{ \lambda r. \text{True} \} f \{ \lambda r s. \text{True} \}, \{ \lambda f s. \text{True} \}$
proof –
have $P: \bigwedge r. (\text{case } r \text{ of } \text{Inl } a \Rightarrow \text{True} \mid - \Rightarrow \text{True}) = \text{True}$
by (*case-tac r, simp-all*)
show *?thesis*
by (*simp add: validE-def P wp-post-taut*)
qed

lemma *hoare-pre-cont* [*simp*]: $\{ \perp \} a \{ P \}$
by (*simp add:valid-def*)

23.5 Strongest Postcondition Rules

lemma *get-sp*:
 $\{ P \} \text{get } \{ \lambda a s. s = a \wedge P s \}$
by (*simp add:get-def valid-def*)

lemma *put-sp*:
 $\{ \top \} \text{put } a \{ \lambda s. s = a \}$
by (*simp add:put-def valid-def*)

lemma *return-sp*:
 $\{ P \} \text{return } a \{ \lambda b s. b = a \wedge P s \}$
by (*simp add:return-def valid-def*)

lemma *assert-sp*:
 $\{ P \} \text{assert } Q \{ \lambda r s. P s \wedge Q \}$
by (*simp add: assert-def fail-def return-def valid-def*)

lemma *hoare-gets-sp*:
 $\{ P \} \text{gets } f \{ \lambda r v s. rv = f s \wedge P s \}$
by (*simp add: valid-def simplifier-gets-def*)

lemma *hoare-return-drop-var* [*iff*]: $\{ Q \} \text{return } x \{ \lambda r. Q \}$
by (*simp add:valid-def return-def*)

lemma *hoare-gets* [*intro*]: $\llbracket \bigwedge s. P s \implies Q (f s) s \rrbracket \implies \{ P \} \text{gets } f \{ Q \}$
by (*simp add:valid-def gets-def get-def bind-def return-def*)

lemma *hoare-modifyE-var*:
 $\llbracket \bigwedge s. P s \implies Q (f s) \rrbracket \implies \{ P \} \text{modify } f \{ \lambda r s. Q s \}$
by (*simp add: valid-def modify-def put-def get-def bind-def*)

lemma *hoare-if*:

$$\llbracket P \implies \{ Q \} a \{ R \}; \neg P \implies \{ Q \} b \{ R \} \rrbracket \implies$$

$$\{ Q \} \text{ if } P \text{ then } a \text{ else } b \{ R \}$$
by (*simp add: valid-def*)

lemma *hoare-pre-subst*: $\llbracket A = B; \{A\} a \{C\} \rrbracket \implies \{B\} a \{C\}$
by (*clarsimp simp: valid-def split-def*)

lemma *hoare-post-subst*: $\llbracket B = C; \{A\} a \{B\} \rrbracket \implies \{A\} a \{C\}$
by (*clarsimp simp: valid-def split-def*)

lemma *hoare-pre-tautI*: $\llbracket \{A \text{ and } P\} a \{B\}; \{A \text{ and not } P\} a \{B\} \rrbracket \implies \{A\} a \{B\}$
by (*fastforce simp: valid-def split-def pred-conj-def pred-neg-def*)

lemma *hoare-pre-imp*: $\llbracket \bigwedge s. P s \implies Q s; \{Q\} a \{R\} \rrbracket \implies \{P\} a \{R\}$
by (*fastforce simp add: valid-def*)

lemma *hoare-post-imp*: $\llbracket \bigwedge r s. Q r s \implies R r s; \{P\} a \{Q\} \rrbracket \implies \{P\} a \{R\}$
by (*fastforce simp: valid-def split-def*)

lemma *hoare-post-impErr'*: $\llbracket \{P\} a \{Q\}, \{E\};$

$$\forall r s. Q r s \longrightarrow R r s;$$

$$\forall e s. E e s \longrightarrow F e s \rrbracket \implies$$

$$\{P\} a \{R\}, \{F\}$$
apply (*simp add: validE-def*)
apply (*rule-tac Q = $\lambda r s. \text{case } r \text{ of } \text{Inl } a \Rightarrow E a s \mid \text{Inr } b \Rightarrow Q b s$ in hoare-post-imp*)
apply (*case-tac r*)
apply *simp-all*
done

lemma *hoare-post-impErr*: $\llbracket \{P\} a \{Q\}, \{E\};$

$$\bigwedge r s. Q r s \implies R r s;$$

$$\bigwedge e s. E e s \implies F e s \rrbracket \implies$$

$$\{P\} a \{R\}, \{F\}$$
apply (*blast intro: hoare-post-impErr'*)
done

lemma *hoare-validE-cases*:

$$\llbracket \{P\} f \{Q\}, \{ \lambda -. \text{True} \}; \{P\} f \{ \lambda -. \text{True} \}, \{R\} \rrbracket$$

$$\implies \{P\} f \{Q\}, \{R\}$$
by (*simp add: validE-def valid-def split: sum.splits*) *blast*

lemma *hoare-post-imp-dc*:

$$\llbracket \{P\} a \{ \lambda r. Q \}; \bigwedge s. Q s \implies R s \rrbracket \implies \{P\} a \{ \lambda r. R \}, \{ \lambda r. R \}$$
by (*simp add: validE-def valid-def split: sum.splits*) *blast*

lemma *hoare-post-imp-dc2*:

$\llbracket \{P\} a \{\lambda r. Q\}; \bigwedge s. Q s \implies R s \rrbracket \implies \{P\} a \{\lambda r. R\}, \{\lambda r s. True\}$
by (*simp add: validE-def valid-def split: sum.splits*) *blast*

lemma *hoare-post-imp-dc2E*:

$\llbracket \{P\} a \{\lambda r. Q\}; \bigwedge s. Q s \implies R s \rrbracket \implies \{P\} a \{\lambda r s. True\}, \{\lambda r. R\}$
by (*simp add: validE-def valid-def split: sum.splits*) *fast*

lemma *hoare-post-imp-dc2E-actual*:

$\llbracket \{P\} a \{\lambda r. R\} \rrbracket \implies \{P\} a \{\lambda r s. True\}, \{\lambda r. R\}$
by (*simp add: validE-def valid-def split: sum.splits*) *fast*

lemma *hoare-post-imp-dc2-actual*:

$\llbracket \{P\} a \{\lambda r. R\} \rrbracket \implies \{P\} a \{\lambda r. R\}, \{\lambda r s. True\}$
by (*simp add: validE-def valid-def split: sum.splits*) *fast*

lemma *hoare-post-impE*: $\llbracket \bigwedge r s. Q r s \implies R r s; \{P\} a \{Q\} \rrbracket \implies \{P\} a \{R\}$
by (*fastforce simp: valid-def split-def*)

lemma *hoare-conjD1*:

$\{P\} f \{\lambda rv. Q rv \text{ and } R rv\} \implies \{P\} f \{\lambda rv. Q rv\}$
unfolding *valid-def* **by** *auto*

lemma *hoare-conjD2*:

$\{P\} f \{\lambda rv. Q rv \text{ and } R rv\} \implies \{P\} f \{\lambda rv. R rv\}$
unfolding *valid-def* **by** *auto*

lemma *hoare-post-disjI1*:

$\{P\} f \{\lambda rv. Q rv\} \implies \{P\} f \{\lambda rv. Q rv \text{ or } R rv\}$
unfolding *valid-def* **by** *auto*

lemma *hoare-post-disjI2*:

$\{P\} f \{\lambda rv. R rv\} \implies \{P\} f \{\lambda rv. Q rv \text{ or } R rv\}$
unfolding *valid-def* **by** *auto*

lemma *hoare-weaken-pre*:

$\llbracket \{Q\} a \{R\}; \bigwedge s. P s \implies Q s \rrbracket \implies \{P\} a \{R\}$
apply (*rule hoare-pre-imp*)
prefer 2
apply *assumption*
apply *blast*
done

lemma *hoare-strengthen-post*:

$\llbracket \{P\} a \{Q\}; \bigwedge r s. Q r s \implies R r s \rrbracket \implies \{P\} a \{R\}$
apply (*rule hoare-post-imp*)
prefer 2
apply *assumption*
apply *blast*
done

lemma *use-valid*: $\llbracket (r, s') \in \text{fst } (f s); \{P\} f \{Q\}; P s \rrbracket \implies Q r s'$
apply (*simp add: valid-def*)
apply *blast*
done

lemma *use-validE-norm*: $\llbracket (\text{Inr } r', s') \in \text{fst } (B s); \{P\} B \{Q\}, \{E\}; P s \rrbracket \implies Q r' s'$
apply (*clarsimp simp: validE-def valid-def*)
apply *force*
done

lemma *use-validE-except*: $\llbracket (\text{Inl } r', s') \in \text{fst } (B s); \{P\} B \{Q\}, \{E\}; P s \rrbracket \implies E r' s'$
apply (*clarsimp simp: validE-def valid-def*)
apply *force*
done

lemma *in-inv-by-hoareD*:
 $\llbracket \bigwedge P. \{P\} f \{\lambda-. P\}; (x, s') \in \text{fst } (f s) \rrbracket \implies s' = s$
by (*auto simp add: valid-def*) *blast*

23.6 Satisfiability

lemma *exs-hoare-post-imp*: $\llbracket \bigwedge r s. Q r s \implies R r s; \{P\} a \exists \{Q\} \rrbracket \implies \{P\} a \exists \{R\}$
apply (*simp add: exs-valid-def*)
apply *safe*
apply (*erule-tac x=s in allE, simp*)
apply *blast*
done

lemma *use-exs-valid*: $\llbracket \{P\} f \exists \{Q\}; P s \rrbracket \implies \exists (r, s') \in \text{fst } (f s). Q r s'$
by (*simp add: exs-valid-def*)

definition *exs-postcondition* $P f \equiv (\lambda a b. \exists (rv, s) \in f a b. P rv s)$

lemma *exs-valid-is-triple*:
 $\text{exs-valid } P f Q = \text{triple-judgement } P f (\text{exs-postcondition } Q (\lambda s f. \text{fst } (f s)))$
by (*simp add: triple-judgement-def exs-postcondition-def exs-valid-def*)

lemmas [*wp-trip*] = *exs-valid-is-triple*

lemma *exs-valid-weaken-pre*[*wp-pre*]:
 $\llbracket \{P'\} f \exists \{Q\}; \bigwedge s. P s \implies P' s \rrbracket \implies \{P\} f \exists \{Q\}$
apply *atomize*
apply (*clarsimp simp: exs-valid-def*)
done

lemma *exs-valid-chain*:

$$\llbracket \{ P \} f \exists \{ Q \}; \bigwedge s. R s \implies P s; \bigwedge r s. Q r s \implies S r s \rrbracket \implies \{ R \} f \exists \{ S \}$$
apply *atomize*
apply (*fastforce simp: exs-valid-def Bex-def*)
done

lemma *exs-valid-assume-pre*:

$$\llbracket \bigwedge s. P s \implies \{ P \} f \exists \{ Q \} \rrbracket \implies \{ P \} f \exists \{ Q \}$$
apply (*fastforce simp: exs-valid-def*)
done

lemma *exs-valid-bind* [*wp-split*]:

$$\llbracket \bigwedge x. \{ B x \} g x \exists \{ C \}; \{ A \} f \exists \{ B \} \rrbracket \implies \{ A \} f >>= (\lambda x. g x) \exists \{ C \}$$
apply *atomize*
apply (*clarsimp simp: exs-valid-def bind-def'*)
apply *blast*
done

lemma *exs-valid-return* [*wp*]:

$$\{ Q v \} \text{return } v \exists \{ Q \}$$
by (*clarsimp simp: exs-valid-def return-def*)

lemma *exs-valid-select* [*wp*]:

$$\{ \lambda s. \exists r \in S. Q r s \} \text{select } S \exists \{ Q \}$$
by (*clarsimp simp: exs-valid-def select-def*)

lemma *exs-valid-get* [*wp*]:

$$\{ \lambda s. Q s s \} \text{get} \exists \{ Q \}$$
by (*clarsimp simp: exs-valid-def get-def*)

lemma *exs-valid-gets* [*wp*]:

$$\{ \lambda s. Q (f s) s \} \text{gets } f \exists \{ Q \}$$
by (*clarsimp simp: gets-def*) *wp*

lemma *exs-valid-put* [*wp*]:

$$\{ Q v \} \text{put } v \exists \{ Q \}$$
by (*clarsimp simp: put-def exs-valid-def*)

lemma *exs-valid-state-assert* [*wp*]:

$$\{ \lambda s. Q () s \wedge G s \} \text{state-assert } G \exists \{ Q \}$$
by (*clarsimp simp: state-assert-def exs-valid-def get-def assert-def bind-def' return-def*)

lemmas *exs-valid-guard* = *exs-valid-state-assert*

lemma *exs-valid-fail* [*wp*]:

$$\{ \lambda -. \text{False} \} \text{fail} \exists \{ Q \}$$
by (*clarsimp simp: fail-def exs-valid-def*)

lemma *exs-valid-condition* [wp]:

$$\begin{aligned} & \llbracket \{ P \} L \exists \{ Q \}; \{ P' \} R \exists \{ Q \} \rrbracket \implies \\ & \quad \{ \lambda s. (C\ s \wedge P\ s) \vee (\neg C\ s \wedge P'\ s) \} \text{condition } C\ L\ R \exists \{ Q \} \\ & \text{by } (\text{clarsimp simp: condition-def exs-valid-def split: sum.splits}) \end{aligned}$$

23.7 MISC

lemma *hoare-return-simp*:

$$\begin{aligned} & \{ P \} \text{return } x \{ Q \} = (\forall s. P\ s \longrightarrow Q\ x\ s) \\ & \text{by } (\text{simp add: valid-def return-def}) \end{aligned}$$

lemma *hoare-gen-asm*:

$$\begin{aligned} & (P \implies \{ P' \} f \{ Q \}) \implies \{ P' \text{ and } K\ P \} f \{ Q \} \\ & \text{by } (\text{fastforce simp add: valid-def}) \end{aligned}$$

lemma *hoare-gen-asm-lk*:

$$\begin{aligned} & (P \implies \{ P' \} f \{ Q \}) \implies \{ K\ P \text{ and } P' \} f \{ Q \} \\ & \text{by } (\text{fastforce simp add: valid-def}) \end{aligned}$$

— Useful for forward reasoning, when P is known. The first version allows weakening the precondition.

lemma *hoare-gen-asm-spec'*:

$$\begin{aligned} & (\bigwedge s. P\ s \implies S \wedge R\ s) \\ & \implies (S \implies \{ R \} f \{ Q \}) \\ & \implies \{ P \} f \{ Q \} \\ & \text{by } (\text{fastforce simp: valid-def}) \end{aligned}$$

lemma *hoare-gen-asm-spec*:

$$\begin{aligned} & (\bigwedge s. P\ s \implies S) \\ & \implies (S \implies \{ P \} f \{ Q \}) \\ & \implies \{ P \} f \{ Q \} \\ & \text{by } (\text{rule hoare-gen-asm-spec' [where } S=S \text{ and } R=P]) \text{ simp} \end{aligned}$$

lemma *hoare-conjI*:

$$\begin{aligned} & \llbracket \{ P \} f \{ Q \}; \{ P \} f \{ R \} \rrbracket \implies \{ P \} f \{ \lambda r\ s. Q\ r\ s \wedge R\ r\ s \} \\ & \text{unfolding valid-def by blast} \end{aligned}$$

lemma *hoare-disjI1*:

$$\begin{aligned} & \llbracket \{ P \} f \{ Q \} \rrbracket \implies \{ P \} f \{ \lambda r\ s. Q\ r\ s \vee R\ r\ s \} \\ & \text{unfolding valid-def by blast} \end{aligned}$$

lemma *hoare-disjI2*:

$$\begin{aligned} & \llbracket \{ P \} f \{ R \} \rrbracket \implies \{ P \} f \{ \lambda r\ s. Q\ r\ s \vee R\ r\ s \} \\ & \text{unfolding valid-def by blast} \end{aligned}$$

lemma *hoare-assume-pre*:

$$\begin{aligned} & (\bigwedge s. P\ s \implies \{ P \} f \{ Q \}) \implies \{ P \} f \{ Q \} \\ & \text{by } (\text{auto simp: valid-def}) \end{aligned}$$

lemma *hoare-returnOk-sp*:

$\{P\} \text{returnOk } x \{ \lambda r \ s. \ r = x \wedge P \ s \}, \{Q\}$
by (*simp add: valid-def validE-def returnOk-def return-def*)

lemma *hoare-assume-preE*:

$(\bigwedge s. P \ s \implies \{P\} \ f \ \{Q\}, \{R\}) \implies \{P\} \ f \ \{Q\}, \{R\}$
by (*auto simp: valid-def validE-def*)

lemma *hoare-allI*:

$(\bigwedge x. \{P\} \ f \ \{Q \ x\}) \implies \{P\} \ f \ \{ \lambda r \ s. \ \forall x. \ Q \ x \ r \ s \}$
by (*simp add: valid-def*) *blast*

lemma *validE-allI*:

$(\bigwedge x. \{P\} \ f \ \{ \lambda r \ s. \ Q \ x \ r \ s \}, \{E\}) \implies \{P\} \ f \ \{ \lambda r \ s. \ \forall x. \ Q \ x \ r \ s \}, \{E\}$
by (*fastforce simp: valid-def validE-def split: sum.splits*)

lemma *hoare-exI*:

$\{P\} \ f \ \{Q \ x\} \implies \{P\} \ f \ \{ \lambda r \ s. \ \exists x. \ Q \ x \ r \ s \}$
by (*simp add: valid-def*) *blast*

lemma *hoare-impI*:

$(R \implies \{P\} \ f \ \{Q\}) \implies \{P\} \ f \ \{ \lambda r \ s. \ R \longrightarrow Q \ r \ s \}$
by (*simp add: valid-def*) *blast*

lemma *validE-impI*:

$\llbracket \bigwedge E. \{P\} \ f \ \{ \lambda - \ . \ True \}, \{E\}; (P' \implies \{P\} \ f \ \{Q\}, \{E\}) \rrbracket \implies$
 $\{P\} \ f \ \{ \lambda r \ s. \ P' \longrightarrow Q \ r \ s \}, \{E\}$
by (*fastforce simp: validE-def valid-def split: sum.splits*)

lemma *hoare-case-option-wp*:

$\llbracket \{P\} \ f \ None \ \{Q\};$
 $\bigwedge x. \ \{P' \ x\} \ f \ (Some \ x) \ \{Q' \ x\} \rrbracket$
 $\implies \{case-option \ P \ P' \ v\} \ f \ v \ \{ \lambda rv. \ case \ v \ of \ None \Rightarrow Q \ rv \mid Some \ x \Rightarrow Q' \ x \ rv \}$
by (*cases v*) *auto*

23.8 Reasoning directly about states

lemma *in-throwError*:

$((v, s') \in fst \ (throwError \ e \ s)) = (v = Inl \ e \wedge s' = s)$
by (*simp add: throwError-def return-def*)

lemma *in-returnOk*:

$((v', s') \in fst \ (returnOk \ v \ s)) = (v' = Inr \ v \wedge s' = s)$
by (*simp add: returnOk-def return-def*)

lemma *in-bind*:

$((r, s') \in fst \ ((do \ x \leftarrow f; \ g \ x \ od) \ s)) =$
 $(\exists s'' \ x. (x, s'') \in fst \ (f \ s) \wedge (r, s') \in fst \ (g \ x \ s''))$
apply (*simp add: bind-def split-def*)

apply *force*
done

lemma *in-bindE-R*:

$((\text{Inr } r, s') \in \text{fst } ((\text{doE } x \leftarrow f; g \ x \text{ odE } s))) =$
 $(\exists s'' x. (\text{Inr } x, s'') \in \text{fst } (f \ s) \wedge (\text{Inr } r, s') \in \text{fst } (g \ x \ s''))$
apply (*simp add: bindE-def lift-def split-def bind-def*)
apply (*clarsimp simp: throwError-def return-def lift-def split: sum.splits*)
apply *safe*
apply (*case-tac a*)
apply *fastforce*
apply *fastforce*
apply *force*
done

lemma *in-bindE-L*:

$((\text{Inl } r, s') \in \text{fst } ((\text{doE } x \leftarrow f; g \ x \text{ odE } s))) \implies$
 $(\exists s'' x. (\text{Inr } x, s'') \in \text{fst } (f \ s) \wedge (\text{Inl } r, s') \in \text{fst } (g \ x \ s'')) \vee ((\text{Inl } r, s') \in \text{fst } (f \ s))$
apply (*simp add: bindE-def lift-def bind-def*)
apply *safe*
apply (*simp add: return-def throwError-def lift-def split-def split: sum.splits if-split-asm*)
apply *force*
done

lemma *in-liftE*:

$((v, s') \in \text{fst } (\text{liftE } f \ s)) = (\exists v'. v = \text{Inr } v' \wedge (v', s') \in \text{fst } (f \ s))$
by (*force simp add: liftE-def bind-def return-def split-def*)

lemma *in-whenE*: $((v, s') \in \text{fst } (\text{whenE } P \ f \ s)) = ((P \longrightarrow (v, s') \in \text{fst } (f \ s)) \wedge (\neg P \longrightarrow v = \text{Inr } () \wedge s' = s))$
by (*simp add: whenE-def in-returnOk*)

lemma *inl-whenE*:

$((\text{Inl } x, s') \in \text{fst } (\text{whenE } P \ f \ s)) = (P \wedge (\text{Inl } x, s') \in \text{fst } (f \ s))$
by (*auto simp add: in-whenE*)

lemma *inr-in-unlessE-throwError[termination-simp]*:

$(\text{Inr } (), s') \in \text{fst } (\text{unlessE } P \ (\text{throwError } E) \ s) = (P \wedge s' = s)$
by (*simp add: unlessE-def returnOk-def throwError-def return-def*)

lemma *in-fail*:

$r \in \text{fst } (\text{fail } s) = \text{False}$
by (*simp add: fail-def*)

lemma *in-return*:

$(r, s') \in \text{fst } (\text{return } v \ s) = (r = v \wedge s' = s)$
by (*simp add: return-def*)

lemma *in-assert*:

$(r, s') \in \text{fst } (\text{assert } P \ s) = (P \wedge s' = s)$
by (*simp add: assert-def return-def fail-def*)

lemma *in-assertE*:

$(r, s') \in \text{fst } (\text{assertE } P \ s) = (P \wedge r = \text{Inr } () \wedge s' = s)$
by (*simp add: assertE-def returnOk-def return-def fail-def*)

lemma *in-assert-opt*:

$(r, s') \in \text{fst } (\text{assert-opt } v \ s) = (v = \text{Some } r \wedge s' = s)$
by (*auto simp: assert-opt-def in-fail in-return split: option.splits*)

lemma *in-get*:

$(r, s') \in \text{fst } (\text{get } s) = (r = s \wedge s' = s)$
by (*simp add: get-def*)

lemma *in-gets*:

$(r, s') \in \text{fst } (\text{gets } f \ s) = (r = f \ s \wedge s' = s)$
by (*simp add: simpler-gets-def*)

lemma *in-put*:

$(r, s') \in \text{fst } (\text{put } x \ s) = (s' = x \wedge r = ())$
by (*simp add: put-def*)

lemma *in-when*:

$(v, s') \in \text{fst } (\text{when } P \ f \ s) = ((P \longrightarrow (v, s') \in \text{fst } (f \ s)) \wedge (\neg P \longrightarrow v = () \wedge s' = s))$
by (*simp add: when-def in-return*)

lemma *in-modify*:

$(v, s') \in \text{fst } (\text{modify } f \ s) = (s' = f \ s \wedge v = ())$
by (*simp add: modify-def bind-def get-def put-def*)

lemma *gets-the-in-monad*:

$((v, s') \in \text{fst } (\text{gets-the } f \ s)) = (s' = s \wedge f \ s = \text{Some } v)$
by (*auto simp: gets-the-def in-bind in-gets in-assert-opt split: option.split*)

lemma *in-alternative*:

$(r, s') \in \text{fst } ((f \sqcap g) \ s) = ((r, s') \in \text{fst } (f \ s) \vee (r, s') \in \text{fst } (g \ s))$
by (*simp add: alternative-def*)

lemmas *in-monad = inl-whenE in-whenE in-liftE in-bind in-bindE-L*

in-bindE-R in-returnOk in-throwError in-fail
in-assertE in-assert in-return in-assert-opt
in-get in-gets in-put in-when unlessE-whenE
unless-when in-modify gets-the-in-monad
in-alternative

23.9 Non-Failure

lemma *no-failD*:

$\llbracket \text{no-fail } P \text{ m}; P \text{ s} \rrbracket \implies \neg(\text{snd } (m \text{ s}))$
by (*simp add: no-fail-def*)

lemma *non-fail-modify* [*wp, simp*]:

no-fail \top (*modify f*)
by (*simp add: no-fail-def modify-def get-def put-def bind-def*)

lemma *non-fail-gets-simp*[*simp*]:

no-fail *P* (*gets f*)
unfolding *no-fail-def gets-def get-def return-def bind-def*
by *simp*

lemma *non-fail-gets*:

no-fail \top (*gets f*)
by *simp*

lemma *non-fail-select* [*simp*]:

no-fail \top (*select S*)
by (*simp add: no-fail-def select-def*)

lemma *no-fail-pre*:

$\llbracket \text{no-fail } P \text{ f}; \bigwedge s. Q \text{ s} \implies P \text{ s} \rrbracket \implies \text{no-fail } Q \text{ f}$
by (*simp add: no-fail-def*)

lemma *no-fail-alt* [*wp*]:

$\llbracket \text{no-fail } P \text{ f}; \text{no-fail } Q \text{ g} \rrbracket \implies \text{no-fail } (P \text{ and } Q) (f \text{ OR } g)$
by (*simp add: no-fail-def alternative-def*)

lemma *no-fail-return* [*simp, wp*]:

no-fail \top (*return x*)
by (*simp add: return-def no-fail-def*)

lemma *no-fail-get* [*simp, wp*]:

no-fail \top *get*
by (*simp add: get-def no-fail-def*)

lemma *no-fail-put* [*simp, wp*]:

no-fail \top (*put s*)
by (*simp add: put-def no-fail-def*)

lemma *no-fail-when* [*wp*]:

$(P \implies \text{no-fail } Q \text{ f}) \implies \text{no-fail } (\text{if } P \text{ then } Q \text{ else } \top) (\text{when } P \text{ f})$
by (*simp add: when-def*)

lemma *no-fail-unless* [*wp*]:

$(\neg P \implies \text{no-fail } Q \text{ f}) \implies \text{no-fail } (\text{if } P \text{ then } \top \text{ else } Q) (\text{unless } P \text{ f})$
by (*simp add: unless-def when-def*)

```

lemma no-fail-fail [simp, wp]:
  no-fail  $\perp$  fail
  by (simp add: fail-def no-fail-def)

lemmas [wp] = non-fail-gets

lemma no-fail-assert [simp, wp]:
  no-fail ( $\lambda\cdot$ . P) (assert P)
  by (simp add: assert-def)

lemma no-fail-assert-opt [simp, wp]:
  no-fail ( $\lambda\cdot$ . P  $\neq$  None) (assert-opt P)
  by (simp add: assert-opt-def split: option.splits)

lemma no-fail-case-option [wp]:
  assumes f: no-fail P f
  assumes g:  $\bigwedge x$ . no-fail (Q x) (g x)
  shows no-fail (if x = None then P else Q (the x)) (case-option f g x)
  by (clarsimp simp add: f g)

lemma no-fail-if [wp]:
   $\llbracket P \implies \text{no-fail } Q \text{ f}; \neg P \implies \text{no-fail } R \text{ g} \rrbracket \implies$ 
  no-fail (if P then Q else R) (if P then f else g)
  by simp

lemma no-fail-apply [wp]:
  no-fail P (f (g x))  $\implies$  no-fail P (f $ g x)
  by simp

lemma no-fail-undefined [simp, wp]:
  no-fail  $\perp$  undefined
  by (simp add: no-fail-def)

lemma no-fail-returnOK [simp, wp]:
  no-fail  $\top$  (returnOk x)
  by (simp add: returnOk-def)

lemma no-fail-bind [wp]:
  assumes f: no-fail P f
  assumes g:  $\bigwedge rv$ . no-fail (R rv) (g rv)
  assumes v:  $\llbracket Q \rrbracket f \llbracket R \rrbracket$ 
  shows no-fail (P and Q) (f >>= ( $\lambda rv$ . g rv))
  apply (clarsimp simp: no-fail-def bind-def)
  apply (rule conjI)
  prefer 2
  apply (erule no-failD [OF f])
  apply clarsimp
  apply (drule (1) use-valid [OF - v])

```

```

apply (drule no-failD [OF g])
apply simp
done

```

Empty results implies non-failure

```

lemma empty-fail-modify [simp, wp]:
  empty-fail (modify f)
by (simp add: empty-fail-def simplifier-modify-def)

```

```

lemma empty-fail-gets [simp, wp]:
  empty-fail (gets f)
by (simp add: empty-fail-def simplifier-gets-def)

```

```

lemma empty-failD:
   $\llbracket \text{empty-fail } m; \text{fst } (m \ s) = \{\} \rrbracket \implies \text{snd } (m \ s)$ 
by (simp add: empty-fail-def)

```

```

lemma empty-fail-select-f [simp]:
  assumes ef:  $\text{fst } S = \{\} \implies \text{snd } S$ 
  shows empty-fail (select-f S)
by (fastforce simp add: empty-fail-def select-f-def intro: ef)

```

```

lemma empty-fail-bind [simp]:
   $\llbracket \text{empty-fail } a; \bigwedge x. \text{empty-fail } (b \ x) \rrbracket \implies \text{empty-fail } (a \ >=> \ b)$ 
apply (simp add: bind-def empty-fail-def split-def)
apply clarsimp
apply (case-tac fst (a \ s) = \{\})
apply blast
apply (clarsimp simp: ex-in-conv [symmetric])
done

```

```

lemma empty-fail-return [simp, wp]:
  empty-fail (return x)
by (simp add: empty-fail-def return-def)

```

```

lemma empty-fail-mapM [simp]:
  assumes m:  $\bigwedge x. \text{empty-fail } (m \ x)$ 
  shows empty-fail (mapM m xs)
proof (induct xs)
  case Nil
  thus ?case by (simp add: mapM-def sequence-def)
next
  case Cons
  have P:  $\bigwedge m \ x \ xs. \text{mapM } m \ (x \ \# \ xs) = (\text{do } y \leftarrow m \ x; \text{ys} \leftarrow (\text{mapM } m \ xs);$ 
   $\text{return } (y \ \# \ \text{ys}) \text{ od})$ 
  by (simp add: mapM-def sequence-def Let-def)
  from Cons
  show ?case by (simp add: P m)
qed

```

```

lemma empty-fail [simp]:
  empty-fail fail
  by (simp add: fail-def empty-fail-def)

lemma empty-fail-assert-opt [simp]:
  empty-fail (assert-opt x)
  by (simp add: assert-opt-def split: option.splits)

lemma empty-fail-mk-ef:
  empty-fail (mk-ef o m)
  by (simp add: empty-fail-def mk-ef-def)

lemma empty-fail-gets-map[simp]:
  empty-fail (gets-map f p)
  unfolding gets-map-def by simp

```

23.10 Failure

```

lemma fail-wp:  $\{\lambda x. \text{True}\} \text{fail} \{Q\}$ 
  by (simp add: valid-def fail-def)

lemma failE-wp:  $\{\lambda x. \text{True}\} \text{fail} \{Q\}, \{E\}$ 
  by (simp add: validE-def fail-wp)

lemma fail-update [iff]:
  fail (f s) = fail s
  by (simp add: fail-def)

```

We can prove postconditions using hoare triples

```

lemma post-by-hoare:  $\llbracket \{P\} f \{Q\}; P \ s; (r, \ s') \in \text{fst} \ (f \ s) \rrbracket \implies Q \ r \ s'$ 
  apply (simp add: valid-def)
  apply blast
  done

```

Weakest Precondition Rules

```

lemma hoare-vcg-prop:
   $\{\lambda s. P\} f \{\lambda rv \ s. P\}$ 
  by (simp add: valid-def)

lemma return-wp:
   $\{P \ x\} \text{return } x \{P\}$ 
  by(simp add:valid-def return-def)

lemma get-wp:
   $\{\lambda s. P \ s \ s\} \text{get} \{P\}$ 
  by(simp add:valid-def split-def get-def)

lemma gets-wp:

```

$\{\lambda s. P (f s) s\} \text{ gets } f \{P\}$
by(simp add:valid-def split-def gets-def return-def get-def bind-def)

lemma modify-wp:
 $\{\lambda s. P () (f s)\} \text{ modify } f \{P\}$
by(simp add:valid-def split-def modify-def get-def put-def bind-def)

lemma put-wp:
 $\{\lambda s. P () x\} \text{ put } x \{P\}$
by(simp add:valid-def put-def)

lemma returnOk-wp:
 $\{P x\} \text{ returnOk } x \{P\}, \{E\}$
by(simp add:validE-def2 returnOk-def return-def)

lemma throwError-wp:
 $\{E e\} \text{ throwError } e \{P\}, \{E\}$
by(simp add:validE-def2 throwError-def return-def)

lemma returnOKE-R-wp : $\{P x\} \text{ returnOk } x \{P\}, -$
by (simp add: validE-R-def validE-def valid-def returnOk-def return-def)

lemma liftE-wp:
 $\{P\} f \{Q\} \implies \{P\} \text{ liftE } f \{Q\}, \{E\}$
by(clarsimp simp:valid-def validE-def2 liftE-def split-def Let-def bind-def return-def)

lemma catch-wp:
 $\llbracket \bigwedge x. \{E x\} \text{ handler } x \{Q\}; \{P\} f \{Q\}, \{E\} \rrbracket \implies$
 $\{P\} \text{ catch } f \text{ handler } \{Q\}$
apply (unfold catch-def valid-def validE-def return-def)
apply (fastforce simp: bind-def split: sum.splits)
done

lemma handleE'-wp:
 $\llbracket \bigwedge x. \{F x\} \text{ handler } x \{Q\}, \{E\}; \{P\} f \{Q\}, \{F\} \rrbracket \implies$
 $\{P\} f <\text{handle2}> \text{ handler } \{Q\}, \{E\}$
apply (unfold handleE'-def valid-def validE-def return-def)
apply (fastforce simp: bind-def split: sum.splits)
done

lemma handleE-wp:
assumes $x: \bigwedge x. \{F x\} \text{ handler } x \{Q\}, \{E\}$
assumes $y: \{P\} f \{Q\}, \{F\}$
shows $\{P\} f <\text{handle}> \text{ handler } \{Q\}, \{E\}$
by (simp add: handleE-def handleE'-wp [OF x y])

lemma hoare-vcg-if-split:
 $\llbracket P \implies \{Q\} f \{S\}; \neg P \implies \{R\} g \{S\} \rrbracket \implies$
 $\{\lambda s. (P \longrightarrow Q s) \wedge (\neg P \longrightarrow R s)\} \text{ if } P \text{ then } f \text{ else } g \{S\}$

by *simp*

lemma *hoare-vcg-if-splitE*:

$\llbracket P \implies \{Q\} f \{S\}, \{E\}; \neg P \implies \{R\} g \{S\}, \{E\} \rrbracket \implies$
 $\{ \lambda s. (P \longrightarrow Q s) \wedge (\neg P \longrightarrow R s) \} \text{ if } P \text{ then } f \text{ else } g \{S\}, \{E\}$
 by *simp*

lemma *hoare-liftM-subst*: $\{P\} \text{ liftM } f m \{Q\} = \{P\} m \{Q \circ f\}$

apply (*simp add: liftM-def bind-def return-def split-def*)

apply (*simp add: valid-def Ball-def*)

apply (*rule-tac f=All in arg-cong*)

apply (*rule ext*)

apply *fastforce*

done

lemma *liftE-validE[simp]*: $\{P\} \text{ liftE } f \{Q\}, \{E\} = \{P\} f \{Q\}$

apply (*simp add: liftE-liftM validE-def hoare-liftM-subst o-def*)

done

lemma *liftM-wp*: $\{P\} m \{Q \circ f\} \implies \{P\} \text{ liftM } f m \{Q\}$

by (*simp add: hoare-liftM-subst*)

lemma *hoare-liftME-subst*: $\{P\} \text{ liftME } f m \{Q\}, \{E\} = \{P\} m \{Q \circ f\}, \{E\}$

apply (*simp add: validE-def liftME-liftM hoare-liftM-subst o-def*)

apply (*rule-tac f=valid P m in arg-cong*)

apply (*rule ext*)+

apply (*case-tac x, simp-all*)

done

lemma *liftME-wp*: $\{P\} m \{Q \circ f\}, \{E\} \implies \{P\} \text{ liftME } f m \{Q\}, \{E\}$

by (*simp add: hoare-liftME-subst*)

lemma *o-const-simp[simp]*: $(\lambda x. C) \circ f = (\lambda x. C)$

by (*simp add: o-def*)

lemma *hoare-vcg-split-case-option*:

$\llbracket \bigwedge x. x = \text{None} \implies \{P x\} f x \{R x\};$
 $\bigwedge x y. x = \text{Some } y \implies \{Q x y\} g x y \{R x\} \rrbracket \implies$
 $\{ \lambda s. (x = \text{None} \longrightarrow P x s) \wedge$
 $(\forall y. x = \text{Some } y \longrightarrow Q x y s) \}$
case x of None \Rightarrow f x
 $\mid \text{Some } y \Rightarrow g x y$
 $\{R x\}$

apply(*simp add:valid-def split-def*)

apply(*case-tac x, simp-all*)

done

lemma *hoare-vcg-split-case-optionE*:

assumes *none-case*: $\bigwedge x. x = \text{None} \implies \{P\ x\} f\ x\ \{R\ x\}, \{E\ x\}$
assumes *some-case*: $\bigwedge x\ y. x = \text{Some } y \implies \{Q\ x\ y\} g\ x\ y\ \{R\ x\}, \{E\ x\}$
shows $\{ \lambda s. (x = \text{None} \longrightarrow P\ x\ s) \wedge$
 $\quad (\forall y. x = \text{Some } y \longrightarrow Q\ x\ y\ s) \}$
 $\quad \text{case } x \text{ of } \text{None} \Rightarrow f\ x$
 $\quad \quad | \text{Some } y \Rightarrow g\ x\ y$
 $\quad \{R\ x\}, \{E\ x\}$
apply(*case-tac* *x*, *simp-all*)
apply(*rule none-case*, *simp*)
apply(*rule some-case*, *simp*)
done

lemma *hoare-vcg-split-case-sum*:
 $\llbracket \bigwedge x\ a. x = \text{Inl } a \implies \{P\ x\ a\} f\ x\ a\ \{R\ x\};$
 $\quad \bigwedge x\ b. x = \text{Inr } b \implies \{Q\ x\ b\} g\ x\ b\ \{R\ x\} \rrbracket \implies$
 $\{ \lambda s. (\forall a. x = \text{Inl } a \longrightarrow P\ x\ a\ s) \wedge$
 $\quad (\forall b. x = \text{Inr } b \longrightarrow Q\ x\ b\ s) \}$
 $\quad \text{case } x \text{ of } \text{Inl } a \Rightarrow f\ x\ a$
 $\quad \quad | \text{Inr } b \Rightarrow g\ x\ b$
 $\quad \{R\ x\}$
apply(*simp add:valid-def split-def*)
apply(*case-tac* *x*, *simp-all*)
done

lemma *hoare-vcg-split-case-sumE*:
assumes *left-case*: $\bigwedge x\ a. x = \text{Inl } a \implies \{P\ x\ a\} f\ x\ a\ \{R\ x\}$
assumes *right-case*: $\bigwedge x\ b. x = \text{Inr } b \implies \{Q\ x\ b\} g\ x\ b\ \{R\ x\}$
shows $\{ \lambda s. (\forall a. x = \text{Inl } a \longrightarrow P\ x\ a\ s) \wedge$
 $\quad (\forall b. x = \text{Inr } b \longrightarrow Q\ x\ b\ s) \}$
 $\quad \text{case } x \text{ of } \text{Inl } a \Rightarrow f\ x\ a$
 $\quad \quad | \text{Inr } b \Rightarrow g\ x\ b$
 $\quad \{R\ x\}$
apply(*case-tac* *x*, *simp-all*)
apply(*rule left-case*, *simp*)
apply(*rule right-case*, *simp*)
done

lemma *hoare-vcg-precond-imp*:
 $\llbracket \{Q\} f\ \{R\}; \bigwedge s. P\ s \implies Q\ s \rrbracket \implies \{P\} f\ \{R\}$
by (*fastforce simp add:valid-def*)

lemma *hoare-vcg-precond-impE*:
 $\llbracket \{Q\} f\ \{R\}, \{E\}; \bigwedge s. P\ s \implies Q\ s \rrbracket \implies \{P\} f\ \{R\}, \{E\}$
by (*fastforce simp add:validE-def2*)

lemma *hoare-seq-ext*:
assumes *g-valid*: $\bigwedge x. \{B\ x\} g\ x\ \{C\}$
assumes *f-valid*: $\{A\} f\ \{B\}$
shows $\{A\} \text{do } x \leftarrow f; g\ x \text{od } \{C\}$


```

apply(insert f-valid g-valid)
apply(blast intro: seq-ext')
done

```

```

lemma hoare-vcg-seqE:
  assumes g-valid:  $\bigwedge x. \{B\ x\} \ g\ x\ \{C\}, \{E\}$ 
  assumes f-valid:  $\{A\} \ f\ \{B\}, \{E\}$ 
  shows  $\{A\} \ doE\ x \leftarrow f; \ g\ x \ odE\ \{C\}, \{E\}$ 
  apply(insert f-valid g-valid)
  apply(blast intro: seqE')
done

```

```

lemma hoare-seq-ext-nobind:
   $\llbracket \{B\} \ g\ \{C\};$ 
   $\{A\} \ f\ \{\lambda r\ s. B\ s\} \rrbracket \implies$ 
   $\{A\} \ do\ f; \ g\ od\ \{C\}$ 
  apply (clarsimp simp: valid-def bind-def Let-def split-def)
  apply fastforce
done

```

```

lemma hoare-seq-ext-nobindE:
   $\llbracket \{B\} \ g\ \{C\}, \{E\};$ 
   $\{A\} \ f\ \{\lambda r\ s. B\ s\}, \{E\} \rrbracket \implies$ 
   $\{A\} \ doE\ f; \ g\ odE\ \{C\}, \{E\}$ 
  apply (clarsimp simp: validE-def)
  apply (simp add: bindE-def Let-def split-def bind-def lift-def)
  apply (fastforce simp add: valid-def throwError-def return-def lift-def
    split: sum.splits)
done

```

```

lemma hoare-chain:
   $\llbracket \{P\} \ f\ \{Q\};$ 
   $\bigwedge s. R\ s \implies P\ s;$ 
   $\bigwedge r\ s. Q\ r\ s \implies S\ r\ s \rrbracket \implies$ 
   $\{R\} \ f\ \{S\}$ 
  by(fastforce simp add: valid-def split-def)

```

```

lemma validE-weaken:
   $\llbracket \{P'\} \ A\ \{Q'\}, \{E'\}; \bigwedge s. P\ s \implies P'\ s; \bigwedge r\ s. Q'\ r\ s \implies Q\ r\ s; \bigwedge r\ s. E'\ r\ s$ 
   $\implies E\ r\ s \rrbracket \implies \{P\} \ A\ \{Q\}, \{E\}$ 
  by (fastforce simp: validE-def2 split: sum.splits)

```

lemmas *hoare-chainE* = *validE-weaken*

```

lemma hoare-vcg-handle-elseE:
   $\llbracket \{P\} \ f\ \{Q\}, \{E\};$ 
   $\bigwedge e. \{E\ e\} \ g\ e\ \{R\}, \{F\};$ 
   $\bigwedge x. \{Q\ x\} \ h\ x\ \{R\}, \{F\} \rrbracket \implies$ 
   $\{P\} \ f\ <handle> \ g\ <else> \ h\ \{R\}, \{F\}$ 

```

```

apply (simp add: handle-elseE-def validE-def)
apply (rule seq-ext)
apply assumption
apply (case-tac x, simp-all)
done

lemma alternative-valid:
  assumes x:  $\{P\} f \{Q\}$ 
  assumes y:  $\{P\} f' \{Q\}$ 
  shows  $\{P\} f \text{ OR } f' \{Q\}$ 
  apply (simp add: valid-def alternative-def)
  apply safe
  apply (simp add: post-by-hoare [OF x])
  apply (simp add: post-by-hoare [OF y])
  done

lemma alternative-wp:
  assumes x:  $\{P\} f \{Q\}$ 
  assumes y:  $\{P'\} f' \{Q\}$ 
  shows  $\{P \text{ and } P'\} f \text{ OR } f' \{Q\}$ 
  apply (rule alternative-valid)
  apply (rule hoare-pre-imp [OF - x], simp)
  apply (rule hoare-pre-imp [OF - y], simp)
  done

lemma alternativeE-wp:
  assumes x:  $\{P\} f \{Q\}, \{E\}$  and y:  $\{P'\} f' \{Q\}, \{E\}$ 
  shows  $\{P \text{ and } P'\} f \text{ OR } f' \{Q\}, \{E\}$ 
  apply (unfold validE-def)
  apply (wp add: x y alternative-wp | simp | fold validE-def)+
  done

lemma alternativeE-R-wp:
   $\llbracket \{P\} f \{Q\}, -; \{P'\} f' \{Q\}, - \rrbracket \implies \{P \text{ and } P'\} f \text{ OR } f' \{Q\}, -$ 
  apply (simp add: validE-R-def)
  apply (rule alternativeE-wp)
  apply assumption+
  done

lemma alternative-R-wp:
   $\llbracket \{P\} f -, \{Q\}; \{P'\} g -, \{Q\} \rrbracket \implies \{P \text{ and } P'\} f \sqcap g -, \{Q\}$ 
  by (fastforce simp: alternative-def validE-E-def validE-def valid-def)

lemma select-wp:  $\{\lambda s. \forall x \in S. Q x s\} \text{ select } S \{Q\}$ 
  by (simp add: select-def valid-def)

lemma select-f-wp:
   $\{\lambda s. \forall x \in \text{fst } S. Q x s\} \text{ select-f } S \{Q\}$ 
  by (simp add: select-f-def valid-def)

```

lemma *state-select-wp* [wp]: $\llbracket \lambda s. \forall t. (s, t) \in f \longrightarrow P () t \rrbracket \text{state-select } f \llbracket P \rrbracket$
apply (clarsimp simp: state-select-def)
apply (clarsimp simp: valid-def)
done

lemma *condition-wp* [wp]:
 $\llbracket \llbracket Q \rrbracket A \llbracket P \rrbracket; \llbracket R \rrbracket B \llbracket P \rrbracket \rrbracket \Longrightarrow \llbracket \lambda s. \text{if } C \text{ then } Q \text{ else } R \rrbracket \text{condition}$
 $C \ A \ B \llbracket P \rrbracket$
apply (clarsimp simp: condition-def)
apply (clarsimp simp: valid-def pred-conj-def pred-neg-def split-def)
done

lemma *conditionE-wp* [wp]:
 $\llbracket \llbracket P \rrbracket A \llbracket Q \rrbracket, \llbracket R \rrbracket; \llbracket P' \rrbracket B \llbracket Q \rrbracket, \llbracket R \rrbracket \rrbracket \Longrightarrow \llbracket \lambda s. \text{if } C \text{ then } P \text{ else } P' \rrbracket \text{condition } C \ A \ B \llbracket Q \rrbracket, \llbracket R \rrbracket$
apply (clarsimp simp: condition-def)
apply (clarsimp simp: validE-def valid-def)
done

lemma *state-assert-wp* [wp]: $\llbracket \lambda s. f \ s \longrightarrow P () \ s \rrbracket \text{state-assert } f \llbracket P \rrbracket$
apply (clarsimp simp: state-assert-def get-def
assert-def bind-def valid-def return-def fail-def)
done

The weakest precondition handler which works on conjunction

lemma *hoare-vcg-conj-lift*:
assumes $x: \llbracket P \rrbracket f \llbracket Q \rrbracket$
assumes $y: \llbracket P' \rrbracket f \llbracket Q' \rrbracket$
shows $\llbracket \lambda s. P \ s \wedge P' \ s \rrbracket f \llbracket \lambda r v \ s. Q \ r v \ s \wedge Q' \ r v \ s \rrbracket$
apply (subst bipred-conj-def[symmetric], rule hoare-post-conj)
apply (rule hoare-pre-imp [OF - x], simp)
apply (rule hoare-pre-imp [OF - y], simp)
done

lemma *hoare-vcg-conj-liftE1*:
 $\llbracket \llbracket P \rrbracket f \llbracket Q \rrbracket, -; \llbracket P' \rrbracket f \llbracket Q' \rrbracket, \llbracket E \rrbracket \rrbracket \Longrightarrow$
 $\llbracket P \text{ and } P' \rrbracket f \llbracket \lambda r \ s. Q \ r \ s \wedge Q' \ r \ s \rrbracket, \llbracket E \rrbracket$
unfolding valid-def validE-R-def validE-def
apply (clarsimp simp: split-def split: sum.splits)
apply (erule allE, erule (1) impE)
apply (erule allE, erule (1) impE)
apply (drule (1) bspec)
apply (drule (1) bspec)
apply clarsimp
done

lemma *hoare-vcg-disj-lift*:
assumes $x: \llbracket P \rrbracket f \llbracket Q \rrbracket$

```

assumes  $y: \{P'\} f \{Q'\}$ 
shows  $\{\lambda s. P\ s \vee P'\ s\} f \{\lambda rv\ s. Q\ rv\ s \vee Q'\ rv\ s\}$ 
apply (simp add: valid-def)
apply safe
apply (erule(1) post-by-hoare [OF x])
apply (erule notE)
apply (erule(1) post-by-hoare [OF y])
done

```

lemma *hoare-vcg-const-Ball-lift*:

```

 $\llbracket \bigwedge x. x \in S \implies \{P\ x\} f \{Q\ x\}, - \rrbracket \implies \{\lambda s. \forall x \in S. P\ x\ s\} f \{\lambda rv\ s. \forall x \in S. Q\ x\ rv\ s\}$ 
by (fastforce simp: valid-def)

```

lemma *hoare-vcg-const-Ball-lift-R*:

```

 $\llbracket \bigwedge x. x \in S \implies \{P\ x\} f \{Q\ x\}, - \rrbracket \implies$ 
 $\{\lambda s. \forall x \in S. P\ x\ s\} f \{\lambda rv\ s. \forall x \in S. Q\ x\ rv\ s\}, -$ 
apply (simp add: validE-R-def validE-def)
apply (rule hoare-strengthen-post)
apply (erule hoare-vcg-const-Ball-lift)
apply (simp split: sum.splits)
done

```

lemma *hoare-vcg-all-lift*:

```

 $\llbracket \bigwedge x. \{P\ x\} f \{Q\ x\} \rrbracket \implies \{\lambda s. \forall x. P\ x\ s\} f \{\lambda rv\ s. \forall x. Q\ x\ rv\ s\}$ 
by (fastforce simp: valid-def)

```

lemma *hoare-vcg-all-lift-R*:

```

 $(\bigwedge x. \{P\ x\} f \{Q\ x\}, -) \implies \{\lambda s. \forall x. P\ x\ s\} f \{\lambda rv\ s. \forall x. Q\ x\ rv\ s\}, -$ 
by (rule hoare-vcg-const-Ball-lift-R[where S=UNIV, simplified])

```

lemma *hoare-vcg-imp-lift*:

```

 $\llbracket \{P'\} f \{\lambda rv\ s. \neg P\ rv\ s\}; \{Q'\} f \{Q\} \rrbracket \implies \{\lambda s. P'\ s \vee Q'\ s\} f \{\lambda rv\ s. P\ rv\ s \longrightarrow Q\ rv\ s\}$ 
apply (simp only: imp-conv-disj)
apply (erule(1) hoare-vcg-disj-lift)
done

```

lemma *hoare-vcg-imp-lift'*:

```

 $\llbracket \{P'\} f \{\lambda rv\ s. \neg P\ rv\ s\}; \{Q'\} f \{Q\} \rrbracket \implies \{\lambda s. \neg P'\ s \longrightarrow Q'\ s\} f \{\lambda rv\ s. P\ rv\ s \longrightarrow Q\ rv\ s\}$ 
apply (simp only: imp-conv-disj)
apply simp
apply (erule (1) hoare-vcg-imp-lift)
done

```

lemma *hoare-vcg-imp-conj-lift[wp-comb]*:

```

 $\{P\} f \{\lambda rv\ s. Q\ rv\ s \longrightarrow Q''\ rv\ s\} \implies \{P\} f \{\lambda rv\ s. (Q\ rv\ s \longrightarrow Q''\ rv\ s) \wedge$ 

```

$Q''' \text{ rv } s \}$
 $\implies \{P \text{ and } P'\} f \{ \lambda \text{rv } s. (Q \text{ rv } s \longrightarrow Q' \text{ rv } s \wedge Q'' \text{ rv } s) \wedge Q''' \text{ rv } s \}$
by (*auto simp: valid-def*)

lemmas *hoare-vcg-imp-conj-lift'*[*wp-unsafe*] = *hoare-vcg-imp-conj-lift*[**where** $Q''' = \top\top$, *simplified*]

lemma *hoare-absorb-imp*:

$\{P\} f \{ \lambda \text{rv } s. Q \text{ rv } s \wedge R \text{ rv } s \} \implies \{P\} f \{ \lambda \text{rv } s. Q \text{ rv } s \longrightarrow R \text{ rv } s \}$
by (*erule hoare-post-imp[rotated], blast*)

lemma *hoare-weaken-imp*:

$\llbracket \bigwedge \text{rv } s. Q \text{ rv } s \implies Q' \text{ rv } s ; \{P\} f \{ \lambda \text{rv } s. Q' \text{ rv } s \longrightarrow R \text{ rv } s \} \rrbracket$
 $\implies \{P\} f \{ \lambda \text{rv } s. Q \text{ rv } s \longrightarrow R \text{ rv } s \}$
by (*clarsimp simp: NonDetMonad.valid-def split-def*)

lemma *hoare-vcg-const-imp-lift*:

$\llbracket P \implies \{Q\} m \{R\} \rrbracket \implies$
 $\{ \lambda s. P \longrightarrow Q s \} m \{ \lambda \text{rv } s. P \longrightarrow R \text{ rv } s \}$
by (*cases P, simp-all add: hoare-vcg-prop*)

lemma *hoare-vcg-const-imp-lift-R*:

$(P \implies \{Q\} m \{R\}, -) \implies \{ \lambda s. P \longrightarrow Q s \} m \{ \lambda \text{rv } s. P \longrightarrow R \text{ rv } s \}, -$
by (*fastforce simp: validE-R-def validE-def valid-def split-def split: sum.splits*)

lemma *hoare-weak-lift-imp*:

$\{P'\} f \{Q\} \implies \{ \lambda s. P \longrightarrow P' s \} f \{ \lambda \text{rv } s. P \longrightarrow Q \text{ rv } s \}$
by (*auto simp add: valid-def split-def*)

lemma *hoare-vcg-weaken-imp*:

$\llbracket \bigwedge \text{rv } s. Q \text{ rv } s \implies Q' \text{ rv } s ; \{P\} f \{ \lambda \text{rv } s. Q' \text{ rv } s \longrightarrow R \text{ rv } s \} \rrbracket$
 $\implies \{P\} f \{ \lambda \text{rv } s. Q \text{ rv } s \longrightarrow R \text{ rv } s \}$
by (*clarsimp simp: valid-def split-def*)

lemma *hoare-vcg-ex-lift*:

$\llbracket \bigwedge x. \{P x\} f \{Q x\} \rrbracket \implies \{ \lambda s. \exists x. P x s \} f \{ \lambda \text{rv } s. \exists x. Q x \text{ rv } s \}$
by (*clarsimp simp: valid-def, blast*)

lemma *hoare-vcg-ex-lift-R1*:

$(\bigwedge x. \{P x\} f \{Q\}, -) \implies \{ \lambda s. \exists x. P x s \} f \{Q\}, -$
by (*fastforce simp: valid-def validE-R-def validE-def split: sum.splits*)

lemma *hoare-liftP-ext*:

assumes $\bigwedge P x. m \{ \lambda s. P (f s x) \}$
shows $m \{ \lambda s. P (f s) \}$
unfolding *valid-def*
apply *clarsimp*
apply (*erule rsubst[where P=P]*)
apply (*rule ext*)

```

apply (drule use-valid, rule assms, rule refl)
apply simp
done

lemma hoare-triv:  $\{P\}f\{Q\} \Longrightarrow \{P\}f\{Q\}$  .
lemma hoare-trivE:  $\{P\}f\{Q\},\{E\} \Longrightarrow \{P\}f\{Q\},\{E\}$  .
lemma hoare-trivE-R:  $\{P\}f\{Q\},- \Longrightarrow \{P\}f\{Q\},-$  .
lemma hoare-trivR-R:  $\{P\}f-, \{E\} \Longrightarrow \{P\}f-, \{E\}$  .

lemma hoare-weaken-preE-E:
   $\llbracket \{P\}f-, \{Q\}; \bigwedge s. P\ s \Longrightarrow P'\ s \rrbracket \Longrightarrow \{P\}f-, \{Q\}$ 
  by (fastforce simp add: validE-E-def validE-def valid-def)

lemma hoare-vcg-E-conj:
   $\llbracket \{P\}f-, \{E\}; \{P'\}f\{Q'\}, \{E'\} \rrbracket$ 
   $\Longrightarrow \{\lambda s. P\ s \wedge P'\ s\}f\{Q'\}, \{\lambda rv\ s. E\ rv\ s \wedge E'\ rv\ s\}$ 
  apply (unfold validE-def validE-E-def)
  apply (rule hoare-post-imp [OF - hoare-vcg-conj-lift], simp-all)
  apply (case-tac r, simp-all)
done

lemma hoare-vcg-E-elim:
   $\llbracket \{P\}f-, \{E\}; \{P'\}f\{Q'\}, - \rrbracket$ 
   $\Longrightarrow \{\lambda s. P\ s \wedge P'\ s\}f\{Q'\}, \{E\}$ 
  by (rule hoare-post-impErr [OF hoare-vcg-E-conj],
    (simp add: validE-R-def)+)

lemma hoare-vcg-R-conj:
   $\llbracket \{P\}f\{Q\}, -; \{P'\}f\{Q'\}, - \rrbracket$ 
   $\Longrightarrow \{\lambda s. P\ s \wedge P'\ s\}f\{\lambda rv\ s. Q\ rv\ s \wedge Q'\ rv\ s\}, -$ 
  apply (unfold validE-R-def validE-def)
  apply (rule hoare-post-imp [OF - hoare-vcg-conj-lift], simp-all)
  apply (case-tac r, simp-all)
done

lemma valid-validE:
   $\{P\}f\{\lambda rv. Q\} \Longrightarrow \{P\}f\{\lambda rv. Q\}, \{\lambda rv. Q\}$ 
  apply (simp add: validE-def)
done

lemma valid-validE2:
   $\llbracket \{P\}f\{\lambda -. Q'\}; \bigwedge s. Q'\ s \Longrightarrow Q\ s; \bigwedge s. Q'\ s \Longrightarrow E\ s \rrbracket \Longrightarrow \{P\}f\{\lambda -. Q'\}, \{\lambda -. E\}$ 
  unfolding valid-def validE-def
  by (clarsimp split: sum.splits) blast

lemma validE-valid:  $\{P\}f\{\lambda rv. Q\}, \{\lambda rv. Q\} \Longrightarrow \{P\}f\{\lambda rv. Q\}$ 
  apply (unfold validE-def)

```

```

apply (rule hoare-post-imp)
defer
apply assumption
apply (case-tac r, simp-all)
done

lemma valid-validE-R:
   $\{P\} f \{\lambda rv. Q\} \implies \{P\} f \{\lambda rv. Q\}, -$ 
by (simp add: validE-R-def hoare-post-impErr [OF valid-validE])

lemma valid-validE-E:
   $\{P\} f \{\lambda rv. Q\} \implies \{P\} f -, \{\lambda rv. Q\}$ 
by (simp add: validE-E-def hoare-post-impErr [OF valid-validE])

lemma validE-validE-R:  $\{P\} f \{Q\}, \{\top\top\} \implies \{P\} f \{Q\}, -$ 
by (simp add: validE-R-def)

lemma validE-R-validE:  $\{P\} f \{Q\}, - \implies \{P\} f \{Q\}, \{\top\top\}$ 
by (simp add: validE-R-def)

lemma validE-validE-E:  $\{P\} f \{\top\top\}, \{E\} \implies \{P\} f -, \{E\}$ 
by (simp add: validE-E-def)

lemma validE-E-validE:  $\{P\} f -, \{E\} \implies \{P\} f \{\top\top\}, \{E\}$ 
by (simp add: validE-E-def)

lemma hoare-post-imp-R:  $\llbracket \{P\} f \{Q'\}, -; \bigwedge r s. Q' r s \implies Q r s \rrbracket \implies \{P\} f \{Q\}, -$ 
apply (unfold validE-R-def)
apply (erule hoare-post-impErr, simp+)
done

lemma hoare-post-imp-E:  $\llbracket \{P\} f -, \{Q'\}; \bigwedge r s. Q' r s \implies Q r s \rrbracket \implies \{P\} f -, \{Q\}$ 
apply (unfold validE-E-def)
apply (erule hoare-post-impErr, simp+)
done

lemma hoare-post-comb-imp-conj:
   $\llbracket \{P'\} f \{Q\}; \{P\} f \{Q'\}; \bigwedge s. P s \implies P' s \rrbracket \implies \{P\} f \{\lambda rv s. Q r v s \wedge Q' r v s\}$ 
apply (rule hoare-pre-imp)
defer
apply (rule hoare-vcg-conj-lift)
apply assumption+
apply simp
done

lemma hoare-vcg-precond-impE-R:  $\llbracket \{P'\} f \{Q\}, -; \bigwedge s. P s \implies P' s \rrbracket \implies \{P\}$ 

```

$f \{Q\}, -$
by (*unfold validE-R-def*, *rule hoare-vcg-precond-impE*, *simp+*)

lemma *valid-is-triple*:

$\text{valid } P \ f \ Q = \text{triple-judgement } P \ f \ (\text{postcondition } Q \ (\lambda s \ f. \text{fst } (f \ s)))$
by (*simp add: triple-judgement-def valid-def postcondition-def*)

lemma *validE-is-triple*:

$\text{validE } P \ f \ Q \ E = \text{triple-judgement } P \ f$
 $(\text{postconditions } (\text{postcondition } Q \ (\lambda s \ f. \{(rv, s'). (Inr \ rv, \ s') \in \text{fst } (f \ s)\}))$
 $(\text{postcondition } E \ (\lambda s \ f. \{(rv, s'). (Inl \ rv, \ s') \in \text{fst } (f \ s)\})))$
apply (*simp add: validE-def triple-judgement-def valid-def postcondition-def*
postconditions-def split-def split: sum.split)
apply *fastforce*
done

lemma *validE-R-is-triple*:

$\text{validE-R } P \ f \ Q = \text{triple-judgement } P \ f$
 $(\text{postcondition } Q \ (\lambda s \ f. \{(rv, s'). (Inr \ rv, \ s') \in \text{fst } (f \ s)\}))$
by (*simp add: validE-R-def validE-is-triple postconditions-def postcondition-def*)

lemma *validE-E-is-triple*:

$\text{validE-E } P \ f \ E = \text{triple-judgement } P \ f$
 $(\text{postcondition } E \ (\lambda s \ f. \{(rv, s'). (Inl \ rv, \ s') \in \text{fst } (f \ s)\}))$
by (*simp add: validE-E-def validE-is-triple postconditions-def postcondition-def*)

lemmas *hoare-wp-combs = hoare-vcg-conj-lift*

lemmas *hoare-wp-combsE =*

validE-validE-R
hoare-vcg-R-conj
hoare-vcg-E-elim
hoare-vcg-E-conj

lemmas *hoare-wp-state-combsE =*

valid-validE-R
hoare-vcg-R-conj [*OF valid-validE-R*]
hoare-vcg-E-elim [*OF valid-validE-E*]
hoare-vcg-E-conj [*OF valid-validE-E*]

lemmas *hoare-classic-wp-combs*

= hoare-post-comb-imp-conj hoare-vcg-precond-imp hoare-wp-combs

lemmas *hoare-classic-wp-combsE*

= hoare-vcg-precond-impE hoare-vcg-precond-impE-R hoare-wp-combsE

lemmas *hoare-classic-wp-state-combsE*

= hoare-vcg-precond-impE [*OF valid-validE*]
hoare-vcg-precond-impE-R [*OF valid-validE-R*] *hoare-wp-state-combsE*

lemmas *all-classic-wp-combs =*

hoare-classic-wp-state-combsE hoare-classic-wp-combsE hoare-classic-wp-combs

lemmas *hoare-wp-splits* [*wp-split*] =
hoare-seq-ext hoare-vcg-seqE handleE'-wp handleE-wp
validE-validE-R [OF hoare-vcg-seqE [OF validE-R-validE]]
validE-validE-R [OF handleE'-wp [OF validE-R-validE]]
validE-validE-R [OF handleE-wp [OF validE-R-validE]]
catch-wp hoare-vcg-if-split hoare-vcg-if-splitE
validE-validE-R [OF hoare-vcg-if-splitE [OF validE-R-validE validE-R-validE]]
liftM-wp liftME-wp
validE-validE-R [OF liftME-wp [OF validE-R-validE]]
validE-valid

lemmas [*wp-comb*] = *hoare-wp-state-combsE hoare-wp-combsE hoare-wp-combs*

lemmas [*wp*] = *hoare-vcg-prop*
wp-post-taut
return-wp
put-wp
get-wp
gets-wp
modify-wp
returnOk-wp
throwError-wp
fail-wp
failE-wp
liftE-wp
select-f-wp

lemmas [*wp-trip*] = *valid-is-triple validE-is-triple validE-E-is-triple validE-R-is-triple*

lemmas *validE-E-combs*[*wp-comb*] =
hoare-vcg-E-conj[where Q' = $\top \top$, folded validE-E-def]
valid-validE-E
hoare-vcg-E-conj[where Q' = $\top \top$, folded validE-E-def, OF valid-validE-E]

Simplifications on conjunction

lemma *hoare-post-eq*: $\llbracket Q = Q'; \{P\} f \{Q'\} \rrbracket \implies \{P\} f \{Q\}$
by *simp*
lemma *hoare-post-eqE1*: $\llbracket Q = Q'; \{P\} f \{Q'\}, \{E\} \rrbracket \implies \{P\} f \{Q\}, \{E\}$
by *simp*
lemma *hoare-post-eqE2*: $\llbracket E = E'; \{P\} f \{Q\}, \{E'\} \rrbracket \implies \{P\} f \{Q\}, \{E\}$
by *simp*
lemma *hoare-post-eqE-R*: $\llbracket Q = Q'; \{P\} f \{Q'\}, - \rrbracket \implies \{P\} f \{Q\}, -$
by *simp*

lemma *pred-conj-apply-elim*: $(\lambda r. Q \ r \text{ and } Q' \ r) = (\lambda r \ s. Q \ r \ s \wedge Q' \ r \ s)$
by (*simp add: pred-conj-def*)

lemma *pred-conj-conj-elim*: $(\lambda r \ s. (Q \ r \text{ and } Q' \ r) \ s \wedge Q'' \ r \ s) = (\lambda r \ s. Q \ r \ s \wedge Q' \ r \ s \wedge Q'' \ r \ s)$

by *simp*
lemma *conj-assoc-apply*: $(\lambda r s. (Q r s \wedge Q' r s) \wedge Q'' r s) = (\lambda r s. Q r s \wedge Q' r s \wedge Q'' r s)$
by *simp*
lemma *all-elim*: $(\lambda r v s. \forall x. P r v s) = P$
by *simp*
lemma *all-conj-elim*: $(\lambda r v s. (\forall x. P r v s) \wedge Q r v s) = (\lambda r v s. P r v s \wedge Q r v s)$
by *simp*

lemmas *vcg-rhs-simps* = *pred-conj-apply-elim pred-conj-conj-elim conj-assoc-apply all-elim all-conj-elim*

lemma *if-apply-reduct*: $\{P\} \text{ If } P' (f x) (g x) \{Q\} \Longrightarrow \{P\} \text{ If } P' f g x \{Q\}$
by (*cases P', simp-all*)
lemma *if-apply-reductE*: $\{P\} \text{ If } P' (f x) (g x) \{Q\}, \{E\} \Longrightarrow \{P\} \text{ If } P' f g x \{Q\}, \{E\}$
by (*cases P', simp-all*)
lemma *if-apply-reductE-R*: $\{P\} \text{ If } P' (f x) (g x) \{Q\}, - \Longrightarrow \{P\} \text{ If } P' f g x \{Q\}, -$
by (*cases P', simp-all*)

lemmas *hoare-wp-simps* [*wp-split*] =
vcg-rhs-simps [THEN hoare-post-eq] vcg-rhs-simps [THEN hoare-post-eqE1]
vcg-rhs-simps [THEN hoare-post-eqE2] vcg-rhs-simps [THEN hoare-post-eqE-R]
if-apply-reduct if-apply-reductE if-apply-reductE-R TrueI

schematic-goal *if-apply-test*: $\{?Q\} (\text{if } A \text{ then returnOk else } K \text{ fail}) x \{P\}, \{E\}$
by *wpsimp*

lemma *hoare-elim-pred-conj*:
 $\{P\} f \{\lambda r s. Q r s \wedge Q' r s\} \Longrightarrow \{P\} f \{\lambda r. Q r \text{ and } Q' r\}$
by (*unfold pred-conj-def*)

lemma *hoare-elim-pred-conjE1*:
 $\{P\} f \{\lambda r s. Q r s \wedge Q' r s\}, \{E\} \Longrightarrow \{P\} f \{\lambda r. Q r \text{ and } Q' r\}, \{E\}$
by (*unfold pred-conj-def*)

lemma *hoare-elim-pred-conjE2*:
 $\{P\} f \{Q\}, \{\lambda x s. E x s \wedge E' x s\} \Longrightarrow \{P\} f \{Q\}, \{\lambda x. E x \text{ and } E' x\}$
by (*unfold pred-conj-def*)

lemma *hoare-elim-pred-conjE-R*:
 $\{P\} f \{\lambda r s. Q r s \wedge Q' r s\}, - \Longrightarrow \{P\} f \{\lambda r. Q r \text{ and } Q' r\}, -$
by (*unfold pred-conj-def*)

lemmas *hoare-wp-pred-conj-elim* =
hoare-elim-pred-conj hoare-elim-pred-conjE1
hoare-elim-pred-conjE2 hoare-elim-pred-conjE-R

lemmas *hoare-weaken-preE* = *hoare-vcg-precond-impE*

```

lemmas hoare-pre [wp-pre] =
  hoare-weaken-pre
  hoare-weaken-preE
  hoare-vcg-precond-impE-R
  hoare-weaken-preE-E

declare no-fail-pre [wp-pre]

bundle no-pre = hoare-pre [wp-pre del] no-fail-pre [wp-pre del]

bundle classic-wp-pre = hoare-pre [wp-pre del] no-fail-pre [wp-pre del]
  all-classic-wp-combs[wp-comb del] all-classic-wp-combs[wp-comb]

```

Miscellaneous lemmas on hoare triples

```

lemma hoare-vcg-mp:
  assumes a:  $\{P\} f \{Q\}$ 
  assumes b:  $\{P\} f \{\lambda r s. Q r s \longrightarrow Q' r s\}$ 
  shows  $\{P\} f \{Q'\}$ 
  using assms
  by (auto simp: valid-def split-def)

lemma hoare-add-post:
  assumes r:  $\{P'\} f \{Q'\}$ 
  assumes impP:  $\bigwedge s. P s \implies P' s$ 
  assumes impQ:  $\{P\} f \{\lambda rv s. Q' rv s \longrightarrow Q rv s\}$ 
  shows  $\{P\} f \{Q\}$ 
  apply (rule hoare-chain)
  apply (rule hoare-vcg-conj-lift)
  apply (rule r)
  apply (rule impQ)
  apply simp
  apply (erule impP)
  apply simp
  done

```

```

lemma hoare-gen-asmE:
   $(P \implies \{P'\} f \{Q\}, -) \implies \{P' \text{ and } K P\} f \{Q\}, -$ 
  by (simp add: validE-R-def validE-def valid-def) blast

```

```

lemma hoare-list-case:
  assumes P1:  $\{P1\} f f1 \{Q\}$ 
  assumes P2:  $\bigwedge y ys. xs = y \# ys \implies \{P2 y ys\} f (f2 y ys) \{Q\}$ 
  shows  $\{case\ xs\ of\ [] \Rightarrow P1 \mid y \# ys \Rightarrow P2\ y\ ys\}$ 
     $f (case\ xs\ of\ [] \Rightarrow f1 \mid y \# ys \Rightarrow f2\ y\ ys)$ 
     $\{Q\}$ 
  apply (cases xs; simp)

```

apply (*rule P1*)
apply (*rule P2*)
apply *simp*
done

lemma *hoare-when-wp* [*wp-split*]:
 $\llbracket P \implies \{Q\} f \{R\} \rrbracket \implies \{ \text{if } P \text{ then } Q \text{ else } R \ () \} \text{ when } P f \{R\}$
by (*clarsimp simp: when-def valid-def return-def*)

lemma *hoare-unless-wp* [*wp-split*]:
 $(\neg P \implies \{Q\} f \{R\}) \implies \{ \text{if } P \text{ then } R \ () \text{ else } Q \} \text{ unless } P f \{R\}$
unfolding *unless-def* **by** *wp auto*

lemma *hoare-whenE-wp*:
 $(P \implies \{Q\} f \{R\}, \{E\}) \implies \{ \text{if } P \text{ then } Q \text{ else } R \ () \} \text{ whenE } P f \{R\}, \{E\}$
unfolding *whenE-def* **by** *clarsimp wp*

lemmas *hoare-whenE-wps* [*wp-split*]
 $= \text{hoare-whenE-wp hoare-whenE-wp} [\text{THEN validE-validE-R}] \text{ hoare-whenE-wp} [\text{THEN validE-validE-E}]$

lemma *hoare-unlessE-wp*:
 $(\neg P \implies \{Q\} f \{R\}, \{E\}) \implies \{ \text{if } P \text{ then } R \ () \text{ else } Q \} \text{ unlessE } P f \{R\}, \{E\}$
unfolding *unlessE-def* **by** *wp auto*

lemmas *hoare-unlessE-wps* [*wp-split*]
 $= \text{hoare-unlessE-wp hoare-unlessE-wp} [\text{THEN validE-validE-R}] \text{ hoare-unlessE-wp} [\text{THEN validE-validE-E}]$

lemma *hoare-use-eq*:
assumes $x: \bigwedge P. \{ \lambda s. P (f s) \} m \{ \lambda rv s. P (f s) \}$
assumes $y: \bigwedge f. \{ \lambda s. P f s \} m \{ \lambda rv s. Q f s \}$
shows $\{ \lambda s. P (f s) s \} m \{ \lambda rv s. Q (f s :: 'c :: \text{type}) s \}$
apply (*rule-tac Q= $\lambda rv s. \exists f'. f' = f s \wedge Q f' s$ in hoare-post-imp*)
apply *simp*
apply (*wp simp wp: hoare-vcg-ex-lift x y*)
done

lemma *hoare-return-sp*:
 $\{P\} \text{ return } x \{ \lambda r. P \text{ and } K (r = x) \}$
by (*simp add: valid-def return-def*)

lemma *hoare-fail-any* [*simp*]:
 $\{P\} \text{ fail } \{Q\} \text{ by } wp$

lemma *hoare-failE* [*simp*]: $\{P\} \text{ fail } \{Q\}, \{E\} \text{ by } wp$

lemma *hoare-FalseE* [*simp*]:
 $\{ \lambda s. \text{False} \} f \{Q\}, \{E\}$

by (*simp add: valid-def validE-def*)

lemma *hoare-K-bind* [*wp-split*]:

$\{P\} f \{Q\} \implies \{P\} K\text{-bind } f x \{Q\}$

by *simp*

lemma *validE-K-bind* [*wp-split*]:

$\{P\} x \{Q\}, \{E\} \implies \{P\} K\text{-bind } x f \{Q\}, \{E\}$

by *simp*

Setting up the precondition case splitter.

lemma *wpc-helper-valid*:

$\{Q\} g \{S\} \implies \text{wpc-helper } (P, P') (Q, Q') \{P\} g \{S\}$

by (*clarsimp simp: wpc-helper-def elim!: hoare-pre*)

lemma *wpc-helper-validE*:

$\{Q\} f \{R\}, \{E\} \implies \text{wpc-helper } (P, P') (Q, Q') \{P\} f \{R\}, \{E\}$

by (*clarsimp simp: wpc-helper-def elim!: hoare-pre*)

lemma *wpc-helper-validE-R*:

$\{Q\} f \{R\}, - \implies \text{wpc-helper } (P, P') (Q, Q') \{P\} f \{R\}, -$

by (*clarsimp simp: wpc-helper-def elim!: hoare-pre*)

lemma *wpc-helper-validR-R*:

$\{Q\} f -, \{E\} \implies \text{wpc-helper } (P, P') (Q, Q') \{P\} f -, \{E\}$

by (*clarsimp simp: wpc-helper-def elim!: hoare-pre*)

lemma *wpc-helper-no-fail-final*:

no-fail $Q f \implies \text{wpc-helper } (P, P') (Q, Q') (\text{no-fail } P f)$

by (*clarsimp simp: wpc-helper-def elim!: no-fail-pre*)

lemma *wpc-helper-empty-fail-final*:

empty-fail $f \implies \text{wpc-helper } (P, P') (Q, Q') (\text{empty-fail } f)$

by (*clarsimp simp: wpc-helper-def*)

lemma *wpc-helper-validNF*:

$\{Q\} g \{S\}! \implies \text{wpc-helper } (P, P') (Q, Q') \{P\} g \{S\}!$

apply (*clarsimp simp: wpc-helper-def*)

by (*metis hoare-vcg-precond-imp no-fail-pre validNF-def*)

wpc-setup $\lambda m. \{P\} m \{Q\} \text{wpc-helper-valid}$

wpc-setup $\lambda m. \{P\} m \{Q\}, \{E\} \text{wpc-helper-validE}$

wpc-setup $\lambda m. \{P\} m \{Q\}, - \text{wpc-helper-validE-R}$

wpc-setup $\lambda m. \{P\} m -, \{E\} \text{wpc-helper-validR-R}$

wpc-setup $\lambda m. \text{no-fail } P m \text{wpc-helper-no-fail-final}$

wpc-setup $\lambda m. \text{empty-fail } m \text{wpc-helper-empty-fail-final}$

wpc-setup $\lambda m. \{P\} m \{Q\}! \text{wpc-helper-validNF}$

lemma *in-liftM*:

$((r, s') \in \text{fst } (\text{liftM } t \text{ f } s)) = (\exists r'. (r', s') \in \text{fst } (f \text{ s}) \wedge r = t \text{ r}')$
apply (*simp add: liftM-def return-def bind-def*)
apply (*simp add: Bex-def*)
done

lemmas *handy-liftM-lemma = in-liftM*

lemma *hoare-fun-app-wp*[*wp*]:
 $\{P\} f' x \{Q\} \implies \{P\} f' \$ x \{Q\}$
 $\{P\} f x \{Q\}, \{E\} \implies \{P\} f \$ x \{Q\}, \{E\}$
 $\{P\} f x \{Q\}, - \implies \{P\} f \$ x \{Q\}, -$
 $\{P\} f x -, \{E\} \implies \{P\} f \$ x -, \{E\}$
by *simp+*

lemma *hoare-validE-pred-conj*:
 $\llbracket \{P\} f \{Q\}, \{E\}; \{P\} f \{R\}, \{E\} \rrbracket \implies \{P\} f \{Q \text{ And } R\}, \{E\}$
unfolding *valid-def validE-def* **by** (*simp add: split-def split: sum.splits*)

lemma *hoare-validE-conj*:
 $\llbracket \{P\} f \{Q\}, \{E\}; \{P\} f \{R\}, \{E\} \rrbracket \implies \{P\} f \{\lambda r s. Q \text{ r } s \wedge R \text{ r } s\}, \{E\}$
unfolding *valid-def validE-def* **by** (*simp add: split-def split: sum.splits*)

lemmas *hoare-valid-validE = valid-validE*

lemma *liftE-validE-E* [*wp*]:
 $\{\top\} \text{liftE } f -, \{Q\}$
by (*clarsimp simp: validE-E-def valid-def*)

declare *validE-validE-E*[*wp-comb*]

lemmas *if-validE-E* [*wp-split*] =
validE-validE-E [*OF hoare-vcg-if-splitE* [*OF validE-E-validE validE-E-validE*]]

lemma *returnOk-E* [*wp*]:
 $\{\top\} \text{returnOk } r -, \{Q\}$
by (*simp add: validE-E-def wp*)

lemma *hoare-drop-imp*:
 $\{P\} f \{Q\} \implies \{P\} f \{\lambda r s. R \text{ r } s \longrightarrow Q \text{ r } s\}$
by (*auto simp: valid-def*)

lemma *hoare-drop-impE*:
 $\llbracket \{P\} f \{\lambda r. Q\}, \{E\} \rrbracket \implies \{P\} f \{\lambda r s. R \text{ r } s \longrightarrow Q \text{ s}\}, \{E\}$
by (*simp add: validE-weaken*)

lemma *hoare-drop-impE-R*:
 $\{P\} f \{Q\}, - \implies \{P\} f \{\lambda r s. R \text{ r } s \longrightarrow Q \text{ r } s\}, -$

by (*auto simp: validE-R-def validE-def valid-def split-def split: sum.splits*)

lemma *hoare-drop-impE-E*:

$\{P\} f -, \{Q\} \implies \{P\} f -, \{\lambda r s. R r s \longrightarrow Q r s\}$

by (*auto simp: validE-E-def validE-def valid-def split-def split: sum.splits*)

lemmas *hoare-drop-imps* = *hoare-drop-imp hoare-drop-impE-R hoare-drop-impE-E*

lemma *hoare-drop-imp-conj*[*wp-unsafe*]:

$\{P\} f \{Q\} \implies \{P'\} f \{\lambda rv s. (Q rv s \longrightarrow Q'' rv s) \wedge Q''' rv s\}$

$\implies \{P \text{ and } P'\} f \{\lambda rv s. (Q rv s \longrightarrow Q' rv s \wedge Q'' rv s) \wedge Q''' rv s\}$

by (*auto simp: valid-def*)

lemmas *hoare-drop-imp-conj'*[*wp-unsafe*] = *hoare-drop-imp-conj*[**where** $Q''' = \top$, *simplified*]

lemma *bind-det-exec*:

$\text{fst } (a s) = \{(r, s')\} \implies \text{fst } ((a >>= b) s) = \text{fst } (b r s')$

by (*simp add: bind-def*)

lemma *in-bind-det-exec*:

$\text{fst } (a s) = \{(r, s')\} \implies (s'' \in \text{fst } ((a >>= b) s)) = (s'' \in \text{fst } (b r s'))$

by (*simp add: bind-def*)

lemma *exec-put*:

$(\text{put } s' >>= m) s = m () s'$

by (*simp add: bind-def put-def*)

lemma *bind-execI*:

$\llbracket (r'', s'') \in \text{fst } (f s); \exists x \in \text{fst } (g r'' s''). P x \rrbracket \implies$

$\exists x \in \text{fst } ((f >>= g) s). P x$

by (*force simp: in-bind split-def bind-def*)

lemma *True-E-E* [*wp*]: $\{\top\} f -, \{\top\top\}$

by (*auto simp: validE-E-def validE-def valid-def split: sum.splits*)

lemmas [*wp-split*] =

validE-validE-E [*OF hoare-vcg-seqE* [*OF validE-E-validE*]]

lemma *case-option-wp*:

assumes $x: \bigwedge x. \{P x\} m x \{Q\}$

assumes $y: \{P'\} m' \{Q\}$

shows $\{\lambda s. (x = \text{None} \longrightarrow P' s) \wedge (x \neq \text{None} \longrightarrow P (\text{the } x) s)\}$

case-option $m' m x \{Q\}$

apply (*cases x; simp*)

apply (*rule y*)

apply (*rule x*)

done

lemma *case-option-wpE*:

assumes $x: \bigwedge x. \{P\ x\} \ m\ x\ \{Q\}, \{E\}$
 assumes $y: \{P'\} \ m'\ \{Q\}, \{E\}$
 shows $\{\lambda s. (x = \text{None} \longrightarrow P'\ s) \wedge (x \neq \text{None} \longrightarrow P\ (\text{the } x)\ s)\}$
 $\text{case-option } m'\ m\ x\ \{Q\}, \{E\}$
 apply (cases x; simp)
 apply (rule y)
 apply (rule x)
 done

lemma *in-bindE*:

$(rv, s') \in \text{fst } ((f \gg E (\lambda rv'. g\ rv'))\ s) =$
 $((\exists ex. rv = \text{Inl } ex \wedge (\text{Inl } ex, s') \in \text{fst } (f\ s)) \vee$
 $(\exists rv' s''. (rv, s') \in \text{fst } (g\ rv' s'') \wedge (\text{Inr } rv', s'') \in \text{fst } (f\ s)))$
 apply (rule iffI)
 apply (clarsimp simp: bindE-def bind-def)
 apply (case-tac a)
 apply (clarsimp simp: lift-def throwError-def return-def)
 apply (clarsimp simp: lift-def)
 apply safe
 apply (clarsimp simp: bindE-def bind-def)
 apply (erule rev-bexI)
 apply (simp add: lift-def throwError-def return-def)
 apply (clarsimp simp: bindE-def bind-def)
 apply (erule rev-bexI)
 apply (simp add: lift-def)
 done

lemmas $[\text{wp-split}] = \text{validE-validE-E } [\text{OF liftME-wp, simplified, OF validE-E-validE}]$

lemma *assert-A-True[simp]*: *assert True = return ()*

by (simp add: assert-def)

lemma *assert-wp* [wp]: $\{\lambda s. P \longrightarrow Q\ ()\ s\} \text{ assert } P\ \{Q\}$

by (cases P, (simp add: assert-def | wp)+)

lemma *list-cases-wp*:

assumes $a: \{P-A\} \ a\ \{Q\}$
 assumes $b: \bigwedge x\ xs. ts = x \# xs \Longrightarrow \{P-B\ x\ xs\} \ b\ x\ xs\ \{Q\}$
 shows $\{\text{case-list } P-A\ P-B\ ts\} \text{ case } ts \text{ of } [] \Rightarrow a \mid x \# xs \Rightarrow b\ x\ xs\ \{Q\}$
 by (cases ts, auto simp: a b)

lemma *whenE-throwError-wp*:

$\{\lambda s. \neg Q \longrightarrow P\ s\} \text{ whenE } Q\ (\text{throwError } e)\ \{\lambda rv. P\}, -$
 unfolding *whenE-def* by *wpsimp*

lemma *select-throwError-wp*:
 $\{\lambda s. \forall x \in S. Q\ x\ s\} \text{ select } S \gg= \text{ throwError } -, \{\!Q\!\}$
by (*simp add: bind-def throwError-def return-def select-def validE-E-def*
validE-def valid-def)

lemma *assert-opt-wp*[*wp*]:
 $\{\lambda s. x \neq \text{None} \longrightarrow Q\ (\text{the } x)\ s\} \text{ assert-opt } x \{\!Q\!\}$
by (*case-tac x, (simp add: assert-opt-def | wp)+*)

lemma *gets-the-wp*[*wp*]:
 $\{\lambda s. (f\ s \neq \text{None}) \longrightarrow Q\ (\text{the } (f\ s))\ s\} \text{ gets-the } f \{\!Q\!\}$
by (*unfold gets-the-def, wp*)

lemma *gets-the-wp'*:
 $\{\lambda s. \forall rv. f\ s = \text{Some } rv \longrightarrow Q\ rv\ s\} \text{ gets-the } f \{\!Q\!\}$
unfolding *gets-the-def* **by** *wsimp*

lemma *gets-map-wp*:
 $\{\lambda s. f\ s\ p \neq \text{None} \longrightarrow Q\ (\text{the } (f\ s\ p))\ s\} \text{ gets-map } f\ p \{\!Q\!\}$
unfolding *gets-map-def* **by** *wsimp*

lemma *gets-map-wp'*[*wp*]:
 $\{\lambda s. \forall rv. f\ s\ p = \text{Some } rv \longrightarrow Q\ rv\ s\} \text{ gets-map } f\ p \{\!Q\!\}$
unfolding *gets-map-def* **by** *wsimp*

lemma *no-fail-gets-map*[*wp*]:
no-fail ($\lambda s. f\ s\ p \neq \text{None}$) (*gets-map* *f p*)
unfolding *gets-map-def* **by** *wsimp*

lemma *hoare-vcg-set-pred-lift*:
assumes $\bigwedge P\ x. m\ \{\! \lambda s. P\ (f\ x\ s) \!\}$
shows $m\ \{\! \lambda s. P\ \{x. f\ x\ s\} \!\}$
using *assms[where P= $\lambda x. x$] assms[where P=Not] use-valid*
by (*fastforce simp: valid-def elim!: rsubst[where P=P]*)

lemma *hoare-vcg-set-pred-lift-mono*:
assumes $f: \bigwedge x. m\ \{\! f\ x \!\}$
assumes *mono*: $\bigwedge A\ B. A \subseteq B \implies P\ A \implies P\ B$
shows $m\ \{\! \lambda s. P\ \{x. f\ x\ s\} \!\}$
by (*fastforce simp: valid-def elim!: mono[rotated] dest: use-valid[OF - f]*)

24 validNF Rules

24.1 Basic validNF theorems

lemma *validNF* [*intro?*]:
 $\llbracket \{\! P \!\} f \{\! Q \!\}; \text{ no-fail } P\ f \rrbracket \implies \{\! P \!\} f \{\! Q \!\}!$
by (*clarsimp simp: validNF-def*)

lemma *validNF-valid*: $\llbracket \{ P \} f \{ Q \}! \rrbracket \Longrightarrow \{ P \} f \{ Q \}$
by (*clarsimp simp: validNF-def*)

lemma *validNF-no-fail*: $\llbracket \{ P \} f \{ Q \}! \rrbracket \Longrightarrow \text{no-fail } P f$
by (*clarsimp simp: validNF-def*)

lemma *snd-validNF*:
 $\llbracket \{ P \} f \{ Q \}!; P s \rrbracket \Longrightarrow \neg \text{snd } (f s)$
by (*clarsimp simp: validNF-def no-fail-def*)

lemma *use-validNF*:
 $\llbracket (r', s') \in \text{fst } (f s); \{ P \} f \{ Q \}!; P s \rrbracket \Longrightarrow Q r' s'$
by (*fastforce simp: validNF-def valid-def*)

24.2 validNF weakest pre-condition rules

lemma *validNF-return* [*wp*]:
 $\{ P x \} \text{return } x \{ P \}!$
by (*wp validNF*)⁺

lemma *validNF-get* [*wp*]:
 $\{ \lambda s. P s s \} \text{get } \{ P \}!$
by (*wp validNF*)⁺

lemma *validNF-put* [*wp*]:
 $\{ \lambda s. P () x \} \text{put } x \{ P \}!$
by (*wp validNF*)⁺

lemma *validNF-K-bind* [*wp*]:
 $\{ P \} x \{ Q \}! \Longrightarrow \{ P \} K\text{-bind } x f \{ Q \}!$
by *simp*

lemma *validNF-fail* [*wp*]:
 $\{ \lambda s. \text{False} \} \text{fail } \{ Q \}!$
by (*clarsimp simp: validNF-def fail-def no-fail-def*)

lemma *validNF-prop* [*wp-unsafe*]:
 $\llbracket \text{no-fail } (\lambda s. P) f \rrbracket \Longrightarrow \{ \lambda s. P \} f \{ \lambda r v s. P \}!$
by (*wp validNF*)⁺

lemma *validNF-post-conj* [*intro!*]:
 $\llbracket \{ P \} a \{ Q \}!; \{ P \} a \{ R \}! \rrbracket \Longrightarrow \{ P \} a \{ Q \text{ And } R \}!$
by (*auto simp: validNF-def*)

lemma *no-fail-or*:
 $\llbracket \text{no-fail } P a; \text{no-fail } Q a \rrbracket \Longrightarrow \text{no-fail } (P \text{ or } Q) a$
by (*clarsimp simp: no-fail-def*)

lemma *validNF-pre-disj* [intro!]:

$\llbracket \{ P \} a \{ R \}!; \{ Q \} a \{ R \}! \rrbracket \Longrightarrow \{ P \text{ or } Q \} a \{ R \}!$

by (*rule validNF*) (*auto dest: validNF-valid validNF-no-fail intro: no-fail-or*)

definition *validNF-property* $Q\ s\ b \equiv \neg \text{snd}\ (b\ s) \wedge (\forall (r', s') \in \text{fst}\ (b\ s). Q\ r'\ s')$

lemma *validNF-is-triple* [wp-trip]:

validNF $P\ f\ Q = \text{triple-judgement}\ P\ f\ (\text{validNF-property}\ Q)$

apply (*clarsimp simp: validNF-def triple-judgement-def validNF-property-def*)

apply (*auto simp: no-fail-def valid-def*)

done

lemma *validNF-weaken-pre*[wp-pre]:

$\llbracket \{ Q \} a \{ R \}!; \bigwedge s. P\ s \Longrightarrow Q\ s \rrbracket \Longrightarrow \{ P \} a \{ R \}!$

by (*metis hoare-pre-imp no-fail-pre validNF-def*)

lemma *validNF-post-comb-imp-conj*:

$\llbracket \{ P \} f \{ Q \}!; \{ P \} f \{ Q \}!; \bigwedge s. P\ s \Longrightarrow P'\ s \rrbracket \Longrightarrow \{ P \} f \{ \lambda rv\ s. Q\ rv\ s \wedge Q'\ rv\ s \}!$

by (*fastforce simp: validNF-def valid-def*)

lemma *validNF-post-comb-conj-L*:

$\llbracket \{ P \} f \{ Q \}!; \{ P \} f \{ Q \}! \rrbracket \Longrightarrow \llbracket \lambda s. P\ s \wedge P'\ s \rrbracket f \{ \lambda rv\ s. Q\ rv\ s \wedge Q'\ rv\ s \}!$

apply (*clarsimp simp: validNF-def valid-def no-fail-def*)

apply *force*

done

lemma *validNF-post-comb-conj-R*:

$\llbracket \{ P \} f \{ Q \}!; \{ P \} f \{ Q \}! \rrbracket \Longrightarrow \llbracket \lambda s. P\ s \wedge P'\ s \rrbracket f \{ \lambda rv\ s. Q\ rv\ s \wedge Q'\ rv\ s \}!$

apply (*clarsimp simp: validNF-def valid-def no-fail-def*)

apply *force*

done

lemma *validNF-post-comb-conj*:

$\llbracket \{ P \} f \{ Q \}!; \{ P \} f \{ Q \}! \rrbracket \Longrightarrow \llbracket \lambda s. P\ s \wedge P'\ s \rrbracket f \{ \lambda rv\ s. Q\ rv\ s \wedge Q'\ rv\ s \}!$

apply (*clarsimp simp: validNF-def valid-def no-fail-def*)

apply *force*

done

lemma *validNF-if-split* [wp-split]:

$\llbracket P \Longrightarrow \{ Q \} f \{ S \}!; \neg P \Longrightarrow \{ R \} g \{ S \}! \rrbracket \Longrightarrow \llbracket \lambda s. (P \longrightarrow Q\ s) \wedge (\neg P \longrightarrow R\ s) \rrbracket \text{ if } P \text{ then } f \text{ else } g \{ S \}!$

by *simp*

lemma *validNF-vcg-conj-lift*:

$\llbracket \{ P \} f \{ Q \}!; \{ P \} f \{ Q \}! \rrbracket \Longrightarrow$

```

     $\{\lambda s. P\ s \wedge P'\ s\} f\ \{\lambda rv\ s. Q\ rv\ s \wedge Q'\ rv\ s\}!$ 
  apply (subst bipred-conj-def[symmetric], rule validNF-post-conj)
  apply (erule validNF-weaken-pre, fastforce)
  apply (erule validNF-weaken-pre, fastforce)
done

```

```

lemma validNF-vcg-disj-lift:
   $\llbracket \{P\} f\ \{Q\}!; \{P'\} f\ \{Q'\}! \rrbracket \implies$ 
   $\{\lambda s. P\ s \vee P'\ s\} f\ \{\lambda rv\ s. Q\ rv\ s \vee Q'\ rv\ s\}!$ 
  apply (clarsimp simp: validNF-def)
  apply safe
  apply (auto intro!: hoare-vcg-disj-lift)[1]
  apply (clarsimp simp: no-fail-def)
done

```

```

lemma validNF-vcg-all-lift [wp]:
   $\llbracket \bigwedge x. \{P\ x\} f\ \{Q\ x\}! \rrbracket \implies \{\lambda s. \forall x. P\ x\ s\} f\ \{\lambda rv\ s. \forall x. Q\ x\ rv\ s\}!$ 
  apply atomize
  apply (rule validNF)
  apply (clarsimp simp: validNF-def)
  apply (rule hoare-vcg-all-lift)
  apply force
  apply (clarsimp simp: no-fail-def validNF-def)
done

```

```

lemma validNF-bind [wp-split]:
   $\llbracket \bigwedge x. \{B\ x\} g\ x\ \{C\}!; \{A\} f\ \{B\}! \rrbracket \implies$ 
   $\{A\} do\ x \leftarrow f; g\ x\ od\ \{C\}!$ 
  apply (rule validNF)
  apply (metis validNF-valid hoare-seq-ext)
  apply (clarsimp simp: no-fail-def validNF-def bind-def' valid-def)
  apply blast
done

```

lemmas validNF-seq-ext = validNF-bind

24.3 validNF compound rules

```

lemma validNF-state-assert [wp]:
   $\{\lambda s. P\ ()\ s \wedge G\ s\} state-assert\ G\ \{P\}!$ 
  apply (rule validNF)
  apply wpsimp
  apply (clarsimp simp: no-fail-def state-assert-def
    bind-def' assert-def return-def get-def)
done

```

```

lemma validNF-modify [wp]:
   $\{\lambda s. P\ ()\ (f\ s)\} modify\ f\ \{P\}!$ 
  apply (clarsimp simp: modify-def)

```

```

apply wp
done

lemma validNF-gets [wp]:
   $\llbracket \lambda s. P \ (f \ s) \ s \rrbracket \text{ gets } f \ \llbracket P \rrbracket!$ 
apply (clarsimp simp: gets-def)
apply wp
done

lemma validNF-condition [wp]:
   $\llbracket \llbracket Q \rrbracket A \ \llbracket P \rrbracket!; \llbracket R \rrbracket B \ \llbracket P \rrbracket! \rrbracket \implies \llbracket \lambda s. \text{ if } C \ s \text{ then } Q \ s \text{ else } R \ s \rrbracket \text{ condition } C$ 
   $A \ B \ \llbracket P \rrbracket!$ 
apply rule
apply (drule validNF-valid)+
apply (erule (1) condition-wp)
apply (drule validNF-no-fail)+
apply (clarsimp simp: no-fail-def condition-def)
done

lemma validNF-alt-def:
   $\text{validNF } P \ m \ Q = (\forall s. P \ s \longrightarrow ((\forall (r', s') \in \text{fst } (m \ s)). Q \ r' \ s') \wedge \neg \text{snd } (m \ s)))$ 
by (fastforce simp: validNF-def valid-def no-fail-def)

lemma validNF-assert [wp]:
   $\llbracket (\lambda s. P) \text{ and } (R \ ()) \rrbracket \text{ assert } P \ \llbracket R \rrbracket!$ 
apply (rule validNF)
apply (clarsimp simp: valid-def in-return)
apply (clarsimp simp: no-fail-def return-def)
done

lemma validNF-false-pre:
   $\llbracket \lambda -. \text{ False } \rrbracket P \ \llbracket Q \rrbracket!$ 
by (clarsimp simp: validNF-def no-fail-def)

lemma validNF-chain:
   $\llbracket \llbracket P' \rrbracket a \ \llbracket R' \rrbracket!; \bigwedge s. P \ s \implies P' \ s; \bigwedge r \ s. R' \ r \ s \implies R \ r \ s \rrbracket \implies \llbracket P \rrbracket a \ \llbracket R \rrbracket!$ 
by (fastforce simp: validNF-def valid-def no-fail-def Ball-def)

lemma validNF-case-prod [wp]:
   $\llbracket \bigwedge x \ y. \text{ validNF } (P \ x \ y) \ (B \ x \ y) \ Q \rrbracket \implies \text{ validNF } (\text{case-prod } P \ v) \ (\text{case-prod } (\lambda x$ 
   $y. B \ x \ y) \ v) \ Q$ 
by (metis prod.exhaust split-conv)

lemma validE-NF-case-prod [wp]:
   $\llbracket \bigwedge a \ b. \llbracket P \ a \ b \rrbracket f \ a \ b \ \llbracket Q \rrbracket, \llbracket E \rrbracket! \rrbracket \implies$ 
   $\llbracket \text{case } x \text{ of } (a, b) \Rightarrow P \ a \ b \rrbracket \text{ case } x \text{ of } (a, b) \Rightarrow f \ a \ b \ \llbracket Q \rrbracket, \llbracket E \rrbracket!$ 
apply (clarsimp simp: validE-NF-alt-def)
apply (erule validNF-case-prod)
done

```

lemma *no-fail-is-validNF-True*: *no-fail* $P\ s = (\llbracket P \rrbracket\ s\ \llbracket \lambda\ -. \ True \rrbracket!)$
by (*clarsimp simp: no-fail-def validNF-def valid-def*)

24.4 validNF reasoning in the exception monad

lemma *validE-NF [intro?]*:
 $\llbracket \llbracket P \rrbracket\ f\ \llbracket Q \rrbracket, \llbracket E \rrbracket! ; \text{no-fail } P\ f \rrbracket \Longrightarrow \llbracket P \rrbracket\ f\ \llbracket Q \rrbracket, \llbracket E \rrbracket!$
apply (*clarsimp simp: validE-NF-def*)
done

lemma *validE-NF-valid*:
 $\llbracket \llbracket P \rrbracket\ f\ \llbracket Q \rrbracket, \llbracket E \rrbracket! \rrbracket \Longrightarrow \llbracket P \rrbracket\ f\ \llbracket Q \rrbracket, \llbracket E \rrbracket$
apply (*clarsimp simp: validE-NF-def*)
done

lemma *validE-NF-no-fail*:
 $\llbracket \llbracket P \rrbracket\ f\ \llbracket Q \rrbracket, \llbracket E \rrbracket! \rrbracket \Longrightarrow \text{no-fail } P\ f$
apply (*clarsimp simp: validE-NF-def*)
done

lemma *validE-NF-weaken-pre[wp-pre]*:
 $\llbracket \llbracket Q \rrbracket\ a\ \llbracket R \rrbracket, \llbracket E \rrbracket! ; \bigwedge s. P\ s \Longrightarrow Q\ s \rrbracket \Longrightarrow \llbracket P \rrbracket\ a\ \llbracket R \rrbracket, \llbracket E \rrbracket!$
apply (*clarsimp simp: validE-NF-alt-def*)
apply (*erule validNF-weaken-pre*)
apply *simp*
done

lemma *validE-NF-post-comb-conj-L*:
 $\llbracket \llbracket P \rrbracket\ f\ \llbracket Q \rrbracket, \llbracket E \rrbracket! ; \llbracket P' \rrbracket\ f\ \llbracket Q' \rrbracket, \llbracket \lambda\ -. \ True \rrbracket \rrbracket \Longrightarrow \llbracket \lambda s. P\ s \wedge P'\ s \rrbracket\ f$
 $\llbracket \lambda rv\ s. Q\ rv\ s \wedge Q'\ rv\ s \rrbracket, \llbracket E \rrbracket!$
apply (*clarsimp simp: validE-NF-alt-def validE-def validNF-def*
valid-def no-fail-def split: sum.splits)
apply *force*
done

lemma *validE-NF-post-comb-conj-R*:
 $\llbracket \llbracket P \rrbracket\ f\ \llbracket Q \rrbracket, \llbracket \lambda\ -. \ True \rrbracket ; \llbracket P' \rrbracket\ f\ \llbracket Q' \rrbracket, \llbracket E \rrbracket! \rrbracket \Longrightarrow \llbracket \lambda s. P\ s \wedge P'\ s \rrbracket\ f$
 $\llbracket \lambda rv\ s. Q\ rv\ s \wedge Q'\ rv\ s \rrbracket, \llbracket E \rrbracket!$
apply (*clarsimp simp: validE-NF-alt-def validE-def validNF-def*
valid-def no-fail-def split: sum.splits)
apply *force*
done

lemma *validE-NF-post-comb-conj*:
 $\llbracket \llbracket P \rrbracket\ f\ \llbracket Q \rrbracket, \llbracket E \rrbracket! ; \llbracket P' \rrbracket\ f\ \llbracket Q' \rrbracket, \llbracket E \rrbracket! \rrbracket \Longrightarrow \llbracket \lambda s. P\ s \wedge P'\ s \rrbracket\ f\ \llbracket \lambda rv\ s. Q$
 $rv\ s \wedge Q'\ rv\ s \rrbracket, \llbracket E \rrbracket!$
apply (*clarsimp simp: validE-NF-alt-def validE-def validNF-def*
valid-def no-fail-def split: sum.splits)

apply *force*
done

lemma *validE-NF-chain*:

$\llbracket \{P\} a \{R\}, \{E\}! \rrbracket;$
 $\bigwedge s. P s \implies P' s;$
 $\bigwedge r' s'. R' r' s' \implies R r' s';$
 $\bigwedge r'' s''. E' r'' s'' \implies E r'' s'' \implies$
 $\llbracket \lambda s. P s \rrbracket a \llbracket \lambda r' s'. R r' s' \rrbracket, \llbracket \lambda r'' s''. E r'' s'' \rrbracket!$
by (*fastforce simp: validE-NF-def validE-def2 no-fail-def Ball-def split: sum.splits*)

lemma *validE-NF-bind-wp* [wp]:

$\llbracket \bigwedge x. \{B x\} g x \{C\}, \{E\}!; \{A\} f \{B\}, \{E\}! \rrbracket \implies \{A\} f >>=E (\lambda x. g x) \{C\}, \{E\}!$
apply (*unfold validE-NF-alt-def bindE-def*)
apply (*rule validNF-bind [rotated]*)
apply *assumption*
apply (*clarsimp simp: lift-def throwError-def split: sum.splits*)
apply *wpsimp*
done

lemma *validNF-catch* [wp]:

$\llbracket \bigwedge x. \{E x\} \text{handler } x \{Q\}!; \{P\} f \{Q\}, \{E\}! \rrbracket \implies \{P\} f <\text{catch}> (\lambda x. \text{handler } x) \{Q\}!$
apply (*unfold validE-NF-alt-def catch-def*)
apply (*rule validNF-bind [rotated]*)
apply *assumption*
apply (*clarsimp simp: lift-def throwError-def split: sum.splits*)
apply *wp*
done

lemma *validNF-throwError* [wp]:

$\{E e\} \text{throwError } e \{P\}, \{E\}!$
by (*unfold validE-NF-alt-def throwError-def o-def*) *wpsimp*

lemma *validNF-returnOk* [wp]:

$\{P e\} \text{returnOk } e \{P\}, \{E\}!$
by (*clarsimp simp: validE-NF-alt-def returnOk-def*) *wpsimp*

lemma *validNF-whenE* [wp]:

$(P \implies \{Q\} f \{R\}, \{E\}!) \implies \{if P \text{ then } Q \text{ else } R ()\} \text{whenE } P f \{R\}, \{E\}!$
unfolding *whenE-def* **by** *clarsimp wp*

lemma *validNF-nobindE* [wp]:

$\llbracket \{B\} g \{C\}, \{E\}!; \{A\} f \{ \lambda r s. B s \}, \{E\}! \rrbracket \implies$
 $\{A\} \text{doE } f; g \text{odE } \{C\}, \{E\}!$
by *clarsimp wp*

Setup triple rules for *validE-NF* so that we can use wp combinator rules.

definition *validE-NF-property* $Q\ E\ s\ b \equiv \neg\ \text{snd}\ (b\ s)$
 $\wedge (\forall (r', s') \in \text{fst}\ (b\ s). \text{case } r' \text{ of } \text{Inl } x \Rightarrow E\ x\ s' \mid \text{Inr } x \Rightarrow Q\ x\ s')$

lemma *validE-NF-is-triple* [wp-trip]:
 $\text{validE-NF}\ P\ f\ Q\ E = \text{triple-judgement}\ P\ f\ (\text{validE-NF-property}\ Q\ E)$
apply (*clarsimp simp: validE-NF-def validE-def2 no-fail-def triple-judgement-def*
validE-NF-property-def split: sum.splits)
apply *blast*
done

lemma *validNF-cong*:
 $\llbracket \bigwedge s. P\ s = P'\ s; \bigwedge s. P\ s \Longrightarrow m\ s = m'\ s; \bigwedge r'\ s'\ s. \llbracket P\ s; (r', s') \in \text{fst}\ (m\ s) \rrbracket \Longrightarrow Q\ r'\ s' = Q'\ r'\ s' \rrbracket \Longrightarrow$
 $(\llbracket P \rrbracket m\ \llbracket Q \rrbracket!) = (\llbracket P' \rrbracket m'\ \llbracket Q' \rrbracket!)$
by (*fastforce simp: validNF-alt-def*)

lemma *validE-NF-liftE* [wp]:
 $\llbracket P \rrbracket f\ \llbracket Q \rrbracket! \Longrightarrow \llbracket P \rrbracket\ \text{liftE}\ f\ \llbracket Q \rrbracket, \llbracket E \rrbracket!$
by (*wpsimp simp: validE-NF-alt-def liftE-def*)

lemma *validE-NF-handleE'* [wp]:
 $\llbracket \bigwedge x. \llbracket F\ x \rrbracket\ \text{handler}\ x\ \llbracket Q \rrbracket, \llbracket E \rrbracket!; \llbracket P \rrbracket f\ \llbracket Q \rrbracket, \llbracket F \rrbracket! \rrbracket \Longrightarrow$
 $\llbracket P \rrbracket f\ <\text{handle2}> (\lambda x. \text{handler}\ x)\ \llbracket Q \rrbracket, \llbracket E \rrbracket!$
apply (*unfold validE-NF-alt-def handleE'-def*)
apply (*rule validNF-bind [rotated]*)
apply *assumption*
apply (*clarsimp split: sum.splits*)
apply *wpsimp*
done

lemma *validE-NF-handleE* [wp]:
 $\llbracket \bigwedge x. \llbracket F\ x \rrbracket\ \text{handler}\ x\ \llbracket Q \rrbracket, \llbracket E \rrbracket!; \llbracket P \rrbracket f\ \llbracket Q \rrbracket, \llbracket F \rrbracket! \rrbracket \Longrightarrow$
 $\llbracket P \rrbracket f\ <\text{handle}> \text{handler}\ \llbracket Q \rrbracket, \llbracket E \rrbracket!$
apply (*unfold handleE-def*)
apply (*metis validE-NF-handleE'*)
done

lemma *validE-NF-condition* [wp]:
 $\llbracket \llbracket Q \rrbracket A\ \llbracket P \rrbracket, \llbracket E \rrbracket!; \llbracket R \rrbracket B\ \llbracket P \rrbracket, \llbracket E \rrbracket! \rrbracket$
 $\Longrightarrow \llbracket \lambda s. \text{if } C\ s \text{ then } Q\ s \text{ else } R\ s \rrbracket\ \text{condition}\ C\ A\ B\ \llbracket P \rrbracket, \llbracket E \rrbracket!$
apply *rule*
apply (*drule validE-NF-valid*) +
apply *wp*
apply (*drule validE-NF-no-fail*) +
apply (*clarsimp simp: no-fail-def condition-def*)
done

Strengthen setup.

context *strengthen-implementation* **begin**

lemma *strengthen-hoare* [strg]:
 $(\bigwedge r s. st F \longrightarrow (Q r s) (R r s))$
 $\implies st F \longrightarrow (\llbracket P \rrbracket f \llbracket Q \rrbracket) (\llbracket P \rrbracket f \llbracket R \rrbracket)$
by (cases *F*, auto elim: hoare-strengthen-post)

lemma *strengthen-validE-R-cong*[strg]:
 $(\bigwedge r s. st F \longrightarrow (Q r s) (R r s))$
 $\implies st F \longrightarrow (\llbracket P \rrbracket f \llbracket Q \rrbracket, -) (\llbracket P \rrbracket f \llbracket R \rrbracket, -)$
by (cases *F*, auto intro: hoare-post-imp-R)

lemma *strengthen-validE-cong*[strg]:
 $(\bigwedge r s. st F \longrightarrow (Q r s) (R r s))$
 $\implies (\bigwedge r s. st F \longrightarrow (S r s) (T r s))$
 $\implies st F \longrightarrow (\llbracket P \rrbracket f \llbracket Q \rrbracket, \llbracket S \rrbracket) (\llbracket P \rrbracket f \llbracket R \rrbracket, \llbracket T \rrbracket)$
by (cases *F*, auto elim: hoare-post-impErr)

lemma *strengthen-validE-E-cong*[strg]:
 $(\bigwedge r s. st F \longrightarrow (S r s) (T r s))$
 $\implies st F \longrightarrow (\llbracket P \rrbracket f -, \llbracket S \rrbracket) (\llbracket P \rrbracket f -, \llbracket T \rrbracket)$
by (cases *F*, auto elim: hoare-post-impErr simp: validE-E-def)

lemma *wpfix-strengthen-hoare*:
 $(\bigwedge s. st (\neg F) \longrightarrow (P s) (P' s))$
 $\implies (\bigwedge r s. st F \longrightarrow (Q r s) (Q' r s))$
 $\implies st F \longrightarrow (\llbracket P \rrbracket f \llbracket Q \rrbracket) (\llbracket P' \rrbracket f \llbracket Q' \rrbracket)$
by (cases *F*, auto elim: hoare-chain)

lemma *wpfix-strengthen-validE-R-cong*:
 $(\bigwedge s. st (\neg F) \longrightarrow (P s) (P' s))$
 $\implies (\bigwedge r s. st F \longrightarrow (Q r s) (Q' r s))$
 $\implies st F \longrightarrow (\llbracket P \rrbracket f \llbracket Q \rrbracket, -) (\llbracket P' \rrbracket f \llbracket Q' \rrbracket, -)$
by (cases *F*, auto elim: hoare-chainE simp: validE-R-def)

lemma *wpfix-strengthen-validE-cong*:
 $(\bigwedge s. st (\neg F) \longrightarrow (P s) (P' s))$
 $\implies (\bigwedge r s. st F \longrightarrow (Q r s) (R r s))$
 $\implies (\bigwedge r s. st F \longrightarrow (S r s) (T r s))$
 $\implies st F \longrightarrow (\llbracket P \rrbracket f \llbracket Q \rrbracket, \llbracket S \rrbracket) (\llbracket P' \rrbracket f \llbracket R \rrbracket, \llbracket T \rrbracket)$
by (cases *F*, auto elim: hoare-chainE)

lemma *wpfix-strengthen-validE-E-cong*:
 $(\bigwedge s. st (\neg F) \longrightarrow (P s) (P' s))$
 $\implies (\bigwedge r s. st F \longrightarrow (S r s) (T r s))$
 $\implies st F \longrightarrow (\llbracket P \rrbracket f -, \llbracket S \rrbracket) (\llbracket P' \rrbracket f -, \llbracket T \rrbracket)$
by (cases *F*, auto elim: hoare-chainE simp: validE-E-def)

lemma *wpfix-no-fail-cong*:
 $(\bigwedge s. st (\neg F) \longrightarrow (P s) (P' s))$

```

 $\Rightarrow st\ F\ (\longrightarrow)\ (no\text{-}fail\ P\ f)\ (no\text{-}fail\ P'\ f)$ 
by (cases  $F$ , auto elim: no-fail-pre)

```

```

lemmas nondet-wpfix-strgs =
  wpfix-strengthen-validE-R-cong
  wpfix-strengthen-validE-E-cong
  wpfix-strengthen-validE-cong
  wpfix-strengthen-hoare
  wpfix-no-fail-cong

```

```

end

```

```

lemmas nondet-wpfix-strgs[wp-fix-strgs]
  = strengthen-implementation.nondet-wpfix-strgs

```

```

end

```

25 lsm hooks [lsm_hooks]

```

theory LSM-Cap
imports
  Element
  ../lib/Monad-WP/NonDetMonadVCG

```

```

begin

```

```

definition ns-capable :: user-namespace  $\Rightarrow$  int  $\Rightarrow$  bool
  where ns-capable ns cap  $\equiv$  True

```

```

definition cap-inode-setxattr :: 's  $\Rightarrow$  dentry  $\Rightarrow$  xattr  $\Rightarrow$  string  $\Rightarrow$  int  $\Rightarrow$  int  $\Rightarrow$  ('s,
int) nondet-monad
  where cap-inode-setxattr s dentry name value size' flags'  $\equiv$  do
    ns  $\leftarrow$  return (s-user-ns (d-sb dentry));
    rc  $\leftarrow$  (if name  $\neq$  XATTR-SECURITY-PREFIX then return 0 else
      if name = XATTR-NAME-CAPS then return 0 else
      if  $\neg$ (ns-capable ns CAP-SYS-ADMIN) then return ( $-$ EPERM) else
      return 0);
    return(rc)
  od

```

```

definition CAP-TO-INDEX x  $\equiv$  ((x) >> 5)

```

```

definition CAP-TO-MASK x  $\equiv$  (1 << (nat(x AND 31)))

```

```

term (kcap k) ! (nat(CAP-TO-INDEX flag))

```

```

definition cap-raised :: kernel-cap-t  $\Rightarrow$  int  $\Rightarrow$  int

```

```

  where cap-raised k flag  $\equiv$  ((kcap k) ! (nat(CAP-TO-INDEX flag))) AND (CAP-TO-MASK
flag)

```

end

26 lsm hooks [lsm_hooks]

```
theory Linux-LSM-Hooks
  imports
    Element
    ../lib/Monad-WP/NonDetMonadVCG
    SOAC
```

begin

In this theory, we introduce LSM hooks

26.1 lsm hook

```
locale lsm-superblock-hooks =
  fixes s0 :: 's
  fixes state :: 's
  fixes sb-security :: 's  $\Rightarrow$  super-block  $\Rightarrow$  'sbsec option
  fixes hook-sb-alloc :: 's  $\Rightarrow$  super-block  $\Rightarrow$  ('s, int) nondet-monad
  fixes hook-sb-free :: 's  $\Rightarrow$  super-block  $\Rightarrow$  ('s, unit) nondet-monad
  fixes hook-sb-copy-data :: 's  $\Rightarrow$  string  $\Rightarrow$  string  $\Rightarrow$  ('s, int) nondet-monad
  fixes hook-sb-remount :: 's  $\Rightarrow$  super-block  $\Rightarrow$  Void  $\Rightarrow$  ('s, int) nondet-monad
  fixes hook-sb-kern-mount :: 's  $\Rightarrow$  super-block  $\Rightarrow$  int  $\Rightarrow$  string  $\Rightarrow$  ('s, int) nondet-monad
  fixes hook-sb-show-options :: 's  $\Rightarrow$  seq-file  $\Rightarrow$  super-block  $\Rightarrow$  ('s, int) nondet-monad
  fixes hook-sb-statfs :: 's  $\Rightarrow$  dentry  $\Rightarrow$  ('s, int) nondet-monad
  fixes hook-sb-mount :: 's  $\Rightarrow$  string  $\Rightarrow$  path  $\Rightarrow$  string  $\Rightarrow$  int  $\Rightarrow$  Void  $\Rightarrow$  ('s, int)
nondet-monad
  fixes hook-sb-umount :: 's  $\Rightarrow$  vfsmount  $\Rightarrow$  int  $\Rightarrow$  ('s, int) nondet-monad
  fixes hook-sb-pivotroot :: 's  $\Rightarrow$  path  $\Rightarrow$  path  $\Rightarrow$  ('s, int) nondet-monad
  fixes hook-sb-set-mnt-opts :: 's  $\Rightarrow$  super-block  $\Rightarrow$  opts  $\Rightarrow$  nat  $\Rightarrow$  nat  $\Rightarrow$  ('s, int)
nondet-monad
  fixes hook-sb-clone-mnt-opts :: 's  $\Rightarrow$  super-block  $\Rightarrow$  super-block  $\Rightarrow$  int  $\Rightarrow$  int
 $\Rightarrow$  ('s, int) nondet-monad
  fixes hook-sb-parse-opts-str :: 's  $\Rightarrow$  string  $\Rightarrow$  opts  $\Rightarrow$  ('s, int) nondet-monad

  assumes stb-sb-alloc-hook :
     $\bigwedge sa. \{ \lambda s. s = sa \} \text{hook-sb-alloc } s \text{ sb } \{ \lambda r s. r = 0 \vee r = -ENOMEM \}$ 
  assumes stb-sb-free :
     $\bigwedge sa. \{ \lambda s. s = sa \} \text{hook-sb-free } s \text{ sb } \{ \lambda r s. r = \text{unit} \}$ 
  assumes stb-sb-copy-data :
     $\{ \lambda s. \text{True} \} \text{hook-sb-copy-data } s \text{ orig } \text{smackopts } \{ \lambda r s. s = sa \wedge (r = 0 \vee r =$ 
     $(\text{uminus } 12)) \}$ 
  assumes stb-sb-remount :
     $\bigwedge sa. \{ \lambda s. s = sa \} \text{hook-sb-remount } s \text{ sb } \text{data}' \{ \lambda r s. s = sa \wedge (r = 0 \vee r$ 
     $\neq 0) \}$ 
  assumes stb-sb-kern-mount :
```

$\bigwedge sa. \{ \lambda s . s = sa \} \text{ hook-sb-kern-mount } s \text{ sb flag data } \{ \lambda r s . s = sa \wedge (r = 0 \vee r \neq 0) \}$
assumes *stb-sb-show-options* :
 $\bigwedge sa. \{ \lambda s . s = sa \} \text{ hook-sb-show-options } s \text{ sq sb } \{ \lambda r s . s = sa \wedge (r = 0 \vee r \neq 0) \}$
assumes *stb-sb-statfs* :
 $\bigwedge sa. \{ \lambda s . s = sa \} \text{ hook-sb-statfs } s \text{ d } \{ \lambda r s . s = sa \wedge (r = 0 \vee r \neq 0) \}$
assumes *stb-sb-mount* :
 $\bigwedge sa. \{ \lambda s . s = sa \} \text{ hook-sb-mount } s \text{ devname path type flag data' } \{ \lambda r s . s = sa \wedge (r = 0 \vee r \neq 0) \}$
assumes *stb-sb-umount* :
 $\bigwedge sa. \{ \lambda s . s = sa \} \text{ hook-sb-umount } s \text{ mnt' flag } \{ \lambda r s . s = sa \wedge (r = 0 \vee r \neq 0) \}$
assumes *stb-sb-pivotroot* :
 $\bigwedge sa. \{ \lambda s . s = sa \} \text{ hook-sb-pivotroot } s \text{ old-path new-path } \{ \lambda r s . s = sa \wedge (r = 0 \vee r \neq 0) \}$
assumes *stb-sb-set-mnt-opts* :
 $\bigwedge sa. \{ \lambda s . s = sa \} \text{ hook-sb-set-mnt-opts } s \text{ sb opt kflag sflag } \{ \lambda r s . s = sa \wedge (r = 0 \vee r \neq 0) \}$
assumes *stb-sb-clone-mnt-opts* :
 $\bigwedge sa. \{ \lambda s . s = sa \} \text{ hook-sb-clone-mnt-opts } s \text{ oldsb newsb kflag sflag } \{ \lambda r s . s = sa \wedge (r = 0 \vee r \neq 0) \}$
assumes *stb-parse-opts-str* :
 $\bigwedge sa. \{ \lambda s . s = sa \} \text{ hook-sb-parse-opts-str } s \text{ str opt } \{ \lambda r s . s = sa \wedge (r = 0 \vee r \neq 0) \}$

locale *lsm-task-hooks* =

fixes *s0* :: 's

fixes *t-security* :: 's \Rightarrow Cred \Rightarrow 'tsec option

fixes *hook-task-alloc* :: 's \Rightarrow Task \Rightarrow nat \Rightarrow ('s, int) nondet-monad

fixes *hook-task-free* :: 's \Rightarrow Task \Rightarrow ('s, unit) nondet-monad

fixes *hook-cred-alloc-blank* :: 's \Rightarrow Cred \Rightarrow nat \Rightarrow ('s, int) nondet-monad

fixes *hook-cred-free* :: 's \Rightarrow Cred \Rightarrow ('s, unit) nondet-monad

fixes *hook-prepare-creds* :: 's \Rightarrow Cred \Rightarrow Cred \Rightarrow nat \Rightarrow ('s, int) nondet-monad

fixes *hook-transfer-creds* :: 's \Rightarrow Cred \Rightarrow Cred \Rightarrow ('s, unit) nondet-monad

fixes *hook-cred-getsecid* :: 's \Rightarrow Cred \Rightarrow u32 \Rightarrow ('s, unit) nondet-monad

fixes *hook-task-fix-setuid* :: 's \Rightarrow Cred \Rightarrow Cred \Rightarrow int \Rightarrow ('s, int) nondet-monad

fixes *hook-task-setpgid* :: 's \Rightarrow Task \Rightarrow pid-t \Rightarrow ('s, int) nondet-monad

fixes *hook-task-getpgid* :: 's \Rightarrow Task \Rightarrow ('s, int) nondet-monad

fixes *hook-task-getsid* :: 's \Rightarrow Task \Rightarrow ('s, int) nondet-monad

fixes *hook-task-getsecid* :: 's \Rightarrow Task \Rightarrow u32 \Rightarrow ('s, unit) nondet-monad

fixes *hook-task-setnice* :: 's \Rightarrow Task \Rightarrow int \Rightarrow ('s, int) nondet-monad

fixes *hook-task-setioprio* :: 's \Rightarrow Task \Rightarrow int \Rightarrow ('s, int) nondet-monad

fixes *hook-task-getsid* :: 's \Rightarrow Task \Rightarrow ('s, int) nondet-monad

fixes *hook-task-prlimit* :: 's \Rightarrow Cred \Rightarrow Cred \Rightarrow nat \Rightarrow ('s, int) nondet-monad

fixes *hook-task-setrlimit* :: 's \Rightarrow Task \Rightarrow nat \Rightarrow rlimit \Rightarrow ('s, int) nondet-monad

fixes *hook-task-setscheduler* :: 's \Rightarrow Task \Rightarrow ('s, int) nondet-monad

fixes *hook-task-getscheduler* :: 's \Rightarrow Task \Rightarrow ('s, int) nondet-monad

fixes *hook-task-movememory* :: 's \Rightarrow Task \Rightarrow ('s, int) nondet-monad
fixes *hook-task-kill* :: 's \Rightarrow Task \Rightarrow siginfo \Rightarrow int \Rightarrow Cred option \Rightarrow ('s, int) nondet-monad
fixes *hook-task-prctl* :: 's \Rightarrow int \Rightarrow nat \Rightarrow nat \Rightarrow nat \Rightarrow nat \Rightarrow ('s, int) nondet-monad
fixes *hook-task-to-inode* :: 's \Rightarrow Task \Rightarrow inode \Rightarrow ('s, unit) nondet-monad

assumes *stb-task-alloc* :
 $\bigwedge sa. \{\lambda s. s = sa\} \text{hook-task-alloc } s \text{ task } cflag \{\lambda r s. r = 0 \vee r \neq 0\}$
assumes *stb-task-free* :
 $\bigwedge sa. \{\lambda s. s = sa\} \text{hook-task-free } s \text{ task } \{\lambda r s. r = \text{unit}\}$
assumes *stb-cred-alloc-blank* :
 $\bigwedge sa. \{\lambda s. s = sa\} \text{hook-cred-alloc-blank } s \text{ cred' gfp' } \{\lambda r s. r = 0 \vee r \neq 0\}$
assumes *stb-cred-free* :
 $\bigwedge sa. \{\lambda s. s = sa\} \text{hook-cred-free } s c \{\lambda r s. r = \text{unit}\}$
assumes *stb-prepare-creds* :
 $\bigwedge sa. \{\lambda s. s = sa\} \text{hook-prepare-creds } s \text{ new' old gfp' } \{\lambda r s. s = sa \wedge (r = 0 \vee r \neq 0)\}$
assumes *stb-transfer-creds* :
 $\bigwedge sa. \{\lambda s. s = sa\} \text{hook-transfer-creds } s \text{ new' old } \{\lambda r s. r = \text{unit}\}$
assumes *stb-task-setpgid*:
 $\bigwedge sa. \{\lambda s. s = sa\} \text{hook-task-setpgid } s t \text{ pid } \{\lambda r s. s = sa \wedge (r = 0 \vee r \neq 0)\}$
assumes *stb-task-getpgid*:
 $\bigwedge sa. \{\lambda s. s = sa\} \text{hook-task-getpgid } s t \{\lambda r s. s = sa \wedge (r = 0 \vee r \neq 0)\}$
assumes *stb-task-getsid*:
 $\bigwedge sa. \{\lambda s. s = sa\} \text{hook-task-getsid } s t \{\lambda r s. s = sa \wedge (r = 0 \vee r \neq 0)\}$
assumes *stb-task-getsecid*:
 $\bigwedge sa. \{\lambda s. s = sa\} \text{hook-task-getsecid } s t \text{ secid' } \{\lambda r s. r = \text{unit}\}$
assumes *stb-task-setnice*:
 $\bigwedge sa. \{\lambda s. s = sa\} \text{hook-task-setnice } s t \text{ nice } \{\lambda r s. s = sa \wedge (r = 0 \vee r \neq 0)\}$
assumes *stb-task-setioprio*:
 $\bigwedge sa. \{\lambda s. s = sa\} \text{hook-task-setioprio } s t \text{ ioprio } \{\lambda r s. s = sa \wedge (r = 0 \vee r \neq 0)\}$
assumes *stb-task-getioprio*:
 $\bigwedge sa. \{\lambda s. s = sa\} \text{hook-task-getioprio } s t \{\lambda r s. s = sa \wedge (r = 0 \vee r \neq 0)\}$
assumes *stb-task-setrlimit*:
 $\bigwedge sa. \{\lambda s. s = sa\} \text{hook-task-setrlimit } s t \text{ resource new } \{\lambda r s. s = sa \wedge (r = 0 \vee r \neq 0)\}$
assumes *stb-task-setscheduler*:
 $\bigwedge sa. \{\lambda s. s = sa\} \text{hook-task-setscheduler } s t \{\lambda r s. s = sa \wedge (r = 0 \vee r \neq 0)\}$
assumes *stb-task-getscheduler*:
 $\bigwedge sa. \{\lambda s. s = sa\} \text{hook-task-getscheduler } s t \{\lambda r s. s = sa \wedge (r = 0 \vee r \neq 0)\}$
assumes *stb-task-movememory*:
 $\bigwedge sa. \{\lambda s. s = sa\} \text{hook-task-movememory } s t \{\lambda r s. s = sa \wedge (r = 0 \vee r \neq 0)\}$

```

≠ 0) }
assumes stb-task-kill:
   $\bigwedge sa. \{ \lambda s. s = sa \} \text{hook-task-kill } s \ t \ \text{info } sig \ c' \{ \lambda r \ s. s = sa \wedge (r = 0 \vee r \neq 0) \}$ 
assumes stb-task-prctl :
   $\bigwedge sa. \{ \lambda s. s = sa \} \text{hook-task-prctl } s \ opt' \ arg2 \ arg3 \ arg4 \ arg5 \{ \lambda r \ s. s = sa \wedge (r = 0 \vee r \neq 0) \}$ 
assumes stb-task-to-inode :
   $\bigwedge sa. \{ \lambda s. s = sa \} \text{hook-task-to-inode } s \ t \ inode \{ \lambda r \ s. r = unit \}$ 

locale lsm-binder-hooks =
  fixes s0 :: 's
  fixes hook-binder-set-context-mgr :: 's  $\Rightarrow$  Task  $\Rightarrow$  ('s, int) nondet-monad
  fixes hook-binder-transaction :: 's  $\Rightarrow$  Task  $\Rightarrow$  Task  $\Rightarrow$  ('s, int) nondet-monad
  fixes hook-binder-transfer-binder :: 's  $\Rightarrow$  Task  $\Rightarrow$  Task  $\Rightarrow$  ('s, int) nondet-monad
  fixes hook-binder-transfer-file :: 's  $\Rightarrow$  Task  $\Rightarrow$  Task  $\Rightarrow$  Files  $\Rightarrow$  ('s, int) nondet-monad

  assumes stb-binder-set-context-mgr :
     $\bigwedge sa. \{ \lambda s. s = sa \} \text{hook-binder-set-context-mgr } s \ mgr \{ \lambda r \ s. s = sa \wedge (r = 0 \vee r \neq 0) \}$ 
  assumes stb-binder-transaction :
     $\bigwedge sa. \{ \lambda s. s = sa \} \text{hook-binder-transaction } s \ from \ to \{ \lambda r \ s. s = sa \wedge (r = 0 \vee r \neq 0) \}$ 
  assumes stb-binder-transfer-binder :
     $\bigwedge sa. \{ \lambda s. s = sa \} \text{hook-binder-transfer-binder } s \ from \ to \{ \lambda r \ s. s = sa \wedge (r = 0 \vee r \neq 0) \}$ 
  assumes stb-binder-transfer-file:
     $\bigwedge sa. \{ \lambda s. s = sa \} \text{hook-binder-transfer-file } s \ from \ to \ file \{ \lambda r \ s. s = sa \wedge (r = 0 \vee r \neq 0) \}$ 

locale lsm-pttrace-hooks =
  fixes s0 :: 's

  fixes hook-pttrace-access-check :: 's  $\Rightarrow$  Task  $\Rightarrow$  nat  $\Rightarrow$  ('s, int) nondet-monad

  fixes hook-pttrace-traceme :: 's  $\Rightarrow$  Task  $\Rightarrow$  ('s, int) nondet-monad
  assumes stb-pttrace-access-check :
     $\bigwedge sa. \{ \lambda s. s = sa \} \text{hook-pttrace-access-check } s \ child \ m \{ \lambda r \ s. s = sa \wedge (r = 0 \vee r \neq 0) \}$ 
  assumes stb-pttrace-traceme:
     $\bigwedge sa. \{ \lambda s. s = sa \} \text{hook-pttrace-traceme } s \ parent' \{ \lambda r \ s. s = sa \wedge (r = 0 \vee r \neq 0) \}$ 

locale lsm-capable-hooks =
  fixes s0 :: 's

```

```

fixes hook-capget :: 's ⇒ Task ⇒ kct ⇒ kct ⇒ kct ⇒ ('s, int) nondet-monad
fixes hook-capset :: 's ⇒ Cred ⇒ Cred ⇒ kct ⇒ kct ⇒ kct ⇒ ('s, int) nondet-monad
fixes hook-capable :: 's ⇒ Cred ⇒ ns ⇒ cap ⇒ ('s, int) nondet-monad
fixes hook-capable-noaudit :: 's ⇒ Cred ⇒ ns ⇒ cap ⇒ ('s, int) nondet-monad
fixes hook-quotactl :: 's ⇒ int ⇒ int ⇒ int ⇒ super-block option ⇒ ('s, int)
nondet-monad
fixes hook-quota-on :: 's ⇒ dentry ⇒ ('s, int) nondet-monad
fixes hook-syslog :: 's ⇒ int ⇒ ('s, int) nondet-monad
fixes hook-settime64 :: 's ⇒ ts ⇒ tz option ⇒ ('s, int) nondet-monad
fixes hook-vm-enough-memory-mm :: 's ⇒ mm ⇒ pages ⇒ ('s, int) nondet-monad
assumes stb-capget :
  ∧sa. {λs . s = sa } hook-capget s target effective inheritable permitted
    {λr s. s = sa ∧ (r = 0 ∨ r ≠ 0)}
assumes stb-capset :
  ∧sa. {λs . s = sa } hook-capset s new old effective inheritable permitted
    {λr s. s = sa ∧ (r = 0 ∨ r ≠ 0)}
assumes stb-capable :
  ∧sa. {λs . s = sa } hook-capable s c ns cap {λr s. s = sa ∧ (r = 0 ∨ r ≠
0)}
assumes stb-capable-noaudit :
  ∧sa. {λs . s = sa } hook-capable-noaudit s c ns cap {λr s. s = sa ∧ (r = 0
∨ r ≠ 0)}
assumes stb-quotactl :
  ∧sa. {λs . s = sa } hook-quotactl s cmds t id' sb {λr s. s = sa ∧ (r = 0 ∨
r ≠ 0)}
assumes stb-quota-on :
  ∧sa. {λs . s = sa } hook-quota-on s dentry {λr s. s = sa ∧ (r = 0 ∨ r ≠
0)}
assumes stb-syslog :
  ∧sa. {λs . s = sa } hook-syslog s type {λr s. s = sa ∧ (r = 0 ∨ r ≠ 0)}
assumes stb-settime64 :
  ∧sa. {λs . s = sa } hook-settime64 s ts tz {λr s. s = sa ∧ (r = 0 ∨ r ≠ 0)}

assumes stb-vm-enough-memory-mm :
  ∧sa. {λs . s = sa } hook-vm-enough-memory-mm s mm' pages {λr s. s = sa
∧ (r = 0 ∨ r ≠ 0)}

```

locale lsm-bprm-hooks =

```

fixes s0 :: 's
fixes hook-bprm-set-creds :: 's ⇒ linux-binprm ⇒ ('s, int) nondet-monad
fixes hook-bprm-check :: 's ⇒ linux-binprm ⇒ ('s, int) nondet-monad
fixes hook-bprm-committing-creds :: 's ⇒ linux-binprm ⇒ ('s, unit) nondet-monad
fixes hook-bprm-committed-creds :: 's ⇒ linux-binprm ⇒ ('s, unit) nondet-monad

assumes stb-bprm-set-creds :
  ∧sa. {λs . s = sa } hook-bprm-set-creds s bprm {λr s. s = sa ∧ (r = 0 ∨ r
≠ 0)}

```

```

assumes stb-bprm-check :
   $\bigwedge sa. \{ \lambda s. s = sa \} \text{hook-bprm-check } s \text{ bprm } \{ \lambda r s. s = sa \wedge (r = 0 \vee r \neq 0) \}$ 
assumes stb-bprm-committing-creds :
   $\bigwedge sa. \{ \lambda s. s = sa \} \text{hook-bprm-committing-creds } s \text{ bprm } \{ \lambda r s. r = \text{unit} \}$ 
assumes stb-bprm-committed-creds :
   $\bigwedge sa. \{ \lambda s. s = sa \} \text{hook-bprm-committed-creds } s \text{ bprm } \{ \lambda r s. r = \text{unit} \}$ 

locale lsm-file-hooks =
  fixes s0 :: 's
  fixes access :: 's  $\Rightarrow$  Subj  $\Rightarrow$  Obj  $\Rightarrow$  access  $\Rightarrow$  bool
  fixes current :: 's  $\Rightarrow$  process-id
  fixes f-security :: 's  $\Rightarrow$  Files  $\Rightarrow$  'fsec option
  fixes hook-file-permission :: 's  $\Rightarrow$  Files  $\Rightarrow$  int  $\Rightarrow$  ('s, int) nondet-monad
  fixes hook-file-alloc :: 's  $\Rightarrow$  Files  $\Rightarrow$  ('s, int) nondet-monad
  fixes hook-file-free :: 's  $\Rightarrow$  Files  $\Rightarrow$  ('s, unit) nondet-monad
  fixes hook-file-ioctl :: 's  $\Rightarrow$  Files  $\Rightarrow$  IOC-DIR  $\Rightarrow$  nat  $\Rightarrow$  ('s, int) nondet-monad
  fixes hook-mmap-file :: 's  $\Rightarrow$  Files option  $\Rightarrow$  nat  $\Rightarrow$  nat  $\Rightarrow$  nat  $\Rightarrow$  ('s, int) nondet-monad
  fixes hook-mmap-addr :: 's  $\Rightarrow$  nat  $\Rightarrow$  ('s, int) nondet-monad
  fixes hook-file-mprotect :: 's  $\Rightarrow$  vm-area-struct  $\Rightarrow$  nat  $\Rightarrow$  nat  $\Rightarrow$  ('s, int) nondet-monad
  fixes hook-file-lock :: 's  $\Rightarrow$  Files  $\Rightarrow$  nat  $\Rightarrow$  ('s, int) nondet-monad
  fixes hook-file-fcntl :: 's  $\Rightarrow$  Files  $\Rightarrow$  nat  $\Rightarrow$  nat  $\Rightarrow$  ('s, int) nondet-monad
  fixes hook-file-set-fowner :: 's  $\Rightarrow$  Files  $\Rightarrow$  ('s, unit) nondet-monad
  fixes hook-file-send-sigiotask :: 's  $\Rightarrow$  Task  $\Rightarrow$  fown-struct  $\Rightarrow$  int  $\Rightarrow$  ('s, int)
nondet-monad
  fixes hook-file-receive :: 's  $\Rightarrow$  Files  $\Rightarrow$  ('s, int) nondet-monad
  fixes hook-file-open :: 's  $\Rightarrow$  Files  $\Rightarrow$  ('s, int) nondet-monad

  assumes stb-file-permission :
     $\bigwedge sa \text{ file mask}. \{ \lambda s. s = sa \} \text{hook-file-permission } sa \text{ file mask} \{ \lambda r s. s = sa \wedge (r = 0 \vee r \neq 0) \}$ 
  assumes stb-file-alloc-security :
     $\bigwedge sa \text{ file}. \{ \lambda s. s = sa \wedge f\text{-security } s \text{ file} = \text{None} \} \text{hook-file-alloc } sa \text{ file} \{ \lambda r s. (r = 0 \wedge f\text{-security } s \text{ file} \neq \text{None} \wedge s \neq sa) \vee (r \neq 0 \wedge s = sa) \}$ 
  assumes stb-file-free-security :
     $\bigwedge sa \text{ file}. \{ \lambda s. s = sa \} \text{hook-file-free } sa \text{ file} \{ \lambda r s. r = \text{unit} \wedge f\text{-security } s \text{ file} = \text{None} \}$ 
  assumes stb-file-ioctl :
     $\bigwedge sa. \{ \lambda s. s = sa \} \text{hook-file-ioctl } sa \text{ file cmd arg } \{ \lambda r s. s = sa \}$ 
  assumes file-ioctl-ac :
     $(\exists p. \text{access } s (\text{current } s) (\text{File } \text{file}) p = \text{True} \longrightarrow \{ \lambda s. \text{True} \} \text{hook-file-ioctl } sa \text{ file cmd arg } \{ \lambda r s. r = 0 \}) \vee$ 
     $(\exists p. \text{access } s (\text{current } s) (\text{File } \text{file}) p = \text{False} \longrightarrow \{ \lambda s. \text{True} \} \text{hook-file-ioctl } sa \text{ file cmd arg } \{ \lambda r s. r \neq 0 \})$ 
  assumes stb-mmap-addr :

```



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 $\bigwedge sa. \llbracket \lambda s. s = sa \rrbracket \text{hook-mmap-addr } sa \text{ addr } \llbracket \lambda r s. s = sa \wedge (r = 0 \vee r \neq 0) \rrbracket$ 

assumes stb-mmap-file :
   $\bigwedge sa. \llbracket \lambda s. s = sa \rrbracket \text{hook-mmap-file } sa \text{ file' prot mprot flgs } \llbracket \lambda r s. s = sa \wedge (r = 0 \vee r \neq 0) \rrbracket$ 
assumes stb-file-mprotect :
   $\bigwedge sa. \llbracket \lambda s. s = sa \rrbracket \text{hook-file-mprotect } sa \text{ vma reqprot prot } \llbracket \lambda r s. s = sa \wedge (r = 0 \vee r \neq 0) \rrbracket$ 
assumes stb-file-lock :
   $\bigwedge sa. \llbracket \lambda s. s = sa \rrbracket \text{hook-file-lock } sa \text{ file fcmd } \llbracket \lambda r s. s = sa \wedge (r = 0 \vee r \neq 0) \rrbracket$ 
assumes stb-file-fcntl :
   $\bigwedge sa. \llbracket \lambda s. s = sa \rrbracket \text{hook-file-fcntl } sa \text{ file fcmd arg } \llbracket \lambda r s. s = sa \wedge (r = 0 \vee r \neq 0) \rrbracket$ 
assumes stb-file-set-fowner :
   $\bigwedge sa \text{ file. } \llbracket \lambda s. s = sa \rrbracket \text{hook-file-set-fowner } sa \text{ file } \llbracket \lambda r s. r = \text{unit} \rrbracket$ 
assumes stb-file-send-sigiotask :
   $\bigwedge sa. \llbracket \lambda s. s = sa \rrbracket \text{hook-file-send-sigiotask } sa \text{ tsk' fown sig } \llbracket \lambda r s. s = sa \wedge (r = 0 \vee r \neq 0) \rrbracket$ 
assumes stb-file-receive :
   $\bigwedge sa. \llbracket \lambda s. s = sa \rrbracket \text{hook-file-receive } sa \text{ file } \llbracket \lambda r s. s = sa \wedge (r = 0 \vee r \neq 0) \rrbracket$ 
assumes stb-file-open :
   $\bigwedge sa. \llbracket \lambda s. s = sa \rrbracket \text{hook-file-open } sa \text{ file } \llbracket \lambda r s. s = sa \wedge (r = 0 \vee r \neq 0) \rrbracket$ 

begin
end

```

locale *lsm-dentry-hooks* =

```

fixes s0 :: 's
fixes hook-dentry-init-security :: 's  $\Rightarrow$  dentry  $\Rightarrow$  mode  $\Rightarrow$  string  $\Rightarrow$  string  $\Rightarrow$  int
 $\Rightarrow$  ('s, int) nondet-monad
fixes hook-dentry-create-files-as :: 's  $\Rightarrow$  dentry  $\Rightarrow$  mode  $\Rightarrow$  string  $\Rightarrow$  Cred  $\Rightarrow$  Cred
 $\Rightarrow$  ('s, int) nondet-monad
assumes stb-dentry-init-security :
   $\bigwedge sa. \llbracket \lambda s. s = sa \rrbracket$ 
    hook-dentry-init-security s dentry m name ctx ctxlen
     $\llbracket \lambda r s. s = sa \wedge (r = 0 \vee r \neq 0) \rrbracket$ 
assumes stb-dentry-create-files-as :
   $\bigwedge sa. \llbracket \lambda s. s = sa \rrbracket$ 
    hook-dentry-create-files-as s dentry m name old new
     $\llbracket \lambda r s. s = sa \wedge (r = 0 \vee r \neq 0) \rrbracket$ 

```

locale *lsm-inode-hooks* =

```

fixes s0 :: 's
fixes i-security :: 's  $\Rightarrow$  inode  $\Rightarrow$  'isec option
fixes hook-inode-alloc :: 's  $\Rightarrow$  inode  $\Rightarrow$  ('s, int) nondet-monad

```

```

fixes hook-inode-free :: 's ⇒ inode ⇒ ('s, unit) nondet-monad
fixes hook-inode-init-security :: 's ⇒ inode ⇒ inode ⇒ string ⇒ string ⇒ string
⇒ int ⇒ ('s, int) nondet-monad
fixes hook-old-inode-init-security :: 's ⇒ inode ⇒ inode ⇒ qstr ⇒ string ⇒
string ⇒ int ⇒ ('s, int) nondet-monad
fixes hook-inode-create :: 's ⇒ inode ⇒ dentry ⇒ mode ⇒ ('s, int) nondet-monad
fixes hook-inode-link :: 's ⇒ dentry ⇒ inode ⇒ dentry ⇒ ('s, int) nondet-monad
fixes hook-inode-unlink :: 's ⇒ inode ⇒ dentry ⇒ ('s, int) nondet-monad
fixes hook-inode-symlink :: 's ⇒ inode ⇒ dentry ⇒ string ⇒ ('s, int) nondet-monad
fixes hook-inode-mkdir :: 's ⇒ inode ⇒ dentry ⇒ mode ⇒ ('s, int) nondet-monad
fixes hook-inode-rmdir :: 's ⇒ inode ⇒ dentry ⇒ ('s, int) nondet-monad
fixes hook-inode-mknod :: 's ⇒ inode ⇒ dentry ⇒ mode ⇒ dev-t => ('s, int)
nondet-monad
fixes hook-inode-rename :: 's ⇒ inode ⇒ dentry ⇒ inode ⇒ dentry ⇒ ('s, int)
nondet-monad
fixes hook-inode-readlink :: 's ⇒ dentry ⇒ ('s, int) nondet-monad
fixes hook-inode-follow-link :: 's ⇒ dentry ⇒ inode ⇒ bool ⇒ ('s, int) nondet-monad
fixes hook-inode-permission :: 's ⇒ inode ⇒ mask ⇒ ('s, int) nondet-monad
fixes hook-inode-setattr :: 's ⇒ dentry ⇒ iattr ⇒ ('s, int) nondet-monad
fixes hook-inode-getattr :: 's ⇒ path ⇒ ('s, int) nondet-monad
fixes hook-inode-setxattr :: 's ⇒ dentry ⇒ xattr ⇒ string ⇒ int ⇒ flags ⇒ ('s,
int) nondet-monad
fixes hook-inode-post-setxattr :: 's ⇒ dentry ⇒ xattr ⇒ string ⇒ int ⇒ flags
⇒ ('s, unit) nondet-monad
fixes hook-inode-getxattr :: 's ⇒ dentry ⇒ xattr ⇒ ('s, int) nondet-monad
fixes hook-inode-listxattr :: 's ⇒ dentry ⇒ ('s, int) nondet-monad
fixes hook-inode-removexattr :: 's ⇒ dentry ⇒ xattr ⇒ ('s, int) nondet-monad
fixes hook-inode-need-killpriv :: 's ⇒ dentry ⇒ ('s, int) nondet-monad
fixes hook-inode-killpriv :: 's ⇒ dentry ⇒ ('s, int) nondet-monad
fixes hook-inode-getsecurity :: 's ⇒ inode ⇒ xattr ⇒ Void ⇒ bool ⇒ ('s, int)
nondet-monad
fixes hook-inode-setsecurity :: 's ⇒ inode ⇒ xattr ⇒ Void ⇒ nat ⇒ int ⇒ ('s,
int) nondet-monad
fixes hook-inode-listsecurity :: 's ⇒ inode ⇒ Void ⇒ int ⇒ ('s, int) nondet-monad
fixes hook-inode-getsecid :: 's ⇒ inode ⇒ u32 ⇒ ('s, unit) nondet-monad
fixes hook-inode-copy-up :: 's ⇒ dentry ⇒ Cred option ⇒ ('s, int) nondet-monad
fixes hook-inode-copy-up-xattr :: 's ⇒ xattr ⇒ ('s, int) nondet-monad
fixes hook-inode-invalidate-secctx :: 's ⇒ inode ⇒ ('s, unit) nondet-monad
fixes hook-inode-notifysecctx :: 's ⇒ inode ⇒ string ⇒ u32 ⇒ ('s, int) nondet-monad
fixes hook-inode-setsecctx :: 's ⇒ dentry ⇒ string ⇒ u32 ⇒ ('s, int) nondet-monad
fixes hook-inode-getsecctx :: 's ⇒ inode ⇒ string ⇒ u32 ⇒ ('s, int) nondet-monad
assumes stb-inode-alloc :
  ∧sa. {λs . s = sa} hook-inode-alloc s inode {λr s. s = sa ∧ (r = 0 ∨ r ≠
0)}
assumes stb-inode-free :
  ∧sa. {λs . s = sa} hook-inode-free s inode {λr s. r = unit}
assumes stb-inode-init-security :
  ∧sa. {λs . s = sa} hook-inode-init-security s inode dir qstr name value len'
    {λr s. s = sa ∧ (r = 0 ∨ r ≠ 0)}

```

assumes *stb-old-inode-init-security* :
 $\bigwedge sa. \{ \lambda s. s = sa \} \text{ hook-old-inode-init-security } s \text{ inode } dir \text{ qstr } name \text{ value } len'$
 $\{ \lambda r s. s = sa \wedge (r = 0 \vee r \neq 0) \}$
assumes *stb-inode-create* :
 $\bigwedge sa. \{ \lambda s. s = sa \} \text{ hook-inode-create } s \text{ dir } dentry \text{ m } \{ \lambda r s. s = sa \wedge (r = 0 \vee r \neq 0) \}$
assumes *stb-inode-link* :
 $\bigwedge sa. \{ \lambda s. s = sa \} \text{ hook-inode-link } s \text{ old-dentry } dir \text{ new-dentry } \{ \lambda r s. s = sa \wedge (r = 0 \vee r \neq 0) \}$
assumes *stb-inode-unlink* :
 $\bigwedge sa. \{ \lambda s. s = sa \} \text{ hook-inode-unlink } s \text{ dir } dentry \{ \lambda r s. s = sa \wedge (r = 0 \vee r \neq 0) \}$
assumes *stb-inode-symlink* :
 $\bigwedge sa. \{ \lambda s. s = sa \} \text{ hook-inode-symlink } s \text{ dir } dentry \text{ old-name } \{ \lambda r s. s = sa \wedge (r = 0 \vee r \neq 0) \}$
assumes *stb-inode-mkdir* :
 $\bigwedge sa. \{ \lambda s. s = sa \} \text{ hook-inode-mkdir } s \text{ dir } dentry \text{ m } \{ \lambda r s. s = sa \wedge (r = 0 \vee r \neq 0) \}$
assumes *stb-inode-rmdir* :
 $\bigwedge sa. \{ \lambda s. s = sa \} \text{ hook-inode-rmdir } s \text{ dir } dentry \{ \lambda r s. s = sa \wedge (r = 0 \vee r \neq 0) \}$
assumes *stb-inode-mknod* :
 $\bigwedge sa. \{ \lambda s. s = sa \} \text{ hook-inode-mknod } s \text{ dir } dentry \text{ m } dev \{ \lambda r s. s = sa \wedge (r = 0 \vee r \neq 0) \}$
assumes *stb-inode-rename* :
 $\bigwedge sa. \{ \lambda s. s = sa \} \text{ hook-inode-rename } s \text{ new-dir } new-dentry \text{ old-dir } old-dentry$
 $\{ \lambda r s. s = sa \wedge (r = 0 \vee r \neq 0) \}$
assumes *stb-inode-readlink* :
 $\bigwedge sa. \{ \lambda s. s = sa \} \text{ hook-inode-readlink } s \text{ dentry } \{ \lambda r s. s = sa \wedge (r = 0 \vee r \neq 0) \}$
assumes *stb-inode-follow-link* :
 $\bigwedge sa. \{ \lambda s. s = sa \} \text{ hook-inode-follow-link } s \text{ dentry } inode \text{ rcu}'$
 $\{ \lambda r s. s = sa \wedge (r = 0 \vee r \neq 0) \}$
assumes *stb-inode-permission* :
 $\bigwedge sa. \{ \lambda s. s = sa \} \text{ hook-inode-permission } s \text{ inode } m \{ \lambda r s. s = sa \wedge (r = 0 \vee r \neq 0) \}$
assumes *stb-inode-setattr* :
 $\bigwedge sa. \{ \lambda s. s = sa \} \text{ hook-inode-setattr } s \text{ dentry } attr' \{ \lambda r s. s = sa \wedge (r = 0 \vee r \neq 0) \}$
assumes *stb-inode-getattr* :
 $\bigwedge sa. \{ \lambda s. s = sa \} \text{ hook-inode-getattr } s \text{ path } \{ \lambda r s. s = sa \wedge (r = 0 \vee r \neq 0) \}$
assumes *stb-inode-setxattr* :
 $\bigwedge sa. \{ \lambda s. s = sa \} \text{ hook-inode-setxattr } s \text{ dentry } name' \text{ value } size' \text{ flgs}$
 $\{ \lambda r s. s = sa \wedge (r = 0 \vee r \neq 0) \}$
assumes *stb-inode-post-setxattr* :
 $\bigwedge sa. \{ \lambda s. s = sa \} \text{ hook-inode-post-setxattr } s \text{ dentry } name' \text{ value } size' \text{ flgs}$

$\{\lambda r s. r = \text{unit}\}$
assumes *stb-inode-getxattr* :
 $\bigwedge sa. \{\lambda s. s = sa \} \text{ hook-inode-getxattr } s \text{ dentry name' } \{\lambda r s. s = sa \wedge (r = 0 \vee r \neq 0)\}$
assumes *stb-inode-listxattr* :
 $\bigwedge sa. \{\lambda s. s = sa \} \text{ hook-inode-listxattr } s \text{ dentry } \{\lambda r s. s = sa \wedge (r = 0 \vee r \neq 0)\}$
assumes *stb-inode-removexattr* :
 $\bigwedge sa. \{\lambda s. s = sa \} \text{ hook-inode-removexattr } s \text{ dentry name' } \{\lambda r s. s = sa \wedge (r = 0 \vee r \neq 0)\}$
assumes *stb-inode-need-killpriv* :
 $\bigwedge sa. \{\lambda s. s = sa \} \text{ hook-inode-need-killpriv } s \text{ dentry } \{\lambda r s. s = sa \wedge (r = 0 \vee r \neq 0)\}$
assumes *stb-inode-killpriv* :
 $\bigwedge sa. \{\lambda s. s = sa \} \text{ hook-inode-killpriv } s \text{ dentry } \{\lambda r s. s = sa \wedge (r = 0 \vee r \neq 0)\}$
assumes *stb-inode-getsecurity* :
 $\bigwedge sa. \{\lambda s. s = sa \} \text{ hook-inode-getsecurity } s \text{ inode name' buffer alloc } \{\lambda r s. s = sa \wedge (r = 0 \vee r \neq 0)\}$
assumes *stb-inode-setsecurity* :
 $\bigwedge sa. \{\lambda s. s = sa \} \text{ hook-inode-setsecurity } s \text{ inode name' va size' flgs } \{\lambda r s. s = sa \wedge (r = 0 \vee r \neq 0)\}$
assumes *stb-inode-listsecurity* :
 $\bigwedge sa. \{\lambda s. s = sa \} \text{ hook-inode-listsecurity } s \text{ inode buffer bsize } \{\lambda r s. s = sa \wedge (r = 0 \vee r \neq 0)\}$
assumes *stb-inode-getsecid* : $\bigwedge sa. \{\lambda s. s = sa \} \text{ hook-inode-getsecid } s \text{ inode secid' } \{\lambda r s. r = \text{unit}\}$
assumes *stb-inode-copy-up* :
 $\bigwedge sa. \{\lambda s. s = sa \} \text{ hook-inode-copy-up } s \text{ src new } \{\lambda r s. s = sa \wedge (r = 0 \vee r \neq 0)\}$
assumes *stb-inode-copy-up-xattr* :
 $\bigwedge sa. \{\lambda s. s = sa \} \text{ hook-inode-copy-up-xattr } s \text{ name' } \{\lambda r s. s = sa \wedge (r = 0 \vee r \neq 0)\}$
assumes *stb-inode-invalidate-secctx* :
 $\bigwedge sa. \{\lambda s. s = sa \} \text{ hook-inode-invalidate-secctx } s \text{ inode } \{\lambda r s. r = \text{unit}\}$
assumes *stb-inode-notifysecctx* :
 $\bigwedge sa. \{\lambda s. s = sa \} \text{ hook-inode-notifysecctx } s \text{ inode ctx ctxlen } \{\lambda r s. s = sa \wedge (r = 0 \vee r \neq 0)\}$
assumes *stb-inode-setsecctx* :
 $\bigwedge sa. \{\lambda s. s = sa \} \text{ hook-inode-setsecctx } s \text{ dentry ctx ctxlen } \{\lambda r s. s = sa \wedge (r = 0 \vee r \neq 0)\}$
assumes *stb-inode-getsecctx* :
 $\bigwedge sa. \{\lambda s. s = sa \} \text{ hook-inode-getsecctx } s \text{ inode ctx ctxlen } \{\lambda r s. s = sa \wedge (r = 0 \vee r \neq 0)\}$

locale *lsm-kernel-hooks* =

fixes *s0* :: 's

fixes *hook-kernel-act-as* :: 's \Rightarrow Cred \Rightarrow u32 \Rightarrow ('s, int) nondet-monad

```

fixes hook-kernel-create-files-as :: 's ⇒ Cred ⇒ inode ⇒ ('s, int) nondet-monad
fixes hook-kernel-module-request :: 's ⇒ string ⇒ ('s, int) nondet-monad
fixes hook-kernel-load-data :: 's ⇒ kernel-load-data-id ⇒ ('s, int) nondet-monad
fixes hook-kernel-read-file :: 's ⇒ Files ⇒ kernel-read-file-id ⇒ ('s, int) nondet-monad
fixes hook-kernel-post-read-file :: 's ⇒ Files ⇒ string ⇒ nat ⇒ kernel-read-file-id
                                     ⇒ ('s, int) nondet-monad

assumes stb-kernel-act-as :
  ∧sa. {λs . s = sa} hook-kernel-act-as s new secid' {λr s. s = sa ∧ (r = 0 ∨
r ≠ 0)}
assumes stb-kernel-create-files-as :
  ∧sa. {λs . s = sa} hook-kernel-create-files-as s c inode {λr s. s = sa ∧ (r =
0 ∨ r ≠ 0)}
assumes stb-kernel-module-request :
  ∧sa. {λs . s = sa} hook-kernel-module-request s name {λr s. s = sa ∧ (r =
0 ∨ r ≠ 0)}
assumes stb-kernel-load-data :
  ∧sa. {λs . s = sa} hook-kernel-load-data s ldataid {λr s. s = sa ∧ (r = 0 ∨
r ≠ 0)}
assumes stb-kernel-read-file:
  ∧sa. {λs . s = sa} hook-kernel-read-file s f rfid {λr s. s = sa ∧ (r = 0 ∨ r
≠ 0)}
assumes stb-hook-kernel-post-read-file :
  ∧sa. {λs . s = sa}
    hook-kernel-post-read-file s file buf size' kid {λr s. s = sa ∧ (r = 0 ∨ r
≠ 0)}

```

```

locale lsm-ipc-hooks =
  fixes s0 :: 's
  fixes ipc-security :: 's ⇒ kern-ipc-perm ⇒ 'ipcsec option
  fixes msg-security :: 's ⇒ msg-msg ⇒ 'msgsec option
  fixes hook-ipc-permission :: 's ⇒ kern-ipc-perm ⇒ int ⇒ ('s, int) nondet-monad
  fixes hook-ipc-getsecid :: 's ⇒ kern-ipc-perm ⇒ u32 ⇒ ('s, unit) nondet-monad
  fixes hook-msg-msg-alloc :: 's ⇒ msg-msg ⇒ ('s, int) nondet-monad
  fixes hook-msg-msg-free :: 's ⇒ msg-msg ⇒ ('s, unit) nondet-monad
  fixes hook-msg-queue-alloc :: 's ⇒ kern-ipc-perm ⇒ ('s, int) nondet-monad
  fixes hook-msg-queue-free :: 's ⇒ kern-ipc-perm ⇒ ('s, unit) nondet-monad
  fixes hook-msg-queue-associate :: 's ⇒ kern-ipc-perm ⇒ int ⇒ ('s, int) nondet-monad
  fixes hook-msg-queue-msgctl :: 's ⇒ kern-ipc-perm ⇒ IPC-CMD ⇒ ('s, int)
nondet-monad
  fixes hook-msg-queue-msgsnd :: 's ⇒ kern-ipc-perm ⇒ msg-msg ⇒ int ⇒ ('s,
int) nondet-monad
  fixes hook-msg-queue-msgrcv :: 's ⇒ kern-ipc-perm ⇒ msg-msg ⇒ Task ⇒ int
⇒ int
                                     ⇒ ('s, int) nondet-monad
  fixes hook-shm-alloc :: 's ⇒ kern-ipc-perm ⇒ ('s, int) nondet-monad

```

fixes *hook-shm-free* :: 's \Rightarrow kern-ipc-perm \Rightarrow ('s, unit) nondet-monad
fixes *hook-shm-associate* :: 's \Rightarrow kern-ipc-perm \Rightarrow int \Rightarrow ('s, int) nondet-monad
fixes *hook-shm-shmctl* :: 's \Rightarrow kern-ipc-perm \Rightarrow IPC-CMD \Rightarrow ('s, int) nondet-monad
fixes *hook-shm-shmat* :: 's \Rightarrow kern-ipc-perm \Rightarrow string \Rightarrow int \Rightarrow ('s, int) nondet-monad
fixes *hook-sem-alloc* :: 's \Rightarrow kern-ipc-perm \Rightarrow ('s, int) nondet-monad
fixes *hook-sem-free* :: 's \Rightarrow kern-ipc-perm \Rightarrow ('s, unit) nondet-monad
fixes *hook-sem-associate* :: 's \Rightarrow kern-ipc-perm \Rightarrow int \Rightarrow ('s, int) nondet-monad
fixes *hook-sem-semctl* :: 's \Rightarrow kern-ipc-perm \Rightarrow IPC-CMD \Rightarrow ('s, int) nondet-monad
fixes *hook-sem-semop* :: 's \Rightarrow kern-ipc-perm \Rightarrow sembuf \Rightarrow nat \Rightarrow int \Rightarrow ('s, int) nondet-monad

assumes *stb-ipc-permission* :

$\bigwedge sa. \{ \lambda s. s = sa \} \text{hook-ipc-permission } s \text{ ipcp flg } \{ \lambda r s. s = sa \wedge (r = 0 \vee r \neq 0) \}$

assumes *stb-ipc-getsecid* :

$\bigwedge sa. \{ \lambda s. s = sa \} \text{hook-ipc-getsecid } s \text{ ipcp secid' } \{ \lambda r s. r = \text{unit} \}$

assumes *stb-msg-msg-alloc* :

$\bigwedge sa. \{ \lambda s. s = sa \} \text{hook-msg-msg-alloc } s \text{ msg } \{ \lambda r s. r = 0 \vee r \neq 0 \}$

assumes *stb-msg-msg-free* :

$\bigwedge sa. \{ \lambda s. s = sa \} \text{hook-msg-msg-free } s \text{ msg } \{ \lambda r s. r = \text{unit} \}$

assumes *stb-msg-queue-alloc*:

$\bigwedge sa. \{ \lambda s. s = sa \} \text{hook-msg-queue-alloc } s \text{ msg } \{ \lambda r s. s = sa \wedge (r = 0 \vee r \neq 0) \}$

assumes *stb-msg-queue-free* :

$\bigwedge sa. \{ \lambda s. s = sa \} \text{hook-msg-queue-free } s \text{ msg } \{ \lambda r s. r = \text{unit} \}$

assumes *stb-msg-queue-associate* :

$\bigwedge sa. \{ \lambda s. s = sa \} \text{hook-msg-queue-associate } s \text{ msg msgflg } \{ \lambda r s. s = sa \wedge (r = 0 \vee r \neq 0) \}$

assumes *stb-msg-queue-msgctl*:

$\bigwedge sa. \{ \lambda s. s = sa \} \text{hook-msg-queue-msgctl } s \text{ msg cmd } \{ \lambda r s. s = sa \wedge (r = 0 \vee r \neq 0) \}$

assumes *stb-msg-queue-msgsnd* :

$\bigwedge sa. \{ \lambda s. s = sa \} \text{hook-msg-queue-msgsnd } s \text{ msg msg msgflg } \{ \lambda r s. s = sa \wedge (r = 0 \vee r \neq 0) \}$

assumes *stb-msg-queue-msgrcv*:

$\bigwedge sa. \{ \lambda s. s = sa \} \text{hook-msg-queue-msgrcv } s \text{ msg msg target type m } \{ \lambda r s. s = sa \wedge (r = 0 \vee r \neq 0) \}$

assumes *stb-shm-alloc*:

$\bigwedge sa. \{ \lambda s. s = sa \} \text{hook-shm-alloc } s \text{ shp } \{ \lambda r s. r = 0 \vee r \neq 0 \}$

assumes *stb-shm-free* :

$\bigwedge sa. \{ \lambda s. s = sa \} \text{hook-shm-free } s \text{ shp } \{ \lambda r s. r = \text{unit} \}$

assumes *stb-shm-associate* :

$\bigwedge sa. \{ \lambda s. s = sa \} \text{hook-shm-associate } s \text{ shp shmflg } \{ \lambda r s. s = sa \wedge (r = 0 \vee r \neq 0) \}$

assumes *stb-shm-shmctl*:

$\bigwedge sa. \{ \lambda s. s = sa \} \text{hook-shm-shmctl } s \text{ shp cmd } \{ \lambda r s. s = sa \wedge (r = 0 \vee r \neq 0) \}$

assumes *stb-shm-shmat*:

$\bigwedge sa. \{ \lambda s. s = sa \} \text{hook-shm-shmat } s \text{ shp shmaddr shmflg } \{ \lambda r s. s = sa \wedge (r = 0 \vee r \neq 0) \}$

```

= 0 ∨ r ≠ 0)⟩
assumes stb-sem-alloc:
  ∧sa. {λs . s = sa} hook-sem-alloc s sma {λr s. r = 0 ∨ r ≠ 0}
assumes stb-sem-free :
  ∧sa. {λs . s = sa} hook-sem-free s sma {λr s. r = unit}
assumes stb-sem-associate :
  ∧sa. {λs . s = sa} hook-sem-associate s sma semflg {λr s. s = sa ∧ (r = 0
  ∨ r ≠ 0)}
assumes stb-sem-shmctl:
  ∧sa. {λs . s = sa} hook-sem-semctl s sma cmd {λr s. s = sa ∧ (r = 0 ∨ r
  ≠ 0)}
assumes stb-sem-shmat:
  ∧sa. {λs . s = sa} hook-sem-semop s sma sops nsops alter {λr s. s = sa ∧ (r
  = 0 ∨ r ≠ 0)}

```

```

locale lsm-other-hooks =
  fixes s0 :: 's
  fixes hook-d-instantiate:: 's ⇒ dentry ⇒ inode option ⇒ ('s, unit) nondet-monad
  fixes hook-getprocattr :: 's ⇒ Task ⇒ string ⇒ string ⇒ ('s, int) nondet-monad
  fixes hook-setprocattr :: 's ⇒ string ⇒ string ⇒ int ⇒ ('s, int) nondet-monad
  fixes hook-netlink-send :: 's ⇒ sock ⇒ sk-buff ⇒ ('s, int) nondet-monad
  fixes hook-ismaclabel :: 's ⇒ xattr ⇒ ('s, int) nondet-monad
  fixes hook-secid-to-secctx :: 's ⇒ u32 ⇒ string ⇒ u32 ⇒ ('s, int) nondet-monad
  fixes hook-secctx-to-secid :: 's ⇒ string ⇒ u32 ⇒ u32 ⇒ ('s, int) nondet-monad
  fixes hook-release-secctx :: 's ⇒ string ⇒ u32 ⇒ ('s, unit) nondet-monad
  assumes stb-d-instantiate :
    ∧sa. {λs . s = sa} hook-d-instantiate sa dentry inode {λr s. r = unit}
  assumes stb-getprocattr :
    ∧sa. {λs . s = sa} hook-getprocattr sa p name value {λr s. s = sa ∧ (r = 0
    ∨ r ≠ 0)}
  assumes stb-setprocattr :
    ∧sa. {λs . s = sa} hook-setprocattr sa name value size' {λr s. s = sa ∧ (r =
    0 ∨ r ≠ 0)}
  assumes stb-netlink-send :
    ∧sa. {λs . s = sa} hook-netlink-send s sk' skb {λr s. s = sa ∧ (r = 0 ∨ r
    ≠ 0)}
  assumes stb-ismaclabel :
    ∧sa. {λs. s = sa} hook-ismaclabel s name' {λr s. s = sa ∧ (r = 0 ∨ r ≠ 0)}
  assumes stb-secid-to-secctx:
    ∧sa. {λs. s = sa} hook-secid-to-secctx s secid' secdata seclen {λr s. s = sa
    ∧ (r = 0 ∨ r ≠ 0)}
  assumes stb-secctx-to-secid :
    ∧sa. {λs. s = sa} hook-secctx-to-secid s secdata seclen secid' {λr s. s = sa
    ∧ (r = 0 ∨ r ≠ 0)}
  assumes stb-release-secctx:
    ∧sa. {λs. s = sa} hook-release-secctx s secdata seclen {λr s. r = unit}

```

locale *lsm-network-hooks* =

```

fixes s0 :: 's
fixes sk-security :: 's  $\Rightarrow$  sock  $\Rightarrow$  'ssec option
fixes hook-unix-stream-connect :: 's  $\Rightarrow$  sock  $\Rightarrow$  sock  $\Rightarrow$  sock  $\Rightarrow$  ('s, int)
nondet-monad
fixes hook-unix-may-send :: 's  $\Rightarrow$  socket  $\Rightarrow$  socket  $\Rightarrow$  ('s, int) nondet-monad
fixes hook-socket-create :: 's  $\Rightarrow$  Sk-Family  $\Rightarrow$  int  $\Rightarrow$  int  $\Rightarrow$  int  $\Rightarrow$  ('s, int)
nondet-monad
fixes hook-socket-post-create :: 's  $\Rightarrow$  socket  $\Rightarrow$  Sk-Family  $\Rightarrow$  int  $\Rightarrow$  int  $\Rightarrow$  int
 $\Rightarrow$  ('s, int) nondet-monad
fixes hook-socket-socketpair :: 's  $\Rightarrow$  socket  $\Rightarrow$  socket  $\Rightarrow$  ('s, int) nondet-monad
fixes hook-socket-bind :: 's  $\Rightarrow$  socket  $\Rightarrow$  sockaddr  $\Rightarrow$  int  $\Rightarrow$  ('s, int) nondet-monad
fixes hook-socket-connect :: 's  $\Rightarrow$  socket  $\Rightarrow$  sockaddr  $\Rightarrow$  int  $\Rightarrow$  ('s, int) nondet-monad
fixes hook-socket-listen :: 's  $\Rightarrow$  socket  $\Rightarrow$  int  $\Rightarrow$  ('s, int) nondet-monad
fixes hook-socket-accept :: 's  $\Rightarrow$  socket  $\Rightarrow$  socket  $\Rightarrow$  ('s, int) nondet-monad
fixes hook-socket-sendmsg :: 's  $\Rightarrow$  socket  $\Rightarrow$  msghdr  $\Rightarrow$  int  $\Rightarrow$  ('s, int) nondet-monad
fixes hook-socket-recvmsg :: 's  $\Rightarrow$  socket  $\Rightarrow$  msghdr  $\Rightarrow$  int  $\Rightarrow$  int  $\Rightarrow$  ('s, int)
nondet-monad
fixes hook-socket-getsockname :: 's  $\Rightarrow$  socket  $\Rightarrow$  ('s, int) nondet-monad
fixes hook-socket-getpeername :: 's  $\Rightarrow$  socket  $\Rightarrow$  ('s, int) nondet-monad
fixes hook-socket-getsockopt :: 's  $\Rightarrow$  socket  $\Rightarrow$  int  $\Rightarrow$  int  $\Rightarrow$  ('s, int) nondet-monad
fixes hook-socket-setsockopt :: 's  $\Rightarrow$  socket  $\Rightarrow$  int  $\Rightarrow$  int  $\Rightarrow$  ('s, int) nondet-monad
fixes hook-socket-shutdown :: 's  $\Rightarrow$  socket  $\Rightarrow$  int  $\Rightarrow$  ('s, int) nondet-monad
fixes hook-sock-rcv-skb :: 's  $\Rightarrow$  sock  $\Rightarrow$  sk-buff  $\Rightarrow$  ('s, int) nondet-monad
fixes hook-socket-getpeersec-stream :: 's  $\Rightarrow$  socket  $\Rightarrow$  string  $\Rightarrow$  int  $\Rightarrow$  nat  $\Rightarrow$  ('s,
int) nondet-monad
fixes hook-socket-getpeersec-dgram :: 's  $\Rightarrow$  socket  $\Rightarrow$  sk-buff option  $\Rightarrow$  u32  $\Rightarrow$  ('s,
int) nondet-monad
fixes hook-sk-alloc :: 's  $\Rightarrow$  sock  $\Rightarrow$  int  $\Rightarrow$  gfp-t  $\Rightarrow$  ('s, int) nondet-monad
fixes hook-sk-free :: 's  $\Rightarrow$  sock  $\Rightarrow$  ('s, unit) nondet-monad
fixes hook-sk-clone :: 's  $\Rightarrow$  sock  $\Rightarrow$  sock  $\Rightarrow$  ('s, unit) nondet-monad
fixes hook-sk-classify-flow :: 's  $\Rightarrow$  sock  $\Rightarrow$  flowi  $\Rightarrow$  ('s, unit) nondet-monad
fixes hook-req-classify-flow :: 's  $\Rightarrow$  request-sock  $\Rightarrow$  flowi  $\Rightarrow$  ('s, unit) nondet-monad
fixes hook-sock-graft :: 's  $\Rightarrow$  sock  $\Rightarrow$  socket  $\Rightarrow$  ('s, unit) nondet-monad
fixes hook-inet-conn-request :: 's  $\Rightarrow$  sock  $\Rightarrow$  sk-buff  $\Rightarrow$  request-sock  $\Rightarrow$  ('s, int)
nondet-monad
fixes hook-inet-csk-clone :: 's  $\Rightarrow$  sock  $\Rightarrow$  request-sock  $\Rightarrow$  ('s, unit) nondet-monad
fixes hook-inet-conn-established :: 's  $\Rightarrow$  sock  $\Rightarrow$  sk-buff  $\Rightarrow$  ('s, unit) nondet-monad
fixes hook-secmark-relabel-packet :: 's  $\Rightarrow$  u32  $\Rightarrow$  ('s, int) nondet-monad
fixes hook-secmark-refcount-inc :: 's  $\Rightarrow$  ('s, unit) nondet-monad
fixes hook-secmark-refcount-dec :: 's  $\Rightarrow$  ('s, unit) nondet-monad

fixes hook-tun-dev-alloc-security :: 's  $\Rightarrow$  'security  $\Rightarrow$  ('s, int) nondet-monad
fixes hook-tun-dev-free-security :: 's  $\Rightarrow$  'security  $\Rightarrow$  ('s, unit) nondet-monad
fixes hook-tun-dev-create :: 's  $\Rightarrow$  ('s, int) nondet-monad
fixes hook-tun-dev-attach-queue :: 's  $\Rightarrow$  'security  $\Rightarrow$  ('s, int) nondet-monad
fixes hook-tun-dev-attach :: 's  $\Rightarrow$  sock  $\Rightarrow$  'security  $\Rightarrow$  ('s, int) nondet-monad
fixes hook-tun-dev-open :: 's  $\Rightarrow$  'security  $\Rightarrow$  ('s, int) nondet-monad

```


fixes *hook-sctp-assoc-request* :: 's \Rightarrow sctp-endpoint \Rightarrow sk-buff \Rightarrow ('s, int) nondet-monad
fixes *hook-sctp-bind-connect* :: 's \Rightarrow sock \Rightarrow int \Rightarrow sockaddr \Rightarrow int \Rightarrow ('s, int)
nondet-monad
fixes *hook-sctp-sk-clone* :: 's \Rightarrow sctp-endpoint \Rightarrow sock \Rightarrow sock \Rightarrow ('s, unit)
nondet-monad

assumes *stb-unix-stream-connect* :
 $\bigwedge sa. \{ \lambda s. s = sa \}$
hook-unix-stream-connect s sock other newsk
 $\{ \lambda r s. s = sa \wedge (r = 0 \vee r \neq 0) \}$
assumes *security-unix-may-send* :
 $\bigwedge sa. \{ \lambda s. s = sa \}$ *hook-unix-may-send* s sock' other' $\{ \lambda r s. s = sa \wedge (r = 0 \vee r \neq 0) \}$
assumes *security-socket-create* :
 $\bigwedge sa. \{ \lambda s. s = sa \}$ *hook-socket-create* s family type pro kern $\{ \lambda r s. s = sa \wedge (r = 0 \vee r \neq 0) \}$
assumes *security-socket-post-create* :
 $\bigwedge sa. \{ \lambda s. s = sa \}$ *hook-socket-post-create* s sock' family type pro kern
 $\{ \lambda r s. s = sa \wedge (r = 0 \vee r \neq 0) \}$
assumes *security-socket-socketpair* :
 $\bigwedge sa. \{ \lambda s. s = sa \}$ *hook-socket-socketpair* s socka sockb $\{ \lambda r s. s = sa \wedge (r = 0 \vee r \neq 0) \}$
assumes *security-socket-bind* :
 $\bigwedge sa. \{ \lambda s. s = sa \}$ *hook-socket-bind* s sock' address addrlen $\{ \lambda r s. s = sa \wedge (r = 0 \vee r \neq 0) \}$
assumes *security-socket-connect* :
 $\bigwedge sa. \{ \lambda s. s = sa \}$ *hook-socket-connect* s sock' address addrlen
 $\{ \lambda r s. s = sa \wedge (r = 0 \vee r \neq 0) \}$
assumes *security-socket-listen* :
 $\bigwedge sa. \{ \lambda s. s = sa \}$ *hook-socket-listen* s sock' backlog $\{ \lambda r s. s = sa \wedge (r = 0 \vee r \neq 0) \}$
assumes *security-socket-accept* :
 $\bigwedge sa. \{ \lambda s. s = sa \}$ *hook-socket-accept* s sock' newsock $\{ \lambda r s. s = sa \wedge (r = 0 \vee r \neq 0) \}$
assumes *security-socket-sendmsg* :
 $\bigwedge sa. \{ \lambda s. s = sa \}$ *hook-socket-sendmsg* s sock' msg size' $\{ \lambda r s. s = sa \wedge (r = 0 \vee r \neq 0) \}$
assumes *security-socket-recvmsg* :
 $\bigwedge sa. \{ \lambda s. s = sa \}$ *hook-socket-recvmsg* s sock' msg size' flags $\{ \lambda r s. s = sa \wedge (r = 0 \vee r \neq 0) \}$
assumes *security-socket-getsockname* :
 $\bigwedge sa. \{ \lambda s. s = sa \}$ *hook-socket-getsockname* s sock' $\{ \lambda r s. s = sa \wedge (r = 0 \vee r \neq 0) \}$
assumes *security-socket-getpeername* :
 $\bigwedge sa. \{ \lambda s. s = sa \}$ *hook-socket-getpeername* s sock' $\{ \lambda r s. s = sa \wedge (r = 0 \vee r \neq 0) \}$
assumes *security-socket-getsockopt* :
 $\bigwedge sa. \{ \lambda s. s = sa \}$
hook-socket-getsockopt s sock' level' optname

$\{\lambda r s. s = sa \wedge (r = 0 \vee r \neq 0)\}$
assumes *security-socket-setsockopt* :
 $\bigwedge sa. \{\lambda s. s = sa \} \text{hook-socket-setsockopt } s \text{ sock' level' optname}$
 $\{\lambda r s. s = sa \wedge (r = 0 \vee r \neq 0)\}$
assumes *security-socket-shutdown*:
 $\bigwedge sa. \{\lambda s. s = sa \} \text{hook-socket-shutdown } s \text{ sock' how } \{\lambda r s. s = sa \wedge (r = 0 \vee r \neq 0)\}$
assumes *security-sock-rcv-skb* :
 $\bigwedge sa. \{\lambda s. s = sa \} \text{hook-sock-rcv-skb } s \text{ sock skb } \{\lambda r s. s = sa \wedge (r = 0 \vee r \neq 0)\}$
assumes *security-socket-getpeersec-stream* :
 $\bigwedge sa. \{\lambda s. s = sa \} \text{hook-socket-getpeersec-stream } s \text{ sock' optval optlen len'}$
 $\{\lambda r s. s = sa \wedge (r = 0 \vee r \neq 0)\}$
assumes *security-socket-getpeersec-dgram* :
 $\bigwedge sa. \{\lambda s. s = sa \}$
 $\text{hook-socket-getpeersec-dgram } s \text{ sock' skb' secid'}$
 $\{\lambda r s. s = sa \wedge (r = 0 \vee r \neq 0)\}$
assumes *security-sk-alloc* :
 $\bigwedge sa. \{\lambda s. s = sa \} \text{hook-sk-alloc } s \text{ sk' family' priority } \{\lambda r s. s = sa \wedge (r = 0 \vee r \neq 0)\}$
assumes *security-sk-free* :
 $\bigwedge sa. \{\lambda s. s = sa \} \text{hook-sk-free } s \text{ sock } \{\lambda r s. r = \text{unit}\}$
assumes *security-sk-clone* :
 $\bigwedge sa. \{\lambda s. s = sa \} \text{hook-sk-clone } s \text{ sk' newsk } \{\lambda r s. r = \text{unit}\}$
assumes *security-sk-classify-flow* :
 $\bigwedge sa. \{\lambda s. s = sa \} \text{hook-sk-classify-flow } s \text{ sock fl } \{\lambda r s. r = \text{unit}\}$
assumes *security-req-classify-flow* :
 $\bigwedge sa. \{\lambda s. s = sa \} \text{hook-req-classify-flow } s \text{ req fl } \{\lambda r s. r = \text{unit}\}$
assumes *security-sock-graft* :
 $\bigwedge sa. \{\lambda s. s = sa \} \text{hook-sock-graft } s \text{ sk' parent' } \{\lambda r s. r = \text{unit}\}$
assumes *security-inet-conn-request* :
 $\bigwedge sa. \{\lambda s. s = sa \} \text{hook-inet-conn-request } s \text{ sk' skb req } \{\lambda r s. s = sa \wedge (r = 0 \vee r \neq 0)\}$
assumes *security-inet-csk-clone* :
 $\bigwedge sa. \{\lambda s. s = sa \} \text{hook-inet-csk-clone } s \text{ newsk req } \{\lambda r s. r = \text{unit}\}$
assumes *security-inet-conn-established* :
 $\bigwedge sa. \{\lambda s. s = sa \} \text{hook-inet-conn-established } s \text{ sk' skb } \{\lambda r s. r = \text{unit}\}$
assumes *security-secmark-relabel-packet* :
 $\bigwedge sa. \{\lambda s. s = sa \} \text{hook-secmark-relabel-packet } s \text{ secid' } \{\lambda r s. s = sa \wedge (r = 0 \vee r \neq 0)\}$
assumes *security-secmark-refcount-inc* :
 $\bigwedge sa. \{\lambda s. s = sa \} \text{hook-secmark-refcount-inc } s \{\lambda r s. r = \text{unit}\}$
assumes *security-secmark-refcount-dec* :
 $\bigwedge sa. \{\lambda s. s = sa \} \text{hook-secmark-refcount-dec } s \{\lambda r s. r = \text{unit}\}$
assumes *security-tun-dev-alloc-security* :
 $\bigwedge sa. \{\lambda s. s = sa \} \text{hook-tun-dev-alloc-security } s \text{ security } \{\lambda r s. s = sa \wedge (r = 0 \vee r \neq 0)\}$
assumes *security-tun-dev-free-security* :
 $\bigwedge sa. \{\lambda s. s = sa \} \text{hook-tun-dev-free-security } s \text{ security } \{\lambda r s. r = \text{unit}\}$

assumes *security-tun-dev-create* :
 $\bigwedge sa. \{\lambda s . s = sa\} \text{hook-tun-dev-create } s \{\lambda r s. s = sa \wedge (r = 0 \vee r \neq 0)\}$
assumes *security-tun-dev-attach-queue* :
 $\bigwedge sa. \{\lambda s . s = sa\} \text{hook-tun-dev-attach-queue } s \text{security} \{\lambda r s. s = sa \wedge (r = 0 \vee r \neq 0)\}$
assumes *security-tun-dev-attach* :
 $\bigwedge sa. \{\lambda s . s = sa\} \text{hook-tun-dev-attach } s \text{sk}' \text{security} \{\lambda r s. s = sa \wedge (r = 0 \vee r \neq 0)\}$
assumes *security-tun-dev-open* :
 $\bigwedge sa. \{\lambda s . s = sa\} \text{hook-tun-dev-open } s \text{security} \{\lambda r s. s = sa \wedge (r = 0 \vee r \neq 0)\}$
assumes *security-sctp-assoc-request* :
 $\bigwedge sa. \{\lambda s . s = sa\} \text{hook-sctp-assoc-request } s \text{ep skb} \{\lambda r s. s = sa \wedge (r = 0 \vee r \neq 0)\}$
assumes *security-sctp-bind-connect* :
 $\bigwedge sa. \{\lambda s . s = sa\} \text{hook-sctp-bind-connect } s \text{sk}' \text{optname address addrlen}$
 $\{\lambda r s. s = sa \wedge (r = 0 \vee r \neq 0)\}$
assumes *security-sctp-sk-clone* :
 $\bigwedge sa. \{\lambda s . s = sa\} \text{hook-sctp-sk-clone } s \text{ep sk}' \text{newsk} \{\lambda r s. r = \text{unit}\}$

locale *lsm-infiniband-hooks* =

fixes *s0* :: 's
fixes *hook-ib-pkey-access* :: 's \Rightarrow 'v \Rightarrow nat \Rightarrow nat \Rightarrow ('s, int) nondet-monad
fixes *hook-ib-endport-manage-subnet* :: 's \Rightarrow 'v \Rightarrow string \Rightarrow nat \Rightarrow ('s, int) nondet-monad
fixes *hook-ib-alloc-security* :: 's \Rightarrow 'v list \Rightarrow ('s, int) nondet-monad
fixes *hook-ib-free-security* :: 's \Rightarrow 'v list \Rightarrow ('s, unit) nondet-monad
assumes *stb-ib-pkey-access* :
 $\bigwedge sa. \{\lambda s . s = sa\} \text{hook-ib-pkey-access } sa \text{sec prefix}' \text{pkey} \{\lambda r s. s = sa \wedge (r = 0 \vee r \neq 0)\}$
assumes *stb-ib-endport-manage-subnet* :
 $\bigwedge sa. \{\lambda s . s = sa\} \text{hook-ib-endport-manage-subnet } sa \text{sec dev-name prot-num}$
 $\{\lambda r s. s = sa \wedge (r = 0 \vee r \neq 0)\}$
assumes *stb-ib-alloc-security* :
 $\bigwedge sa. \{\lambda s . s = sa\} \text{hook-ib-alloc-security } sa \text{sec}' \{\lambda r s. r = 0 \vee r \neq 0\}$
assumes *stb-ib-free-security* :
 $\bigwedge sa. \{\lambda s . s = sa\} \text{hook-ib-free-security } sa \text{sec}' \{\lambda r s. r = \text{unit}\}$

locale *lsm-network-xfrm-hooks* =

fixes *s0* :: 's
fixes *hook-xfrm-policy-alloc* :: 's \Rightarrow xfrm-sec-ctx \Rightarrow xfrm-user-sec-ctx \Rightarrow gfp-t \Rightarrow ('s, int) nondet-monad
fixes *hook-xfrm-policy-clone* :: 's \Rightarrow xfrm-sec-ctx \Rightarrow xfrm-user-sec-ctx \Rightarrow ('s, int) nondet-monad
fixes *hook-xfrm-policy-free* :: 's \Rightarrow xfrm-sec-ctx \Rightarrow ('s, unit) nondet-monad
fixes *hook-xfrm-policy-delete* :: 's \Rightarrow xfrm-sec-ctx \Rightarrow ('s, int) nondet-monad
fixes *hook-xfrm-state-alloc* :: 's \Rightarrow xfrm-state \Rightarrow xfrm-sec-ctx \Rightarrow ('s, int) nondet-monad

```

fixes hook-xfrm-state-alloc-acquire :: 's ⇒ xfrm-state ⇒ xfrm-sec-ctx ⇒ u32
⇒ ('s, int) nondet-monad
fixes hook-xfrm-state-delete :: 's ⇒ xfrm-state ⇒ ('s, int) nondet-monad
fixes hook-xfrm-state-free :: 's ⇒ xfrm-state ⇒ ('s, unit) nondet-monad
fixes hook-xfrm-policy-lookup :: 's ⇒ xfrm-sec-ctx ⇒ u32 ⇒ u8 ⇒ ('s, int)
nondet-monad
fixes hook-xfrm-state-pol-flow-match :: 's ⇒ xfrm-state ⇒ xfrm-policy ⇒ flowi
⇒ ('s, int) nondet-monad
fixes hook-xfrm-decode-session :: 's ⇒ sk-buff ⇒ u32 ⇒ ('s, int) nondet-monad
fixes hook-skb-classify-flow :: 's ⇒ sk-buff ⇒ flowi ⇒ ('s, unit) nondet-monad
assumes stb-xfrm-policy-alloc :
  ∧ sa. {λ s . s = sa } hook-xfrm-policy-alloc sa ctxp sec-ctx gfp' {λ r s. r = 0 ∨
r ≠ 0}
assumes stb-xfrm-policy-clone :
  ∧ sa. {λ s . s = sa } hook-xfrm-policy-clone sa old-ctx new-ctxp {λ r s. r = 0 ∨
r ≠ 0}
assumes stb-xfrm-policy-free :
  ∧ sa. {λ s . s = sa } hook-xfrm-policy-free sa ctx {λ r s. r = unit}
assumes stb-xfrm-policy-delete :
  ∧ sa. {λ s . s = sa } hook-xfrm-policy-delete sa ctx {λ r s. r = 0 ∨ r ≠ 0}
assumes stb-xfrm-state-alloc :
  ∧ sa. {λ s . s = sa } hook-xfrm-state-alloc sa x sec-ctx' {λ r s. r = 0 ∨ r ≠ 0}
assumes stb-xfrm-state-alloc-acquire :
  ∧ sa. {λ s . s = sa } hook-xfrm-state-alloc-acquire sa x plosec secid' {λ r s. r =
0 ∨ r ≠ 0}
assumes stb-xfrm-state-delete :
  ∧ sa. {λ s . s = sa } hook-xfrm-state-delete sa x {λ r s. r = 0 ∨ r ≠ 0}
assumes stb-xfrm-state-free :
  ∧ sa. {λ s . s = sa } hook-xfrm-state-free sa x {λ r s. r = unit}
assumes stb-xfrm-policy-lookup :
  ∧ sa. {λ s . s = sa } hook-xfrm-policy-lookup sa ctx fl-secid dir {λ r s. s = sa ∧
(r = 0 ∨ r ≠ 0)}
assumes stb-xfrm-state-pol-flow-match :
  ∧ sa. {λ s . s = sa } hook-xfrm-state-pol-flow-match sa x xp fl {λ r s. s = sa ∧ (r
= 0 ∨ r ≠ 0)}
assumes stb-xfrm-decode-session :
  ∧ sa. {λ s . s = sa } hook-xfrm-decode-session sa skb secid' {λ r s. r = 0 ∨ r ≠
0}
assumes stb-skb-classify-flow :
  ∧ sa. {λ s . s = sa } hook-skb-classify-flow sa skb fl {λ r s. r = unit}

```

locale lsm-path-hooks =

```

fixes s0 :: 's
fixes hook-path-unlink :: 's ⇒ path ⇒ dentry ⇒ ('s, int) nondet-monad
fixes hook-path-mkdir :: 's ⇒ path ⇒ dentry ⇒ nat ⇒ ('s, int) nondet-monad
fixes hook-path-rmdir :: 's ⇒ path ⇒ dentry ⇒ ('s, int) nondet-monad
fixes hook-path-mknod :: 's ⇒ path ⇒ dentry ⇒ nat ⇒ nat ⇒ ('s, int)
nondet-monad

```

```

fixes hook-path-truncate :: 's ⇒ path ⇒ ('s, int) nondet-monad
fixes hook-path-symlink :: 's ⇒ path ⇒ dentry ⇒ string ⇒ ('s, int) nondet-monad
fixes hook-path-link :: 's ⇒ dentry ⇒ path ⇒ dentry ⇒ ('s, int) nondet-monad
fixes hook-path-rename :: 's ⇒ path ⇒ dentry ⇒ path ⇒ dentry ⇒ ('s, int)
nondet-monad
fixes hook-path-chmod :: 's ⇒ path ⇒ nat ⇒ ('s, int) nondet-monad
fixes hook-path-chown :: 's ⇒ path ⇒ kuid-t ⇒ kgid-t ⇒ ('s, int) nondet-monad
fixes hook-path-chroot :: 's ⇒ path ⇒ ('s, int) nondet-monad
assumes stb-path-unlink :
  ∧sa. {λs . s = sa} hook-path-unlink s dir dentry {λr s. s = sa ∧ (r = 0 ∨ r
≠ 0)}
assumes stb-path-mkdir :
  ∧sa. {λs . s = sa} hook-path-mkdir s dir dentry m {λr s. s = sa ∧ (r = 0 ∨
r ≠ 0)}
assumes stb-path-rmdir :
  ∧sa. {λs . s = sa} hook-path-rmdir s dir dentry {λr s. s = sa ∧ (r = 0 ∨ r
≠ 0)}
assumes stb-path-mknod :
  ∧sa. {λs . s = sa} hook-path-mknod s dir dentry m dev {λr s. s = sa ∧ (r =
0 ∨ r ≠ 0)}
assumes stb-path-truncate :
  ∧sa. {λs . s = sa} hook-path-truncate s dir {λr s. s = sa ∧ (r = 0 ∨ r ≠
0)}
assumes stb-path-symlink :
  ∧sa. {λs . s = sa} hook-path-symlink s dir dentry old-name {λr s. s = sa ∧
(r = 0 ∨ r ≠ 0)}
assumes stb-path-link :
  ∧sa. {λs . s = sa} hook-path-link s old-dentry new-dir new-dentry
{λr s. s = sa ∧ (r = 0 ∨ r ≠ 0)}
assumes stb-path-rename :
  ∧sa. {λs . s = sa} hook-path-rename s old-dir old-dentry new-dir new-dentry
{λr s. s = sa ∧ (r = 0 ∨ r ≠ 0)}
assumes stb-path-chmod :
  ∧sa. {λs . s = sa} hook-path-chmod s path m {λr s. s = sa ∧ (r = 0 ∨ r ≠
0)}
assumes stb-path-chown :
  ∧sa. {λs . s = sa} hook-path-chown s path uid' gid' {λr s. s = sa ∧ (r = 0
∨ r ≠ 0)}
assumes stb-path-chroot :
  ∧sa. {λs . s = sa} hook-path-chroot s path {λr s. s = sa ∧ (r = 0 ∨ r ≠ 0)}

```

locale lsm-key-hooks =

```

fixes s0 :: 's
fixes key-security :: 's ⇒ key ⇒ 'ksec option
fixes hook-key-alloc :: 's ⇒ key ⇒ Cred ⇒ nat ⇒ ('s, int) nondet-monad
fixes hook-key-free :: 's ⇒ key ⇒ ('s, unit) nondet-monad

```

fixes *hook-key-permission* :: 's \Rightarrow key-ref-t \Rightarrow Cred \Rightarrow nat \Rightarrow ('s, int) nondet-monad
fixes *hook-key-getsecurity* :: 's \Rightarrow key \Rightarrow string \Rightarrow ('s, int) nondet-monad

assumes *stb-key-alloc*:
 $\bigwedge sa. \llbracket \lambda s. s = sa \rrbracket$ *hook-key-alloc* sa k cred' flag $\llbracket \lambda r s. r = 0 \vee r \neq 0 \rrbracket$
assumes *stb-key-free* :
 $\bigwedge sa. \llbracket \lambda s. s = sa \rrbracket$ *hook-key-free* sa k $\llbracket \lambda r s. r = \text{unit} \wedge \text{key-security } s \text{ k} = \text{None} \rrbracket$
assumes *stb-key-permission*:
 $\bigwedge sa. \llbracket \lambda s. s = sa \rrbracket$ *hook-key-permission* sa key-ref c perm $\llbracket \lambda r s. s = sa \wedge (r = 0 \vee r \neq 0) \rrbracket$
assumes *stb-key-getsecurity*:
 $\bigwedge sa. \llbracket \lambda s. s = sa \rrbracket$ *hook-key-getsecurity* sa key' buffer $\llbracket \lambda r s. s = sa \wedge (r = 0 \vee r \neq 0) \rrbracket$

locale *lsm-audit-hooks* =

fixes *s0* :: 's
fixes *hook-audit-rule-init* :: 's \Rightarrow nat \Rightarrow enum-audit \Rightarrow string \Rightarrow string
 \Rightarrow ('s, int) nondet-monad
fixes *hook-audit-rule-known* :: 's \Rightarrow audit-krule \Rightarrow ('s, int) nondet-monad
fixes *hook-audit-rule-match* :: 's \Rightarrow nat \Rightarrow nat \Rightarrow enum-audit \Rightarrow string \Rightarrow
audit-context
 \Rightarrow ('s, int) nondet-monad
fixes *hook-audit-rule-free* :: 's \Rightarrow string \Rightarrow ('s, unit) nondet-monad

assumes *stb-audit-rule-init*:
 $\bigwedge sa. \llbracket \lambda s. s = sa \rrbracket$ *hook-audit-rule-init* s field op rulestr vrule $\llbracket \lambda r s. r = 0 \vee r \neq 0 \rrbracket$
assumes *stb-audit-rule-known* :
 $\bigwedge sa. \llbracket \lambda s. s = sa \rrbracket$ *hook-audit-rule-known* s krule $\llbracket \lambda r s. r = 0 \vee r \neq 0 \rrbracket$
assumes *stb-audit-rule-match*:
 $\bigwedge sa. \llbracket \lambda s. s = sa \rrbracket$ *hook-audit-rule-match* s secid' field op vrule actx $\llbracket \lambda r s. r = 0 \vee r \neq 0 \rrbracket$
assumes *stb-key-audit-rule-free*:
 $\bigwedge sa. \llbracket \lambda s. s = sa \rrbracket$ *hook-audit-rule-free* s lsmrule $\llbracket \lambda r s. r = \text{unit} \rrbracket$

locale *lsm-bpf-hooks* =

fixes *s0* :: 's
fixes *hook-bpf* :: 's \Rightarrow int \Rightarrow bpf-attr \Rightarrow nat \Rightarrow ('s, int) nondet-monad
fixes *hook-bpf-map* :: 's \Rightarrow bpf-map \Rightarrow mode \Rightarrow ('s, int) nondet-monad
fixes *hook-bpf-prog* :: 's \Rightarrow bpf-prog \Rightarrow ('s, int) nondet-monad
fixes *hook-bpf-map-alloc* :: 's \Rightarrow bpf-map \Rightarrow ('s, int) nondet-monad
fixes *hook-bpf-map-free* :: 's \Rightarrow bpf-map \Rightarrow ('s, unit) nondet-monad
fixes *hook-bpf-prog-alloc* :: 's \Rightarrow bpf-prog-aux \Rightarrow ('s, int) nondet-monad
fixes *hook-bpf-prog-free* :: 's \Rightarrow bpf-prog-aux \Rightarrow ('s, unit) nondet-monad
assumes *stb-bpf* :

```

     $\bigwedge sa. \llbracket \lambda s. s = sa \rrbracket \text{hook-bpf } sa \text{ cmd attr' size' } \llbracket \lambda r s. r = 0 \vee r \neq 0 \rrbracket$ 
assumes stb-bpf-map :
     $\bigwedge sa. \llbracket \lambda s. s = sa \rrbracket \text{hook-bpf-map } sa \text{ bmap fmode } \llbracket \lambda r s. r = 0 \vee r \neq 0 \rrbracket$ 
assumes stb-bpf-prog:
     $\bigwedge sa. \llbracket \lambda s. s = sa \rrbracket \text{hook-bpf-prog } sa \text{ prog } \llbracket \lambda r s. r = 0 \vee r \neq 0 \rrbracket$ 
assumes stb-bpf-map-alloc:
     $\bigwedge sa. \llbracket \lambda s. s = sa \rrbracket \text{hook-bpf-map-alloc } sa \text{ bmap } \llbracket \lambda r s. r = 0 \vee r \neq 0 \rrbracket$ 
assumes stb-bpf-map-free:
     $\bigwedge sa. \llbracket \lambda s. s = sa \rrbracket \text{hook-bpf-map-free } sa \text{ bmap } \llbracket \lambda r s. r = \text{unit} \rrbracket$ 
assumes stb-bpf-prog-alloc:
     $\bigwedge sa. \llbracket \lambda s. s = sa \rrbracket \text{hook-bpf-prog-alloc } sa \text{ proga } \llbracket \lambda r s. r = 0 \vee r \neq 0 \rrbracket$ 
assumes stb-bpf-prog-free:
     $\bigwedge sa. \llbracket \lambda s. s = sa \rrbracket \text{hook-bpf-prog-free } sa \text{ proga } \llbracket \lambda r s. r = \text{unit} \rrbracket$ 

```

```

locale lsm-hooks =
  lsm-superblock-hooks s0 +
  lsm-task-hooks s0 +
  lsm-binder-hooks s0 +
  lsm-pttrace-hooks s0 +
  lsm-capable-hooks s0 +
  lsm-bprm-hooks s0 +
  lsm-dentry-hooks s0 +
  lsm-inode-hooks s0 +
  lsm-file-hooks s0 +
  lsm-kernel-hooks s0 +
  lsm-ipc-hooks s0 +
  lsm-other-hooks s0 +
  lsm-network-hooks s0 +
  lsm-infiniband-hooks s0 +
  lsm-network-xfrm-hooks s0 +
  lsm-path-hooks s0 +
  lsm-key-hooks s0 +
  lsm-audit-hooks s0 +
  lsm-bpf-hooks s0
for s0 :: 's

```

```

begin
end
end

```

27 LSM Model

```

theory Linux-LSM-Model
imports
  SOAC
  LSM-Cap
  Linux-LSM-Hooks
  ../lib/Monad-WP/NonDetMonadVCG

```

begin

In this theory, we introduce LSM Model

27.1 def security opts type

definition *security-init-mnt-opts* $\equiv (\text{mnt-opts} = [], \text{mnt-opts-flags} = [], \text{num-mnt-opts}=0)$

27.2 lsm model

locale *lsm* = *lsm-hooks state* + *SOModel subj-label obj-label access-rules Subj Obj request*

for *state* :: 's
and *subj-label* :: 's \Rightarrow Subj \Rightarrow subject-label
and *obj-label* :: 's \Rightarrow Obj \Rightarrow object-label
and *access-rules* :: Label \Rightarrow Label \Rightarrow access set
and *Subj* :: 's \Rightarrow Subj set
and *Obj* :: 's \Rightarrow Obj set
and *request* :: 's \Rightarrow Subj \Rightarrow Obj \Rightarrow Request \Rightarrow decision
+
fixes *k-task* :: 's \Rightarrow process-id \rightarrow Task
fixes *inodes* :: 's \Rightarrow inum \rightarrow inode

begin

definition *security-capget* :: 's \Rightarrow Task \Rightarrow kct \Rightarrow kct \Rightarrow kct \Rightarrow ('s, int) nondet-monad
where *security-capget* *s target effective inheritable permitted* \equiv
hook-capget *s target effective inheritable permitted*

definition *security-capset* :: 's \Rightarrow Cred \Rightarrow Cred \Rightarrow kct \Rightarrow kct \Rightarrow kct \Rightarrow ('s, int) nondet-monad
where *security-capset* *s new old effective inheritable permitted* \equiv
hook-capset *s new old effective inheritable permitted*

definition *security-capable* :: 's \Rightarrow Cred \Rightarrow ns \Rightarrow cap \Rightarrow ('s, int) nondet-monad
where *security-capable* *s c ns cap* \equiv *hook-capable* *s c ns cap*

definition *security-capable-noaudit* :: 's \Rightarrow Cred \Rightarrow ns \Rightarrow cap \Rightarrow ('s, int) nondet-monad
where *security-capable-noaudit* *s c ns cap* \equiv *hook-capable-noaudit* *s c ns cap*

definition *security-quotactl* :: 's \Rightarrow int \Rightarrow int \Rightarrow int \Rightarrow super-block option \Rightarrow ('s, int) nondet-monad
where *security-quotactl* *s cmds t id' sb* \equiv *hook-quotactl* *s cmds t id' sb*

definition *security-quota-on* :: 's \Rightarrow dentry \Rightarrow ('s, int) nondet-monad
where *security-quota-on* *s dentry* \equiv *hook-quota-on* *s dentry*

definition *security-settime64* :: 's \Rightarrow ts \Rightarrow tz option \Rightarrow ('s, int) nondet-monad

where *security-settime64* *s ts tz* \equiv *hook-settime64* *s ts tz*

definition *vm-enough-memory* :: '*s* \Rightarrow *mm* \Rightarrow *pages* \Rightarrow *int* \Rightarrow *int*
where *vm-enough-memory* *s mm' p pages* \equiv 0

definition *security-vm-enough-memory-mm* :: '*s* \Rightarrow *mm* \Rightarrow *pages* \Rightarrow ('*s*, *int*)
nondet-monad
where *security-vm-enough-memory-mm* *s mm' pages* \equiv *do*
 rc \leftarrow *hook-vm-enough-memory-mm* *s mm' pages*;
 cap-sys-admin \leftarrow (if *rc* \leq 0 then return 0
 else return 1
);
 return(*vm-enough-memory* *s mm' pages cap-sys-admin*)
od

definition *security-binder-set-context-mgr* :: '*s* \Rightarrow *Task* \Rightarrow ('*s*, *int*) *nondet-monad*
where *security-binder-set-context-mgr* *s mgr* \equiv *hook-binder-set-context-mgr* *s mgr*

definition *security-binder-transaction* :: '*s* \Rightarrow *Task* \Rightarrow *Task* \Rightarrow ('*s*, *int*) *nondet-monad*
where *security-binder-transaction* *s from to* \equiv *hook-binder-transaction* *s from to*

definition *security-binder-transfer-binder* :: '*s* \Rightarrow *Task* \Rightarrow *Task* \Rightarrow ('*s*, *int*) *nondet-monad*
where *security-binder-transfer-binder* *s from to* \equiv *hook-binder-transfer-binder* *s from to*

definition *security-binder-transfer-file* :: '*s* \Rightarrow *Task* \Rightarrow *Task* \Rightarrow *Files* \Rightarrow ('*s*, *int*)
nondet-monad
where *security-binder-transfer-file* *s from to file* \equiv *hook-binder-transfer-file* *s from to file*

definition *security-pttrace-access-check* :: '*s* \Rightarrow *Task* \Rightarrow *nat* \Rightarrow ('*s*, *int*) *nondet-monad*
where *security-pttrace-access-check* *s child m* \equiv *hook-pttrace-access-check* *s child m*

definition *security-pttrace-traceme* :: '*s* \Rightarrow *Task* \Rightarrow ('*s*, *int*) *nondet-monad*
where *security-pttrace-traceme* *s parent'* \equiv *hook-pttrace-traceme* *s parent'*

definition *security-syslog* :: '*s* \Rightarrow *int* \Rightarrow ('*s*, *int*) *nondet-monad*
where *security-syslog* *s type* \equiv *hook-syslog* *s type*

definition *ima-bprm-check* *bprm* = 0

definition *security-bprm-set-creds* :: '*s* \Rightarrow *linux-binprm* \Rightarrow ('*s*, *int*) *nondet-monad*
where *security-bprm-set-creds* *s bprm* \equiv *hook-bprm-set-creds* *s bprm*

definition *security-bprm-check* :: 's ⇒ linux-binprm ⇒ ('s, int) nondet-monad
where *security-bprm-check* s bprm ≡ do
 ret ← hook-bprm-check s bprm;
 rc ← (if ret ≠ 0 then return ret
 else return (ima-bprm-check bprm));
 return rc
 od

definition *security-bprm-committing-creds* :: 's ⇒ linux-binprm ⇒ ('s, unit) nondet-monad
where *security-bprm-committing-creds* s bprm ≡ hook-bprm-committing-creds s bprm

definition *security-bprm-committed-creds* :: 's ⇒ linux-binprm ⇒ ('s, unit) nondet-monad
where *security-bprm-committed-creds* s bprm ≡ hook-bprm-committed-creds s bprm

definition *security-sb-alloc* :: 's ⇒ super-block ⇒ ('s, int) nondet-monad
where *security-sb-alloc* s sb ≡ hook-sb-alloc s sb

definition *security-sb-free* :: 's ⇒ super-block ⇒ ('s, unit) nondet-monad
where *security-sb-free* s sb ≡ hook-sb-free s sb

definition *security-sb-copy-data* :: 's ⇒ string ⇒ string ⇒ ('s, int) nondet-monad
where *security-sb-copy-data* s orig copy ≡ hook-sb-copy-data s orig copy

definition *security-sb-remount* :: 's ⇒ super-block ⇒ Void ⇒ ('s, int) nondet-monad
where *security-sb-remount* s sb data ≡ hook-sb-remount s sb data

definition *security-sb-kern-mount* :: 's ⇒ super-block ⇒ int ⇒ string ⇒ ('s, int) nondet-monad
where *security-sb-kern-mount* s sb flgs data ≡ hook-sb-kern-mount s sb flgs data

definition *security-sb-show-options* :: 's ⇒ seq-file ⇒ super-block ⇒ ('s, int) nondet-monad
where *security-sb-show-options* s m sb ≡ hook-sb-show-options s m sb

definition *security-sb-statfs* :: 's ⇒ dentry ⇒ ('s, int) nondet-monad
where *security-sb-statfs* s dentry ≡ hook-sb-statfs s dentry

definition *security-sb-mount* :: 's ⇒ string ⇒ path ⇒ string ⇒ int ⇒ Void ⇒ ('s, int) nondet-monad
where *security-sb-mount* s dev-name path type flgs data ≡
 hook-sb-mount s dev-name path type flgs data

definition *security-sb-umount* :: 's ⇒ vfstmount ⇒ int ⇒ ('s, int) nondet-monad
where *security-sb-umount* s vmnt flgs ≡ hook-sb-umount s vmnt flgs

definition *security-sb-pivotroot* :: 's ⇒ path ⇒ path ⇒ ('s, int) nondet-monad
where *security-sb-pivotroot* s old-path new-path ≡ *hook-sb-pivotroot* s old-path new-path

definition *security-sb-set-mnt-opts* :: 's ⇒ super-block ⇒ opts ⇒ nat ⇒ nat ⇒ ('s, int) nondet-monad
where *security-sb-set-mnt-opts* s sb opt kern-flags set-kern-flags ≡ *hook-sb-set-mnt-opts* s sb opt kern-flags set-kern-flags

definition *security-sb-clone-mnt-opts* :: 's ⇒ super-block ⇒ super-block ⇒ int ⇒ int ⇒ ('s, int) nondet-monad
where *security-sb-clone-mnt-opts* s oldsb newsb kern-flags set-kern-flags ≡ *hook-sb-clone-mnt-opts* s oldsb newsb kern-flags set-kern-flags

definition *security-sb-parse-opts-str* :: 's ⇒ string ⇒ opts ⇒ ('s, int) nondet-monad
where *security-sb-parse-opts-str* s options opt ≡ *hook-sb-parse-opts-str* s options opt

definition *d-backing-inode* :: 's ⇒ dentry ⇒ inode option
where *d-backing-inode* s upper ≡ ((*inodes* s)(*d-inode* upper))

definition *integrity-inode-free* :: 's ⇒ inode ⇒ ('s, unit) nondet-monad
where *integrity-inode-free* s inode ≡ *return*()

definition *security-inode-alloc* :: 's ⇒ inode ⇒ ('s, int) nondet-monad
where *security-inode-alloc* s inode ≡ *hook-inode-alloc* s inode

definition *security-inode-free* :: 's ⇒ inode ⇒ ('s, unit) nondet-monad
where *security-inode-free* s inode ≡ do
 integrity-inode-free s inode;
 hook-inode-free s inode
 od

definition *evm-inode-init-security* :: inode ⇒ xattrs ⇒ xattrs ⇒ int
where *evm-inode-init-security* inode xattr-array evm ≡ 0

definition *initxattrss* :: inode ⇒ xattrs list ⇒ string ⇒ int
where *initxattrss* inode xattr-array fs-data ≡ 1

definition *security-inode-init-security* :: 's ⇒ inode ⇒ inode ⇒ string ⇒ initxattrs
 ⇒ string ⇒ ('s, int) nondet-monad
where *security-inode-init-security* s inode dir qstr initxattrs' fsdata = do
 new-xattrs ← *return*(SOME x::xattrs list. True);
 lsm-xattr ← *return*(SOME x::xattrs. True);
 evm-xattr ← *return*(SOME x::xattrs. True);

```

    xattr ← return(SOME x::xattr. True);
    rc ← (if unlikely (IS-PRIVATE inode) then return (0)
        else
            if initxattrs' = 0 then
                (hook-inode-init-security s inode dir qstr "" "" 0)
            else do
                lsm-xattrs ← return (new-xattrs);
                lsm-xattr ← return (lsm-xattrs ! 0);
                ret ← (hook-inode-init-security s inode dir qstr (xattr-name
lsm-xattr)
                                (xattr-value lsm-xattr) (xattr-value-len
lsm-xattr)));
                if ret ≠ 0 then
                    if ret = (−EOPNOTSUPP) then
                        return 0
                    else return ret
                else do
                    evm-xattr ← return(lsm-xattrs ! 1);
                    ret ← return(evm-inode-init-security inode lsm-xattr
evm-xattr);
                    if ret ≠ 0 then
                        if ret = (−EOPNOTSUPP) then
                            (return 0)
                        else return ret
                    else
                        do
                            ret ← return (initxattrss inode new-xattrs
fsdata);
                            if ret = (−EOPNOTSUPP) then (
                                return 0)
                            else return ret
                        od
                    od
                od
            od
        );
    return rc
od

```

definition *security-old-inode-init-security* :: 's ⇒ inode ⇒ inode ⇒ qstr ⇒ string

⇒ string ⇒ int ⇒ ('s, int) nondet-monad

where *security-old-inode-init-security* s inode dir qstr name value len' ≡
hook-old-inode-init-security s inode dir qstr name value len'

definition *security-inode-create* :: 's ⇒ inode ⇒ dentry ⇒ mode ⇒ ('s, int) nondet-monad

where *security-inode-create* s dir dentry m ≡
 if unlikely (IS-PRIVATE dir) then

```

    return 0
else
    hook-inode-create s dir dentry m

```

definition *security-inode-link* :: 's \Rightarrow dentry \Rightarrow inode \Rightarrow dentry \Rightarrow ('s, int) nondet-monad
where *security-inode-link* s old-dentry dir new-dentry \equiv
 if unlikely (IS-PRIVATE (the(d-backing-inode s old-dentry))) then
 return 0
 else
 hook-inode-link s old-dentry dir new-dentry

definition *security-inode-unlink* :: 's \Rightarrow inode \Rightarrow dentry \Rightarrow ('s, int) nondet-monad
where *security-inode-unlink* s dir dentry \equiv
 if unlikely (IS-PRIVATE (the(d-backing-inode s dentry))) then
 return 0
 else
 hook-inode-unlink s dir dentry

definition *security-inode-symlink* :: 's \Rightarrow inode \Rightarrow dentry \Rightarrow string \Rightarrow ('s, int) nondet-monad
where *security-inode-symlink* s dir dentry old-name \equiv
 if unlikely (IS-PRIVATE dir) then
 return 0
 else
 hook-inode-symlink s dir dentry old-name

definition *security-inode-mkdir* :: 's \Rightarrow inode \Rightarrow dentry \Rightarrow mode \Rightarrow ('s, int) nondet-monad
where *security-inode-mkdir* s dir dentry m \equiv
 if unlikely (IS-PRIVATE dir) then
 return 0
 else
 hook-inode-mkdir s dir dentry m

definition *security-inode-rmdir* :: 's \Rightarrow inode \Rightarrow dentry \Rightarrow ('s, int) nondet-monad
where *security-inode-rmdir* s dir dentry \equiv
 if unlikely (IS-PRIVATE (the(d-backing-inode s dentry))) then
 return 0
 else
 hook-inode-rmdir s dir dentry

definition *security-inode-mknod* :: 's \Rightarrow inode \Rightarrow dentry \Rightarrow mode \Rightarrow dev-t \Rightarrow ('s, int) nondet-monad
where *security-inode-mknod* s dir dentry m dev \equiv
 if unlikely (IS-PRIVATE dir) then
 return 0
 else
 hook-inode-mknod s dir dentry m dev

definition *security-inode-rename* :: 's \Rightarrow inode \Rightarrow dentry \Rightarrow inode \Rightarrow dentry \Rightarrow

flags

$\Rightarrow ('s, int) \text{ nondet-monad}$

where *security-inode-rename* *s old-dir old-dentry new-dir new-dentry flgs* \equiv
 if unlikely (*IS-PRIVATE* (*the(d-backing-inode s old-dentry)*)) \vee
 ((*d-is-positive new-dentry*) \wedge *IS-PRIVATE* (*the(d-backing-inode s*
old-dentry))) $\neq 0$)
 then return 0
 else if ((*int flgs*) AND *RENAME-EXCHANGE*) $\neq 0$ then
 do
 err \leftarrow (*hook-inode-rename s new-dir new-dentry old-dir old-dentry*);
 if *err* $\neq 0$ then
 return *err*
 else (*hook-inode-rename s old-dir old-dentry new-dir new-dentry*)
 od
 else
 (*hook-inode-rename s old-dir old-dentry new-dir new-dentry*)

definition *security-inode-readlink* $:: 's \Rightarrow \text{dentry} \Rightarrow ('s, int) \text{ nondet-monad}$

where *security-inode-readlink s dentry* \equiv
 if unlikely (*IS-PRIVATE* (*the(d-backing-inode s dentry)*))) then
 return 0
 else
 hook-inode-readlink s dentry

definition *security-inode-follow-link* $:: 's \Rightarrow \text{dentry} \Rightarrow \text{inode} \Rightarrow \text{bool} \Rightarrow ('s, int) \text{ nondet-monad}$

where *security-inode-follow-link s dentry inode rcu'* \equiv
 if unlikely (*IS-PRIVATE inode*) then
 return 0
 else
 hook-inode-follow-link s dentry inode rcu'

definition *security-inode-permission* $:: 's \Rightarrow \text{inode} \Rightarrow \text{mask} \Rightarrow ('s, int) \text{ nondet-monad}$

where *security-inode-permission s inode m* \equiv
 if unlikely (*IS-PRIVATE inode*) then
 return 0
 else
 hook-inode-permission s inode m

definition *evm-inode-setattr* $:: 's \Rightarrow \text{dentry} \Rightarrow \text{iattr} \Rightarrow ('s, int) \text{ nondet-monad}$

where *evm-inode-setattr s dentry at* \equiv return 0

definition *security-inode-setattr* $:: 's \Rightarrow \text{dentry} \Rightarrow \text{iattr} \Rightarrow ('s, int) \text{ nondet-monad}$

where *security-inode-setattr s dentry attr'* \equiv
 if unlikely (*IS-PRIVATE* (*the(d-backing-inode s dentry)*))) then
 return 0
 else do
 ret \leftarrow *hook-inode-setattr s dentry attr'*;

```

    if ret  $\neq$  0 then
      return ret
    else
      evm-inode-setattr s dentry attr'
  od

```

definition *security-inode-getattr* :: 's \Rightarrow path \Rightarrow ('s, int) nondet-monad
where *security-inode-getattr* s path \equiv
 if unlikely (IS-PRIVATE (the(d-backing-inode s (p-dentry path))))
 then
 return 0
 else
 hook-inode-getattr s path

definition *ima-inode-setxattr* :: 's \Rightarrow dentry \Rightarrow xattr \Rightarrow string \Rightarrow int \Rightarrow ('s, int) nondet-monad
where *ima-inode-setxattr* s d x value flg \equiv return 0

definition *evm-inode-setxattr* :: 's \Rightarrow dentry \Rightarrow xattr \Rightarrow string \Rightarrow int \Rightarrow ('s, int) nondet-monad
where *evm-inode-setxattr* s d x value flg \equiv return 0

definition *security-inode-setxattr* :: 's \Rightarrow dentry \Rightarrow xattr \Rightarrow string \Rightarrow int \Rightarrow flags \Rightarrow ('s, int) nondet-monad
where *security-inode-setxattr* s dentry name value size' flgs \equiv
 if unlikely (IS-PRIVATE (the(d-backing-inode s dentry)))
 then return 0
 else do
 ret \leftarrow hook-inode-setxattr s dentry name value size' flgs;
 if ret \neq 1 then
 cap-inode-setxattr s dentry name value size' flgs
 else if ret \neq 0 then
 return ret
 else
 do
 ret \leftarrow ima-inode-setxattr s dentry name value size';
 if ret \neq 0 then
 return ret
 else
 evm-inode-setxattr s dentry name value size'
 od
 od

definition *evm-inode-post-setxattr* :: 's \Rightarrow dentry \Rightarrow xattr \Rightarrow string \Rightarrow int \Rightarrow ('s, unit) nondet-monad
where *evm-inode-post-setxattr* s d x value flg \equiv return ()

definition *security-inode-post-setxattr* :: 's \Rightarrow dentry \Rightarrow xattr \Rightarrow string \Rightarrow int \Rightarrow

flags

$\Rightarrow ('s, \text{unit}) \text{ nondet-monad}$

where *security-inode-post-setxattr* *s dentry name value size' flags* \equiv
 if unlikely (*IS-PRIVATE* (*the(d-backing-inode s dentry)*)) then
 return ()
 else
 do
 hook-inode-post-setxattr s dentry name value size' flags;
 evm-inode-post-setxattr s dentry name value size'
 od

definition *security-inode-getxattr* :: '*s* \Rightarrow *dentry* \Rightarrow *xattr* \Rightarrow ('*s*, *int*) nondet-monad

where *security-inode-getxattr* *s dentry name* \equiv
 if unlikely (*IS-PRIVATE* (*the(d-backing-inode s dentry)*))
 then
 return 0
 else
 hook-inode-getxattr s dentry name

definition *security-inode-listxattr* :: '*s* \Rightarrow *dentry* \Rightarrow ('*s*, *int*) nondet-monad

where *security-inode-listxattr* *s dentry* \equiv
 if unlikely (*IS-PRIVATE* (*the(d-backing-inode s dentry)*))
 then
 return 0
 else
 hook-inode-listxattr s dentry

definition *current-user-ns* :: '*s* \Rightarrow *ns*

where *current-user-ns* *s* = *user-ns* (*cred(the((k-task s) (current s)))*)

definition *privileged-wrt-inode-uidgid* :: *ns* \Rightarrow *inode* \Rightarrow *bool*

where *privileged-wrt-inode-uidgid* *ns inode* \equiv
 (*kuid-has-mapping ns (i-uid inode)*)
 \wedge (*kgid-has-mapping ns (i-gid inode)*)

definition *capable-wrt-inode-uidgid* :: '*s* \Rightarrow *inode* \Rightarrow *int* \Rightarrow *bool*

where *capable-wrt-inode-uidgid* *s inode cap* \equiv
 let *ns* = *current-user-ns s*
 in (*ns-capable ns cap*) \wedge *privileged-wrt-inode-uidgid ns inode*

definition *cap-inode-removexattr* :: '*s* \Rightarrow *dentry* \Rightarrow *xattr* \Rightarrow ('*s*, *int*) nondet-monad

where *cap-inode-removexattr* *s dentry name* \equiv do
 ns \leftarrow return (*s-user-ns (d-sb dentry)*);
 rc \leftarrow (if *name* = *XATTR-SECURITY-PREFIX*
 then
 return 0
 else
 if *name* = *XATTR-NAME-CAPS* then


```

do
  inode ← return ((d-backing-inode s dentry));
  if inode = None then
    return(−EINVAL)
  else
    if ¬(capable-wrt-inode-uidgid s (the inode) CAP-SETFCAP)
then
    return(−EPERM)
  else
    return 0
od
else
  if ¬(ns-capable ns CAP-SYS-ADMIN)
then
    return (−EPERM)
  else
    return 0
);
return(rc)
od

```

definition *ima-inode-removexattr* :: *dentry* ⇒ *xattr* ⇒ *int*
where *ima-inode-removexattr dentry name* ≡ 0

definition *evm-inode-removexattr* :: *dentry* ⇒ *xattr* ⇒ *int*
where *evm-inode-removexattr dentry name* ≡ 0

definition *security-inode-removexattr* :: 's ⇒ *dentry* ⇒ *xattr* ⇒ ('s, int) nondet-monad

where *security-inode-removexattr s dentry name* ≡
 if unlikely (IS-PRIVATE (the(d-backing-inode s dentry))) then return 0
 else do
 ret ← hook-inode-removexattr s dentry name;
 rc ← if ret = 1 then
 cap-inode-removexattr s dentry name
 else if ret ≠ 0 then
 return ret
 else do
 ret ← return(ima-inode-removexattr dentry name);
 if ret ≠ 0 then
 return ret
 else
 return(evm-inode-removexattr dentry name)
 od ;
 return rc
 od

definition *security-inode-need-killpriv* :: 's ⇒ *dentry* ⇒ ('s, int) nondet-monad
where *security-inode-need-killpriv s dentry* ≡ hook-inode-need-killpriv s dentry

definition *security-inode-killpriv* :: 's \Rightarrow dentry \Rightarrow ('s, int) nondet-monad
where *security-inode-killpriv* s dentry \equiv *hook-inode-killpriv* s dentry

definition *security-inode-getsecurity* :: 's \Rightarrow inode \Rightarrow xattr \Rightarrow Void \Rightarrow bool \Rightarrow ('s, int) nondet-monad
where *security-inode-getsecurity* s inode name buffer alloc \equiv
 if unlikely (IS-PRIVATE (inode)) then return (−EOPNOTSUPP)
 else do
 rc \leftarrow *hook-inode-getsecurity* s inode name buffer alloc;
 if rc \neq (−EOPNOTSUPP)
 then
 return rc
 else
 return(−EOPNOTSUPP)
 od

definition *security-inode-setsecurity* :: 's \Rightarrow inode \Rightarrow xattr \Rightarrow Void \Rightarrow nat \Rightarrow int \Rightarrow ('s, int) nondet-monad
where *security-inode-setsecurity* s inode name value size' flgs \equiv
 if unlikely (IS-PRIVATE (inode))
 then
 return (−EOPNOTSUPP)
 else do
 rc \leftarrow *hook-inode-setsecurity* s inode name value size' flgs ;
 if rc \neq (−EOPNOTSUPP)
 then
 return rc
 else
 return(−EOPNOTSUPP)
 od

definition *security-inode-listsecurity* :: 's \Rightarrow inode \Rightarrow Void \Rightarrow int \Rightarrow ('s, int) nondet-monad
where *security-inode-listsecurity* s inode buffer bsize \equiv
 if unlikely (IS-PRIVATE (inode))
 then
 return 0
 else
 hook-inode-listsecurity s inode buffer bsize

definition *security-inode-getsecid* :: 's \Rightarrow inode \Rightarrow u32 \Rightarrow ('s, unit) nondet-monad
where *security-inode-getsecid* s inode secid' \equiv *hook-inode-getsecid* s inode secid'

definition *security-inode-copy-up* :: 's \Rightarrow dentry \Rightarrow Cred option \Rightarrow ('s, int) nondet-monad
where *security-inode-copy-up* s src new \equiv *hook-inode-copy-up* s src new

definition *security-inode-copy-up-xattr* :: 's \Rightarrow xattr \Rightarrow ('s, int) nondet-monad

where *security-inode-copy-up-xattr s name* \equiv *hook-inode-copy-up-xattr s name*

definition *security-inode-invalidate-secctx* :: *'s* \Rightarrow *inode* \Rightarrow (*'s*, *unit*) *nondet-monad*
where *security-inode-invalidate-secctx s inode* \equiv *hook-inode-invalidate-secctx s inode*

definition *security-inode-notifysecctx* :: *'s* \Rightarrow *inode* \Rightarrow *string* \Rightarrow *u32* \Rightarrow (*'s*, *int*) *nondet-monad*
where *security-inode-notifysecctx s inode ctx ctxlen* \equiv *hook-inode-notifysecctx s inode ctx ctxlen*

definition *security-inode-setsecctx* :: *'s* \Rightarrow *dentry* \Rightarrow *string* \Rightarrow *u32* \Rightarrow (*'s*, *int*) *nondet-monad*
where *security-inode-setsecctx s dentry ctx ctxlen* \equiv *hook-inode-setsecctx s dentry ctx ctxlen*

definition *security-inode-getsecctx* :: *'s* \Rightarrow *inode* \Rightarrow *string* \Rightarrow *u32* \Rightarrow (*'s*, *int*) *nondet-monad*
where *security-inode-getsecctx s dentry ctx ctxlen* \equiv *hook-inode-getsecctx s dentry ctx ctxlen*

definition *security-task-alloc* :: *'s* \Rightarrow *Task* \Rightarrow *nat* \Rightarrow (*'s*, *int*) *nondet-monad*
where *security-task-alloc s task clone-flags* \equiv *hook-task-alloc s task clone-flags*

definition *security-task-free* :: *'s* \Rightarrow *Task* \Rightarrow (*'s*, *unit*) *nondet-monad*
where *security-task-free s task* \equiv *hook-task-free s task*

definition *security-cred-alloc-blank* :: *'s* \Rightarrow *Cred* \Rightarrow *nat* \Rightarrow (*'s*, *int*) *nondet-monad*
where *security-cred-alloc-blank s cred' gfp'* \equiv *hook-cred-alloc-blank s cred' gfp'*

definition *security-cred-free* :: *'s* \Rightarrow *Cred* \Rightarrow (*'s*, *unit*) *nondet-monad*
where *security-cred-free s cred'* \equiv *hook-cred-free s cred'*

definition *security-prepare-creds* :: *'s* \Rightarrow *Cred* \Rightarrow *Cred* \Rightarrow *nat* \Rightarrow (*'s*, *int*) *nondet-monad*
where *security-prepare-creds s new old gfp'* \equiv *hook-prepare-creds s new old gfp'*

definition *security-transfer-creds* :: *'s* \Rightarrow *Cred* \Rightarrow *Cred* \Rightarrow (*'s*, *unit*) *nondet-monad*
where *security-transfer-creds s new old* \equiv *hook-transfer-creds s new old*

definition *security-cred-getsecid* :: *'s* \Rightarrow *Cred* \Rightarrow *u32* \Rightarrow (*'s*, *unit*) *nondet-monad*
where *security-cred-getsecid s c secid'* \equiv *do*
secid \leftarrow *return 0*;
hook-cred-getsecid s c secid
od

definition *security-task-fix-setuid* :: *'s* \Rightarrow *Cred* \Rightarrow *Cred* \Rightarrow *int* \Rightarrow (*'s*, *int*)

nondet-monad

where *security-task-fix-setuid s new old flgs* \equiv *hook-task-fix-setuid s new old flgs*

definition *security-task-setpgid* :: 's \Rightarrow Task \Rightarrow pid-t \Rightarrow ('s, int) *nondet-monad*

where *security-task-setpgid s p pgid* \equiv *hook-task-setpgid s p pgid*

definition *security-task-getpgid* :: 's \Rightarrow Task \Rightarrow ('s, int) *nondet-monad*

where *security-task-getpgid s p* \equiv *hook-task-getpgid s p*

definition *security-task-getsid* :: 's \Rightarrow Task \Rightarrow ('s, int) *nondet-monad*

where *security-task-getsid s p* \equiv *hook-task-getsid s p*

definition *security-task-getsecid* :: 's \Rightarrow Task \Rightarrow u32 \Rightarrow ('s, unit) *nondet-monad*

where *security-task-getsecid s c secid'* \equiv *do*

secid \leftarrow *return 0*;

hook-task-getsecid s c secid

od

definition *security-task-setnice* :: 's \Rightarrow Task \Rightarrow int \Rightarrow ('s, int) *nondet-monad*

where *security-task-setnice s p nice* \equiv *hook-task-setnice s p nice*

definition *security-task-setioprio* :: 's \Rightarrow Task \Rightarrow int \Rightarrow ('s, int) *nondet-monad*

where *security-task-setioprio s p ioprio* \equiv *hook-task-setioprio s p ioprio*

definition *security-task-getioprio* :: 's \Rightarrow Task \Rightarrow ('s, int) *nondet-monad*

where *security-task-getioprio s p* \equiv *hook-task-getioprio s p*

definition *security-task-prlimit* :: 's \Rightarrow Cred \Rightarrow Cred \Rightarrow nat \Rightarrow ('s, int) *nondet-monad*

where *security-task-prlimit s cred' tcred flgs* \equiv *hook-task-prlimit s cred' tcred flgs*

definition *security-task-setrlimit* :: 's \Rightarrow Task \Rightarrow nat \Rightarrow rlimit \Rightarrow ('s, int) *nondet-monad*

where *security-task-setrlimit s p res new-rlim* \equiv *hook-task-setrlimit s p res new-rlim*

definition *security-task-setscheduler* :: 's \Rightarrow Task \Rightarrow ('s, int) *nondet-monad*

where *security-task-setscheduler s p* \equiv *hook-task-setscheduler s p*

definition *security-task-getscheduler* :: 's \Rightarrow Task \Rightarrow ('s, int) *nondet-monad*

where *security-task-getscheduler s p* \equiv *hook-task-getscheduler s p*

definition *security-task-movememory* :: 's \Rightarrow Task \Rightarrow ('s, int) *nondet-monad*

where *security-task-movememory s p* \equiv *hook-task-movememory s p*

definition *security-task-kill* :: 's \Rightarrow Task \Rightarrow siginfo \Rightarrow int \Rightarrow Cred option \Rightarrow ('s, int) *nondet-monad*

where *security-task-kill s t info sig c* \equiv *hook-task-kill s t info sig c*

definition *security-task-prctl* :: 's \Rightarrow int \Rightarrow nat \Rightarrow nat \Rightarrow nat \Rightarrow nat \Rightarrow ('s, int)

nondet-monad

where *security-task-prctl* *s opt arg2 arg3 arg4 arg5* \equiv *do*
 rc \leftarrow *return*($-ENOSYS$);
 thisrc \leftarrow *hook-task-prctl* *s opt arg2 arg3 arg4 arg5*;
 if thisrc \neq ($-ENOSYS$)
 then
 return thisrc
 else
 return rc
od

definition *security-task-to-inode* :: '*s* \Rightarrow *Task* \Rightarrow *inode* \Rightarrow ('*s*, *unit*) *nondet-monad*
where *security-task-to-inode* *s p inode* \equiv *hook-task-to-inode* *s p inode*

definition *security-ipc-permission* :: '*s* \Rightarrow *kern-ipc-perm* \Rightarrow *nat* \Rightarrow ('*s*, *int*) *nondet-monad*

where *security-ipc-permission* *s ipcp flg* \equiv *hook-ipc-permission* *s ipcp flg*

definition *security-ipc-getsecid* :: '*s* \Rightarrow *kern-ipc-perm* \Rightarrow *u32* \Rightarrow ('*s*, *unit*) *nondet-monad*

where *security-ipc-getsecid* *s ipcp secid'* \equiv *do*

secid \leftarrow *return* 0;
 hook-ipc-getsecid *s ipcp secid*
od

definition *security-msg-msg-alloc* :: '*s* \Rightarrow *msg-msg* \Rightarrow ('*s*, *int*) *nondet-monad*

where *security-msg-msg-alloc* *s msg* \equiv *hook-msg-msg-alloc* *s msg*

definition *security-msg-msg-free* :: '*s* \Rightarrow *msg-msg* \Rightarrow ('*s*, *unit*) *nondet-monad*

where *security-msg-msg-free* *s msg* \equiv *hook-msg-msg-free* *s msg*

definition *security-msg-queue-alloc* :: '*s* \Rightarrow *kern-ipc-perm* \Rightarrow ('*s*, *int*) *nondet-monad*

where *security-msg-queue-alloc* *s msq* \equiv *hook-msg-queue-alloc* *s msq*

definition *security-msg-queue-free* :: '*s* \Rightarrow *kern-ipc-perm* \Rightarrow ('*s*, *unit*) *nondet-monad*

where *security-msg-queue-free* *s msq* \equiv *hook-msg-queue-free* *s msq*

definition *security-msg-queue-associate* :: '*s* \Rightarrow *kern-ipc-perm* \Rightarrow *int* \Rightarrow ('*s*, *int*) *nondet-monad*

where *security-msg-queue-associate* *s msq msqflg* \equiv *hook-msg-queue-associate* *s msq msqflg*

definition *security-msg-queue-msgctl* :: '*s* \Rightarrow *kern-ipc-perm* \Rightarrow *IPC-CMD* \Rightarrow ('*s*, *int*) *nondet-monad*

where *security-msg-queue-msgctl* *s msq cmd* \equiv *hook-msg-queue-msgctl* *s msq cmd*

definition *security-msg-queue-msgsnd* :: '*s* \Rightarrow *kern-ipc-perm* \Rightarrow *msg-msg* \Rightarrow *int* \Rightarrow ('*s*, *int*) *nondet-monad*

where *security-msg-queue-msgsnd* *s msq msg msqflg* \equiv *hook-msg-queue-msgsnd* *s msq msg msqflg*

definition *security-msg-queue-msgrcv* :: *'s* \Rightarrow *kern-ipc-perm* \Rightarrow *msg-msg* \Rightarrow *Task* \Rightarrow *int*

\Rightarrow *int* \Rightarrow (*'s*, *int*) *nondet-monad*

where *security-msg-queue-msgrcv* *s msq msg target type m* \equiv
hook-msg-queue-msgrcv *s msq msg target type m*

definition *security-shm-alloc* :: *'s* \Rightarrow *kern-ipc-perm* \Rightarrow (*'s*, *int*) *nondet-monad*
where *security-shm-alloc* *s shp* \equiv *hook-shm-alloc* *s shp*

definition *security-shm-free* :: *'s* \Rightarrow *kern-ipc-perm* \Rightarrow (*'s*, *unit*) *nondet-monad*
where *security-shm-free* *s shp* \equiv *hook-shm-free* *s shp*

definition *security-shm-associate* :: *'s* \Rightarrow *kern-ipc-perm* \Rightarrow *int* \Rightarrow (*'s*, *int*) *nondet-monad*
where *security-shm-associate* *s shp shmflg* \equiv *hook-shm-associate* *s shp shmflg*

definition *security-shm-shmctl* :: *'s* \Rightarrow *kern-ipc-perm* \Rightarrow *IPC-CMD* \Rightarrow (*'s*, *int*) *nondet-monad*
where *security-shm-shmctl* *s shp cmd* \equiv *hook-shm-shmctl* *s shp cmd*

definition *security-shm-shmat* :: *'s* \Rightarrow *kern-ipc-perm* \Rightarrow *string* \Rightarrow *int* \Rightarrow (*'s*, *int*) *nondet-monad*
where *security-shm-shmat* *s shp shmaddr shmflg* \equiv *hook-shm-shmat* *s shp shmaddr shmflg*

definition *security-sem-alloc* :: *'s* \Rightarrow *kern-ipc-perm* \Rightarrow (*'s*, *int*) *nondet-monad*
where *security-sem-alloc* *s sma* \equiv *hook-sem-alloc* *s sma*

definition *security-sem-free* :: *'s* \Rightarrow *kern-ipc-perm* \Rightarrow (*'s*, *unit*) *nondet-monad*
where *security-sem-free* *s sma* \equiv *hook-sem-free* *s sma*

definition *security-sem-associate* :: *'s* \Rightarrow *kern-ipc-perm* \Rightarrow *int* \Rightarrow (*'s*, *int*) *nondet-monad*
where *security-sem-associate* *s sma semflg* \equiv *hook-sem-associate* *s sma semflg*

definition *security-sem-semctl* :: *'s* \Rightarrow *kern-ipc-perm* \Rightarrow *IPC-CMD* \Rightarrow (*'s*, *int*) *nondet-monad*
where *security-sem-semctl* *s sma cmd* \equiv *hook-sem-semctl* *s sma cmd*

definition *security-sem-semop* :: *'s* \Rightarrow *kern-ipc-perm* \Rightarrow *sembuf* \Rightarrow *nat* \Rightarrow *int* \Rightarrow (*'s*, *int*) *nondet-monad*
where *security-sem-semop* *s sma sops nsops alter* \equiv *hook-sem-semop* *s sma sops nsops alter*

definition *file-inode* :: *Files* \Rightarrow *inode*
where *file-inode* *f* \equiv *f-inode* *f*

definition *fsnotify-perm* :: 's \Rightarrow Files \Rightarrow mask \Rightarrow ('s, int) nondet-monad
where *fsnotify-perm* s file m \equiv do
 path \leftarrow return(f-path file);
 inode \leftarrow return(file-inode file);
 return(0)
od

definition *security-file-permission* :: 's \Rightarrow Files \Rightarrow int \Rightarrow ('s, int) nondet-monad
where *security-file-permission* s file mask' \equiv do
 ret \leftarrow hook-file-permission s file mask' ;
 if ret \neq 0 then return ret
 else *fsnotify-perm* s file mask'
od

definition *security-file-alloc* :: 's \Rightarrow Files \Rightarrow ('s, int) nondet-monad
where *security-file-alloc* s file \equiv hook-file-alloc s file

definition *security-file-free* :: 's \Rightarrow Files \Rightarrow ('s, unit) nondet-monad
where *security-file-free* s file \equiv hook-file-free s file

definition *security-file-ioctl* :: 's \Rightarrow Files \Rightarrow IOC-DIR \Rightarrow nat \Rightarrow ('s, int) nondet-monad
where *security-file-ioctl* s file cmd arg \equiv hook-file-ioctl s file cmd arg

definition *mmap-capabilities* :: Files \Rightarrow nat
where *mmap-capabilities* f \equiv 0

definition *mmap-prot-mmu* :: Files \Rightarrow nat \Rightarrow nat
where *mmap-prot-mmu* f prot \equiv
 if CONFIG-MMU then
 let
 fop = f-op f;
 caps = *mmap-capabilities* f
 in
 if fop = fop-mmap-capabilities then
 if \neg ((caps AND NOMMU-MAP-EXEC) \neq 0)
 then prot
 else
 nat(bitOR (int prot) PROT-EXEC)
 else
 nat(bitOR (int prot) PROT-EXEC)
 else
 nat(bitOR (int prot) PROT-EXEC)

definition *mmap-prot* :: 's \Rightarrow Files option \Rightarrow nat \Rightarrow ('s, int) nondet-monad
where *mmap-prot* s file' prot \equiv do
 flag1 \leftarrow return(((int prot) AND (bitOR PROT-READ PROT-EXEC))
 \neq PROT-READ);

```

    personality ← return(personality (the((k-task s)(current s))));
    flag2 ← return((personality AND READ-IMPLIES-EXEC) = 0);
    rc ← (if flag1 ∨ flag2 then
        return (int prot)
    else if file' ≠ None
        then return(bitOR (int prot) PROT-EXEC)
        else if ¬(path-noexec (f-path (the file'))) then
            return(int (mmap-prot-mmu (the file') prot))
        else
            return((int prot))
    );
    return rc
od

```

definition *ima-file-mmap* :: *Files* ⇒ *nat* ⇒ *int*
where *ima-file-mmap* file prot ≡ 0

definition *security-mmap-file* :: '*s*' ⇒ *Files* ⇒ *nat* ⇒ *nat* ⇒ ('*s*', *int*) *nondet-monad*

```

where security-mmap-file s file prot flgs ≡ do
    mprot ← mmap-prot s (Some file) flgs;
    ret ← hook-mmap-file s (Some file) prot (nat mprot) flgs;
    if ret ≠ 0 then
        return ret
    else
        return(ima-file-mmap file prot)
od

```

definition *security-mmap-addr* :: '*s*' ⇒ *nat* ⇒ ('*s*', *int*) *nondet-monad*
where *security-mmap-addr* s addr ≡ hook-mmap-addr s addr

definition *security-file-mprotect* :: '*s*' ⇒ *vm-area-struct* ⇒ *nat* ⇒ *nat* ⇒ ('*s*', *int*) *nondet-monad*
where *security-file-mprotect* s vma reqprot prot ≡ hook-file-mprotect s vma reqprot prot

definition *security-file-lock* :: '*s*' ⇒ *Files* ⇒ *nat* ⇒ ('*s*', *int*) *nondet-monad*
where *security-file-lock* s file cmd ≡ hook-file-lock s file cmd

definition *security-file-fcntl* :: '*s*' ⇒ *Files* ⇒ *nat* ⇒ *nat* ⇒ ('*s*', *int*) *nondet-monad*
where *security-file-fcntl* s file cmd arg ≡ hook-file-fcntl s file cmd arg

definition *security-file-set-fowner* :: '*s*' ⇒ *Files* ⇒ ('*s*', *unit*) *nondet-monad*
where *security-file-set-fowner* s file ≡ hook-file-set-fowner s file

definition *security-file-send-sigiotask* :: '*s*' ⇒ *Task* ⇒ *fown-struct* ⇒ *int* ⇒ ('*s*', *int*) *nondet-monad*
where *security-file-send-sigiotask* s tsk' fown sig ≡ hook-file-send-sigiotask s tsk' fown sig

definition *security-file-receive* :: 's \Rightarrow Files \Rightarrow ('s, int) nondet-monad
where *security-file-receive* s file \equiv hook-file-receive s file

definition *security-file-open* :: 's \Rightarrow Files \Rightarrow ('s, int) nondet-monad
where *security-file-open* s file \equiv do
 ret \leftarrow (hook-file-open s file);
 rc \leftarrow (if ret \neq 0 then
 return ret
 else (fsnotify-perm s file MAY-OPEN));
 return rc
od

definition *security-kernel-act-as* :: 's \Rightarrow Cred \Rightarrow u32 \Rightarrow ('s, int) nondet-monad
where *security-kernel-act-as* s new secid' \equiv hook-kernel-act-as s new secid'

definition *security-kernel-create-files-as* :: 's \Rightarrow Cred \Rightarrow inode \Rightarrow ('s, int) nondet-monad
where *security-kernel-create-files-as* s new inode \equiv hook-kernel-create-files-as s new inode

definition *integrity-kernel-module-request* :: 's \Rightarrow string \Rightarrow ('s, int) nondet-monad
where *integrity-kernel-module-request* s name \equiv return 0

definition *security-kernel-module-request* :: 's \Rightarrow string \Rightarrow ('s, int) nondet-monad
where *security-kernel-module-request* s name \equiv do
 ret \leftarrow hook-kernel-module-request s name;
 if ret \neq 0 then
 return ret
 else
 integrity-kernel-module-request s name
od

definition *ima-load-data* :: 's \Rightarrow kernel-load-data-id \Rightarrow ('s, int) nondet-monad
where *ima-load-data* s kid \equiv return 0

definition *security-kernel-load-data* :: 's \Rightarrow kernel-load-data-id \Rightarrow ('s, int) nondet-monad
where *security-kernel-load-data* s kid \equiv do
 ret \leftarrow hook-kernel-load-data s kid;
 if ret \neq 0 then
 return ret
 else
 ima-load-data s kid
od

definition *ima-read-file* :: 's \Rightarrow Files \Rightarrow kernel-read-file-id \Rightarrow ('s, int) nondet-monad
where *ima-read-file* s file kid \equiv return 0

definition *security-kernel-read-file* :: 's \Rightarrow Files \Rightarrow kernel-read-file-id
 \Rightarrow ('s, int) nondet-monad

where *security-kernel-read-file* s file kid \equiv do
 ret \leftarrow hook-kernel-read-file s file kid;
 if ret \neq 0 then
 return ret
 else
 ima-read-file s file kid
od

definition *ima-post-read-file* :: 's \Rightarrow Files \Rightarrow string \Rightarrow nat \Rightarrow kernel-read-file-id
 \Rightarrow ('s, int) nondet-monad

where *ima-post-read-file* s file buf size' kid \equiv return 0

definition *security-kernel-post-read-file* :: 's \Rightarrow Files \Rightarrow string \Rightarrow nat \Rightarrow kernel-read-file-id

\Rightarrow ('s, int) nondet-monad
where *security-kernel-post-read-file* s file buf size' kid \equiv do
 ret \leftarrow hook-kernel-post-read-file s file buf size' kid;
 if ret \neq 0 then
 return ret
 else
 ima-post-read-file s file buf size' kid
od

definition *security-dentry-init-security* :: 's \Rightarrow dentry \Rightarrow mode \Rightarrow string \Rightarrow string
 \Rightarrow int

\Rightarrow ('s, int) nondet-monad
where *security-dentry-init-security* s dentry m name ctx xtlen \equiv
hook-dentry-init-security s dentry m name ctx xtlen

definition *security-dentry-create-files-as* :: 's \Rightarrow dentry \Rightarrow mode \Rightarrow string \Rightarrow Cred
 \Rightarrow Cred

\Rightarrow ('s, int) nondet-monad
where *security-dentry-create-files-as* s dentry m name old new \equiv
hook-dentry-create-files-as s dentry m name old new

definition *security-d-instantiate* :: 's \Rightarrow dentry \Rightarrow inode \Rightarrow ('s, unit) nondet-monad

where *security-d-instantiate* s dentry inode \equiv
if unlikely (IS-PRIVATE (inode)) then
return ()
else
hook-d-instantiate s dentry (Some inode)

definition *security-getprocattr* :: 's \Rightarrow Task \Rightarrow string \Rightarrow string \Rightarrow ('s, int)
nondet-monad

where *security-getprocattr* s p name value \equiv hook-getprocattr s p name value

definition *security-setprocattr* :: 's ⇒ string ⇒ string ⇒ int ⇒ ('s, int) nondet-monad
where *security-setprocattr* s name value size' ≡ *hook-setprocattr* s name value size'

definition *security-netlink-send* :: 's ⇒ sock ⇒ sk-buff ⇒ ('s, int) nondet-monad
where *security-netlink-send* s sk' skb ≡ *hook-netlink-send* s sk' skb

definition *security-ismaclabel* :: 's ⇒ xattr ⇒ ('s, int) nondet-monad
where *security-ismaclabel* s name ≡ *hook-ismaclabel* s name

definition *security-secid-to-secctx* :: 's ⇒ u32 ⇒ string ⇒ u32 ⇒ ('s, int) nondet-monad
where *security-secid-to-secctx* s secid' secdata seclen ≡
hook-secid-to-secctx s secid' secdata seclen

definition *security-secctx-to-secid* :: 's ⇒ string ⇒ u32 ⇒ u32 ⇒ ('s, int) nondet-monad
where *security-secctx-to-secid* s secdata seclen secid' ≡ do
secid ← return 0;
hook-secctx-to-secid s secdata seclen secid
od

definition *security-release-secctx* :: 's ⇒ string ⇒ u32 ⇒ ('s, unit) nondet-monad
where *security-release-secctx* s secdata seclen ≡ *hook-release-secctx* s secdata seclen

definition *security-unix-stream-connect* :: 's ⇒ sock ⇒ sock ⇒ sock ⇒ ('s, int) nondet-monad
where *security-unix-stream-connect* s sock other newsk ≡ *hook-unix-stream-connect* s sock other newsk

definition *security-unix-may-send* :: 's ⇒ socket ⇒ socket ⇒ ('s, int) nondet-monad
where *security-unix-may-send* s sock other ≡ *hook-unix-may-send* s sock other

definition *security-socket-create* :: 's ⇒ Sk-Family ⇒ int ⇒ int ⇒ int ⇒ ('s, int) nondet-monad
where *security-socket-create* s family type pro kern ≡ *hook-socket-create* s family type pro kern

definition *security-socket-post-create* :: 's ⇒ socket ⇒ Sk-Family ⇒ int ⇒ int ⇒ int ⇒ ('s, int) nondet-monad
where *security-socket-post-create* s sock family type pro kern ≡
hook-socket-post-create s sock family type pro kern

definition *security-socket-socketpair* :: 's ⇒ socket ⇒ socket ⇒ ('s, int) nondet-monad
where *security-socket-socketpair* s socka sockb ≡ *hook-socket-socketpair* s socka sockb

definition *security-socket-bind* :: 's ⇒ socket ⇒ sockaddr ⇒ int ⇒ ('s, int)

nondet-monad

where *security-socket-bind* *s sock address addrlen* \equiv *hook-socket-bind* *s sock address addrlen*

definition *security-socket-connect* :: *'s* \Rightarrow *socket* \Rightarrow *sockaddr* \Rightarrow *int* \Rightarrow (*'s*, *int*) *nondet-monad*

where *security-socket-connect* *s sock address addrlen* \equiv *hook-socket-connect* *s sock address addrlen*

definition *security-socket-listen* :: *'s* \Rightarrow *socket* \Rightarrow *int* \Rightarrow (*'s*, *int*) *nondet-monad*
where *security-socket-listen* *s sock backlog* \equiv *hook-socket-listen* *s sock backlog*

definition *security-socket-accept* :: *'s* \Rightarrow *socket* \Rightarrow *socket* \Rightarrow (*'s*, *int*) *nondet-monad*
where *security-socket-accept* *s sock newsock* \equiv *hook-socket-accept* *s sock newsock*

definition *security-socket-sendmsg* :: *'s* \Rightarrow *socket* \Rightarrow *msghdr* \Rightarrow *int* \Rightarrow (*'s*, *int*) *nondet-monad*

where *security-socket-sendmsg* *s sock msg size'* \equiv *hook-socket-sendmsg* *s sock msg size'*

definition *security-socket-recvmsg* :: *'s* \Rightarrow *socket* \Rightarrow *msghdr* \Rightarrow *int* \Rightarrow *int* \Rightarrow (*'s*, *int*) *nondet-monad*

where *security-socket-recvmsg* *s sock msg size' flgs* \equiv *hook-socket-recvmsg* *s sock msg size' flgs*

definition *security-socket-getsockname* :: *'s* \Rightarrow *socket* \Rightarrow (*'s*, *int*) *nondet-monad*
where *security-socket-getsockname* *s sock* \equiv *hook-socket-getsockname* *s sock*

definition *security-socket-getpeername* :: *'s* \Rightarrow *socket* \Rightarrow (*'s*, *int*) *nondet-monad*
where *security-socket-getpeername* *s sock* \equiv *hook-socket-getpeername* *s sock*

definition *security-socket-getsockopt* :: *'s* \Rightarrow *socket* \Rightarrow *int* \Rightarrow *int* \Rightarrow (*'s*, *int*) *nondet-monad*

where *security-socket-getsockopt* *s sock level' optname* \equiv
hook-socket-getsockopt *s sock level' optname*

definition *security-socket-setsockopt* :: *'s* \Rightarrow *socket* \Rightarrow *int* \Rightarrow *int* \Rightarrow (*'s*, *int*) *nondet-monad*

where *security-socket-setsockopt* *s sock level' optname* \equiv
hook-socket-setsockopt *s sock level' optname*

definition *security-socket-shutdown* :: *'s* \Rightarrow *socket* \Rightarrow *int* \Rightarrow (*'s*, *int*) *nondet-monad*
where *security-socket-shutdown* *s sock how* \equiv *hook-socket-shutdown* *s sock how*

definition *security-sock-rcv-skb* :: *'s* \Rightarrow *sock* \Rightarrow *sk-buff* \Rightarrow (*'s*, *int*) *nondet-monad*
where *security-sock-rcv-skb* *s sock skb* \equiv *hook-sock-rcv-skb* *s sock skb*

definition *security-socket-getpeersec-stream* :: *'s* \Rightarrow *socket* \Rightarrow *string* \Rightarrow *int* \Rightarrow *nat*

$\Rightarrow ('s, \text{int}) \text{ nondet-monad}$

where $\text{security-socket-getpeersec-stream } s \text{ sock optval optlen len}' \equiv$
 $\text{hook-socket-getpeersec-stream } s \text{ sock optval optlen len}'$

definition $\text{security-socket-getpeersec-dgram} :: 's \Rightarrow \text{socket} \Rightarrow \text{sk-buff option} \Rightarrow \text{u32}$
 $\Rightarrow ('s, \text{int}) \text{ nondet-monad}$

where $\text{security-socket-getpeersec-dgram } s \text{ sock skb secid}' \equiv$
 $\text{hook-socket-getpeersec-dgram } s \text{ sock skb secid}'$

definition $\text{security-sk-alloc} :: 's \Rightarrow \text{sock} \Rightarrow \text{int} \Rightarrow \text{gfp-t} \Rightarrow ('s, \text{int}) \text{ nondet-monad}$
where $\text{security-sk-alloc } s \text{ sk}' \text{ family priority} \equiv \text{hook-sk-alloc } s \text{ sk}' \text{ family priority}$

definition $\text{security-sk-free} :: 's \Rightarrow \text{sock} \Rightarrow ('s, \text{unit}) \text{ nondet-monad}$
where $\text{security-sk-free } s \text{ sock} \equiv \text{hook-sk-free } s \text{ sock}$

definition $\text{security-sk-clone} :: 's \Rightarrow \text{sock} \Rightarrow \text{sock} \Rightarrow ('s, \text{unit}) \text{ nondet-monad}$
where $\text{security-sk-clone } s \text{ sk}' \text{ newsk} \equiv \text{hook-sk-clone } s \text{ sk}' \text{ newsk}$

definition $\text{security-sk-classify-flow} :: 's \Rightarrow \text{sock} \Rightarrow \text{flowi} \Rightarrow ('s, \text{unit}) \text{ nondet-monad}$
where $\text{security-sk-classify-flow } s \text{ sock}' \text{ fl} \equiv \text{hook-sk-classify-flow } s \text{ sock}' \text{ fl}$

definition $\text{security-req-classify-flow} :: 's \Rightarrow \text{request-sock} \Rightarrow \text{flowi} \Rightarrow ('s, \text{unit})$
 nondet-monad
where $\text{security-req-classify-flow } s \text{ req fl} \equiv \text{hook-req-classify-flow } s \text{ req fl}$

definition $\text{security-sock-graft} :: 's \Rightarrow \text{sock} \Rightarrow \text{socket} \Rightarrow ('s, \text{unit}) \text{ nondet-monad}$
where $\text{security-sock-graft } s \text{ sk}' \text{ parent}' \equiv \text{hook-sock-graft } s \text{ sk}' \text{ parent}'$

definition $\text{security-inet-conn-request} :: 's \Rightarrow \text{sock} \Rightarrow \text{sk-buff} \Rightarrow \text{request-sock}$
 $\Rightarrow ('s, \text{int}) \text{ nondet-monad}$
where $\text{security-inet-conn-request } s \text{ sk}' \text{ skb req} \equiv \text{hook-inet-conn-request } s \text{ sk}' \text{ skb req}$

definition $\text{security-inet-csk-clone} :: 's \Rightarrow \text{sock} \Rightarrow \text{request-sock} \Rightarrow ('s, \text{unit})$
 nondet-monad
where $\text{security-inet-csk-clone } s \text{ newsk req} \equiv \text{hook-inet-csk-clone } s \text{ newsk req}$

definition $\text{security-inet-conn-established} :: 's \Rightarrow \text{sock} \Rightarrow \text{sk-buff} \Rightarrow ('s, \text{unit})$
 nondet-monad
where $\text{security-inet-conn-established } s \text{ sk}' \text{ skb} \equiv \text{hook-inet-conn-established } s \text{ sk}' \text{ skb}$

definition $\text{security-secmark-relabel-packet} :: 's \Rightarrow \text{u32} \Rightarrow ('s, \text{int}) \text{ nondet-monad}$
where $\text{security-secmark-relabel-packet } s \text{ secid}' \equiv \text{hook-secmark-relabel-packet } s \text{ secid}'$

definition $\text{security-secmark-refcount-inc} :: 's \Rightarrow ('s, \text{unit}) \text{ nondet-monad}$
where $\text{security-secmark-refcount-inc } s \equiv \text{hook-secmark-refcount-inc } s$

definition *security-secmark-refcount-dec* :: 's \Rightarrow ('s, unit) nondet-monad
where *security-secmark-refcount-dec* s \equiv *hook-secmark-refcount-dec* s

definition *security-tun-dev-alloc-security* :: 's \Rightarrow 'h \Rightarrow ('s, int) nondet-monad
where *security-tun-dev-alloc-security* s *security* \equiv *hook-tun-dev-alloc-security* s *security*

definition *security-tun-dev-free-security* :: 's \Rightarrow 'h \Rightarrow ('s, unit) nondet-monad
where *security-tun-dev-free-security* s *security* \equiv *hook-tun-dev-free-security* s *security*

definition *security-tun-dev-create* :: 's \Rightarrow ('s, int) nondet-monad
where *security-tun-dev-create* s \equiv *hook-tun-dev-create* s

definition *security-tun-dev-attach-queue* :: 's \Rightarrow 'h \Rightarrow ('s, int) nondet-monad
where *security-tun-dev-attach-queue* s *security* \equiv *hook-tun-dev-attach-queue* s *security*

definition *security-tun-dev-attach* :: 's \Rightarrow sock \Rightarrow 'h \Rightarrow ('s, int) nondet-monad
where *security-tun-dev-attach* s sk' *security* \equiv *hook-tun-dev-attach* s sk' *security*

definition *security-tun-dev-open* :: 's \Rightarrow 'h \Rightarrow ('s, int) nondet-monad
where *security-tun-dev-open* s *security* \equiv *hook-tun-dev-open* s *security*

definition *security-sctp-assoc-request* :: 's \Rightarrow sctp-endpoint \Rightarrow sk-buff \Rightarrow ('s, int) nondet-monad
where *security-sctp-assoc-request* s ep skb \equiv *hook-sctp-assoc-request* s ep skb

definition *security-sctp-bind-connect* :: 's \Rightarrow sock \Rightarrow int \Rightarrow sockaddr \Rightarrow int \Rightarrow ('s, int) nondet-monad
where *security-sctp-bind-connect* s sk' optname address addrlen \equiv *hook-sctp-bind-connect* s sk' optname address addrlen

definition *security-sctp-sk-clone* :: 's \Rightarrow sctp-endpoint \Rightarrow sock \Rightarrow sock \Rightarrow ('s, unit) nondet-monad
where *security-sctp-sk-clone* s ep sk' newsk \equiv *hook-sctp-sk-clone* s ep sk' newsk

definition *security-ib-pkey-access* :: 's \Rightarrow 'i \Rightarrow nat \Rightarrow nat \Rightarrow ('s, int) nondet-monad
where *security-ib-pkey-access* s sec subnet-prefix pkey \equiv *hook-ib-pkey-access* s sec subnet-prefix pkey

definition *security-ib-endport-manage-subnet* :: 's \Rightarrow 'i \Rightarrow string \Rightarrow nat \Rightarrow ('s, int) nondet-monad
where *security-ib-endport-manage-subnet* s sec dev-name port-num \equiv *hook-ib-endport-manage-subnet* s sec dev-name port-num

definition *security-ib-alloc-security* :: 's \Rightarrow 'i list \Rightarrow ('s, int) nondet-monad

where *security-ib-alloc-security* *s sec* \equiv *hook-ib-alloc-security* *s sec*

definition *security-ib-free-security* $:: 's \Rightarrow 'i \text{ list} \Rightarrow ('s, \text{unit}) \text{ nondet-monad}$
where *security-ib-free-security* *s sec* \equiv *hook-ib-free-security* *s sec*

definition *security-path-unlink* $:: 's \Rightarrow \text{path} \Rightarrow \text{dentry} \Rightarrow ('s, \text{int}) \text{ nondet-monad}$
where *security-path-unlink* *s dir dentry* \equiv
 if unlikely (*IS-PRIVATE* (*the*(*d-backing-inode* *s* (*p-dentry* *dir*))))
 then
 return 0
 else
 hook-path-unlink *s dir dentry*

definition *security-path-mkdir* $:: 's \Rightarrow \text{path} \Rightarrow \text{dentry} \Rightarrow \text{nat} \Rightarrow ('s, \text{int}) \text{ nondet-monad}$
where *security-path-mkdir* *s dir dentry m* \equiv
 if unlikely (*IS-PRIVATE* (*the*(*d-backing-inode* *s* (*p-dentry* *dir*))))
 then
 return 0
 else
 hook-path-mkdir *s dir dentry m*

definition *security-path-rmdir* $:: 's \Rightarrow \text{path} \Rightarrow \text{dentry} \Rightarrow ('s, \text{int}) \text{ nondet-monad}$
where *security-path-rmdir* *s dir dentry* \equiv
 if unlikely (*IS-PRIVATE* (*the*(*d-backing-inode* *s* (*p-dentry* *dir*))))
 then
 return 0
 else
 hook-path-rmdir *s dir dentry*

definition *security-path-mknod* $:: 's \Rightarrow \text{path} \Rightarrow \text{dentry} \Rightarrow \text{nat} \Rightarrow \text{nat} \Rightarrow ('s, \text{int}) \text{ nondet-monad}$
where *security-path-mknod* *s dir dentry m dev* \equiv
 if unlikely (*IS-PRIVATE* (*the*(*d-backing-inode* *s* (*p-dentry* *dir*))))
 then return 0
 else hook-path-mknod *s dir dentry m dev*

definition *security-path-truncate* $:: 's \Rightarrow \text{path} \Rightarrow ('s, \text{int}) \text{ nondet-monad}$
where *security-path-truncate* *s dir* \equiv
 if unlikely (*IS-PRIVATE* (*the*(*d-backing-inode* *s* (*p-dentry* *dir*))))
 then
 return 0
 else
 hook-path-truncate *s dir*

definition *security-path-symlink* $:: 's \Rightarrow \text{path} \Rightarrow \text{dentry} \Rightarrow \text{string} \Rightarrow ('s, \text{int}) \text{ nondet-monad}$
where *security-path-symlink* *s dir dentry old-name* \equiv
 if unlikely (*IS-PRIVATE* (*the*(*d-backing-inode* *s* (*p-dentry* *dir*))))

```

then
  return 0
else
  hook-path-symlink s dir dentry old-name

```

definition *security-path-link* :: 's \Rightarrow dentry \Rightarrow path \Rightarrow dentry \Rightarrow ('s, int) nondet-monad
where *security-path-link* s old-dentry new-dir new-dentry \equiv
 if unlikely (IS-PRIVATE (the(d-backing-inode s (old-dentry))))
 then
 return 0
 else
 hook-path-link s old-dentry new-dir new-dentry

definition *security-path-rename* :: 's \Rightarrow path \Rightarrow dentry \Rightarrow path \Rightarrow dentry \Rightarrow nat
 \Rightarrow ('s, int) nondet-monad
where *security-path-rename* s old-dir old-dentry new-dir new-dentry flgs \equiv
 if unlikely (IS-PRIVATE (the(d-backing-inode s old-dentry))) \vee
 ((d-is-positive new-dentry) \wedge IS-PRIVATE (the(d-backing-inode s
 new-dentry))) \neq 0)
 then
 return 0
 else if (((int flgs) AND RENAME-EXCHANGE) \neq 0) then
 do
 err \leftarrow (hook-path-rename s new-dir new-dentry old-dir old-dentry);
 if err \neq 0 then
 return err
 else
 (hook-path-rename s old-dir old-dentry new-dir new-dentry)
 od
 else
 (hook-path-rename s old-dir old-dentry new-dir new-dentry)

definition *security-path-chmod* :: 's \Rightarrow path \Rightarrow nat \Rightarrow ('s, int) nondet-monad
where *security-path-chmod* s path m \equiv
 if unlikely (IS-PRIVATE (the(d-backing-inode s (p-dentry path))))
 then
 return 0
 else
 hook-path-chmod s path m

definition *security-path-chown* :: 's \Rightarrow path \Rightarrow kuid-t \Rightarrow kgid-t \Rightarrow ('s, int) nondet-monad
where *security-path-chown* s path uid' gid' \equiv
 if unlikely (IS-PRIVATE (the(d-backing-inode s (p-dentry path))))
 then return 0
 else hook-path-chown s path uid' gid'

definition *security-path-chroot* :: 's \Rightarrow path \Rightarrow ('s, int) nondet-monad
where *security-path-chroot* s path \equiv hook-path-chroot s path

definition *security-key-alloc* :: 's \Rightarrow key \Rightarrow Cred \Rightarrow nat \Rightarrow ('s, int) nondet-monad
where *security-key-alloc* s key' c flgs \equiv *hook-key-alloc* s key' c flgs

definition *security-key-free* :: 's \Rightarrow key \Rightarrow ('s, unit) nondet-monad
where *security-key-free* s key' \equiv *hook-key-free* s key'

definition *security-key-permission* :: 's \Rightarrow key-ref-t \Rightarrow Cred \Rightarrow nat \Rightarrow ('s, int) nondet-monad
where *security-key-permission* s key-ref c perm \equiv *hook-key-permission* s key-ref c perm

definition *security-key-getsecurity* :: 's \Rightarrow key \Rightarrow string \Rightarrow ('s, int) nondet-monad
where *security-key-getsecurity* s key' buffer \equiv *hook-key-getsecurity* s key' buffer

definition *security-audit-rule-init* :: 's \Rightarrow nat \Rightarrow enum-audit \Rightarrow string \Rightarrow string \Rightarrow ('s, int) nondet-monad
where *security-audit-rule-init* s field op rulestr lsmrule \equiv *hook-audit-rule-init* s field op rulestr lsmrule

definition *security-audit-rule-known* :: 's \Rightarrow audit-krule \Rightarrow ('s, int) nondet-monad
where *security-audit-rule-known* s krule \equiv *hook-audit-rule-known* s krule

definition *security-audit-rule-match* :: 's \Rightarrow nat \Rightarrow nat \Rightarrow enum-audit \Rightarrow string \Rightarrow audit-context \Rightarrow ('s, int) nondet-monad
where *security-audit-rule-match* s secid' field op lsmrule actx \equiv *hook-audit-rule-match* s secid' field op lsmrule actx

definition *security-audit-rule-free* :: 's \Rightarrow string \Rightarrow ('s, unit) nondet-monad
where *security-audit-rule-free* s lsmrule \equiv *hook-audit-rule-free* s lsmrule

definition *security-xfrm-policy-alloc* :: 's \Rightarrow xfrm-sec-ctx \Rightarrow xfrm-user-sec-ctx \Rightarrow gfp-t \Rightarrow ('s, int) nondet-monad
where *security-xfrm-policy-alloc* s ctxp sec-ctx gfp' \equiv *hook-xfrm-policy-alloc* s ctxp sec-ctx gfp'

definition *security-xfrm-policy-clone* :: 's \Rightarrow xfrm-sec-ctx \Rightarrow xfrm-user-sec-ctx \Rightarrow ('s, int) nondet-monad
where *security-xfrm-policy-clone* s old-ctx new-ctxp \equiv *hook-xfrm-policy-clone* s old-ctx new-ctxp

definition *security-xfrm-policy-free* :: 's \Rightarrow xfrm-sec-ctx \Rightarrow ('s, unit) nondet-monad
where *security-xfrm-policy-free* s ctx \equiv hook-xfrm-policy-free s ctx

definition *security-xfrm-policy-delete* :: 's \Rightarrow xfrm-sec-ctx \Rightarrow ('s, int) nondet-monad
where *security-xfrm-policy-delete* s ctx \equiv hook-xfrm-policy-delete s ctx

definition *security-xfrm-state-alloc* :: 's \Rightarrow xfrm-state \Rightarrow xfrm-sec-ctx \Rightarrow ('s, int) nondet-monad
where *security-xfrm-state-alloc* s x sec-ctx \equiv hook-xfrm-state-alloc s x sec-ctx

definition *security-xfrm-state-alloc-acquire* :: 's \Rightarrow xfrm-state \Rightarrow xfrm-sec-ctx \Rightarrow u32 \Rightarrow ('s, int) nondet-monad
where *security-xfrm-state-alloc-acquire* s x plosec secid' \equiv hook-xfrm-state-alloc-acquire s x plosec secid'

definition *security-xfrm-state-delete* :: 's \Rightarrow xfrm-state \Rightarrow ('s, int) nondet-monad
where *security-xfrm-state-delete* s x \equiv hook-xfrm-state-delete s x

definition *security-xfrm-state-free* :: 's \Rightarrow xfrm-state \Rightarrow ('s, unit) nondet-monad
where *security-xfrm-state-free* s x \equiv hook-xfrm-state-free s x

definition *security-xfrm-policy-lookup* :: 's \Rightarrow xfrm-sec-ctx \Rightarrow u32 \Rightarrow u8 \Rightarrow ('s, int) nondet-monad
where *security-xfrm-policy-lookup* s ctx fl-secid dir \equiv hook-xfrm-policy-lookup s ctx fl-secid dir

definition *security-xfrm-state-pol-flow-match* :: 's \Rightarrow xfrm-state \Rightarrow xfrm-policy \Rightarrow flowi \Rightarrow ('s, int) nondet-monad
where *security-xfrm-state-pol-flow-match* s x xp fl \equiv return 1

definition *security-xfrm-decode-session* :: 's \Rightarrow sk-buff \Rightarrow u32 \Rightarrow ('s, int) nondet-monad
where *security-xfrm-decode-session* s skb secid' \equiv hook-xfrm-decode-session s skb 1

definition *security-skb-classify-flow* :: 's \Rightarrow sk-buff \Rightarrow flowi \Rightarrow ('s, unit) nondet-monad
where *security-skb-classify-flow* s skb fl \equiv hook-skb-classify-flow s skb fl

definition *security-bpf* :: 's \Rightarrow int \Rightarrow bpf-attr \Rightarrow nat \Rightarrow ('s, int) nondet-monad
where *security-bpf* s cmd attr' size' \equiv hook-bpf s cmd attr' size'

definition *security-bpf-map* :: 's \Rightarrow bpf-map \Rightarrow mode \Rightarrow ('s, int) nondet-monad
where *security-bpf-map* s bmap fmode \equiv hook-bpf-map s bmap fmode

definition *security-bpf-prog* :: 's \Rightarrow bpf-prog \Rightarrow ('s, int) nondet-monad
where *security-bpf-prog* s prog \equiv hook-bpf-prog s prog

definition *security-bpf-map-alloc* :: 's \Rightarrow bpf-map \Rightarrow ('s, int) nondet-monad
where *security-bpf-map-alloc* s bmap \equiv *hook-bpf-map-alloc* s bmap

definition *security-bpf-map-free* :: 's \Rightarrow bpf-map \Rightarrow ('s, unit) nondet-monad
where *security-bpf-map-free* s bmap \equiv *hook-bpf-map-free* s bmap

definition *security-bpf-prog-alloc* :: 's \Rightarrow bpf-prog-aux \Rightarrow ('s, int) nondet-monad
where *security-bpf-prog-alloc* s aux' \equiv *hook-bpf-prog-alloc* s aux'

definition *security-bpf-prog-free* :: 's \Rightarrow bpf-prog-aux \Rightarrow ('s, unit) nondet-monad
where *security-bpf-prog-free* s aux' \equiv *hook-bpf-prog-free* s aux'

27.3 func lemma

27.4 binder state lemma

lemma *security-binder-set-context-mgr-notchgstate* :
 $\bigwedge sa . \{\lambda s . s = sa\}$ *security-binder-set-context-mgr* sa mgr $\{\lambda r s . s = sa\}$
using *security-binder-set-context-mgr-def* *stb-binder-set-context-mgr*
by *simp*

lemma *security-binder-transaction-notchgstate* :
 $\bigwedge sa . \{\lambda s . s = sa\}$ *security-binder-transaction* sa from to $\{\lambda r s . s = sa\}$
using *security-binder-transaction-def* *stb-binder-transaction*
by *simp*

lemma *security-binder-transfer-binder-notchgstate* :
 $\bigwedge sa . \{\lambda s . s = sa\}$ *security-binder-transfer-binder* s from to $\{\lambda r s . s = sa\}$
using *security-binder-transfer-binder-def* *stb-binder-transfer-binder*
by *simp*

lemma *security-binder-transfer-file-notchgstate* :
 $\bigwedge sa . \{\lambda s . s = sa\}$ *security-binder-transfer-file* s from to file $\{\lambda r s . s = sa\}$
using *security-binder-transfer-file-def* *stb-binder-transfer-file*
by *simp*

27.5 ptrace state lemma

lemma *security-pttrace-access-check-notchgstate* :
 $\bigwedge sa . \{\lambda s . s = sa\}$ *security-pttrace-access-check* s child m $\{\lambda r s . s = sa\}$
using *security-pttrace-access-check-def* *stb-pttrace-access-check*
by *simp*

lemma *security-pttrace-traceme-notchgstate* :
 $\bigwedge sa . \{\lambda s . s = sa\}$ *security-pttrace-traceme* s parent' $\{\lambda r s . s = sa\}$
using *security-pttrace-traceme-def* *stb-pttrace-traceme*
by *simp*

27.6 file state lemma

lemma *security-file-permission-notchgstate* :

$\bigwedge sa . \{\lambda s . s = sa\}$ *security-file-permission* *sa file mask'* $\{\lambda r s . s = sa\}$
unfolding *security-file-permission-def fsnotify-perm-def*
apply (*simp add: bind-def return-def split-def valid-def*)
apply *wsimp*
using *stb-file-permission*
apply *auto*
apply (*simp add: valid-def split-def*)
by *fastforce*

lemma *security-file-ioctl-notchgstate* :

$\bigwedge sa \text{ file} . \{\lambda s . s = sa\}$ *security-file-ioctl* *sa file cmd arg* $\{\lambda r s . s = sa\}$
unfolding *security-file-ioctl-def*
using *stb-file-ioctl*
apply *auto[1]*
done

lemma *security-mmap-addr-notchgstate* :

$\bigwedge sa . \{\lambda s . s = sa\}$ *security-mmap-addr* *sa addr* $\{\lambda r s . s = sa\}$
unfolding *security-mmap-addr-def*
using *stb-mmap-addr*
by *simp*

lemma *security-mmap-file-notchgstate* :

$\bigwedge sa . \{\lambda s . s = sa\}$ *security-mmap-file* *sa file prot flgs* $\{\lambda r s . s = sa\}$
unfolding *security-mmap-file-def bind-def ima-file-mmap-def*
apply *wsimp*
apply(*simp add: valid-def mmap-prot-def return-def bind-def*)
apply(*simp add: PROT-READ-def PROT-EXEC-def return-def READ-IMPLIES-EXEC-def*)
using *stb-mmap-file*
apply (*simp add: valid-def split-def*)
apply *auto[1]*
by(*simp add: return-def*) +

lemma *security-file-mprotect-notchgstate* :

$\bigwedge sa . \{\lambda s . s = sa\}$ *security-file-mprotect* *sa vma reqprot prot* $\{\lambda r s . s = sa\}$
unfolding *security-file-mprotect-def*
using *stb-file-mprotect*
by *simp*

lemma *security-file-lock-notchgstate* :

$\bigwedge sa . \{\lambda s . s = sa\}$ *security-file-lock* *sa file cmd* $\{\lambda r s . s = sa\}$
unfolding *security-file-lock-def*
using *stb-file-lock*
by *simp*

lemma *security-file-fcntl-notchgstate* :

$\bigwedge sa . \{ \lambda s . s = sa \}$ *security-file-fcntl* *sa file cmd arg* $\{ \lambda r s . s = sa \}$
unfolding *security-file-fcntl-def*
using *stb-file-fcntl*
by *simp*

lemma *security-file-send-sigiotask-notchgstate* :
 $\bigwedge sa . \{ \lambda s . s = sa \}$ *security-file-send-sigiotask* *sa tsk' fown sig* $\{ \lambda r s . s = sa \}$
unfolding *security-file-send-sigiotask-def*
using *stb-file-send-sigiotask*
by *simp*

lemma *security-file-receive-notchgstate* :
 $\bigwedge sa . \{ \lambda s . s = sa \}$ *security-file-receive* *sa file* $\{ \lambda r s . s = sa \}$
unfolding *security-file-receive-def*
using *stb-file-receive*
by *simp*

lemma *security-file-open-notchgstate* :
 $\bigwedge sa . \{ \lambda s . s = sa \}$ *security-file-open* *sa file* $\{ \lambda r s . s = sa \}$
unfolding *security-file-open-def return-def bind-def valid-def*
apply *auto*
using *stb-file-open*
apply(*simp add: valid-def*)
apply *simp*
using *fsnotify-perm-def* **apply** *auto*
by (*smt case-prodD fst-conv return-def singleton-iff*)

lemma *do-ioctl-state*:
 $\bigwedge sa . \{ \lambda s . s = sa \}$ *security-file-ioctl* *sa file cmd arg* $\{ \lambda r s . s = sa \} \wedge$
 $\det (security-file-ioctl\ sa\ file\ cmd\ arg) \longrightarrow$
 $snd (the-run-state (security-file-ioctl\ sa\ file\ cmd\ arg)\ sa) = sa$
apply(*simp add: valid-def*)
apply *auto*[1]
using *all-not-in-conv det-def fst-conv insert-not-empty*
 $the-run-state-def\ the-run-state-det\ prod.case-eq-if$
by *smt*

27.7 cap state lemma

lemma *security-capget-notchgstate* :
 $\bigwedge sa . \{ \lambda s . s = sa \}$ *security-capget* *s target effective inheritable permitted* $\{ \lambda r s .$
 $s = sa \}$
unfolding *security-capget-def*
using *stb-capget*
by *simp*

lemma *security-capset-notchgstate* :
 $\bigwedge sa . \{ \lambda s . s = sa \}$ *security-capset* *s new old effective inheritable permitted*
 $\{ \lambda r s . s = sa \}$

```

unfolding security-capset-def
using stb-capset
by simp

lemma security-capable-notchgstate :
   $\bigwedge sa . \{ \lambda s . s = sa \} \text{ security-capable } s \ c \ ns \ cap$ 
   $\{ \lambda r \ s . s = sa \}$ 
unfolding security-capable-def
using stb-capable
by simp

lemma security-capable-noaudit-notchgstate :
   $\bigwedge sa . \{ \lambda s . s = sa \} \text{ security-capable-noaudit } s \ c \ ns \ cap$ 
   $\{ \lambda r \ s . s = sa \}$ 
unfolding security-capable-noaudit-def
using stb-capable-noaudit
by simp

lemma security-quotactl-notchgstate :
   $\bigwedge sa . \{ \lambda s . s = sa \} \text{ security-quotactl } s \ cmds \ t \ id' \ sb$ 
   $\{ \lambda r \ s . s = sa \}$ 
unfolding security-quotactl-def
using stb-quotactl
by simp

lemma security-quota-on-notchgstate :
   $\bigwedge sa . \{ \lambda s . s = sa \} \text{ security-quota-on } s \ dentry$ 
   $\{ \lambda r \ s . s = sa \}$ 
unfolding security-quota-on-def
using stb-quota-on
by simp

lemma security-settime64-notchgstate :
   $\bigwedge sa . \{ \lambda s . s = sa \} \text{ security-settime64 } s \ ts \ tz$ 
   $\{ \lambda r \ s . s = sa \}$ 
unfolding security-settime64-def
using stb-settime64
by simp

lemma security-vm-enough-memory-mm-notchgstate :
   $\bigwedge sa . \{ \lambda s . s = sa \} \text{ security-vm-enough-memory-mm } s \ mm' \ pages$ 
   $\{ \lambda r \ s . s = sa \}$ 
unfolding security-vm-enough-memory-mm-def bind-def
apply auto
using stb-vm-enough-memory-mm
by (simp add: valid-def return-def split-def)

lemma security-syslog-notchgstate :
   $\bigwedge sa . \{ \lambda s . s = sa \} \text{ security-syslog } s \ type$ 

```

$\{\lambda r s. s = sa\}$
unfolding *security-syslog-def*
using *stb-syslog*
by *simp*

lemma *security-bprm-set-creds-notchgstate* :
 $\bigwedge sa. \{\lambda s. s = sa\} \text{ security-bprm-set-creds } s \text{ bprm}$
 $\{\lambda r s. s = sa\}$
unfolding *security-bprm-set-creds-def*
using *stb-bprm-set-creds*
by *simp*

lemma *security-bprm-check-notchgstate* :
 $\bigwedge sa. \{\lambda s. s = sa\} \text{ security-bprm-check } s \text{ bprm}$
 $\{\lambda r s. s = sa\}$
unfolding *security-bprm-check-def*
using *stb-bprm-check*
by (*simp add: valid-def return-def bind-def split-def*)

lemma *security-bprm-committing-creds-notchgstate* :
 $\bigwedge sa. \{\lambda s. s = sa\} \text{ security-bprm-committing-creds } s \text{ bprm}$
 $\{\lambda r s. \text{True}\}$
unfolding *security-bprm-committing-creds-def*
using *stb-bprm-committing-creds*
by *simp*

lemma *security-bprm-committed-creds-notchgstate* :
 $\bigwedge sa. \{\lambda s. s = sa\} \text{ security-bprm-committed-creds } s \text{ bprm}$
 $\{\lambda r s. \text{True}\}$
unfolding *security-bprm-committed-creds-def*
using *stb-bprm-committed-creds*
by *simp*

27.8 sb state lemma

lemma *security-sb-alloc-notchgstate* :
 $\bigwedge sa. \{\lambda s. s = sa\} \text{ security-sb-alloc } s \text{ sb}$
 $\{\lambda r s. r = 0 \vee r = -ENOMEM\}$
unfolding *security-sb-alloc-def*
using *stb-sb-alloc-hook*
by *simp*

lemma *security-sb-free-r* :
 $\bigwedge sa. \{\lambda s. s = sa\} \text{ security-sb-free } s \text{ sb}$
 $\{\lambda r s. r = \text{unit}\}$
unfolding *security-sb-free-def*
using *stb-sb-free*
by *simp*

lemma *security-sb-copy-data-notchgstate* :
 $\bigwedge sa . \{ \lambda s . s = sa \} \text{ security-sb-copy-data } s \text{ orig copy}$
 $\{ \lambda r s . s = sa \}$
unfolding *security-sb-copy-data-def*
using *stb-sb-copy-data*
by(*simp add: valid-def return-def bind-def split-def*)

lemma *security-sb-remount-notchgstate* :
 $\bigwedge sa . \{ \lambda s . s = sa \} \text{ security-sb-remount } s \text{ sb data}$
 $\{ \lambda r s . s = sa \}$
unfolding *security-sb-remount-def*
using *stb-sb-remount*
by(*simp add: valid-def*)

lemma *security-sb-kern-mount-notchgstate* :
 $\bigwedge sa . \{ \lambda s . s = sa \} \text{ security-sb-kern-mount } s \text{ sb flgs data}$
 $\{ \lambda r s . s = sa \}$
unfolding *security-sb-kern-mount-def*
using *stb-sb-kern-mount*
by(*simp add: valid-def*)

lemma *security-sb-show-options-notchgstate* :
 $\bigwedge sa . \{ \lambda s . s = sa \} \text{ security-sb-show-options } s \text{ m sb}$
 $\{ \lambda r s . s = sa \}$
unfolding *security-sb-show-options-def*
using *stb-sb-show-options*
by(*simp add: valid-def*)

lemma *security-sb-statfs-notchgstate* :
 $\bigwedge sa . \{ \lambda s . s = sa \} \text{ security-sb-statfs } s \text{ dentry}$
 $\{ \lambda r s . s = sa \}$
unfolding *security-sb-statfs-def*
using *stb-sb-statfs*
by(*simp add: valid-def*)

lemma *security-sb-mount-notchgstate* :
 $\bigwedge sa . \{ \lambda s . s = sa \} \text{ security-sb-mount } s \text{ dev-name path type flgs data}$
 $\{ \lambda r s . s = sa \}$
unfolding *security-sb-mount-def*
using *stb-sb-mount*
by *simp*

lemma *security-sb-umount-notchgstate* :
 $\bigwedge sa . \{ \lambda s . s = sa \} \text{ security-sb-umount } s \text{ vmnt flgs}$
 $\{ \lambda r s . s = sa \}$
unfolding *security-sb-umount-def*
using *stb-sb-umount*

by *simp*

lemma *security-sb-pivotroot-notchgstate* :
 $\bigwedge sa . \{\lambda s . s = sa\} \text{security-sb-pivotroot } s \text{ old-path new-path}$
 $\{\lambda r s . s = sa\}$
unfolding *security-sb-pivotroot-def*
using *stb-sb-pivotroot*
by *simp*

lemma *security-sb-set-mnt-opts-notchgstate* :
 $\bigwedge sa . \{\lambda s . s = sa\} \text{security-sb-set-mnt-opts } s \text{ sb opt kern-flags set-kern-flags}$
 $\{\lambda r s . s = sa\}$
unfolding *security-sb-set-mnt-opts-def*
using *stb-sb-set-mnt-opts*
by *simp*

end

27.9 init lsm hooks func

definition *security-binder-set-context-mgr'*:: 's \Rightarrow Task \Rightarrow ('s, int) nondet-monad
where *security-binder-set-context-mgr' s mgr* \equiv do
 $r \leftarrow (\text{return } 0);$
 $\text{return}(r)$
od

lemma *binder-set-context-mgr'*:: $\{\lambda s . \text{True}\} \text{security-binder-set-context-mgr' } s \text{ t } \{\lambda r$
 $s . r = 0\}$
apply(*simp add :security-binder-set-context-mgr'-def*)
apply *upsimp*
done

definition *security-binder-transaction'*:: 's \Rightarrow Task \Rightarrow Task \Rightarrow ('s, int) nondet-monad
where *security-binder-transaction' s from to* \equiv do
 $r \leftarrow (\text{return } 0);$
 $\text{return}(r)$
od

definition *security-binder-transfer-binder'*:: 's \Rightarrow Task \Rightarrow Task \Rightarrow ('s, int) nondet-monad
where *security-binder-transfer-binder' s from to* \equiv do
 $r \leftarrow (\text{return } 0);$
 $\text{return}(r)$
od

definition *security-binder-transfer-file'*:: 's \Rightarrow Task \Rightarrow Task \Rightarrow Files \Rightarrow ('s, int)
nondet-monad
where *security-binder-transfer-file' s from to file* \equiv do
 $r \leftarrow (\text{return } 0);$
 $\text{return}(r)$

od

definition *security-syslog'* :: 's ⇒ int ⇒ ('s, int) nondet-monad
where *security-syslog' s type'* ≡ do
 r ← (return 0);
 return(*r*)
od

definition *security-bprm-check'* :: 's ⇒ linux-binprm ⇒ ('s, int) nondet-monad
where *security-bprm-check' s bprm* ≡ do
 r ← (return 0);
 return(*r*)
od

definition *security-bprm-committing-creds'* :: 's ⇒ linux-binprm ⇒ ('s, unit) nondet-monad
where *security-bprm-committing-creds' s bprm* ≡ return()

definition *security-bprm-committed-creds'* :: 's ⇒ linux-binprm ⇒ ('s, unit) nondet-monad
where *security-bprm-committed-creds' s bprm* ≡ do
 r ← (return bprm);
 return()
od

definition *security-sb-alloc'* :: 's ⇒ super-block ⇒ ('s, int) nondet-monad
where *security-sb-alloc' s sb* ≡ do
 r ← (return 0);
 return(*r*)
od

definition *security-sb-free'* :: 's ⇒ super-block ⇒ ('s, unit) nondet-monad
where *security-sb-free' s sb* ≡ return()

definition *security-sb-copy-data'* :: 's ⇒ string ⇒ string ⇒ ('s, int) nondet-monad
where *security-sb-copy-data' s orig copy* ≡ do
 r ← (return 0);
 return(*r*)
od

definition *security-sb-remount'* :: 's ⇒ super-block ⇒ Void ⇒ ('s, int) nondet-monad
where *security-sb-remount' s sb data* ≡ do
 r ← (return 0);
 return(*r*)
od

definition *security-sb-kern-mount'* :: 's ⇒ super-block ⇒ int ⇒ Void ⇒ ('s, int) nondet-monad

where *security-sb-kern-mount'* *s sb flag data* \equiv *do*
 r \leftarrow (*return* 0);
 return(*r*)
od

definition *security-sb-show-options'* $:: 's \Rightarrow \text{seq-file} \Rightarrow \text{super-block} \Rightarrow ('s, \text{int}) \text{ nondet-monad}$
where *security-sb-show-options'* *s m sb* \equiv *do*
 r \leftarrow (*return* 0);
 return(*r*)
od

definition *security-sb-stats'* $:: 's \Rightarrow \text{dentry} \Rightarrow ('s, \text{int}) \text{ nondet-monad}$
where *security-sb-stats'* *s dentry* \equiv *do*
 r \leftarrow (*return* 0);
 return(*r*)
od

definition *security-sb-mount'* $:: 's \Rightarrow \text{string} \Rightarrow \text{path} \Rightarrow \text{string} \Rightarrow \text{int} \Rightarrow \text{Void} \Rightarrow ('s, \text{int}) \text{ nondet-monad}$
where *security-sb-mount'* *s devname path type flag data* \equiv *do*
 r \leftarrow (*return* 0);
 return(*r*)
od

definition *security-sb-umount'* $:: 's \Rightarrow \text{vfsmount} \Rightarrow \text{int} \Rightarrow ('s, \text{int}) \text{ nondet-monad}$
where *security-sb-umount'* *s mnt' flag* \equiv *do*
 r \leftarrow (*return* 0);
 return(*r*)
od

definition *security-sb-pivotroot'* $:: 's \Rightarrow \text{path} \Rightarrow \text{path} \Rightarrow ('s, \text{int}) \text{ nondet-monad}$
where *security-sb-pivotroot'* *s old new* \equiv *do*
 r \leftarrow (*return* 0);
 return(*r*)
od

definition *security-sb-set-mnt-opts'* $:: 's \Rightarrow \text{super-block} \Rightarrow \text{opts} \Rightarrow \text{int} \Rightarrow \text{int} \Rightarrow ('s, \text{int}) \text{ nondet-monad}$
where *security-sb-set-mnt-opts'* *s sb opts' kflags set-kflags* \equiv *do*
 r \leftarrow (*return* 0);
 return(*r*)
od

definition *security-sb-clone-mnt-opts'* $:: 's \Rightarrow \text{super-block} \Rightarrow \text{super-block} \Rightarrow \text{int} \Rightarrow \text{int} \Rightarrow ('s, \text{int}) \text{ nondet-monad}$
where *security-sb-clone-mnt-opts'* *s oldsb newsb kflags set-kflags* \equiv *do*
 r \leftarrow (*return* 0);
 return(*r*)
od

definition *security-sb-parse-opts-str'* :: 's ⇒ string ⇒ opts ⇒ ('s, int) nondet-monad
where *security-sb-parse-opts-str'* s options opt ≡ do
 r ← (return 0);
 return(r)
od

definition *security-task-alloc'* :: 's ⇒ Task ⇒ nat ⇒ ('s, int) nondet-monad
where *security-task-alloc'* s p f ≡ do
 r ← (return 0);
 return(r)
od

definition *security-task-free'* :: 's ⇒ Task ⇒ ('s, unit) nondet-monad
where *security-task-free'* s p ≡ return()

definition *security-task-fix-setuid'* :: 's ⇒ Cred ⇒ Cred ⇒ int ⇒ ('s, int) nondet-monad
where *security-task-fix-setuid'* s new old f ≡ do
 r ← (return 0);
 return(r)
od

definition *security-task-prlimit'* :: 's ⇒ Cred ⇒ Cred ⇒ int ⇒ ('s, int) nondet-monad
where *security-task-prlimit'* s c tc f ≡ do
 r ← (return 0);
 return(r)
od

definition *security-task-setrlimit'* :: 's ⇒ Task ⇒ nat ⇒ rlimit ⇒ ('s, int) nondet-monad
where *security-task-setrlimit'* s p r f ≡ do
 r ← (return 0);
 return(r)
od

definition *security-task-prctl'* :: 's ⇒ int ⇒ nat ⇒ nat ⇒ nat ⇒ nat ⇒ ('s, int) nondet-monad
where *security-task-prctl'* s op arg2 arg3 arg4 arg5 ≡ do
 r ← (return 0);
 return(r)
od

lemma *l-security-sb-alloc*: {λs. True} security-sb-alloc' s sb {λr s. r = 0}
apply(simp add :security-sb-alloc'-def)
apply wpsimp
done

lemma *l-security-sb-copy-data*: {λs. True} security-sb-copy-data' s orig copy {λr
s. r = 0}
apply(simp add :security-sb-copy-data'-def)
apply wpsimp
done

lemma *l-security-sb-set-mnt-opts*: $\{\lambda s. \text{True}\}$ *security-sb-set-mnt-opts'* *s sb opts'*
kflags set-kflags $\{\lambda r s. r = 0\}$
apply (*simp add :security-sb-set-mnt-opts'-def*)
apply *wpsimp*
done

definition *security-capget'* :: *'s* \Rightarrow *Task* \Rightarrow *kct* \Rightarrow *kct* \Rightarrow *kct* \Rightarrow (*'s*, *int*) *nondet-monad*
where *security-capget' s target effective inheritable permitted* \equiv *return 0*

definition *security-capset'* :: *'s* \Rightarrow *Cred* \Rightarrow *Cred* \Rightarrow *kct* \Rightarrow *kct* \Rightarrow *kct* \Rightarrow (*'s*, *int*) *nondet-monad*
where *security-capset' s new old effective inheritable permitted* \equiv *return 0*

definition *security-capable'* :: *'s* \Rightarrow *Cred* \Rightarrow *ns* \Rightarrow *cap* \Rightarrow (*'s*, *int*) *nondet-monad*
where *security-capable' s c ns cap* \equiv *return 0*

definition *security-capable-noaudit'* :: *'s* \Rightarrow *Cred* \Rightarrow *ns* \Rightarrow *cap* \Rightarrow (*'s*, *int*) *nondet-monad*
where *security-capable-noaudit' s c ns cap* \equiv *return 0*

definition *security-quotactl'* :: *'s* \Rightarrow *int* \Rightarrow *int* \Rightarrow *int* \Rightarrow *super-block option* \Rightarrow (*'s*, *int*) *nondet-monad*
where *security-quotactl' s cmds t id' sb* \equiv *return 0*

definition *security-quota-on'* :: *'s* \Rightarrow *dentry* \Rightarrow (*'s*, *int*) *nondet-monad*
where *security-quota-on' s dentry* \equiv *return 0*

definition *security-settime64'* :: *'s* \Rightarrow *ts* \Rightarrow *tz option* \Rightarrow (*'s*, *int*) *nondet-monad*
where *security-settime64' s ts tz* \equiv *return 0*

definition *security-vm-enough-memory-mm'* :: *'s* \Rightarrow *mm* \Rightarrow *pages* \Rightarrow (*'s*, *int*) *nondet-monad*
where *security-vm-enough-memory-mm' s mm' pages* \equiv *return 0*

definition *security-bprm-set-creds'* :: *'s* \Rightarrow *linux-binprm* \Rightarrow (*'s*, *int*) *nondet-monad*
where *security-bprm-set-creds' s bprm* \equiv *return 0*

definition *security-dentry-init-security'* :: *'s* \Rightarrow *dentry* \Rightarrow *mode* \Rightarrow *string* \Rightarrow *string* \Rightarrow *int* \Rightarrow (*'s*, *int*) *nondet-monad*
where *security-dentry-init-security' s dentry m name ctx txlen* \equiv *return 0*

definition *security-dentry-create-files-as'* :: *'s* \Rightarrow *dentry* \Rightarrow *mode* \Rightarrow *string* \Rightarrow *Cred* \Rightarrow *Cred* \Rightarrow (*'s*, *int*) *nondet-monad*
where *security-dentry-create-files-as' s dentry m name old new* \equiv *return 0*

definition *security-d-instantiate'* :: *'s* \Rightarrow *dentry* \Rightarrow *inode* \Rightarrow (*'s*, *unit*) *nondet-monad*
where *security-d-instantiate' s dentry inode* \equiv *return ()*

definition *security-getprocattr'* :: 's \Rightarrow Task \Rightarrow string \Rightarrow string \Rightarrow ('s, int) nondet-monad
where *security-getprocattr'* s p name value \equiv return 0

definition *security-setprocattr'* :: 's \Rightarrow string \Rightarrow string \Rightarrow int \Rightarrow ('s, int) nondet-monad
where *security-setprocattr'* s name value size' \equiv return 0

definition *security-inode-alloc'* :: 's \Rightarrow inode \Rightarrow ('s, int) nondet-monad
where *security-inode-alloc'* s inode \equiv return 0

definition *security-inode-free'* :: 's \Rightarrow inode \Rightarrow ('s, unit) nondet-monad
where *security-inode-free'* s inode \equiv return()

definition *security-inode-init-security'* :: 's \Rightarrow inode \Rightarrow inode \Rightarrow string \Rightarrow string \Rightarrow string \Rightarrow int \Rightarrow ('s, int) nondet-monad
where *security-inode-init-security'* s inode dir qstr name value len' \equiv return 0

definition *security-old-inode-init-security'* :: 's \Rightarrow inode \Rightarrow inode \Rightarrow qstr \Rightarrow string \Rightarrow string \Rightarrow int \Rightarrow ('s, int) nondet-monad
where *security-old-inode-init-security'* s inode dir qstr name value len' \equiv return 0

definition *security-inode-create'* :: 's \Rightarrow inode \Rightarrow dentry \Rightarrow mode \Rightarrow ('s, int) nondet-monad
where *security-inode-create'* s dir dentry m \equiv return 0

definition *security-inode-link'* :: 's \Rightarrow dentry \Rightarrow inode \Rightarrow dentry \Rightarrow ('s, int) nondet-monad
where *security-inode-link'* s old-dentry dir new-dentry \equiv return 0

definition *security-inode-unlink'* :: 's \Rightarrow inode \Rightarrow dentry \Rightarrow ('s, int) nondet-monad
where *security-inode-unlink'* s dir dentry \equiv return 0

definition *security-inode-symlink'* :: 's \Rightarrow inode \Rightarrow dentry \Rightarrow string \Rightarrow ('s, int) nondet-monad
where *security-inode-symlink'* s dir dentry old-name \equiv return 0

definition *security-inode-mkdir'* :: 's \Rightarrow inode \Rightarrow dentry \Rightarrow mode \Rightarrow ('s, int) nondet-monad
where *security-inode-mkdir'* s dir dentry m \equiv return 0

definition *security-inode-rmdir'* :: 's \Rightarrow inode \Rightarrow dentry \Rightarrow ('s, int) nondet-monad
where *security-inode-rmdir'* s dir dentry \equiv return 0

definition *security-inode-mknod'* :: 's \Rightarrow inode \Rightarrow dentry \Rightarrow mode \Rightarrow dev-t \Rightarrow ('s, int) nondet-monad
where *security-inode-mknod'* s dir dentry m dev \equiv return 0

definition *security-inode-rename'* :: 's ⇒ inode ⇒ dentry ⇒ inode ⇒ dentry ⇒ ('s, int) nondet-monad
where *security-inode-rename'* s old-dir old-dentry new-dir new-dentry ≡ return 0

definition *security-inode-readlink'* :: 's ⇒ dentry ⇒ ('s, int) nondet-monad
where *security-inode-readlink'* s dentry ≡ return 0

definition *security-inode-follow-link'* :: 's ⇒ dentry ⇒ inode ⇒ bool ⇒ ('s, int) nondet-monad
where *security-inode-follow-link'* s dentry inode rcu' ≡ return 0

definition *security-inode-permission'* :: 's ⇒ inode ⇒ mask ⇒ ('s, int) nondet-monad
where *security-inode-permission'* s inode m ≡ return 0

definition *security-inode-setattr'* :: 's ⇒ dentry ⇒ iattr ⇒ ('s, int) nondet-monad
where *security-inode-setattr'* s dentry attr' ≡ return 0

definition *security-inode-getattr'* :: 's ⇒ path ⇒ ('s, int) nondet-monad
where *security-inode-getattr'* s path ≡ return 0

definition *security-inode-setxattr'* :: 's ⇒ dentry ⇒ xattr ⇒ string ⇒ int ⇒ flags ⇒ ('s, int) nondet-monad
where *security-inode-setxattr'* s dentry name value size' flgs ≡ return 0

definition *evm-inode-post-setxattr'* :: 's ⇒ dentry ⇒ xattr ⇒ string ⇒ int ⇒ ('s, unit) nondet-monad
where *evm-inode-post-setxattr'* s d x value flg ≡ return ()

definition *security-inode-post-setxattr'* :: 's ⇒ dentry ⇒ xattr ⇒ string ⇒ int ⇒ flags ⇒ ('s, unit) nondet-monad
where *security-inode-post-setxattr'* s dentry name value size' flgs ≡ return ()

definition *security-inode-getxattr'* :: 's ⇒ dentry ⇒ xattr ⇒ ('s, int) nondet-monad
where *security-inode-getxattr'* s dentry name ≡ return 0

definition *security-inode-listxattr'* :: 's ⇒ dentry ⇒ ('s, int) nondet-monad
where *security-inode-listxattr'* s dentry ≡ return 0

definition *security-inode-removexattr'* :: 's ⇒ dentry ⇒ xattr ⇒ ('s, int) nondet-monad

where *security-inode-removeattr' s dentry name* \equiv *return 0*

definition *security-inode-need-killpriv' :: 's \Rightarrow dentry \Rightarrow ('s, int) nondet-monad*
where *security-inode-need-killpriv' s dentry* \equiv *return 0*

definition *security-inode-killpriv' :: 's \Rightarrow dentry \Rightarrow ('s, int) nondet-monad*
where *security-inode-killpriv' s dentry* \equiv *return 0*

definition *security-inode-getsecurity' :: 's \Rightarrow inode \Rightarrow xattr \Rightarrow Void \Rightarrow bool \Rightarrow ('s, int) nondet-monad*
where *security-inode-getsecurity' s inode name buffer alloc* \equiv *return (-EOPNOTSUPP)*

definition *security-inode-setsecurity' :: 's \Rightarrow inode \Rightarrow xattr \Rightarrow Void \Rightarrow nat \Rightarrow int \Rightarrow ('s, int) nondet-monad*
where *security-inode-setsecurity' s inode name value size' flgs* \equiv *return (-EOPNOTSUPP)*

definition *security-inode-listsecurity' :: 's \Rightarrow inode \Rightarrow Void \Rightarrow int \Rightarrow ('s, int) nondet-monad*
where *security-inode-listsecurity' s inode buffer bsize* \equiv *return 0*

definition *security-inode-getsecid' :: 's \Rightarrow inode \Rightarrow u32 \Rightarrow ('s, unit) nondet-monad*
where *security-inode-getsecid' s inode secid'* \equiv *return()*

definition *security-inode-copy-up' :: 's \Rightarrow dentry \Rightarrow Cred option \Rightarrow ('s, int) nondet-monad*
where *security-inode-copy-up' s src new* \equiv *return 0*

definition *security-inode-copy-up-xattr' :: 's \Rightarrow string \Rightarrow ('s, int) nondet-monad*
where *security-inode-copy-up-xattr' s name* \equiv *return 0*

definition *security-inode-invalidate-secctx' :: 's \Rightarrow inode \Rightarrow ('s, unit) nondet-monad*
where *security-inode-invalidate-secctx' s inode* \equiv *return ()*

definition *security-inode-notifysecctx' :: 's \Rightarrow inode \Rightarrow string \Rightarrow u32 \Rightarrow ('s, int) nondet-monad*
where *security-inode-notifysecctx' s inode ctx ctxlen* \equiv *return 0*

definition *security-inode-setsecctx' :: 's \Rightarrow dentry \Rightarrow string \Rightarrow u32 \Rightarrow ('s, int) nondet-monad*
where *security-inode-setsecctx' s dentry ctx ctxlen* \equiv *return 0*

definition *security-inode-getsecctx' :: 's \Rightarrow inode \Rightarrow string \Rightarrow u32 \Rightarrow ('s, int) nondet-monad*
where *security-inode-getsecctx' s dentry ctx ctxlen* \equiv *return 0*

definition *security-file-permission' :: 's \Rightarrow Files \Rightarrow int \Rightarrow ('s, int) nondet-monad*
where *security-file-permission' s file mask'* \equiv *return 0*

definition *security-file-alloc'* :: 's \Rightarrow Files \Rightarrow ('s, int) nondet-monad
where *security-file-alloc'* s file \equiv return 0

definition *security-file-free'* :: 's \Rightarrow Files \Rightarrow ('s, unit) nondet-monad
where *security-file-free'* s file \equiv return ()

definition *security-file-iocctl'* :: 's \Rightarrow Files \Rightarrow IOC-DIR \Rightarrow nat \Rightarrow ('s, int) nondet-monad
where *security-file-iocctl'* s file cmd arg \equiv return 0

definition *security-mmap-file'* :: 's \Rightarrow Files option \Rightarrow nat \Rightarrow nat \Rightarrow ('s, int) nondet-monad
where *security-mmap-file'* s file prot flgs \equiv return 0

definition *security-mmap-addr'* :: 's \Rightarrow nat \Rightarrow ('s, int) nondet-monad
where *security-mmap-addr'* s addr \equiv return 0

definition *security-file-mprotect'* :: 's \Rightarrow vm-area-struct \Rightarrow nat \Rightarrow nat \Rightarrow ('s, int) nondet-monad
where *security-file-mprotect'* s vma reqprot prot \equiv return 0

definition *security-file-lock'* :: 's \Rightarrow Files \Rightarrow nat \Rightarrow ('s, int) nondet-monad
where *security-file-lock'* s file cmd \equiv return 0

definition *security-file-fcntl'* :: 's \Rightarrow Files \Rightarrow nat \Rightarrow nat \Rightarrow ('s, int) nondet-monad
where *security-file-fcntl'* s file cmd arg \equiv return 0

definition *security-file-set-fowner'* :: 's \Rightarrow Files \Rightarrow ('s, unit) nondet-monad
where *security-file-set-fowner'* s file \equiv return ()

definition *security-file-send-sigiotask'* :: 's \Rightarrow Task \Rightarrow fown-struct \Rightarrow int \Rightarrow ('s, int) nondet-monad
where *security-file-send-sigiotask'* s tsk' fown sig \equiv return 0

definition *security-file-receive'* :: 's \Rightarrow Files \Rightarrow ('s, int) nondet-monad
where *security-file-receive'* s file \equiv return 0

definition *security-file-open'* :: 's \Rightarrow Files \Rightarrow ('s, int) nondet-monad
where *security-file-open'* s file \equiv return 0

definition *security-kernel-act-as'* :: 's \Rightarrow Cred \Rightarrow u32 \Rightarrow ('s, int) nondet-monad
where *security-kernel-act-as'* s new secid' \equiv return 0

definition *security-kernel-create-files-as'* :: 's \Rightarrow Cred \Rightarrow inode \Rightarrow ('s, int) nondet-monad
where *security-kernel-create-files-as'* s new inode \equiv return 0

definition *security-kernel-module-request'* :: 's \Rightarrow string \Rightarrow ('s, int) nondet-monad
where *security-kernel-module-request'* s name \equiv return 0

definition *security-kernel-load-data'* :: 's \Rightarrow kernel-load-data-id \Rightarrow ('s, int) nondet-monad
where *security-kernel-load-data'* s kid \equiv return 0

definition *security-kernel-read-file'* :: 's \Rightarrow Files \Rightarrow kernel-read-file-id \Rightarrow ('s, int) nondet-monad
where *security-kernel-read-file'* s file kid \equiv return 0

definition *security-kernel-post-read-file'* :: 's \Rightarrow Files \Rightarrow string \Rightarrow nat \Rightarrow kernel-read-file-id \Rightarrow ('s, int) nondet-monad
where *security-kernel-post-read-file'* s file buf size' kid \equiv return 0

definition *security-ipc-permission'* :: 's \Rightarrow kern-ipc-perm \Rightarrow nat \Rightarrow ('s, int) nondet-monad
where *security-ipc-permission'* s ipcp flg \equiv return 0

definition *security-ipc-getsecid'* :: 's \Rightarrow kern-ipc-perm \Rightarrow u32 \Rightarrow ('s, unit) nondet-monad
where *security-ipc-getsecid'* s ipcp secid' \equiv return ()

definition *security-msg-msg-alloc'* :: 's \Rightarrow msg-msg \Rightarrow ('s, int) nondet-monad
where *security-msg-msg-alloc'* s msg \equiv return 0

definition *security-msg-msg-free'* :: 's \Rightarrow msg-msg \Rightarrow ('s, unit) nondet-monad
where *security-msg-msg-free'* s msg \equiv return ()

definition *security-msg-queue-alloc'* :: 's \Rightarrow kern-ipc-perm \Rightarrow ('s, int) nondet-monad
where *security-msg-queue-alloc'* s msq \equiv return 0

definition *security-msg-queue-free'* :: 's \Rightarrow kern-ipc-perm \Rightarrow ('s, int) nondet-monad
where *security-msg-queue-free'* s msq \equiv return 0

definition *security-msg-queue-associate'* :: 's \Rightarrow kern-ipc-perm \Rightarrow int \Rightarrow ('s, int) nondet-monad
where *security-msg-queue-associate'* s msq msqflg \equiv return 0

definition *security-msg-queue-msgctl'* :: 's \Rightarrow kern-ipc-perm \Rightarrow IPC-CMD \Rightarrow ('s, int) nondet-monad
where *security-msg-queue-msgctl'* s msq cmd \equiv return 0

definition *security-msg-queue-msgsnd'* :: 's \Rightarrow kern-ipc-perm \Rightarrow msg-msg \Rightarrow int \Rightarrow ('s, int) nondet-monad
where *security-msg-queue-msgsnd'* s msq msg msqflg \equiv return 0

definition *security-msg-queue-msgrcv'* :: 's \Rightarrow kern-ipc-perm \Rightarrow msg-msg \Rightarrow Task \Rightarrow int \Rightarrow int \Rightarrow ('s, int) nondet-monad
where *security-msg-queue-msgrcv'* s msq msg target type m \equiv return 0

definition *security-shm-alloc'* :: 's \Rightarrow kern-ipc-perm \Rightarrow ('s, int) nondet-monad
where *security-shm-alloc'* s shp \equiv return 0

definition *security-shm-free'* :: 's \Rightarrow kern-ipc-perm \Rightarrow ('s, unit) nondet-monad
where *security-shm-free'* s shp \equiv return ()

definition *security-shm-associate'* :: 's \Rightarrow kern-ipc-perm \Rightarrow int \Rightarrow ('s, int) nondet-monad
where *security-shm-associate'* s shp shmflg \equiv return 0

definition *security-shm-shmctl'* :: 's \Rightarrow kern-ipc-perm \Rightarrow IPC-CMD \Rightarrow ('s, int) nondet-monad
where *security-shm-shmctl'* s shp cmd \equiv return 0

definition *security-shm-shmat'* :: 's \Rightarrow kern-ipc-perm \Rightarrow string \Rightarrow int \Rightarrow ('s, int) nondet-monad
where *security-shm-shmat'* s shp shmaddr shmflg \equiv return 0

definition *security-sem-alloc'* :: 's \Rightarrow kern-ipc-perm \Rightarrow ('s, int) nondet-monad
where *security-sem-alloc'* s sma \equiv return 0

definition *security-sem-free'* :: 's \Rightarrow kern-ipc-perm \Rightarrow ('s, unit) nondet-monad
where *security-sem-free'* s sma \equiv return ()

definition *security-sem-associate'* :: 's \Rightarrow kern-ipc-perm \Rightarrow int \Rightarrow ('s, int) nondet-monad
where *security-sem-associate'* s sma semflg \equiv return 0

definition *security-sem-semctl'* :: 's \Rightarrow kern-ipc-perm \Rightarrow IPC-CMD \Rightarrow ('s, int) nondet-monad
where *security-sem-semctl'* s sma cmd \equiv return 0

definition *security-sem-semop'* :: 's \Rightarrow kern-ipc-perm \Rightarrow sembuf \Rightarrow nat \Rightarrow int \Rightarrow ('s, int) nondet-monad
where *security-sem-semop'* s sma sops nsops alter \equiv return 0

definition *security-netlink-send'* :: 's \Rightarrow sock \Rightarrow sk-buff \Rightarrow ('s, int) nondet-monad
where *security-netlink-send'* s sk' skb \equiv return 0

definition *security-ismaclabel'* :: 's \Rightarrow xattr \Rightarrow ('s, int) nondet-monad
where *security-ismaclabel'* s name \equiv return 0

definition *security-secid-to-secctx'* :: 's \Rightarrow u32 \Rightarrow string \Rightarrow u32 \Rightarrow ('s, int) nondet-monad
where *security-secid-to-secctx'* s secid' secdata seclen \equiv return 0

definition *security-secctx-to-secid'* :: 's \Rightarrow string \Rightarrow u32 \Rightarrow u32 \Rightarrow ('s, int) nondet-monad
where *security-secctx-to-secid'* s secdata seclen secid' \equiv return 0

definition *security-release-secctx'* :: 's \Rightarrow string \Rightarrow u32 \Rightarrow ('s, unit) nondet-monad
where *security-release-secctx'* s secdata seclen \equiv return ()

definition *security-unix-stream-connect'* :: 's \Rightarrow sock \Rightarrow sock \Rightarrow sock \Rightarrow ('s, int) nondet-monad
where *security-unix-stream-connect'* s sock other newsk \equiv return 0

definition *security-unix-may-send'* :: 's \Rightarrow socket \Rightarrow socket \Rightarrow ('s, int) nondet-monad
where *security-unix-may-send'* s sock other \equiv return 0

definition *security-socket-create'* :: 's \Rightarrow Sk-Family \Rightarrow int \Rightarrow int \Rightarrow int \Rightarrow ('s, int) nondet-monad
where *security-socket-create'* s family type pro kern \equiv return 0

definition *security-socket-post-create'* :: 's \Rightarrow socket \Rightarrow Sk-Family \Rightarrow int \Rightarrow int \Rightarrow int \Rightarrow ('s, int) nondet-monad
where *security-socket-post-create'* s sock family type pro kern \equiv return 0

definition *security-socket-socketpair'* :: 's \Rightarrow socket \Rightarrow socket \Rightarrow ('s, int) nondet-monad
where *security-socket-socketpair'* s socka sockb \equiv return 0

definition *security-socket-bind'* :: 's \Rightarrow socket \Rightarrow sockaddr \Rightarrow int \Rightarrow ('s, int) nondet-monad
where *security-socket-bind'* s sock address addrlen \equiv return 0

definition *security-socket-connect'* :: 's \Rightarrow socket \Rightarrow sockaddr \Rightarrow int \Rightarrow ('s, int) nondet-monad
where *security-socket-connect'* s sock address addrlen \equiv return 0

definition *security-socket-listen'* :: 's \Rightarrow socket \Rightarrow int \Rightarrow ('s, int) nondet-monad
where *security-socket-listen'* s sock backlog \equiv return 0

definition *security-socket-accept'* :: 's \Rightarrow socket \Rightarrow socket \Rightarrow ('s, int) nondet-monad
where *security-socket-accept'* s sock newsock \equiv return 0

definition *security-socket-sendmsg'* :: 's \Rightarrow socket \Rightarrow msghdr \Rightarrow int \Rightarrow ('s, int) nondet-monad
where *security-socket-sendmsg'* s sock msg size' \equiv return 0

definition *security-socket-recvmsg'* :: 's \Rightarrow socket \Rightarrow msghdr \Rightarrow int \Rightarrow int \Rightarrow ('s, int) nondet-monad
where *security-socket-recvmsg'* s sock msg size' flgs \equiv return 0

definition *security-socket-getsockname'* :: 's \Rightarrow socket \Rightarrow ('s, int) nondet-monad
where *security-socket-getsockname'* s sock \equiv return 0

definition *security-socket-getpeername'* :: 's \Rightarrow socket \Rightarrow ('s, int) nondet-monad
where *security-socket-getpeername'* s sock \equiv return 0

definition *security-socket-getsockopt'* :: 's \Rightarrow socket \Rightarrow int \Rightarrow int \Rightarrow ('s, int) nondet-monad
where *security-socket-getsockopt'* s sock level' optname \equiv return 0

definition *security-socket-setsockopt'* :: 's \Rightarrow socket \Rightarrow int \Rightarrow int \Rightarrow ('s, int) nondet-monad
where *security-socket-setsockopt'* s sock level' optname \equiv return 0

definition *security-socket-shutdown'* :: 's \Rightarrow socket \Rightarrow int \Rightarrow ('s, int) nondet-monad
where *security-socket-shutdown'* s sock how \equiv return 0

definition *security-sock-rcv-skb'* :: 's \Rightarrow sock \Rightarrow sk-buff \Rightarrow ('s, int) nondet-monad
where *security-sock-rcv-skb'* s sock skb \equiv return 0

definition *security-socket-getpeersec-stream'* :: 's \Rightarrow socket \Rightarrow string \Rightarrow int \Rightarrow nat \Rightarrow ('s, int) nondet-monad
where *security-socket-getpeersec-stream'* s sock optval optlen len' \equiv return 0

definition *security-socket-getpeersec-dgram'* :: 's \Rightarrow socket \Rightarrow sk-buff option \Rightarrow u32 \Rightarrow ('s, int) nondet-monad
where *security-socket-getpeersec-dgram'* s sock skb secid' \equiv return 0

definition *security-sk-alloc'* :: 's \Rightarrow sock \Rightarrow int \Rightarrow gfp-t \Rightarrow ('s, int) nondet-monad
where *security-sk-alloc'* s sk' family priority \equiv return 0

definition *security-sk-free'* :: 's \Rightarrow sock \Rightarrow ('s, unit) nondet-monad
where *security-sk-free'* s sock \equiv return ()

definition *security-sk-clone'* :: 's \Rightarrow sock \Rightarrow sock \Rightarrow ('s, unit) nondet-monad
where *security-sk-clone'* s sk' newsk \equiv return()

definition *security-sk-classify-flow'* :: 's \Rightarrow sock \Rightarrow flowi \Rightarrow ('s, unit) nondet-monad
where *security-sk-classify-flow'* s sock' fl \equiv return ()

definition *security-req-classify-flow'* :: 's \Rightarrow request-sock \Rightarrow flowi \Rightarrow ('s, unit) nondet-monad
where *security-req-classify-flow'* s req fl \equiv return ()

definition *security-sock-graft'* :: 's \Rightarrow sock \Rightarrow socket \Rightarrow ('s, unit) nondet-monad
where *security-sock-graft'* s sk' parent' \equiv return ()

definition *security-inet-conn-request'* :: 's \Rightarrow sock \Rightarrow sk-buff \Rightarrow request-sock \Rightarrow ('s, int) nondet-monad
where *security-inet-conn-request'* s sk' skb req \equiv return 0

definition *security-inet-csk-clone'* :: 's \Rightarrow sock \Rightarrow request-sock \Rightarrow ('s, unit) nondet-monad
where *security-inet-csk-clone'* s newsk req \equiv return ()

definition *security-inet-conn-established'* :: 's \Rightarrow sock \Rightarrow sk-buff \Rightarrow ('s, unit) nondet-monad
where *security-inet-conn-established'* s sk' skb \equiv return()

definition *security-secmark-relabel-packet'* :: 's \Rightarrow u32 \Rightarrow ('s, int) nondet-monad
where *security-secmark-relabel-packet'* s secid' \equiv return 0

definition *security-secmark-refcount-inc* :: 's \Rightarrow ('s, unit) nondet-monad
where *security-secmark-refcount-inc* s \equiv return ()

definition *security-secmark-refcount-dec'* :: 's \Rightarrow ('s, unit) nondet-monad
where *security-secmark-refcount-dec'* s \equiv return ()

definition *security-tun-dev-alloc-security'* :: 's \Rightarrow 'b \Rightarrow ('s, int) nondet-monad
where *security-tun-dev-alloc-security'* s security \equiv return 0

definition *security-tun-dev-free-security'* :: 's \Rightarrow 'b \Rightarrow ('s, unit) nondet-monad
where *security-tun-dev-free-security'* s security \equiv return ()

definition *security-tun-dev-create* :: 's \Rightarrow ('s, int) nondet-monad
where *security-tun-dev-create* s \equiv return 0

definition *security-tun-dev-attach-queue'* :: 's \Rightarrow 'b \Rightarrow ('s, int) nondet-monad
where *security-tun-dev-attach-queue'* s security \equiv return 0

definition *security-tun-dev-attach'* :: 's \Rightarrow sock \Rightarrow 'b \Rightarrow ('s, int) nondet-monad
where *security-tun-dev-attach'* s sk' security \equiv return 0

definition *security-tun-dev-open'* :: 's \Rightarrow 'b \Rightarrow ('s, int) nondet-monad
where *security-tun-dev-open'* s security \equiv return 0

definition *security-sctp-assoc-request'* :: 's \Rightarrow sctp-endpoint \Rightarrow sk-buff \Rightarrow ('s, int) nondet-monad
where *security-sctp-assoc-request'* s ep skb \equiv return 0

definition *security-sctp-bind-connect'* :: 's \Rightarrow sock \Rightarrow int \Rightarrow sockaddr \Rightarrow int \Rightarrow ('s, int) nondet-monad
where *security-sctp-bind-connect'* s sk' optname address addrlen \equiv return 0

definition *security-sctp-sk-clone'* :: 's \Rightarrow sctp-endpoint \Rightarrow sock \Rightarrow sock \Rightarrow ('s, unit) nondet-monad
where *security-sctp-sk-clone'* s ep sk' newsk \equiv return ()

definition *security-ib-pkey-access'* :: 's \Rightarrow 'i \Rightarrow nat \Rightarrow nat \Rightarrow ('s, int) nondet-monad

where $\text{security-ib-pkey-access}' s \text{ sec subnet-prefix pkey} \equiv \text{return } 0$

definition $\text{security-ib-endport-manage-subnet}' :: 's \Rightarrow 'i \Rightarrow \text{string} \Rightarrow \text{nat} \Rightarrow ('s, \text{int}) \text{ nondet-monad}$
where $\text{security-ib-endport-manage-subnet}' s \text{ sec dev-name port-num} \equiv \text{return } 0$

definition $\text{security-ib-alloc-security}' :: 's \Rightarrow 'i \text{ list} \Rightarrow ('s, \text{int}) \text{ nondet-monad}$
where $\text{security-ib-alloc-security}' s \text{ sec} \equiv \text{return } 0$

definition $\text{security-ib-free-security}' :: 's \Rightarrow 'i \text{ list} \Rightarrow ('s, \text{unit}) \text{ nondet-monad}$
where $\text{security-ib-free-security}' s \text{ sec} \equiv \text{return } ()$

definition $\text{security-xfrm-policy-alloc}' :: 's \Rightarrow \text{xfrm-sec-ctx} \Rightarrow \text{xfrm-user-sec-ctx} \Rightarrow \text{gfp-t}$
 $\Rightarrow ('s, \text{int}) \text{ nondet-monad}$
where $\text{security-xfrm-policy-alloc}' s \text{ ctx sec-ctx gfp}' \equiv \text{return } 0$

definition $\text{security-xfrm-policy-clone}' :: 's \Rightarrow \text{xfrm-sec-ctx} \Rightarrow \text{xfrm-user-sec-ctx}$
 $\Rightarrow ('s, \text{int}) \text{ nondet-monad}$
where $\text{security-xfrm-policy-clone}' s \text{ old-ctx new-ctx} \equiv \text{return } 0$

definition $\text{security-xfrm-policy-free}' :: 's \Rightarrow \text{xfrm-sec-ctx} \Rightarrow ('s, \text{unit}) \text{ nondet-monad}$
where $\text{security-xfrm-policy-free}' s \text{ ctx} \equiv \text{return } ()$

definition $\text{security-xfrm-policy-delete}' :: 's \Rightarrow \text{xfrm-sec-ctx} \Rightarrow ('s, \text{int}) \text{ nondet-monad}$
where $\text{security-xfrm-policy-delete}' s \text{ ctx} \equiv \text{return } 0$

definition $\text{security-xfrm-state-alloc}' :: 's \Rightarrow \text{xfrm-state} \Rightarrow \text{xfrm-sec-ctx} \Rightarrow ('s, \text{int}) \text{ nondet-monad}$
where $\text{security-xfrm-state-alloc}' s x \text{ sec-ctx} \equiv \text{return } 0$

definition $\text{security-xfrm-state-alloc-acquire}' :: 's \Rightarrow \text{xfrm-state} \Rightarrow \text{xfrm-sec-ctx} \Rightarrow \text{u32}$
 $\Rightarrow ('s, \text{int}) \text{ nondet-monad}$
where $\text{security-xfrm-state-alloc-acquire}' s x \text{ plosec secid}' \equiv \text{return } 0$

definition $\text{security-xfrm-state-delete}' :: 's \Rightarrow \text{xfrm-state} \Rightarrow ('s, \text{int}) \text{ nondet-monad}$
where $\text{security-xfrm-state-delete}' s x \equiv \text{return } 0$

definition $\text{security-xfrm-state-free}' :: 's \Rightarrow \text{xfrm-state} \Rightarrow ('s, \text{unit}) \text{ nondet-monad}$
where $\text{security-xfrm-state-free}' s x \equiv \text{return } ()$

definition $\text{security-xfrm-policy-lookup}' :: 's \Rightarrow \text{xfrm-sec-ctx} \Rightarrow \text{u32} \Rightarrow \text{u8} \Rightarrow ('s, \text{int}) \text{ nondet-monad}$
where $\text{security-xfrm-policy-lookup}' s \text{ ctx fl-secid dir} \equiv \text{return } 0$

definition $\text{security-xfrm-state-pol-flow-match}' :: 's \Rightarrow \text{xfrm-state} \Rightarrow \text{xfrm-policy} \Rightarrow \text{flowi}$

$\Rightarrow ('s, \text{int}) \text{ nondet-monad}$

where *security-xfrm-state-pol-flow-match'* $s \ x \ xp \ fl \equiv \text{return } 0$

definition *security-xfrm-decode-session'* $:: 's \Rightarrow \text{sk-buff} \Rightarrow \text{u32} \Rightarrow ('s, \text{int}) \text{ nondet-monad}$
where *security-xfrm-decode-session'* $s \ \text{skb} \ \text{secid}' \equiv \text{return } 0$

definition *security-skb-classify-flow'* $:: 's \Rightarrow \text{sk-buff} \Rightarrow \text{flowi} \Rightarrow ('s, \text{unit}) \text{ nondet-monad}$
where *security-skb-classify-flow'* $s \ \text{skb} \ fl \equiv \text{return } ()$

definition *security-path-unlink'* $:: 's \Rightarrow \text{path} \Rightarrow \text{dentry} \Rightarrow ('s, \text{int}) \text{ nondet-monad}$
where *security-path-unlink'* $s \ \text{dir} \ \text{dentry} \equiv \text{return } 0$

definition *security-path-mkdir'* $:: 's \Rightarrow \text{path} \Rightarrow \text{dentry} \Rightarrow \text{nat} \Rightarrow ('s, \text{int}) \text{ nondet-monad}$
where *security-path-mkdir'* $s \ \text{dir} \ \text{dentry} \ m \equiv \text{return } 0$

definition *security-path-rmdir'* $:: 's \Rightarrow \text{path} \Rightarrow \text{dentry} \Rightarrow ('s, \text{int}) \text{ nondet-monad}$
where *security-path-rmdir'* $s \ \text{dir} \ \text{dentry} \equiv \text{return } 0$

definition *security-path-mknod'* $:: 's \Rightarrow \text{path} \Rightarrow \text{dentry} \Rightarrow \text{nat} \Rightarrow \text{nat} \Rightarrow ('s, \text{int}) \text{ nondet-monad}$
where *security-path-mknod'* $s \ \text{dir} \ \text{dentry} \ m \ \text{dev} \equiv \text{return } 0$

definition *security-path-truncate'* $:: 's \Rightarrow \text{path} \Rightarrow ('s, \text{int}) \text{ nondet-monad}$
where *security-path-truncate'* $s \ \text{dir} \equiv \text{return } 0$

definition *security-path-symlink'* $:: 's \Rightarrow \text{path} \Rightarrow \text{dentry} \Rightarrow \text{string} \Rightarrow ('s, \text{int}) \text{ nondet-monad}$
where *security-path-symlink'* $s \ \text{dir} \ \text{dentry} \ \text{old-name} \equiv \text{return } 0$

definition *security-path-link'* $:: 's \Rightarrow \text{dentry} \Rightarrow \text{path} \Rightarrow \text{dentry} \Rightarrow ('s, \text{int}) \text{ nondet-monad}$
where *security-path-link'* $s \ \text{old-dentry} \ \text{new-dir} \ \text{new-dentry} \equiv \text{return } 0$

definition *security-path-rename'* $:: 's \Rightarrow \text{path} \Rightarrow \text{dentry} \Rightarrow \text{path} \Rightarrow \text{dentry} \Rightarrow ('s, \text{int}) \text{ nondet-monad}$
where *security-path-rename'* $s \ \text{old-dir} \ \text{old-dentry} \ \text{new-dir} \ \text{new-dentry} \equiv \text{return } 0$

definition *security-path-chmod'* $:: 's \Rightarrow \text{path} \Rightarrow \text{nat} \Rightarrow ('s, \text{int}) \text{ nondet-monad}$
where *security-path-chmod'* $s \ \text{path} \ m \equiv \text{return } 0$

definition *security-path-chown'* $:: 's \Rightarrow \text{path} \Rightarrow \text{kuid-t} \Rightarrow \text{kgid-t} \Rightarrow ('s, \text{int}) \text{ nondet-monad}$
where *security-path-chown'* $s \ \text{path} \ \text{uid}' \ \text{gid}' \equiv \text{return } 0$

definition *security-path-chroot'* $:: 's \Rightarrow \text{path} \Rightarrow ('s, \text{int}) \text{ nondet-monad}$
where *security-path-chroot'* $s \ \text{path} \equiv \text{return } 0$

definition *security-bpf'* :: 's ⇒ int ⇒ bpf-attr ⇒ nat ⇒ ('s, int) nondet-monad
where *security-bpf' s cmd attr' size' ≡ return 0*

definition *security-bpf-map'* :: 's ⇒ bpf-map ⇒ mode ⇒ ('s, int) nondet-monad
where *security-bpf-map' s bmap fmode ≡ return 0*

definition *security-bpf-prog'* :: 's ⇒ bpf-prog ⇒ ('s, int) nondet-monad
where *security-bpf-prog' s prog ≡ return 0*

definition *security-bpf-map-alloc'* :: 's ⇒ bpf-map ⇒ ('s, int) nondet-monad
where *security-bpf-map-alloc' s bmap ≡ return 0*

definition *security-bpf-map-free'* :: 's ⇒ bpf-map ⇒ ('s, unit) nondet-monad
where *security-bpf-map-free' s bmap ≡ return ()*

definition *security-bpf-prog-alloc'* :: 's ⇒ bpf-prog-aux ⇒ ('s, int) nondet-monad
where *security-bpf-prog-alloc' s aux' ≡ return 0*

definition *security-bpf-prog-free'* :: 's ⇒ bpf-prog-aux ⇒ ('s, unit) nondet-monad
where *security-bpf-prog-free' s aux' ≡ return ()*

definition *security-key-alloc'* :: 's ⇒ key ⇒ Cred ⇒ nat ⇒ ('s, int) nondet-monad
where *security-key-alloc' s key' c flgs ≡ return 0*

definition *security-key-free'* :: 's ⇒ key ⇒ ('s, unit) nondet-monad
where *security-key-free' s key' ≡ return ()*

definition *security-key-permission'* :: 's ⇒ key-ref-t ⇒ Cred ⇒ nat ⇒ ('s, int) nondet-monad
where *security-key-permission' s key-ref c perm ≡ return 0*

definition *security-key-getsecurity'* :: 's ⇒ key ⇒ string ⇒ ('s, int) nondet-monad
where *security-key-getsecurity' s key' buffer ≡ return 0*

definition *security-audit-rule-init'* :: 's ⇒ nat ⇒ enum-audit ⇒ string ⇒ string
 ⇒ ('s, int) nondet-monad
where *security-audit-rule-init' s field op rulestr lsmrule ≡ return 0*

definition *security-audit-rule-known'* :: 's ⇒ audit-krule ⇒ ('s, int) nondet-monad
where *security-audit-rule-known' s krule ≡ return 0*

definition *security-audit-rule-match'* :: 's ⇒ nat ⇒ nat ⇒ enum-audit ⇒ string
 ⇒ audit-context
 ⇒ ('s, int) nondet-monad
where *security-audit-rule-match' s secid' field op lsmrule actx ≡ return 0*

```

definition security-audit-rule-free' :: 's  $\Rightarrow$  string  $\Rightarrow$  ('s, unit) nondet-monad
  where security-audit-rule-free' s lsmrule  $\equiv$  return ()

end
theory Dynamic-model
imports Main
begin

```

27.10 Security State Machine

```

locale SM =
  fixes s0 :: 's
  fixes step :: 's  $\Rightarrow$  'e  $\Rightarrow$  's
  fixes domain :: 'e  $\Rightarrow$  ('d option)
  fixes vpeq :: 's  $\Rightarrow$  'd  $\Rightarrow$  's  $\Rightarrow$  bool ((-  $\sim$  -  $\sim$  -))
  fixes interferes :: 'd  $\Rightarrow$  's  $\Rightarrow$  'd  $\Rightarrow$  bool ((- @ - -))
  assumes
    vpeq-transitive-lemma :  $\forall$  s t r d. (s  $\sim$  d  $\sim$  t)  $\wedge$  (t  $\sim$  d  $\sim$  r)  $\longrightarrow$  (s  $\sim$  d  $\sim$  r)
  and
    vpeq-symmetric-lemma :  $\forall$  s t d. (s  $\sim$  d  $\sim$  t)  $\longrightarrow$  (t  $\sim$  d  $\sim$  s) and
    vpeq-reflexive-lemma :  $\forall$  s d. (s  $\sim$  d  $\sim$  s) and
    interf-reflexive :  $\forall$  d s. (d @ s d)
begin

  definition non-interferes :: 'd  $\Rightarrow$  's  $\Rightarrow$  'd  $\Rightarrow$  bool ((- @ - \ -))
    where (u @ s \ v)  $\equiv$  (u @ s v)

  definition ivpeq :: 's  $\Rightarrow$  'd set  $\Rightarrow$  's  $\Rightarrow$  bool ((-  $\approx$  -  $\approx$  -))
    where ivpeq s D t  $\equiv$   $\forall$  d  $\in$  D. (s  $\sim$  d  $\sim$  t)

  primrec run :: 's  $\Rightarrow$  'e list  $\Rightarrow$  's
    where run-Nil: run s [] = s |
      run-Cons: run s (a#as) = run (step s a) as

  definition reachable :: 's  $\Rightarrow$  's  $\Rightarrow$  bool ((-  $\hookrightarrow$  -) [70,71] 60) where
    reachable s1 s2  $\equiv$  ( $\exists$  as. run s1 as = s2 )

  definition reachable0 :: 's  $\Rightarrow$  bool where
    reachable0 s  $\equiv$  reachable s0 s

  declare non-interferes-def[cong] and ivpeq-def[cong] and reachable-def[cong]
    and reachable0-def[cong] and run.simps(1)[cong] and run.simps(2)[cong]

  lemma reachable-s0 : reachable0 s0
    by (metis SM.reachable-def SM-axioms reachable0-def run.simps(1))

  lemma reachable-self : reachable s s

```

```

using reachable-def run.simps(1) by fastforce

lemma reachable-step :  $s' = \text{step } s \ a \implies \text{reachable } s \ s'$ 
proof-
  assume a0:  $s' = \text{step } s \ a$ 
  then have  $s' = \text{run } s \ [a]$  by auto
  then show ?thesis using reachable-def by blast
qed

lemma run-trans :  $\forall C \ T \ V \ as \ bs. \ T = \text{run } C \ as \wedge V = \text{run } T \ bs \longrightarrow V =$ 
 $\text{run } C \ (as@bs)$ 
proof -
  {
    fix  $T \ V \ as \ bs$ 
    have  $\forall C. \ T = \text{run } C \ as \wedge V = \text{run } T \ bs \longrightarrow V = \text{run } C \ (as@bs)$ 
    proof(induct as)
      case Nil show ?case by simp
    next
      case (Cons c cs)
      assume a0:  $\forall C. \ T = \text{run } C \ cs \wedge V = \text{run } T \ bs \longrightarrow V = \text{run } C \ (cs @$ 
 $bs)$ 
      show ?case
      proof-
        {
          fix  $C$ 
          have  $T = \text{run } C \ (c \# cs) \wedge V = \text{run } T \ bs \longrightarrow V = \text{run } C \ ((c \#$ 
 $cs) @ bs)$ 
          proof
            assume b0:  $T = \text{run } C \ (c \# cs) \wedge V = \text{run } T \ bs$ 
            from b0 obtain  $C'$  where b2:  $C' = \text{step } C \ c \wedge T = \text{run } C' \ cs$ 
            by auto
            with a0 b0 have  $V = \text{run } C' \ (cs@bs)$  by blast
            with b2 show  $V = \text{run } C \ ((c \# cs) @ bs)$ 
            using append-Cons run-Cons by auto
          qed
        }
      then show ?thesis by blast
    qed
  }
  then show ?thesis by auto
qed

lemma reachable-trans :  $\llbracket \text{reachable } C \ T; \text{reachable } T \ V \rrbracket \implies \text{reachable } C \ V$ 
proof-
  assume a0:  $\text{reachable } C \ T$ 
  assume a1:  $\text{reachable } T \ V$ 
  from a0 have  $C = T \vee (\exists as. \ T = \text{run } C \ as)$  by auto
  then show ?thesis

```

```

proof
  assume  $b0: C = T$ 
  show ?thesis
  proof –
    from  $a1$  have  $T = V \vee (\exists as. V = \text{run } T \text{ as})$  by auto
    then show ?thesis
    proof
      assume  $c0: T = V$ 
      with  $a0$  show ?thesis by auto
    next
      assume  $c0: (\exists as. V = \text{run } T \text{ as})$ 
      then show ?thesis using  $a1$   $b0$  by auto
    qed
  qed
next
  assume  $b0: \exists as. T = \text{run } C \text{ as}$ 
  show ?thesis
  proof –
    from  $a1$  have  $T = V \vee (\exists as. V = \text{run } T \text{ as})$  by auto
    then show ?thesis
    proof
      assume  $c0: T = V$ 
      then show ?thesis using  $a0$  by auto
    next
      assume  $c0: (\exists as. V = \text{run } T \text{ as})$ 
      from  $b0$  obtain  $as$  where  $d0: T = \text{run } C \text{ as}$  by auto
      from  $c0$  obtain  $bs$  where  $d1: V = \text{run } T \text{ bs}$  by auto
      then show ?thesis using  $d0$  run-trans by fastforce
    qed
  qed
qed
qed

lemma reachableStep :  $\llbracket \text{reachable0 } C; C' = \text{step } C \text{ a} \rrbracket \implies \text{reachable0 } C'$ 
  apply (simp add: reachable0-def)
  using reachable-step reachable-trans by blast

lemma reachable0-reach :  $\llbracket \text{reachable0 } C; \text{reachable } C \text{ } C' \rrbracket \implies \text{reachable0 } C'$ 
  using reachable-trans by fastforce

declare reachable-def[cong del] and reachable0-def[cong del]
end

```

27.11 Information flow security properties

```

locale SM-enabled = SM s0 step domain vpeq interferes
  for  $s0 :: 's$  and
     $\text{step} :: 's \Rightarrow 'e \Rightarrow 's$  and
     $\text{domain} :: 'e \Rightarrow ('d \text{ option})$  and

```

```

    vpeq :: 's ⇒ 'd ⇒ 's ⇒ bool ((- ~ - ~ -)) and
    interferes :: 'd ⇒ 's ⇒ 'd ⇒ bool ((- @ - -))
+
assumes enabled0: ∀ s a. reachable0 s ⟶ (∃ s'. s' = step s a)
and policy-respect: ∀ v u s t. (s ~ u ~ t)
    ⟶ (interferes v s u = interferes v t u)

begin

lemma enabled : reachable0 s ⟹ (∃ s'. s' = step s a)
  using enabled0 by simp

primrec sources :: 'e list ⇒ 'd ⇒ 's ⇒ 'd set where
  sources-Nil:sources [] d s = {d} |
  sources-Cons:sources (a # as) d s = (⋃ {sources as d (step s a)}) ∪
    {w . w = the (domain a) ∧ (∃ v . interferes w s v ∧
v ∈ sources as d (step s a))}
  declare sources-Nil [simp del]
  declare sources-Cons [simp del]

primrec ipurge :: 'e list ⇒ 'd ⇒ 's ⇒ 'e list where
  ipurge-Nil: ipurge [] u s = [] |
  ipurge-Cons: ipurge (a # as) u s = (if (the (domain a) ∈ (sources (a # as) u
s))
    then
      a # ipurge as u (step s a)
    else
      ipurge as u (step s a)
    )

definition observ-equivalence :: 's ⇒ 'e list ⇒ 's ⇒
  'e list ⇒ 'd ⇒ bool ((- - ≅ - - @ -))
where observ-equivalence s as t bs d ≡
  ((run s as) ~ d ~ (run t bs))
declare observ-equivalence-def [cong]

lemma observ-equiv-sym:
  (s as ≅ t bs @ d) ⟹ (t bs ≅ s as @ d)
  using observ-equivalence-def vpeq-symmetric-lemma by blast

lemma observ-equiv-trans:
  [[reachable0 t; (s as ≅ t bs @ d); (t bs ≅ x cs @ d)] ⟹ (s as ≅ x cs
@ d)
  using observ-equivalence-def vpeq-transitive-lemma by blast

```

definition *noninterference-r* :: bool
where *noninterference-r* $\equiv \forall d \text{ as } s. \text{reachable0 } s \longrightarrow (s \text{ as } \cong s \text{ (ipurge as } d \text{ s) @ } d)$

definition *noninterference* :: bool
where *noninterference* $\equiv \forall d \text{ as. } (s0 \text{ as } \cong s0 \text{ (ipurge as } d \text{ s0) @ } d)$

definition *weak-noninterference* :: bool
where *weak-noninterference* $\equiv \forall d \text{ as bs. ipurge as } d \text{ s0} = \text{ipurge bs } d \text{ s0} \longrightarrow (s0 \text{ as } \cong s0 \text{ bs @ } d)$

definition *weak-noninterference-r* :: bool
where *weak-noninterference-r* $\equiv \forall d \text{ as bs s. reachable0 } s \wedge \text{ipurge as } d \text{ s} = \text{ipurge bs } d \text{ s} \longrightarrow (s \text{ as } \cong s \text{ bs @ } d)$

definition *noninfluence* :: bool
where *noninfluence* $\equiv \forall d \text{ as s t. reachable0 } s \wedge \text{reachable0 } t \wedge (s \approx (\text{sources as } d \text{ s}) \approx t) \longrightarrow (s \text{ as } \cong t \text{ (ipurge as } d \text{ t) @ } d)$

definition *weak-noninfluence* :: bool
where *weak-noninfluence* $\equiv \forall d \text{ as bs s t. reachable0 } s \wedge \text{reachable0 } t \wedge (s \approx (\text{sources as } d \text{ s}) \approx t) \wedge \text{ipurge as } d \text{ t} = \text{ipurge bs } d \text{ t} \longrightarrow (s \text{ as } \cong t \text{ bs @ } d)$

definition *weak-noninfluence2* :: bool
where *weak-noninfluence2* $\equiv \forall d \text{ as bs s t. reachable0 } s \wedge \text{reachable0 } t \wedge (s \approx (\text{sources as } d \text{ s}) \approx t) \wedge \text{ipurge as } d \text{ s} = \text{ipurge bs } d \text{ t} \longrightarrow (s \text{ as } \cong t \text{ bs @ } d)$

definition *nonleakage* :: bool
where *nonleakage* $\equiv \forall d \text{ as s t. reachable0 } s \wedge \text{reachable0 } t \wedge (s \approx (\text{sources as } d \text{ s}) \approx t) \longrightarrow (s \text{ as } \cong t \text{ as @ } d)$

declare *noninterference-r-def*[cong] **and** *noninterference-def*[cong] **and** *weak-noninterference-def*[cong] **and**
weak-noninterference-r-def[cong] **and** *noninfluence-def*[cong] **and**
weak-noninfluence-def[cong] **and** *weak-noninfluence2-def*[cong] **and** *nonleakage-def*[cong]

27.12 Unwinding conditions

definition *dynamic-step-consistent* :: bool **where**
dynamic-step-consistent $\equiv \forall a \text{ d s t. reachable0 } s \wedge \text{reachable0 } t \wedge (s \sim d \sim t) \wedge (((\text{the } (\text{domain } a)) \text{ @ } s \text{ d}) \longrightarrow (s \sim (\text{the } (\text{domain } a)) \sim t))$

$$\longrightarrow ((\text{step } s \ a) \sim d \sim (\text{step } t \ a))$$

definition *dynamic-weakly-step-consistent* :: *bool* **where**

$$\begin{aligned} \text{dynamic-weakly-step-consistent} &\equiv \forall a \ d \ s \ t. \text{reachable0 } s \wedge \text{reachable0 } t \wedge \\ &(s \sim d \sim t) \wedge \\ &((\text{the } (\text{domain } a)) @ s \ d) \wedge (s \sim (\text{the } (\text{domain } a)) \sim t) \\ &\longrightarrow ((\text{step } s \ a) \sim d \sim (\text{step } t \ a)) \end{aligned}$$

definition *dynamic-weakly-step-consistent-e* :: '*e* \Rightarrow *bool*' **where**

$$\begin{aligned} \text{dynamic-weakly-step-consistent-e } a &\equiv \forall d \ s \ t. \text{reachable0 } s \wedge \text{reachable0 } t \wedge \\ &(s \sim d \sim t) \wedge \\ &((\text{the } (\text{domain } a)) @ s \ d) \wedge (s \sim (\text{the } (\text{domain } a)) \sim t) \\ &\longrightarrow ((\text{step } s \ a) \sim d \sim (\text{step } t \ a)) \end{aligned}$$

lemma *dynamic-weakly-step-consistent-all-evt* : *dynamic-weakly-step-consistent*
 $= (\forall a. \text{dynamic-weakly-step-consistent-e } a)$
by (*simp add: dynamic-weakly-step-consistent-def dynamic-weakly-step-consistent-e-def*)

definition *dynamic-local-respect* :: *bool* **where**

$$\begin{aligned} \text{dynamic-local-respect} &\equiv \forall a \ d \ s. \text{reachable0 } s \wedge \neg((\text{the } (\text{domain } a)) @ s \ d) \\ &\longrightarrow (s \sim d \sim (\text{step } s \ a)) \end{aligned}$$

definition *dynamic-local-respect-e* :: '*e* \Rightarrow *bool*' **where**

$$\begin{aligned} \text{dynamic-local-respect-e } a &\equiv \forall d \ s. \text{reachable0 } s \wedge \neg((\text{the } (\text{domain } a)) @ s \\ d) &\longrightarrow (s \sim d \sim (\text{step } s \ a)) \end{aligned}$$

lemma *dynamic-local-respect-all-evt* : *dynamic-local-respect* = $(\forall a. \text{dynamic-local-respect-e } a)$

by (*simp add: dynamic-local-respect-def dynamic-local-respect-e-def*)

declare *dynamic-step-consistent-def* [*cong*] **and** *dynamic-weakly-step-consistent-def*
[*cong*] **and**
dynamic-local-respect-def [*cong*]

lemma *step-cons-impl-weak* : *dynamic-step-consistent* \implies *dynamic-weakly-step-consistent*
using *dynamic-step-consistent-def dynamic-weakly-step-consistent-def* **by** *blast*

definition *lemma-local* :: *bool* **where**

$$\begin{aligned} \text{lemma-local} &\equiv \forall s \ a \ as \ u. \text{the } (\text{domain } a) \notin \text{sources } (a \# as) \ u \ s \longrightarrow (s \approx \\ &(\text{sources } (a \# as) \ u \ s) \approx (\text{step } s \ a)) \end{aligned}$$

lemma *weak-with-step-cons*:

assumes *p1*: *dynamic-weakly-step-consistent*

and *p2*: *dynamic-local-respect*

shows *dynamic-step-consistent*

proof –

{

fix *a d s t*

have *reachable0 s* \wedge *reachable0 t* \wedge (*s* \sim *d* \sim *t*) \wedge

```

      (((the (domain a)) @ s d) → (s ~ (the (domain a)) ~ t))
      → ((step s a) ~ d ~ (step t a))
proof -
{
  assume a0: reachable0 s
  assume a1: reachable0 t
  assume a2: (s ~ d ~ t)
  assume a3: (((the (domain a)) @ s d) → (s ~ (the (domain a)) ~ t))
  have ((step s a) ~ d ~ (step t a))
  proof (cases ((the (domain a)) @ s d))
    assume b0: ((the (domain a)) @ s d)
    have b1: (s ~ (the (domain a)) ~ t)
      using b0 a3 by auto
    have b2: ((step s a) ~ d ~ (step t a))
      using a0 a1 a2 b0 b1 p1 dynamic-weakly-step-consistent-def by blast
    then show ?thesis by auto
  next
    assume b0: ¬((the (domain a)) @ s d)
    have b1: ¬((the (domain a)) @ t d)
      using a0 a1 a2 b0 policy-respect by auto
    have b2: s ~ d ~ (step s a)
      using b0 p2 a0 by auto
    have b3: t ~ d ~ (step t a)
      using b1 p2 a1 by auto
    have b4: ((step s a) ~ d ~ (step t a))
      using b2 b3 a2 vpeq-symmetric-lemma vpeq-transitive-lemma by
blast
    then show ?thesis by auto
  }
  then show ?thesis by auto
qed
}
then show ?thesis by auto
qed
}
then show ?thesis by auto
qed

```

27.13 Lemmas for the inference framework

```

lemma sources-refl: reachable0 s ⇒ u ∈ sources as u s
  apply(induct as arbitrary: s)
  apply(simp add: sources-Nil)
  apply(simp add: sources-Cons)
  using enabled reachableStep
  by metis

```

```

lemma lemma-1-sub-1 : [[reachable0 s ;
  dynamic-local-respect;
  the (domain a) ∉ sources (a # as) u s;

```


$(s \approx (\text{sources } (a \# \text{as}) \ u \ s) \approx t)$
 $\implies (s \approx (\text{sources as u } (\text{step } s \ a)) \approx (\text{step } s \ a))$
apply (*simp add:dynamic-local-respect-def sources-Cons*)
by *blast*

lemma *lemma-1-sub-2* : $\llbracket \text{reachable0 } s ;$
 $\text{reachable0 } t ;$
 $\text{dynamic-local-respect};$
 $\text{the } (\text{domain } a) \notin \text{sources } (a \# \text{as}) \ u \ s;$
 $(s \approx (\text{sources } (a \# \text{as}) \ u \ s) \approx t) \rrbracket$
 $\implies (t \approx (\text{sources as u } (\text{step } s \ a)) \approx (\text{step } t \ a))$

proof –

assume *a1*: *reachable0 s*
assume *a2*: *reachable0 t*
assume *a3*: *dynamic-local-respect*
assume *a6*: *the (domain a) ∉ sources (a # as) u s*
assume *a7*: $(s \approx (\text{sources } (a \# \text{as}) \ u \ s) \approx t)$
have *b1*: $\forall v. v \in \text{sources as u } (\text{step } s \ a) \longrightarrow \neg \text{interferes } (\text{the } (\text{domain } a))$

s v

using *a6 sources-Cons* **by** *auto*
have *b2*: $\text{sources } (a \# \text{as}) \ u \ s = \text{sources as u } (\text{step } s \ a)$
using *a6 sources-Cons* **by** *auto*
have *b3*: $\forall v. v \in \text{sources as u } (\text{step } s \ a) \longrightarrow (s \sim v \sim t)$
using *a7 b2 ivpeq-def* **by** *blast*
have *b4*: $\forall v. v \in \text{sources as u } (\text{step } s \ a) \longrightarrow \neg \text{interferes } (\text{the } (\text{domain } a))$

t v

using *a1 a2 policy-respect b1 b3* **by** *blast*
have *b5*: $\forall v. v \in \text{sources as u } (\text{step } s \ a) \longrightarrow (t \sim v \sim (\text{step } t \ a))$
using *a2 a3 b4* **by** *auto*
then show *?thesis*
using *ivpeq-def* **by** *auto*
qed

lemma *lemma-1-sub-3* : \llbracket
 $\text{the } (\text{domain } a) \notin \text{sources } (a \# \text{as}) \ u \ s;$
 $(s \approx (\text{sources } (a \# \text{as}) \ u \ s) \approx t) \rrbracket$
 $\implies (s \approx (\text{sources as u } (\text{step } s \ a)) \approx t)$
apply (*simp add:sources-Cons*)
apply (*simp add:sources-Cons*)
done

lemma *lemma-1-sub-4* : $\llbracket (s \approx (\text{sources as u } (\text{step } s \ a)) \approx t);$
 $(s \approx (\text{sources as u } (\text{step } s \ a)) \approx (\text{step } s \ a));$
 $(t \approx (\text{sources as u } (\text{step } s \ a)) \approx (\text{step } t \ a)) \rrbracket$
 $\implies ((\text{step } s \ a) \approx (\text{sources as u } (\text{step } s \ a)) \approx (\text{step } t \ a))$
by (*meson ivpeq-def vpeq-symmetric-lemma vpeq-transitive-lemma*)

lemma *lemma-1* : $\llbracket \text{reachable0 } s;$

```

    reachable0 t;
    dynamic-step-consistent;
    dynamic-local-respect;
    (s ≈ (sources (a # as) u s) ≈ t)]
    ⇒ ((step s a) ≈ (sources as u (step s a)) ≈ (step t a))
  apply (case-tac the (domain a) ∈ sources (a # as) u s)
  apply (simp add: dynamic-step-consistent-def)
  apply (simp add: sources-Cons)
  proof -
    assume a1: dynamic-local-respect
    assume a4: the (domain a) ∉ sources (a # as) u s
    assume a5: (s ≈ (sources (a # as) u s) ≈ t)
    assume b0: reachable0 s
    assume b1: reachable0 t

    have a6: (s ≈ (sources as u (step s a)) ≈ t)
      using a1 policy-respect a4 a5 lemma-1-sub-3 by auto
    then have a7: (s ≈ (sources as u (step s a)) ≈ (step s a))
      using b0 a1 policy-respect a4 a5 lemma-1-sub-1 by auto
    then have a8: (t ≈ (sources as u (step s a)) ≈ (step t a))
      using b1 b0 a1 policy-respect a4 a5 lemma-1-sub-2 by auto
    then show ((step s a) ≈ (sources as u (step s a)) ≈ (step t a))
      using a6 a7 lemma-1-sub-4 by blast
  qed

```

```

lemma lemma-2 : [reachable0 s;
  dynamic-local-respect;
  the (domain a) ∉ sources (a # as) u s]
  ⇒ (s ≈ (sources as u (step s a)) ≈ (step s a))
  apply (simp add: dynamic-local-respect-def)
  apply (simp add: sources-Cons)
  by blast

```

```

lemma sources-eq1: ∀ s t as u. reachable0 s ∧
  reachable0 t ∧
  dynamic-step-consistent ∧
  dynamic-local-respect ∧
  (s ≈ (sources as u s) ≈ t)
  → (sources as u s) = (sources as u t)
  proof -
    {
      fix as
      have ∀ s t u. reachable0 s ∧
        reachable0 t ∧
        dynamic-step-consistent ∧
        dynamic-local-respect ∧
        (s ≈ (sources as u s) ≈ t)
        → (sources as u s) = (sources as u t)
      proof(induct as)

```

```

    case Nil then show ?case by (simp add: sources-Nil)
next
case (Cons b bs)
assume p0:  $\forall s\ t\ u. ((\text{reachable0}\ s) \wedge (\text{reachable0}\ t) \wedge \text{dynamic-step-consistent} \wedge \text{dynamic-local-respect} \wedge (s \approx (\text{sources}\ bs\ u\ s) \approx t)) \longrightarrow (\text{sources}\ bs\ u\ s) = (\text{sources}\ bs\ u\ t))$ 
then show ?case
proof -
{
  fix s t u
  assume p1:  $\text{reachable0}\ s$ 
  assume p2:  $\text{reachable0}\ t$ 
  assume p3:  $\text{dynamic-step-consistent}$ 
  assume p5:  $\text{dynamic-local-respect}$ 
  assume p9:  $(s \approx (\text{sources}\ (b \# bs)\ u\ s) \approx t)$ 
  have a2:  $((\text{step}\ s\ b) \approx (\text{sources}\ bs\ u\ (\text{step}\ s\ b)) \approx (\text{step}\ t\ b))$ 
    using lemma-1 p1 p2 p3 policy-respect p5 p9 by blast
  have a3:  $\text{sources}\ (b \# bs)\ u\ s = \text{sources}\ (b \# bs)\ u\ t$ 
    proof (cases the (domain b)  $\in$  (sources (b # bs) u s))
    assume b0: the (domain b)  $\in$  (sources (b # bs) u s)
    have b1:  $s \sim (\text{the}(\text{domain}\ b)) \sim t$ 
      using b0 p9 by auto
    have b3:  $\text{interferes}\ (\text{the}\ (\text{domain}\ b))\ s\ u = \text{interferes}\ (\text{the}\ (\text{domain}\ b))\ t\ u$ 
      using p1 p2 policy-respect p9 sources-refl by fastforce
    have b4:  $(\text{sources}\ bs\ u\ (\text{step}\ s\ b)) = (\text{sources}\ bs\ u\ (\text{step}\ t\ b))$ 
      using a2 p0 p1 p2 p3 p5 reachableStep by blast
    have b5:  $\forall v. v \in \text{sources}\ bs\ u\ (\text{step}\ s\ b) \longrightarrow \text{interferes}\ (\text{the}\ (\text{domain}\ b))\ t\ v$ 
      using p1 p2 ivpeq-def policy-respect p9 sources-Cons by fastforce
    then show sources (b # bs) u s = sources (b # bs) u t
      using b4 b5 sources-Cons by auto
    next
    assume b0: the (domain b)  $\notin$  (sources (b # bs) u s)
    have b1:  $\text{sources}\ (b \# bs)\ u\ s = \text{sources}\ bs\ u\ (\text{step}\ s\ b)$ 
      using b0 sources-Cons by auto
    have b2:  $(\text{sources}\ bs\ u\ (\text{step}\ s\ b)) = (\text{sources}\ bs\ u\ (\text{step}\ t\ b))$ 
      using a2 p0 p1 p2 p3 p5 reachableStep by blast
    have b3:  $\forall v. v \in \text{sources}\ bs\ u\ (\text{step}\ s\ b) \longrightarrow \neg \text{interferes}\ (\text{the}\ (\text{domain}\ b))\ s\ v$ 
      using b0 sources-Cons by auto
    have b4:  $\forall v. v \in \text{sources}\ bs\ u\ (\text{step}\ s\ b) \longrightarrow \neg \text{interferes}\ (\text{the}\ (\text{domain}\ b))\ t\ v$ 
      using b1 b3 p1 p2 p9 policy-respect by fastforce
    have b5:  $\forall v. v \in \text{sources}\ bs\ u\ (\text{step}\ t\ b) \longrightarrow \neg \text{interferes}\ (\text{the}\ (\text{domain}\ b))\ s\ v$ 

```

```

(domain b)) t v
  by (simp add: b2 b4)
  have b6: the (domain b)  $\notin$  (sources (b # bs) u t)
  using b0 b2 b5 sources.simps(2) by auto
  have b7: sources (b # bs) u t = sources bs u (step t b)
  using b6 sources-Cons by auto
  then show ?thesis
    by (simp add: b1 b2)
  qed
}
then show ?thesis by blast
qed
}
then show ?thesis by blast
qed

lemma ipurge-eq:  $\forall s\ t\ as\ u.$  reachable0 s  $\wedge$ 
  reachable0 t  $\wedge$ 
  dynamic-step-consistent  $\wedge$ 
  dynamic-local-respect  $\wedge$ 
  ( $s \approx$  (sources as u s)  $\approx$  t)
 $\longrightarrow$  (ipurge as u s) = (ipurge as u t)

proof -
{
  fix as
  have  $\forall s\ t\ u.$  reachable0 s  $\wedge$ 
    reachable0 t  $\wedge$ 
    dynamic-step-consistent  $\wedge$ 
    dynamic-local-respect  $\wedge$ 
    ( $s \approx$  (sources as u s)  $\approx$  t)
 $\longrightarrow$  (ipurge as u s) = (ipurge as u t)

  proof(induct as)
    case Nil then show ?case by (simp add: sources-Nil)
  next
    case (Cons b bs)
    assume p0:  $\forall s\ t\ u.$  (reachable0 s
       $\wedge$  (reachable0 t)
       $\wedge$  dynamic-step-consistent
       $\wedge$  dynamic-local-respect
       $\wedge$  ( $s \approx$  (sources bs u s)  $\approx$  t))
       $\longrightarrow$  (ipurge bs u s) = (ipurge bs u t)

    then show ?case
      proof -
      {
        fix s t u
        assume p1: reachable0 s
        assume p2: reachable0 t

```

```

    assume p3: dynamic-step-consistent
    assume p5: dynamic-local-respect
    assume p9:  $(s \approx (\text{sources } (b \# bs) \ u \ s) \approx t)$ 
    have a1:  $((\text{step } s \ b) \approx (\text{sources } bs \ u \ (\text{step } s \ b)) \approx (\text{step } t \ b))$ 
      using lemma-1 p1 p2 p3 p5 p9 by blast
    have a2:  $(\text{ipurge } bs \ u \ (\text{step } s \ b)) = (\text{ipurge } bs \ u \ (\text{step } t \ b))$ 
      using a1 p0 p1 p2 p3 p5 p9 reachableStep by blast
    have a3:  $\text{sources } (b \# bs) \ u \ s = \text{sources } (b \# bs) \ u \ t$ 
      using p1 p2 p3 p5 p9 sources-eq1 by blast
    have a4:  $\text{ipurge } (b \# bs) \ u \ s = \text{ipurge } (b \# bs) \ u \ t$ 
    proof (cases the (domain b)  $\in$  (sources (b # bs) u s))
      assume b0: the (domain b)  $\in$  (sources (b # bs) u s)
      have b1:  $s \sim (\text{the}(\text{domain } b)) \sim t$ 
        using b0 p9 by auto
      have b3: the (domain b)  $\in$  (sources (b # bs) u t)
        using a3 b0 by auto
      then show ?thesis
        using a2 b0 ipurge-Cons by auto
    next
      assume b0: the (domain b)  $\notin$  (sources (b # bs) u s)
      have b1:  $\text{sources } (b \# bs) \ u \ s = \text{sources } bs \ u \ (\text{step } s \ b)$ 
        using b0 sources-Cons by auto
      have b3:  $\forall v. v \in \text{sources } bs \ u \ (\text{step } s \ b) \longrightarrow \neg \text{interferes } (\text{the}$ 
        (domain b)) s v
      using b0 sources-Cons by auto
      have b4:  $\forall v. v \in \text{sources } bs \ u \ (\text{step } s \ b) \longrightarrow \neg \text{interferes } (\text{the}$ 
        (domain b)) t v
      using b1 b3 p1 p2 p9 policy-respect by fastforce
      have b5: the (domain b)  $\notin$  (sources (b # bs) u t)
        using a3 b1 b4 interf-reflexive by auto
      have b6:  $\text{ipurge } (b \# bs) \ u \ s = \text{ipurge } bs \ u \ (\text{step } s \ b)$ 
        using b0 by auto
      have b7:  $\text{ipurge } (b \# bs) \ u \ t = \text{ipurge } bs \ u \ (\text{step } t \ b)$ 
        using b5 by auto
      then show ?thesis
        using b6 b7 a2 by auto
    qed
  }
  then show ?thesis by blast
  qed
}
then show ?thesis by blast
qed

```

```

lemma non-influence-lemma:  $\forall s \ t \text{ as } u. \text{reachable0 } s \wedge$ 
   $\text{reachable0 } t \wedge$ 
   $\text{dynamic-step-consistent} \wedge$ 
   $\text{dynamic-local-respect} \wedge$ 

```

```

      (s ≈ (sources as u s) ≈ t)
      → ((s as ≅ t (ipurge as u t) @ u))
proof -
{
  fix as
  have ∀ s t u. reachable0 s ∧
    reachable0 t ∧
    dynamic-step-consistent ∧
    dynamic-local-respect ∧
    (s ≈ (sources as u s) ≈ t)
    → ((s as ≅ t (ipurge as u t) @ u))
proof (induct as)
  case Nil show ?case using sources-Nil by auto
next
  case (Cons b bs)
  assume p0: ∀ s t u. ((reachable0 s)
    ∧ (reachable0 t)
    ∧ dynamic-step-consistent
    ∧ dynamic-local-respect
    ∧ (s ≈ (sources bs u s) ≈ t)) →
    ((s bs ≅ t (ipurge bs u t) @ u))
  then show ?case
  proof -
  {
    fix s t u
    assume p1: reachable0 s
    assume p2: reachable0 t
    assume p3: dynamic-step-consistent
    assume p4: dynamic-local-respect
    assume p8: (s ≈ (sources (b # bs) u s) ≈ t)
    have a1: ((step s b) ≈ (sources bs u (step s b)) ≈ (step t b))
      using lemma-1 p1 p2 p3 p4 p8 by blast
    have s b # bs ≅ t ipurge (b # bs) u t @ u
    proof (cases the (domain b) ∈ sources (b # bs) u s)
      assume b0: the (domain b) ∈ sources (b # bs) u s
      have b1: interferes (the (domain b)) s u = interferes (the (domain
b)) t u
      using p1 p2 policy-respect p8 sources-refl by fastforce
      have b2: ∀ v. v ∈ sources bs u (step s b)
        → interferes (the (domain b)) s v = interferes (the (domain
b)) t v
      using p1 p2 ivpeq-def policy-respect p8 sources-Cons by fastforce
      have b3: ipurge (b # bs) u t = b # (ipurge bs u (step t b))
      by (metis b0 ipurge-Cons p1 p2 p3 p4 p8 sources-eq1)
      have b4: (((step s b) bs ≅ (step t b) (ipurge bs u (step t b)) @ u))
        using a1 p0 p1 p2 p3 p4 reachableStep by blast
      show ?thesis
      using b3 b4 by auto
    next

```

```

      assume b0: the (domain b)  $\notin$  sources (b # bs) u s
      have b1: ipurge (b # bs) u t = (ipurge bs u (step t b))
    by (metis a1 b0 ipurge-Cons ipurge-eq p1 p2 p3 p4 p8 reachableStep)
      have b2: (s  $\approx$  (sources bs u (step s b))  $\approx$  (step s b))
        using b0 lemma-2 p1 p4 by blast
      have b3: (s  $\approx$  (sources bs u (step s b))  $\approx$  t)
        using b0 lemma-1-sub-3 p8 by blast
      have b4: ((step s b)  $\approx$  (sources bs u (step s b))  $\approx$  t)
    by (meson b3 b2 vpeq-def vpeq-symmetric-lemma vpeq-transitive-lemma)
      have b5: (((step s b) bs  $\cong$  t (ipurge bs u t) @ u))
        using b4 p0 p1 p2 p3 p4 reachableStep by blast
      have b6: (t  $\approx$  (sources bs u (step s b))  $\approx$  (step t b))
        using p1 p2 b0 lemma-1-sub-2 p4 p8 by blast
      have b7: ipurge bs u t = ipurge bs u (step t b)
        by (metis a1 b4 ipurge-eq p1 p2 p3 p4 reachableStep)
      have b8: (((step s b) bs  $\cong$  t (ipurge bs u (step t b)) @ u))
        using b5 b7 by auto
      then show ?thesis
        using b1 observ-equivalence-def run-Cons by auto
    qed
  }
  then show ?thesis by blast
qed
}
then show ?thesis by blast
qed

```

27.14 Interference framework of information flow security properties

theorem *nonintf-impl-weak*: *noninterference* \impl *weak-noninterference*
 by (metis *noninterference-def* *observ-equiv-sym* *observ-equiv-trans* *reachable-s0* *weak-noninterference-def*)

theorem *wk-nonintf-r-impl-wk-nonintf*: *weak-noninterference-r* \impl *weak-noninterference*
 using *reachable-s0* by auto

theorem *nonintf-r-impl-noninterf*: *noninterference-r* \impl *noninterference*
 using *noninterference-def* *noninterference-r-def* *reachable-s0* by auto

theorem *nonintf-r-impl-wk-nonintf-r*: *noninterference-r* \impl *weak-noninterference-r*
 by (metis *noninterference-r-def* *observ-equiv-sym* *observ-equiv-trans* *weak-noninterference-r-def*)

lemma *noninf-impl-nonintf-r*: *noninfluence* \impl *noninterference-r*
 using *vpeq-def* *noninfluence-def* *noninterference-r-def* *vpeq-reflexive-lemma*
 by blast

lemma *noninf-impl-nonlk*: *noninfluence* \impl *nonleakage*

```

using noninterference-r-def nonleakage-def observ-equiv-sym
observ-equiv-trans noninfluence-def noninf-impl-nonintf-r by blast

lemma wk-noninfl-impl-nonlk: weak-noninfluence  $\impl$  nonleakage
using weak-noninfluence-def nonleakage-def by blast

lemma wk-noninfl-impl-wk-nonintf-r: weak-noninfluence  $\impl$  weak-noninterference-r
using ivpeq-def weak-noninfluence-def vpeq-reflexive-lemma weak-noninterference-r-def
by blast

lemma sources-step2:
 $\llbracket \text{reachable0 } s; (\text{the } (\text{domain } a)) @ s \text{ } d \rrbracket \impl \text{sources } [a] \text{ } d \text{ } s = \{\text{the } (\text{domain } a), d\}$ 
apply(auto simp: sources-Cons sources-Nil enabled dest: enabled)
done

lemma exec-equiv-both:
 $\llbracket \text{reachable0 } C1; \text{reachable0 } C2; (\text{step } C1 \text{ } a) \text{ } as \cong (\text{step } C2 \text{ } b) \text{ } bs @ u \rrbracket$ 
 $\impl (C1 \text{ } (a \# as) \cong C2 \text{ } (b \# bs) @ u)$ 
by auto

lemma sources-unwinding-step:
 $\llbracket \text{reachable0 } s; \text{reachable0 } t; s \approx (\text{sources } (a \# as) \text{ } d \text{ } s) \approx t; \text{dynamic-step-consistent} \rrbracket$ 
 $\impl ((\text{step } s \text{ } a) \approx (\text{sources } as \text{ } d \text{ } (\text{step } s \text{ } a)) \approx (\text{step } t \text{ } a))$ 
apply(clarsimp simp: ivpeq-def sources-Cons)
using UnionI dynamic-step-consistent-def by blast

lemma nonlk-imp-sc: nonleakage  $\impl$  dynamic-step-consistent
proof –
assume p0: nonleakage
have p1:  $\forall as \text{ } d \text{ } s \text{ } t. \text{reachable0 } s \wedge \text{reachable0 } t$ 
 $\wedge (s \approx (\text{sources } as \text{ } d \text{ } s) \approx t) \longrightarrow (s \text{ } as \cong t \text{ } as @ d)$ 
using p0 nonleakage-def by auto
have p2:  $\forall a \text{ } d \text{ } s \text{ } t. \text{reachable0 } s \wedge \text{reachable0 } t \wedge (s \sim d \sim t) \wedge$ 
 $((\text{the } (\text{domain } a)) @ s \text{ } d \longrightarrow (s \sim (\text{the } (\text{domain } a)) \sim t))$ 
 $\longrightarrow ((\text{step } s \text{ } a) \sim d \sim (\text{step } t \text{ } a))$ 
proof –
{
fix a d s t
assume a0:  $\text{reachable0 } s \wedge \text{reachable0 } t \wedge (s \sim d \sim t) \wedge$ 
 $((\text{the } (\text{domain } a)) @ s \text{ } d \longrightarrow (s \sim (\text{the } (\text{domain } a)) \sim t))$ 
have a4:  $s \approx (\text{sources } [] \text{ } d \text{ } s) \approx t$ 
using a0 sources-Nil by auto
have a5:  $(s \text{ } [] \cong t \text{ } [] @ d)$ 
using a4 a0 p1 by auto
have a6:  $((\text{step } s \text{ } a) \sim d \sim (\text{step } t \text{ } a))$ 
proof (cases  $(\text{the } (\text{domain } a)) @ s \text{ } d$ )
assume b0:  $(\text{the } (\text{domain } a)) @ s \text{ } d$ 

```



```

    have b1: sources [a] d s = {d, (the (domain a))}
      using b0 sources-Cons sources-Nil by auto
    have c0: (s ~ (the (domain a)) ~ t)
      using b0 a0 by auto
    have b2: s ≈ (sources [a] d s) ≈ t
      using b1 a0 c0 by auto
    have b3: (s [a] ≅ t [a] @ d)
      using b2 a0 p1 by auto
    have b4: ((step s a) ~ d ~ (step t a))
      using b3 by auto
    then show ?thesis by auto
  next
    assume b0: ¬((the (domain a))@s d)
    have b1: sources [a] d s = {d}
      using b0 sources-Cons sources-Nil by auto
    have b2: (s ≈ (sources [a] d s) ≈ t)
      using b1 a0 by auto
    have b3: (s [a] ≅ t [a] @ d)
      using b2 a0 p1 by auto
    have b4: ((step s a) ~ d ~ (step t a))
      using b3 by auto
    then show ?thesis by auto
  qed
}
then show ?thesis
  by auto
qed
then show ?thesis by auto
qed

lemma sc-imp-nonlk: dynamic-step-consistent ⟹ nonleakage
proof -
  assume p0: dynamic-step-consistent
  have p1: ∀ a d s t. reachable0 s ∧ reachable0 t ∧ (s ~ d ~ t) ∧
    (s ~ (the (domain a)) ~ t) ⟶ ((step s a) ~ d ~ (step t a))
    using p0 dynamic-step-consistent-def by auto
  have p2: ∀ as d s t. reachable0 s ∧ reachable0 t
    ∧ (s ≈ (sources as d s) ≈ t) ⟶ (s as ≅ t as @ d)
  proof -
    {
      fix as
      have ∀ d s t. reachable0 s ∧ reachable0 t
        ∧ (s ≈ (sources as d s) ≈ t) ⟶ (s as ≅ t as @ d)
      proof (induct as)
        case Nil show ?case using sources-refl by auto
      next
        case (Cons b bs)
        assume a0: ∀ d s t. reachable0 s ∧ reachable0 t
          ∧ (s ≈ (sources bs d s) ≈ t) ⟶ (s bs ≅ t bs @ d)

```

```

show ?case
proof -
{
  fix d s t
  assume b0: reachable0 s  $\wedge$  reachable0 t
  assume b1: (s  $\approx$  (sources (b#bs) d s)  $\approx$  t)
  have b2: ((step s b)  $\approx$  (sources bs d (step s b)))  $\approx$  (step t b))
    using b0 b1 p0 sources-unwinding-step by auto
  have b3: (step s b) bs  $\cong$  (step t b) bs @ d
    using Cons.hyps b0 b2 reachableStep by blast
  have b4: s b # bs  $\cong$  t b # bs @ d
    using b3 by auto
}
then show ?thesis by auto
qed
qed
}
then show ?thesis by auto
qed
then show ?thesis by auto
qed

```

theorem sc-eq-nonlk: dynamic-step-consistent = nonleakage
using nonlk-imp-sc sc-imp-nonlk **by** blast

lemma noninf-imp-dlr: noninfluence \implies dynamic-local-respect

```

proof -
  assume p0: noninfluence
  have p1:  $\forall$  d as s t. reachable0 s  $\wedge$  reachable0 t
     $\wedge$  (s  $\approx$  (sources as d s)  $\approx$  t)
     $\longrightarrow$  (s as  $\cong$  t (ipurge as d t) @ d)
  using p0 noninfluence-def by auto
  have  $\forall$  a d s. reachable0 s  $\wedge$   $\neg$ ((the (domain a)) @ s d)
     $\longrightarrow$  (s  $\sim$  d  $\sim$  (step s a))
  proof -
  {
    fix a d s
    assume a0: reachable0 s  $\wedge$   $\neg$ ((the (domain a)) @ s d)
    have a1: sources [a] d s = {d}
      using a0 sources-Cons sources-Nil by auto
    have a2: (ipurge [a] d s) = []
      using a0 a1 interf-reflexive by auto
    have a3: s  $\sim$  d  $\sim$  s
      using vpeq-reflexive-lemma by auto
    have a4: (s  $\approx$  (sources [a] d s)  $\approx$  s)
      using a1 a3 by auto
    have a5: (s [a]  $\cong$  s (ipurge [a] d s) @ d)
      using a4 a0 p1 by auto
    have a6: (s [a]  $\cong$  s [] @ d)

```

```

      using a5 a2 by auto
      have a7: (s ~ d ~ (step s a))
      using a6 vpeq-symmetric-lemma by auto
    }
  then show ?thesis by auto
qed
then show ?thesis by auto
qed

lemma noninf-imp-sc: noninfluence  $\implies$  dynamic-step-consistent
  using nonlk-imp-sc noninf-impl-nonlk by blast

theorem UnwindingTheorem :  $\llbracket$ dynamic-step-consistent;
  dynamic-local-respect $\rrbracket$ 
 $\implies$  noninfluence

proof -
  assume p3: dynamic-step-consistent
  assume p4: dynamic-local-respect
  {
    fix as d
    have  $\forall s t. \text{reachable0 } s \wedge$ 
       $\text{reachable0 } t \wedge$ 
       $(s \approx (\text{sources as } d \ s) \approx t)$ 
       $\longrightarrow ((s \text{ as } \cong t \ (\text{ipurge as } d \ t) \ @ \ d))$ 
    proof(induct as)
      case Nil show ?case using sources-Nil by auto
    next
      case (Cons b bs)
      assume p0:  $\forall s t. \text{reachable0 } s \wedge$ 
         $\text{reachable0 } t \wedge$ 
         $(s \approx (\text{sources bs } d \ s) \approx t)$ 
         $\longrightarrow ((s \text{ bs } \cong t \ (\text{ipurge bs } d \ t) \ @ \ d))$ 
      then show ?case
        proof -
          {
            fix s t
            assume p1:  $\text{reachable0 } s$ 
            assume p2:  $\text{reachable0 } t$ 
            assume p8:  $(s \approx (\text{sources } (b \ \# \ bs) \ d \ s) \approx t)$ 
            have a1:  $((\text{step } s \ b) \approx (\text{sources bs } d \ (\text{step } s \ b)) \approx (\text{step } t \ b))$ 
              using lemma-1 p1 p2 p3 p4 p8 by blast
            have a2:  $s \ b \ \# \ bs \cong t \ \text{ipurge } (b \ \# \ bs) \ d \ t \ @ \ d$ 
              proof (cases the (domain b)  $\in$  sources (b # bs) d s)
                assume b0: the (domain b)  $\in$  sources (b # bs) d s
                have b1:  $\text{interferes } (\text{the } (\text{domain } b)) \ s \ d = \text{interferes } (\text{the } (\text{domain } b)) \ t \ d$ 
                  using p1 p2 policy-respect p8 sources-refl by fastforce
                have b2:  $\forall v. v \in \text{sources bs } d \ (\text{step } s \ b)$ 
                   $\longrightarrow \text{interferes } (\text{the } (\text{domain } b)) \ s \ v = \text{interferes } (\text{the } (\text{domain } b)) \ t \ v$ 

```

b)) $t \ v$

```

    using p1 p2 ivpeq-def policy-respect p8 sources-Cons by fastforce
    have b3: ipurge (b # bs) d t = b # (ipurge bs d (step t b))
    by (metis b0 ipurge-Cons p1 p2 p3 p4 p8 sources-eq1)
    have b4: (((step s b) bs  $\cong$  (step t b) (ipurge bs d (step t b)) @ d))
    using a1 p0 p1 p2 p3 p4 reachableStep by blast
    then show ?thesis
    using b3 b4 by auto
  next
    assume b0: the (domain b)  $\notin$  sources (b # bs) d s
    have b1: ipurge (b # bs) d t = (ipurge bs d (step t b))
    by (metis a1 b0 ipurge-Cons ipurge-eq p1 p2 p3 p4 p8 reachableStep)
    have b2: (s  $\approx$  (sources bs d (step s b))  $\approx$  (step s b))
    using b0 lemma-2 p1 p4 by blast
    have b3: (s  $\approx$  (sources bs d (step s b))  $\approx$  t)
    using b0 lemma-1-sub-3 p8 by blast
    have b4: ((step s b)  $\approx$  (sources bs d (step s b))  $\approx$  t)
    by (meson b3 b2 ivpeq-def vpeq-symmetric-lemma vpeq-transitive-lemma)
    have b5: (((step s b) bs  $\cong$  t (ipurge bs d t) @ d))
    using b4 p0 p1 p2 p3 p4 reachableStep by blast
    have b6: (t  $\approx$  (sources bs d (step s b))  $\approx$  (step t b))
    using p1 p2 b0 lemma-1-sub-2 p4 p8 by blast
    have b7: ipurge bs d t = ipurge bs d (step t b)
    by (metis a1 b4 ipurge-eq p1 p2 p3 p4 reachableStep)
    have b8: (((step s b) bs  $\cong$  t (ipurge bs d (step t b)) @ d))
    using b5 b7 by auto
    then show ?thesis
    using b1 observ-equivalence-def run-Cons by auto
  qed
}
then show ?thesis by blast
qed
qed
}
then show ?thesis using noninfluence-def by blast
qed

theorem UnwindingTheorem1 : [[dynamic-weakly-step-consistent;
dynamic-local-respect]]  $\implies$  noninfluence
using UnwindingTheorem weak-with-step-cons by blast

theorem uc-eq-noninf : (dynamic-step-consistent  $\wedge$  dynamic-local-respect) =
noninfluence
using UnwindingTheorem1 step-cons-impl-weak noninf-imp-dlr noninf-imp-sc
by blast

theorem noninf-impl-weak:noninfluence  $\implies$  weak-noninfluence

```

```

proof –
assume  $p0$ : noninfluence
have  $p1$ :  $\forall d \text{ as } s \ t. \text{reachable0 } s \wedge \text{reachable0 } t$ 
            $\wedge (s \approx (\text{sources as } d \ s) \approx t)$ 
            $\longrightarrow (s \text{ as } \cong t \text{ (ipurge as } d \ t) @ d)$ 
using  $p0$  noninfluence-def by auto
have  $p2$ : (dynamic-step-consistent  $\wedge$  dynamic-local-respect)
using  $p0$  uc-eq-noninf by auto
have  $\forall d \text{ as } bs \ s \ t. \text{reachable0 } s \wedge \text{reachable0 } t \wedge (s \approx (\text{sources as } d \ s) \approx t)$ 
            $\wedge \text{ipurge as } d \ t = \text{ipurge bs } d \ t$ 
            $\longrightarrow (s \text{ as } \cong t \text{ bs } @ d)$ 
proof –
{
  fix  $d \text{ as } bs \ s \ t$ 
  assume  $a0$ :  $\text{reachable0 } s \wedge \text{reachable0 } t \wedge (s \approx (\text{sources as } d \ s) \approx t)$ 
            $\wedge \text{ipurge as } d \ t = \text{ipurge bs } d \ t$ 
  have  $a4$ : noninterference-r
  using noninf-impl-nonintf-r  $p0$  by auto
  have  $a7$ : weak-noninterference-r
  using  $a4$  nonintf-r-impl-wk-nonintf-r by auto
  have  $a6$ :  $\text{ipurge as } d \ s = \text{ipurge as } d \ t$ 
  using  $a0$   $p2$  ipurge-eq by auto
  have  $b1$ :  $(s \text{ as } \cong t \text{ (ipurge as } d \ t) @ d)$ 
  using  $a0$   $p1$  by auto
  have  $b4$ :  $(s \text{ as } \cong t \text{ as } @ d)$ 
  using  $a0$  noninf-imp-sc nonleakage-def  $p0$  sc-imp-nonlk by blast
  have  $b5$ :  $(t \text{ bs } \cong t \text{ (ipurge bs } d \ t) @ d)$ 
  using  $a0$   $a4$  by auto
  have  $b6$ :  $(t \text{ bs } \cong t \text{ (ipurge as } d \ t) @ d)$ 
  using  $b5$   $a0$  by auto
  have  $b7$ :  $(s \text{ as } \cong t \text{ bs } @ d)$ 
  using  $a0$   $b1$   $b6$  observ-equiv-sym observ-equiv-trans by blast
}
then show ?thesis by auto
qed
then show ?thesis by auto
qed

```

lemma *wk-nonintf-r-and-nonlk-impl-noninfl*: $\llbracket \text{weak-noninterference-r}; \text{nonleakage} \rrbracket \implies \text{weak-noninfluence}$

```

proof –
assume  $p0$ : weak-noninterference-r
assume  $p1$ : nonleakage
have  $p2$ :  $\forall d \text{ as } bs \ s. \text{reachable0 } s \wedge \text{ipurge as } d \ s = \text{ipurge bs } d \ s$ 
            $\longrightarrow (s \text{ as } \cong s \text{ bs } @ d)$ 
using weak-noninterference-r-def  $p0$  by auto
have  $p3$ :  $\forall d \text{ as } s \ t. \text{reachable0 } s \wedge \text{reachable0 } t$ 
            $\wedge (s \approx (\text{sources as } d \ s) \approx t) \longrightarrow (s \text{ as } \cong t \text{ as } @ d)$ 

```

```

    using nonleakage-def p1 by auto
    have  $\forall d \text{ as } bs \ s \ t. \text{reachable0 } s \wedge \text{reachable0 } t \wedge (s \approx (\text{sources as } d \ s) \approx$ 
t)
 $\wedge \text{ipurge as } d \ t = \text{ipurge bs } d \ t$ 
 $\longrightarrow (s \text{ as } \cong t \text{ bs } @ d)$ 

  proof -
  {
    fix d as bs s t
    assume a0:  $\text{reachable0 } s \wedge \text{reachable0 } t \wedge (s \approx (\text{sources as } d \ s) \approx t)$ 
 $\wedge \text{ipurge as } d \ t = \text{ipurge bs } d \ t$ 
    have a1:  $s \text{ as } \cong t \text{ as } @ d$ 
    using a0 p3 by blast
    have a2:  $t \text{ as } \cong t \text{ bs } @ d$ 
    using a0 p2 by auto
    have a3:  $(s \text{ as } \cong t \text{ bs } @ d)$ 
    using a0 a1 a2 observ-equiv-trans by blast
  }
  then show ?thesis by auto
qed
then show ?thesis by auto
qed

lemma nonintf-r-and-nonlk-impl-noninfl:  $\llbracket \text{noninterference-r}; \text{nonleakage} \rrbracket \Longrightarrow$ 
noninfluence
  proof -
    assume p0: noninterference-r
    assume p1: nonleakage
    have p2:  $\forall d \text{ as } s. \text{reachable0 } s \longrightarrow (s \text{ as } \cong s \ (\text{ipurge as } d \ s) @ d)$ 
    using p0 noninterference-r-def by auto
    have p3:  $\forall d \text{ as } s \ t. \text{reachable0 } s \wedge \text{reachable0 } t$ 
 $\wedge (s \approx (\text{sources as } d \ s) \approx t) \longrightarrow (s \text{ as } \cong t \text{ as } @ d)$ 
    using p1 nonleakage-def by auto
    have  $\forall d \text{ as } s \ t. \text{reachable0 } s \wedge \text{reachable0 } t$ 
 $\wedge (s \approx (\text{sources as } d \ s) \approx t)$ 
 $\longrightarrow (s \text{ as } \cong t \ (\text{ipurge as } d \ t) @ d)$ 

  proof -
  {
    fix d as bs s t
    assume a0:  $\text{reachable0 } s \wedge \text{reachable0 } t$ 
 $\wedge (s \approx (\text{sources as } d \ s) \approx t)$ 
    have a1:  $s \text{ as } \cong t \text{ as } @ d$ 
    using p3 a0 by blast
    have a2:  $s \text{ as } \cong s \ (\text{ipurge as } d \ s) @ d$ 
    using a0 p2 by fast
    have a3:  $t \text{ as } \cong t \ (\text{ipurge as } d \ t) @ d$ 
    using a0 p2 by fast
    have  $s \text{ as } \cong t \ (\text{ipurge as } d \ t) @ d$ 
    using a0 a1 a3 observ-equiv-trans by blast
  }

```

```

    then show ?thesis by auto
  qed
  then show ?thesis using noninfluence-def by blast
qed

theorem nonintf-r-and-nonlk-eq-strnoninfl: (noninterference-r  $\wedge$  nonleakage)
= noninfluence
  using nonintf-r-and-nonlk-impl-noninfl noninf-impl-nonintf-r noninf-impl-nonlk
  by blast

end

end

```

28 Security policy model of Linux Security Module

```

theory
  LSM-SPM
  imports
    Dynamic-model
begin

locale LSM-Security-model = SM-enabled s0 step domain vpeq interferes
  for s0 :: 's and
    step :: 's  $\Rightarrow$  'e  $\Rightarrow$  's and
    domain :: 'e  $\Rightarrow$  ('d option) and
    vpeq :: 's  $\Rightarrow$  'd  $\Rightarrow$  's  $\Rightarrow$  bool ((-  $\sim$  -  $\sim$  -)) and
    interferes :: 'd  $\Rightarrow$  's  $\Rightarrow$  'd  $\Rightarrow$  bool ((- @ - -))
  +

  fixes observe :: 's  $\Rightarrow$  'd  $\Rightarrow$  'obj set (infixl 65)
    and alter :: 's  $\Rightarrow$  'd  $\Rightarrow$  'obj set (infixl 66)
    and contents :: 's  $\Rightarrow$  'obj  $\Rightarrow$  'v

  assumes contents-consistent: ( $\forall$  s u t. (s  $\sim$  u  $\sim$  t)  $\longrightarrow$  ( $\forall$  n  $\in$  observe s u.
    contents s n = contents t n))
    and observed-consistent : ( $\forall$  s t u. ((s  $\sim$  u  $\sim$  t)  $\longrightarrow$  s u = t u))
    and ac-interferes :  $\forall$  s u v. (alter s u  $\cap$  observe s v)  $\neq$  {}  $\longrightarrow$  (u @ s v)
begin

definition drma2s :: bool
  where drma2s  $\equiv$  ( $\forall$  s t a n. (n  $\in$  alter s (the(domain a))  $\cap$  alter t (the(domain
    a))))  $\wedge$ 
    (s  $\sim$  (the (domain a))  $\sim$  t)  $\wedge$ 
    (contents s n = contents t n)

```

$\longrightarrow (\text{contents } (\text{step } s \ a) \ n = \text{contents } (\text{step } t \ a) \ n))$

definition *drma2* :: *bool*

where *drma2* $\equiv (\forall \ s \ t \ a \ n. (\ s \sim \text{the}(\text{domain } a) \sim t) \wedge$
 $((\text{contents } (\text{step } s \ a) \ n) \neq (\text{contents } s \ n)$
 $\vee (\text{contents } (\text{step } t \ a) \ n) \neq (\text{contents } t \ n)))$
 $\longrightarrow (\text{contents } (\text{step } s \ a) \ n = \text{contents } (\text{step } t \ a) \ n))$

definition *drma3s* :: *bool*

where *drma3s* $\equiv (\forall \ a \ n \ s. (\text{contents } (\text{step } s \ a) \ n) \neq (\text{contents } s \ n)$
 $\longrightarrow n \in \text{alter } s \ (\text{the}(\text{domain } a)) \wedge n \in \text{alter } (\text{step } s \ a) \ (\text{the}(\text{domain } a)))$

definition *drma4s* :: *bool*

where *drma4s* $\equiv (\forall \ s \ u \ a. (((\text{step } s \ a) \ u) - (s \ u)) \subseteq (s \ (\text{the}(\text{domain } a))))$

definition *drma5s* :: *bool*

where *drma5s* $\equiv (\forall \ s \ t \ u \ v. (u \ @ \ s \ v) \wedge (u \ @ \ t \ v))$

definition *drma5s'* $\equiv \forall \ s \ t \ u \ v. (s \sim u \sim t) \wedge (s \sim v \sim t) \longrightarrow (\text{alter } s \ v \cap$
 $\text{observe } s \ u) = (\text{alter } t \ v \cap \text{observe } t \ u)$

definition *drma3* $\equiv (\forall \ a \ n \ s. (\text{contents } (\text{step } s \ a) \ n) \neq (\text{contents } s \ n)$
 $\longrightarrow n \in \text{alter } s \ (\text{the}(\text{domain } a)))$

end

end

29 The Core of the linux kernel abstract event

theory

kernelA

imports

Linux-LSM-Model

LSM-SPM

begin

29.1 kernel

locale *Kernel* = *lsm* +

fixes *k-superblock* :: '*a* \Rightarrow *t-sb* \rightarrow *super-block*

fixes *sdentry* :: '*a* \Rightarrow *dname* \rightarrow *dentry*

fixes *sockets* :: '*a* \Rightarrow *socketdesp* \rightarrow *socket*

fixes *keys* :: '*a* \Rightarrow *keyid* \rightarrow *key*

fixes *kfiles* :: '*a* \Rightarrow *fname* \rightarrow *Files*

fixes *msg-msgs* :: '*a* \Rightarrow *msg-mid* \rightarrow *msg-msg*

fixes *msg-queues* :: '*a* \Rightarrow *msg-qid* \rightarrow *kern-ipc-perm*

fixes *contents* :: '*a* \Rightarrow *Obj* \Rightarrow '*v*


```

begin
definition current-process :: 'a  $\Rightarrow$  Task
  where current-process s = the (k-task s (current s))

definition current-cred :: 'a  $\Rightarrow$  Cred
  where current-cred s = cred (current-process s)

definition current-real-cred :: 'a  $\Rightarrow$  Cred
  where current-real-cred s = real-cred (current-process s)

definition task-cred :: 'a  $\Rightarrow$  Task  $\Rightarrow$  Cred
  where task-cred s t = real-cred t

definition get-process-by-pid :: 'a  $\Rightarrow$  nat  $\Rightarrow$  Task
  where get-process-by-pid s p  $\equiv$  the((k-task s) p)

definition get-processid :: 'a  $\Rightarrow$  Task  $\Rightarrow$  nat
  where get-processid s t  $\equiv$  SOME x . (k-task s) x = Some t

definition get-inode :: 'a  $\Rightarrow$  inum  $\Rightarrow$  inode
  where get-inode s inum  $\equiv$  SOME x . (inodes s) inum = Some x

definition get-dentry :: 'a  $\Rightarrow$  string  $\Rightarrow$  dentry
  where get-dentry s dname  $\equiv$  SOME x . (sdentry s) dname = Some x

definition get-file :: 'a  $\Rightarrow$  string  $\Rightarrow$  Files
  where get-file s name  $\equiv$  SOME x . (kfiles s) name = Some x

definition get-socket :: 'a  $\Rightarrow$  socketdsp  $\Rightarrow$  socket
  where get-socket s dsp  $\equiv$  SOME x . (sockets s) dsp = Some x

definition current-sbs :: 'a  $\Rightarrow$  t-sb set
  where current-sbs s = {t .  $\forall$  sb . k-superblock s = (k-superblock s) (t := Some sb) }

definition current-tasks :: 'a  $\Rightarrow$  process-id set
  where current-tasks s = {t .  $\forall$  sb . k-task s = (k-task s) (t := Some sb) }

datatype Event-sb =
  | Event-sb-copy-data process-id t-sb
  | Event-sb-remount process-id path Void
  | Event-sb-kern-mount process-id file-system-type int string string
  | Event-sb-show-options process-id seq-file t-sb
  | Event-sb-statfs process-id dentry
  | Event-sb-mount process-id string string string nat Void
  | Event-sb-umount process-id mount int
  | Event-sb-pivotroot process-id

```

```

| Event-set-mnt-opts process-id btrfs-fs-info super-block opts
| Event-set-sb-security process-id super-block dentry nfs-mount-info
| Event-sb-clone-mnt-opts process-id super-block dentry nfs-mount-info
| Event-sb-parse-opts-str process-id string opts

```

datatype *Event-tsk* =

```

  Event-prepare-creds process-id

```

```

| Event-sys-setreuid process-id kuid kuid
| Event-setpgid process-id pid-t pid-t
| Event-do-getpgid process-id pid-t
| Event-getsid process-id pid-t
| Event-getsecid process-id Task u32
| Event-task-setnice process-id Task int
| Event-set-task-ioprio process-id Task int
| Event-get-task-ioprio process-id Task
| Event-check-prlimit-permission process-id Task nat
| Event-do-prlimit process-id Task nat
| Event-task-setscheduler process-id Task
| Event-task-getscheduler process-id Task
| Event-task-movememory process-id Task
| Event-task-kill process-id Task siginfo int Cred
| Event-task-prctl process-id int nat nat nat nat

```

datatype *Event-Binder* = *Event-binder-set-context-mgr* process-id Task

```

| Event-binder-transaction process-id Task Task
| Event-binder-transfer-binder process-id Task Task
| Event-binder-transfer-file process-id Task Task

```

datatype *Event-Ptrace* = *Event-pttrace-access-check* process-id Task nat

```

| Event-pttrace-traceme process-id

```

datatype *Event-sys* = *Event-smack-syslog* process-id int

```

| Event-prepare-binprm process-id linux-binprm

```

datatype *Event-ipc* = *Event-ipc-permission* process-id kern-ipc-perm nat

```

| Event-ipc-getsecid process-id kern-ipc-perm
| Event-msg-queue-associate process-id kern-ipc-perm int
| Event-msg-queue-msgctl process-id kern-ipc-perm IPC-CMD
| Event-msg-queue-msgsnd process-id kern-ipc-perm msg-msg int
| Event-msg-queue-msgrcv process-id kern-ipc-perm msg-msg Task int int
| Event-shm-associate process-id kern-ipc-perm int
| Event-shm-shmctl process-id kern-ipc-perm IPC-CMD
| Event-shm-shmat process-id kern-ipc-perm string int
| Event-sem-associate process-id kern-ipc-perm int
| Event-sem-semctl process-id kern-ipc-perm IPC-CMD

```

```

| Event-sem-semop process-id kern-ipc-perm sembuf nat int

datatype Event-inode =
  | Event-vfs-link process-id dentry inode dentry inode
  | Event-vfs-unlink process-id inode dentry inode
  | Event-vfs-rmdir process-id inode dentry
  | Event-vfs-rename process-id inode dentry inode dentry inode nat
  | Event-inode-permission process-id inode int
  | Event-notify-change process-id dentry iattr inode
  | Event-fat-ioctl-set-attributes process-id Files
  | Event-vfs-getattr process-id path
  | Event-vfs-setxattr process-id dentry xattr string nat nat

  | Event-vfs-getxattr process-id dentry xattr string nat
  | Event-vfs-removexattr process-id dentry xattr
  | Event-xattr-getsecurity process-id inode xattr string int

  | Event-nfs4-listxattr-nfs4-label process-id inode string int
  | Event-sockfs-listxattr process-id dentry string int

datatype Event-network-sock = Event-unix-stream-connect process-id socket
sockaddr int int
  | Event-unix-dgram-connect process-id socket sockaddr int int
  | Event-unix-dgram-sendmsg process-id socket sockaddr int

  | Event-sys-bind' process-id int sockaddr int
  | Event-sys-connect' process-id int sockaddr int
  | Event-sock-sendmsg process-id socket msghdr
  | Event-sock-recvmsg process-id socket msghdr int
  | Event-sk-filter-trim-cap process-id sock sk-buff int
  | Event-sock-getsockopt process-id socket int int string int
  | Event-unix-get-peersec-dgram process-id socket scm-cookie

datatype Event-network = Event-sk-alloc
  | Event-sk-classify-flow
  | Event-req-classify-flow
  | Event-inet-conn-established
  | Event-secmark-relabel-packet
  | Event-secmark-refcount-inc
  | Event-secmark-refcount-dec
  | Event-tun-dev-alloc-Event
  | Event-tun-dev-free-Event
  | Event-tun-dev-create
  | Event-tun-dev-attach-queue
  | Event-tun-dev-attach
  | Event-tun-dev-open
  | Event-sctp-assoc-request

```

```

| Event-sctp-bind-connect
| Event-sctp-sk-clone

datatype Event-Infiniband = Event-ib-pkey-access
| Event-ib-endport-manage-subnet
| Event-ib-alloc-Event
| Event-ib-free-Event

datatype Event-Path = Event-path-unlink path dentry
| Event-path-mkdir path dentry nat
| Event-path-rmdir path dentry
| Event-path-mknod path dentry nat nat
| Event-path-truncate path
| Event-path-symlink path dentry string
| Event-path-link dentry path dentry
| Event-path-rename path dentry path
| Event-path-chmod path nat
| Event-path-chown path kuid kgid
| Event-path-chroot path

datatype Event-Key =
  Event-key-permission process-id key-ref-t Cred nat
| Event-key-getsecurity process-id key-serial-t string int

datatype Event-audit = Event-audit-data-to-entry process-id
| Event-audit-dupe-lsm-field process-id audit-field audit-field
| Event-audit-rule-known process-id audit-krule
| Event-audit-rule-match process-id int
| Event-audit-rule-free process-id audit-field

datatype Event-file =
  Event-do-ioctl process-id Files IOC-DIR nat
| Event-syscall-ioctl process-id nat IOC-DIR nat
| Event-ksys-ioctl process-id nat IOC-DIR nat
| Event-vm-mmap-pgoff process-id Files nat nat nat nat nat
| Event-do-sys-vm86 process-id
| Event-get-unmapped-area process-id Files nat
| Event-validate-mmap-request process-id Files nat

| Event-generic-setlease process-id Files int
| Event-syscall-lock process-id nat nat
| Event-do-lock-file-wait process-id Files int file-lock
| Event-file-fcntl process-id Files nat nat

| Event-file-send-sigiotask process-id Task fown-struct int
| Event-file-receive process-id Files

```

```

| Event-do-dentry-open process-id Files

datatype Event-d-instantiate-procattr = Event-d-instantiate process-id dentry inode option
| Event-d-instantiate-new process-id dentry inode
| Event-d-instantiate-anon' process-id dentry inode bool
| Event-d-add process-id dentry inode option
| Event-d-splice-alias process-id inode dentry
| Event-nfs-get-root process-id super-block nfs-fh string
| Event-proc-pid-attr-read process-id Files string nat loff-t
| Event-proc-pid-attr-write process-id Files string nat loff-t

datatype Event-ismaclabel = Event-nfs4-xattr-set-nfs4-label process-id xattr inode string
| Event-nfs4-xattr-get-nfs4-label process-id xattr inode string

datatype Event-id2secctx =
  Event-scm-passec process-id socket msghdr scm-cookie
| Event-audit-receive-msg process-id sk-buff nlmsghdr
| Event-audit-log-name process-id audit-names
| Event-audit-log-task-context process-id audit-buffer
| Event-audit-log-pid-context process-id u32
| Event-show-special process-id audit-context
| Event-ctnetlink-dump-secctx process-id sk-buff nf-conn
| Event-ctnetlink-secctx-size process-id nf-conn
| Event-ct-show-secctx process-id seq-file nf-conn
| Event-nfqnl-get-sk-secctx process-id sk-buff string
| Event-netlbl-unlshsh-func3 process-id u32
| Event-netlbl-unlabel-staticlist-gen process-id u32
| Event-netlbl-audit-start-common process-id int netlbl-audit

datatype Event-secctxtoid =
  Event-set-security-override-from-ctx process-id Cred string
| Event-netlbl-unlabel-staticadd process-id

datatype Event-inodesecctx =
  Event-kernfs-refresh-inode process-id kernfs-node inode
| Event-nfs-setsecurity process-id inode nfs4-label
| Event-nfsd4-security-inode-setsecctx process-id svc-fh xdr-netobj u32
| Event-nfsd4-set-nfs4-label process-id svc-fh xdr-netobj
| Event-nfsd4-encode-fattr process-id dentry
| Event-ovl-get-tmpfile process-id ovl-copy-up-ctx
| Event-ovl-copy-xattr process-id dentry dentry
| Event-ovl-create-or-link process-id dentry inode ovl-cattr bool

datatype Event-others = Evt-ismaclabel Event-ismaclabel | Evt-id2secctx Event-id2secctx
| Evt-secctxtoid Event-secctxtoid | Evt-inodesecctx Event-inodesecctx

```

definition $result\ s\ f \equiv if\ fst\ (the-run-state\ f\ s) \neq 0\ then\ False\ else\ True$

definition $resultU\ s\ f \equiv if\ fst\ (the-run-state\ f\ s) = ()\ then\ True\ else\ False$

definition $resultValue\ s\ f \equiv fst\ (the-run-state\ f\ s)$

definition $funcState\ s\ f \equiv snd\ (the-run-state\ f\ s)$

definition $getsb-by-id\ s\ i \equiv the((k-superblock\ s)\ i)$

definition $getsb-id\ s\ sb \equiv SOME\ i.\ sb = the((k-superblock\ s)\ i)$

29.2 kernel action about superblock

kernel create new superblock Allocate and attach a security structure if operation was successful created superblock else create fail

29.2.1 kernel action of security_{sballoc}

definition $k-create-new-superblock :: 'a \Rightarrow process-id \Rightarrow t-sb \Rightarrow ('a \times super-block\ option)$

where $k-create-new-superblock\ s\ pid\ p \equiv$
 $let\ t = getsb-by-id\ s\ p$
 in
 $if\ result\ s\ (security-sb-alloc\ s\ t)\ then$
 $(snd\ (the-run-state\ (security-sb-alloc\ s\ t)\ s),\ Some\ t)$
 $else$
 $(s,\ None)$

kernel free superblock sb Deallocate and clear the sb security field.

29.2.2 kernel action of security_{sbfree}

definition $k-sb-free :: 'a \Rightarrow process-id \Rightarrow t-sb \Rightarrow ('a \times unit)$

where $k-sb-free\ s\ pid\ t \equiv$
 $let\ s' = snd(the-run-state(security-sb-free\ s\ ((getsb-by-id\ s\ t)))\ s)$
 $in\ (s',())$

29.2.3 kernel action of security_{sbcopydata}

definition $k-sb-copy-data :: 'a \Rightarrow process-id \Rightarrow 'a \times int$

where $k-sb-copy-data\ s\ pid \equiv$
 $let\ copy = SOME\ x::string.\ True; orig = []$
 in
 $if\ result\ s\ (security-sb-copy-data\ s\ orig\ copy)$
 $then\ (s, resultValue\ s\ (security-sb-copy-data\ s\ orig\ copy))$
 $else\ (s, 0)$

29.2.4 kernel action of security_{sb}remount

Extracts security system specific mount options and verifies no changes are being made to those options.

definition *do-remount* :: 'a ⇒ path ⇒ Void ⇒ ('a × int)
 where *do-remount* s p data ≡
 if result s (security-sb-remount s (mnt-sb (p-mnt p)) data)
 then (s, resultValue s (security-sb-remount s (mnt-sb (p-mnt p)) data))
 else (s, 0)

29.2.5 kernel action of security_{sb}kernmount

definition *mount-fs* :: 'a ⇒ file-system-type ⇒ int ⇒ string
 ⇒ string ⇒ ('a × dentry option)
 where *mount-fs* s type f name data ≡
 let
 secddata = (SOME x :: string . True);
 root = (SOME x :: dentry . True) ;
 t = getsb-id s (d-sb root)
 in
 if ¬(result s (security-sb-copy-data s data secddata)
 ∧ result s (security-sb-kern-mount s (d-sb root) f secddata))
 then
 (s, Some root)
 else
 (s, None)

29.2.6 kernel action of security_{sb}showoptions

definition *show-sb-opts* :: 'a ⇒ process-id ⇒ seq-file ⇒ t-sb ⇒ 'a × int
 where *show-sb-opts* s pid m t ≡
 (s, resultValue s (security-sb-show-options s m (getsb-by-id s t)))

29.2.7 kernel action of security_{sb}stats

definition *stats-by-dentry* :: 'a ⇒ process-id ⇒ dentry ⇒ 'a × int
 where *stats-by-dentry* s pid d ≡ (s, resultValue s (security-sb-stats s d))

29.2.8 kernel action of security_{sb}mount

definition *do-mount* :: 'a ⇒ process-id ⇒ string ⇒ string ⇒ string ⇒ nat ⇒ Void
 ⇒ 'a × int
 where *do-mount* s pid dev-name dir-name type-page flags' data-page ≡
 let p = SOME x :: path. True
 in
 (s, resultValue s (security-sb-mount s dev-name p type-page flags' data-page))

29.2.9 kernel action of security_{sb}umount

definition *do-umount* :: 'a ⇒ process-id ⇒ mount ⇒ int ⇒ 'a × int

where *do-umount s pid m f* \equiv
 let m' = (mnt m)
 in
 (*s,resultValue s (security-sb-umount s m' f)*)

29.2.10 kernel action of security_s*b_pivotroot*

definition *pivot-root :: 'a \Rightarrow process-id \Rightarrow 'a \times int*
where *pivot-root s pid* \equiv
 let new = SOME x:: path. True;
 old = SOME x:: path. True
 in
 (*s, resultValue s (security-sb-pivotroot s new old)*)

29.2.11 kernel action of security_s*b_set_mnt_opts*

definition *set-sb-security :: 'a \Rightarrow process-id \Rightarrow super-block \Rightarrow dentry*
 \Rightarrow nfs-mount-info \Rightarrow 'a \times int
where *set-sb-security s pid sb d nfs* \equiv
 let opt = lsm-opts (parsed nfs);
 kflags = 0 ;
 kflags-out = 0
 in
 (*s,resultValue s (security-sb-set-mnt-opts s sb opt kflags kflags-out)*)

definition *setup-security-options :: 'a \Rightarrow process-id \Rightarrow btrfs-fs-info \Rightarrow super-block*
 \Rightarrow opts \Rightarrow 'a \times int

where *setup-security-options s pid fsinfo sb sec-opts* \equiv
 (*s,resultValue s (security-sb-set-mnt-opts s sb sec-opts 0 0)*)

29.2.12 kernel action of security_s*b_clone_mnt_opts*

definition *nfs-clone-sb-security :: 'a \Rightarrow process-id \Rightarrow super-block \Rightarrow dentry \Rightarrow*
 nfs-mount-info \Rightarrow 'a \times int
where *nfs-clone-sb-security s pid sb' mntroot minfo* \equiv
 let oldsb = nfsc-sb (cloned minfo);
 kflags = 0;
 kflags-out = 0
 in if result s (security-sb-clone-mnt-opts s oldsb sb' kflags kflags-out) then
 (*s,resultValue s (security-sb-clone-mnt-opts s oldsb sb' kflags kflags-out)*)
 else
 (*s,0*)

29.2.13 kernel action of security_s*b_parse_opts_str*

definition *parse-security-options :: 'a \Rightarrow process-id \Rightarrow string \Rightarrow opts \Rightarrow 'a \times int*
where *parse-security-options s pid orig sec-opts* \equiv
 let secdata = SOME x:: string. True
 in

$(s, \text{resultValue } s \text{ (security-sb-parse-opts-str } s \text{ secdata sec-opts)})$

29.3 task

29.3.1 kernel action of security_{task_{alloc}}

definition *copy-process* :: 'a \Rightarrow process-id \Rightarrow nat \Rightarrow 'a \times Task option
where *copy-process* *s* *pid* *cflags* \equiv
 let *t* = SOME *x*:: Task. True; *p* = SOME *x* :: nat. True in
 if result *s* (security-task-alloc *s* *t* *cflags*)
 then (*s*, None)
 else
 (funcState *s* (security-task-alloc *s* *t* *cflags*) , Some *t*)

29.3.2 kernel action of security_{task_{free}}

definition *task-free* :: 'a \Rightarrow process-id \Rightarrow Task \Rightarrow 'a \times unit
where *task-free* *s* *p* *t* \equiv
 let *pid* = get-processid *s* *t* ;
s' = snd(the-run-state(security-task-free *s* *t*) *s*)
 in (*s'*, ())

29.3.3 kernel action of security_{cred_{alloc}blank}

definition *cred-alloc-blank* :: 'a \Rightarrow process-id \Rightarrow 'a \times Cred option
where *cred-alloc-blank* *s* *pid* \equiv let *new* = SOME *x*:: Cred. True in
 if resultValue *s* (security-cred-alloc-blank *s* *new* 0) \leq 0 then
 (*s*, None)
 else
 (*s*, Some *new*)

29.3.4 kernel action of security_{cred_{free}}

definition *cred-free* :: 'a \Rightarrow process-id \Rightarrow 'a \times unit
where *cred-free* *s* *pid* \equiv
 let *cred* = SOME *x*:: Cred. True ;
s' = snd(the-run-state(security-cred-free *s* *cred*) *s*)
 in (*s'*, ())

29.3.5 kernel action of security_{prepare_{creds}}

definition *prepare-creds* :: 'a \Rightarrow process-id \Rightarrow 'a \times Cred option
where *prepare-creds* *s* *pid* \equiv
 let *task* = current-process *s*;
new = SOME *x*:: Cred. True;
old = cred *task*
 in
 if resultValue *s* (security-prepare-creds *s* *new* *old* 0) $<$ 0 then (*s*, None)
 else (*s*, Some *new*)

29.3.6 kernel action of security_{transfer_creds}

definition *key-change-session-keyring* :: 'a \Rightarrow process-id \Rightarrow 'a \times unit
where *key-change-session-keyring* s pid \equiv
 let new = SOME x :: Cred. True;
 old = current-cred s;
 s' = snd(the-run-state(security-transfer-creds s new old) s)
 in (s',())

29.3.7 kernel action of security_{task_fix_setuid}

definition *sys-setreuid* :: 'a \Rightarrow process-id \Rightarrow kuid \Rightarrow kuid \Rightarrow 'a \times int
where *sys-setreuid* s pid ruid euid' \equiv
 let new = snd(prepare-creds s pid);
 old = current-cred s ;
 retval = resultValue s (security-task-fix-setuid s (the new)
 old LSM-SETID-RE)
 in
 if new = None then
 (s, -ENOMEM)
 else
 if retval < 0 then
 (s, retval)
 else
 (s, 0)

29.3.8 kernel action of security_{task_setpgid}

definition *setpgid* :: 'a \Rightarrow process-id \Rightarrow pid-t \Rightarrow pid-t \Rightarrow 'a \times int
where *setpgid* s p pid pgid \equiv
 let pgid = if pgid = 0 then pid else pgid;
 p = get-process-by-pid s (nat pid) in
 if pgid < 0 then
 (s, -EINVAL)
 else
 let err = resultValue s (security-task-setpgid s p pgid)
 in
 if err \neq 0 then
 (s, err)
 else
 (s, 0)

29.3.9 kernel action of security_{task_getpgid}

definition *do-getpgid* :: 'a \Rightarrow process-id \Rightarrow pid-t \Rightarrow 'a \times int
where *do-getpgid* s p pid \equiv
 let p = get-process-by-pid s (nat pid);
 retval = resultValue s (security-task-getpgid s p)
 in if retval \neq 0 then
 (s, retval)

else
 (s, pid)

29.3.10 kernel action of security_{task_getsid}

definition getsid :: 'a ⇒ process-id ⇒ pid-t ⇒ 'a × int

where getsid s p pid ≡
 if pid = 0 then (s, current s)
 else
 let p = get-process-by-pid s (nat pid);
 retval = resultValue s (security-task-getsid s p)
 in
 if retval ≠ 0 then
 (s, retval)
 else
 (s, pid)

29.3.11 kernel action of security_{task_getsecid}

definition getsecid :: 'a ⇒ process-id ⇒ Task ⇒ u32 ⇒ 'a × unit

where getsecid s pid p secid' ≡
 let secid' = 0;
 retval = resultValue s (security-task-getsecid s p secid')
 in (s, retval)

29.3.12 kernel action of security_{task_setnice}

definition task-setnice :: 'a ⇒ process-id ⇒ Task ⇒ int ⇒ 'a × int

where task-setnice s pid p nice ≡
 let
 retval = resultValue s (security-task-setnice s p nice)
 in if retval ≠ 0 then
 (s, retval)
 else
 (s, 0)

29.3.13 kernel action of security_{task_setioprio}

definition set-task-ioprio :: 'a ⇒ process-id ⇒ Task ⇒ int ⇒ 'a × int

where set-task-ioprio s pid p ioprio ≡
 let
 retval = resultValue s (security-task-setioprio s p ioprio)
 in if retval ≠ 0 then (s, retval) else (s, 0)

29.3.14 kernel action of security_{task_getioprio}

definition get-task-ioprio :: 'a ⇒ process-id ⇒ Task ⇒ 'a × int

where get-task-ioprio s pid p ≡
 let
 retval = resultValue s (security-task-getioprio s p)

in if retval \neq 0 then (s,retval) else (s,0)

29.3.15 kernel action of security_{task_prlimit}

definition *check-prlimit-permission* :: 'a \Rightarrow process-id \Rightarrow Task \Rightarrow nat \Rightarrow 'a \times int
where *check-prlimit-permission* s pid p flags' \equiv
 let current = current-process s;
 cred = current-cred s;
 tcred = task-cred s p
in
 if current = p *then*
 (s,0)
 else
 (s,resultValue s (security-task-prlimit s cred tcred flags'))

29.3.16 kernel action of security_{task_setrlimit}

definition *do-prlimit* :: 'a \Rightarrow process-id \Rightarrow Task \Rightarrow nat \Rightarrow 'a \times int
where *do-prlimit* s pid p resource \equiv
 let new-rlim = SOME x:: rlimit. True
 in (s,resultValue s (security-task-setrlimit s p resource new-rlim))

29.3.17 kernel action of security_{task_setscheduler}

definition *task-setscheduler* :: 'a \Rightarrow process-id \Rightarrow Task \Rightarrow 'a \times int
where *task-setscheduler* s pid p \equiv
 let retval = resultValue s (security-task-setscheduler s p)
 in if retval \neq 0 *then*
 (s,retval)
 else (s,0)

29.3.18 kernel action of security_{task_getscheduler}

definition *task-getscheduler* :: 'a \Rightarrow process-id \Rightarrow Task \Rightarrow 'a \times int
where *task-getscheduler* s pid p \equiv
 let retval = resultValue s (security-task-getscheduler s p)
 in if retval \neq 0 *then* (s,retval) *else* (s,0)

29.3.19 kernel action of security_{task_movememory}

definition *task-movememory* :: 'a \Rightarrow process-id \Rightarrow Task \Rightarrow 'a \times int
where *task-movememory* s pid p \equiv
 let retval = resultValue s (security-task-movememory s p)
 in if retval \neq 0 *then* (s,retval) *else* (s,0)

29.3.20 kernel action of security_{task_kill}

definition *task-kill* :: 'a \Rightarrow process-id \Rightarrow Task \Rightarrow siginfo \Rightarrow int \Rightarrow Cred \Rightarrow 'a \times int
where *task-kill* s pid p info sig c \equiv

```

let retval = resultValue s ( security-task-kill s p info sig (Some c))
in if retval  $\neq$  0 then (s,retval)
   else (s,0)

```

29.3.21 kernel action of security_{task_prctl}

definition *task-prctl* :: 'a \Rightarrow process-id \Rightarrow int \Rightarrow nat \Rightarrow nat \Rightarrow nat \Rightarrow nat \Rightarrow 'a \times int

```

where task-prctl s pid op arg2 arg3 arg4 arg5  $\equiv$ 
  let retval = resultValue s ( security-task-prctl s op arg2 arg3 arg4 arg5)
  in if retval  $\neq$  (-ENOSYS) then
      (s,retval)
    else
      (s,0)

```

29.3.22 kernel action of security_{task_getsecid}

definition *ima-bprm-check'* :: 'a \Rightarrow process-id \Rightarrow linux-binprm \Rightarrow 'a \times int

```

where ima-bprm-check' s pid bprm  $\equiv$ 
  let secid = SOME x::u32. True;
  ret = security-task-getsecid s (current-process s) secid
  in (s,0)

```

29.3.23 kernel action of security_{kernel_act_as}

definition *set-security-override* :: 'a \Rightarrow process-id \Rightarrow Cred \Rightarrow u32 \Rightarrow 'a \times int

```

where set-security-override s pid new secid'  $\equiv$ 
  let retval = resultValue s ( security-kernel-act-as s new secid')
  in (s,retval)

```

29.3.24 kernel action of security_{kernel_create_files_as}

definition *set-create-files-as* :: 'a \Rightarrow process-id \Rightarrow Cred \Rightarrow inode \Rightarrow 'a \times int

```

where set-create-files-as s pid new inode  $\equiv$ 
  let
    new = new (fsuid := i-uid inode, fsgid := i-gid inode);
    retval = resultValue s ( security-kernel-create-files-as s new inode)
  in (s,retval)

```

29.3.25 kernel action of security_{kernel_module_request}

definition *request-module'* :: 'a \Rightarrow process-id \Rightarrow 'a \times int

```

where request-module' s pid  $\equiv$ 
  let
    module-name = SOME x::string. True;
    retval = resultValue s ( security-kernel-module-request s module-name)
  in (s,retval)

```

29.3.26 kernel action of security_{kernel_read_file}

definition *kernel-read-file* :: 'a \Rightarrow process-id \Rightarrow Files \Rightarrow string

$\Rightarrow \text{kernel-read-file-id} \Rightarrow 'a \times \text{int}$

where $\text{kernel-read-file } s \text{ pid file buf id}' \equiv$
 let
 $\text{retval} = \text{resultValue } s \text{ (security-kernel-read-file } s \text{ file id')}$
 $\text{in if } \text{retval} \neq 0 \text{ then } (s, \text{retval})$
 else
 let
 $i\text{-size}' = \text{nat}(i\text{-size (file-inode file)});$
 $\text{retval} = \text{resultValue } s \text{ (security-kernel-post-read-file } s \text{ file buf } i\text{-size}'$
 $\text{id}')$
 $\text{in } (s, \text{retval})$

29.3.27 kernel action of security_{kernelloaddata}

definition $\text{load-data} :: 'a \Rightarrow \text{process-id} \Rightarrow 'a \times \text{int}$
where $\text{load-data } s \text{ pid} \equiv$
 let
 $\text{load} = \text{SOME } x :: \text{kernel-load-data-id. True};$
 $\text{retval} = \text{resultValue } s \text{ (security-kernel-load-data } s \text{ load)}$
 $\text{in if } \text{retval} \neq 0 \text{ then } (s, \text{retval}) \text{ else } (s, 0)$

29.3.28 kernel action of security_{tasktoinode}

definition $\text{task-to-inode} :: 'a \Rightarrow \text{process-id} \Rightarrow \text{Task} \Rightarrow \text{inode} \Rightarrow 'a \times \text{unit}$
where $\text{task-to-inode } s \text{ pid task inode} \equiv$
 let
 $\text{load} = \text{SOME } x :: \text{kernel-load-data-id. True};$
 $s' = \text{funcState } s \text{ (security-task-to-inode } s \text{ task inode)}$
 $\text{in } (s, ())$

29.3.29 kernel action of security_{getprocattr}

definition $\text{PROC-I} :: \text{inode} \Rightarrow \text{proc-inode}$
where $\text{PROC-I inode} \equiv \text{SOME proc . vfs-inode proc} = \text{inode}$

definition $\text{proc-pid} :: \text{inode} \Rightarrow \text{ppid}$
where $\text{proc-pid inode} \equiv \text{proci-pid (PROC-I inode)}$

definition $\text{get-pid-task} :: 'a \Rightarrow \text{ppid} \Rightarrow \text{Task}$
where $\text{get-pid-task } s \text{ p} \equiv \text{the } ((k\text{-task } s)(\text{tid } p))$

definition $\text{proc-pid-attr-read} :: 'a \Rightarrow \text{process-id} \Rightarrow \text{Files} \Rightarrow \text{string} \Rightarrow \text{nat} \Rightarrow \text{loff-t}$
 $\Rightarrow 'a \times \text{int}$

where $\text{proc-pid-attr-read } s \text{ pid file buf count' ppos} \equiv$
 let
 $p = \text{SOME } x :: \text{string. True};$
 $\text{inode} = \text{file-inode file};$
 $\text{ppid}' = \text{proc-pid inode};$
 $\text{task} = \text{get-pid-task } s \text{ ppid}';$

$retval = resultValue\ s\ (security-getprocattr\ s\ task\ (d-name(p-dentry(f-path\ file)))\ p)$
 $in\ (s, retval)$

29.3.30 kernel action of security_{etprocattr}

definition $proc-pid-attr-write :: 'a \Rightarrow process-id \Rightarrow Files \Rightarrow string \Rightarrow nat \Rightarrow loff-t \Rightarrow 'a \times int$

where $proc-pid-attr-write\ s\ pid\ file\ buf\ count'\ ppos \equiv$
 let
 $p = SOME\ x :: string.\ True;$
 $inode = file-inode\ file;$
 $ppid' = proc-pid\ inode;$
 $task = get-pid-task\ s\ ppid';$
 $name = (d-name(p-dentry(f-path\ file)));$
 $retval = resultValue\ s\ (security-setprocattr\ s\ name\ p\ (int\ count'))$
 $in\ (s, retval)$

29.4 binder

29.4.1 kernel action of security_{binder_set_context_mgr}

definition $binder-ioctl-set-ctx-mgr :: 'a \Rightarrow process-id \Rightarrow Files \Rightarrow 'a \times int$

where $binder-ioctl-set-ctx-mgr\ s\ pid\ files' \equiv$
 $let\ proc = private-data\ files';$
 $task = tsk\ proc\ ;$
 $retval = resultValue\ s\ (security-binder-set-context-mgr\ s\ task)$
 $in\ if\ retval < 0\ then$
 $(s, retval)$
 $else$
 $(s, 0)$

29.4.2 kernel action of security_{binder_transaction}

definition $binder-transaction :: 'a \Rightarrow process-id \Rightarrow binder-proc \Rightarrow binder-thread \Rightarrow 'a \times unit$

where $binder-transaction\ s\ pid\ proc'\ thread \equiv$
 let
 $task = tsk\ proc';$
 $target-task = tsk\ (proc\ thread);$
 $retval = resultValue\ s\ (security-binder-transaction\ s\ task\ target-task)$
 $in\ if\ retval < 0\ then$
 $(s, ())$
 $else$
 $(s, ())$

29.4.3 kernel action of security_{binder_transfer_binder}

definition $binder-translate-binder :: 'a \Rightarrow process-id \Rightarrow flat-binder-object$

$\Rightarrow \text{binder-transaction} \Rightarrow \text{binder-thread} \Rightarrow 'a \times \text{int}$

where $\text{binder-translate-binder } s \text{ pid fp } t \text{ thread} \equiv$
 let
 $\text{target-task} = \text{tsk } (\text{to-proc } t) ;$
 $\text{task} = \text{tsk } (\text{proc } \text{thread});$
 $\text{retval} = \text{resultValue } s \text{ (security-binder-transfer-binder } s \text{ task target-task)}$
 $\text{in if } \text{retval} \neq 0 \text{ then}$
 $\quad (s, -\text{EPERM})$
 else
 $\quad (s, 0)$

29.4.4 kernel action of security_{binder_ttransfer_{file}}

definition $\text{binder-translate-fd} :: 'a \Rightarrow \text{process-id} \Rightarrow \text{int} \Rightarrow \text{binder-transaction} \Rightarrow \text{binder-thread}$

$\Rightarrow \text{binder-transaction} \Rightarrow 'a \times \text{int}$

where $\text{binder-translate-fd } s \text{ pid fd } t \text{ thread in-reply-to} \equiv$
 let
 $\text{target-task} = \text{tsk } (\text{to-proc } t) ;$
 $\text{task} = \text{tsk } (\text{proc } \text{thread});$
 $f = \text{SOME } x :: \text{Files. True};$
 $\text{retval} = \text{resultValue } s \text{ (security-binder-transfer-file } s \text{ task target-task } f)$
 $\text{in if } \text{retval} < 0 \text{ then}$
 $\quad (s, -\text{EPERM})$
 else
 $\quad (s, 0)$

29.5 ptrace sys

29.5.1 kernel action of security_{ptrace_access_check}

definition $\text{ptrace-may-access} :: 'a \Rightarrow \text{process-id} \Rightarrow \text{Task} \Rightarrow \text{nat} \Rightarrow 'a \times \text{int}$
where $\text{ptrace-may-access } s \text{ pid task } m \equiv$
 $\text{let } \text{retval} = \text{resultValue } s \text{ (security-ptrace-access-check } s \text{ task } m)$
 $\text{in } (s, \text{retval})$

29.5.2 kernel action of security_{ptrace_traceme}

definition $\text{ptrace-traceme} :: 'a \Rightarrow \text{process-id} \Rightarrow 'a \times \text{int}$
where $\text{ptrace-traceme } s \text{ pid} \equiv$
 $\text{if } \text{ptrace } (\text{current-process } s) = 0$
 $\text{then } (s, -\text{EPERM})$
 else
 $\quad \text{let } \text{parent} = \text{get-process-by-pid } s \text{ (parent(current-process } s));$
 $\quad \text{retval} = \text{resultValue } s \text{ (security-ptrace-traceme } s \text{ parent)}$
 $\text{in } (s, \text{retval})$

29.5.3 kernel action of security_{syslog}

definition $\text{check-syslog-permissions} :: 'a \Rightarrow \text{process-id} \Rightarrow \text{int} \Rightarrow 'a \times \text{int}$

where *check-syslog-permissions* *s pid t* \equiv
 let *retval* = *resultValue s (security-syslog s t)*
 in (*s,retval*)

29.5.4 kernel action of security_{quotactl}

definition *check-quotactl-permission* :: '*a* \Rightarrow *process-id* \Rightarrow *super-block* \Rightarrow *int* \Rightarrow *int*
 \Rightarrow *int* \Rightarrow '*a* \times *int*

where *check-quotactl-permission* *s pid sb type' cmd id'* \equiv
 let *retval* = *resultValue s (security-quotactl s cmd type' id' (Some sb))*
 in (*s,retval*)

definition *quota-sync-all* :: '*a* \Rightarrow *process-id* \Rightarrow *int* \Rightarrow '*a* \times *int*

where *quota-sync-all* *s pid t* \equiv
 let *retval* = *resultValue s (security-quotactl s Q-SYNC t 0 None)*
 in (*s,retval*)

29.5.5 kernel action of security_{quotaon}

definition *dquot-quota-on* :: '*a* \Rightarrow *process-id* \Rightarrow *super-block* \Rightarrow *int* \Rightarrow *int* \Rightarrow *path*
 \Rightarrow '*a* \times *int*

where *dquot-quota-on* *s pid sb type' fromat-id path* \equiv
 let *retval* = *resultValue s (security-quota-on s (p-dentry path))*
 in (*s,retval*)

definition *dquot-quota-on-mount* :: '*a* \Rightarrow *process-id* \Rightarrow *super-block* \Rightarrow *string* \Rightarrow *int*
 \Rightarrow *int* \Rightarrow '*a* \times *int*

where *dquot-quota-on-mount* *s pid sb qf-name fromat-id type'* \equiv
 let *dentry* = *SOME x :: dentry. True*;
 retval = *resultValue s (security-quota-on s dentry)*
 in (*s,retval*)

29.5.6 kernel action of security_{settime64}

definition *syscall-stime* :: '*a* \Rightarrow *process-id* \Rightarrow '*a* \times *int*

where *syscall-stime* *s pid* \equiv
 let *tv* = *SOME x :: timespec64. True*;
 retval = *resultValue s (security-settime64 s tv None)*
 in *if* *retval* \neq 0 *then* (*s,retval*) *else* (*s,0*)

definition *do-sys-settimeofday64* :: '*a* \Rightarrow *process-id* \Rightarrow *timespec64* \Rightarrow *tz* \Rightarrow '*a* \times
int

where *do-sys-settimeofday64* *s pid tv tz* \equiv
 let
 retval = *resultValue s (security-settime64 s tv (Some tz))*
 in *if* *retval* \neq 0 *then* (*s,retval*) *else* (*s,0*)

type-synonym *pages* = *int*

29.5.7 kernel action of security_{vm}enough_{memory}_{mm}

definition *frontswap-unuse-pages* :: 'a \Rightarrow process-id \Rightarrow nat \Rightarrow nat \Rightarrow int \Rightarrow 'a \times int

where *frontswap-unuse-pages* s pid total' unused swapid \equiv
 let pages = SOME x :: pages. True;
 mm = mm (current-process s);
 retval = resultValue s (security-vm-enough-memory-mm s mm pages)
 in if retval \neq 0 then (s, -ENOMEM) else (s, 0)

definition *vma-pages* :: vm-area-struct \Rightarrow nat

where *vma-pages* vma \equiv nat((int (vm-end vma - vm-start vma)) >> PAGE-SHIFT)

definition *latent-entropy* :: 'a \Rightarrow process-id \Rightarrow mm \Rightarrow mm \Rightarrow 'a \times int

where *latent-entropy* s pid mm' oldmm \equiv
 let pages = SOME x :: pages. True;
 len = vma-pages(mmap oldmm);
 retval = resultValue s (security-vm-enough-memory-mm s oldmm pages)
 in if retval \neq 0 then (s, -ENOMEM) else (s, 0)

definition *mmap-region* :: 'a \Rightarrow process-id \Rightarrow nat \Rightarrow 'a \times int

where *mmap-region* s pid len' \equiv
 let mm = mm (current-process s);
 charged = (len' >> PAGE-SHIFT);
 retval = resultValue s (security-vm-enough-memory-mm s mm charged)
 in if retval \neq 0 then (s, -ENOMEM) else (s, 0)

definition *acct-stack-growth* :: 'a \Rightarrow process-id \Rightarrow vm-area-struct \Rightarrow nat \Rightarrow nat \Rightarrow 'a \times int

where *acct-stack-growth* s pid vma size' grow \equiv
 let mm = SOME x :: mm. True;
 retval = resultValue s (security-vm-enough-memory-mm s mm grow)
 in if retval \neq 0 then (s, -ENOMEM) else (s, 0)

definition *do-brk-flags* :: 'a \Rightarrow process-id \Rightarrow nat \Rightarrow 'a \times int

where *do-brk-flags* s pid len' \equiv
 let mm = mm (current-process s);
 charged = (len' >> PAGE-SHIFT);
 retval = resultValue s (security-vm-enough-memory-mm s mm charged)
 in if retval \neq 0 then (s, -ENOMEM) else (s, 0)

definition *insert-vm-struct* :: 'a \Rightarrow process-id \Rightarrow mm \Rightarrow vm-area-struct \Rightarrow 'a \times int

where *insert-vm-struct* s pid mm' vma \equiv
 let pages = SOME x :: pages. True;
 len = vma-pages(vma);
 retval = resultValue s (security-vm-enough-memory-mm s mm')

pages)
in if retval \neq 0 then (s, -ENOMEM) else (s, 0)

definition mprotect-fixup :: 'a \Rightarrow process-id \Rightarrow vm-area-struct \Rightarrow nat \Rightarrow nat \Rightarrow 'a \times int

where mprotect-fixup s pid vma end start \equiv
let mm = SOME x :: mm. True;
len = end - start;
nrpages = (len >> PAGE-SHIFT);
retval = resultValue s (security-vm-enough-memory-mm s mm nrpages)
in if retval \neq 0 then (s, -ENOMEM) else (s, 0)

definition vma-to-resize :: 'a \Rightarrow process-id \Rightarrow nat \Rightarrow nat \Rightarrow nat \Rightarrow nat \Rightarrow 'a \times vm-area-struct option

where vma-to-resize s pid addr old-len new-len p \equiv
let mm = mm (current-process s);
len = old-len - new-len;
charged = (len >> PAGE-SHIFT);
vma = SOME x :: vm-area-struct. True;
retval = resultValue s (security-vm-enough-memory-mm s mm charged)
in if retval \neq 0 then (s, None) else (s, Some vma)

definition PAGE-MASK \equiv NOT (PAGE-SIZE - 1)

definition PAGE-ALIGN addr \equiv (addr + PAGE-SIZE - 1) AND PAGE-MASK

definition VM-ACCT size' \equiv PAGE-ALIGN(size') >> PAGE-SHIFT

definition shmем-acct-size :: 'a \Rightarrow process-id \Rightarrow nat \Rightarrow loff-t \Rightarrow 'a \times int

where shmем-acct-size s pid flags' size' \equiv
let mm = mm (current-process s);
charged = VM-ACCT size';
retval = (if ((int flags') AND VM-NORESERVE) \neq 0 then 0
else
resultValue s (security-vm-enough-memory-mm s mm charged))
in (s, retval)

definition shmем-reacct-size :: 'a \Rightarrow process-id \Rightarrow nat \Rightarrow loff-t \Rightarrow loff-t \Rightarrow 'a \times int

where shmем-reacct-size s pid flags' oldsize newsize \equiv
let mm = mm (current-process s);
charged = VM-ACCT newsize - VM-ACCT oldsize;
retval = (if charged > 0 then
resultValue s (security-vm-enough-memory-mm s mm charged)
else
0)
in (s, retval)

definition *shmem-acct-block* :: 'a \Rightarrow process-id \Rightarrow nat \Rightarrow nat \Rightarrow 'a \times int
where *shmem-acct-block* s pid flags' pages' \equiv
 let mm = mm (current-process s);
 charged = pages' * (VM-ACCT PAGE-SIZE) ;
 retval = (if ((int flags') AND VM-NORESERVE) \neq 0 then 0
 else
 resultValue s (security-vm-enough-memory-mm s mm
 charged))
 in (s,retval)

definition *syscall-swapoff* :: 'a \Rightarrow process-id \Rightarrow 'a \times int
where *syscall-swapoff* s pid \equiv
 let mm = mm (current-process s);
 pages = SOME x :: pages. True;
 retval = resultValue s (security-vm-enough-memory-mm s mm pages)
 in if retval \neq 0 then (s,-ENOMEM) else (s,0)

29.6 cap

29.6.1 kernel action of security_{capget}

definition *cap-get-target-pid* :: 'a \Rightarrow process-id \Rightarrow kernel-cap-t \Rightarrow kernel-cap-t \Rightarrow
 kernel-cap-t
 \Rightarrow 'a \times int
where *cap-get-target-pid* s pid pEp pIp pPp \equiv
 let task = SOME x :: Task. True;
 retval = resultValue s (security-capget s task pEp pIp pPp)
 in (s,retval)

29.6.2 kernel action of security_{capset}

definition *kcapsset* :: 'a \Rightarrow process-id \Rightarrow 'a \times int
where *kcapsset* s pid \equiv
 let task = SOME x :: Task. True;
 effective = SOME x :: kernel-cap-t. True;
 inheritable = SOME x :: kernel-cap-t. True;
 permitted = SOME x :: kernel-cap-t. True;
 new = (the(snd(prepare-creds s pid)));
 old = current-cred s;
 retval = resultValue s (security-capsset s new old effective inheritable
 permitted)
 in if retval < 0 then (s,retval)
 else (s,0)

29.6.3 kernel action of security_{capable}

definition *has-ns-capability* :: 'a \Rightarrow process-id \Rightarrow Task \Rightarrow ns \Rightarrow int \Rightarrow 'a \times bool
where *has-ns-capability* s pid t ns cap \equiv
 let c = task-cred s t;
 retval = resultValue s (security-capable s c ns cap)

in if retval = 0 then (s,True)
 else (s,False)

definition ns-capable-common :: 'a \Rightarrow process-id \Rightarrow ns \Rightarrow int \Rightarrow bool \Rightarrow 'a \times bool
where ns-capable-common s pid ns cap audit \equiv
 let c = current-cred s;
 capable =
 (if audit then resultValue s (security-capable s c ns cap)
 else
 resultValue s (security-capable-noaudit s c ns cap))
 in if capable = 0 then
 (s,True)
 else
 (s,False)

definition file-ns-capable :: 'a \Rightarrow process-id \Rightarrow Files \Rightarrow ns \Rightarrow int \Rightarrow 'a \times bool
where file-ns-capable s pid files' ns cap \equiv
 let c = f-cred files';
 retval= resultValue s (security-capable s c ns cap)
 in if retval \neq 0 then
 (s,True)
 else
 (s,False)

29.6.4 kernel action of security_capable_noaudit

definition has-ns-capability-noaudit :: 'a \Rightarrow process-id \Rightarrow Task \Rightarrow ns \Rightarrow int \Rightarrow 'a
 \times bool
where has-ns-capability-noaudit s pid t ns cap \equiv
 let c = task-cred s t;
 retval= resultValue s (security-capable-noaudit s c ns cap)
 in if retval = 0 then
 (s,True)
 else
 (s,False)

definition ptracer-capable :: 'a \Rightarrow process-id \Rightarrow Task \Rightarrow ns \Rightarrow 'a \times bool
where ptracer-capable s pid t ns \equiv
 let c = ptracer-cred t;
 retval= (if c = None then 0
 else
 resultValue s (security-capable-noaudit s (the c) ns
 CAP-SYS-PTRACE))
 in if retval = 0 then
 (s,True)
 else
 (s,False)

29.7 bprm

29.7.1 kernel action of security_{bprm_setc_{reds}}

definition *prepare-binprm* :: 'a \Rightarrow process-id \Rightarrow linux-binprm \Rightarrow 'a \times int
where *prepare-binprm* *s* *pid* *bprm* \equiv
 let
 retval = resultValue *s* (security-bprm-set-creds *s* *bprm*)
 in
 if retval \neq 0 then (*s*,retval)
 else (*s*,0)

29.7.2 kernel action of security_{bprm_ccheck}

definition *search-binary-handler* :: 'a \Rightarrow process-id \Rightarrow linux-binprm \Rightarrow 'a \times int
where *search-binary-handler* *s* *pid* *bprm* \equiv
 let
 retval = resultValue *s* (security-bprm-check *s* *bprm*)
 in
 if retval \neq 0 then (*s*,retval)
 else (*s*,-ENOENT)

29.7.3 kernel action of security_{bprm_ccommitting_creds}security_{bprm_ccommitted_creds}

definition *install-exec-creds* :: 'a \Rightarrow process-id \Rightarrow linux-binprm \Rightarrow 'a \times unit
where *install-exec-creds* *s* *pid* *bprm* \equiv
 let
 s' = snd (the-run-state (security-bprm-committing-creds *s* *bprm*) *s*);
 s'' = snd (the-run-state (security-bprm-committed-creds *s'* *bprm*) *s'*)
 in
 (*s''*,())

29.8 inode part 1

29.8.1 kernel action of security_{inode_aalloc}

definition *inode-init-always* :: 'a \Rightarrow process-id \Rightarrow super-block \Rightarrow inode \Rightarrow 'a \times int
where *inode-init-always* *s* *pid* *sb* *inode* \equiv
 let *inode* = inode(|i-opflags := 0,
 i-sb := sb,
 i-flags := 0|);
 s' = snd (the-run-state (security-inode-alloc *s* *inode*) *s*);
 retval = resultValue *s* (security-inode-alloc *s* *inode*)
 in if retval \neq 0 then
 (*s*,-ENOMEM)
 else
 (*s'*,0)

29.8.2 kernel action of security_{inode_ffree}

definition *destroy-inode'* :: 'a \Rightarrow process-id \Rightarrow inode \Rightarrow 'a \times unit

where *destroy-inode* 's pid inode \equiv
 let
 s' = *snd* (*the-run-state* (*security-inode-free* s inode) s)
 in (*s'*,())

29.8.3 kernel action of *security_dentry_init_security*

definition *nfs4-label-init-security*:: 'a \Rightarrow process-id \Rightarrow inode \Rightarrow dentry \Rightarrow iattr \Rightarrow nfs4-label

\Rightarrow 'a \times nfs4-label option
where *nfs4-label-init-security* s pid dir dentry sattr label' \equiv
 let imode = *ia-mode* sattr;
 dname = *d-name* dentry;
 label = label label';
 len = len label';
 s' = *snd* (*the-run-state* (*security-dentry-init-security* s dentry imode
 dname label len) s);
 retval = *resultValue* s (*security-dentry-init-security* s dentry imode
 dname label len)
 in if retval = 0 then
 (*s'*,Some label')
 else
 (*s'*,None)

29.8.4 kernel action of *security_dentry_create_files_as*

definition *override-creds* :: 'a \Rightarrow Cred \Rightarrow Cred option

where *override-creds* s new \equiv
 let old = *current-cred* s in Some old

definition *ovl-override-creds* :: 'a \Rightarrow super-block \Rightarrow Cred

where *ovl-override-creds* s sb \equiv
 let ofs = *s-fs-info* sb
 in the(*override-creds* s (*creator-cred* ofs))

definition *ovl-create-or-link*:: 'a \Rightarrow process-id \Rightarrow dentry \Rightarrow inode
 \Rightarrow ovl-cattr \Rightarrow bool \Rightarrow 'a \times int

where *ovl-create-or-link* s pid dentry inode attr' origin \equiv
 let
 dname = *d-name* dentry;
 mode = *mode* attr';
 old-cred = *ovl-override-creds* s (*d-sb* dentry);
 override-cred = (*the*(*snd*(*prepare-creds* s pid))) ;
 s' = *snd* (*the-run-state* (*security-dentry-create-files-as* s dentry mode
 dname old-cred override-cred) s);
 retval = *resultValue* s (*security-dentry-create-files-as* s dentry mode
 dname old-cred override-cred)
 in if retval = 0 then
 (*s'*,0)
 else

$(s', 0)$

29.8.5 kernel action of security_{old;inode;init;security}

definition *ocfs2-init-security-get*:: 'a \Rightarrow process-id \Rightarrow inode \Rightarrow inode
 \Rightarrow string \Rightarrow ocfs2-security-xattr-info option \Rightarrow 'a

\times int

where *ocfs2-init-security-get* s pid inode dir qstr si \equiv
 if si \neq None then
 let
 name = oname (the si);
 value = vvalue (the si);
 len = value-len (the si);
 s' = snd (the-run-state (security-old-inode-init-security s inode dir qstr
 name value len) s);
 retval = resultValue s (security-old-inode-init-security s inode dir qstr
 name value len)
 in (s',retval)
 else
 let
 s' = snd (the-run-state (security-inode-init-security s inode dir qstr
 0 []) s);
 retval = resultValue s (security-inode-init-security s inode dir qstr 0
 [])
 in (s',retval)

definition *reiserfs-security-init*:: 'a \Rightarrow process-id \Rightarrow inode \Rightarrow inode \Rightarrow qstr
 \Rightarrow reiserfs-security-handle \Rightarrow 'a \times int

where *reiserfs-security-init* s pid inode dir qstr sec \equiv
 let
 name = rsh-name sec;
 value = rsh-value sec;
 len = rsh-len sec;
 s' = snd (the-run-state (security-old-inode-init-security s inode dir qstr
 name value len) s);
 retval = resultValue s (security-old-inode-init-security s inode dir qstr
 name value len)
 in (s',retval)

29.8.6 kernel action of security_{inode;init;security}

definition *xattr-security-init*:: 'a \Rightarrow process-id \Rightarrow inode \Rightarrow inode
 \Rightarrow qstr \Rightarrow int \Rightarrow 'a \times int

where *xattr-security-init* s pid inode dir qstr btrfs-initxattrs \equiv
 let
 s' = funcState s (security-inode-init-security s inode dir qstr btrfs-initxattrs
 ""') ;
 retval = resultValue s (security-inode-init-security s inode dir qstr
 btrfs-initxattrs ""')
 in (s',retval)

29.9 path

29.9.1 kernel action of security_{path_mkdir}

definition *FSCACHE-COOKIE-TYPE-INDEX* $\equiv 0$

definition *container-of-cache* :: *fscache-cache* \Rightarrow *cachefiles-cache*
where *container-of-cache ptr* \equiv *SOME type. (cache type) = ptr*

definition *cachefiles-walk-to-object* :: '*a* \Rightarrow *cachefiles-object* \Rightarrow *cachefiles-object* \Rightarrow *string*

\Rightarrow *cachefiles-xattr* \Rightarrow '*a* \times *int*

where *cachefiles-walk-to-object s parent' object key' auxdata* \equiv
let cache = container-of-cache (fsojb-cache (fscache parent'));
path = SOME x:: path . True ;
dir = co-dentry parent';
path = path (\sqcup p-mnt := cc-mnt cache, p-dentry := dir);
next = SOME x:: dentry . True
in

if (length(key') $\neq 0 \vee$ (co-type object = FSCACHE-COOKIE-TYPE-INDEX
))

then

let s' = funcState s (security-path-mkdir s path next 0);
retval = resultValue s (security-path-mkdir s path next 0)
in if retval < 0 then
(s',retval)
else
(s',0)

else

let s' = funcState s (security-path-mknod s path next S-IFREG 0);
retval = resultValue s (security-path-mknod s path next S-IFREG
0)

in if retval < 0 then
(s',retval)
else
(s',0)

29.9.2 kernel action of security_{path_mknode_{security_inode_ccreate}}

definition *may-o-create* :: '*a* \Rightarrow *process-id* \Rightarrow *path* \Rightarrow *dentry* \Rightarrow *mode* \Rightarrow '*a* \times *int*

where *may-o-create s pid dir dentry m* \equiv
let
error = resultValue s (security-path-mknod s dir dentry (nat m) 0)
in if error $\neq 0$ then (s,error)
else
let
s' = funcState s (security-inode-create s (get-inode s (d-inode (p-dentry
dir))) dentry m);
retval = resultValue s (security-inode-create s (get-inode s (d-inode

(*p-dentry dir*))) *dentry m*)
 in (s',retval)

definition *filename-create* :: *int* \Rightarrow *string* \Rightarrow *path* \Rightarrow *nat* \Rightarrow *dentry option*
 where *filename-create* *dfd name path lookup-flags* \equiv *Some(SOME x:: dentry . True)*

definition *getname pathname* \equiv *SOME x::string . True*

definition *user-path-create* :: *int* \Rightarrow *string* \Rightarrow *path* \Rightarrow *nat* \Rightarrow *dentry option*
 where *user-path-create* *dfd pathname path lookup-flags* \equiv
 let name = getname pathname in
 filename-create *dfd name path lookup-flags*

definition *do-mknodat* :: '*a* \Rightarrow *process-id* \Rightarrow *int* \Rightarrow *string* \Rightarrow *mode* \Rightarrow *nat* \Rightarrow '*a* \times *int*
 where *do-mknodat s pid dfd filename m dev* \equiv
 let
 path = SOME x:: path . True ;
 lookup-flags = 0;
 dentry = (the (user-path-create dfd filename path lookup-flags));
 error = resultValue s (security-path-mknod s path dentry (nat m) dev)
 in if error \neq 0 then
 (s,error)
 else
 (s,0)

typedecl *bpf-type*

definition *current-umask* :: '*a* \Rightarrow *int*
 where *current-umask s* \equiv *umask (fs (current-process s))*

definition *bpf-obj-do-pin* :: '*a* \Rightarrow *process-id* \Rightarrow *string* \Rightarrow *string* \Rightarrow *bpf-type* \Rightarrow '*a* \times *int*
 where *bpf-obj-do-pin s pid pathname raw type'* \equiv
 let
 path = SOME x:: path . True ;
 mode = bitOR S-IFREG ((bitOR S-IRUSR S-IWUSR) AND (NOT
 current-umask s)) ;
 dentry = SOME x::dentry . True;
 ret = resultValue s (security-path-mknod s path dentry (nat mode) 0)
 in if ret \neq 0 then
 (s,ret)
 else
 (s,0)

definition *unix-mknod* :: '*a* \Rightarrow *process-id* \Rightarrow *string* \Rightarrow *mode* \Rightarrow *path* \Rightarrow '*a* \times *int*
 where *unix-mknod s pid sun-path m res* \equiv
 let

```

    path = SOME x:: path . True ;
    dentry = SOME x::dentry . True;
    ret = resultValue s (security-path-mknod s path dentry (nat m) 0)
  in if ret ≠ 0 then
    (s,ret)
  else
    (s,0)

```

29.9.3 kernel action of security_{path_mkdir}

definition *lookup-one-len* :: 'a ⇒ string ⇒ dentry ⇒ int ⇒ dentry
where *lookup-one-len* s name base len' ≡ SOME x :: dentry . True

definition *cachefiles-get-directory* :: 'a ⇒ process-id ⇒ cachefiles-cache
 ⇒ dentry ⇒ string ⇒ 'a × dentry option
where *cachefiles-get-directory* s pid cache' dir dirname ≡
 let
 path = SOME x:: path . True ;
 path = path (| p-mnt := cc-mnt cache', p-dentry := dir|);
 subdir = lookup-one-len s dirname dir (int (length(dirname)));
 ret = resultValue s (security-path-mkdir s path subdir 448)
 in if ret < 0 then (s,None)
 else (s,Some subdir)

definition *SB-POSIXACL* ≡ 1 << 16

definition *IS-FLG'* inode flg ≡ (int(s-flags (i-sb inode))) AND flg

definition *IS-POSIXACL* :: inode ⇒ int
where *IS-POSIXACL* inode ≡ *IS-FLG'* inode *SB-POSIXACL*

definition *do-mkdirat* :: 'a ⇒ process-id ⇒ int ⇒ string ⇒ mode ⇒ 'a × int
where *do-mkdirat* s pid dfd pathname m ≡
 let
 path = SOME x:: path . True ;
 dentry = SOME x::dentry . True;
 inode = get-inode s (d-inode (p-dentry path));
 mode = if ((*IS-POSIXACL* inode) = 0)
 then (m AND (NOT (current-umask s)))
 else (m);
 ret = resultValue s (security-path-mkdir s path dentry (nat mode))
 in (s,ret)

29.9.4 kernel action of security_{path_rmdir}

definition *do-rmdir* :: 'a ⇒ process-id ⇒ int ⇒ string ⇒ 'a × int
where *do-rmdir* s pid dir dentry ≡
 let
 path = SOME x:: path . True ;
 dentry = SOME x::dentry . True;

```

    ret = resultValue s ( security-path-rmdir s path dentry )
in (s,ret)

```

typeddecl *fscache-why-object-killed*
type-synonym *fswhyok* = *fscache-why-object-killed*

29.9.5 kernel action of security_{path_uunlink}

definition *cachefiles-bury-object* :: 'a ⇒ process-id ⇒ cachefiles-cache ⇒ cachefiles-object

```

    ⇒ dentry ⇒ dentry ⇒ bool ⇒ fswhyok ⇒ 'a × int
where cachefiles-bury-object s pid cache' object dir rep preemptive why ≡
    if ¬ (d-is-dir rep) then
    let
        path = SOME x:: path .True ;
        path = path (| p-mnt := cc-mnt cache', p-dentry := dir|);
        ret = resultValue s ( security-path-unlink s path rep )
    in if ret < 0 then (s,ret) else (s,0)
    else
    let
        path = SOME x:: path .True ;
        path-to-graveyard = SOME x:: path .True ;
        path = path (| p-mnt := cc-mnt cache', p-dentry := dir|);
        path-to-graveyard = path-to-graveyard (| p-mnt := cc-mnt cache', p-dentry
:= graveyard cache'|);
        nbuffer = SOME x::string .True;
        grave = lookup-one-len s nbuffer (graveyard cache') (int(length(nbuffer)));
        ret = resultValue s ( security-path-rename s path rep path-to-graveyard
grave 0)
    in if ret < 0 then (s,ret) else (s,0)

```

definition *do-unlinkat* :: 'a ⇒ process-id ⇒ int ⇒ string ⇒ 'a × int

```

where do-unlinkat s pid dfd name≡
    let
        path = SOME x:: path .True ;
        dentry = SOME x::dentry . True;
        ret = resultValue s ( security-path-unlink s path dentry )
    in (s,ret)

```

29.9.6 kernel action of security_{path_ssymlink}

definition *do-symlinkat* :: 'a ⇒ process-id ⇒ string ⇒ int ⇒ string ⇒ 'a × int

```

where do-symlinkat s pid oldname newdfd newname≡
    let
        path = SOME x:: path .True ;
        lookup-flags = 0;
        dentry = user-path-create newdfd newname path lookup-flags;
        ret = resultValue s ( security-path-symlink s path (the dentry) oldname)
    in (s,ret)

```

29.9.7 kernel action of security_{pathlink}

definition *do-linkat* :: 'a \Rightarrow process-id \Rightarrow int \Rightarrow string \Rightarrow int \Rightarrow string \Rightarrow int \Rightarrow 'a \times int

where *do-linkat* *s* *pid* *olddfd* *oldname* *newdfd* *newname* *flgs* \equiv
 let
 oldpath = *SOME* *x*:: *path* .*True* ;
 newpath = *SOME* *x*:: *path* .*True* ;
 path = *p-dentry* *oldpath*;
 dentry = *SOME* *x*::*dentry* . *True*;
 how = 0;
 how = if (*flgs* AND *AT-EMPTY-PATH*) \neq 0 then *LOOKUP-EMPTY*
 else *how*;
 how = if (*flgs* AND *AT-SYMLINK-FOLLOW*) \neq 0 then bitOR *how* *LOOKUP-FOLLOW*
 else *how*;
 lookup-flgs = (*how* AND *LOOKUP-REVAL*);
 new-dentry = (*the*(*user-path-create* *newdfd* *newname* *newpath* (*nat* *lookup-flgs*)));
 ret = *resultValue* *s* (*security-path-link* *s* *path* *newpath* *new-dentry*)
 in (*s*,*ret*)

29.9.8 kernel action of security_{pathrename}

definition *do-renameat2* :: 'a \Rightarrow process-id \Rightarrow int \Rightarrow string \Rightarrow int \Rightarrow string \Rightarrow nat \Rightarrow 'a \times int

where *do-renameat2* *s* *pid* *olddfd* *oldname* *newdfd* *newname* *flgs* \equiv
 let
 old-path = *SOME* *x*:: *path* .*True* ;
 new-path = *SOME* *x*:: *path* .*True* ;
 old-dentry = *SOME* *x*::*dentry* . *True*;
 new-dentry = *SOME* *x*::*dentry* . *True*;
 ret = *resultValue* *s* (*security-path-rename* *s* *old-path* *old-dentry* *new-path* *new-dentry* *flgs*)
 in (*s*,*ret*)

29.9.9 kernel action of security_{pathtruncate}

definition *handle-truncate* :: 'a \Rightarrow process-id \Rightarrow Files \Rightarrow 'a \times int

where *handle-truncate* *s* *pid* *filp* \equiv
 let
 path = *f-path* *filp*;
 ret = *resultValue* *s* (*security-path-truncate* *s* *path*)
 in (*s*,*ret*)

definition *vfs-truncate* :: 'a \Rightarrow process-id \Rightarrow path \Rightarrow loff-t \Rightarrow 'a \times int

where *vfs-truncate s pid path length'* \equiv
 let
 ret = *resultValue s (security-path-truncate s path)*
 in (s,ret)

definition *FMODE-PATH* $\equiv 0x4000$

definition *f-fget-light* :: '*a* \Rightarrow *nat* \Rightarrow *int* \Rightarrow *nat*
 where *f-fget-light s fd mask'* \equiv *let files = files (current-process s)*
 in (nat(count files))

definition *f-fdget* :: '*a* \Rightarrow *nat* \Rightarrow *nat*
 where *f-fdget s fd* \equiv *f-fget-light s fd FMODE-PATH*

definition *do-sys-ftruncate* :: '*a* \Rightarrow *process-id* \Rightarrow *int* \Rightarrow *loff-t* \Rightarrow *int* \Rightarrow '*a* \times *int*
 where *do-sys-ftruncate s pid fd length' small* \equiv
 let
 f = *SOME x :: fd. True*;
 files = *fdfile f*;
 path = *f-path files*;
 ret = *resultValue s (security-path-truncate s path)*
 in (s,ret)

29.9.10 kernel action of security_{path}chmod

definition *chmod-common* :: '*a* \Rightarrow *process-id* \Rightarrow *path* \Rightarrow *mode* \Rightarrow '*a* \times *int*
 where *chmod-common s pid path mode'* \equiv
 let
 inode = *get-inode s (d-inode (p-dentry path))*;
 mode = *nat mode'*;
 ret = *resultValue s (security-path-chmod s path mode)*
 in (s,ret)

29.9.11 kernel action of security_{path}chown

definition *chown-common* :: '*a* \Rightarrow *process-id* \Rightarrow *path* \Rightarrow *uid-t* \Rightarrow *gid-t* \Rightarrow '*a* \times *int*
 where *chown-common s pid path user group'* \equiv
 let
 inode = *get-inode s (d-inode (p-dentry path))*;
 uid = *make-kuid (current-user-ns s) user*;
 gid = *make-kgid (current-user-ns s) group'*;
 ret = *resultValue s (security-path-chown s path uid gid)*
 in (s,ret)

29.9.12 kernel action of security_{path}chroot

definition *ksys-chroot* :: '*a* \Rightarrow *process-id* \Rightarrow *string* \Rightarrow '*a* \times *int*

where *ksys-chroot s pid filename* \equiv
 let
 path = *SOME x*:: *path* . *True* ;
 ret = *resultValue s* (*security-path-chroot s path*)
 in (*s,ret*)

29.10 inode

29.10.1 kernel action of *security_inode_create*

definition *cachefiles-check-cache-dir* :: '*a* \Rightarrow *process-id* \Rightarrow *cachefiles-cache*
 \Rightarrow *dentry* \Rightarrow '*a* \times *int*

where *cachefiles-check-cache-dir s pid cache' root* \equiv
 let
 ret = *resultValue s* (*security-inode-mkdir s* (*the(d-backing-inode s root)*))
root 0)
 in if *ret* < 0 then (*s,ret*)
 else
 let
 ret = *resultValue s* (*security-inode-create s* (*the(d-backing-inode s*
root))) *root 0*)
 in if *ret* < 0 then (*s, ret*)
 else (*s,0*)

definition *vfs-create* :: '*a* \Rightarrow *process-id* \Rightarrow *inode* \Rightarrow *dentry* \Rightarrow *mode* \Rightarrow *bool*
 \Rightarrow '*a* \times *int*

where *vfs-create s pid dir dentry m want-excl* \equiv
 let *mode* = *m AND S-IALLUGO*;
 mode = *bitOR mode S-IFREG*;
 ret = *resultValue s* (*security-inode-create s dir dentry mode*)
 in (*s,ret*)

definition *vfs-mkobj* :: '*a* \Rightarrow *process-id* \Rightarrow *dentry* \Rightarrow *mode* \Rightarrow '*a* \times *int*

where *vfs-mkobj s pid dentry m* \equiv
 let
 dir = *get-inode s* (*d-inode* (*get-dentry s* (*d-parent dentry*)));
 mode = *m AND S-IALLUGO*;
 mode = *bitOR mode S-IFREG*;
 ret = *resultValue s* (*security-inode-create s dir dentry mode*)
 in (*s,ret*)

29.10.2 kernel action of *security_inode_link*

definition *vfs-link* :: '*a* \Rightarrow *process-id* \Rightarrow *dentry* \Rightarrow *inode* \Rightarrow *dentry* \Rightarrow *inode* \Rightarrow
'*a* \times *int*

where *vfs-link s pid old-dentry dir new-dentry delegated-inode* \equiv
 let
 ret = *resultValue s* (*security-inode-link s old-dentry dir new-dentry*)
 in (*s,ret*)

29.10.3 kernel action of security_{inode_uunlink}

definition $vfs-unlink :: 'a \Rightarrow process-id \Rightarrow inode \Rightarrow dentry \Rightarrow inode \Rightarrow 'a \times int$
where $vfs-unlink\ s\ pid\ dir\ dentry\ delegated-inode \equiv$
 let
 $ret = resultValue\ s\ (security-inode-unlink\ s\ dir\ dentry)$
 $in\ (s,ret)$

29.10.4 kernel action of security_{inode_ssymlink}

definition $vfs-symlink :: 'a \Rightarrow process-id \Rightarrow inode \Rightarrow dentry \Rightarrow string \Rightarrow 'a \times int$
where $vfs-symlink\ s\ pid\ dir\ dentry\ oldname \equiv$
 let
 $ret = resultValue\ s\ (security-inode-symlink\ s\ dir\ dentry\ oldname)$
 $in\ (s,ret)$

29.10.5 kernel action of security_{inode_mmkdir}

definition $vfs-mkdir :: 'a \Rightarrow process-id \Rightarrow inode \Rightarrow dentry \Rightarrow mode \Rightarrow 'a \times int$
where $vfs-mkdir\ s\ pid\ dir\ dentry\ m \equiv$
 let
 $ret = resultValue\ s\ (security-inode-mkdir\ s\ dir\ dentry\ m)$
 $in\ (s,ret)$

29.10.6 kernel action of security_{inode_rrmdir}

definition $vfs-rmdir :: 'a \Rightarrow process-id \Rightarrow inode \Rightarrow dentry \Rightarrow 'a \times int$
where $vfs-rmdir\ s\ pid\ dir\ dentry \equiv$
 let
 $ret = resultValue\ s\ (security-inode-rmdir\ s\ dir\ dentry)$
 $in\ (s,ret)$

29.10.7 kernel action of security_{inode_mmknod}

definition $vfs-mknod :: 'a \Rightarrow process-id \Rightarrow inode \Rightarrow dentry \Rightarrow mode \Rightarrow dev-t \Rightarrow 'a \times int$
where $vfs-mknod\ s\ pid\ dir\ dentry\ m\ dev \equiv$
 let
 $ret = resultValue\ s\ (security-inode-mknod\ s\ dir\ dentry\ m\ dev)$
 $in\ (s,ret)$

29.10.8 kernel action of security_{inode_rrename}

definition $vfs-rename :: 'a \Rightarrow process-id \Rightarrow inode \Rightarrow dentry$
 $\Rightarrow inode \Rightarrow dentry \Rightarrow inode \Rightarrow nat \Rightarrow 'a \times int$

where *vfs-rename* *s pid old-dir old-dentry new-dir new-dentry delegated-inode flgs*
 \equiv
 let
 $\text{ret} = \text{resultValue } s \text{ (security-inode-rename } s \text{ old-dir old-dentry new-dir new-dentry flgs)}$
 $\text{in } (s, \text{ret})$

29.10.9 kernel action of security_{inode_readlink}

definition *vfs-get-link* :: '*a* \Rightarrow process-id \Rightarrow dentry \Rightarrow delayed-call \Rightarrow '*a* \times int
where *vfs-get-link* *s pid dentry done* \equiv
 let
 $\text{ret} = \text{resultValue } s \text{ (security-inode-readlink } s \text{ dentry)}$
 $\text{in } (s, \text{ret})$

definition *do-readlinkat* :: '*a* \Rightarrow process-id \Rightarrow int \Rightarrow string \Rightarrow string \Rightarrow int \Rightarrow '*a* \times int
where *do-readlinkat* *s pid dfd pathname buf bufsize* \equiv
 let
 $\text{path} = \text{SOME } x :: \text{path. True};$
 $\text{dentry} = \text{p-dentry path};$
 $\text{ret} = \text{resultValue } s \text{ (security-inode-readlink } s \text{ dentry)}$
 $\text{in } (s, \text{ret})$

29.10.10 kernel action of security_{inode_followlink}

definition *get-link* :: '*a* \Rightarrow process-id \Rightarrow nameidata \Rightarrow '*a* \times int
where *get-link* *s pid nd* \equiv
 let
 $\text{depth} = \text{depth } nd - 1;$
 $\text{last} = \text{stack } nd ! \text{depth};$
 $\text{dentry} = \text{p-dentry}(\text{saved-link last});$
 $\text{inode} = \text{link-inode } nd;$
 $n = (\text{int}(\text{nd-flgs } nd)) \text{ AND LOOKUP-RCU};$
 $\text{rcu} = \text{if } n \neq 0 \text{ then True else False};$
 $\text{ret} = \text{resultValue } s \text{ (security-inode-follow-link } s \text{ dentry inode rcu)}$
 $\text{in } (s, \text{ret})$

29.10.11 kernel action of security_{inode_permission}

definition *inode-permission* :: '*a* \Rightarrow process-id \Rightarrow inode \Rightarrow int \Rightarrow '*a* \times int
where *inode-permission* *s pid inode mask'* \equiv
 let
 $\text{ret} = \text{resultValue } s \text{ (security-inode-permission } s \text{ inode mask')}$
 $\text{in } (s, \text{ret})$

29.10.12 kernel action of security_inode_setattrsecurity_inode_need_kkillpriv

definition *notify-change* :: 'a ⇒ process-id ⇒ dentry ⇒ iattr ⇒ inode ⇒ 'a × int

where *notify-change* *s* *pid* *dentry* *attr'* *delegated-inode* ≡
 let
 inode = *get-inode* *s* (*d-inode* *dentry*);
 ia-valid = *ia-valid* *attr'*;
 ret = (if (int *ia-valid* AND *ATTR-KILL-PRIV*) = 0 then
 resultValue *s* (*security-inode-setattr* *s* *dentry* *attr'*)
 else
 resultValue *s* (*security-inode-need-killpriv* *s* *dentry*))
 in (*s*,*ret*)

definition *current-time* :: inode ⇒ timespec64

where *current-time* *i* ≡ *SOME* *x*:: timespec64. *True*

29.10.13 kernel action of security_inode_setattr

definition *fat-iocctl-set-attributes* :: 'a ⇒ process-id ⇒ Files ⇒ 'a × int

where *fat-iocctl-set-attributes* *s* *pid* *f* ≡
 let
 dentry = *p-dentry*(*f-path* *f*);
 inode = *file-inode* *f*;
 is-dir = *S-ISDIR* (*i-mode* *inode*);
 ia = *SOME* *x*:: iattr . *True*;
 sbi = *SOME* *x*:: msdos-sb-info . *True*;
 ia-valid' = *nat*(*bitOR* *ATTR-MODE* *ATTR-CTIME*);
 attr' = *SOME* *x*::char. *True*;
 ia-mode' = if *is-dir* then *fat-make-mode* *sbi* *attr'* (*nat* *S-IRWXUGO*)
 else *fat-make-mode* *sbi* *attr'* (*nat* ((*bitOR* (*bitOR* *S-IRUGO*
S-IWUGO)
 (*i-mode* *inode* AND *S-IXUGO*)))));
 ia = *ia* | *ia-valid* := *ia-valid'*, *ia-ctime* := *current-time* *inode* |;
 ret = *resultValue* *s* (*security-inode-setattr* *s* *dentry* *ia*)
 in (*s*,*ret*)

29.10.14 kernel action of security_inode_getattr

definition *vfs-getattr* :: 'a ⇒ process-id ⇒ path ⇒ 'a × int

where *vfs-getattr* *s* *pid* *path* ≡
 let
 ret = *resultValue* *s* (*security-inode-getattr* *s* *path*)
 in (*s*,*ret*)

29.10.15 kernel action of security_inode_setxattr

definition *vfs-setxattr* :: 'a ⇒ process-id ⇒ dentry ⇒ xattr ⇒ string ⇒ nat ⇒ nat ⇒ 'a × int

where $vfs\text{-}setxattr\ s\ pid\ dentry\ name\ value\ size'\ flgs \equiv$
 let
 $ret = resultValue\ s\ (security\text{-}inode\text{-}setxattr\ s\ dentry\ name\ value\ size'\ flgs)$
 $in\ (s,ret)$

definition $vfs\text{-}setxattr\text{-}noperm :: 'a \Rightarrow process\text{-}id \Rightarrow dentry \Rightarrow xattr \Rightarrow Void$
 $\Rightarrow nat \Rightarrow nat \Rightarrow 'a \times int$

where $vfs\text{-}setxattr\text{-}noperm\ s\ pid\ dentry\ name\ value\ size'\ flgs \equiv$
 let
 $inode = get\text{-}inode\ s\ (d\text{-}inode\ dentry);$
 $f = int(i\text{-}opflags\ inode)\ AND\ IOP\text{-}XATTR\ ;$
 $value' = SOME\ v.\ String\ v = value;$
 $s' = funcState\ s\ (security\text{-}inode\text{-}post\text{-}setxattr\ s\ dentry\ name\ value'\ size'\ flgs)$
 $in\ if\ f \neq 0\ then\ (s',0)$
 $else$
 let
 $suffix' = SOME\ x::xattr.\ True;$
 $s' = funcState\ s\ (security\text{-}inode\text{-}setsecurity\ s\ inode\ suffix'\ value\ size'\ flgs);$
 $ret = resultValue\ s\ (security\text{-}inode\text{-}setsecurity\ s\ inode\ suffix'\ value\ size'\ flgs)$
 $in\ (s',ret)$

29.10.16 kernel action of $security_{inode_getxattr}$

definition $vfs\text{-}getxattr :: 'a \Rightarrow process\text{-}id \Rightarrow dentry \Rightarrow xattr \Rightarrow string \Rightarrow nat \Rightarrow 'a \times int$

where $vfs\text{-}getxattr\ s\ pid\ dentry\ name\ value\ size' \equiv$
 let
 $ret = resultValue\ s\ (security\text{-}inode\text{-}getxattr\ s\ dentry\ name)$
 $in\ (s,ret)$

29.10.17 kernel action of $security_{inode_listxattr}$

definition $vfs\text{-}listxattr :: 'a \Rightarrow process\text{-}id \Rightarrow dentry \Rightarrow string \Rightarrow nat \Rightarrow 'a \times int$

where $vfs\text{-}listxattr\ s\ pid\ dentry\ value\ size' \equiv$
 let
 $inode = get\text{-}inode\ s\ (d\text{-}inodeid\ dentry);$
 $ret = resultValue\ s\ (security\text{-}inode\text{-}listxattr\ s\ dentry)$
 $in\ if\ (ret \neq 0)\ then\ (s,ret)$
 $else$
 let
 $ret = resultValue\ s\ (security\text{-}inode\text{-}listsecurity\ s\ inode\ (String\ value)\ size')$
 $in\ (s,ret)$

29.10.18 kernel action of security_inode_rremovexattr

definition *vfs-removexattr* :: 'a ⇒ process-id ⇒ dentry ⇒ xattr ⇒ 'a × int
where *vfs-removexattr* s pid dentry name ≡
let
ret = resultValue s (security-inode-removexattr s dentry name)
in (s,ret)

29.10.19 kernel action of security_inode_need_killpriv

definition *dentry-needs-remove-privs* :: 'a ⇒ process-id ⇒ dentry ⇒ 'a × int
where *dentry-needs-remove-privs* s pid dentry ≡
let
ret = resultValue s (security-inode-need-killpriv s dentry)
in (s,ret)

definition *setattr-prepare* :: 'a ⇒ process-id ⇒ dentry ⇒ iattr ⇒ 'a × int
where *setattr-prepare* s pid dentry attr' ≡
let
ret = resultValue s (security-inode-killpriv s dentry)
in (s,ret)

29.10.20 kernel action of security_inode_getsecurity

definition *xattr-getsecurity* :: 'a ⇒ process-id ⇒ inode
⇒ xattr ⇒ string ⇒ int ⇒ 'a × int
where *xattr-getsecurity* s pid inode name value size' ≡
let
buffer = [];
ret = resultValue s (security-inode-getsecurity s inode name (String
buffer) True)
in (s,ret)

29.10.21 kernel action of security_inode_setsecurity

definition *kernfs-node-setsecddata* :: kernfs-iattrs ⇒ string ⇒ nat ⇒ int
where *kernfs-node-setsecddata* ka value len' ≡ 0

definition *kernfs-security-xattr-set* :: 'a ⇒ process-id ⇒ inode ⇒ xattr
⇒ string ⇒ nat ⇒ int ⇒ 'a × int
where *kernfs-security-xattr-set* s pid inode suffix' value size' flgs ≡
let
secddata = [];
attrs = SOME x :: kernfs-iattrs . True;
ret = resultValue s (security-inode-setsecurity s inode suffix' (String
value) size' flgs);
s' = funcState s (security-inode-setsecurity s inode suffix' (String value)
size' flgs)
in if (ret ≠ 0) then (s',ret)
else

```

let
  ret = resultValue s ( security-inode-getsecctx s inode ( secdata) 0 )
in if (ret ≠ 0) then (s,ret)
   else let
     error = kernfs-node-setsecdata attrs secdata 0;
     s' = funcState s ( security-release-secctx s secdata 0)
   in (s,0)

```

29.10.22 kernel action of security_inode_{list}security

definition *nfs4-listxattr-nfs4-label* :: 'a ⇒ process-id ⇒ inode ⇒ string ⇒ int ⇒ 'a × int

where *nfs4-listxattr-nfs4-label* s pid inode name size' ≡

```

let
  ret = resultValue s (security-inode-listsecurity s inode (String name)
size')
in (s,ret)

```

definition *sockfs-listxattr* :: 'a ⇒ process-id ⇒ dentry ⇒ string ⇒ int ⇒ 'a × int

where *sockfs-listxattr* s pid dentry buffer size' ≡

```

let
  inode = get-inode s (d-inodeid dentry);
  ret = resultValue s ( security-inode-listsecurity s inode (String buffer)
size')
in (s,ret)

```

29.10.23 kernel action of security_inode_{getsecid}

definition *audit-copy-inode* :: 'a ⇒ process-id ⇒ audit-names ⇒ dentry ⇒ inode ⇒ 'a × unit

where *audit-copy-inode* s pid name dentry inode ≡

```

let
  s' = funcState s (security-inode-getsecid s inode (osid name))
in (s',())

```

definition *ima-match-rules* :: 'a ⇒ process-id ⇒ inode ⇒ 'a × bool

where *ima-match-rules* s pid inode ≡

```

let
  osid = SOME x:: u32 . True;
  s' = funcState s (security-inode-getsecid s inode osid )
in (s',True)

```

29.10.24 kernel action of security_inode_{copy_{up}}

definition *ovl-get-tmpfile* :: 'a ⇒ process-id ⇒ ovl-copy-up-ctx ⇒ 'a × int

where *ovl-get-tmpfile* s pid c ≡

```

let
  dentry = copy-dentry c;
  new-creds = None;

```

ret = *resultValue s (security-inode-copy-up s dentry new-creds)*
in (s,ret)

29.10.25 kernel action of security_{inode-copy-up}_{xattr}

definition *ovl-copy-xattr* :: 'a ⇒ process-id ⇒ dentry ⇒ dentry ⇒ 'a × int
where *ovl-copy-xattr s pid old new* ≡
let
name = *SOME x:: xattr . True*;
ret = *resultValue s (security-inode-copy-up-xattr s name)*
in (s,ret)

29.11 ipc

definition *ipcperms* :: 'a ⇒ process-id ⇒ kern-ipc-perm ⇒ nat ⇒ 'a × int
where *ipcperms s pid ipcp flg* ≡
let retval = *resultValue s (security-ipc-permission s ipcp flg)*
in (s,retval)

definition *audit-ipc-obj* :: 'a ⇒ process-id ⇒ kern-ipc-perm ⇒ 'a × unit
where *audit-ipc-obj s pid ipcp* ≡
let retval = *resultU (security-ipc-getsecid s ipcp 0)*
in (s,())

definition *load-msg* :: 'a ⇒ process-id ⇒ msg-msg ⇒ 'a × msg-msg option
where *load-msg s pid msg* ≡
let retval = *resultValue s (security-msg-msg-alloc s msg)*
in if retval = 0
then (snd(the-run-state(security-msg-msg-alloc s msg) s), Some msg)
else (s,None)

definition *free-msg* :: 'a ⇒ process-id ⇒ msg-msg ⇒ 'a × unit
where *free-msg s pid msg* ≡ (*snd(the-run-state(security-msg-msg-free s msg) s)*,
())

definition *newque* :: 'a ⇒ process-id ⇒ kern-ipc-perm ⇒ 'a × int
where *newque s pid msq* ≡
let retval = *resultValue s (security-msg-queue-alloc s msq)*
in if retval = 0
then (snd(the-run-state(security-msg-queue-alloc s msq) s), id msq)
else (s,retval)

definition *msg-rcu-free* :: 'a ⇒ process-id ⇒ kern-ipc-perm ⇒ 'a × unit
where *msg-rcu-free s pid msq* ≡
(*snd(the-run-state(security-msg-queue-free s msq) s)*, *()*)

definition *ksys-msgget* :: 'a ⇒ process-id ⇒ kern-ipc-perm ⇒ int ⇒ 'a × int
where *ksys-msgget s pid msq msqflg* ≡
let retval = *resultValue s (security-msg-queue-associate s msq msqflg)*
in (s,retval)

definition *msg-queue-msgctl* :: 'a \Rightarrow process-id \Rightarrow kern-ipc-perm \Rightarrow IPC-CMD \Rightarrow 'a \times int
where *msg-queue-msgctl* s pid msq cmd \equiv
let retval = resultValue s (security-msg-queue-msgctl s msq cmd)
in (s,retval)

definition *do-msgsnd* :: 'a \Rightarrow process-id \Rightarrow kern-ipc-perm \Rightarrow msg-msg \Rightarrow int \Rightarrow 'a \times int
where *do-msgsnd* s pid msq msg msgflg \equiv
let retval = resultValue s (security-msg-queue-msgsnd s msq msg msgflg)
in if retval \neq 0 then (s,retval) else (s,0)

definition *msg-queue-msgrcv* :: 'a \Rightarrow process-id \Rightarrow kern-ipc-perm \Rightarrow msg-msg \Rightarrow Task \Rightarrow int \Rightarrow int \Rightarrow 'a \times int
where *msg-queue-msgrcv* s pid isp msq p long msgflg \equiv
let retval = resultValue s (security-msg-queue-msgrcv s isp msq p long msgflg)
in (s,retval)

definition *newseg* :: 'a \Rightarrow process-id \Rightarrow ipc-namespace \Rightarrow ipc-params \Rightarrow 'a \times int
where *newseg* s pid ns params \equiv
let shp = SOME x :: shmid-kernel . True;
shm-perm = shm-perm shp;
retval = resultValue s (security-shm-alloc s shm-perm)
in if retval = 0
then (snd(the-run-state(security-shm-alloc s shm-perm) s), 0)
else (s,retval)

definition *shm-rcu-free* :: 'a \Rightarrow process-id \Rightarrow kern-ipc-perm \Rightarrow 'a \times unit
where *shm-rcu-free* s pid shmperm \equiv
(snd(the-run-state(security-shm-free s shmperm) s), ())

definition *ksys-shmget* :: 'a \Rightarrow process-id \Rightarrow kern-ipc-perm \Rightarrow int \Rightarrow 'a \times int
where *ksys-shmget* s pid shm shmflg \equiv
let retval = resultValue s (security-shm-associate s shm shmflg)
in (s,retval)

definition *shm-msgctl* :: 'a \Rightarrow process-id \Rightarrow kern-ipc-perm \Rightarrow IPC-CMD \Rightarrow 'a \times int
where *shm-msgctl* s pid shm cmd \equiv
let retval = resultValue s (security-shm-shmctl s shm cmd)
in (s,retval)

definition *do-shmat* :: 'a \Rightarrow process-id \Rightarrow kern-ipc-perm \Rightarrow string \Rightarrow int \Rightarrow 'a \times int
where *do-shmat* s pid shp shmaddr shmflg \equiv

```

let
  flgs = MAP-SHARED;
  retval = resultValue s ( security-shm-shmat s shp shmaddr shmflg)
in if retval  $\neq$  0 then (s,retval)
else
  let
    file = SOME x:: Files. True;
    prot = if (shmflg AND SHM-RDONLY )  $\neq$  0 then PROT-READ
  else (bitOR PROT-READ PROT-WRITE);
    prot = if (shmflg AND SHM-EXEC)  $\neq$  0 then bitOR prot
  PROT-EXEC else prot;
  retval = resultValue s ( security-mmap-file s file (nat prot) flgs)
in (s,retval)

```

definition *newary* :: 'a \Rightarrow process-id \Rightarrow ipc-namespace \Rightarrow ipc-params \Rightarrow 'a \times int
where *newary* s pid ns params \equiv
 let sma = SOME x:: sem-array . True;
 sem-perm = sem-perm sma;
 retval = resultValue s (security-sem-alloc s sem-perm)
 in if retval = 0
 then (snd(the-run-state(security-sem-alloc s sem-perm) s), id sem-perm)
 else (s,retval)

definition *sem-rcu-free* :: 'a \Rightarrow process-id \Rightarrow kern-ipc-perm \Rightarrow 'a \times unit
where *sem-rcu-free* s pid semperm \equiv
 (snd(the-run-state(security-sem-free s semperm) s), ())

definition *ksys-semget* :: 'a \Rightarrow process-id \Rightarrow kern-ipc-perm \Rightarrow int \Rightarrow 'a \times int
where *ksys-semget* s pid sem semflg \equiv
 let retval = resultValue s (security-sem-associate s sem semflg)
 in (s,retval)

definition *sem-msgctl* :: 'a \Rightarrow process-id \Rightarrow kern-ipc-perm \Rightarrow IPC-CMD \Rightarrow 'a \times int
where *sem-msgctl* s pid sem cmd \equiv
 let retval = resultValue s (security-sem-semctl s sem cmd)
 in (s,retval)

definition *do-semtimedop* :: 'a \Rightarrow process-id \Rightarrow kern-ipc-perm \Rightarrow sembuf \Rightarrow nat \Rightarrow int \Rightarrow 'a \times int
where *do-semtimedop* s pid sma sops nsops alter \equiv
 let retval = resultValue s (security-sem-semop s sma sops nsops alter)
 in if retval \neq 0 then (s,retval) else (s,0)

29.12 d_instantiate

29.12.1 kernel action of security_{d_instantiate}

definition *d-instantiate* :: 'a \Rightarrow process-id \Rightarrow dentry \Rightarrow inode option \Rightarrow 'a \times unit
where *d-instantiate* s pid entry inode \equiv


```

if inode ≠ None then
let
  inode = the inode;
  retval = resultValue s ( security-d-instantiate s entry inode);
  s' = funcState s ( security-d-instantiate s entry inode)
in
  (s', retval)
else (s,())

```

definition $d\text{-instantiate-new} :: 'a \Rightarrow \text{process-id} \Rightarrow \text{dentry} \Rightarrow \text{inode} \Rightarrow 'a \times \text{unit}$
where $d\text{-instantiate-new } s \text{ pid entry inode} \equiv$
 let
 $\text{retval} = \text{resultValue } s \text{ (security-d-instantiate } s \text{ entry inode);}$
 $s' = \text{funcState } s \text{ (security-d-instantiate } s \text{ entry inode)}$
in
 (s', retval)

definition $d\text{-instantiate-anon}' :: 'a \Rightarrow \text{process-id} \Rightarrow \text{dentry} \Rightarrow \text{inode} \Rightarrow \text{bool} \Rightarrow 'a \times \text{dentry option}$
where $d\text{-instantiate-anon}' s \text{ pid entry inode disconnected} \equiv$
 let
 $\text{res} = \text{SOME } x :: \text{dentry} . \text{True};$
 $\text{retval} = \text{resultValue } s \text{ (security-d-instantiate } s \text{ entry inode);}$
 $s' = \text{funcState } s \text{ (security-d-instantiate } s \text{ entry inode)}$
in
 $(s', \text{Some res})$

definition $d\text{-add} :: 'a \Rightarrow \text{process-id} \Rightarrow \text{dentry} \Rightarrow \text{inode option} \Rightarrow 'a \times \text{unit}$
where $d\text{-add } s \text{ pid entry inode} \equiv$
 if inode ≠ None then
 let
 inode = the inode;
 retval = resultValue s (security-d-instantiate s entry inode);
 s' = funcState s (security-d-instantiate s entry inode)
in
 (s', retval)
 else (s,())

definition $d\text{-splice-alias} :: 'a \Rightarrow \text{process-id} \Rightarrow \text{inode} \Rightarrow \text{dentry} \Rightarrow 'a \times \text{dentry option}$
where $d\text{-splice-alias } s \text{ pid inode dentry} \equiv$
 let
 new = SOME x :: dentry . True;
 retval = resultValue s (security-d-instantiate s dentry inode);
 s' = funcState s (security-d-instantiate s dentry inode)
in
 (s', Some new)

definition $\text{nfs-get-root} :: 'a \Rightarrow \text{process-id} \Rightarrow \text{super-block} \Rightarrow \text{nfs-fh} \Rightarrow \text{string} \Rightarrow 'a \times \text{dentry option}$

where *nfs-get-root s pid sb mntfh devname* \equiv
 let
 inode = *SOME x* :: *inode* . *True*;
 ret = *SOME x* :: *dentry* . *True*;
 retval = *resultValue s* (*security-d-instantiate s ret inode*);
 s' = *funcState s* (*security-d-instantiate s ret inode*)
 in
 (*s'*, *Some ret*)

29.13 file

29.13.1 kernel action of security_{file_permission}

definition *iterate-dir* :: '*a* \Rightarrow *process-id* \Rightarrow *Files* \Rightarrow '*a* \times *int*

where *iterate-dir s pid file* \equiv
 let *retval* = *resultValue s* (*security-file-permission s file MAY-READ*) ;
 s' = *funcState s* (*security-file-permission s file MAY-READ*)
 in (*s'*, *retval*)

definition *vfs-fallocate* :: '*a* \Rightarrow *process-id* \Rightarrow *Files* \Rightarrow *int* \Rightarrow *loff-t* \Rightarrow *loff-t* \Rightarrow '*a* \times *int*

where *vfs-fallocate s pid file m offset len'* \equiv
 let *retval* = *resultValue s* (*security-file-permission s file MAY-WRITE*)
 in *if* *retval* \neq 0 *then*
 (*s*, *retval*)
 else
 (*s*, 0)

definition *rw-verify-area* :: '*a* \Rightarrow *process-id* \Rightarrow *int* \Rightarrow *Files* \Rightarrow *loff-t* \Rightarrow *nat* \Rightarrow '*a* \times *int*

where *rw-verify-area s pid rw file ppos count'* \equiv
 let
 flgs = *if* *rw* = *KREAD* *then* *MAY-READ* *else* *MAY-WRITE*;
 retval = *resultValue s* (*security-file-permission s file flgs*)
 in
 (*s*, *retval*)

definition *clone-verify-area* :: '*a* \Rightarrow *process-id* \Rightarrow *Files* \Rightarrow *loff-t* \Rightarrow *nat* \Rightarrow *bool* \Rightarrow '*a* \times *int*

where *clone-verify-area s pid file pos len' write* \equiv
 let
 flgs = *if* *write* *then* *MAY-READ* *else* *MAY-WRITE*;
 retval = *resultValue s* (*security-file-permission s file flgs*)
 in
 (*s*, *retval*)

29.13.2 kernel action of security_{file_alloc}

definition *alloc-file* :: '*a* \Rightarrow *process-id* \Rightarrow *Files* \Rightarrow *Cred* \Rightarrow '*a* \times *Files option*

where *alloc-file s pid file c* \equiv

```

let retval = resultValue s ( security-file-alloc s file );
  s' = funcState s ( security-file-alloc s file )
in
  if retval  $\neq$  0 then
    (s,None)
  else
    (s',Some file)

```

29.13.3 kernel action of security_{file_free}

definition *file-free* :: 'a \Rightarrow process-id \Rightarrow Files \Rightarrow 'a \times unit
where *file-free* s pid file \equiv (funcState s (security-file-free s file) ,())

29.13.4 kernel action of security_{file_ioctl}

definition *do-ioctl* :: 'a \Rightarrow process-id \Rightarrow Files \Rightarrow IOC-DIR \Rightarrow nat \Rightarrow 'a \times int
where *do-ioctl* s pid file cmd arg \equiv
 let retval = resultValue s (security-file-ioctl s file cmd arg);
 s' = funcState s (security-file-ioctl s file cmd arg)
 in if retval \neq 0 then (s',retval)
 else (s',0)

definition *syscall-ioctl* :: 'a \Rightarrow process-id \Rightarrow nat \Rightarrow IOC-DIR \Rightarrow nat \Rightarrow 'a \times int
where *syscall-ioctl* s pid fd cmd arg \equiv
 let
 file = SOME x :: Files. True;
 retval = resultValue s (security-file-ioctl s file cmd arg)
 in (s,retval)

definition *ksys-ioctl* :: 'a \Rightarrow process-id \Rightarrow nat \Rightarrow IOC-DIR \Rightarrow nat \Rightarrow 'a \times int
where *ksys-ioctl* s pid fd cmd arg \equiv
 let
 file = SOME x :: Files. True;
 retval = resultValue s (security-file-ioctl s file cmd arg)
 in (s,retval)

29.13.5 kernel action of security_{mmap_file}

definition *vm-mmap-pgoff* :: 'a \Rightarrow process-id \Rightarrow Files \Rightarrow nat
 \Rightarrow nat \Rightarrow nat \Rightarrow nat \Rightarrow 'a \times int
where *vm-mmap-pgoff* s pid file addr len' prot flag pgoff \equiv
 let
 retval = resultValue s (security-mmap-file s file prot flag)
 in (s,retval)

29.13.6 kernel action of security_{mmap_addr}

definition *do-sys-vm86* :: 'a \Rightarrow process-id \Rightarrow 'a \times int
where *do-sys-vm86* s pid \equiv

```

let
  retval = resultValue s ( security-mmap-addr s 0)
in
  (s,retval)

```

definition *get-unmapped-area* :: 'a \Rightarrow process-id \Rightarrow Files \Rightarrow nat \Rightarrow 'a \times int
where *get-unmapped-area* s pid file addr \equiv
 let
 retval = resultValue s (security-mmap-addr s addr)
 in if retval \neq 0 then
 (s,retval)
 else (s,addr)

definition *validate-mmap-request* :: 'a \Rightarrow process-id \Rightarrow Files \Rightarrow nat \Rightarrow 'a \times int
where *validate-mmap-request* s pid file addr \equiv
 let
 retval = resultValue s (security-mmap-addr s addr)
 in if retval < 0 then
 (s,retval)
 else
 (s,0)

29.13.7 kernel action of security_{file_mprotect}

definition *do-mprotect-pkey* :: 'a \Rightarrow process-id \Rightarrow nat \Rightarrow nat \Rightarrow nat \Rightarrow int \Rightarrow 'a \times int
where *do-mprotect-pkey* s pid start len' prot pkey \equiv
 let
 vma = SOME x:: vm-area-struct .True;
 rier = (int(personality (current-process s)) AND READ-IMPLIES-EXEC)
 \neq 0 \wedge
 (((int prot) AND PROT-READ) \neq 0);
 prot = (int prot) AND (NOT (bitOR PROT-GROWSDOWN PROT-GROWSUP));
 reqprot = (nat prot);
 prot = if rier \wedge (vm-flags vma AND VM-MAYEXEC) \neq 0
 then bitOR prot PROT-EXEC
 else prot;
 retval = resultValue s (security-file-mprotect s vma reqprot (nat
 prot))
 in (s,retval)

29.13.8 kernel action of security_{file_lock}

definition *generic-setlease* :: 'a \Rightarrow process-id \Rightarrow Files \Rightarrow int \Rightarrow 'a \times int
where *generic-setlease* s pid file arg \equiv
 let retval = resultValue s (security-file-lock s file (nat arg))
 in if retval \neq 0 then (s,retval) else (s,-EINVAL)

definition *syscall-lock* :: 'a \Rightarrow process-id \Rightarrow nat \Rightarrow nat \Rightarrow 'a \times int

where *syscall-lock* *s* *pid* *fd* *cmd* \equiv
 let *file* = *SOME* *x::Files*. *True*;
 retval = *resultValue* *s* (*security-file-lock* *s* *file* *cmd*)
 in (*s*,*retval*)

definition *do-lock-file-wait* :: '*a* \Rightarrow *process-id* \Rightarrow *Files* \Rightarrow *int* \Rightarrow *file-lock* \Rightarrow '*a* \times *int*

where *do-lock-file-wait* *s* *pid* *file* *cmd* *fl* \equiv
 let
 arg = *of-char* (*fl-type* *fl*);
 retval = *resultValue* *s* (*security-file-lock* *s* *file* (*nat* *arg*))
 in *if* *retval* \neq 0 *then* (*s*,*retval*) *else* (*s*,0)

29.13.9 kernel action of security_{filefcntl}

definition *file-fcntl* :: '*a* \Rightarrow *process-id* \Rightarrow *Files* \Rightarrow *nat* \Rightarrow *nat* \Rightarrow '*a* \times *int*

where *file-fcntl* *s* *pid* *file* *cmd* *arg* \equiv
 let *retval* = *resultValue* *s* (*security-file-fcntl* *s* *file* *cmd* *arg*)
 in *if* *retval* \neq 0 *then* (*s*,*retval*) *else* (*s*,0)

29.13.10 kernel action of security_{file_setfowner}

definition *f-setown* :: '*a* \Rightarrow *process-id* \Rightarrow *Files* \Rightarrow '*a* \times *unit*

where *f-setown* *s* *pid* *file* \equiv (*snd*(*the-run-state*(*security-file-set-fowner* *s* *file*)
s),())

29.13.11 kernel action of security_{file_send_sigiotask}

definition *file-send-sigiotask* :: '*a* \Rightarrow *process-id* \Rightarrow *Task* \Rightarrow *fown-struct* \Rightarrow *int* \Rightarrow '*a* \times *int*

where *file-send-sigiotask* *s* *pid* *t* *fown* *sig* \equiv
 let *retval* = *resultValue* *s* (*security-file-send-sigiotask* *s* *t* *fown* *sig*)
 in (*s*,*retval*)

29.13.12 kernel action of security_{file_receive}

definition *file-receive* :: '*a* \Rightarrow *process-id* \Rightarrow *Files* \Rightarrow '*a* \times *int*

where *file-receive* *s* *pid* *f* \equiv
 let *retval* = *resultValue* *s* (*security-file-receive* *s* *f*)
 in (*s*,*retval*)

29.13.13 kernel action of security_{file_open}

definition *do-dentry-open* :: '*a* \Rightarrow *process-id* \Rightarrow *Files* \Rightarrow '*a* \times *int*

where *do-dentry-open* *s* *pid* *f* \equiv
 let *retval* = *resultValue* *s* (*security-file-open* *s* *f*)
 in (*s*,*retval*)

29.14 net

29.14.1 kernel action of security_{netlink_send}

definition *netlink-sendmsg* :: 'a ⇒ process-id ⇒ socket ⇒ msghdr ⇒ nat ⇒ 'a × int

where *netlink-sendmsg* *s pid sock msg len* ≡
 let
 sk' = the(*sk sock*);
 skb = SOME *x*:: *sk-buff* .True;
 retval = resultValue *s* (security-netlink-send *s sk' skb*)
 in (*s*,*retval*)

29.14.2 kernel action of security_{ismaclabel}

definition *nfs4-xattr-set-nfs4-label* :: 'a ⇒ process-id ⇒ xattr
 ⇒ inode ⇒ string ⇒ 'a × int

where *nfs4-xattr-set-nfs4-label* *s pid key' inode buf* ≡
 let
 retval = resultValue *s* (security-ismaclabel *s key'*)
 in if *retval* ≠ 0 then (*s*,0)
 else (*s*,−EOPNOTSUPP)

definition *nfs4-xattr-get-nfs4-label* :: 'a ⇒ process-id ⇒ xattr
 ⇒ inode ⇒ string ⇒ 'a × int

where *nfs4-xattr-get-nfs4-label* *s pid key' inode buf* ≡
 let
 retval = resultValue *s* (security-ismaclabel *s key'*)
 in if *retval* ≠ 0 then (*s*,0)
 else (*s*,−EOPNOTSUPP)

29.15 secid_{to_secctx}

29.15.1 kernel action of security_{secid_{to_secctx}}

definition *scm-passec* :: 'a ⇒ process-id ⇒ socket ⇒ msghdr ⇒ scm-cookie ⇒ 'a × unit

where *scm-passec* *s pid sock msg scm* ≡
 let
 secd = SOME *x*:: *string* .True;
 seclen' = length(*secd*);
 secid = scm-secid *scm*;
 retval = resultValue *s* (security-secid-to-secctx *s secid secd seclen'*)
 in if *retval* = 0 then
 let *s'* = funcState *s* (security-release-secctx *s secd seclen'*)
 in (*s'*,())
 else (*s*,())

definition *audit-receive-msg* :: 'a ⇒ process-id ⇒ sk-buff ⇒ nlmsghdr ⇒ 'a × int

where *audit-receive-msg* *s pid skb nlh* ≡
 let

```

    msg-type = nmsg-type nlh
  in
    if msg-type = nat(AUDIT-SIGNAL-INFO) then let
      secdata = "";
      seclen' = 0;
      secid' = nat audit-sig-sid;
      retval = resultValue s ( security-secid-to-secctx s secid' secdata seclen')

    in (s,retval)
    else (s,0)

```

definition *audit-log-name* :: 'a ⇒ process-id ⇒ audit-names ⇒ 'a × unit
where *audit-log-name* s pid n ≡
 let
 secdata = "";
 seclen' = length(secdata);
 secid = osid n;
 retval = resultValue s (security-secid-to-secctx s secid secdata seclen')
 in if retval = 0 then
 let s' = funcState s (security-release-secctx s secdata seclen')
 in (s',())
 else (s,())

definition *audit-log-task-context* :: 'a ⇒ process-id ⇒ audit-buffer ⇒ 'a × int
where *audit-log-task-context* s pid skb ≡
 let
 secdata = "";
 seclen' = 0;
 secid' = SOME x :: nat . True;
 retval = resultValue s (security-secid-to-secctx s secid' secdata seclen')
 in if retval = 0 then
 let s' = funcState s (security-release-secctx s secdata seclen')
 in (s',0)
 else (s,0)

definition *audit-log-pid-context* :: 'a ⇒ process-id ⇒ u32 ⇒ 'a × int
where *audit-log-pid-context* s pid sid ≡
 if sid ≠ 0 then
 let
 secdata = "";
 seclen' = 0;
 retval = resultValue s (security-secid-to-secctx s sid secdata seclen')
 in if retval = 0 then
 let s' = funcState s (security-release-secctx s secdata seclen')
 in (s',0)
 else (s,1)
 else (s,0)

definition *show-special* :: 'a \Rightarrow process-id \Rightarrow audit-context \Rightarrow 'a \times unit
where *show-special* s pid context \equiv
 let
 secdata = "";
 seclen' = length(secdata);
 secid = audit-context-ipc-osid (ipc context);
 retval = resultValue s (security-secid-to-secctx s secid secdata seclen')
 in if retval = 0 then
 let s' = funcState s (security-release-secctx s secdata seclen')
 in (s',())
 else (s,())

definition *ctnetlink-dump-secctx* :: 'a \Rightarrow process-id \Rightarrow sk-buff \Rightarrow nf-conn \Rightarrow 'a \times int
where *ctnetlink-dump-secctx* s pid skb ct \equiv
 let
 secdata = "";
 seclen' = 0;
 sid = nf-secmark ct;
 retval = resultValue s (security-secid-to-secctx s sid secdata seclen')
 in if retval \neq 0 then (s,0)
 else
 let s' = funcState s (security-release-secctx s secdata seclen')
 in (s',-1)

definition *ctnetlink-secctx-size* :: 'a \Rightarrow process-id \Rightarrow nf-conn \Rightarrow 'a \times int
where *ctnetlink-secctx-size* s pid ct \equiv
 let
 secdata = "";
 seclen' = 0;
 sid = nf-secmark ct;
 retval = resultValue s (security-secid-to-secctx s sid secdata seclen')
 in if retval \neq 0 then (s,0)
 else (s,-1)

definition *ct-show-secctx* :: 'a \Rightarrow process-id \Rightarrow seq-file \Rightarrow nf-conn \Rightarrow 'a \times unit
where *ct-show-secctx* s pid seqfile ct \equiv
 let
 secdata = SOME x::string . True;
 seclen' = length(secdata);
 secid = nf-secmark ct;
 retval = resultValue s (security-secid-to-secctx s secid secdata seclen')
 in if retval = 0 then
 let s' = funcState s (security-release-secctx s secdata seclen')
 in (s',())
 else (s,())

definition *nfqnl-get-sk-secctx* :: 'a \Rightarrow process-id \Rightarrow sk-buff \Rightarrow string \Rightarrow 'a \times int
where *nfqnl-get-sk-secctx* s pid skb secdata \equiv


```

let
  seclen' = 0;
  sid = secmark skb;
  retval = resultValue s (security-secid-to-secctx s sid secdata seclen')
in (s,int seclen')

```

definition *netlbl-unlshsh-func3* :: 'a \Rightarrow process-id \Rightarrow u32 \Rightarrow 'a \times int
where *netlbl-unlshsh-func3* s pid secid' \equiv

```

let
  secdata = "";
  secctx-len = SOME x:: u32. True;
  ret-val = SOME x:: int. True;
  sid = secid';
  retval = resultValue s (security-secid-to-secctx s sid secdata secctx-len)
in if retval  $\neq$  0 then (s,0)
   else
     let s' = funcState s ( security-release-secctx s secdata secctx-len)
     in (s',ret-val)

```

definition *netlbl-unlabel-staticlist-gen* :: 'a \Rightarrow process-id \Rightarrow u32 \Rightarrow 'a \times int
where *netlbl-unlabel-staticlist-gen* s pid secid' \equiv

```

let
  secctx = SOME x:: string. True;
  secctx-len = SOME x:: u32. True;
  sid = secid';
  retval = resultValue s (security-secid-to-secctx s sid secctx secctx-len)
in if retval  $\neq$  0 then (s,retval)
   else
     let s' = funcState s ( security-release-secctx s secctx secctx-len)
     in (s',0)

```

definition *netlbl-audit-start-common* :: 'a \Rightarrow process-id \Rightarrow int
 \Rightarrow netlbl-audit \Rightarrow 'a \times audit-buffer option
where *netlbl-audit-start-common* s pid type' audit-info \equiv

```

let
  buf = SOME x:: audit-buffer. True;
  secctx = SOME x:: string. True;
  secctx-len = SOME x:: u32. True;
  sid = netlbl-audit-secid audit-info;
  retval = resultValue s (security-secid-to-secctx s (nat sid) secctx secctx-len)
in if sid  $\neq$  0  $\wedge$  retval = 0 then
  let s' = funcState s ( security-release-secctx s secctx secctx-len)
  in (s',Some buf)
   else (s,Some buf)

```

29.15.2 kernel action of $\text{security}_{\text{secctx}_t o_{\text{secid}}}$

definition $\text{set-security-override-from-ctx} :: 'a \Rightarrow \text{process-id} \Rightarrow \text{Cred} \Rightarrow \text{string} \Rightarrow 'a \times \text{int}$

where $\text{set-security-override-from-ctx } s \text{ pid new secctx} \equiv$
 let
 $\text{secid} = \text{SOME } x :: u32 . \text{True};$
 $\text{len} = \text{length}(\text{secctx});$
 $\text{retval} = \text{resultValue } s \text{ (security-secctx-to-secid } s \text{ secctx len secid}$
 $)$
 $\text{in if } \text{retval} < 0 \text{ then } (s, \text{retval})$
 $\text{else } (s, \text{snd}(\text{set-security-override } s \text{ pid new secid}))$

definition $\text{netlbl-unlabel-staticadd} :: 'a \Rightarrow \text{process-id} \Rightarrow 'a \times \text{int}$

where $\text{netlbl-unlabel-staticadd } s \text{ pid} \equiv$
 let
 $\text{secid} = \text{SOME } x :: u32 . \text{True};$
 $\text{secctx} = \text{SOME } x :: \text{string} . \text{True};$
 $\text{len} = \text{length}(\text{secctx});$
 $\text{retval} = \text{resultValue } s \text{ (security-secctx-to-secid } s \text{ secctx len secid}$
 $)$
 $\text{in if } \text{retval} \neq 0 \text{ then } (s, \text{retval})$
 $\text{else } (s, 0)$

29.15.3 kernel action of $\text{security}_{\text{release}_{\text{secctx}}}$

definition $\text{kernfs-put} :: 'a \Rightarrow \text{process-id} \Rightarrow \text{kernfs-node} \Rightarrow 'a \times \text{unit}$

where $\text{kernfs-put } s \text{ pid kn} \equiv$
 let
 $\text{secddata} = \text{ia-secddata } (\text{kn-iattr } \text{kn});$
 $\text{seclen}' = \text{ia-secddata-len } (\text{kn-iattr } \text{kn});$
 $s' = \text{funcState } s \text{ (security-release-secctx } s \text{ secddata seclen')}$
 $\text{in } (s', ())$

definition $\text{nfs4-label-release-security} :: 'a \Rightarrow \text{process-id} \Rightarrow \text{nfs4-label option} \Rightarrow 'a \times \text{unit}$

where $\text{nfs4-label-release-security } s \text{ pid label'} \equiv (\text{if } \text{label}' \neq \text{None} \text{ then}$
 let
 $\text{secddata} = \text{label } (\text{the label}');$
 $\text{seclen}' = \text{len } (\text{the label}');$
 $s' = \text{funcState } s \text{ (security-release-secctx } s \text{ secddata seclen')}$
 $\text{in } (s', ()) \text{ else } (s, ()))$

29.15.4 kernel action of $\text{security}_{\text{inode}_i \text{invalidate}_{\text{secctx}}}$

definition $\text{inode-go-inval} :: 'a \Rightarrow \text{process-id} \Rightarrow 'a \times \text{unit}$

where $\text{inode-go-inval } s \text{ pid} \equiv$
 let
 $\text{ip} = \text{SOME } x :: \text{gfs2-inode} . \text{True};$
 $i = \text{i-inode } \text{ip};$

$s' = \text{funcState } s \text{ (security-inode-invalidate-secctx } s \text{ i)}$
 $\text{in}(s',())$

29.15.5 kernel action of security_{inode_notifysecctx}

definition *kernfs-refresh-inode*:: 'a \Rightarrow process-id \Rightarrow kernfs-node \Rightarrow inode \Rightarrow 'a \times unit

where *kernfs-refresh-inode* *s* *pid* *kn* *inode* \equiv
 let
 $\text{attrs} = \text{kn-iattr } \text{kn};$
 $s' = \text{funcState } s \text{ (security-inode-notifysecctx } s \text{ inode (ia-secddata attrs)}$
 $\text{(ia-secddata-len attrs))}$
 $\text{in}(s',())$

definition *nfs-setsecurity*:: 'a \Rightarrow process-id \Rightarrow inode \Rightarrow nfs4-label \Rightarrow 'a \times unit

where *nfs-setsecurity* *s* *pid* *inode* *label'* \equiv
 let
 $\text{secddata} = \text{label } \text{label}';$
 $\text{slen} = \text{len } \text{label}';$
 $s' = \text{funcState } s \text{ (security-inode-notifysecctx } s \text{ inode (secddata) slen)}$
 $\text{in}(s',())$

29.15.6 kernel action of security_{inode_setsecctx}

definition *nfsd4-security-inode-setsecctx*:: 'a \Rightarrow process-id \Rightarrow svc-fh \Rightarrow xdr-netobj \Rightarrow u32 \Rightarrow 'a \times unit

where *nfsd4-security-inode-setsecctx* *s* *pid* *resfh* *label'* *bmval* \equiv
 let
 $d = \text{fh-dentry } \text{resfh};$
 $\text{secddata} = \text{xdr-data } \text{label}';$
 $\text{slen} = \text{xdr-len } \text{label}';$
 $s' = \text{funcState } s \text{ (security-inode-setsecctx } s \text{ d (secddata) slen)}$
 $\text{in}(s',())$

definition *nfsd4-set-nfs4-label*:: 'a \Rightarrow process-id \Rightarrow svc-fh \Rightarrow xdr-netobj \Rightarrow 'a \times int

where *nfsd4-set-nfs4-label* *s* *pid* *resfh* *label'* \equiv
 let
 $d = \text{fh-dentry } \text{resfh};$
 $\text{secddata} = \text{xdr-data } \text{label}';$
 $\text{slen} = \text{xdr-len } \text{label}';$
 $s' = \text{funcState } s \text{ (security-inode-setsecctx } s \text{ d (secddata) slen);}$
 $\text{retval} = \text{resultValue } s \text{ (security-inode-setsecctx } s \text{ d (secddata) slen)}$
 $\text{in}(s', \text{retval})$

29.15.7 kernel action of security_{inode_getsecctx}

definition *nfsd4-encode-fattr*:: 'a \Rightarrow process-id \Rightarrow dentry \Rightarrow 'a \times int

where *nfsd4-encode-fattr* *s* *pid* *dentry'* \equiv

```

let
  d = get-inode s (d-inodeid dentry');
  context = ""';
  slen = SOME x:: int . True;
  retval = resultValue s ( security-inode-getsecctx s d (context) slen)
in (s,retval)

```

29.16 socket

29.16.1 kernel action of security_{unixstreamconnect}

definition *unix-stream-connect* :: 'a ⇒ process-id ⇒ socket ⇒ sockaddr ⇒ int ⇒ int ⇒ 'a × int

where *unix-stream-connect* s pid sock uaddr addr-len flags' ≡

```

let
  sk' = the(sk sock);
  other = SOME x:: sock . True;
  newsk = SOME x:: sock . True;
  retval = resultValue s ( security-unix-stream-connect s sk' other
newsk)
in (s,retval)

```

29.16.2 kernel action of security_{unixmaysend}

definition *unix-dgram-connect* :: 'a ⇒ process-id ⇒ socket ⇒ sockaddr ⇒ int ⇒ int ⇒ 'a × int

where *unix-dgram-connect* s pid sock uaddr alen flags' ≡

```

let
  sk' = the(sk sock);
  newsk = get-socket s (sk-socket sk');
  other = SOME x:: sock . True;
  othersk = get-socket s (sk-socket other);
  retval = resultValue s ( security-unix-may-send s newsk othersk)
in (s,retval)

```

definition *unix-dgram-sendmsg* :: 'a ⇒ process-id ⇒ socket ⇒ sockaddr ⇒ int ⇒ 'a × int

where *unix-dgram-sendmsg* s pid sock uaddr alen ≡

```

let
  sk' = the(sk sock);
  newsk = get-socket s (sk-socket sk');
  other = SOME x:: sock . True;
  othersk = get-socket s (sk-socket other);
  retval = resultValue s ( security-unix-may-send s newsk othersk)
in (s,retval)

```

29.16.3 kernel action of security_{socketcreatesecuritysocketpostcreate}

definition *sock-alloc* :: 'a ⇒ socket option

where *sock-alloc* s ≡ Some(SOME x:: socket. True)

definition *sock-create-lite* :: 'a \Rightarrow process-id \Rightarrow Sk-Family \Rightarrow int \Rightarrow int \Rightarrow socket \Rightarrow 'a \times int

where *sock-create-lite* s pid family type protocol' res \equiv

```

    let
      retval = resultValue s ( security-socket-create s family type protocol' 1)
    in if retval  $\neq$  0 then (s,retval)
      else
        let
          sock = sock-alloc s
        in
          if sock = None then (s,-ENOMEM)
          else
            let
              sock = the sock;
              etval = resultValue s ( security-socket-post-create s sock family
type protocol' 1);
              s' = funcState s ( security-socket-post-create s sock family type
protocol' 1)
            in
              (s',retval)

```

definition *sock-create'* :: 'a \Rightarrow process-id \Rightarrow net \Rightarrow Sk-Family \Rightarrow int \Rightarrow int \Rightarrow socket \Rightarrow int \Rightarrow 'a \times int

where *sock-create'* s pid net' family type protocol' kern \equiv

```

    let
      retval = resultValue s ( security-socket-create s family type protocol' kern)
    in
      if retval  $\neq$  0 then
        (s,retval)
      else
        let
          sock = sock-alloc s in
          if sock = None then (s,-ENFILE)
          else
            let
              sock = the sock;
              retval = resultValue s ( security-socket-post-create s sock
family type protocol' 1);
              s' = funcState s ( security-socket-post-create s sock family
type protocol' 1)
            in
              (s',retval)

```

29.16.4 kernel action of security_{socket}socketpair

definition *sys-socketpair'* :: 'a \Rightarrow process-id \Rightarrow int \Rightarrow int \Rightarrow int \Rightarrow int \Rightarrow 'a \times int

where $\text{sys-socketpair}' s \text{ pid family type protocol}' \text{ usockvec} \equiv$
 let
 $\text{sock1} = \text{SOME } x :: \text{socket} . \text{True};$
 $\text{sock2} = \text{SOME } x :: \text{socket} . \text{True};$
 $\text{retval} = \text{resultValue } s \text{ (security-socket-socketpair } s \text{ sock1 sock2)};$
 $s' = \text{funcState } s \text{ (security-socket-socketpair } s \text{ sock1 sock2)}$
 in
 (s', retval)

29.16.5 kernel action of security_{socket_{bind}}

definition $\text{sys-bind}' :: 'a \Rightarrow \text{process-id} \Rightarrow \text{int} \Rightarrow \text{sockaddr} \Rightarrow \text{int} \Rightarrow 'a \times \text{int}$
where $\text{sys-bind}' s \text{ pid fd umyaddr addrlen} \equiv$
 let
 $\text{sock} = \text{SOME } x :: \text{socket} . \text{True};$
 $\text{address} = \text{SOME } x :: \text{sockaddr} . \text{True};$
 $\text{retval} = \text{resultValue } s \text{ (security-socket-bind } s \text{ sock address}$
 $\text{addrlen})$
 in
 (s, retval)

29.16.6 kernel action of security_{socket_{connect}}

definition $\text{sys-connect}' :: 'a \Rightarrow \text{process-id} \Rightarrow \text{int} \Rightarrow \text{sockaddr} \Rightarrow \text{int} \Rightarrow 'a \times \text{int}$
where $\text{sys-connect}' s \text{ pid fd uservaddr addrlen} \equiv$
 let
 $\text{sock} = \text{SOME } x :: \text{socket} . \text{True};$
 $\text{address} = \text{SOME } x :: \text{sockaddr} . \text{True};$
 $\text{retval} = \text{resultValue } s \text{ (security-socket-connect } s \text{ sock address}$
 $\text{addrlen})$
 in
 (s, retval)

29.16.7 kernel action of security_{socket_{listen}}

definition $\text{sys-listen}' :: 'a \Rightarrow \text{process-id} \Rightarrow \text{int} \Rightarrow \text{int} \Rightarrow 'a \times \text{int}$
where $\text{sys-listen}' s \text{ pid fd backlog} \equiv$
 let
 $\text{sock} = \text{SOME } x :: \text{socket} . \text{True};$
 $\text{retval} = \text{resultValue } s \text{ (security-socket-listen } s \text{ sock backlog)}$
 in
 (s, retval)

29.16.8 kernel action of security_{socket_{accept}}

definition $\text{sys-accept4}' :: 'a \Rightarrow \text{process-id} \Rightarrow \text{int} \Rightarrow \text{sockaddr} \Rightarrow \text{int} \Rightarrow \text{int} \Rightarrow 'a \times \text{int}$
where $\text{sys-accept4}' s \text{ pid fd upeer-sockaddr upeer-addrlen flags}' \equiv$
 let
 $\text{sock} = \text{SOME } x :: \text{socket} . \text{True};$

```

newsock = SOME x:: socket . True;
newsock = newsock (|skt-type := skt-type sock |);
retval = resultValue s ( security-socket-accept s sock newsock)
in
(s,retval)

```

29.16.9 kernel action of security_{socket}sendmsg

definition *iov-iter-count* :: *iov-iter* \Rightarrow *nat*
where *iov-iter-count* *i* \equiv *iov-count* *i*

definition *msg-data-left* :: *msghdr* \Rightarrow *nat*
where *msg-data-left* *msg* \equiv *iov-iter-count* (*msg-iter* *msg*)

definition *sock-sendmsg* :: '*a* \Rightarrow *process-id* \Rightarrow *socket* \Rightarrow *msghdr* \Rightarrow '*a* \times *int*
where *sock-sendmsg* *s* *pid* *sock* *msg* \equiv
let
sock = SOME x:: socket . True;
l = msg-data-left *msg*;
retval = resultValue s (security-socket-sendmsg s sock *msg* l)
in
(s,retval)

29.16.10 kernel action of security_{socket}recvmsg

definition *sock-recvmsg* :: '*a* \Rightarrow *process-id* \Rightarrow *socket* \Rightarrow *msghdr* \Rightarrow *int* \Rightarrow '*a* \times *int*
where *sock-recvmsg* *s* *pid* *sock* *msg* *flags'* \equiv
let
sock = SOME x:: socket . True;
l = msg-data-left *msg*;
retval = resultValue s (security-socket-recvmsg s sock *msg* l
flags')
in
(s,retval)

29.16.11 kernel action of security_{socket}getsockname

definition *sys-getsockname* :: '*a* \Rightarrow *process-id* \Rightarrow *int* \Rightarrow *sockaddr* \Rightarrow *int* \Rightarrow '*a* \times *int*
where *sys-getsockname* *s* *pid* *fd* *usockaddr* *usockaddr-len* \equiv
let
sock = SOME x:: socket . True;
retval = resultValue s (security-socket-getsockname s sock)
in
(s,retval)

29.16.12 kernel action of security_{socket}getpeername

definition *sys-getpeername* :: '*a* \Rightarrow *process-id* \Rightarrow *int* \Rightarrow *sockaddr* \Rightarrow *int* \Rightarrow '*a* \times *int*
where *sys-getpeername* *s* *pid* *fd* *usockaddr* *usockaddr-len* \equiv

```

let
  sock = SOME x:: socket . True;
  retval = resultValue s ( security-socket-getpeername s sock )
in
  (s,retval)

```

29.16.13 kernel action of security_{socket}getsockopt

definition *compat-sys-getsockopt'* :: 'a ⇒ process-id ⇒ int ⇒ int ⇒ int ⇒ string ⇒ int ⇒ 'a × int

```

where compat-sys-getsockopt' s pid fd level' optname optval optlen ≡
  let
    sock = SOME x:: socket . True;
    retval = resultValue s ( security-socket-getsockopt s sock level' optname)
  in
    (s,retval)

```

definition *sys-getsockopt'* :: 'a ⇒ process-id ⇒ int ⇒ int ⇒ int ⇒ string ⇒ int ⇒ 'a × int

```

where sys-getsockopt' s pid fd level' optname optval optlen ≡
  let
    sock = SOME x:: socket . True;
    retval = resultValue s ( security-socket-getsockopt s sock level' optname)
  in
    (s,retval)

```

29.16.14 kernel action of security_{socket}setsockopt

definition *compat-sys-setsockopt'* :: 'a ⇒ process-id ⇒ int ⇒ int ⇒ int ⇒ string ⇒ int ⇒ 'a × int

```

where compat-sys-setsockopt' s pid fd level' optname optval optlen ≡
  let
    sock = SOME x:: socket . True;
    retval = resultValue s ( security-socket-setsockopt s sock level' optname)
  in
    (s,retval)

```

definition *sys-setsockopt'* :: 'a ⇒ process-id ⇒ int ⇒ int ⇒ int ⇒ string ⇒ int ⇒ 'a × int

```

where sys-setsockopt' s pid fd level' optname optval optlen ≡
  let
    sock = SOME x:: socket . True;
    retval = resultValue s ( security-socket-setsockopt s sock level' optname)
  in
    (s,retval)

```

29.16.15 kernel action of security_{socket}shutdown

definition *sys-shutdown'* :: 'a ⇒ process-id ⇒ int ⇒ int ⇒ 'a × int

```

where sys-shutdown' s pid fd how ≡

```



```

let
  sock = SOME x:: socket . True;
  retval = resultValue s ( security-socket-shutdown s sock how)
in
  (s,retval)

```

29.16.16 kernel action of security_{sock_rcv_sskb}

definition *sk-filter-trim-cap* :: 'a ⇒ process-id ⇒ sock ⇒ sk-buff ⇒ int ⇒ 'a × int
where *sk-filter-trim-cap s pid sk' skb cap* ≡
 let
 retval = resultValue s (security-sock-rcv-skb s sk' skb)
in
 (s,retval)

29.16.17 kernel action of security_{socket_{getpeersec_sstream}}

definition *sock-getsockopt* :: 'a ⇒ process-id ⇒ socket ⇒ int ⇒ int ⇒ string ⇒ int ⇒ 'a × int
where *sock-getsockopt s pid sock level' optname optval optlen* ≡
 if optname = SO-PEERSEC then
 let
 sock = SOME x:: socket . True;
 len = SOME x:: int . True;
 retval = resultValue s (security-socket-getpeersec-stream s sock optval
 optlen len)
in
 (s,retval)
else (s,0)

29.16.18 kernel action of security_{socket_{getpeersec_{dgram}}}

definition *unix-get-peersec-dgram* :: 'a ⇒ process-id ⇒ socket ⇒ scm-cookie ⇒ 'a × unit
where *unix-get-peersec-dgram s pid sock scm* ≡
 let
 sock = SOME x:: socket . True;
 secid = scm-secid scm;
 skb = None;
 retval = resultValue s (security-socket-getpeersec-dgram s sock
 skb secid)
in
 (s,())

definition *ip-cmsg-recv-security* :: 'a ⇒ process-id ⇒ msghdr ⇒ sk-buff ⇒ 'a × unit
where *ip-cmsg-recv-security s pid msg skb* ≡
 let
 sock = SOME x:: socket . True;
 secid = SOME x:: u32 . True;

```

      skb = Some skb;
      retval = resultValue s ( security-socket-getpeersec-dgram s sock
skb secid)
      in if retval ≠ 0 then
        (s,())
      else
        let
          secdata = SOME x:: string . True;
          seclen = SOME x:: u32. True;
          retval = resultValue s ( security-secid-to-secctx s secid
secdata seclen)
          in if retval ≠ 0 then
            (s,())
          else let s' = funcState s ( security-release-secctx s secdata
seclen)
              in (s',())

```

29.16.19 kernel action of security_sk_alloc

definition *sk-prot-alloc* :: 'a ⇒ process-id ⇒ proto ⇒ gfp-t ⇒ int ⇒ 'a × sock option

```

  where sk-prot-alloc s pid prot priority family ≡
    let
      sk' = SOME x:: sock option . True in
      if sk' ≠ None then
        let
          retval = resultValue s ( security-sk-alloc s (the sk') family
priority);
          s' = funcState s ( security-sk-alloc s (the sk') family priority)
          in
            (s', sk')
          else (s, None)

```

29.16.20 kernel action of security_sk_free

definition *sk-prot-free* :: 'a ⇒ process-id ⇒ proto ⇒ sock ⇒ 'a × unit

```

  where sk-prot-free s pid prot sk' ≡
    let
      retval = resultValue s ( security-sk-free s sk');
      s' = funcState s ( security-sk-free s sk')
    in
      (s', retval)

```

29.16.21 kernel action of security_sk_clone

definition *sk-clone* :: 'a ⇒ process-id ⇒ sock ⇒ sock ⇒ 'a × unit

```

  where sk-clone s pid sk' newsk ≡
    let
      retval = resultValue s ( security-sk-clone s sk' newsk);

```

$s' = \text{funcState } s \text{ (security-sk-clone } s \text{ sk' newsk)}$
in
 (s', retval)

29.16.22 kernel action of security_{sk}classify_flow

definition $\text{sk-classify-flow} :: 'a \Rightarrow \text{process-id} \Rightarrow \text{sock} \Rightarrow \text{flowi} \Rightarrow 'a \times \text{unit}$
where $\text{sk-classify-flow } s \text{ pid } sk' \text{ fl} \equiv$
let
 $\text{retval} = \text{resultValue } s \text{ (security-sk-classify-flow } s \text{ sk' fl)}$;
 $s' = \text{funcState } s \text{ (security-sk-classify-flow } s \text{ sk' fl)}$
in
 (s', retval)

29.16.23 kernel action of security_{req}classify_flow

definition $\text{req-classify-flow} :: 'a \Rightarrow \text{process-id} \Rightarrow \text{request-sock} \Rightarrow \text{flowi} \Rightarrow 'a \times \text{unit}$
where $\text{req-classify-flow } s \text{ pid } sk' \text{ fl} \equiv$
let
 $\text{retval} = \text{resultValue } s \text{ (security-req-classify-flow } s \text{ sk' fl)}$;
 $s' = \text{funcState } s \text{ (security-req-classify-flow } s \text{ sk' fl)}$
in
 (s', retval)

29.16.24 kernel action of security_{sock}graft

definition $\text{af-alg-accept} :: 'a \Rightarrow \text{process-id} \Rightarrow \text{sock} \Rightarrow \text{socket} \Rightarrow \text{bool} \Rightarrow 'a \times \text{unit}$
where $\text{af-alg-accept } s \text{ pid } sk' \text{ newsock } \text{kern} \equiv$
let
 $sk2 = \text{SOME } x :: \text{sock} . \text{True}$;
 $\text{retval} = \text{resultValue } s \text{ (security-sock-graft } s \text{ sk2 newsock)}$;
 $s' = \text{funcState } s \text{ (security-sock-graft } s \text{ sk2 newsock)}$
in
 (s', retval)

definition $\text{sock-graft} :: 'a \Rightarrow \text{process-id} \Rightarrow \text{sock} \Rightarrow \text{socket} \Rightarrow 'a \times \text{unit}$

where $\text{sock-graft } s \text{ pid } sk' \text{ parent'} \equiv$
let
 $\text{retval} = \text{resultValue } s \text{ (security-sock-graft } s \text{ sk' parent')}$;
 $s' = \text{funcState } s \text{ (security-sock-graft } s \text{ sk' parent')}$
in
 (s', retval)

29.16.25 kernel action of security_{inet}conn_request

definition $\text{inet-conn-request} :: 'a \Rightarrow \text{process-id} \Rightarrow \text{sock} \Rightarrow \text{sk-buff} \Rightarrow \text{request-sock} \Rightarrow 'a \times \text{int}$
where $\text{inet-conn-request } s \text{ pid } sk' \text{ skb } \text{req} \equiv$
let
 $\text{retval} = \text{resultValue } s \text{ (security-inet-conn-request } s \text{ sk' skb req)}$;

$s' = \text{funcState } s \text{ (security-inet-conn-request } s \text{ sk' skb req)}$
in
 (s', retval)

29.16.26 kernel action of security_{inet_csk_clone}

definition *inet-csk-clone-lock* :: 'a \Rightarrow process-id \Rightarrow sock \Rightarrow request-sock \Rightarrow gfp-t \Rightarrow 'a \times sock option

where *inet-csk-clone-lock* *s* *pid* *sk'* *req* *priority* \equiv
let
newsk = SOME *x*::sock option. True
in if *newsk* \neq None then
let
newsk = the *newsk*;
retval = resultValue *s* (security-inet-csk-clone *s* *newsk* *req*);
s' = funcState *s* (security-inet-csk-clone *s* *newsk* *req*)
in
(*s'*,Some *newsk*)
else (*s*,None)

29.16.27 kernel action of security_{inet_conn_established}

definition *tcp-finish-connect* :: 'a \Rightarrow process-id \Rightarrow sock \Rightarrow sk-buff \Rightarrow 'a \times unit

where *tcp-finish-connect* *s* *pid* *sk'* *skb* \equiv
let
retval = resultValue *s* (security-inet-conn-established *s* *sk'* *skb*);
s' = funcState *s* (security-inet-conn-established *s* *sk'* *skb*)
in
(*s'*, *retval*)

definition *sctp-sf-do-5-1E-ca* :: 'a \Rightarrow process-id \Rightarrow sctp-endpoint \Rightarrow 'a \times unit

where *sctp-sf-do-5-1E-ca* *s* *pid* *ep* \equiv
let
chunk = SOME *x*:: sctp-chunk .True;
skb = sctp-skb *chunk*;
sk' = sctp-ep-sk(sctp-base *ep*);
retval = resultValue *s* (security-inet-conn-established *s* *sk'* *skb*);
s' = funcState *s* (security-inet-conn-established *s* *sk'* *skb*)
in
(*s'*, *retval*)

29.16.28 kernel action of security_{secmark_rlabel_packetsecurity_secmark_refcount_inc}

definition *checkentry-lsm* :: 'a \Rightarrow process-id \Rightarrow xt-secmark-target-info \Rightarrow 'a \times int

where *checkentry-lsm* *s* *pid* *info* \equiv
let
secid' = xt-secid *info*;
secctx = xt-secctx *info*;
err = resultValue *s* (security-secctx-to-secid *s* *secctx* 256 *secid'*)

```

    in if err  $\neq$  0 then (s,err)
  else let
    retval = resultValue s ( security-secmark-relabel-packet s secid');
    s' = funcState s ( security-secmark-relabel-packet s secid' );
    in if retval  $\neq$  0 then (s',retval)
  else
    let s'' = funcState s ( security-secmark-refcount-inc s )
    in (s'',0)

```

29.16.29 kernel action of security_{secmark_refcount_dec}

term (int(of-char xt-mode))

definition secmark-tg-destroy :: 'a \Rightarrow process-id \Rightarrow 'a \times unit

where secmark-tg-destroy s pid \equiv
 if (int(of-char xt-mode)) = SECMARK-MODE-SEL then
 let
 s' = funcState s (security-secmark-refcount-dec s)
 in
 (s', ())
 else
 (s,())

29.17 key

29.17.1 kernel action of security_{key_alloc}

definition key-alloc :: 'a \Rightarrow process-id \Rightarrow key-type \Rightarrow string \Rightarrow kuid-t \Rightarrow kgid-t
 \Rightarrow Cred \Rightarrow nat \Rightarrow 'a \times key option

where key-alloc s pid ktype desc uid' gid' cred' flags' \equiv
 let
 key = SOME x::key. True;
 retval = resultValue s (security-key-alloc s key cred' flags');
 s' = funcState s (security-key-alloc s key cred' flags')
 in if retval < 0 then
 (s,None)
 else
 (s', Some key)

29.17.2 kernel action of security_{key_free}

definition key-free :: 'a \Rightarrow process-id \Rightarrow key \Rightarrow 'a \times unit

where key-free s pid key' \equiv
 let
 retval = resultValue s (security-key-free s key');
 s' = funcState s (security-key-free s key')
 in
 (s',retval)

29.17.3 kernel action of security_{keypermission}

definition *key-task-permission* :: 'a \Rightarrow process-id \Rightarrow key-ref-t \Rightarrow Cred \Rightarrow nat \Rightarrow 'a \times int

where *key-task-permission* s pid key-ref cred' perm \equiv
 let
 retval = resultValue s (security-key-permission s key-ref cred'
 perm)
 in
 (s,retval)

29.17.4 kernel action of security_{keygetsecurity}

definition *key-ref-to-ptr* :: 'a \Rightarrow key-ref-t \Rightarrow key option

where *key-ref-to-ptr* s key-ref \equiv ((keys s) key-ref)

definition *keyctl-get-security* :: 'a \Rightarrow process-id \Rightarrow key-serial-t \Rightarrow string \Rightarrow int \Rightarrow 'a \times int

where *keyctl-get-security* s pid keyid' buffer buflen \equiv
 let
 key-ref = keyid';
 key = the(key-ref-to-ptr s key-ref);
 context = ""';
 retval = resultValue s (security-key-getsecurity s key context)
 in
 (s,retval)

29.18 audit

29.18.1 kernel action of security_{audit_rule_init}

definition *audit-data-to-entry* :: 'a \Rightarrow process-id \Rightarrow 'a \times int

where *audit-data-to-entry* s pid \equiv
 let
 f = SOME x:: audit-field. True;
 ftype = atype f;
 fop = aop f;
 rule = lsm-rule f;
 str = SOME x:: string. True;
 retval = resultValue s (security-audit-rule-init s ftype fop str
 rule)
 in
 (s,retval)

definition *audit-dupe-lsm-field* :: 'a \Rightarrow process-id \Rightarrow audit-field \Rightarrow audit-field \Rightarrow 'a \times int

where *audit-dupe-lsm-field* s pid df sf \equiv
 let
 df = df(lsm-str := lsm-str sf);
 ftype = atype df;

```

      fop = aop df;
      rule = lsm-rule df;
      str = lsm-str sf;
      retval = resultValue s (security-audit-rule-init s ftype fop str
rule)
    in if retval = (-EINVAL) then (s,0)
      else
        (s,retval)

```

29.18.2 kernel action of security_{audit}rule_{known}

definition *update-lsm-rule* :: 'a \Rightarrow process-id \Rightarrow audit-krule \Rightarrow 'a \times int
where *update-lsm-rule* s pid r \equiv
 let
 retval = resultValue s (security-audit-rule-known s r)
 in
 (s,retval)

29.18.3 kernel action of security_{audit}rule_{free}

definition *audit-free-lsm-field* :: 'a \Rightarrow process-id \Rightarrow audit-field \Rightarrow 'a \times unit
where *audit-free-lsm-field* s pid f \equiv
 if (atype f) = AUDIT-OBJ-LEV-HIGH then
 let
 retval = resultValue s (security-audit-rule-free s (lsm-rule f))
 in
 (s,retval)
 else (s,())

29.18.4 kernel action of security_{audit}rule_{match}

definition *audit-rule-match* :: 'a \Rightarrow process-id \Rightarrow int \Rightarrow 'a \times int
where *audit-rule-match* s pid sid \equiv
 let
 f = SOME x:: audit-field. True;
 ftype = atype f;
 fop = aop f;
 rule = lsm-rule f;
 ac = SOME x:: audit-context. True;
 sid = nat sid;
 retval = resultValue s (security-audit-rule-match s sid ftype fop
rule ac)
 in
 (s,retval)

29.19 bpf

29.19.1 kernel action of security_{bpf}

definition *syscall-bpf* :: 'a \Rightarrow process-id \Rightarrow int \Rightarrow nat \Rightarrow 'a \times int

where *syscall-bpf s pid cmd size'* \equiv
 let
 attr = *SOME x:: bpf-attr . True*;

 retval = *resultValue s (security-bpf s cmd attr size')*
 in if *retval < 0* *then*
 (*s,retval*)
 else
 (*s,0*)

29.19.2 kernel action of security_{bpf_map}

definition *bpf-map-new-fd :: 'a \Rightarrow process-id \Rightarrow bpf-map \Rightarrow int \Rightarrow 'a \times int*
where *bpf-map-new-fd s pid map' flags'* \equiv
 let
 attr = *SOME x:: bpf-attr . True*;
 flag = *OPEN-FMODE flags'*;
 retval = *resultValue s (security-bpf-map s map' flag)*
 in if *retval < 0* *then*
 (*s,retval*)
 else
 (*s,0*)

29.19.3 kernel action of security_{bpf_prog}

definition *get-prog-inode :: 'a \Rightarrow process-id \Rightarrow bpf-map \Rightarrow int \Rightarrow 'a \times bpf-prog option*
where *get-prog-inode s pid map' flags'* \equiv
 let
 prog = *SOME x:: bpf-prog . True*;
 retval = *resultValue s (security-bpf-prog s prog)*
 in if *retval < 0* *then*
 (*s,None*)
 else
 (*s,Some prog*)

definition *bpf-prog-new-fd :: 'a \Rightarrow process-id \Rightarrow bpf-prog \Rightarrow 'a \times int*
where *bpf-prog-new-fd s pid prog* \equiv
 let
 retval = *resultValue s (security-bpf-prog s prog)*
 in if *retval < 0* *then*
 (*s,retval*)
 else
 (*s,0*)

29.19.4 kernel action of security_{bpf_map_{alloc}}

definition *map-create :: 'a \Rightarrow process-id \Rightarrow bpf-attr \Rightarrow 'a \times int*
where *map-create s pid attr'* \equiv
 let


```

    map= SOME x:: bpf-map . True;
    retval = resultValue s (security-bpf-map-alloc s map);
    s' = funcState s (security-bpf-map-alloc s map)
in  if retval < 0 then
    (s,retval)
  else
    (s',0)

```

29.19.5 kernel action of security_{bpf_{prog_aalloc}}

definition *bpf-prog-load* :: 'a \Rightarrow process-id \Rightarrow bpf-attr \Rightarrow 'a \times int
where *bpf-prog-load* s pid attr' \equiv
 let
 prog= SOME x:: bpf-prog . True;
 aux' = aux prog;
 retval = resultValue s (security-bpf-prog-alloc s aux');
 s' = funcState s (security-bpf-prog-alloc s aux')
in if retval < 0 then
 (s,retval)
 else
 (s',0)

29.19.6 kernel action of security_{bpf_{map_{free}}}

definition *container-of-map* :: work-struct \Rightarrow bpf-map
where *container-of-map* work' \equiv SOME x . work x = work'
definition *bpf-map-free-deferred* :: 'a \Rightarrow process-id \Rightarrow work-struct \Rightarrow 'a \times unit
where *bpf-map-free-deferred* s pid work' \equiv
 let
 map= container-of-map work';
 s' = funcState s (security-bpf-map-free s map)
in
 (s',())

29.19.7 kernel action of security_{bpf_{prog_{free}}}

definition *container-of-progfree* :: rcu-head \Rightarrow bpf-prog-aux
where *container-of-progfree* rcu' \equiv SOME x . rcu x = rcu'
definition *bpf-prog-put-rcu* :: 'a \Rightarrow process-id \Rightarrow rcu-head \Rightarrow 'a \times unit
where *bpf-prog-put-rcu* s pid work' \equiv
 let
 aux = container-of-progfree work';
 s' = funcState s (security-bpf-prog-free s aux)
in
 (s',())

29.20 event pid

definition *getpid-from-sb-event* :: *Event-sb* \Rightarrow *process-id*

where *getpid-from-sb-event* *evt* \equiv (case *evt* of
 Event-sb-copy-data *pid sb* \Rightarrow *pid*
 | *Event-sb-remount* *pid p v* \Rightarrow *pid*
 | *Event-sb-kern-mount* *pid f t name data* \Rightarrow *pid*
 | *Event-sb-show-options* *pid sq sb* \Rightarrow *pid*
 | *Event-sb-statfs* *pid d* \Rightarrow *pid*
 | *Event-sb-mount* *pid devname dirname t f p* \Rightarrow *pid*
 | *Event-sb-umount* *pid m i* \Rightarrow *pid*
 | *Event-sb-pivotroot* *pid* \Rightarrow *pid*
 | *Event-set-mnt-opts* *pid n sb opt* \Rightarrow *pid*
 | *Event-set-sb-security* *pid sb d info* \Rightarrow *pid*
 | *Event-sb-clone-mnt-opts* *pid sb d minfo* \Rightarrow *pid*
 | *Event-sb-parse-opts-str* *pid string opts* \Rightarrow *pid*
)

definition *getpid-from-tsk-event* :: *Event-tsk* \Rightarrow *process-id*

where *getpid-from-tsk-event* *e* \equiv (case *e* of
 (*Event-prepare-creds* *process-id*) \Rightarrow *process-id*
 | (*Event-sys-setreuid* *process-id uid' euid'*) \Rightarrow *process-id*
 | (*Event-setpgid* *process-id i pgid*) \Rightarrow *process-id*
 | (*Event-do-getpgid* *process-id pgid*) \Rightarrow *process-id*
 | (*Event-getsid* *process-id sid*) \Rightarrow *process-id*
 | (*Event-getsecid* *process-id p u*) \Rightarrow *process-id*
 | (*Event-task-setnice* *process-id p nice*) \Rightarrow *process-id*
 | (*Event-set-task-ioprio* *process-id p ioprio*) \Rightarrow *process-id*
 | (*Event-get-task-ioprio* *process-id p*) \Rightarrow *process-id*
 | (*Event-check-prlimit-permission* *process-id p i*) \Rightarrow
 process-id
 | (*Event-do-prlimit* *process-id p i*) \Rightarrow *process-id*
 | (*Event-task-setscheduler* *process-id p*) \Rightarrow *process-id*
 | (*Event-task-getscheduler* *process-id p*) \Rightarrow *process-id*
 | (*Event-task-movememory* *process-id p*) \Rightarrow *process-id*
 | (*Event-task-kill* *process-id p siginfo i c*) \Rightarrow *process-id*
 | (*Event-task-prctl* *process-id op arg2 arg3 arg4 arg5*) \Rightarrow
 process-id
)

definition *getpid-from-pttrace-event* :: *Event-Ptrace* \Rightarrow *process-id*

where *getpid-from-pttrace-event* *e* \equiv (case *e* of
 Event-pttrace-access-check *process-id Task m*
 \Rightarrow *process-id*
 | *Event-pttrace-traceme* *process-id* \Rightarrow *process-id*)

definition *getpid-from-sys-event* :: *Event-sys* \Rightarrow *process-id*

where *getpid-from-sys-event* *e* \equiv (case *e* of
 Event-smack-syslog *process-id t* \Rightarrow *process-id* |
 Event-prepare-binprm *process-id bprm* \Rightarrow *process-id*)

definition *getpid-from-kern-ipc-event* :: *Event-ipc* \Rightarrow *process-id*
where *getpid-from-kern-ipc-event* *e* \equiv (case *e* of
 (*Event-ipc-permission* *process-id* *kern-ipc-perm* *flg*) \Rightarrow *process-id*
 | (*Event-ipc-getsecid* *process-id* *kern-ipc-perm*) \Rightarrow *process-id*
 | (*Event-msg-queue-associate* *process-id* *kern-ipc-perm* *flg*)
 \Rightarrow *process-id*
 | (*Event-msg-queue-msgctl* *process-id* *kern-ipc-perm* *flg*) \Rightarrow *process-id*
 | (*Event-msg-queue-msgsnd* *process-id* *kern-ipc-perm* *msg-msg* *flg*)
 \Rightarrow *process-id*
 | (*Event-msg-queue-msgrcv* *process-id* *kern-ipc-perm* *msg-msg* *p*
long *msgflg*) \Rightarrow *process-id*
 | (*Event-shm-associate* *process-id* *kern-ipc-perm* *flg*) \Rightarrow *process-id*
 | (*Event-shm-shmctl* *process-id* *kern-ipc-perm* *flg*) \Rightarrow *process-id*
 | (*Event-shm-shmat* *process-id* *kern-ipc-perm* *string* *flg*) \Rightarrow *process-id*

 | (*Event-sem-associate* *process-id* *kern-ipc-perm* *flg*) \Rightarrow *process-id*
 | (*Event-sem-semctl* *process-id* *kern-ipc-perm* *flg*) \Rightarrow *process-id*
 | (*Event-sem-semop* *process-id* *kern-ipc-perm* *sembuf* *nsops* *alter*)
 \Rightarrow *process-id*
)

definition *getpid-from-file-event* :: *Event-file* \Rightarrow *process-id*
where *getpid-from-file-event* *e* = (case *e* of
 Event-do-ioctl *process-id* *Files* *IOC-DIR* *arg* \Rightarrow
process-id
 | *Event-syscall-ioctl* *process-id* *fd* *IOC-DIR* *arg* \Rightarrow
process-id
 | *Event-ksys-ioctl* *process-id* *fd* *IOC-DIR* *arg* \Rightarrow
process-id
 | *Event-vm-mmap-pgoff* *process-id* *file* *addr* *len'* *prot*
flag *pgoff* \Rightarrow *process-id*
 | *Event-do-sys-vm86* *process-id* \Rightarrow *process-id*
 | *Event-get-unmapped-area* *process-id* *Files* *addr* \Rightarrow
process-id
 | *Event-validate-mmap-request* *process-id* *Files* *addr* \Rightarrow
process-id
 | *Event-generic-setlease* *process-id* *Files* *arg* \Rightarrow
process-id
 | *Event-syscall-lock* *process-id* *fd* *cmd* \Rightarrow *process-id*
 | *Event-do-lock-file-wait* *process-id* *Files* *cmd* *file-lock*
 \Rightarrow *process-id*
 | *Event-file-fcntl* *process-id* *Files* *cmd* *arg* \Rightarrow *process-id*
 | *Event-file-send-sigiotask* *process-id* *Task* *fown-struct*
sig \Rightarrow *process-id*
 | *Event-file-receive* *process-id* *Files* \Rightarrow *process-id*
 | *Event-do-dentry-open* *process-id* *Files* \Rightarrow *process-id*)

definition *getpid-from-key-evevt* :: *Event-Key* \Rightarrow *process-id*

where *getpid-from-key-evevt* *e* = (case *e* of
 Event-key-permission *process-id* *key-ref-t* *Cred* *prem* \Rightarrow *process-id*
 | *Event-key-getsecurity* *process-id* *key-serial-t* *buffer* *buflen* \Rightarrow *process-id*)

definition *getpid-from-aduit-evevt* :: *Event-audit* \Rightarrow *process-id*

where *getpid-from-aduit-evevt* *e* = (case *e* of
 Event-audit-data-to-entry *process-id* \Rightarrow *process-id*
 | *Event-audit-dupe-lsm-field* *process-id* *df* *sf* \Rightarrow *process-id*
 | *Event-audit-rule-known* *process-id* *krule* \Rightarrow *process-id*
 | *Event-audit-rule-match* *process-id* *sid* \Rightarrow *process-id*
 | *Event-audit-rule-free* *process-id* *field* \Rightarrow *process-id*)

definition *getpid-from-socket-evevt* :: *Event-network-sock* \Rightarrow *process-id*

where *getpid-from-socket-evevt* *e* = (case *e* of
 Event-unix-stream-connect *process-id* *sock* *uaddr* *addr-len* *flags'* \Rightarrow
process-id
 | *Event-unix-dgram-connect* *process-id* *sock* *uaddr* *alen* *flags'* \Rightarrow *process-id*

 | *Event-unix-dgram-sendmsg* *process-id* *sock* *uaddr* *alen* \Rightarrow *process-id*

 | *Event-sys-bind'* *process-id* *fd* *umyaddr* *addrlen* \Rightarrow *process-id*
 | *Event-sys-connect'* *process-id* *fd* *uservaddr* *addrlen* \Rightarrow *process-id*
 | *Event-sock-sendmsg* *process-id* *sock* *msg* \Rightarrow *process-id*
 | *Event-sock-recvmmsg* *process-id* *sock* *msg* *flags'* \Rightarrow *process-id*
 | *Event-sk-filter-trim-cap* *process-id* *sk'* *skb* *cap* \Rightarrow *process-id*
 | *Event-sock-getsockopt* *process-id* *sock* *level'* *optname* *optval* *optlen* \Rightarrow
process-id
 | *Event-unix-get-peersec-dgram* *process-id* *sock* *scm* \Rightarrow *process-id*
)

definition *getpid-from-inode-evevt* :: *Event-inode* \Rightarrow *process-id*

where *getpid-from-inode-evevt* *e* = (case *e* of
 Event-vfs-link *process-id* *old* *dir* *new* *delegated-inode* \Rightarrow *process-id*
 | *Event-vfs-unlink* *process-id* *dir* *dentry* *delegated-inode* \Rightarrow *process-id*
 | *Event-vfs-rmdir* *process-id* *inode* *dentry* \Rightarrow *process-id*
 | *Event-vfs-rename* *process-id* *old-dir* *old-dentry* *new-dir* *new-dentry* *delegated-inode*
flgs \Rightarrow *process-id*
 | *Event-inode-permission* *process-id* *inode* *mask'* \Rightarrow *process-id*
 | *Event-notify-change* *process-id* *dentry* *iattr* *inode* \Rightarrow *process-id*
 | *Event-fat-ioctl-set-attributes* *process-id* *Files* \Rightarrow *process-id*
 | *Event-vfs-getattr* *process-id* *path* \Rightarrow *process-id*
 | *Event-vfs-setxattr* *process-id* *dentry* *xattr* *string* *size'* *flgs* \Rightarrow *process-id*
 | *Event-vfs-getxattr* *process-id* *dentry* *xattr* *string* *size'* \Rightarrow *process-id*
 | *Event-vfs-removexattr* *process-id* *dentry* *xattr* \Rightarrow *process-id*
 | *Event-xattr-getsecurity* *process-id* *inode* *name* *value* *size'* \Rightarrow *process-id*)

```

| Event-nfs4-listxattr-nfs4-label process-id inode string size'  $\Rightarrow$  process-id
| Event-sockfs-listxattr process-id dentry string size'  $\Rightarrow$  process-id
)

```

definition *getpid-from-istpro-evevt* :: *Event-d-instantiate-procattr* \Rightarrow *process-id*
where *getpid-from-istpro-evevt* *e* = (case *e* of
 | *Event-d-instantiate* *pid* *entry* *inode* \Rightarrow *pid*
 | *Event-d-instantiate-new* *pid* *entry* *inode* \Rightarrow *pid*
 | *Event-d-instantiate-anon'* *pid* *entry* *inode* *disconnected* \Rightarrow *pid*
 | *Event-d-add* *pid* *entry* *inode* \Rightarrow *pid*
 | *Event-d-splice-alias* *pid* *inode* *dentry* \Rightarrow *pid*
 | *Event-nfs-get-root* *pid* *sb* *mntfh* *devname* \Rightarrow *pid*
 | *Event-proc-pid-attr-read* *pid* *file* *buf* *count'* *ppos* \Rightarrow *pid*
 | *Event-proc-pid-attr-write* *pid* *file* *buf* *count'* *ppos* \Rightarrow *pid*)

definition *getpid-from-other-evevt* :: *Event-others* \Rightarrow *process-id*
where *getpid-from-other-evevt* *e* = (case *e* of
 | *Evt-ismaclabel*(*Event-nfs4-xattr-set-nfs4-label* *pid* *key'* *inode* *buf*) \Rightarrow *pid*
 | *Evt-ismaclabel*(*Event-nfs4-xattr-get-nfs4-label* *pid* *key'* *inode* *buf*) \Rightarrow *pid*
 | *Evt-id2secctx*(*Event-scm-passec* *pid* *sock* *msg* *scm*) \Rightarrow *pid*
 | *Evt-id2secctx*(*Event-audit-receive-msg* *pid* *skb* *nlh*) \Rightarrow *pid*
 | *Evt-id2secctx*(*Event-audit-log-name* *pid* *n*) \Rightarrow *pid*
 | *Evt-id2secctx*(*Event-audit-log-task-context* *pid* *skb*) \Rightarrow *pid*
 | *Evt-id2secctx*(*Event-audit-log-pid-context* *pid* *sid*) \Rightarrow *pid*
 | *Evt-id2secctx*(*Event-show-special* *pid* *context*) \Rightarrow *pid*
 | *Evt-id2secctx*(*Event-ctnetlink-dump-secctx* *pid* *skb* *ct*) \Rightarrow *pid*
 | *Evt-id2secctx*(*Event-ctnetlink-secctx-size* *pid* *ct*) \Rightarrow *pid*
 | *Evt-id2secctx*(*Event-ct-show-secctx* *pid* *seqfile* *ct*) \Rightarrow *pid*
 | *Evt-id2secctx*(*Event-nfqnl-get-sk-secctx* *pid* *skb* *secdta*) \Rightarrow *pid*
 | *Evt-id2secctx*(*Event-netlbl-unlsh-func3* *pid* *secid'*) \Rightarrow *pid*
 | *Evt-id2secctx*(*Event-netlbl-unlabel-staticlist-gen* *pid* *secid'*) \Rightarrow *pid*
 | *Evt-id2secctx*(*Event-netlbl-audit-start-common* *pid* *type'* *audit-info*) \Rightarrow *pid*
 | *Evt-secctxtoid*(*Event-set-security-override-from-ctx* *pid* *new* *secctx*) \Rightarrow *pid*
 | *Evt-secctxtoid*(*Event-netlbl-unlabel-staticadd* *pid*) \Rightarrow *pid*
 | *Evt-inodesecctx*(*Event-kernfs-refresh-inode* *pid* *kn* *inode*) \Rightarrow *pid*
 | *Evt-inodesecctx*(*Event-nfs-setsecurity* *pid* *inode* *label'*) \Rightarrow *pid*
 | *Evt-inodesecctx*(*Event-nfsd4-security-inode-setsecctx* *pid* *resfh* *label'* *bmval*) \Rightarrow *pid*
 | *Evt-inodesecctx*(*Event-nfsd4-set-nfs4-label* *pid* *resfh* *label'*) \Rightarrow *pid*
 | *Evt-inodesecctx*(*Event-nfsd4-encode-fattr* *pid* *dentry'*) \Rightarrow *pid*
 | *Evt-inodesecctx*(*Event-ovl-get-tmpfile* *pid* *c*) \Rightarrow *pid*
 | *Evt-inodesecctx*(*Event-ovl-copy-xattr* *pid* *old* *new*) \Rightarrow *pid*
 | *Evt-inodesecctx*(*Event-ovl-create-or-link* *pid* *dentry* *inode* *attr'* *origin*) \Rightarrow *pid*)

datatype *Event* = *SbEvt* *Event-sb*
 | *TskEvt* *Event-tsk*
 | *PtraceEvt* *Event-Ptrace*

```

| SysEvt Event-sys
| FileEvt Event-file
| KIpcEvt Event-ipc
| KeyEvt Event-Key
| AuditEvt Event-audit
| SocketEvt Event-network-sock
| InodeEvt Event-inode

```

datatype *Event-manage-hooks* = *Event-alloc-file process-id Files Cred*
| *Event-file-free process-id Files*

definition *getpid-from-manage-hooks* :: *Event-manage-hooks* \Rightarrow *process-id option*
where *getpid-from-manage-hooks* *e* = (case *e* of
Event-alloc-file process-id Files Cred \Rightarrow *Some process-id*
| *Event-file-free process-id Files* \Rightarrow *Some process-id*
)

definition *exec-manage-event* :: '*a* \Rightarrow *Event-manage-hooks* \Rightarrow '*a*
where *exec-manage-event* *s e* = (case *e* of
Event-alloc-file pid file c \Rightarrow *fst(alloc-file s pid file c)* |
Event-file-free pid file \Rightarrow *fst(file-free s pid file)*)

29.21 Instantiation and Its Proofs of IFS Model

definition *exec-event* :: '*a* \Rightarrow *Event* \Rightarrow '*a*
where *exec-event* *s e* = (case *e* of
SbEvt (Event-sb-copy-data pid sb) \Rightarrow *fst(k-sb-copy-data s pid)* |
SbEvt (Event-sb-remount pid p v) \Rightarrow *fst(do-remount s p v)* |
SbEvt (Event-sb-kern-mount pid t f name data) \Rightarrow *fst(mount-fs s t f name data)* |
SbEvt (Event-sb-show-options pid sq sb) \Rightarrow *fst(show-sb-opts s pid sq sb)* |
SbEvt (Event-sb-statfs pid d) \Rightarrow *fst(statfs-by-dentry s pid d)* |
SbEvt (Event-sb-mount pid devname dirname t f p) \Rightarrow *fst(do-mount s pid devname dirname t f p)* |
SbEvt (Event-sb-umount pid m i) \Rightarrow *fst (do-umount s pid m i)* |
SbEvt (Event-sb-pivotroot pid) \Rightarrow *fst (pivot-root s pid)* |
SbEvt (Event-set-mnt-opts pid n sb opt) \Rightarrow *fst(setup-security-options s pid n sb opt)* |
SbEvt (Event-set-sb-security pid sb d info) \Rightarrow *fst(set-sb-security s pid sb d info)* |
SbEvt (Event-sb-clone-mnt-opts pid sb d minfo) \Rightarrow *fst(nfs-clone-sb-security s pid sb d minfo)* |
SbEvt (Event-sb-parse-opts-str pid str opts) \Rightarrow *fst(parse-security-options s pid str opts)* |

TskEvt ((Event-prepare-creds pid)) \Rightarrow *fst(prepare-creds s pid)* |
TskEvt ((Event-sys-setreuid pid kuid euid')) \Rightarrow *fst(sys-setreuid s pid kuid euid')* |

$TskEvt \ ((Event\text{-}setpgid \ pid \ i \ pgid)) \Rightarrow fst(setpgid \ s \ pid \ i \ pgid) \mid$
 $TskEvt \ ((Event\text{-}do\text{-}getpgid \ pid \ i)) \Rightarrow fst(do\text{-}getpgid \ s \ pid \ i) \mid$
 $TskEvt \ ((Event\text{-}getsid \ pid \ i)) \Rightarrow fst(getsid \ s \ pid \ i) \mid$
 $TskEvt \ ((Event\text{-}getsecid \ pid \ p \ u)) \Rightarrow fst(getsecid \ s \ pid \ p \ u) \mid$
 $TskEvt \ ((Event\text{-}task\text{-}setnice \ pid \ p \ i)) \Rightarrow fst(task\text{-}setnice \ s \ pid \ p \ i) \mid$
 $TskEvt \ ((Event\text{-}set\text{-}task\text{-}ioprio \ pid \ p \ i)) \Rightarrow fst(set\text{-}task\text{-}ioprio \ s \ pid \ p \ i) \mid$
 $TskEvt \ ((Event\text{-}get\text{-}task\text{-}ioprio \ pid \ p)) \Rightarrow fst(get\text{-}task\text{-}ioprio \ s \ pid \ p) \mid$
 $TskEvt \ ((Event\text{-}check\text{-}prlimit\text{-}permission \ pid \ p \ i)) \Rightarrow fst(check\text{-}prlimit\text{-}permission$
 $s \ pid \ p \ i) \mid$
 $TskEvt \ ((Event\text{-}do\text{-}prlimit \ pid \ p \ i)) \Rightarrow fst(do\text{-}prlimit \ s \ pid \ p \ i) \mid$
 $TskEvt \ ((Event\text{-}task\text{-}setscheduler \ pid \ p)) \Rightarrow fst(task\text{-}setscheduler \ s \ pid \ p) \mid$
 $TskEvt \ ((Event\text{-}task\text{-}getscheduler \ pid \ p)) \Rightarrow fst(task\text{-}getscheduler \ s \ pid \ p) \mid$
 $TskEvt \ ((Event\text{-}task\text{-}movememory \ pid \ p)) \Rightarrow fst(task\text{-}movememory \ s \ pid \ p) \mid$
 $TskEvt \ ((Event\text{-}task\text{-}kill \ pid \ p \ sinfo \ i \ c)) \Rightarrow fst(task\text{-}kill \ s \ pid \ p \ sinfo \ i \ c) \mid$
 $TskEvt \ ((Event\text{-}task\text{-}prctl \ pid \ op \ arg2 \ arg3 \ arg4 \ arg5))$
 $\Rightarrow fst(task\text{-}prctl \ s \ pid \ op \ arg2 \ arg3 \ arg4 \ arg5) \mid$

$SysEvt(\ Event\text{-}smack\text{-}syslog \ pid \ t) \Rightarrow fst(\ check\text{-}syslog\text{-}permissions \ s \ pid \ t) \mid$
 $SysEvt(\ Event\text{-}prepare\text{-}binprm \ pid \ bprm) \Rightarrow fst(prepare\text{-}binprm \ s \ pid \ bprm) \mid$
 $PtraceEvt(\ Event\text{-}ptrace\text{-}access\text{-}check \ pid \ p \ m) \Rightarrow fst(ptrace\text{-}may\text{-}access \ s \ pid$
 $p \ m) \mid$
 $PtraceEvt(\ Event\text{-}ptrace\text{-}traceme \ pid) \Rightarrow fst(ptrace\text{-}traceme \ s \ pid) \mid$

$FileEvt(\ Event\text{-}do\text{-}ioctl \ pid \ file \ cmd \ arg) \Rightarrow fst(do\text{-}ioctl \ s \ pid \ file \ cmd \ arg) \mid$
 $FileEvt(\ Event\text{-}syscall\text{-}ioctl \ pid \ fd \ cmd \ arg) \Rightarrow fst(syscall\text{-}ioctl \ s \ pid \ fd \ cmd$
 $arg) \mid$
 $FileEvt(\ Event\text{-}ksys\text{-}ioctl \ pid \ fd \ cmd \ arg) \Rightarrow fst(ksys\text{-}ioctl \ s \ pid \ fd \ cmd \ arg) \mid$
 $FileEvt(\ Event\text{-}vm\text{-}mmap\text{-}pgoff \ pid \ file \ addr \ len' \ prot \ flag \ pgoff)$
 $\Rightarrow fst(vm\text{-}mmap\text{-}pgoff \ s \ pid \ file \ addr \ len' \ prot \ flag \ pgoff) \mid$
 $FileEvt(\ Event\text{-}do\text{-}sys\text{-}vm86 \ pid) \Rightarrow fst(do\text{-}sys\text{-}vm86 \ s \ pid) \mid$
 $FileEvt(\ Event\text{-}get\text{-}unmapped\text{-}area \ pid \ file \ addr) \Rightarrow fst(get\text{-}unmapped\text{-}area$
 $s \ pid \ file \ addr) \mid$
 $FileEvt(\ Event\text{-}validate\text{-}mmap\text{-}request \ pid \ file \ addr) \Rightarrow fst(validate\text{-}mmap\text{-}request$
 $s \ pid \ file \ addr) \mid$
 $FileEvt(\ Event\text{-}generic\text{-}setlease \ pid \ file \ arg) \Rightarrow fst(generic\text{-}setlease \ s \ pid \ file$
 $arg) \mid$
 $FileEvt(\ Event\text{-}syscall\text{-}lock \ pid \ fd \ cmd) \Rightarrow fst(syscall\text{-}lock \ s \ pid \ fd \ cmd) \mid$
 $FileEvt(\ Event\text{-}do\text{-}lock\text{-}file\text{-}wait \ pid \ file \ cmd \ fl) \Rightarrow fst(do\text{-}lock\text{-}file\text{-}wait \ s \ pid$
 $file \ cmd \ fl) \mid$
 $FileEvt(\ Event\text{-}file\text{-}fcntl \ pid \ file \ cmd \ arg) \Rightarrow fst(file\text{-}fcntl \ s \ pid \ file \ cmd$
 $arg) \mid$
 $FileEvt(\ Event\text{-}file\text{-}send\text{-}sigiotask \ pid \ t \ fown \ sig) \Rightarrow fst(file\text{-}send\text{-}sigiotask \ s$
 $pid \ t \ fown \ sig) \mid$
 $FileEvt(\ Event\text{-}file\text{-}receive \ pid \ f) \Rightarrow fst(file\text{-}receive \ s \ pid \ f) \mid$
 $FileEvt(\ Event\text{-}do\text{-}dentry\text{-}open \ pid \ f) \Rightarrow fst(do\text{-}dentry\text{-}open \ s \ pid \ f) \mid$

$KIpcEvt(\ (\ Event\text{-}ipc\text{-}permission \ pid \ ipc \ flg)) \Rightarrow fst(ipcperms \ s \ pid \ ipc \ flg)$
 \mid
 $KIpcEvt(\ (\ Event\text{-}ipc\text{-}getsecid \ pid \ ipc)) \Rightarrow fst(audit\text{-}ipc\text{-}obj \ s \ pid \ ipc) \mid$

$KIpcEvt((Event\text{-}msg\text{-}queue\text{-}associate\ pid\ msq\ msqflg)) \Rightarrow fst(ksys\text{-}msgget\ s\ pid\ msq\ msqflg) \mid$
 $KIpcEvt((Event\text{-}msg\text{-}queue\text{-}msgctl\ pid\ msq\ cmd)) \Rightarrow fst(msg\text{-}queue\text{-}msgctl\ s\ pid\ msq\ cmd) \mid$
 $KIpcEvt((Event\text{-}msg\text{-}queue\text{-}msgsnd\ pid\ msq\ msg\ msgflg)) \Rightarrow fst(do\text{-}msgsnd\ s\ pid\ msq\ msg\ msgflg) \mid$
 $KIpcEvt((Event\text{-}msg\text{-}queue\text{-}msgrcv\ pid\ isp\ msq\ p\ long\ msqflg)) \Rightarrow fst(msg\text{-}queue\text{-}msgrcv\ s\ pid\ isp\ msq\ p\ long\ msqflg) \mid$
 $KIpcEvt((Event\text{-}shm\text{-}associate\ pid\ shm\ shmflg)) \Rightarrow fst(ksys\text{-}shmget\ s\ pid\ shm\ shmflg) \mid$
 $KIpcEvt((Event\text{-}shm\text{-}shmctl\ pid\ shm\ cmd)) \Rightarrow fst(shm\text{-}msgctl\ s\ pid\ shm\ cmd) \mid$
 $KIpcEvt((Event\text{-}shm\text{-}shmat\ pid\ shp\ shmaddr\ shmflg)) \Rightarrow fst(do\text{-}shmat\ s\ pid\ shp\ shmaddr\ shmflg) \mid$
 $KIpcEvt((Event\text{-}sem\text{-}associate\ pid\ sem\ semflg)) \Rightarrow fst(ksys\text{-}semget\ s\ pid\ sem\ semflg) \mid$
 $KIpcEvt((Event\text{-}sem\text{-}semctl\ pid\ sem\ cmd)) \Rightarrow fst(sem\text{-}msgctl\ s\ pid\ sem\ cmd) \mid$
 $KIpcEvt((Event\text{-}sem\text{-}semop\ pid\ sma\ sops\ nsops\ alter)) \Rightarrow fst(do\text{-}semtimedop\ s\ pid\ sma\ sops\ nsops\ alter) \mid$
 $KeyEvt(Event\text{-}key\text{-}permission\ pid\ key\text{-}ref\ cred'\ perm) \Rightarrow fst(key\text{-}task\text{-}permission\ s\ pid\ key\text{-}ref\ cred'\ perm) \mid$
 $KeyEvt(Event\text{-}key\text{-}getsecurity\ pid\ keyid'\ buffer\ buflen) \Rightarrow fst(keyctl\text{-}get\text{-}security\ s\ pid\ keyid'\ buffer\ buflen) \mid$
 $AuditEvt(Event\text{-}audit\text{-}data\text{-}to\text{-}entry\ pid) \Rightarrow fst(audit\text{-}data\text{-}to\text{-}entry\ s\ pid) \mid$
 $AuditEvt(Event\text{-}audit\text{-}dupe\text{-}lsm\text{-}field\ pid\ df\ sf) \Rightarrow fst(audit\text{-}dupe\text{-}lsm\text{-}field\ s\ pid\ df\ sf) \mid$
 $AuditEvt(Event\text{-}audit\text{-}rule\text{-}known\ pid\ krule) \Rightarrow fst(update\text{-}lsm\text{-}rule\ s\ pid\ krule) \mid$
 $AuditEvt(Event\text{-}audit\text{-}rule\text{-}match\ pid\ sid) \Rightarrow fst(audit\text{-}rule\text{-}match\ s\ pid\ sid) \mid$
 $AuditEvt(Event\text{-}audit\text{-}rule\text{-}free\ pid\ f) \Rightarrow fst(audit\text{-}free\text{-}lsm\text{-}field\ s\ pid\ f) \mid$
 $SocketEvt(Event\text{-}unix\text{-}stream\text{-}connect\ pid\ sock\ uaddr\ addr\text{-}len\ flags') \Rightarrow fst(unix\text{-}stream\text{-}connect\ s\ pid\ sock\ uaddr\ addr\text{-}len\ flags') \mid$
 $SocketEvt(Event\text{-}unix\text{-}dgram\text{-}connect\ pid\ sock\ uaddr\ alen\ flags') \Rightarrow fst(unix\text{-}dgram\text{-}connect\ s\ pid\ sock\ uaddr\ alen\ flags') \mid$
 $SocketEvt(Event\text{-}unix\text{-}dgram\text{-}sendmsg\ pid\ sock\ uaddr\ alen) \Rightarrow fst(unix\text{-}dgram\text{-}sendmsg\ s\ pid\ sock\ uaddr\ alen) \mid$
 $SocketEvt(Event\text{-}sys\text{-}bind'\ pid\ fd\ umyaddr\ addrlen) \Rightarrow fst(sys\text{-}bind'\ s\ pid\ fd\ umyaddr\ addrlen) \mid$
 $SocketEvt(Event\text{-}sys\text{-}connect'\ pid\ fd\ usernvaddr\ addrlen) \Rightarrow fst(sys\text{-}connect'\ s\ pid\ fd\ usernvaddr\ addrlen) \mid$
 $SocketEvt(Event\text{-}sock\text{-}sendmsg\ pid\ sock\ msg) \Rightarrow fst(sock\text{-}sendmsg\ s\ pid\ sock\ msg) \mid$
 $SocketEvt(Event\text{-}sock\text{-}recvmsg\ pid\ sock\ msg\ flags') \Rightarrow fst(sock\text{-}recvmsg\ s\ pid\ sock\ msg\ flags') \mid$
 $SocketEvt(Event\text{-}sk\text{-}filter\text{-}trim\text{-}cap\ pid\ sk'\ skb\ cap) \Rightarrow fst(sk\text{-}filter\text{-}trim\text{-}cap\ s\ pid\ sk'\ skb\ cap) \mid$


```

pid sk' skb cap) |
  SocketEvt( Event-sock-getsockopt pid sock level' optname optval optlen )
  ⇒ fst(sock-getsockopt s pid sock level' optname optval optlen) |
  SocketEvt( Event-unix-get-peersec-dgram pid sock scm ) ⇒ fst(unix-get-peersec-dgram
s pid sock scm ) |

  InodeEvt( Event-vfs-link pid old-dentry dir new-dentry delegated-inode )
  ⇒ fst(vfs-link s pid old-dentry dir new-dentry delegated-inode)|
  InodeEvt( Event-vfs-unlink pid dir dentry delegated-inode )
  ⇒ fst(vfs-unlink s pid dir dentry delegated-inode) |
  InodeEvt( Event-vfs-rmdir pid dir dentry ) ⇒ fst(vfs-rmdir s pid dir dentry
) |
  InodeEvt( Event-vfs-rename pid old-dir old-dentry new-dir new-dentry delegated-inode
flgs )
  ⇒ fst(vfs-rename s pid old-dir old-dentry new-dir new-dentry delegated-inode
flgs) |
  InodeEvt( Event-inode-permission pid inode mask' ) ⇒ fst(inode-permission
s pid inode mask') |
  InodeEvt( Event-notify-change pid dentry attr' delegated-inode )
  ⇒ fst(notify-change s pid dentry attr' delegated-inode ) |
  InodeEvt( Event-fat-iocctl-set-attributes pid f ) ⇒ fst(fat-iocctl-set-attributes s
pid f) |
  InodeEvt( Event-vfs-getattr pid path ) ⇒ fst(vfs-getattr s pid path) |
  InodeEvt( Event-vfs-setxattr pid dentry name value size' flgs)
  ⇒ fst(vfs-setxattr s pid dentry name value size' flgs) |
  InodeEvt( Event-vfs-getxattr pid dentry name value size' )
  ⇒ fst(vfs-getxattr s pid dentry name value size' ) |
  InodeEvt( Event-vfs-removexattr pid dentry name )
  ⇒ fst(vfs-removexattr s pid dentry name) |
  InodeEvt( Event-xattr-getsecurity pid inode name value size')
  ⇒ fst(xattr-getsecurity s pid inode name value size') |
  InodeEvt( Event-nfs4-listxattr-nfs4-label pid inode name size')
  ⇒ fst(nfs4-listxattr-nfs4-label s pid inode name size')|
  InodeEvt( Event-sockfs-listxattr pid dentry buffer size')
  ⇒ fst(sockfs-listxattr s pid dentry buffer size')
)

```

definition *observe* :: 'a ⇒ nat ⇒ Obj set (**infixl** 55)
where *observe* s subj ≡ {obj. obj ∈ Obj s ∧
 READ ∈ access-rules (subj-label s subj) (obj-label s
 obj)}

definition *alter* :: 'a ⇒ nat ⇒ Obj set (**infixl** 56)
where *alter* s subj ≡ {obj . obj ∈ Obj s ∧
 WRITE ∈ access-rules (subj-label s subj) (obj-label s
 obj)}

primrec *domain-of-event* :: *Event* \Rightarrow *process-id option* **where**
domain-of-event (*SbEvt* *e*) = *Some* (*getpid-from-sb-event* *e*) |
domain-of-event (*TskEvt* *e*) = *Some* (*getpid-from-tsk-event* *e*) |
domain-of-event (*PtraceEvt* *e*) = *Some* (*getpid-from-pttrace-event* *e*) |
domain-of-event (*SysEvt* *e*) = *Some* (*getpid-from-sys-event* *e*) |
domain-of-event (*FileEvt* *e*) = *Some* (*getpid-from-file-event* *e*) |
domain-of-event (*KIpcEvt* *e*) = *Some* (*getpid-from-kern-ipc-event* *e*) |
domain-of-event (*KeyEvt* *e*) = *Some* (*getpid-from-key-evevt* *e*) |
domain-of-event (*AuditEvt* *e*) = *Some* (*getpid-from-aduit-evevt* *e*) |
domain-of-event (*SocketEvt* *e*) = *Some* (*getpid-from-socket-evevt* *e*) |
domain-of-event (*InodeEvt* *e*) = *Some* (*getpid-from-inode-evevt* *e*)

definition *is-process-privileged* :: '*a* \Rightarrow *process-id* \Rightarrow *bool*
where *is-process-privileged* *s* *pid* \equiv *False*

definition *interference* :: *process-id* \Rightarrow '*a* \Rightarrow *process-id* \Rightarrow *bool* ((- @ - -)) **where**
(*d1* @ *s* *d2*) \equiv
(*if is-process-privileged* *s* *d1* then *True*
else if *d1* = *d2* then *True*
else if (*alter* *s* *d1* \cap *observe* *s* *d2*) \neq {} then *True*
else *False*)

definition *kvpeq* :: '*a* \Rightarrow *process-id* \Rightarrow '*a* \Rightarrow *bool* ((- \sim - \sim -))
where *kvpeq* *s* *d* *t* \equiv
((*subj-label* *s* *d*) = (*subj-label* *t* *d*)) \wedge
(*observe* *s* *d*) = (*observe* *t* *d*) \wedge
($\forall v$. *interference* *v* *s* *d* = *interference* *v* *t* *d*) \wedge
(*let* *obs* = (*observe* *s* *d*) *in* $\forall n$. *n* \in *obs* \longrightarrow (*contents* *s* *n*) =
(*contents* *t* *n*))

definition *non-interference* :: *process-id* \Rightarrow '*a* \Rightarrow *process-id* \Rightarrow *bool* ((- @ - \ -))
where (*u* @ *s* \ *v*) \equiv \neg (*u* @ *s* *v*)

declare *non-interference-def* [*cong*] **and** *domain-of-event-def* [*cong*]

lemma *kvpeq-transitive-lemma* : $\forall s t r d$. (*kvpeq* *s* *d* *t*) \wedge (*kvpeq* *t* *d* *r*) \longrightarrow (*kvpeq* *s* *d* *r*)
by (*simp* *add*: *kvpeq-def*)

lemma *kvpeq-symmetric-lemma* : $\forall s t d$. (*kvpeq* *s* *d* *t*) \longrightarrow (*kvpeq* *t* *d* *s*)
by (*simp* *add*: *kvpeq-def*)

lemma *kvpeq-reflexive-lemma* : $\forall s d$. (*kvpeq* *s* *d* *s*)
by (*auto* *simp* *add*: *kvpeq-def*)

lemma *reachable-top*:

$\forall s \ a. (SM.reachable0 \ s0 \ exec-event) \ s \longrightarrow (\exists s'. \ s' = exec-event \ a)$
by *simp*

lemma *policy-respect1*: $\forall v \ d \ s \ t. (s \sim d \sim t)$

$\longrightarrow (interference \ v \ s \ d = interference \ v \ t \ d)$

using *kvpeq-def* **by** *auto*

definition *obsalter-cons* $\equiv \forall s \ t \ u \ v. (s \sim u \sim t) \wedge (s \sim v \sim t)$

$\longrightarrow (alter \ s \ v \cap observe \ s \ u) = (alter \ t \ v \cap observe \ t \ u)$

lemma *vpeq-def1*: $\forall s \ t \ u. (s \sim u \sim t) \longrightarrow$

$(\forall v. interference \ v \ s \ u = interference \ v \ t \ u) \wedge$
 $(\forall n \in (observe \ s \ u). (contents \ s \ n) = (contents \ t \ n))$

by (*simp add: kvpeq-def*)

lemma *interf-reflexive-lemma* : $\forall d \ s. interference \ d \ s \ d$

using *interference-def* **by** *auto*

lemma *nintf-neq*: $u @ s \setminus v \Longrightarrow u \neq v$

using *interf-reflexive-lemma non-interference-def* **by** *auto*

lemma *nintf-reflx*: $interference \ u \ s \ u$

by (*simp add: interf-reflexive-lemma*)

lemma *contents-consistent'*: $(\forall s \ u \ t. (s \sim u \sim t) \longrightarrow (\forall n \in observe \ s \ u. contents \ s \ n = contents \ t \ n))$

by (*simp add: vpeq-def1*)

lemma *observed-consistent'*: $(\forall s \ t \ u. ((s \sim u \sim t) \longrightarrow s \ u = t \ u))$

using *kvpeq-def* **by** *blast*

lemma *ac-interferes'*: $\forall s \ u \ v \ n. n \in alter \ s \ u \wedge n \in observe \ s \ v \longrightarrow (u @ s \ v)$

using *interference-def* **by** *auto*

thm *LSM-Security-model.intro*

thm *SM-enabled.intro*

thm *LSM-Security-model-axioms.intro*

interpretation *LSM-Security-model s0 exec-event domain-of-event kvpeq interference observe alter contents*

using *kvpeq-transitive-lemma kvpeq-symmetric-lemma kvpeq-reflexive-lemma ac-interferes'*

nintf-reflx policy-respect1 reachable-top contents-consistent' observed-consistent'

SM.intro[of *kvpeq interference*]

SM-enabled-axioms.intro[of *s0 exec-event kvpeq interference*]

SM-enabled.intro[of *kvpeq interference*]

LSM-Security-model.intro[of *s0 exec-event kvpeq interference*]

LSM-Security-model-axioms.intro[of *kvpeq observe contents alter interference*]

by *fast*

29.22 Concrete unwinding condition of "local respect"

29.23 smack superbblock hooks local respect proof

29.23.1 proving "sb_{copy}data" satisfying the "local respect" property

lemma *k-sb-copy-data-local-rsp*:

assumes *p0*: *reachable0 s*
 and *p1*: $\neg(\text{interference } pid \ s \ d)$
 and *p2*: $s' = fst \ (k\text{-sb-copy-data } s \ pid)$
 shows $s \sim d \sim s'$
 proof –
 have *a1*: $s = s'$
 apply (*simp add: p2 k-sb-copy-data-def*)
 by (*metis (mono-tags, lifting) fstI*)
 then show ?thesis
 by (*simp add: kveq-reflexive-lemma*)
 qed

lemma *k-sb-copy-data-local-rsp-e*:

assumes *p0*: *reachable0 s*
 and *p1*: $e = SbEvt \ (Event\text{-sb-copy-data } pid \ sb)$
 and *p2*: *non-interference* (*the*(*domain-of-event e*)) *s d*
 and *p3*: $s' = exec\text{-event } s \ e$
 shows $s \sim d \sim s'$
 proof –
 {
 have *a0*: (*the* (*domain-of-event e*)) = *pid*
 using *p1 domain-of-event-def getpid-from-sb-event-def* by *auto*
 have *a1*: $s' = fst \ (k\text{-sb-copy-data } s \ pid)$
 using *p1 p3 exec-event-def* by *auto*
 have *a2*: $\neg(\text{interference } pid \ s \ d)$
 using *p2 a0 non-interference-def*
 by *blast*
 have *a3*: $s \sim d \sim s'$
 using *a1 a2 p0 k-sb-copy-data-local-rsp* by *blast*
 }
 then show ?thesis
 by *fast*

qed

lemma *k-sb-copy-data-dlocal-rsp-e*: *dynamic-local-respect-e* (*SbEvt* (*Event-sb-copy-data* *pid sb*))

using *dynamic-local-respect-e-def k-sb-copy-data-local-rsp-e non-interference-def*
 by *blast*

29.23.2 proving "do_{remount}" satisfying the "local respect" property

lemma *do-remount-local-rsp*:

assumes $p0$: *reachable0* s
 and $p1$: $\neg(\text{interference } pid \ s \ d)$
 and $p2$: $s' = fst(\text{do-remount } s \ p \ v)$
 shows $s \sim d \sim s'$
 proof –
 have $a1$: $s = s'$
 by (simp add: $p2$ *do-remount-def*)
 then show ?thesis
 by (simp add: *kvpeq-reflexive-lemma*)
 qed

lemma *do-remount-local-rsp-e*:

assumes $p0$: *reachable0* s
 and $p1$: $e = SbEvt \ (\text{Event-sb-remount } pid \ p \ v)$
 and $p2$: *non-interference* (*the*(*domain-of-event* e)) $s \ d$
 and $p3$: $s' = \text{exec-event } s \ e$
 shows $s \sim d \sim s'$
 proof –
 {
 have $a0$: (*the* (*domain-of-event* e)) = pid
 using $p1$ *domain-of-event-def* *getpid-from-sb-event-def* by auto
 have $a1$: $s' = fst(\text{do-remount } s \ p \ v)$
 using $p1$ $p3$ *exec-event-def* by auto
 have $a2$: $\neg(\text{interference } pid \ s \ d)$
 using $p2$ $a0$ *non-interference-def*
 by blast
 have $a3$: $s \sim d \sim s'$
 using $a1$ $a2$ $p0$ *do-remount-local-rsp* by blast
 }
 then show ?thesis
 by fast
 qed

lemma *do-remount-dlocal-rsp-e*: *dynamic-local-respect-e* (*SbEvt* (*Event-sb-remount* $pid \ p \ v$))

using *dynamic-local-respect-e-def* *do-remount-local-rsp-e* *non-interference-def* by blast

thm *mount-fs-def*

29.23.3 proving "mount_fs" satisfying the "local respect" property

lemma *mount-fs-local-rsp*:

assumes $p0$: *reachable0* s
 and $p1$: $\neg(\text{interference } pid \ s \ d)$
 and $p2$: $s' = fst(\text{mount-fs } s \ t \ f \ name \ data \)$
 shows $s \sim d \sim s'$

```

proof-
  have a1:  $s = s'$ 
    apply (simp add: p2 mount-fs-def)
    by (smt fstI)
  then show ?thesis
    by (simp add: kvpeq-reflexive-lemma)
qed

```

```

lemma mount-fs-local-rsp-e:
  assumes p0: reachable0 s
  and p1:  $e = \text{SbEvt } (\text{Event-sb-kern-mount } pid \ t \ f \ name \ data \ )$ 
  and p2: non-interference (the(domain-of-event e)) s d
  and p3:  $s' = \text{exec-event } s \ e$ 
  shows  $s \sim d \sim s'$ 
  proof -
    {
      have a0: (the (domain-of-event e)) = pid
        using p1 domain-of-event-def getpid-from-sb-event-def by auto
      have a1:  $s' = \text{fst}(\text{mount-fs } s \ t \ f \ name \ data \ )$ 
        using p1 p3 exec-event-def by auto
      have a2:  $\neg(\text{interference } pid \ s \ d)$ 
        using p2 a0 non-interference-def
        by blast
      have a3:  $s \sim d \sim s'$ 
        using a1 a2 p0 mount-fs-local-rsp by blast
    }
  then show ?thesis
    by fast
qed

```

```

lemma mount-fs-dlocal-rsp-e: dynamic-local-respect-e (SbEvt (Event-sb-kern-mount
pid t f name data ))
  using dynamic-local-respect-e-def mount-fs-local-rsp-e non-interference-def by
blast

```

29.23.4 proving "show_{sbopts}" satisfying the "local respect" property

```

lemma k-show-sb-opts-local-rsp:
  assumes p0: reachable0 s
  and p1:  $\neg(\text{interference } pid \ s \ d)$ 
  and p2:  $s' = \text{fst}(\text{show-sb-opts } s \ pid \ sq \ t \ )$ 
  shows  $s \sim d \sim s'$ 
  proof-
    have a1:  $s = s'$ 
      by (simp add: p2 show-sb-opts-def)
    then show ?thesis
      by (simp add: kvpeq-reflexive-lemma)
  qed

```

```

lemma k-show-sb-opts-local-rsp-e:
  assumes p0 : reachable0 s
  and p1: e = SbEvt (Event-sb-show-options pid sq t)
  and p2: non-interference (the(domain-of-event e)) s d
  and p3: s' = exec-event s e
shows s ~ d ~ s'
proof –
{
  have a0: (the (domain-of-event e)) = pid
    using p1 domain-of-event-def getpid-from-sb-event-def by auto
  have a1: s' = fst (show-sb-opts s pid sq t )
    using p1 p3 exec-event-def by auto
  have a2:  $\neg(\text{interference pid s d})$ 
    using p2 a0 non-interference-def
    by blast
  have a3: s ~ d ~ s'
    using a1 a2 p0 k-show-sb-opts-local-rsp by blast
}
then show ?thesis
by fast
qed

```

```

lemma k-show-sb-opts-dlocal-rsp-e: dynamic-local-respect-e (SbEvt (Event-sb-show-options
pid sq t))
  using dynamic-local-respect-e-def k-show-sb-opts-local-rsp-e non-interference-def
by blast

```

29.23.5 proving "sb_sstatfs" satisfying the "local respect" property

```

lemma k-sb-statfs-local-rsp:
  assumes p0: reachable0 s
  and p1:  $\neg(\text{interference pid s d})$ 
  and p2: s' = fst (statfs-by-dentry s pid de )
shows s ~ d ~ s'
proof –
  have a1: s = s'
    by (simp add: p2 statfs-by-dentry-def)
  then show ?thesis
    by (simp add: kveq-reflexive-lemma)
qed

```

```

lemma k-sb-statfs-local-rsp-e:
  assumes p0 : reachable0 s
  and p1: e = SbEvt (Event-sb-statfs pid de)
  and p2: non-interference (the(domain-of-event e)) s d
  and p3: s' = exec-event s e
shows s ~ d ~ s'
proof –

```

```

{
  have a0: (the (domain-of-event e)) = pid
    using p1 domain-of-event-def getpid-from-sb-event-def by auto
  have a1: s' = fst (statfs-by-dentry s pid de )
    using p1 p3 exec-event-def by auto
  have a2: ¬(interference pid s d)
    using p2 a0 non-interference-def
    by blast
  have a3: s ~ d ~ s'
    using a1 a2 p0 k-sb-statfs-local-rsp by blast
}
then show ?thesis
  by fast
qed

```

lemma *sb-statfs-dlocal-rsp-e: dynamic-local-respect-e* (*SbEvt (Event-sb-statfs pid de)*)
using dynamic-local-respect-e-def k-sb-statfs-local-rsp-e non-interference-def by blast

29.23.6 proving "do_mount" satisfying the "local respect" property

lemma *do-mount-local-rsp:*
assumes p0: reachable0 s
and p1: ¬(interference pid s d)
and p2: s' = fst (do-mount s pid dev-name dir-name type-page flags' data-page)
shows s ~ d ~ s'
proof –
have a1: s = s'
by (simp add: p2 do-mount-def)
then show ?thesis
by (simp add: kveq-reflexive-lemma)
qed

lemma *do-mount-local-rsp-e:*
assumes p0 : reachable0 s
and p1: e = SbEvt (Event-sb-mount pid devname dirname t f p)
and p2: non-interference (the(domain-of-event e)) s d
and p3: s' = exec-event s e
shows s ~ d ~ s'
proof –
{
 have a0: (the (domain-of-event e)) = pid
 using p1 domain-of-event-def getpid-from-sb-event-def by auto
 have a1: s' = fst (do-mount s pid devname dirname t f p)
 using p1 p3 exec-event-def by auto
 have a2: ¬(interference pid s d)
 using p2 a0 non-interference-def
 by blast
}


```

    have a3:  $s \sim d \sim s'$ 
    using a1 a2 p0 do-mount-local-rsp by blast
  }
  then show ?thesis
    by fast
qed

```

lemma *do-mount-dlocal-rsp-e: dynamic-local-respect-e* (*SbEvt* (*Event-sb-mount* *pid devname dirname t f p*))
 using *do-mount-local-rsp-e dynamic-local-respect-e-def non-interference-def* by *presburger*

29.23.7 proving "do_umount" satisfying the "local respect" property

lemma *do-umount-local-rsp:*
 assumes *p0: reachable0 s*
 and *p1: $\neg(\text{interference pid s d})$*
 and *p2: $s' = \text{fst}(\text{do-umount s pid m f})$*
 shows $s \sim d \sim s'$
 proof –
 have *a1: $s = s'$*
 by (*simp add: p2 do-umount-def*)
 then show ?thesis
 by (*simp add: kveq-reflexive-lemma*)
 qed

lemma *do-umount-local-rsp-e:*
 assumes *p0 : reachable0 s*
 and *p1: $e = \text{SbEvt}(\text{Event-sb-umount pid m f})$*
 and *p2: non-interference (the(domain-of-event e)) s d*
 and *p3: $s' = \text{exec-event s e}$*
 shows $s \sim d \sim s'$
 proof –
 {
 have *a0: (the (domain-of-event e)) = pid*
 using *p1 domain-of-event-def getpid-from-sb-event-def* by auto
 have *a1: $s' = \text{fst}(\text{do-umount s pid m f})$*
 using *p1 p3 exec-event-def* by auto
 have *a2: $\neg(\text{interference pid s d})$*
 using *p2 a0 non-interference-def*
 by blast
 have *a3: $s \sim d \sim s'$*
 using *a1 a2 p0 do-umount-local-rsp* by blast
 }
 then show ?thesis
 by fast
qed

lemma *do-umount-dlocal-rsp-e: dynamic-local-respect-e* (*SbEvt* (*Event-sb-umount*

```

pid m f))
  using do-umount-local-rsp-e dynamic-local-respect-e-def non-interference-def
  by blast

```

29.23.8 proving "pivot_{root}" satisfying the "local respect" property

```

lemma pivot-root-local-rsp:
  assumes p0: reachable0 s
    and p1:  $\neg(\text{interference pid s d})$ 
    and p2:  $s' = \text{fst}(\text{pivot-root s pid})$ 
  shows  $s \sim d \sim s'$ 
  proof -
    have a1:  $s = s'$ 
    by (simp add: p2 pivot-root-def)
    then show ?thesis
    by (simp add: kveq-reflexive-lemma)
  qed

```

```

lemma pivot-root-local-rsp-e:
  assumes p0: reachable0 s
    and p1:  $e = \text{SbEvt}(\text{Event-sb-pivotroot pid})$ 
    and p2: non-interference (the(domain-of-event e)) s d
    and p3:  $s' = \text{exec-event s e}$ 
  shows  $s \sim d \sim s'$ 
  proof -
    {
      have a0: (the (domain-of-event e)) = pid
      using p1 domain-of-event-def getpid-from-sb-event-def by auto
      have a1:  $s' = \text{fst}(\text{pivot-root s pid})$ 
      using p1 p3 exec-event-def by auto
      have a2:  $\neg(\text{interference pid s d})$ 
      using p2 a0 non-interference-def
      by blast
      have a3:  $s \sim d \sim s'$ 
      using a1 a2 p0 pivot-root-local-rsp by blast
    }
    then show ?thesis
    by fast
  qed

```

```

lemma pivot-root-dlocal-rsp-e: dynamic-local-respect-e (SbEvt (Event-sb-pivotroot
pid))
  using pivot-root-local-rsp-e dynamic-local-respect-e-def non-interference-def
  by blast

```

29.23.9 proving "setup_{securityoptions}" satisfying the "local respect" property

```

lemma setup-security-options-local-rsp:
  assumes p0: reachable0 s
    and p1:  $\neg(\text{interference pid s d})$ 

```

```

    and p2: s' = fst(setup-security-options s pid n sb opt)
  shows s ~ d ~ s'
  using p2 setup-security-options-def
  by (simp add: kvpeq-reflexive-lemma)

lemma setup-security-options-local-rsp-e:
  assumes p0 : reachable0 s
  and p1: e = SbEvt (Event-set-mnt-opts pid n sb opt)
  and p2: non-interference (the(domain-of-event e)) s d
  and p3: s' = exec-event s e
  shows s ~ d ~ s'
  proof -
  {
    have a0: (the (domain-of-event e)) = pid
      using p1 domain-of-event-def getpid-from-sb-event-def by auto
    have a1: s' = fst(setup-security-options s pid n sb opt)
      using p1 p3 exec-event-def by auto
    have a2: ¬(interference pid s d)
      using p2 a0 non-interference-def
      by blast
    have a3: s ~ d ~ s'
      using a1 a2 p0 setup-security-options-local-rsp by blast
  }
  then show ?thesis
    by fast
qed

lemma setup-security-options-dlocal-rsp-e: dynamic-local-respect-e (SbEvt (Event-set-mnt-opts
pid n sb opt))
  using setup-security-options-local-rsp-e dynamic-local-respect-e-def non-interference-def

  by blast

29.23.10 proving "setsbsecurity" satisfying the "local respect" property

lemma set-sb-security-local-rsp:
  assumes p0: reachable0 s
  and p1: ¬(interference pid s d)
  and p2: s' = fst (set-sb-security s pid sb de info)
  shows s ~ d ~ s'
  proof -
  have a1: s = s'
    by (simp add: p2 set-sb-security-def)
  then show ?thesis
    by (simp add: kvpeq-reflexive-lemma)
qed

lemma set-sb-security-local-rsp-e:
  assumes p0 : reachable0 s

```

```

    and p1: e = SbEvt (Event-set-sb-security pid sb de info)
    and p2: non-interference (the(domain-of-event e)) s d
    and p3: s' = exec-event s e
shows s ~ d ~ s'
proof -
{
  have a0: (the (domain-of-event e)) = pid
    using p1 domain-of-event-def getpid-from-sb-event-def by auto
  have a1: s' = fst (set-sb-security s pid sb de info)
    using p1 p3 exec-event-def by auto
  have a2: ¬(interference pid s d)
    using p2 a0 non-interference-def
    by blast
  have a3: s ~ d ~ s'
    using a1 a2 p0 set-sb-security-local-rsp by blast
}
then show ?thesis
  by fast
qed

lemma set-sb-security-dlocal-rsp-e: dynamic-local-respect-e ( SbEvt (Event-set-sb-security
pid sb de info))
  using set-sb-security-local-rsp-e dynamic-local-respect-e-def non-interference-def

  by blast

29.23.11 proving "nfs_clone_sb_security" satisfying the "local respect" property
lemma nfs-clone-sb-security-local-rsp:
  assumes p0: reachable0 s
    and p1: ¬(interference pid s d)
    and p2: s' = fst(nfs-clone-sb-security s pid sb de minfo)
  shows s ~ d ~ s'
proof(cases result s (security-sb-clone-mnt-opts' s oldsb sb' kflags kflags-out))
case True
  have a1: s = s'
    using p2 True apply(auto simp add: nfs-clone-sb-security-def )
    by (smt fst-conv)
  then show ?thesis by (simp add: kveq-reflexive-lemma)
next
case False
  have a1: s = s' using p2 False nfs-clone-sb-security-def
    by (smt fst-conv)
  then show ?thesis by (simp add: kveq-reflexive-lemma)
qed

lemma nfs-clone-sb-security-local-rsp-e:
  assumes p0 : reachable0 s
    and p1: e = SbEvt (Event-sb-clone-mnt-opts pid sb de minfo)

```

```

    and p2: non-interference (the(domain-of-event e)) s d
    and p3: s' = exec-event s e
shows   s ~ d ~ s'
proof -
{
  have a0: (the (domain-of-event e)) = pid
    using p1 domain-of-event-def getpid-from-sb-event-def by auto
  have a1: s' = fst(nfs-clone-sb-security s pid sb de minfo)
    using p1 p3 exec-event-def by auto
  have a2: ¬(interference pid s d)
    using p2 a0 non-interference-def
    by blast
  have a3: s ~ d ~ s'
    using a1 a2 p0 nfs-clone-sb-security-local-rsp by blast
}
then show ?thesis
  by fast
qed

```

```

lemma nfs-clone-sb-security-dlocal-rsp-e: dynamic-local-respect-e ( SbEvt (Event-sb-clone-mnt-opts
pid sb d minfo))
  using nfs-clone-sb-security-local-rsp-e dynamic-local-respect-e-def non-interference-def

  by blast

```

29.23.12 proving "parse_ssecurity_{options}" satisfying the "localrespect" property

```

lemma parse-security-options-local-rsp:
  assumes p0: reachable0 s
    and p1: ¬(interference pid s d)
    and p2: s' = fst(parse-security-options s pid str opts')
shows   s ~ d ~ s'
proof -
  have a1: s = s'
    by (simp add: p2 parse-security-options-def)
  then show ?thesis
    by (simp add: kveq-reflexive-lemma)
qed

```

```

lemma parse-security-options-local-rsp-e:
  assumes p0 : reachable0 s
    and p1: e = SbEvt (Event-sb-parse-opts-str pid str opts')
    and p2: non-interference (the(domain-of-event e)) s d
    and p3: s' = exec-event s e
shows   s ~ d ~ s'
proof -
{
  have a0: (the (domain-of-event e)) = pid
    using p1 domain-of-event-def getpid-from-sb-event-def by auto

```

```

    have a1:  $s' = \text{fst}(\text{parse-security-options } s \text{ pid str opts'})$ 
      using p1 p3 exec-event-def by auto
    have a2:  $\neg(\text{interference pid } s \text{ d})$ 
      using p2 a0 non-interference-def
      by blast
    have a3:  $s \sim d \sim s'$ 
      using a1 a2 p0 parse-security-options-local-rsp by blast
  }
  then show ?thesis
    by fast
qed

```

```

lemma parse-security-options-dlocal-rsp-e: dynamic-local-respect-e ( SbEvt (Event-sb-parse-opts-str
pid str opts'))
  using parse-security-options-local-rsp-e dynamic-local-respect-e-def non-interference-def

  by blast

```

29.24 smack task hooks local respect proof

29.24.1 proving "prepare_creds" satisfying the "local respect" property

```

lemma prepare-creds-local-rsp:
  assumes p0: reachable0 s
    and p1:  $\neg(\text{interference pid } s \text{ d})$ 
    and p2:  $s' = \text{fst}(\text{prepare-creds } s \text{ pid})$ 
  shows  $s \sim d \sim s'$ 
  using p2 prepare-creds-def fst-conv vpeq-reflexive-lemma
  by smt

```

```

lemma prepare-creds-local-rsp-e:
  assumes p0 : reachable0 s
    and p1:  $e = \text{TskEvt } ( \text{Event-prepare-creds pid} )$ 
    and p2: non-interference (the(domain-of-event e)) s d
    and p3:  $s' = \text{exec-event } s \text{ e}$ 
  shows  $s \sim d \sim s'$ 
  proof -
  {
    have a0: (the (domain-of-event e)) = pid
      using p1 domain-of-event-def getpid-from-tsk-event-def by auto
    have a1:  $s' = \text{fst}(\text{prepare-creds } s \text{ pid})$ 
      using p1 p3 exec-event-def by auto
    have a2:  $\neg(\text{interference pid } s \text{ d})$ 
      using p2 a0 non-interference-def
      by blast
    have a3:  $s \sim d \sim s'$ 
      using a1 a2 p0 prepare-creds-local-rsp by blast
  }
  then show ?thesis
    by fast

```

qed

lemma *prepare-creds-dlocal-rsp-e: dynamic-local-respect-e* (*TskEvt* ((*Event-prepare-creds* *pid*)))
using *prepare-creds-local-rsp-e dynamic-local-respect-e-def non-interference-def*
by *blast*

29.24.2 proving "sys_setreuid" satisfying the "local respect" property

lemma *sys-setreuid-local-rsp*:
assumes *p0: reachable0 s*
and *p1: $\neg(\text{interference } pid \ s \ d)$*
and *p2: $s' = fst(\text{sys-setreuid } s \ pid \ kuid \ euid')$*
shows $s \sim d \sim s'$
proof (*cases snd (prepare-creds s pid) = None*)
case *True*
have *a1: $s = s'$*
apply (*simp add: p2 sys-setreuid-def*)
by (*simp add: True*)
then show ?thesis **by** (*simp add: vpeq-reflexive-lemma*)
next
case *False*
have *a1: $s = s'$* **using** *p2 False*
apply (*simp add: resultValue-def security-task-fix-setuid'-def the-run-state-def*
return-def
modify-def put-def get-def bind-def Let-def split-def LSM-SETID-RE-def
ENOMEM-def
prepare-creds-def)
by (*smt fst-conv sys-setreuid-def*)
then show ?thesis
using *kvpeq-reflexive-lemma* **by** *blast*
qed

lemma *sys-setreuid-local-rsp-e*:
assumes *p0 : reachable0 s*
and *p1: $e = \text{TskEvt } (\text{Event-sys-setreuid } pid \ kuid \ euid')$*
and *p2: non-interference (the(domain-of-event e)) s d*
and *p3: $s' = \text{exec-event } s \ e$*
shows $s \sim d \sim s'$
proof –
{
have *a0: (the (domain-of-event e)) = pid*
using *p1 domain-of-event-def getpid-from-tsk-event-def* **by** *auto*
have *a1: $s' = fst(\text{sys-setreuid } s \ pid \ kuid \ euid')$*
using *p1 p3 exec-event-def*
by *simp*
have *a2: $\neg(\text{interference } pid \ s \ d)$*
using *p2 a0 non-interference-def*

```

    by blast
  have a3:  $s \sim d \sim s'$ 
    using a1 a2 p0 sys-setreuid-local-rsp by blast
}
then show ?thesis
  by fast
qed

```

```

lemma sys-setreuid-dlocal-rsp-e: dynamic-local-respect-e (TskEvt ( (Event-sys-setreuid
pid kuid evid')))
  using sys-setreuid-local-rsp-e dynamic-local-respect-e-def non-interference-def
  by blast

```

29.24.3 proving "setpgid" satisfying the "local respect" property

```

lemma setpgid-local-rsp:
  assumes p0: reachable0 s
    and p1:  $\neg(\text{interference pid s d})$ 
    and p2:  $s' = \text{fst}(\text{setpgid s pid i pgid})$ 
  shows  $s \sim d \sim s'$ 
  using p2 setpgid-def fst-conv vpeq-reflexive-lemma
  by smt

```

```

lemma setpgid-local-rsp-e:
  assumes p0 : reachable0 s
    and p1:  $e = \text{TskEvt ( (Event-setpgid pid i pgid))}$ 
    and p2: non-interference (the(domain-of-event e)) s d
    and p3:  $s' = \text{exec-event s e}$ 
  shows  $s \sim d \sim s'$ 
  proof -
  {
    have a0: (the (domain-of-event e)) = pid
      using p1 domain-of-event-def getpid-from-tsk-event-def by auto
    have a1:  $s' = \text{fst}(\text{setpgid s pid i pgid})$ 
      using p1 p3 exec-event-def by auto
    have a2:  $\neg(\text{interference pid s d})$ 
      using p2 a0 non-interference-def
      by blast
    have a3:  $s \sim d \sim s'$ 
      using a1 a2 p0 setpgid-local-rsp by blast
  }
  then show ?thesis
    by fast
qed

```

```

lemma setpgid-dlocal-rsp-e: dynamic-local-respect-e (TskEvt ( (Event-setpgid pid i
pgid)))
  using setpgid-local-rsp-e dynamic-local-respect-e-def non-interference-def
  by blast

```


thm *do-getpgid-def*

29.24.4 proving "do_getpgid" satisfying the "local respect" property

lemma *do-getpgid-local-rsp*:

```

  assumes p0: reachable0 s
    and p1:  $\neg(\text{interference } \text{pid } s \ d)$ 
    and p2:  $s' = \text{fst}(\text{do-getpgid } s \ \text{pid } i)$ 
  shows  $s \sim d \sim s'$ 
proof (cases resultValue s (security-task-getpgid s p)  $\neq 0$ )
  case True
    have a1:  $s = s'$ 
      using p2 True do-getpgid-def
      by (smt fst-conv)
    then show ?thesis
      by (simp add: vpeq-reflexive-lemma)
  next
  case False
    then show ?thesis
      by (smt do-getpgid-def p2 prod.simps(1) surjective-pairing vpeq-reflexive-lemma)
qed

```

lemma *do-getpgid-local-rsp-e*:

```

  assumes p0: reachable0 s
    and p1:  $e = \text{TskEvt } ((\text{Event-do-getpgid } \text{pid } i))$ 
    and p2: non-interference (the(domain-of-event e)) s d
    and p3:  $s' = \text{exec-event } s \ e$ 
  shows  $s \sim d \sim s'$ 
proof -
{
  have a0: (the (domain-of-event e)) = pid
    using p1 domain-of-event-def getpid-from-tsk-event-def by auto
  have a1:  $s' = \text{fst}(\text{do-getpgid } s \ \text{pid } i)$ 
    using p1 p3 exec-event-def by auto
  have a2:  $\neg(\text{interference } \text{pid } s \ d)$ 
    using p2 a0 non-interference-def
    by blast
  have a3:  $s \sim d \sim s'$ 
    using a1 a2 p0 do-getpgid-local-rsp by blast
}
  then show ?thesis
    by fast
qed

```

lemma *do-getpgid-dlocal-rsp-e*: *dynamic-local-respect-e* (*TskEvt* (*(Event-do-getpgid* *pid* *i*)))

using *do-getpgid-local-rsp-e* *dynamic-local-respect-e-def* *non-interference-def*

by *blast*

29.24.5 proving "getsid" satisfying the "local respect" property

```

lemma getsid-local-rsp:
  assumes p0: reachable0 s
    and p1:  $\neg(\text{interference pid s d})$ 
    and p2:  $s' = \text{fst}(\text{getsid s pid i})$ 
  shows  $s \sim d \sim s'$ 
  using fst-conv vpeq-reflexive-lemma p2 getsid-def
  by (smt case-prod-conv)

lemma getsid-local-rsp-e:
  assumes p0 : reachable0 s
    and p1:  $e = \text{TskEvt } ((\text{Event-getsid pid i}))$ 
    and p2:  $\text{non-interference } (\text{the}(\text{domain-of-event } e)) \text{ s d}$ 
    and p3:  $s' = \text{exec-event s e}$ 
  shows  $s \sim d \sim s'$ 
  proof -
  {
    have a0:  $(\text{the } (\text{domain-of-event } e)) = \text{pid}$ 
      using p1 domain-of-event-def getpid-from-tsk-event-def by auto
    have a1:  $s' = \text{fst}(\text{getsid s pid i})$ 
      using p1 p3 exec-event-def by auto
    have a2:  $\neg(\text{interference pid s d})$ 
      using p2 a0 non-interference-def
      by blast
    have a3:  $s \sim d \sim s'$ 
      using a1 a2 p0 getsid-local-rsp by blast
  }
  then show ?thesis
    by fast
qed

```

```

lemma getsid-dlocal-rsp-e: dynamic-local-respect-e ( $\text{TskEvt } ((\text{Event-getsid pid i}))$ )
  using getsid-local-rsp-e dynamic-local-respect-e-def non-interference-def
  by blast

```

29.24.6 proving "getsecid" satisfying the "local respect" property

```

lemma getsecid-local-rsp:
  assumes p0: reachable0 s
    and p1:  $\neg(\text{interference pid s d})$ 
    and p2:  $s' = \text{fst}(\text{getsecid s pid p u})$ 
  shows  $s \sim d \sim s'$ 
  using p2 getsecid-def by (simp add: vpeq-reflexive-lemma)

lemma getsecid-local-rsp-e:
  assumes p0 : reachable0 s

```

```

    and p1: e = TskEvt ((Event-getsecid pid p u))
    and p2: non-interference (the(domain-of-event e)) s d
    and p3: s' = exec-event s e
shows s ~ d ~ s'
proof -
{
  have a0: (the (domain-of-event e)) = pid
    using p1 domain-of-event-def getpid-from-tsk-event-def by auto
  have a1: s' = fst(getsecid s pid p u)
    using p1 p3 exec-event-def by auto
  have a2: ¬(interference pid s d)
    using p2 a0 non-interference-def
    by blast
  have a3: s ~ d ~ s'
    using a1 a2 p0 getsecid-local-rsp by blast
}
then show ?thesis
  by fast
qed

```

```

lemma getsecid-dlocal-rsp-e: dynamic-local-respect-e (TskEvt ((Event-getsecid pid
p u)))
  using getsecid-local-rsp-e dynamic-local-respect-e-def non-interference-def
  by blast

```

29.24.7 proving "task_setnice" satisfying the "localrespect" property

```

lemma task-setnice-local-rsp:
  assumes p0: reachable0 s
    and p1: ¬(interference pid s d)
    and p2: s' = fst(task-setnice s pid p i)
  shows s ~ d ~ s'
proof(cases resultValue s (security-task-setnice s p nice))
case (nonneg n)
  have a1: s = s' using p2 nonneg task-setnice-def
    by (smt fst-conv)
  then show ?thesis by (simp add: vpeq-reflexive-lemma)
next
case (neg n)
  then show ?thesis using p2 neg task-setnice-def
    by (smt fst-conv vpeq-reflexive-lemma)
qed

```

```

lemma task-setnice-local-rsp-e:
  assumes p0 : reachable0 s
    and p1: e = TskEvt ((Event-task-setnice pid p i))
    and p2: non-interference (the(domain-of-event e)) s d
    and p3: s' = exec-event s e
  shows s ~ d ~ s'

```

```

proof –
{
  have  $a0$ : (the (domain-of-event  $e$ )) =  $pid$ 
    using  $p1$  domain-of-event-def getpid-from-tsk-event-def by auto
  have  $a1$ :  $s' = fst(task-setnice\ s\ pid\ p\ i)$ 
    using  $p1\ p3$  exec-event-def by auto
  have  $a2$ :  $\neg(interference\ pid\ s\ d)$ 
    using  $p2\ a0$  non-interference-def
    by blast
  have  $a3$ :  $s \sim d \sim s'$ 
    using  $a1\ a2\ p0$  task-setnice-local-rsp by blast
}
then show ?thesis
by fast
qed

```

```

lemma task-setnice-dlocal-rsp-e: dynamic-local-respect-e (TskEvt ((Event-task-setnice
pid p i)))
using task-setnice-local-rsp-e dynamic-local-respect-e-def non-interference-def
by blast

```

29.24.8 proving "set_iask_ioprio" satisfying the "localrespect" property

```

lemma set-task-ioprio-local-rsp:
  assumes  $p0$ : reachable0  $s$ 
    and  $p1$ :  $\neg(interference\ pid\ s\ d)$ 
    and  $p2$ :  $s' = fst(set-task-ioprio\ s\ pid\ p\ i)$ 
  shows  $s \sim d \sim s'$ 
proof (cases resultValue  $s$  (security-task-setioprio  $s\ p\ ioprio$  ))
case (nonneg  $n$ )
  have  $a1$ :  $s = s'$  using  $p2$  nonneg set-task-ioprio-def
    by (smt fst-conv)
  then show ?thesis by (simp add: vpeq-reflexive-lemma)
next
  case (neg  $n$ )
  then show ?thesis using  $p2$  neg set-task-ioprio-def
    by (smt fst-conv vpeq-reflexive-lemma)
qed

```

```

lemma set-task-ioprio-local-rsp-e:
  assumes  $p0$ : reachable0  $s$ 
    and  $p1$ :  $e = TskEvt ((Event-set-task-ioprio\ pid\ p\ i))$ 
    and  $p2$ : non-interference (the(domain-of-event  $e$ ))  $s\ d$ 
    and  $p3$ :  $s' = exec-event\ s\ e$ 
  shows  $s \sim d \sim s'$ 
  proof –
  {
    have  $a0$ : (the (domain-of-event  $e$ )) =  $pid$ 

```

```

    using p1 domain-of-event-def getpid-from-tsk-event-def by auto
  have a1:  $s' = \text{fst}(\text{set-task-ioprio } s \text{ pid } p \ i)$ 
    using p1 p3 exec-event-def by auto
  have a2:  $\neg(\text{interference pid } s \ d)$ 
    using p2 a0 non-interference-def
    by blast
  have a3:  $s \sim d \sim s'$ 
    using a1 a2 p0 set-task-ioprio-local-rsp by blast
}
then show ?thesis
  by fast
qed

```

```

lemma set-task-ioprio-dlocal-rsp-e: dynamic-local-respect-e ( TskEvt ((Event-set-task-ioprio
pid p i)))
  using set-task-ioprio-local-rsp-e dynamic-local-respect-e-def non-interference-def

  by blast

```

29.24.9 proving "get_{taskioprio}" satisfying the "local respect" property

```

lemma get-task-ioprio-local-rsp:
  assumes p0: reachable0 s
    and p1:  $\neg(\text{interference pid } s \ d)$ 
    and p2:  $s' = \text{fst}(\text{get-task-ioprio } s \text{ pid } p)$ 
  shows  $s \sim d \sim s'$ 
  using fst-conv vpeq-reflexive-lemma p2 get-task-ioprio-def
  by smt

```

```

lemma get-task-ioprio-local-rsp-e:
  assumes p0 : reachable0 s
    and p1:  $e = \text{TskEvt } ((\text{Event-get-task-ioprio pid } p \ ))$ 
    and p2:  $\text{non-interference } (\text{the}(\text{domain-of-event } e)) \ s \ d$ 
    and p3:  $s' = \text{exec-event } s \ e$ 
  shows  $s \sim d \sim s'$ 
  proof -
  {
    have a0:  $(\text{the } (\text{domain-of-event } e)) = \text{pid}$ 
      using p1 domain-of-event-def getpid-from-tsk-event-def by auto
    have a1:  $s' = \text{fst}(\text{get-task-ioprio } s \text{ pid } p \ )$ 
      using p1 p3 exec-event-def by auto
    have a2:  $\neg(\text{interference pid } s \ d)$ 
      using p2 a0 non-interference-def
      by blast
    have a3:  $s \sim d \sim s'$ 
      using a1 a2 p0 get-task-ioprio-local-rsp by blast
  }
  then show ?thesis
    by fast

```

qed

lemma *get-task-ioprio-dlocal-rsp-e: dynamic-local-respect-e* (*TskEvt* ((*Event-get-task-ioprio* *pid p*)))
using *get-task-ioprio-local-rsp-e* *dynamic-local-respect-e-def* *non-interference-def*
by *blast*

29.24.10 proving "check_{prlimit}permission" satisfying the "localrespect" property

lemma *check-prlimit-permission-local-rsp:*
assumes *p0: reachable0 s*
and *p1: ¬(interference pid s d)*
and *p2: s' = fst(check-prlimit-permission s pid p i)*
shows *s ~ d ~ s'*
proof –
 {
have *a1: s = s' using p2 check-prlimit-permission-def*
by (*smt fst-conv*)
then show ?thesis by (*simp add: vpeq-reflexive-lemma*)
 }
 qed

lemma *check-prlimit-permission-local-rsp-e:*
assumes *p0 : reachable0 s*
and *p1: e = TskEvt ((Event-check-prlimit-permission pid p i))*
and *p2: non-interference (the(domain-of-event e)) s d*
and *p3: s' = exec-event s e*
shows *s ~ d ~ s'*
proof –
 {
have *a0: (the (domain-of-event e)) = pid*
using *p1 domain-of-event-def getpid-from-tsk-event-def by auto*
have *a1: s' = fst(check-prlimit-permission s pid p i)*
using *p1 p3 exec-event-def by auto*
have *a2: ¬(interference pid s d)*
using *p2 a0 non-interference-def*
by *blast*
have *a3: s ~ d ~ s'*
using *a1 a2 p0 check-prlimit-permission-local-rsp by blast*
 }
then show ?thesis
by *fast*
 qed

lemma *check-prlimit-permission-dlocal-rsp-e: dynamic-local-respect-e*
 (*TskEvt* ((*Event-check-prlimit-permission* *pid p i*)))
using *check-prlimit-permission-local-rsp-e* *dynamic-local-respect-e-def* *non-interference-def*

by *blast*

29.24.11 proving "do_{prlimit}" satisfying the "local respect" property

```

lemma do-prlimit-local-rsp:
  assumes p0: reachable0 s
    and p1:  $\neg(\text{interference } pid \ s \ d)$ 
    and p2:  $s' = fst(\text{do-prlimit } s \ pid \ p \ i)$ 
  shows  $s \sim d \sim s'$ 
  using p2 do-prlimit-def
  by (simp add: vpeq-reflexive-lemma)

lemma do-prlimit-local-rsp-e:
  assumes p0 : reachable0 s
    and p1:  $e = TskEvt \ ((Event\text{-}do\text{-}prlimit \ pid \ p \ i))$ 
    and p2:  $non\text{-}interference \ (the(\text{domain-of-event } e)) \ s \ d$ 
    and p3:  $s' = exec\text{-}event \ s \ e$ 
  shows  $s \sim d \sim s'$ 
  proof -
  {
    have a0:  $(the \ (domain\text{-}of\text{-}event \ e)) = pid$ 
      using p1 domain-of-event-def getpid-from-tsk-event-def by auto
    have a1:  $s' = fst(\text{do-prlimit } s \ pid \ p \ i)$ 
      using p1 p3 exec-event-def by auto
    have a2:  $\neg(\text{interference } pid \ s \ d)$ 
      using p2 a0 non-interference-def
      by blast
    have a3:  $s \sim d \sim s'$ 
      using a1 a2 p0 do-prlimit-local-rsp by blast
  }
  then show ?thesis
    by fast
qed

```

```

lemma do-prlimit-dlocal-rsp-e: dynamic-local-respect-e
  ( $TskEvt \ ((Event\text{-}do\text{-}prlimit \ pid \ p \ i))$ )
  using do-prlimit-local-rsp-e dynamic-local-respect-e-def non-interference-def
  by blast

```

29.24.12 proving "task_{setscheduler}" satisfying the "local respect" property

```

lemma task-setscheduler-local-rsp:
  assumes p0: reachable0 s
    and p1:  $\neg(\text{interference } pid \ s \ d)$ 
    and p2:  $s' = fst(\text{task-setscheduler } s \ pid \ p)$ 
  shows  $s \sim d \sim s'$ 
  using p2 task-setscheduler-def
  by (smt fstI vpeq-reflexive-lemma)

lemma task-setscheduler-local-rsp-e:

```

```

assumes  $p0 : \text{reachable0 } s$ 
and  $p1 : e = \text{TskEvt } ((\text{Event-task-setscheduler } pid \ p))$ 
and  $p2 : \text{non-interference } (\text{the}(\text{domain-of-event } e)) \ s \ d$ 
and  $p3 : s' = \text{exec-event } s \ e$ 
shows  $s \sim d \sim s'$ 
proof –
{
  have  $a0 : (\text{the } (\text{domain-of-event } e)) = pid$ 
    using  $p1 \ \text{domain-of-event-def } \text{getpid-from-tsk-event-def}$  by auto
  have  $a1 : s' = \text{fst}(\text{task-setscheduler } s \ pid \ p)$ 
    using  $p1 \ p3 \ \text{exec-event-def}$  by auto
  have  $a2 : \neg(\text{interference } pid \ s \ d)$ 
    using  $p2 \ a0 \ \text{non-interference-def}$ 
    by blast
  have  $a3 : s \sim d \sim s'$ 
    using  $a1 \ a2 \ p0 \ \text{task-setscheduler-local-rsp}$  by blast
}
then show ?thesis
by fast
qed

```

```

lemma task-setscheduler-dlocal-rsp-e: dynamic-local-respect-e
  ( $\text{TskEvt } ((\text{Event-task-setscheduler } pid \ p))$ )
using task-setscheduler-local-rsp-e dynamic-local-respect-e-def non-interference-def

by blast

```

29.24.13 proving "task_{getscheduler}" satisfying the "localrespect" property

```

lemma task-getscheduler-local-rsp:
assumes  $p0 : \text{reachable0 } s$ 
and  $p1 : \neg(\text{interference } pid \ s \ d)$ 
and  $p2 : s' = \text{fst}(\text{task-getscheduler } s \ pid \ p)$ 
shows  $s \sim d \sim s'$ 
using  $p2 \ \text{task-getscheduler-def}$ 
by (smt fstI vpeq-reflexive-lemma)

```

```

lemma task-getscheduler-local-rsp-e:
assumes  $p0 : \text{reachable0 } s$ 
and  $p1 : e = \text{TskEvt } ((\text{Event-task-getscheduler } pid \ p))$ 
and  $p2 : \text{non-interference } (\text{the}(\text{domain-of-event } e)) \ s \ d$ 
and  $p3 : s' = \text{exec-event } s \ e$ 
shows  $s \sim d \sim s'$ 
proof –
{
  have  $a0 : (\text{the } (\text{domain-of-event } e)) = pid$ 
    using  $p1 \ \text{domain-of-event-def } \text{getpid-from-tsk-event-def}$  by auto
  have  $a1 : s' = \text{fst}(\text{task-getscheduler } s \ pid \ p)$ 
    using  $p1 \ p3 \ \text{exec-event-def}$  by auto

```



```

    have a2:  $\neg(\text{interference pid } s \ d)$ 
      using p2 a0 non-interference-def
      by blast
    have a3:  $s \sim d \sim s'$ 
      using a1 a2 p0 task-getscheduler-local-rsp by blast
  }
  then show ?thesis
    by fast
qed

```

```

lemma task-getscheduler-dlocal-rsp-e: dynamic-local-respect-e ( $\text{TskEvt } ((\text{Event-task-getscheduler pid } p))$ )
  using dynamic-local-respect-e-def non-interference-def task-getscheduler-local-rsp-e
  by blast

```

29.24.14 proving "task_movememory" satisfying the "local respect" property

```

lemma task-movememory-local-rsp:
  assumes p0: reachable0 s
    and p1:  $\neg(\text{interference pid } s \ d)$ 
    and p2:  $s' = \text{fst}(\text{task-movememory } s \ \text{pid } p)$ 
  shows  $s \sim d \sim s'$ 
  using p2 task-movememory-def
  by (smt fstI vpeq-reflexive-lemma)

```

```

lemma task-movememory-local-rsp-e:
  assumes p0 : reachable0 s
    and p1:  $e = \text{TskEvt } ((\text{Event-task-movememory pid } p))$ 
    and p2: non-interference (the(domain-of-event e)) s d
    and p3:  $s' = \text{exec-event } s \ e$ 
  shows  $s \sim d \sim s'$ 
  proof -
  {
    have a0: (the (domain-of-event e)) = pid
      using p1 domain-of-event-def getpid-from-tsk-event-def by auto
    have a1:  $s' = \text{fst}(\text{task-movememory } s \ \text{pid } p)$ 
      using p1 p3 exec-event-def by auto
    have a2:  $\neg(\text{interference pid } s \ d)$ 
      using p2 a0 non-interference-def
      by blast
    have a3:  $s \sim d \sim s'$ 
      using a1 a2 p0 task-movememory-local-rsp by blast
  }
  then show ?thesis
    by fast
qed

```

```

lemma task-movememory-dlocal-rsp-e: dynamic-local-respect-e ( $\text{TskEvt } ((\text{Event-task-movememory pid } p))$ )

```

```

using task-movememory-local-rsp-e dynamic-local-respect-e-def non-interference-def
by blast

```

29.24.15 proving "task_{kill}" satisfying the "local respect" property

```

lemma task-kill-local-rsp:
  assumes p0: reachable0 s
    and p1:  $\neg(\text{interference } pid \ s \ d)$ 
    and p2:  $s' = fst(\text{task-kill } s \ pid \ p \ sinfo \ i \ c)$ 
  shows  $s \sim d \sim s'$ 
  using p2 task-kill-def
  by (smt fstI vpeq-reflexive-lemma)

lemma task-kill-local-rsp-e:
  assumes p0 : reachable0 s
    and p1:  $e = TskEvt \ ((Event\text{-}task\text{-}kill \ pid \ p \ sinfo \ i \ c))$ 
    and p2: non-interference (the(domain-of-event e)) s d
    and p3:  $s' = exec\text{-}event \ s \ e$ 
  shows  $s \sim d \sim s'$ 
  proof -
  {
    have a0: (the (domain-of-event e)) = pid
      using p1 domain-of-event-def getpid-from-tsk-event-def by auto
    have a1:  $s' = fst(\text{task-kill } s \ pid \ p \ sinfo \ i \ c)$ 
      using p1 p3 exec-event-def by auto
    have a2:  $\neg(\text{interference } pid \ s \ d)$ 
      using p2 a0 non-interference-def
      by blast
    have a3:  $s \sim d \sim s'$ 
      using a1 a2 p0 task-kill-local-rsp by blast
  }
  then show ?thesis
  by fast
qed

```

```

lemma task-kill-dlocal-rsp-e: dynamic-local-respect-e (TskEvt ((Event-task-kill
pid p sinfo i c)))
  using task-kill-local-rsp-e dynamic-local-respect-e-def non-interference-def
  by presburger

```

29.24.16 proving "task_{prctl}" satisfying the "local respect" property

```

lemma task-prctl-local-rsp:
  assumes p0: reachable0 s
    and p1:  $\neg(\text{interference } pid \ s \ d)$ 
    and p2:  $s' = fst(\text{task-prctl } s \ pid \ op \ arg2 \ arg3 \ arg4 \ arg5)$ 
  shows  $s \sim d \sim s'$ 
  using p2 task-prctl-def
  by (smt fst-conv vpeq-reflexive-lemma)

```

```

lemma task-prctl-local-rsp-e:
  assumes  $p0 : \text{reachable0 } s$ 
  and  $p1 : e = \text{TskEvt } ((\text{Event-task-prctl } pid \text{ op } arg2 \text{ arg3 } arg4 \text{ arg5}))$ 
  and  $p2 : \text{non-interference } (the(\text{domain-of-event } e)) \text{ } s \text{ } d$ 
  and  $p3 : s' = \text{exec-event } s \text{ } e$ 
shows  $s \sim d \sim s'$ 
proof –
{
  have  $a0 : (the (\text{domain-of-event } e)) = pid$ 
    using  $p1$  domain-of-event-def getpid-from-tsk-event-def by auto
  have  $a1 : s' = \text{fst}(\text{task-prctl } s \text{ pid op } arg2 \text{ arg3 } arg4 \text{ arg5})$ 
    using  $p1 \text{ } p3$  exec-event-def by auto
  have  $a2 : \neg(\text{interference } pid \text{ } s \text{ } d)$ 
    using  $p2 \text{ } a0$  non-interference-def
    by blast
  have  $a3 : s \sim d \sim s'$ 
    using  $a1 \text{ } a2 \text{ } p0$  task-prctl-local-rsp by blast
}
then show ?thesis
by fast
qed

lemma task-prctl-dlocal-rsp-e: dynamic-local-respect-e
  ( $\text{TskEvt } ((\text{Event-task-prctl } pid \text{ op } arg2 \text{ arg3 } arg4 \text{ arg5}))$ )
using task-prctl-local-rsp-e dynamic-local-respect-e-def non-interference-def
by presburger

```

29.25 smack ptrace hooks local respect proof

29.25.1 proving "ptrace_m may access" satisfying the "local respect" property

```

lemma ptrace-may-access-local-rsp:
  assumes  $p0 : \text{reachable0 } s$ 
  and  $p1 : \neg(\text{interference } pid \text{ } s \text{ } d)$ 
  and  $p2 : s' = \text{fst}(\text{ptrace-may-access } s \text{ pid } p \text{ } m)$ 
shows  $s \sim d \sim s'$ 
proof –
  have  $a1 : s = s'$ 
    by (simp add: p2 ptrace-may-access-def)
  then show ?thesis
    using vpeq-reflexive-lemma by auto
qed

```

```

lemma ptrace-may-access-local-rsp-e:
  assumes  $p0 : \text{reachable0 } s$ 
  and  $p1 : e = \text{PtraceEvt } (\text{Event-ptrace-access-check } pid \text{ } p \text{ } m)$ 
  and  $p2 : \text{non-interference } (the(\text{domain-of-event } e)) \text{ } s \text{ } d$ 
  and  $p3 : s' = \text{exec-event } s \text{ } e$ 
shows  $s \sim d \sim s'$ 

```

```

  proof –
  {
    have a0: (the (domain-of-event e)) = pid
      using p1 domain-of-event-def getpid-from-pttrace-event-def by auto
    have a1: s' = fst(pttrace-may-access s pid p m)
      using p1 p3 exec-event-def by auto
    have a2: ¬(interference pid s d)
      using p2 a0 non-interference-def
      by blast
    have a3: s ~ d ~ s'
      using a1 a2 p0 pttrace-may-access-local-rsp by blast
  }
  then show ?thesis
    by fast
qed

```

```

lemma pttrace-may-access-dlocal-rsp-e: dynamic-local-respect-e (PtraceEvt (Event-pttrace-access-check
pid p m))
  using dynamic-local-respect-e-def pttrace-may-access-local-rsp-e non-interference-def
  by blast

```

29.25.2 proving "pttrace_{traceme}" satisfying the "local respect" property

```

lemma pttrace-traceme-local-rsp:
  assumes p0: reachable0 s
    and p1: ¬(interference pid s d)
    and p2: s' = fst(pttrace-traceme s pid )
  shows s ~ d ~ s'
  proof –
    have a1: s = s'
      by (simp add: p2 pttrace-traceme-def)
    then show ?thesis
      by (simp add: kveq-reflexive-lemma)
  qed

```

```

lemma pttrace-traceme-local-rsp-e:
  assumes p0 : reachable0 s
    and p1: e = PtraceEvt (Event-pttrace-traceme pid )
    and p2: non-interference (the(domain-of-event e)) s d
    and p3: s' = exec-event s e
  shows s ~ d ~ s'
  proof –
  {
    have a0: (the (domain-of-event e)) = pid
      using p1 domain-of-event-def getpid-from-pttrace-event-def by auto
    have a1: s' = fst(pttrace-traceme s pid )
      using p1 p3 exec-event-def by auto
    have a2: ¬(interference pid s d)
      using p2 a0 non-interference-def

```

```

    by blast
  have a3:  $s \sim d \sim s'$ 
    using a1 a2 p0 ptrace-traceme-local-rsp by blast
}
then show ?thesis
  by fast
qed

```

```

lemma ptrace-traceme-dlocal-rsp-e: dynamic-local-respect-e (PtraceEvt (Event-ptrace-traceme
pid ))
  using dynamic-local-respect-e-def ptrace-traceme-local-rsp-e non-interference-def
  by blast

```

29.25.3 proving "prepare_{binprm}" satisfying the "local respect" property

```

lemma prepare-binprm-local-rsp:
  assumes p0: reachable0 s
    and p1:  $\neg(\text{interference pid } s \ d)$ 
    and p2:  $s' = \text{fst}(\text{prepare-binprm } s \ \text{pid } \text{bprm})$ 
  shows  $s \sim d \sim s'$ 
    using p2 prepare-binprm-def
    by (smt fst-conv vpeq-reflexive-lemma)

lemma prepare-binprm-local-rsp-e:
  assumes p0 : reachable0 s
    and p1:  $e = \text{SysEvt}(\text{Event-prepare-binprm pid bprm})$ 
    and p2: non-interference (the(domain-of-event e)) s d
    and p3:  $s' = \text{exec-event } s \ e$ 
  shows  $s \sim d \sim s'$ 
    proof -
    {
      have a0: (the (domain-of-event e)) = pid
        using p1 domain-of-event-def getpid-from-sys-event-def by auto
      have a1:  $s' = \text{fst}(\text{prepare-binprm } s \ \text{pid } \text{bprm})$ 
        using p1 p3 exec-event-def by auto
      have a2:  $\neg(\text{interference pid } s \ d)$ 
        using p2 a0 non-interference-def
        by blast
      have a3:  $s \sim d \sim s'$ 
        using a1 a2 p0 prepare-binprm-local-rsp by blast
    }
    then show ?thesis
      by fast
  qed

```

```

lemma prepare-binprm-dlocal-rsp-e: dynamic-local-respect-e (SysEvt (Event-prepare-binprm
pid bprm) )
  using prepare-binprm-local-rsp-e dynamic-local-respect-e-def non-interference-def

```

by *blast*

29.26 smack file hooks local respect proof

lemma *do-ioctl-detstate*:

$\bigwedge sa . \{\lambda s . s = sa\} \text{ security-file-ioctl } sa \text{ file cmd arg } \{\lambda r s . s = sa\} \longrightarrow$
 $snd \text{ (the-run-state (security-file-ioctl } sa \text{ file cmd arg) } sa) = sa$

apply(*simp add: valid-def*)

apply (*simp add: security-file-ioctl-def the-run-state-def split-def*)

apply *auto*[1]

done

29.26.1 proving "do_{ioctl}" satisfying the "local respect" property

lemma *do-ioctl-local-rsp*:

assumes *p0*: *reachable0 s*

and *p1*: $\neg(\text{interference pid } s \text{ } d)$

and *p2*: $s' = fst(\text{do-ioctl } s \text{ pid file cmd arg})$

shows $s \sim d \sim s'$

proof –

have *a1*: $s = s'$

apply (*simp add: p2 do-ioctl-def*)

using *do-ioctl-detstate fst-conv funcState-def security-file-ioctl-notchgstate*

by *smt*

then show *?thesis*

using *vpeq-reflexive-lemma* by *auto*

qed

lemma *do-ioctl-local-rsp-e*:

assumes *p0* : *reachable0 s*

and *p1*: $e = \text{FileEvt}(\text{Event-do-ioctl pid file cmd arg})$

and *p2*: *non-interference* (*the*(*domain-of-event* *e*)) *s d*

and *p3*: $s' = \text{exec-event } s \text{ } e$

shows $s \sim d \sim s'$

proof –

{

have *a0*: (*the* (*domain-of-event* *e*)) = *pid*

using *p1 domain-of-event-def getpid-from-file-event-def* by *auto*

have *a1*: $s' = fst(\text{do-ioctl } s \text{ pid file cmd arg})$

using *p1 p3 exec-event-def* by *auto*

have *a2*: $\neg(\text{interference pid } s \text{ } d)$

using *p2 a0 non-interference-def*

by *blast*

have *a4*: $s \sim d \sim s'$

using *a1 a2 p0 do-ioctl-local-rsp* by *blast*

}

then show *?thesis*

by *fast*

qed

lemma *do-ioctl-dlocal-rsp-e: dynamic-local-respect-e* (*FileEvt*(*Event-do-ioctl* *pid* *file* *cmd* *arg*))
using *do-ioctl-local-rsp-e dynamic-local-respect-e-def non-interference-def*
by *blast*

29.26.2 proving "syscall_iioctl" satisfying the "local respect" property

lemma *syscall-ioctl-local-rsp:*
assumes *p0: reachable0 s*
and *p1: $\neg(\text{interference } pid \ s \ d)$*
and *p2: $s' = fst(\text{syscall-ioctl } s \ pid \ fd \ cmd \ arg)$*
shows *$s \sim d \sim s'$*
using *p2 syscall-ioctl-def security-file-ioctl-def*
by (*smt fst-conv kvpeq-reflexive-lemma*)

lemma *syscall-ioctl-local-rsp-e:*
assumes *p0 : reachable0 s*
and *p1: $e = \text{FileEvt}(\text{Event-syscall-ioctl } pid \ fd \ cmd \ arg)$*
and *p2: non-interference (the(domain-of-event e)) s d*
and *p3: $s' = \text{exec-event } s \ e$*
shows *$s \sim d \sim s'$*
proof –
{
have *a0: (the (domain-of-event e)) = pid*
using *p1 domain-of-event-def getpid-from-file-event-def* **by** *auto*
have *a1: $s' = fst(\text{syscall-ioctl } s \ pid \ fd \ cmd \ arg)$*
using *p1 p3 exec-event-def* **by** *auto*
have *a2: $\neg(\text{interference } pid \ s \ d)$*
using *p2 a0 non-interference-def*
by *blast*
have *a3: $s \sim d \sim s'$*
using *a1 a2 p0 syscall-ioctl-local-rsp* **by** *blast*
}
then show *?thesis*
by *fast*
qed

lemma *syscall-ioctl-dlocal-rsp-e: dynamic-local-respect-e*(*FileEvt*(*Event-syscall-ioctl* *pid* *fd* *cmd* *arg*))
using *syscall-ioctl-local-rsp-e dynamic-local-respect-e-def non-interference-def*
by *blast*

29.26.3 proving "ksys_iioctl" satisfying the "local respect" property

lemma *ksys-ioctl-local-rsp:*
assumes *p0: reachable0 s*
and *p1: $\neg(\text{interference } pid \ s \ d)$*
and *p2: $s' = fst(\text{ksys-ioctl } s \ pid \ fd \ cmd \ arg)$*

```

shows  $s \sim d \sim s'$ 
using p2 ksys-ioctl-def security-file-ioctl-def
by (smt fst-conv kvpeq-reflexive-lemma)

lemma ksys-ioctl-local-rsp-e:
  assumes p0 : reachable0 s
  and p1:  $e = \text{FileEvt}(\text{Event-ksys-ioctl } pid \text{ fd cmd arg})$ 
  and p2: non-interference (the(domain-of-event e)) s d
  and p3:  $s' = \text{exec-event } s \ e$ 
shows  $s \sim d \sim s'$ 
proof -
{
  have a0: (the (domain-of-event e)) = pid
  using p1 domain-of-event-def getpid-from-file-event-def by auto
  have a1:  $s' = \text{fst}(\text{ksys-ioctl } s \ pid \text{ fd cmd arg})$ 
  using p1 p3 exec-event-def by auto
  have a2:  $\neg(\text{interference } pid \ s \ d)$ 
  using p2 a0 non-interference-def
  by blast
  have a3:  $s \sim d \sim s'$ 
  using a1 a2 p0 ksys-ioctl-local-rsp by blast
}
then show ?thesis
by fast
qed

lemma ksys-ioctl-dlocal-rsp-e: dynamic-local-respect-e( $\text{FileEvt}(\text{Event-ksys-ioctl } pid \text{ fd cmd arg})$ )
using ksys-ioctl-local-rsp-e dynamic-local-respect-e-def non-interference-def
by blast



### 29.26.4 proving "vmmmappgoff" satisfying the "local respect" property



lemma vm-mmap-pgoff-local-rsp:
  assumes p0: reachable0 s
  and p1:  $\neg(\text{interference } pid \ s \ d)$ 
  and p2:  $s' = \text{fst}(\text{vm-mmap-pgoff } s \ pid \text{ file addr len' prot flag pgoff})$ 
shows  $s \sim d \sim s'$ 
using p2 vm-mmap-pgoff-def security-mmap-file-def fst-conv kvpeq-reflexive-lemma
by metis

lemma vm-mmap-pgoff-local-rsp-e:
  assumes p0 : reachable0 s
  and p1:  $e = \text{FileEvt}(\text{Event-vm-mmap-pgoff } pid \text{ file addr len' prot flag pgoff})$ 
  and p2: non-interference (the(domain-of-event e)) s d
  and p3:  $s' = \text{exec-event } s \ e$ 
shows  $s \sim d \sim s'$ 
proof -
{

```



```

have a0: (the (domain-of-event e)) = pid
  using p1 domain-of-event-def getpid-from-file-event-def by auto
have a1: s' = fst(vm-mmap-pgoff s pid file addr len' prot flag pgoff)
  using p1 p3 exec-event-def by auto
have a2: ¬(interference pid s d)
  using p2 a0 non-interference-def
  by blast
have a3: s ~ d ~ s'
  using a1 a2 p0 vm-mmap-pgoff-local-rsp by blast
}
then show ?thesis
  by fast
qed

```

```

lemma vm-mmap-pgoff-dlocal-rsp-e: dynamic-local-respect-e(FileEvt( Event-vm-mmap-pgoff
pid file addr len' prot flag pgoff ))
  using vm-mmap-pgoff-local-rsp-e dynamic-local-respect-e-def non-interference-def

  by presburger

```

29.26.5 proving "do_{sys}vm86" satisfying the "local respect" property

```

lemma do-sys-vm86-local-rsp:
  assumes p0: reachable0 s
    and p1: ¬(interference pid s d)
    and p2: s' = fst(do-sys-vm86 s pid)
  shows s ~ d ~ s'
  using p2 do-sys-vm86-def security-mmap-addr-def
  by (smt fst-conv kvpeq-reflexive-lemma)

```

```

lemma do-sys-vm86-local-rsp-e:
  assumes p0 : reachable0 s
    and p1: e = FileEvt( Event-do-sys-vm86 pid )
    and p2: non-interference (the(domain-of-event e)) s d
    and p3: s' = exec-event s e
  shows s ~ d ~ s'
  proof -
  {
    have a0: (the (domain-of-event e)) = pid
      using p1 domain-of-event-def getpid-from-file-event-def by auto
    have a1: s' = fst(do-sys-vm86 s pid)
      using p1 p3 exec-event-def by auto
    have a2: ¬(interference pid s d)
      using p2 a0 non-interference-def
      by blast
    have a3: s ~ d ~ s'
      using a1 a2 p0 do-sys-vm86-local-rsp by blast
  }
  then show ?thesis

```

by fast
qed

lemma *do-sys-vm86-dlocal-rsp-e*: *dynamic-local-respect-e*(*FileEvt*(*Event-do-sys-vm86* *pid*))
 using *do-sys-vm86-local-rsp-e* *dynamic-local-respect-e-def* *non-interference-def*
 by blast

29.26.6 proving "get_unmapped_area" satisfying the "local respect" property

lemma *get-unmapped-area-local-rsp*:
 assumes *p0*: *reachable0 s*
 and *p1*: $\neg(\text{interference } pid \ s \ d)$
 and *p2*: $s' = fst(\text{get-unmapped-area } s \ pid \ file \ addr)$
 shows $s \sim d \sim s'$
 using *p2* *get-unmapped-area-def* *security-mmap-addr-def*
 by (smt fst-conv kvpeq-reflexive-lemma)

lemma *get-unmapped-area-local-rsp-e*:
 assumes *p0*: *reachable0 s*
 and *p1*: $e = \text{FileEvt}(\text{Event-get-unmapped-area } pid \ file \ addr)$
 and *p2*: *non-interference* (*the*(*domain-of-event* *e*)) *s* *d*
 and *p3*: $s' = \text{exec-event } s \ e$
 shows $s \sim d \sim s'$
 proof –
 {
 have *a0*: (*the* (*domain-of-event* *e*)) = *pid*
 using *p1* *domain-of-event-def* *getpid-from-file-event-def* by auto
 have *a1*: $s' = fst(\text{get-unmapped-area } s \ pid \ file \ addr)$
 using *p1* *p3* *exec-event-def* by auto
 have *a2*: $\neg(\text{interference } pid \ s \ d)$
 using *p2* *a0* *non-interference-def*
 by blast
 have *a3*: $s \sim d \sim s'$
 using *a1* *a2* *p0* *get-unmapped-area-local-rsp* by blast
 }
 then show ?thesis
 by fast
 qed

lemma *get-unmapped-area-dlocal-rsp-e*: *dynamic-local-respect-e*(*FileEvt*(*Event-get-unmapped-area* *pid* *file* *addr*))
 using *get-unmapped-area-local-rsp-e* *dynamic-local-respect-e-def* *non-interference-def*
 by blast

29.26.7 proving "validate_mmap_rrequest" satisfying the "local respect" property

lemma *validate-mmap-request-local-rsp*:
 assumes *p0*: *reachable0 s*

```

    and p1:  $\neg(\text{interference pid } s \ d)$ 
    and p2:  $s' = \text{fst}(\text{validate-mmap-request } s \ \text{pid} \ \text{file} \ \text{addr})$ 
shows  $s \sim d \sim s'$ 
using p2 validate-mmap-request-def security-mmap-addr-def
by (smt fst-conv kveq-reflexive-lemma)

lemma validate-mmap-request-local-rsp-e:
  assumes p0 : reachable0 s
  and p1:  $e = \text{FileEvt}(\text{Event-validate-mmap-request pid file addr})$ 
  and p2: non-interference (the(domain-of-event e)) s d
  and p3:  $s' = \text{exec-event } s \ e$ 
shows  $s \sim d \sim s'$ 
proof -
{
  have a0: (the (domain-of-event e)) = pid
    using p1 domain-of-event-def getpid-from-file-event-def by auto
  have a1:  $s' = \text{fst}(\text{validate-mmap-request } s \ \text{pid} \ \text{file} \ \text{addr})$ 
    using p1 p3 exec-event-def by auto
  have a2:  $\neg(\text{interference pid } s \ d)$ 
    using p2 a0 non-interference-def
    by blast
  have a3:  $s \sim d \sim s'$ 
    using a1 a2 p0 validate-mmap-request-local-rsp by blast
}
then show ?thesis
  by fast
qed

```

```

lemma validate-mmap-request-dlocal-rsp-e: dynamic-local-respect-e( FileEvt( Event-validate-mmap-request
pid file addr))
  using validate-mmap-request-local-rsp-e dynamic-local-respect-e-def non-interference-def

  by blast

```

29.26.8 proving "generic_ssetlease" satisfying the "localrespect" property

```

lemma generic-setlease-local-rsp:
  assumes p0: reachable0 s
  and p1:  $\neg(\text{interference pid } s \ d)$ 
  and p2:  $s' = \text{fst}(\text{generic-setlease } s \ \text{pid} \ \text{file} \ \text{arg})$ 
shows  $s \sim d \sim s'$ 
using p2 generic-setlease-def security-file-lock-def
by (smt fst-conv kveq-reflexive-lemma)

```

```

lemma generic-setlease-local-rsp-e:
  assumes p0 : reachable0 s
  and p1:  $e = \text{FileEvt}(\text{Event-generic-setlease pid file arg})$ 
  and p2: non-interference (the(domain-of-event e)) s d
  and p3:  $s' = \text{exec-event } s \ e$ 

```

```

shows  $s \sim d \sim s'$ 
proof -
{
  have a0: (the (domain-of-event e)) = pid
    using p1 domain-of-event-def getpid-from-file-event-def by auto
  have a1:  $s' = \text{fst}(\text{generic-setlease } s \text{ pid file arg})$ 
    using p1 p3 exec-event-def by auto
  have a2:  $\neg(\text{interference pid } s \text{ d})$ 
    using p2 a0 non-interference-def
    by blast
  have a3:  $s \sim d \sim s'$ 
    using a1 a2 p0 generic-setlease-local-rsp by blast
}
then show ?thesis
  by fast
qed

```

```

lemma generic-setlease-dlocal-rsp-e: dynamic-local-respect-e (FileEvt (Event-generic-setlease
pid file arg))
  using generic-setlease-local-rsp-e dynamic-local-respect-e-def non-interference-def

  by blast

```

29.26.9 proving "syscall_{lock}" satisfying the "local respect" property

```

lemma syscall-lock-local-rsp:
  assumes p0: reachable0 s
    and p1:  $\neg(\text{interference pid } s \text{ d})$ 
    and p2:  $s' = \text{fst}(\text{syscall-lock } s \text{ pid fd cmd})$ 
  shows  $s \sim d \sim s'$ 
  using p2 syscall-lock-def security-file-lock-def
  by (smt fst-conv kvpeq-reflexive-lemma)

```

```

lemma syscall-lock-local-rsp-e:
  assumes p0 : reachable0 s
    and p1:  $e = \text{FileEvt}(\text{Event-syscall-lock pid fd cmd})$ 
    and p2: non-interference (the (domain-of-event e)) s d
    and p3:  $s' = \text{exec-event } s \text{ e}$ 
  shows  $s \sim d \sim s'$ 
  proof -
  {
    have a0: (the (domain-of-event e)) = pid
      using p1 domain-of-event-def getpid-from-file-event-def by auto
    have a1:  $s' = \text{fst}(\text{syscall-lock } s \text{ pid fd cmd})$ 
      using p1 p3 exec-event-def by auto
    have a2:  $\neg(\text{interference pid } s \text{ d})$ 
      using p2 a0 non-interference-def
      by blast
    have a3:  $s \sim d \sim s'$ 

```

```

    using a1 a2 p0 syscall-lock-local-rsp by blast
  }
  then show ?thesis
    by fast
qed

```

```

lemma syscall-lock-dlocal-rsp-e: dynamic-local-respect-e(FileEvt( Event-syscall-lock
pid fd cmd ))
  using syscall-lock-local-rsp-e dynamic-local-respect-e-def non-interference-def
  by blast

```

29.26.10 proving "do_{lock}file_{wait}" satisfying the "local respect" property

```

lemma do-lock-file-wait-local-rsp:
  assumes p0: reachable0 s
    and p1: ¬(interference pid s d)
    and p2: s' = fst(do-lock-file-wait s pid file cmd fl)
  shows s ~ d ~ s'
  using p2 do-lock-file-wait-def security-file-lock-def
  by (smt fst-conv kvpeq-reflexive-lemma)

```

```

lemma do-lock-file-wait-local-rsp-e:
  assumes p0 : reachable0 s
    and p1: e = FileEvt( Event-do-lock-file-wait pid file cmd fl )
    and p2: non-interference (the(domain-of-event e)) s d
    and p3: s' = exec-event s e
  shows s ~ d ~ s'
  proof -
  {
    have a0: (the (domain-of-event e)) = pid
      using p1 domain-of-event-def getpid-from-file-event-def by auto
    have a1: s' = fst(do-lock-file-wait s pid file cmd fl)
      using p1 p3 exec-event-def by auto
    have a2: ¬(interference pid s d)
      using p2 a0 non-interference-def
      by blast
    have a4: s ~ d ~ s'
      using a1 a2 p0 do-lock-file-wait-local-rsp by blast
  }
  then show ?thesis
    by fast
qed

```

```

lemma do-lock-file-wait-dlocal-rsp-e: dynamic-local-respect-e(FileEvt( Event-do-lock-file-wait
pid file cmd fl))
  using do-lock-file-wait-local-rsp-e dynamic-local-respect-e-def non-interference-def

  by blast

```

29.26.11 proving "file_{fcntl}" satisfying the "local respect" property

lemma *file-fcntl-local-rsp*:

assumes $p0$: *reachable0* s
and $p1$: $\neg(\text{interference } pid \ s \ d)$
and $p2$: $s' = \text{fst}(\text{file-fcntl } s \ pid \ \text{file } cmd \ arg)$
shows $s \sim d \sim s'$
using $p2$ *file-fcntl-def security-file-lock-def*
by (*smt fst-conv kvpeq-reflexive-lemma*)

lemma *file-fcntl-local-rsp-e*:

assumes $p0$: *reachable0* s
and $p1$: $e = \text{FileEvt}(\text{Event-file-fcntl } pid \ \text{file } cmd \ arg)$
and $p2$: *non-interference* (*the*(*domain-of-event* e)) $s \ d$
and $p3$: $s' = \text{exec-event } s \ e$
shows $s \sim d \sim s'$
proof –
{
have $a0$: (*the* (*domain-of-event* e)) = pid
using $p1$ *domain-of-event-def getpid-from-file-event-def* **by** *auto*
have $a1$: $s' = \text{fst}(\text{file-fcntl } s \ pid \ \text{file } cmd \ arg)$
using $p1 \ p3$ *exec-event-def* **by** *auto*
have $a2$: $\neg(\text{interference } pid \ s \ d)$
using $p2 \ a0$ *non-interference-def*
by *blast*
have $a3$: $s \sim d \sim s'$
using $a1 \ a2 \ p0$ *file-fcntl-local-rsp* **by** *blast*
}
then show *?thesis*
by *fast*
qed

lemma *file-fcntl-dlocal-rsp-e*: *dynamic-local-respect-e*(*FileEvt*(*Event-file-fcntl* pid *file* cmd arg))
using *file-fcntl-local-rsp-e dynamic-local-respect-e-def non-interference-def*
by *blast*

29.26.12 proving "file_{send-sigiotask}" satisfying the "local respect" property

lemma *file-send-sigiotask-local-rsp*:

assumes $p0$: *reachable0* s
and $p1$: $\neg(\text{interference } pid \ s \ d)$
and $p2$: $s' = \text{fst}(\text{file-send-sigiotask } s \ pid \ t \ fown \ sig)$
shows $s \sim d \sim s'$
using $p2$ *file-send-sigiotask-def security-file-send-sigiotask-def*
by (*smt fst-conv kvpeq-reflexive-lemma*)

lemma *file-send-sigiotask-local-rsp-e*:

assumes $p0$: *reachable0* s
and $p1$: $e = \text{FileEvt}(\text{Event-file-send-sigiotask } pid \ t \ fown \ sig)$

```

    and p2:non-interference (the(domain-of-event e)) s d
    and p3: s' = exec-event s e
shows   s ~ d ~ s'
proof -
{
  have a0: (the (domain-of-event e)) = pid
    using p1 domain-of-event-def getpid-from-file-event-def by auto
  have a1: s' = fst(file-send-sigiotask s pid t fown sig)
    using p1 p3 exec-event-def by auto
  have a2: ¬(interference pid s d)
    using p2 a0 non-interference-def
    by blast
  have a3: s ~ d ~ s'
    using a1 a2 p0 file-send-sigiotask-local-rsp by blast
}
then show ?thesis
  by fast
qed

```

```

lemma file-send-sigiotask-dlocal-rsp-e: dynamic-local-respect-e(FileEvt(Event-file-send-sigiotask
pid t fown sig))
  using file-send-sigiotask-local-rsp-e dynamic-local-respect-e-def non-interference-def

  by blast

```

29.26.13 proving "file_rceive" satisfying the "local respect" property

```

lemma file-recv-local-rsp:
  assumes p0: reachable0 s
    and p1: ¬(interference pid s d)
    and p2: s' = fst(file-recv s pid f)
  shows   s ~ d ~ s'
  using p2 file-recv-def security-file-recv-def
  by (smt fst-conv kvpeq-reflexive-lemma)

```

```

lemma file-recv-local-rsp-e:
  assumes p0 : reachable0 s
    and p1: e = FileEvt (Event-file-recv pid f)
    and p2:non-interference (the(domain-of-event e)) s d
    and p3: s' = exec-event s e
  shows   s ~ d ~ s'
  proof -
  {
    have a0: (the (domain-of-event e)) = pid
      using p1 domain-of-event-def getpid-from-file-event-def by auto
    have a1: s' = fst(file-recv s pid f)
      using p1 p3 exec-event-def by auto
    have a2: ¬(interference pid s d)
      using p2 a0 non-interference-def

```

```

    by blast
  have a3:  $s \sim d \sim s'$ 
    using a1 a2 p0 file-receive-local-rsp by blast
}
then show ?thesis
  by fast
qed

```

```

lemma file-receive-dlocal-rsp-e: dynamic-local-respect-e( FileEvt( Event-file-receive
pid f))
  using file-receive-local-rsp-e dynamic-local-respect-e-def non-interference-def
  by blast

```

29.26.14 proving "do_{dentry}open" satisfying the "local respect" property

```

lemma do-dentry-open-local-rsp:
  assumes p0: reachable0 s
    and p1:  $\neg(\text{interference pid s d})$ 
    and p2:  $s' = \text{fst}(\text{do-dentry-open s pid f})$ 
  shows  $s \sim d \sim s'$ 
  using p2 do-dentry-open-def security-file-open-def
  by (smt fst-conv kvpeq-reflexive-lemma)

```

```

lemma do-dentry-open-local-rsp-e:
  assumes p0: reachable0 s
    and p1:  $e = \text{FileEvt}(\text{Event-do-dentry-open pid f})$ 
    and p2: non-interference (the(domain-of-event e)) s d
    and p3:  $s' = \text{exec-event s e}$ 
  shows  $s \sim d \sim s'$ 
  proof -
  {
    have a0: (the (domain-of-event e)) = pid
      using p1 domain-of-event-def getpid-from-file-event-def by auto
    have a1:  $s' = \text{fst}(\text{do-dentry-open s pid f})$ 
      using p1 p3 exec-event-def by auto
    have a2:  $\neg(\text{interference pid s d})$ 
      using p2 a0 non-interference-def
      by blast
    have a3:  $s \sim d \sim s'$ 
      using a1 a2 p0 do-dentry-open-local-rsp by blast
  }
  then show ?thesis
    by fast
qed

```

```

lemma do-dentry-open-dlocal-rsp-e: dynamic-local-respect-e( FileEvt( Event-do-dentry-open
pid f))
  using do-dentry-open-local-rsp-e dynamic-local-respect-e-def non-interference-def

```


by *blast*

29.27 smack ipc hooks local respect proof

29.27.1 proving "ipcperms" satisfying the "local respect" property

lemma *ipcperms-local-rsp*:

$\llbracket \text{reachable0 } s; \neg(\text{interference } \text{pid } s \ d); s' = \text{fst}(\text{ipcperms } s \ \text{pid } \text{ipcp } \text{flg}) \rrbracket$
 $\implies (s \sim d \sim s')$

using *ipcperms-def security-ipc-permission-def*

by (*smt fst-conv kvpeq-reflexive-lemma*)

lemma *ipcperms-local-rsp-e*:

assumes *p0* : *reachable0 s*

and *p1*: *e = KIpEvt((Event-ipc-permission pid ipcp flg))*

and *p2*: *non-interference (the(domain-of-event e)) s d*

and *p3*: *s' = exec-event s e*

shows *s ~ d ~ s'*

proof –

{

have *a0*: *(the (domain-of-event e)) = pid*

using *p1 domain-of-event-def getpid-from-kern-ipc-event-def* by *auto*

have *a1*: *s' = fst(ipcperms s pid ipcp flg)*

using *p1 p3 exec-event-def* by *auto*

have *a2*: $\neg(\text{interference } \text{pid } s \ d)$

using *p2 a0 non-interference-def*

by *blast*

have *a3*: *s ~ d ~ s'*

using *a1 a2 p0 ipcperms-local-rsp* by *blast*

}

then show *?thesis*

by *fast*

qed

lemma *ipcperms-dlocal-rsp-e*: *dynamic-local-respect-e(KIpEvt((Event-ipc-permission pid ipcp flg)))*

using *ipcperms-local-rsp-e dynamic-local-respect-e-def non-interference-def*

by *blast*

29.27.2 proving "audit_{ipcobj}" satisfying the "local respect" property

lemma *audit-ipc-obj-local-rsp*:

$\llbracket \text{reachable0 } s; \neg(\text{interference } \text{pid } s \ d); s' = \text{fst}(\text{audit-ipc-obj } s \ \text{pid } \text{ipcp}) \rrbracket \implies (s \sim d \sim s')$

using *audit-ipc-obj-def security-ipc-getsecid-def*

by (*simp add: kvpeq-reflexive-lemma*)

lemma *audit-ipc-obj-local-rsp-e*:

assumes *p0* : *reachable0 s*

```

and p1: e = KIpEvt((Event-ipc-getsecid pid ipcp) )
and p2: non-interference (the(domain-of-event e)) s d
and p3: s' = exec-event s e
shows s ~ d ~ s'
proof –
{
  have a0: (the (domain-of-event e)) = pid
    using p1 domain-of-event-def getpid-from-kern-ipc-event-def by auto
  have a1: s' = fst(audit-ipc-obj s pid ipcp)
    using p1 p3 exec-event-def by auto
  have a2: ¬(interference pid s d)
    using p2 a0 non-interference-def
    by blast
  have a3: s ~ d ~ s'
    using a1 a2 p0 audit-ipc-obj-local-rsp by blast
}
then show ?thesis
by fast
qed

```

```

lemma audit-ipc-obj-dlocal-rsp-e: dynamic-local-respect-e(KIpEvt(( Event-ipc-getsecid
pid ipcp )))
using audit-ipc-obj-local-rsp-e dynamic-local-respect-e-def non-interference-def
by blast

```

29.27.3 proving "ksys_msgget" satisfying the "local respect" property

```

lemma ksys-msgget-local-rsp: [[reachable0 s; ¬(interference pid s d); s' = fst(ksys-msgget
s pid msq msqflg)]]
⇒ (s ~ d ~ s')
using ksys-msgget-def security-msg-queue-associate-def
by (simp add: kvpeq-reflexive-lemma)

```

```

lemma ksys-msgget-local-rsp-e:
assumes p0 : reachable0 s
and p1: e = KIpEvt( (Event-msg-queue-associate pid msq msqflg) )
and p2: non-interference (the(domain-of-event e)) s d
and p3: s' = exec-event s e
shows s ~ d ~ s'
proof –
{
  have a0: (the (domain-of-event e)) = pid
    using p1 domain-of-event-def getpid-from-kern-ipc-event-def by auto
  have a1: s' = fst(ksys-msgget s pid msq msqflg)
    using p1 p3 exec-event-def by auto
  have a2: ¬(interference pid s d)
    using p2 a0 non-interference-def
    by blast
  have a3: s ~ d ~ s'

```

```

    using a1 a2 p0 ksys-msgget-local-rsp by blast
  }
  then show ?thesis
    by fast
qed

```

```

lemma ksys-msgget-dlocal-rsp-e: dynamic-local-respect-e(KIpcEvt( (Event-msg-queue-associate
pid msq msqflg)))
  using ksys-msgget-local-rsp-e dynamic-local-respect-e-def non-interference-def
  by blast

```

29.27.4 proving "msg_{queue}msgctl" satisfying the "local respect" property

```

lemma msg-queue-msgctl-local-rsp:
  [[reachable0 s; ¬(interference pid s d); s' = fst(msg-queue-msgctl s pid msq cmd)]]
    ⇒ (s ~ d ~ s')
  using msg-queue-msgctl-def security-msg-queue-msgctl-def
  by (simp add: kvpeq-reflexive-lemma)

```

```

lemma msg-queue-msgctl-local-rsp-e:
  assumes p0 : reachable0 s
    and p1: e = KIpcEvt((Event-msg-queue-msgctl pid msq cmd ))
    and p2: non-interference (the(domain-of-event e)) s d
    and p3: s' = exec-event s e
  shows s ~ d ~ s'
  proof -
  {
    have a0: (the (domain-of-event e)) = pid
      using p1 domain-of-event-def getpid-from-kern-ipc-event-def by auto
    have a1: s' = fst(msg-queue-msgctl s pid msq cmd)
      using p1 p3 exec-event-def by auto
    have a2: ¬(interference pid s d)
      using p2 a0 non-interference-def
      by blast
    have a3: s ~ d ~ s'
      using a1 a2 p0 msg-queue-msgctl-local-rsp by blast
  }
  then show ?thesis
    by fast
qed

```

```

lemma msg-queue-msgctl-dlocal-rsp-e: dynamic-local-respect-e(KIpcEvt((Event-msg-queue-msgctl
pid msq cmd)))
  using msg-queue-msgctl-local-rsp-e dynamic-local-respect-e-def non-interference-def

  by blast

```

29.27.5 proving "do_{msgsnd}" satisfying the "local respect" property

```

lemma do-msgsnd-local-rsp:

```

```

assumes p0: reachable0 s
  and p1:  $\neg(\text{interference pid s d})$ 
  and p2:  $s' = \text{fst}(\text{do-msgsnd s pid msq msg msgflg})$ 
shows  $s \sim d \sim s'$ 
using p2 do-msgsnd-def security-msg-queue-msgsnd-def
proof –
  have  $\forall s n k m i. \text{do-msgsnd s n k m i} =$ 
     $(\text{if resultValue s (security-msg-queue-msgsnd s k m i)} = 0$ 
      then  $(s, 0)$ 
      else
         $(s, \text{resultValue s (security-msg-queue-msgsnd s k m i)}))$ 
    by (simp add: do-msgsnd-def)
  then have  $\text{do-msgsnd s pid msq msg msgflg} =$ 
     $(s, \text{resultValue s (security-msg-queue-msgsnd s msq msg msgflg)})$ 
    by presburger
  then show ?thesis
    using p2
    by (simp add: kvpeq-reflexive-lemma)
qed

```

```

lemma do-msgsnd-local-rsp-e:
  assumes p0 : reachable0 s
  and p1:  $e = \text{KIpcEvt}(\text{Event-msg-queue-msgsnd pid msq msg msgflg})$ 
  and p2: non-interference (the(domain-of-event e)) s d
  and p3:  $s' = \text{exec-event s e}$ 
shows  $s \sim d \sim s'$ 
proof –
  {
    have  $a0: (\text{the (domain-of-event e)}) = \text{pid}$ 
      using p1 domain-of-event-def getpid-from-kern-ipc-event-def by auto
    have  $a1: s' = \text{fst}(\text{do-msgsnd s pid msq msg msgflg})$ 
      using p1 p3 exec-event-def by auto
    have  $a2: \neg(\text{interference pid s d})$ 
      using p2 a0 non-interference-def
      by blast
    have  $a3: s \sim d \sim s'$ 
      using a1 a2 p0 do-msgsnd-local-rsp by blast
  }
  then show ?thesis
    by fast
qed

```

```

lemma do-msgsnd-dlocal-rsp-e: dynamic-local-respect-e( KIpcEvt( Event-msg-queue-msgsnd
  pid msq msg msgflg)))
  using do-msgsnd-local-rsp-e dynamic-local-respect-e-def non-interference-def
  by blast

```

29.27.6 proving "msg_queue_msgrcv" satisfying the "localrespect" property

lemma *msg-queue-msgrcv-local-rsp*:

$\llbracket \text{reachable0 } s; \neg(\text{interference } \text{pid } s \ d); s' = \text{fst}(\text{msg-queue-msgrcv } s \ \text{pid } \text{isp } \text{msq } p \ \text{long } \text{msqflg}) \rrbracket$
 $\implies (s \sim d \sim s')$
using *msg-queue-msgrcv-def security-msg-queue-msgrcv-def*
by (*smt fst-conv kvpeq-reflexive-lemma*)

lemma *msg-queue-msgrcv-local-rsp-e*:

assumes *p0*: *reachable0 s*
and *p1*: *e = KIpEvt((Event-msg-queue-msgrcv pid isp msq p long msqflg))*
and *p2*: *non-interference (the(domain-of-event e)) s d*
and *p3*: *s' = exec-event s e*
shows *s ~ d ~ s'*
proof –
{
 have *a0*: *(the (domain-of-event e)) = pid*
 using *p1 domain-of-event-def getpid-from-kern-ipc-event-def* **by** *auto*
 have *a1*: *s' = fst(msg-queue-msgrcv s pid isp msq p long msqflg)*
 using *p1 p3 exec-event-def* **by** *auto*
 have *a2*: *¬(interference pid s d)*
 using *p2 a0 non-interference-def*
 by *blast*
 have *a3*: *s ~ d ~ s'*
 using *a1 a2 p0 msg-queue-msgrcv-local-rsp* **by** *blast*
}
then show *?thesis*
by *fast*
qed

lemma *msg-queue-msgrcv-dlocal-rsp-e*: *dynamic-local-respect-e(KIpEvt((Event-msg-queue-msgrcv pid isp msq p long msqflg)))*

using *msg-queue-msgrcv-local-rsp-e dynamic-local-respect-e-def non-interference-def*

by *presburger*

29.27.7 proving "ksys_shmget" satisfying the "localrespect" property

lemma *ksys-shmget-local-rsp*:

assumes *p0*: *reachable0 s*
and *p1*: *¬(interference pid s d)*
and *p2*: *s' = fst(ksys-shmget s pid shm shmflg)*
shows *s ~ d ~ s'*
using *p2 ksys-shmget-def*
by (*simp add: kvpeq-reflexive-lemma*)

lemma *ksys-shmget-local-rsp-e*:

assumes *p0*: *reachable0 s*
and *p1*: *e = KIpEvt((Event-shm-associate pid shm shmflg))*

```

    and p2:non-interference (the(domain-of-event e)) s d
    and p3: s' = exec-event s e
shows   s ~ d ~ s'
proof -
{
  have a0: (the (domain-of-event e)) = pid
    using p1 domain-of-event-def getpid-from-kern-ipc-event-def by auto
  have a1: s' = fst(ksys-shmget s pid shm shmflg)
    using p1 p3 exec-event-def by auto
  have a2: ¬(interference pid s d)
    using p2 a0 non-interference-def
    by blast
  have a3: s ~ d ~ s'
    using a1 a2 p0 ksys-shmget-local-rsp by blast
}
then show ?thesis
  by fast
qed

```

```

lemma ksys-shmget-dlocal-rsp-e: dynamic-local-respect-e(KIpcEvt( ( Event-shm-associate
pid shm shmflg )))
  using ksys-shmget-local-rsp-e dynamic-local-respect-e-def non-interference-def
  by blast

```

29.27.8 proving "sem_{msgctl}" satisfying the "localrespect" property

```

lemma sem-msgctl-local-rsp:
  assumes p0: reachable0 s
    and p1: ¬(interference pid s d)
    and p2: s' = fst(sem-msgctl s pid sem cmd)
  shows   s ~ d ~ s'
  using p2 sem-msgctl-def security-sem-semctl-def
  by (simp add: kvpeq-reflexive-lemma)

```

```

lemma sem-msgctl-local-rsp-e:
  assumes p0 :reachable0 s
    and p1: e = KIpcEvt( (Event-sem-semctl pid sem cmd ))
    and p2:non-interference (the(domain-of-event e)) s d
    and p3: s' = exec-event s e
  shows   s ~ d ~ s'
  proof -
  {
    have a0: (the (domain-of-event e)) = pid
      using p1 domain-of-event-def getpid-from-kern-ipc-event-def by auto
    have a1: s' = fst(sem-msgctl s pid sem cmd)
      using p1 p3 exec-event-def by auto
    have a2: ¬(interference pid s d)
      using p2 a0 non-interference-def
      by blast
  }

```

```

    have a3:  $s \sim d \sim s'$ 
    using a1 a2 p0 sem-msgctl-local-rsp by blast
  }
  then show ?thesis
  by fast
qed

```

```

lemma sem-msgctl-dlocal-rsp-e: dynamic-local-respect-e( $KIpcEvt$ ( ( $Event-sem-semctl$ 
pid sem cmd )))
  using sem-msgctl-local-rsp-e dynamic-local-respect-e-def non-interference-def
  by blast

```

29.27.9 proving " $do_{semtimedop}$ " satisfying the "local respect" property

```

lemma do-semtimedop-local-rsp:
  assumes p0: reachable0 s
    and p1:  $\neg(interference\ pid\ s\ d)$ 
    and p2:  $s' = fst(do-semtimedop\ s\ pid\ sma\ sops\ nsops\ alter')$ 
  shows  $s \sim d \sim s'$ 
  using p2 do-semtimedop-def
  by (smt fstI kveq-reflexive-lemma)

```

```

lemma do-semtimedop-local-rsp-e:
  assumes p0 : reachable0 s
    and p1:  $e = KIpcEvt$ ( ( $Event-sem-semop\ pid\ sma\ sops\ nsops\ alter'$ ))
    and p2: non-interference (the(domain-of-event e)) s d
    and p3:  $s' = exec-event\ s\ e$ 
  shows  $s \sim d \sim s'$ 
  proof -
  {
    have a0: (the (domain-of-event e)) = pid
      using p1 domain-of-event-def getpid-from-kern-ipc-event-def by auto
    have a1:  $s' = fst(do-semtimedop\ s\ pid\ sma\ sops\ nsops\ alter')$ 
      using p1 p3 exec-event-def by auto
    have a2:  $\neg(interference\ pid\ s\ d)$ 
      using p2 a0 non-interference-def
      by blast
    have a3:  $s \sim d \sim s'$ 
      using a1 a2 p0 do-semtimedop-local-rsp by blast
  }
  then show ?thesis
  by fast
qed

```

```

lemma do-semtimedop-dlocal-rsp-e: dynamic-local-respect-e( $KIpcEvt$ ( ( $Event-sem-semop$ 
pid sma sops nsops alter'))))
  using do-semtimedop-local-rsp-e dynamic-local-respect-e-def non-interference-def
  by metis

```

29.27.10 proving "do_{shmat}" satisfying the "localrespect" property

```

lemma do-shmat-local-rsp:
  assumes p0: reachable0 s
    and p1:  $\neg(\text{interference } pid \ s \ d)$ 
    and p2:  $s' = fst(\text{do-shmat } s \ pid \ shp \ shmaddr \ shmflg)$ 
  shows  $s \sim d \sim s'$ 
  proof-
    have a1:  $s = s'$ 
      apply (simp add: p2 do-shmat-def)
      by (smt fst-conv)
    then show ?thesis
      by (simp add: kvpeq-reflexive-lemma)
  qed

lemma do-shmat-local-rsp-e:
  assumes p0 : reachable0 s
    and p1:  $e = KIpEvt( (Event-shm-shmat \ pid \ shp \ shmaddr \ shmflg) )$ 
    and p2: non-interference (the(domain-of-event e)) s d
    and p3:  $s' = exec-event \ s \ e$ 
  shows  $s \sim d \sim s'$ 
  proof -
    {
      have a0: (the (domain-of-event e)) = pid
        using p1 domain-of-event-def getpid-from-kern-ipc-event-def by auto
      have a1:  $s' = fst(\text{do-shmat } s \ pid \ shp \ shmaddr \ shmflg)$ 
        using p1 p3 exec-event-def by auto
      have a2:  $\neg(\text{interference } pid \ s \ d)$ 
        using p2 a0 non-interference-def
        by blast
      have a3:  $s \sim d \sim s'$ 
        using a1 a2 p0 do-shmat-local-rsp by blast
    }
    then show ?thesis
      by fast
  qed

```

```

lemma do-shmat-dlocal-rsp-e: dynamic-local-respect-e( KIpEvt( (Event-shm-shmat
pid shp shmaddr shmflg) ))
  using do-shmat-local-rsp-e dynamic-local-respect-e-def non-interference-def
  by blast

```

29.27.11 proving "ksys_{semget}" satisfying the "localrespect" property

```

lemma ksys-semget-local-rsp:
  assumes p0: reachable0 s
    and p1:  $\neg(\text{interference } pid \ s \ d)$ 
    and p2:  $s' = fst(\text{ksys-semget } s \ pid \ sem \ semflg)$ 
  shows  $s \sim d \sim s'$ 
  using p2 ksys-semget-def

```



```

by (smt fst-conv kvpeq-reflexive-lemma)

lemma ksys-semget-local-rsp-e:
  assumes p0 : reachable0 s
  and p1: e = KIpEvt( (Event-sem-associate pid sem semflg ))
  and p2: non-interference (the(domain-of-event e)) s d
  and p3: s' = exec-event s e
  shows s ~ d ~ s'
  proof -
  {
    have a0: (the (domain-of-event e)) = pid
      using p1 domain-of-event-def getpid-from-kern-ipc-event-def by auto
    have a1: s' = fst(ksys-semget s pid sem semflg)
      using p1 p3 exec-event-def by auto
    have a2: ¬(interference pid s d)
      using p2 a0 non-interference-def
      by blast
    have a3: s ~ d ~ s'
      using a1 a2 p0 ksys-semget-local-rsp by blast
  }
  then show ?thesis
    by fast
qed

lemma ksys-semget-dlocal-rsp-e: dynamic-local-respect-e(KIpEvt( (Event-sem-associate
pid sem semflg )))
  using ksys-semget-local-rsp-e dynamic-local-respect-e-def non-interference-def
  by blast

29.27.12 proving "shmmsgctl" satisfying the "local respect" property

lemma shm-msgctl-local-rsp:
  assumes p0: reachable0 s
  and p1: ¬(interference pid s d)
  and p2: s' = fst(shm-msgctl s pid shm cmd)
  shows s ~ d ~ s'
  using p2 shm-msgctl-def security-shm-shmctl-def
  by (simp add: kvpeq-reflexive-lemma)

lemma shm-msgctl-local-rsp-e:
  assumes p0 : reachable0 s
  and p1: e = KIpEvt( (Event-shm-shmctl pid shm cmd ))
  and p2: non-interference (the(domain-of-event e)) s d
  and p3: s' = exec-event s e
  shows s ~ d ~ s'
  proof -
  {
    have a0: (the (domain-of-event e)) = pid

```

```

    using p1 domain-of-event-def getpid-from-kern-ipc-event-def by auto
    have a1:  $s' = \text{fst}(\text{shm-msgctl } s \text{ pid shm cmd})$ 
    using p1 p3 exec-event-def by auto
    have a2:  $\neg(\text{interference pid } s \text{ d})$ 
    using p2 a0 non-interference-def
    by blast
    have a3:  $s \sim d \sim s'$ 
    using a1 a2 p0 shm-msgctl-local-rsp by blast
  }
  then show ?thesis
  by fast
qed

```

```

lemma shm-msgctl-dlocal-rsp-e: dynamic-local-respect-e(KIpcEvt( ( Event-shm-shmctl
pid shm cmd )))
  using shm-msgctl-local-rsp-e dynamic-local-respect-e-def non-interference-def
  by blast

```

29.28 smack key hooks local respect proof

29.28.1 proving "key_{task}_{permission}" satisfying the "local respect" property

```

lemma key-task-permission-local-rsp:
  assumes p0: reachable0 s
    and p1:  $\neg(\text{interference pid } s \text{ d})$ 
    and p2:  $s' = \text{fst}(\text{key-task-permission } s \text{ pid key-ref cred' perm})$ 
  shows  $s \sim d \sim s'$ 
  using p2 key-task-permission-def security-key-permission-def
  by (simp add: kvpeq-reflexive-lemma)

lemma key-task-permission-local-rsp-e:
  assumes p0 : reachable0 s
    and p1:  $e = \text{KeyEvt}(\text{Event-key-permission pid key-ref cred' perm})$ 
    and p2: non-interference (the(domain-of-event e)) s d
    and p3:  $s' = \text{exec-event } s \text{ e}$ 
  shows  $s \sim d \sim s'$ 
  proof -
  {
    have a0: (the (domain-of-event e)) = pid
      using p1 domain-of-event-def getpid-from-key-event-def by auto
    have a1:  $s' = \text{fst}(\text{key-task-permission } s \text{ pid key-ref cred' perm})$ 
      using p1 p3 exec-event-def by auto
    have a2:  $\neg(\text{interference pid } s \text{ d})$ 
      using p2 a0 non-interference-def
      by blast
    have a3:  $s \sim d \sim s'$ 
      using a1 a2 p0 key-task-permission-local-rsp by blast
  }
  then show ?thesis
  by fast

```

qed

lemma *key-task-permission-dlocal-rsp-e*: *dynamic-local-respect-e*(*KeyEvt*(*Event-key-permission* *pid key-ref cred' perm*))
using *key-task-permission-local-rsp-e dynamic-local-respect-e-def non-interference-def*
by *blast*

29.28.2 proving "keyctl_{get}security" satisfying the "localrespect" property

lemma *keyctl-get-security-local-rsp*:
assumes *p0*: *reachable0 s*
and *p1*: $\neg(\text{interference } pid \ s \ d)$
and *p2*: $s' = fst(\text{keyctl-get-security } s \ pid \ keyid' \ buffer \ buflen)$
shows $s \sim d \sim s'$
using *p2 keyctl-get-security-def security-key-getsecurity-def*
by (*simp add: kvpeq-reflexive-lemma*)

lemma *keyctl-get-security-local-rsp-e*:
assumes *p0*: *reachable0 s*
and *p1*: $e = \text{KeyEvt}(\text{Event-key-getsecurity } pid \ keyid' \ buffer \ buflen)$
and *p2*: *non-interference* (*the*(*domain-of-event e*)) *s d*
and *p3*: $s' = \text{exec-event } s \ e$
shows $s \sim d \sim s'$
proof –
{
have *a0*: (*the* (*domain-of-event e*)) = *pid*
using *p1 domain-of-event-def getpid-from-key-event-def* **by** *auto*
have *a1*: $s' = fst(\text{keyctl-get-security } s \ pid \ keyid' \ buffer \ buflen)$
using *p1 p3 exec-event-def* **by** *auto*
have *a2*: $\neg(\text{interference } pid \ s \ d)$
using *p2 a0 non-interference-def*
by *blast*
have *a3*: $s \sim d \sim s'$
using *a1 a2 p0 keyctl-get-security-local-rsp* **by** *blast*
}
then show *?thesis*
by *fast*

qed

lemma *keyctl-get-security-dlocal-rsp-e*: *dynamic-local-respect-e*(*KeyEvt*(*Event-key-getsecurity* *pid keyid' buffer buflen*))
using *keyctl-get-security-local-rsp-e dynamic-local-respect-e-def non-interference-def*
by *blast*

29.28.3 proving "check_{syslog}permissions" satisfying the "localrespect" property

lemma *check-syslog-permissions-local-rsp*:
assumes *p0*: *reachable0 s*

```

    and p1:  $\neg(\text{interference } pid \ s \ d)$ 
    and p2:  $s' = fst(\text{check-syslog-permissions } s \ pid \ t)$ 
shows  $s \sim d \sim s'$ 
using p2 check-syslog-permissions-def
by (smt fst-conv vpeq-reflexive-lemma)

lemma check-syslog-permissions-local-rsp-e:
  assumes p0 : reachable0 s
  and p1:  $e = SysEvt(\text{Event-smack-syslog } pid \ t)$ 
  and p2: non-interference (the(domain-of-event e)) s d
  and p3:  $s' = exec-event \ s \ e$ 
shows  $s \sim d \sim s'$ 
proof -
{
  have a0: (the (domain-of-event e)) = pid
    using p1 domain-of-event-def getpid-from-sys-event-def by auto
  have a1:  $s' = fst(\text{check-syslog-permissions } s \ pid \ t)$ 
    using p1 p3 exec-event-def by auto
  have a2:  $\neg(\text{interference } pid \ s \ d)$ 
    using p2 a0 non-interference-def
    by blast
  have a3:  $s \sim d \sim s'$ 
    using a1 a2 p0 check-syslog-permissions-local-rsp by blast
}
then show ?thesis
  by fast
qed

```

```

lemma check-syslog-permissions-dlocal-rsp-e: dynamic-local-respect-e (SysEvt( Event-smack-syslog
pid t ))
  using check-syslog-permissions-local-rsp-e dynamic-local-respect-e-def non-interference-def

  by blast

```

29.29 smack audit hooks local respect proof

29.29.1 proving "audit_{data to entry}" satisfying the "local respect" property

```

lemma audit-data-to-entry-local-rsp:
  assumes p0: reachable0 s
  and p1:  $\neg(\text{interference } pid \ s \ d)$ 
  and p2:  $s' = fst(\text{audit-data-to-entry } s \ pid)$ 
shows  $s \sim d \sim s'$ 
using p2 audit-data-to-entry-def security-audit-rule-init-def
by (smt fst-conv kvpeq-reflexive-lemma)

```

```

lemma audit-data-to-entry-local-rsp-e:
  assumes p0 : reachable0 s
  and p1:  $e = AuditEvt(\text{Event-audit-data-to-entry } pid)$ 
  and p2: non-interference (the(domain-of-event e)) s d

```

```

    and p3: s' = exec-event s e
shows   s ~ d ~ s'
proof -
{
  have a0: (the (domain-of-event e)) = pid
    using p1 domain-of-event-def getpid-from-aduit-evevt-def by auto
  have a1: s' = fst(audit-data-to-entry s pid )
    using p1 p3 exec-event-def by auto
  have a2: ¬(interference pid s d)
    using p2 a0 non-interference-def
    by blast
  have a3: s ~ d ~ s'
    using a1 a2 p0 audit-data-to-entry-local-rsp by blast
}
then show ?thesis
  by fast
qed

```

```

lemma audit-data-to-entry-dlocal-rsp-e: dynamic-local-respect-e(AuditEvt(Event-audit-data-to-entry
pid))
using audit-data-to-entry-local-rsp-e dynamic-local-respect-e-def non-interference-def

by blast

```

29.29.2 proving "audit_{dupe_lsm_field}" satisfying the "local respect" property

```

lemma audit-dupe-lsm-field-local-rsp:
assumes p0: reachable0 s
and p1: ¬(interference pid s d)
and p2: s' = fst(audit-dupe-lsm-field s pid df sf)
shows   s ~ d ~ s'
proof -
  have a1: s = s'
    apply (simp add: p2 audit-dupe-lsm-field-def )
    by (smt eq-fst-iff)
  then show ?thesis
    using vpeq-reflexive-lemma by auto
qed

```

```

lemma audit-dupe-lsm-field-local-rsp-e:
assumes p0 : reachable0 s
and p1: e = AuditEvt( Event-audit-dupe-lsm-field pid df sf)
and p2: non-interference (the(domain-of-event e)) s d
and p3: s' = exec-event s e
shows   s ~ d ~ s'
proof -
{
  have a0: (the (domain-of-event e)) = pid
    using p1 domain-of-event-def getpid-from-aduit-evevt-def by auto

```

```

    have a1:  $s' = fst(audit-dupe-lsm-field\ s\ pid\ df\ sf)$ 
      using p1 p3 exec-event-def by auto
    have a2:  $\neg(interference\ pid\ s\ d)$ 
      using p2 a0 non-interference-def
      by blast
    have a3:  $s \sim d \sim s'$ 
      using a1 a2 p0 audit-dupe-lsm-field-local-rsp by blast
  }
  then show ?thesis
    by fast
qed

```

```

lemma audit-dupe-lsm-field-dlocal-rsp-e: dynamic-local-respect-e(AuditEvt( Event-audit-dupe-lsm-field
pid df sf) )
  using audit-dupe-lsm-field-local-rsp-e dynamic-local-respect-e-def non-interference-def

  by blast

```

29.29.3 proving "update_{lsm,rule}" satisfying the "local respect" property

```

lemma update-lsm-rule-local-rsp:
  assumes p0: reachable0 s
    and p1:  $\neg(interference\ pid\ s\ d)$ 
    and p2:  $s' = fst(update-lsm-rule\ s\ pid\ krule)$ 
  shows  $s \sim d \sim s'$ 
  using p2 update-lsm-rule-def security-audit-rule-known-def
  by (simp add: kvpeq-reflexive-lemma)

```

```

lemma update-lsm-rule-local-rsp-e:
  assumes p0 : reachable0 s
    and p1:  $e = AuditEvt( Event-audit-rule-known\ pid\ krule)$ 
    and p2: non-interference (the(domain-of-event e)) s d
    and p3:  $s' = exec-event\ s\ e$ 
  shows  $s \sim d \sim s'$ 
  proof -
  {
    have a0: (the (domain-of-event e)) = pid
      using p1 domain-of-event-def getpid-from-aduit-evevt-def by auto
    have a1:  $s' = fst(update-lsm-rule\ s\ pid\ krule)$ 
      using p1 p3 exec-event-def by auto
    have a2:  $\neg(interference\ pid\ s\ d)$ 
      using p2 a0 non-interference-def
      by blast
    have a3:  $s \sim d \sim s'$ 
      using a1 a2 p0 update-lsm-rule-local-rsp by blast
  }
  then show ?thesis
    by fast
qed

```

lemma *update-lsm-rule-dlocal-rsp-e: dynamic-local-respect-e*(*AuditEvt*(*Event-audit-rule-known* *pid krule*))
using *update-lsm-rule-local-rsp-e dynamic-local-respect-e-def non-interference-def*
by *blast*

29.29.4 proving "audit_{rule_m}match" satisfying the "local respect" property

lemma *audit-rule-match-local-rsp:*
assumes *p0: reachable0 s*
and *p1: $\neg(\text{interference } pid \ s \ d)$*
and *p2: $s' = fst(\text{audit-rule-match } s \ pid \ sid)$*
shows *$s \sim d \sim s'$*
using *p2 audit-rule-match-def security-audit-rule-match-def*
by (*metis fstI kvpeq-reflexive-lemma*)

lemma *audit-rule-match-local-rsp-e:*
assumes *p0 : reachable0 s*
and *p1: $e = \text{AuditEvt}(\text{Event-audit-rule-match } pid \ sid)$*
and *p2: non-interference (the(domain-of-event e)) s d*
and *p3: $s' = \text{exec-event } s \ e$*
shows *$s \sim d \sim s'$*
proof –
{
have *a0: (the (domain-of-event e)) = pid*
using *p1 domain-of-event-def getpid-from-aduit-evevt-def* **by** *auto*
have *a1: $s' = fst(\text{audit-rule-match } s \ pid \ sid)$*
using *p1 p3 exec-event-def* **by** *auto*
have *a2: $\neg(\text{interference } pid \ s \ d)$*
using *p2 a0 non-interference-def*
by *blast*
have *a3: $s \sim d \sim s'$*
using *a1 a2 p0 audit-rule-match-local-rsp* **by** *blast*
}
then show *?thesis*
by *fast*
qed

lemma *audit-rule-match-dlocal-rsp-e: dynamic-local-respect-e*(*AuditEvt*(*Event-audit-rule-match* *pid sid*))
using *audit-rule-match-local-rsp-e dynamic-local-respect-e-def non-interference-def*
by *blast*

29.29.5 proving "audit_{free_{lsm}}field" satisfying the "local respect" property

lemma *audit-free-lsm-field-local-rsp:*
assumes *p0: reachable0 s*
and *p1: $\neg(\text{interference } pid \ s \ d)$*

```

    and p2: s' = fst(audit-free-lsm-field s pid f)
  shows s ~ d ~ s'
  using p2 audit-free-lsm-field-def kvpeq-reflexive-lemma
  by auto

```

```

lemma audit-free-lsm-field-local-rsp-e:
  assumes p0 : reachable0 s
  and p1: e = AuditEvt( Event-audit-rule-free pid f)
  and p2: non-interference (the(domain-of-event e)) s d
  and p3: s' = exec-event s e
  shows s ~ d ~ s'
  proof -
  {
    have a0: (the (domain-of-event e)) = pid
      using p1 domain-of-event-def getpid-from-audit-event-def by auto
    have a1: s' = fst(audit-free-lsm-field s pid f)
      using p1 p3 exec-event-def by auto
    have a2: ¬(interference pid s d)
      using p2 a0 non-interference-def
      by blast
    have a3: s ~ d ~ s'
      using a1 a2 p0 audit-free-lsm-field-local-rsp by blast
  }
  then show ?thesis
    by fast
qed

```

```

lemma audit-free-lsm-field-dlocal-rsp-e: dynamic-local-respect-e(AuditEvt( Event-audit-rule-free
pid f))
  using audit-free-lsm-field-local-rsp-e dynamic-local-respect-e-def non-interference-def

  by blast

```

29.30 smack socket hooks local respect proof

29.30.1 proving "unix_sstream_cconnect" satisfying the "local respect" property

```

lemma unix-stream-connect-local-rsp:
  assumes p0: reachable0 s
  and p1: ¬(interference pid s d)
  and p2: s' = fst(unix-stream-connect s pid sock uaddr addr-len flags')
  shows s ~ d ~ s'
  using p2 unix-stream-connect-def
  by (smt fst-conv kvpeq-reflexive-lemma)

```

```

lemma unix-stream-connect-local-rsp-e:
  assumes p0 : reachable0 s
  and p1: e = SocketEvt(Event-unix-stream-connect pid sock uaddr addr-len

```



```

flags')
  and p2:non-interference (the(domain-of-event e)) s d
  and p3: s' = exec-event s e
shows s ~ d ~ s'
proof -
{
  have a0: (the (domain-of-event e)) = pid
    using p1 domain-of-event-def getpid-from-socket-event-def by auto
  have a1: s' = fst(unix-stream-connect s pid sock uaddr addr-len flags')
    using p1 p3 exec-event-def by auto
  have a2: ¬(interference pid s d)
    using p2 a0 non-interference-def
    by blast
  have a3: s ~ d ~ s'
    using a1 a2 p0 unix-stream-connect-local-rsp by blast
}
then show ?thesis
  by fast
qed

```

```

lemma unix-stream-connect-dlocal-rsp-e: dynamic-local-respect-e(SocketEvt( Event-unix-stream-connect
pid sock uaddr addr-len flags'))
  using unix-stream-connect-local-rsp-e dynamic-local-respect-e-def non-interference-def

  by presburger

```

29.30.2 proving "unix_{dgram}connect" satisfying the "local respect" property

```

lemma unix-dgram-connect-local-rsp:
  assumes p0: reachable0 s
  and p1: ¬(interference pid s d)
  and p2: s' = fst(unix-dgram-connect s pid sock uaddr alen flags')
shows s ~ d ~ s'
  using p2 unix-dgram-connect-def security-unix-may-send-def
proof -
  have fst (unix-dgram-connect s pid sock uaddr alen flags') = s
    using unix-dgram-connect-def by auto
  then show ?thesis
    by (metis p2 kwpq-reflexive-lemma)
qed

```

```

lemma unix-dgram-connect-local-rsp-e:
  assumes p0: reachable0 s
  and p1: e = SocketEvt( Event-unix-dgram-connect pid sock uaddr alen flags'
)
  and p2:non-interference (the(domain-of-event e)) s d
  and p3: s' = exec-event s e
shows s ~ d ~ s'

```

```

proof –
{
  have a0: (the (domain-of-event e)) = pid
    using p1 domain-of-event-def getpid-from-socket-evevt-def by auto
  have a1: s' = fst(unix-dgram-connect s pid sock uaddr alen flags')
    using p1 p3 exec-event-def by auto
  have a2: ¬(interference pid s d)
    using p2 a0 non-interference-def
    by blast
  have a3: s ~ d ~ s'
    using a1 a2 p0 unix-dgram-connect-local-rsp by blast
}
then show ?thesis
by fast
qed

```

lemma *unix-dgram-connect-dlocal-rsp-e*: *dynamic-local-respect-e*(SocketEvt(*Event-unix-dgram-connect* *pid* *sock* *uaddr* *alen* *flags'*))
using *unix-dgram-connect-local-rsp-e* *dynamic-local-respect-e-def* *non-interference-def*
by *presburger*

29.30.3 proving "unix_{dgram}_sendmsg" satisfying the "localrespect" property

lemma *unix-dgram-sendmsg-local-rsp*:
assumes *p0*: *reachable0* *s*
and *p1*: ¬(interference *pid* *s* *d*)
and *p2*: *s'* = fst(unix-dgram-sendmsg *s* *pid* *sock* *uaddr* *alen*)
shows *s* ~ *d* ~ *s'*
using *p2* *unix-dgram-sendmsg-def*
by (*metis* *fst-conv* *kupeq-reflexive-lemma*)

lemma *unix-dgram-sendmsg-local-rsp-e*:
assumes *p0*: *reachable0* *s*
and *p1*: *e* = SocketEvt(*Event-unix-dgram-sendmsg* *pid* *sock* *uaddr* *alen*)
and *p2*: *non-interference* (the(domain-of-event *e*)) *s* *d*
and *p3*: *s'* = *exec-event* *s* *e*
shows *s* ~ *d* ~ *s'*
proof –
{
 have *a0*: (the (domain-of-event *e*)) = *pid*
using *p1* domain-of-event-def getpid-from-socket-evevt-def **by** *auto*
have *a1*: *s'* = fst(unix-dgram-sendmsg *s* *pid* *sock* *uaddr* *alen*)
 using *p1* *p3* exec-event-def **by** *auto*
have *a2*: ¬(interference *pid* *s* *d*)
 using *p2* *a0* non-interference-def
 by *blast*
have *a3*: *s* ~ *d* ~ *s'*
using *a1* *a2* *p0* *unix-dgram-sendmsg-local-rsp* **by** *blast*
}

```

}
then show ?thesis
  by fast
qed

```

```

lemma unix-dgram-sendmsg-dlocal-rsp-e: dynamic-local-respect-e(SocketEvt( Event-unix-dgram-sendmsg
pid sock uaddr alen))
  using unix-dgram-sendmsg-local-rsp-e dynamic-local-respect-e-def non-interference-def

  by blast

```

29.30.4 proving "sys_{bind}'" satisfying the "local respect" property

```

lemma sys-bind'-local-rsp:
  assumes p0: reachable0 s
    and p1:  $\neg(\text{interference } pid \ s \ d)$ 
    and p2:  $s' = fst(\text{sys-bind}' \ s \ pid \ fd \ umyaddr \ addrlen)$ 
  shows  $s \sim d \sim s'$ 
  using p2 sys-bind'-def security-socket-bind-def
proof -
  show ?thesis
    by (metis (lifting) fstI p2 sys-bind'-def kveq-reflexive-lemma)
qed

```

```

lemma sys-bind'-local-rsp-e:
  assumes p0 : reachable0 s
    and p1:  $e = \text{SocketEvt}( \text{Event-sys-bind}' \ pid \ fd \ umyaddr \ addrlen )$ 
    and p2: non-interference (the(domain-of-event e)) s d
    and p3:  $s' = \text{exec-event } s \ e$ 
  shows  $s \sim d \sim s'$ 
  proof -
  {
    have a0: (the (domain-of-event e)) = pid
      using p1 domain-of-event-def getpid-from-socket-event-def by auto
    have a1:  $s' = fst(\text{sys-bind}' \ s \ pid \ fd \ umyaddr \ addrlen)$ 
      using p1 p3 exec-event-def by auto
    have a2:  $\neg(\text{interference } pid \ s \ d)$ 
      using p2 a0 non-interference-def
      by blast
    have a3:  $s \sim d \sim s'$ 
      using a1 a2 p0 sys-bind'-local-rsp by blast
  }
  then show ?thesis
    by fast
qed

```

```

lemma sys-bind'-dlocal-rsp-e: dynamic-local-respect-e(SocketEvt( Event-sys-bind'
pid fd umyaddr addrlen ))

```

using *sys-bind'-local-rsp-e* *dynamic-local-respect-e-def* *non-interference-def*
by *blast*

29.30.5 proving "sys_{connect'}" satisfying the "local respect" property

lemma *sys-connect'-local-rsp*:
 assumes *p0*: *reachable0 s*
 and *p1*: $\neg(\text{interference } pid \ s \ d)$
 and *p2*: $s' = fst(\text{sys-connect}' \ s \ pid \ fd \ \text{servaddr} \ \text{addrlen})$
 shows $s \sim d \sim s'$
 using *p2 sys-connect'-def security-socket-connect-def*
 by (*simp add: kvpeq-reflexive-lemma*)

lemma *sys-connect'-local-rsp-e*:
 assumes *p0*: *reachable0 s*
 and *p1*: $e = \text{SocketEvt}(\text{Event-sys-connect}' \ pid \ fd \ \text{servaddr} \ \text{addrlen})$
 and *p2*: *non-interference* (*the*(*domain-of-event* *e*)) *s d*
 and *p3*: $s' = \text{exec-event } s \ e$
 shows $s \sim d \sim s'$
 proof –
 {
 have *a0*: (*the* (*domain-of-event* *e*)) = *pid*
 using *p1 domain-of-event-def getpid-from-socket-event-def* by *auto*
 have *a1*: $s' = fst(\text{sys-connect}' \ s \ pid \ fd \ \text{servaddr} \ \text{addrlen})$
 using *p1 p3 exec-event-def* by *auto*
 have *a2*: $\neg(\text{interference } pid \ s \ d)$
 using *p2 a0 non-interference-def*
 by *blast*
 have *a3*: $s \sim d \sim s'$
 using *a1 a2 p0 sys-connect'-local-rsp* by *blast*
 }
 then show ?*thesis*
 by *fast*
 qed

lemma *sys-connect'-dlocal-rsp-e*: *dynamic-local-respect-e*(*SocketEvt*(*Event-sys-connect'*
pid fd servaddr addrlen))
 using *sys-connect'-local-rsp-e dynamic-local-respect-e-def non-interference-def*
 by *blast*

29.30.6 proving "sock_{sendmsg}" satisfying the "local respect" property

lemma *sock-sendmsg-local-rsp*:
 assumes *p0*: *reachable0 s*
 and *p1*: $\neg(\text{interference } pid \ s \ d)$
 and *p2*: $s' = fst(\text{sock-sendmsg } s \ pid \ \text{sock } \text{msg} \)$
 shows $s \sim d \sim s'$
 using *p2 sock-sendmsg-def*
 by (*simp add: kvpeq-reflexive-lemma*)

```

lemma sock-sendmsg-local-rsp-e:
  assumes p0 :reachable0 s
  and p1: e = SocketEvt( Event-sock-sendmsg pid sock msg )
  and p2:non-interference (the(domain-of-event e)) s d
  and p3: s' = exec-event s e
shows s ~ d ~ s'
proof -
{
  have a0: (the (domain-of-event e)) = pid
    using p1 domain-of-event-def getpid-from-socket-event-def by auto
  have a1: s' = fst(sock-sendmsg s pid sock msg )
    using p1 p3 exec-event-def by auto
  have a2: ¬(interference pid s d)
    using p2 a0 non-interference-def
    by blast
  have a3: s ~ d ~ s'
    using a1 a2 p0 sock-sendmsg-local-rsp by blast
}
then show ?thesis
by fast
qed

```

```

lemma sock-sendmsg-dlocal-rsp-e: dynamic-local-respect-e(SocketEvt( Event-sock-sendmsg
pid sock msg ))
  using sock-sendmsg-local-rsp-e dynamic-local-respect-e-def non-interference-def
by blast

```

29.30.7 proving "sock_recvmsg" satisfying the "localrespect" property

```

lemma sock-recvmsg-local-rsp:
  assumes p0: reachable0 s
  and p1: ¬(interference pid s d)
  and p2: s' = fst(sock-recvmsg s pid sock msg flags')
shows s ~ d ~ s'
using p2 sock-recvmsg-def
by (simp add: kvpeq-reflexive-lemma)

```

```

lemma sock-recvmsg-local-rsp-e:
  assumes p0 :reachable0 s
  and p1: e = SocketEvt( Event-sock-recvmsg pid sock msg flags' )
  and p2:non-interference (the(domain-of-event e)) s d
  and p3: s' = exec-event s e
shows s ~ d ~ s'
proof -
{
  have a0: (the (domain-of-event e)) = pid
    using p1 domain-of-event-def getpid-from-socket-event-def by auto
  have a1: s' = fst(sock-recvmsg s pid sock msg flags')

```

```

    using p1 p3 exec-event-def by auto
  have a2:  $\neg(\text{interference pid } s \ d)$ 
    using p2 a0 non-interference-def
    by blast
  have a3:  $s \sim d \sim s'$ 
    using a1 a2 p0 sock-recvmmsg-local-rsp by blast
}
then show ?thesis
  by fast
qed

```

```

lemma sock-recvmmsg-dlocal-rsp-e: dynamic-local-respect-e( SocketEvt( Event-sock-recvmmsg
pid sock msg flags' ))
  using sock-recvmmsg-local-rsp-e dynamic-local-respect-e-def non-interference-def
  by blast

```

29.30.8 proving "sk-filter-trim-cap" satisfying the "local respect" property

```

lemma sk-filter-trim-cap-local-rsp:
  assumes p0: reachable0 s
    and p1:  $\neg(\text{interference pid } s \ d)$ 
    and p2:  $s' = \text{fst}(\text{sk-filter-trim-cap } s \ \text{pid } \text{sk}' \ \text{skb } \text{cap})$ 
  shows  $s \sim d \sim s'$ 
    using p2 sk-filter-trim-cap-def
    by (simp add: kvpeq-reflexive-lemma)

lemma sk-filter-trim-cap-local-rsp-e:
  assumes p0 : reachable0 s
    and p1:  $e = \text{SocketEvt}(\text{Event-sk-filter-trim-cap pid sk}' \ \text{skb } \text{cap})$ 
    and p2: non-interference (the(domain-of-event e)) s d
    and p3:  $s' = \text{exec-event } s \ e$ 
  shows  $s \sim d \sim s'$ 
    proof -
    {
      have a0: (the (domain-of-event e)) = pid
        using p1 domain-of-event-def getpid-from-socket-event-def by auto
      have a1:  $s' = \text{fst}(\text{sk-filter-trim-cap } s \ \text{pid } \text{sk}' \ \text{skb } \text{cap})$ 
        using p1 p3 exec-event-def by auto
      have a2:  $\neg(\text{interference pid } s \ d)$ 
        using p2 a0 non-interference-def
        by blast
      have a3:  $s \sim d \sim s'$ 
        using a1 a2 p0 sk-filter-trim-cap-local-rsp by blast
    }
  then show ?thesis
    by fast
qed

```

```

lemma sk-filter-trim-cap-dlocal-rsp-e: dynamic-local-respect-e( SocketEvt( Event-sk-filter-trim-cap

```

```

pid sk' skb cap ))
  using sk-filter-trim-cap-local-rsp-e dynamic-local-respect-e-def non-interference-def

  by blast

```

29.30.9 proving "sock_getsockopt" satisfying the "local respect" property

```

lemma sock-getsockopt-local-rsp:
  assumes p0: reachable0 s
    and p1: ¬(interference pid s d)
    and p2: s' = fst(sock-getsockopt s pid sock level' optname optval optlen)
  shows s ~ d ~ s'
proof -
  show ?thesis
  by (metis fst-conv p2 sock-getsockopt-def kvpeq-reflexive-lemma)
qed

```

```

lemma sock-getsockopt-local-rsp-e:
  assumes p0 : reachable0 s
    and p1: e = SocketEvt( Event-sock-getsockopt pid sock level' optname optval
optlen )
    and p2: non-interference (the(domain-of-event e)) s d
    and p3: s' = exec-event s e
  shows s ~ d ~ s'
proof -
  {
    have a0: (the (domain-of-event e)) = pid
      using p1 domain-of-event-def getpid-from-socket-event-def by auto
    have a1: s' = fst(sock-getsockopt s pid sock level' optname optval optlen)
      using p1 p3 exec-event-def by auto
    have a2: ¬(interference pid s d)
      using p2 a0 non-interference-def
      by blast
    have a3: s ~ d ~ s'
      using a1 a2 p0 sock-getsockopt-local-rsp by blast
  }
  then show ?thesis
  by fast
qed

```

```

lemma sock-getsockopt-dlocal-rsp-e: dynamic-local-respect-e( SocketEvt( Event-sock-getsockopt
pid sock level' optname optval optlen ))
  using sock-getsockopt-local-rsp-e dynamic-local-respect-e-def non-interference-def

  by presburger

```

29.30.10 proving "unix_getpeersec_dgram" satisfying the "local respect" property

```

lemma unix-get-peersec-dgram-local-rsp:

```

```

assumes  $p0$ : reachable0  $s$ 
and  $p1$ :  $\neg(\text{interference } pid \ s \ d)$ 
and  $p2$ :  $s' = fst(\text{unix-get-peersec-dgram } s \ pid \ sock \ scm)$ 
shows  $s \sim d \sim s'$ 
using  $p2$  unix-get-peersec-dgram-def
by (smt add: kvpeq-reflexive-lemma)

lemma unix-get-peersec-dgram-local-rsp-e:
assumes  $p0$ : reachable0  $s$ 
and  $p1$ :  $e = \text{SocketEvt}(\text{Event-unix-get-peersec-dgram } pid \ sock \ scm)$ 
and  $p2$ : non-interference (the(domain-of-event  $e$ ))  $s \ d$ 
and  $p3$ :  $s' = \text{exec-event } s \ e$ 
shows  $s \sim d \sim s'$ 
proof –
{
  have  $a0$ : (the (domain-of-event  $e$ )) =  $pid$ 
    using  $p1$  domain-of-event-def getpid-from-socket-event-def by auto
  have  $a1$ :  $s' = fst(\text{unix-get-peersec-dgram } s \ pid \ sock \ scm)$ 
    using  $p1$   $p3$  exec-event-def by auto
  have  $a2$ :  $\neg(\text{interference } pid \ s \ d)$ 
    using  $p2$   $a0$  non-interference-def
    by blast
  have  $a3$ :  $s \sim d \sim s'$ 
    using  $a1$   $a2$   $p0$  unix-get-peersec-dgram-local-rsp by blast
}
then show ?thesis
by fast
qed

```

```

lemma unix-get-peersec-dgram-dlocal-rsp-e: dynamic-local-respect-e( SocketEvt( Event-unix-get-peersec-dgram
 $pid \ sock \ scm$ ))
using unix-get-peersec-dgram-local-rsp-e dynamic-local-respect-e-def non-interference-def

by blast

```

29.31 inode local respect

29.31.1 proving "vfs_{link}" satisfying the "local respect" property

```

lemma vfs-link-local-rsp:
assumes  $p0$ : reachable0  $s$ 
and  $p1$ :  $\neg(\text{interference } pid \ s \ d)$ 
and  $p2$ :  $s' = fst(\text{vfs-link } s \ pid \ old-dentry \ dir \ new-dentry \ delegated-inode)$ 
shows  $s \sim d \sim s'$ 
using  $p2$  vfs-link-def
by (smt fst-conv kvpeq-reflexive-lemma)

```

```

lemma vfs-link-local-rsp-e:
assumes  $p0$ : reachable0  $s$ 
and  $p1$ :  $e = \text{InodeEvt}(\text{Event-vfs-link } pid \ old-dentry \ dir \ new-dentry \ delegated-inode)$ 

```



```

)
  and p2:non-interference (the(domain-of-event e)) s d
  and p3: s' = exec-event s e
shows s ~ d ~ s'
proof -
{
  have a0: (the (domain-of-event e)) = pid
    using p1 domain-of-event-def getpid-from-inode-evevt-def by auto
  have a1: s' = fst(vfs-link s pid old-dentry dir new-dentry delegated-inode)
    using p1 p3 exec-event-def by auto
  have a2: ¬(interference pid s d)
    using p2 a0 non-interference-def
    by blast
  have a3: s ~ d ~ s'
    using a1 a2 p0 vfs-link-local-rsp by blast
}
then show ?thesis
  by fast
qed

```

lemma *vfs-link-dlocal-rsp-e: dynamic-local-respect-e(InodeEvt(Event-vfs-link pid old-dentry dir new-dentry delegated-inode))*
using vfs-link-local-rsp-e dynamic-local-respect-e-def non-interference-def
by presburger

29.31.2 proving "vfs_uunlink" satisfying the "localrespect" property

lemma *vfs-unlink-local-rsp:*
assumes p0: reachable0 s
and p1: ¬(interference pid s d)
and p2: s' = fst(vfs-unlink s pid dir dentry delegated-inode)
shows s ~ d ~ s'
using p2 vfs-unlink-def
by (simp add: kvpeq-reflexive-lemma)

lemma *vfs-unlink-local-rsp-e:*
assumes p0 :reachable0 s
and p1: e = InodeEvt(Event-vfs-unlink pid dir dentry delegated-inode)
and p2:non-interference (the(domain-of-event e)) s d
and p3: s' = exec-event s e
shows s ~ d ~ s'
proof -
{
 have a0: (the (domain-of-event e)) = pid
 using p1 domain-of-event-def getpid-from-inode-evevt-def by auto
 have a1: s' = fst(vfs-unlink s pid dir dentry delegated-inode)
 using p1 p3 exec-event-def by auto
 have a2: ¬(interference pid s d)
 using p2 a0 non-interference-def

```

    by blast
  have a3:  $s \sim d \sim s'$ 
    using a1 a2 p0 vfs-unlink-local-rsp by blast
}
then show ?thesis
  by fast
qed

```

```

lemma vfs-unlink-dlocal-rsp-e: dynamic-local-respect-e(InodeEvt( Event-vfs-unlink
pid dir dentry delegated-inode ))
  using vfs-unlink-local-rsp-e dynamic-local-respect-e-def non-interference-def
  by blast

```

29.31.3 proving "vfs_rmdir" satisfying the "local respect" property

```

lemma vfs-rmdir-local-rsp:
  assumes p0: reachable0 s
    and p1:  $\neg(\text{interference pid s d})$ 
    and p2:  $s' = \text{fst}(\text{vfs-rmdir s pid dir dentry})$ 
  shows  $s \sim d \sim s'$ 
  using p2 vfs-rmdir-def
  by (smt fst-conv kvpeq-reflexive-lemma)

```

```

lemma vfs-rmdir-local-rsp-e:
  assumes p0 : reachable0 s
    and p1:  $e = \text{InodeEvt}(\text{Event-vfs-rmdir pid dir dentry})$ 
    and p2: non-interference (the(domain-of-event e)) s d
    and p3:  $s' = \text{exec-event s e}$ 
  shows  $s \sim d \sim s'$ 
  proof -
  {
    have a0: (the (domain-of-event e)) = pid
      using p1 domain-of-event-def getpid-from-inode-event-def by auto
    have a1:  $s' = \text{fst}(\text{vfs-rmdir s pid dir dentry})$ 
      using p1 p3 exec-event-def by auto
    have a2:  $\neg(\text{interference pid s d})$ 
      using p2 a0 non-interference-def
      by blast
    have a3:  $s \sim d \sim s'$ 
      using a1 a2 p0 vfs-rmdir-local-rsp by blast
  }
  then show ?thesis
    by fast
qed

```

```

lemma vfs-rmdir-dlocal-rsp-e: dynamic-local-respect-e(InodeEvt( Event-vfs-rmdir
pid dir dentry ))
  using vfs-rmdir-local-rsp-e dynamic-local-respect-e-def non-interference-def
  by presburger

```

29.31.4 proving "vfs_rename" satisfying the "localrespect" property

lemma *vfs-rename-local-rsp*:

assumes $p0$: *reachable0 s*
and $p1$: $\neg(\text{interference } pid \ s \ d)$
and $p2$: $s' = \text{fst}(\text{vfs-rename } s \ pid \ \text{old-dir} \ \text{old-dentry} \ \text{new-dir} \ \text{new-dentry} \ \text{delegated-inode} \ \text{flgs})$
shows $s \sim d \sim s'$
using $p2$ *vfs-rename-def*
by (*smt fst-conv kvpeq-reflexive-lemma*)

lemma *vfs-rename-local-rsp-e*:

assumes $p0$: *reachable0 s*
and $p1$: $e = \text{InodeEvt}(\text{Event-vfs-rename } pid \ \text{old-dir} \ \text{old-dentry} \ \text{new-dir} \ \text{new-dentry} \ \text{delegated-inode} \ \text{flgs})$
and $p2$: *non-interference (the(domain-of-event e)) s d*
and $p3$: $s' = \text{exec-event } s \ e$
shows $s \sim d \sim s'$
proof –
{
have $a0$: $(\text{the}(\text{domain-of-event } e)) = pid$
using $p1$ *domain-of-event-def getpid-from-inode-event-def* **by** *auto*
have $a1$: $s' = \text{fst}(\text{vfs-rename } s \ pid \ \text{old-dir} \ \text{old-dentry} \ \text{new-dir} \ \text{new-dentry} \ \text{delegated-inode} \ \text{flgs})$
using $p1 \ p3$ *exec-event-def* **by** *auto*
have $a2$: $\neg(\text{interference } pid \ s \ d)$
using $p2 \ a0$ *non-interference-def*
by *blast*
have $a3$: $s \sim d \sim s'$
using $a1 \ a2 \ p0$ *vfs-rename-local-rsp* **by** *blast*
}
then show *?thesis*
by *fast*
qed

lemma *vfs-rename-dlocal-rsp-e: dynamic-local-respect-e*

$(\text{InodeEvt}(\text{Event-vfs-rename } pid \ \text{old-dir} \ \text{old-dentry} \ \text{new-dir} \ \text{new-dentry} \ \text{delegated-inode} \ \text{flgs}))$
using *vfs-rename-local-rsp-e dynamic-local-respect-e-def non-interference-def*
by *presburger*

29.31.5 proving "inode_permission" satisfying the "localrespect" property

lemma *inode-permission-local-rsp*:

assumes $p0$: *reachable0 s*
and $p1$: $\neg(\text{interference } pid \ s \ d)$
and $p2$: $s' = \text{fst}(\text{inode-permission } s \ pid \ \text{inode } \text{mask})$
shows $s \sim d \sim s'$
using $p2$ *inode-permission-def*
by (*smt fst-conv kvpeq-reflexive-lemma*)

```

lemma inode-permission-local-rsp-e:
  assumes  $p0 : \text{reachable0 } s$ 
  and  $p1 : e = \text{InodeEvt( Event-inode-permission pid inode mask' )}$ 
  and  $p2 : \text{non-interference (the(domain-of-event e)) } s \ d$ 
  and  $p3 : s' = \text{exec-event } s \ e$ 
shows  $s \sim d \sim s'$ 
proof –
{
  have  $a0 : (\text{the (domain-of-event e)}) = \text{pid}$ 
    using  $p1$  domain-of-event-def getpid-from-inode-evevt-def by auto
  have  $a1 : s' = \text{fst(inode-permission } s \ \text{pid inode mask' )}$ 
    using  $p1 \ p3$  exec-event-def by auto
  have  $a2 : \neg(\text{interference pid } s \ d)$ 
    using  $p2 \ a0$  non-interference-def
    by blast
  have  $a3 : s \sim d \sim s'$ 
    using  $a1 \ a2 \ p0$  inode-permission-local-rsp by blast
}
then show ?thesis
by fast
qed

```

```

lemma inode-permission-dlocal-rsp-e: dynamic-local-respect-e(InodeEvt( Event-inode-permission
pid inode mask' ))
using inode-permission-local-rsp-e dynamic-local-respect-e-def non-interference-def

by presburger

```

29.31.6 proving "notify_cchange" satisfying the "local respect" property

```

lemma notify-change-local-rsp:
  assumes  $p0 : \text{reachable0 } s$ 
  and  $p1 : \neg(\text{interference pid } s \ d)$ 
  and  $p2 : s' = \text{fst(notify-change } s \ \text{pid dentry attr' delegated-inode )}$ 
shows  $s \sim d \sim s'$ 
proof –
  show ?thesis
    by (metis fstI notify-change-def p2 kveq-reflexive-lemma)
qed

```

```

lemma notify-change-local-rsp-e:
  assumes  $p0 : \text{reachable0 } s$ 
  and  $p1 : e = \text{InodeEvt( Event-notify-change pid dentry attr' delegated-inode )}$ 
  and  $p2 : \text{non-interference (the(domain-of-event e)) } s \ d$ 
  and  $p3 : s' = \text{exec-event } s \ e$ 
shows  $s \sim d \sim s'$ 
proof –

```

```

{
  have a0: (the (domain-of-event e)) = pid
    using p1 domain-of-event-def getpid-from-inode-event-def by auto
  have a1: s' = fst(notify-change s pid dentry attr' delegated-inode )
    using p1 p3 exec-event-def by auto
  have a2: ¬(interference pid s d)
    using p2 a0 non-interference-def
  by blast
  have a3: s ~ d ~ s'
    using a1 a2 p0 notify-change-local-rsp by blast
}
then show ?thesis
  by fast
qed

```

lemma *notify-change-dlocal-rsp-e: dynamic-local-respect-e(InodeEvt(Event-notify-change pid dentry attr' delegated-inode))*
 using *notify-change-local-rsp-e dynamic-local-respect-e-def non-interference-def*
 by *presburger*

29.31.7 proving "fat_{ioc}tl_{set} attributes" satisfying the "local respect" property

lemma *fat-ioc-tl-set-attributes-local-rsp:*
 assumes *p0: reachable0 s*
 and *p1: ¬(interference pid s d)*
 and *p2: s' = fst(fat-ioc-tl-set-attributes s pid f)*
 shows *s ~ d ~ s'*
 using *p2*
 unfolding *fat-ioc-tl-set-attributes-def*
 by (*metis fstI kvpeq-reflexive-lemma*)

lemma *fat-ioc-tl-set-attributes-local-rsp-e:*
 assumes *p0 : reachable0 s*
 and *p1: e = InodeEvt(Event-fat-ioc-tl-set-attributes pid f)*
 and *p2: non-interference (the(domain-of-event e)) s d*
 and *p3: s' = exec-event s e*
 shows *s ~ d ~ s'*
 proof –
 {
 have a0: (the (domain-of-event e)) = pid
 using p1 domain-of-event-def getpid-from-inode-event-def by auto
 have a1: s' = fst(fat-ioc-tl-set-attributes s pid f)
 using p1 p3 exec-event-def by auto
 have a2: ¬(interference pid s d)
 using p2 a0 non-interference-def
 by blast
 have a3: s ~ d ~ s'
 using a1 a2 p0 fat-ioc-tl-set-attributes-local-rsp by blast
 }

```

}
then show ?thesis
  by fast
qed

```

```

lemma fat-ioctl-set-attributes-dlocal-rsp-e: dynamic-local-respect-e(InodeEvt( Event-fat-ioctl-set-attributes
pid f ))
  using fat-ioctl-set-attributes-local-rsp-e dynamic-local-respect-e-def non-interference-def

  by presburger

```

29.31.8 proving "vfs_getattr" satisfying the "local respect" property

```

lemma vfs-getattr-local-rsp:
  assumes p0: reachable0 s
    and p1:  $\neg(\text{interference pid s d})$ 
    and p2:  $s' = \text{fst}(\text{vfs-getattr s pid path})$ 
  shows  $s \sim d \sim s'$ 
  using p2 vfs-getattr-def
  by (smt fst-conv kvpeq-reflexive-lemma)

```

```

lemma vfs-getattr-local-rsp-e:
  assumes p0 : reachable0 s
    and p1:  $e = \text{InodeEvt}(\text{Event-vfs-getattr pid path})$ 
    and p2: non-interference (the(domain-of-event e)) s d
    and p3:  $s' = \text{exec-event s e}$ 
  shows  $s \sim d \sim s'$ 
  proof -
  {
    have a0: (the (domain-of-event e)) = pid
      using p1 domain-of-event-def getpid-from-inode-event-def by auto
    have a1:  $s' = \text{fst}(\text{vfs-getattr s pid path})$ 
      using p1 p3 exec-event-def by auto
    have a2:  $\neg(\text{interference pid s d})$ 
      using p2 a0 non-interference-def
      by blast
    have a3:  $s \sim d \sim s'$ 
      using a1 a2 p0 vfs-getattr-local-rsp by blast
  }
  then show ?thesis
    by fast
qed

```

```

lemma vfs-getattr-dlocal-rsp-e: dynamic-local-respect-e(InodeEvt( Event-vfs-getattr
pid path ))
  using vfs-getattr-local-rsp-e dynamic-local-respect-e-def non-interference-def
  by presburger

```

29.31.9 proving "vfs_setxattr" satisfying the "local respect" property

lemma *vfs-setxattr-local-rsp*:

assumes *p0*: *reachable0 s*
and *p1*: $\neg(\text{interference } pid \ s \ d)$
and *p2*: $s' = fst(\text{vfs-setxattr } s \ pid \ dentry \ name \ value \ size' \ flgs)$
shows $s \sim d \sim s'$
using *p2* *vfs-setxattr-def*
by (*smt fst-conv kvpeq-reflexive-lemma*)

lemma *vfs-setxattr-local-rsp-e*:

assumes *p0* : *reachable0 s*
and *p1*: $e = \text{InodeEvt}(\ \text{Event-vfs-setxattr } \ pid \ dentry \ name \ value \ size' \ flgs)$
and *p2*: *non-interference* (*the*(*domain-of-event* *e*)) *s d*
and *p3*: $s' = \text{exec-event } s \ e$
shows $s \sim d \sim s'$
proof –
{
have *a0*: (*the* (*domain-of-event* *e*)) = *pid*
using *p1* *domain-of-event-def* *getpid-from-inode-event-def* **by** *auto*
have *a1*: $s' = fst(\text{vfs-setxattr } s \ pid \ dentry \ name \ value \ size' \ flgs)$
using *p1* *p3* *exec-event-def* **by** *auto*
have *a2*: $\neg(\text{interference } pid \ s \ d)$
using *p2* *a0* *non-interference-def*
by *blast*
have *a3*: $s \sim d \sim s'$
using *a1* *a2* *p0* *vfs-setxattr-local-rsp* **by** *blast*
}
then show *?thesis*
by *fast*
qed

lemma *vfs-setxattr-dlocal-rsp-e*: *dynamic-local-respect-e*(*InodeEvt*(*Event-vfs-setxattr* *pid* *dentry* *name* *value* *size'* *flgs*))
using *vfs-setxattr-local-rsp-e* *dynamic-local-respect-e-def* *non-interference-def*
by *presburger*

29.31.10 proving "vfs_sgetxattr" satisfying the "local respect" property

lemma *vfs-getxattr-local-rsp*:

assumes *p0*: *reachable0 s*
and *p1*: $\neg(\text{interference } pid \ s \ d)$
and *p2*: $s' = fst(\text{vfs-getxattr } s \ pid \ dentry \ name \ value \ size')$
shows $s \sim d \sim s'$
using *p2* *vfs-getxattr-def*
by (*smt fst-conv kvpeq-reflexive-lemma*)

lemma *vfs-getxattr-local-rsp-e*:

assumes *p0* : *reachable0 s*
and *p1*: $e = \text{InodeEvt}(\ \text{Event-vfs-getxattr } \ pid \ dentry \ name \ value \ size')$

```

    and p2:non-interference (the(domain-of-event e)) s d
    and p3: s' = exec-event s e
shows   s ~ d ~ s'
proof -
{
  have a0: (the (domain-of-event e)) = pid
    using p1 domain-of-event-def getpid-from-inode-evevt-def by auto
  have a1: s' = fst(vfs-getxattr s pid dentry name value size')
    using p1 p3 exec-event-def by auto
  have a2: ¬(interference pid s d)
    using p2 a0 non-interference-def
    by blast
  have a3: s ~ d ~ s'
    using a1 a2 p0 vfs-getxattr-local-rsp by blast
}
then show ?thesis
  by fast
qed

```

```

lemma vfs-getxattr-dlocal-rsp-e: dynamic-local-respect-e(InodeEvt( Event-vfs-getxattr
pid dentry name value size'))
  using vfs-getxattr-local-rsp-e dynamic-local-respect-e-def non-interference-def
  by presburger

```

29.31.11 proving "vfs_removeattr" satisfying the "local respect" property

```

lemma vfs-removeattr-local-rsp:
  assumes p0: reachable0 s
    and p1: ¬(interference pid s d)
    and p2: s' = fst(vfs-removeattr s pid dentry name)
shows   s ~ d ~ s'
  using p2 vfs-removeattr-def
  by (simp add: kvpeq-reflexive-lemma)

```

```

lemma vfs-removeattr-local-rsp-e:
  assumes p0 : reachable0 s
    and p1: e = InodeEvt( Event-vfs-removeattr pid dentry name )
    and p2:non-interference (the(domain-of-event e)) s d
    and p3: s' = exec-event s e
shows   s ~ d ~ s'
proof -
{
  have a0: (the (domain-of-event e)) = pid
    using p1 domain-of-event-def getpid-from-inode-evevt-def by auto
  have a1: s' = fst(vfs-removeattr s pid dentry name)
    using p1 p3 exec-event-def by auto
  have a2: ¬(interference pid s d)
    using p2 a0 non-interference-def
    by blast
}

```



```

    have a3:  $s \sim d \sim s'$ 
    using a1 a2 p0 vfs-removeattr-local-rsp by blast
  }
  then show ?thesis
  by fast
qed

```

```

lemma vfs-removeattr-dlocal-rsp-e: dynamic-local-respect-e(InodeEvt( Event-vfs-removeattr
pid dentry name ))
  using vfs-removeattr-local-rsp-e dynamic-local-respect-e-def non-interference-def

  by presburger

```

29.31.12 proving "xattr_{getsecurity}" satisfying the "local respect" property

```

lemma xattr-getsecurity-local-rsp:
  assumes p0: reachable0 s
    and p1:  $\neg(\text{interference pid } s \ d)$ 
    and p2:  $s' = \text{fst}(\text{xattr-getsecurity } s \ \text{pid} \ \text{inode name value size})$ 
  shows  $s \sim d \sim s'$ 
  using p2 xattr-getsecurity-def
  by (smt fst-conv kvpeq-reflexive-lemma)

```

```

lemma xattr-getsecurity-local-rsp-e:
  assumes p0 : reachable0 s
    and p1:  $e = \text{InodeEvt}(\text{Event-xattr-getsecurity pid inode name value size})$ 
    and p2: non-interference (the(domain-of-event e)) s d
    and p3:  $s' = \text{exec-event } s \ e$ 
  shows  $s \sim d \sim s'$ 
  proof -
  {
    have a0: (the (domain-of-event e)) = pid
      using p1 domain-of-event-def getpid-from-inode-event-def by auto
    have a1:  $s' = \text{fst}(\text{xattr-getsecurity } s \ \text{pid} \ \text{inode name value size})$ 
      using p1 p3 exec-event-def by auto
    have a2:  $\neg(\text{interference pid } s \ d)$ 
      using p2 a0 non-interference-def
      by blast
    have a3:  $s \sim d \sim s'$ 
      using a1 a2 p0 xattr-getsecurity-local-rsp by blast
  }
  then show ?thesis
  by fast
qed

```

```

lemma xattr-getsecurity-dlocal-rsp-e: dynamic-local-respect-e(InodeEvt( Event-xattr-getsecurity
pid inode name value size'))
  using xattr-getsecurity-local-rsp-e dynamic-local-respect-e-def non-interference-def

```

by presburger

29.31.13 proving "nfs4_listxattr_nf_{s4}label" satisfying the "local respect" property

```

lemma nfs4-listxattr-nfs4-label-local-rsp:
  assumes p0: reachable0 s
    and p1: ¬(interference pid s d)
    and p2: s' = fst(nfs4-listxattr-nfs4-label s pid inode name size')
  shows s ~ d ~ s'
  using p2 nfs4-listxattr-nfs4-label-def
  by (smt fst-conv kvpeq-reflexive-lemma)

lemma nfs4-listxattr-nfs4-label-local-rsp-e:
  assumes p0 : reachable0 s
    and p1: e = InodeEvt( Event-nfs4-listxattr-nfs4-label pid inode name size')
    and p2: non-interference (the(domain-of-event e)) s d
    and p3: s' = exec-event s e
  shows s ~ d ~ s'
  proof -
  {
    have a0: (the (domain-of-event e)) = pid
      using p1 domain-of-event-def getpid-from-inode-event-def by auto
    have a1: s' = fst(nfs4-listxattr-nfs4-label s pid inode name size')
      using p1 p3 exec-event-def by auto
    have a2: ¬(interference pid s d)
      using p2 a0 non-interference-def
      by blast
    have a3: s ~ d ~ s'
      using a1 a2 p0 nfs4-listxattr-nfs4-label-local-rsp by blast
  }
  then show ?thesis
    by fast
qed

```

```

lemma nfs4-listxattr-nfs4-label-dlocal-rsp-e: dynamic-local-respect-e(InodeEvt( Event-nfs4-listxattr-nfs4-label
pid inode name size'))

```

```

  using nfs4-listxattr-nfs4-label-local-rsp-e dynamic-local-respect-e-def non-interference-def

```

by presburger

29.31.14 proving "sockfs_listxattr" satisfying the "local respect" property

```

lemma sockfs-listxattr-local-rsp:
  assumes p0: reachable0 s
    and p1: ¬(interference pid s d)
    and p2: s' = fst(sockfs-listxattr s pid dentry buffer size')
  shows s ~ d ~ s'
  using p2 sockfs-listxattr-def
  by (smt fst-conv kvpeq-reflexive-lemma)

```

```

lemma sockfs-listxattr-local-rsp-e:
  assumes  $p0 : \text{reachable0 } s$ 
  and  $p1 : e = \text{InodeEvt}(\text{Event-sockfs-listxattr } pid \text{ dentry buffer size'})$ 
  and  $p2 : \text{non-interference } (\text{the}(\text{domain-of-event } e)) \ s \ d$ 
  and  $p3 : s' = \text{exec-event } s \ e$ 
shows  $s \sim d \sim s'$ 
proof –
{
  have  $a0 : (\text{the } (\text{domain-of-event } e)) = pid$ 
    using  $p1$  domain-of-event-def getpid-from-inode-event-def by auto
  have  $a1 : s' = \text{fst}(\text{sockfs-listxattr } s \ pid \text{ dentry buffer size'})$ 
    using  $p1 \ p3$  exec-event-def by auto
  have  $a2 : \neg(\text{interference } pid \ s \ d)$ 
    using  $p2 \ a0$  non-interference-def
    by blast
  have  $a3 : s \sim d \sim s'$ 
    using  $a1 \ a2 \ p0$  sockfs-listxattr-local-rsp by blast
}
then show ?thesis
by fast
qed

lemma sockfs-listxattr-dlocal-rsp-e: dynamic-local-respect-e(InodeEvt(Event-sockfs-listxattr
pid dentry buffer size'))
using sockfs-listxattr-local-rsp-e dynamic-local-respect-e-def non-interference-def

by presburger

```

29.31.15 proving the "dynamic local respect" property

```

definition dynamic-local-respect-c :: bool where
  dynamic-local-respect-c  $\equiv \forall e \ d \ s. \text{reachable0 } s$ 
     $\wedge \neg(\text{interference } (\text{the } (\text{domain-of-event } e)) \ s \ d)$ 
     $\longrightarrow (s \sim d \sim (\text{exec-event } s \ e))$ 

```

thm *Event-tsk.induct*

```

theorem dynamic-local-respect:dynamic-local-respect
proof –
{
  fix  $e$ 
  have dynamic-local-respect-e  $e$ 
    apply(induct  $e$ )
  using k-sb-copy-data-dlocal-rsp-e do-remount-dlocal-rsp-e mount-fs-dlocal-rsp-e
k-show-sb-opts-dlocal-rsp-e
sb-statfs-dlocal-rsp-e do-mount-dlocal-rsp-e do-umount-dlocal-rsp-e
pivot-root-dlocal-rsp-e setup-security-options-dlocal-rsp-e set-sb-security-dlocal-rsp-e
nfs-clone-sb-security-dlocal-rsp-e parse-security-options-dlocal-rsp-e
    apply (metis Event-sb.exhaust)
}

```

```

using prepare-creds-dlocal-rsp-e sys-setreuid-dlocal-rsp-e setpgid-dlocal-rsp-e

do-getpgid-dlocal-rsp-e getsid-dlocal-rsp-e getsecid-dlocal-rsp-e
task-setnice-dlocal-rsp-e set-task-ioprio-dlocal-rsp-e
get-task-ioprio-dlocal-rsp-e check-prlimit-permission-dlocal-rsp-e
do-prlimit-dlocal-rsp-e task-scheduler-dlocal-rsp-e
task-scheduler-dlocal-rsp-e task-movememory-dlocal-rsp-e
task-kill-dlocal-rsp-e task-prctl-dlocal-rsp-e
apply (metis Event-tsk.exhaust)
using ptrace-may-access-dlocal-rsp-e ptrace-traceme-dlocal-rsp-e Event-Ptrace.exhaust
apply metis
using check-syslog-permissions-dlocal-rsp-e prepare-binprm-dlocal-rsp-e
apply (metis Event-sys.exhaust)
using do-ioctl-dlocal-rsp-e syscall-ioctl-dlocal-rsp-e
ksys-ioctl-dlocal-rsp-e vm-mmap-pgoff-dlocal-rsp-e do-sys-vm86-dlocal-rsp-e
get-unmapped-area-dlocal-rsp-e
validate-mmap-request-dlocal-rsp-e generic-setlease-dlocal-rsp-e syscall-lock-dlocal-rsp-e

do-lock-file-wait-dlocal-rsp-e file-fcntl-dlocal-rsp-e
file-send-sigiotask-dlocal-rsp-e file-receive-dlocal-rsp-e do-dentry-open-dlocal-rsp-e
apply (metis Event-file.exhaust)
using ipcperms-dlocal-rsp-e audit-ipc-obj-dlocal-rsp-e msg-queue-msgctl-dlocal-rsp-e

do-msgsnd-dlocal-rsp-e msg-queue-msgrcv-dlocal-rsp-e ksys-shmget-dlocal-rsp-e

sem-msgctl-dlocal-rsp-e do-semtimedop-dlocal-rsp-e do-shmat-dlocal-rsp-e

ksys-semget-dlocal-rsp-e shm-msgctl-dlocal-rsp-e ksys-msgget-dlocal-rsp-e
apply (metis Event-ipc.exhaust)
using key-task-permission-dlocal-rsp-e keyctl-get-security-dlocal-rsp-e
apply (metis Event-Key.exhaust)
using audit-data-to-entry-dlocal-rsp-e audit-dupe-lsm-field-dlocal-rsp-e
update-lsm-rule-dlocal-rsp-e
audit-rule-match-dlocal-rsp-e audit-free-lsm-field-dlocal-rsp-e
using Event-audit.exhaust apply metis
using unix-stream-connect-dlocal-rsp-e unix-dgram-connect-dlocal-rsp-e
unix-dgram-sendmsg-dlocal-rsp-e sys-bind'-dlocal-rsp-e
sys-connect'-dlocal-rsp-e sock-sendmsg-dlocal-rsp-e
sock-recvmsg-dlocal-rsp-e sk-filter-trim-cap-dlocal-rsp-e
sock-getsockopt-dlocal-rsp-e unix-get-peersec-dgram-dlocal-rsp-e
apply (metis Event-network-sock.exhaust)
using vfs-link-dlocal-rsp-e vfs-unlink-dlocal-rsp-e vfs-rmdir-dlocal-rsp-e
vfs-rename-dlocal-rsp-e
inode-permission-dlocal-rsp-e notify-change-dlocal-rsp-e fat-ioctl-set-attributes-dlocal-rsp-e

vfs-getattr-dlocal-rsp-e vfs-setxattr-dlocal-rsp-e vfs-getxattr-dlocal-rsp-e
vfs-removexattr-dlocal-rsp-e xattr-getsecurity-dlocal-rsp-e
nfs4-listxattr-nfs4-label-dlocal-rsp-e sockfs-listxattr-dlocal-rsp-e
by (metis Event-inode.exhaust)

```

```

    }
    then show ?thesis
      using dynamic-local-respect-all-evt by blast
  qed

```

29.32 Concrete unwinding condition of "weakly step consistent"

29.33 smack $\text{super}_{\text{lockhooks}} \text{weaklystepconsistent}$

29.33.1 proving " sb_copy_data " satisfying the "weaklystepconsistent" property

```

lemma sb-copy-data-wsc:
  assumes p0: reachable0 s
    and p1: reachable0 t
    and p2:  $s \sim d \sim t$ 
    and p3:  $\text{pid} @ s d$ 
    and p4:  $s \sim \text{pid} \sim t$ 
    and p5:  $s' = \text{fst } (k\text{-sb-copy-data } s \text{ pid})$ 
    and p6:  $t' = \text{fst } (k\text{-sb-copy-data } t \text{ pid})$ 
  shows  $s' \sim d \sim t'$ 
  proof -
  {
    have a0 :  $s = s'$ 
      using p5 k-sb-copy-data-def
      by (smt fstI)
    have a1 :  $t = t'$ 
      using p6 k-sb-copy-data-def
      by (smt fst-conv)
    have a2:  $s' \sim d \sim t'$ 
      using a0 a1 p2
      by blast
  }
  then show ?thesis by auto
qed

```

```

lemma sb-copy-data-wsc-e:
  assumes p0: reachable0 s
    and p1: reachable0 t
    and p2:  $e = \text{SbEvt } (\text{Event-sb-copy-data } \text{pid } sb)$ 
    and p3:  $s \sim d \sim t$ 
    and p4:  $(\text{the } (\text{domain-of-event } e)) @ s d$ 
    and p5:  $s \sim (\text{the } (\text{domain-of-event } e)) \sim t$ 
    and p6:  $s' = \text{exec-event } s e$ 
    and p7:  $t' = \text{exec-event } t e$ 
  shows  $s' \sim d \sim t'$ 
  proof -
  {
    have a0 :  $(\text{the } (\text{domain-of-event } e)) = \text{pid}$ 
      using p2 domain-of-event-def getpid-from-sb-event-def

```

```

    by force
    have a1:  $s' = \text{fst } (k\text{-sb-copy-data } s \text{ pid})$ 
      using p2 p6 exec-event-def by auto
    have a2:  $t' = \text{fst } (k\text{-sb-copy-data } t \text{ pid})$ 
      using p2 p7 exec-event-def by auto
    have a3:  $\text{pid} @ s d$ 
      using p4 a0
    by blast
    have a4:  $s \sim \text{pid} \sim t$  using p5 a0
    by blast
    have a5:  $s' \sim d \sim t'$ 
      using a1 a2 a3 a4 p0 p1 p3 p5 p4 sb-copy-data-wsc
    by blast
  }
  then show ?thesis by auto
qed
lemma sb-copy-data-dwsc-e: dynamic-weakly-step-consistent-e (SbEvt (Event-sb-copy-data
pid sb))
proof -
  {
    have  $\forall d \ s \ t. (\text{reachable0 } s) \wedge (\text{reachable0 } t) \wedge$ 
       $(s \sim d \sim t) \wedge$ 
       $((\text{the } (\text{domain-of-event } (\text{SbEvt } (\text{Event-sb-copy-data } \text{pid } \text{sb})))) @ s \ d) \wedge$ 
       $(s \sim (\text{the } (\text{domain-of-event } (\text{SbEvt } (\text{Event-sb-copy-data } \text{pid } \text{sb})))) \sim t) \longrightarrow$ 
       $((\text{exec-event } s (\text{SbEvt } (\text{Event-sb-copy-data } \text{pid } \text{sb}))) \sim d \sim (\text{exec-event } t$ 
       $(\text{SbEvt } (\text{Event-sb-copy-data } \text{pid } \text{sb}))))$ 
    proof -
      {
        fix d s t
        let ?e = SbEvt (Event-sb-copy-data pid sb)
        assume p2: reachable0 s
        assume p3: reachable0 t
        assume p4:  $s \sim d \sim t$ 
        assume p5:  $(\text{the } (\text{domain-of-event } ?e)) @ s \ d$ 
        assume p6:  $s \sim (\text{the } (\text{domain-of-event } ?e)) \sim t$ 
        have a0:  $(\text{the } (\text{domain-of-event } ?e)) = \text{pid}$ 
          using domain-of-event-def getpid-from-sb-event-def
          by auto
        have  $(\text{exec-event } s \ ?e) \sim d \sim (\text{exec-event } t \ ?e)$ 
          using p2 p3 p4 p5 p6 sb-copy-data-wsc-e
          by blast
      }
    then show ?thesis by blast
  }
qed
then show ?thesis
  using dynamic-weakly-step-consistent-e-def by blast
qed

```

29.33.2 proving "do_remount" satisfying the "weakly step consistent" property

lemma *do-remount-wsc*:

```

assumes p0: reachable0 s
  and p1: reachable0 t
  and p2: s ~ d ~ t
  and p3: pid @ s d
  and p4: s ~ pid ~ t
  and p5: s' = fst(do-remount s p v)
  and p6: t' = fst(do-remount t p v)
shows s' ~ d ~ t'
proof -
{
  have a0 : s = s'
    using p5 do-remount-def
    by simp
  have a1 : t = t'
    using p6 do-remount-def
    by simp
  have a2: s' ~ d ~ t'
    using a0 a1 p2 by blast
}
then show ?thesis by auto
qed

```

lemma *do-remount-wsc-e*:

```

assumes p0: reachable0 s
  and p1: reachable0 t
  and p2: e = SbEvt (Event-sb-remount pid p v)
  and p3: s ~ d ~ t
  and p4: (the (domain-of-event e)) @ s d
  and p5: s ~ (the (domain-of-event e)) ~ t
  and p6: s' = exec-event s e
  and p7: t' = exec-event t e
shows s' ~ d ~ t'
proof -
{
  have a0 : (the (domain-of-event e)) = pid
    using p2 domain-of-event-def getpid-from-sb-event-def
    by force
  have a1: s' = fst(do-remount s p v)
    using p2 p6 exec-event-def by auto
  have a2: t' = fst(do-remount t p v)
    using p2 p7 exec-event-def
    by auto
  have a3: pid @ s d
    using p4 a0
    by blast
  have a4 : s ~ pid ~ t using p5 a0
    by blast
}

```

```

    have a5:  $s' \sim d \sim t'$ 
      using a1 a2 a3 a4 p0 p1 p3 p5 p4 do-remount-wsc
      by blast
  }
  then show ?thesis by auto
qed
lemma do-remount-dwsc-e: dynamic-weakly-step-consistent-e (SbEvt (Event-sb-remount
pid p v))
  using dynamic-weakly-step-consistent-e-def do-remount-wsc-e by blast

```

29.33.3 proving "mount_fs" satisfying the "weakly step consistent" property

```

lemma mount-fs-wsc:
  assumes p0: reachable0 s
    and p1: reachable0 t
    and p2:  $s \sim d \sim t$ 
    and p3: pid @ s d
    and p4:  $s \sim pid \sim t$ 
    and p5:  $s' = fst(mount-fs s ts f name data)$ 
    and p6:  $t' = fst(mount-fs t ts f name data)$ 
  shows  $s' \sim d \sim t'$ 
  proof -
    {
      have a0 :  $s = s'$ 
        using p5 mount-fs-def
        by (smt fstI)
      have a1 :  $t = t'$ 
        using p6 mount-fs-def
        by (smt fstI)
      have a2:  $s' \sim d \sim t'$ 
        using a0 a1 p2 by blast
    }
    then show ?thesis by auto
  qed

lemma mount-fs-wsc-e:
  assumes p0: reachable0 s
    and p1: reachable0 t
    and p2:  $e = SbEvt (Event-sb-kern-mount pid ts f name data)$ 
    and p3:  $s \sim d \sim t$ 
    and p4: (the (domain-of-event e)) @ s d
    and p5:  $s \sim (the (domain-of-event e)) \sim t$ 
    and p6:  $s' = exec-event s e$ 
    and p7:  $t' = exec-event t e$ 
  shows  $s' \sim d \sim t'$ 
  proof -
    {
      have a0 : (the (domain-of-event e)) = pid
        using p2 domain-of-event-def getpid-from-sb-event-def

```



```

    by force
  have a1:  $s' = fst(\text{mount-fs } s \text{ ts } f \text{ name } data)$ 
    using p2 p6 exec-event-def by auto
  have a2:  $t' = fst(\text{mount-fs } t \text{ ts } f \text{ name } data)$ 
    using p2 p7 exec-event-def
    by auto
  have a3:  $pid @ s d$ 
    using p4 a0
    by blast
  have a4 :  $s \sim pid \sim t$  using p5 a0
    by blast
  have a5:  $s' \sim d \sim t'$ 
    using a1 a2 a3 a4 p0 p1 p3 p5 p4 mount-fs-wsc
    by fast
}
then show ?thesis by auto
qed
lemma mount-fs-dwsc-e: dynamic-weakly-step-consistent-e ( SbEvt (Event-sb-kern-mount
pid t f name data ))
  using dynamic-weakly-step-consistent-e-def mount-fs-wsc-e by blast

```

29.33.4 proving "show_{sb-opts}" satisfying the "weakly step consistent" property

```

lemma show-sb-opts-wsc:
  assumes p0: reachable0 s
    and p1: reachable0 t
    and p2:  $s \sim d \sim t$ 
    and p3:  $pid @ s d$ 
    and p4:  $s \sim pid \sim t$ 
    and p5:  $s' = fst(\text{show-sb-opts } s \text{ pid sq sb})$ 
    and p6:  $t' = fst(\text{show-sb-opts } t \text{ pid sq sb})$ 
  shows  $s' \sim d \sim t'$ 
  proof -
  {
    have a0 :  $s = s'$ 
      using p5 show-sb-opts-def
      by simp
    have a1 :  $t = t'$ 
      using p6 show-sb-opts-def
      by simp
    have a2:  $s' \sim d \sim t'$ 
      using a0 a1 p2 by blast
  }
  then show ?thesis by auto
qed

```

```

lemma show-sb-opts-wsc-e:
  assumes p0: reachable0 s

```

```

and p1: reachable0 t
and p2: e = SbEvt (Event-sb-show-options pid sq sb )
and p3: s ~ d ~ t
and p4: (the (domain-of-event e)) @ s d
and p5: s ~ (the (domain-of-event e)) ~ t
and p6: s' = exec-event s e
and p7: t' = exec-event t e
shows s' ~ d ~ t'
proof -
{
  have a0 : (the (domain-of-event e)) = pid
    using p2 domain-of-event-def getpid-from-sb-event-def
    by force
  have a1: s' = fst(show-sb-opts s pid sq sb)
    using p2 p6 exec-event-def by auto
  have a2: t' = fst(show-sb-opts t pid sq sb)
    using p2 p7 exec-event-def
    by auto
  have a3: pid @ s d
    using p4 a0
    by blast
  have a4 : s ~ pid ~ t using p5 a0
    by blast
  have a5: s' ~ d ~ t'
    using a1 a2 a3 a4 p0 p1 p3 p5 p4 show-sb-opts-wsc
    by blast
}
then show ?thesis by auto
qed
lemma show-sb-opts-dwsc-e: dynamic-weakly-step-consistent-e (SbEvt (Event-sb-show-options
pid sq sb ))
  using dynamic-weakly-step-consistent-e-def show-sb-opts-wsc-e by blast

```

29.33.5 proving "statfs_{by_dentry}" satisfying the "weakly step consistent" property

```

lemma statfs-by-dentry-wsc:
assumes p0: reachable0 s
and p1: reachable0 t
and p2: s ~ d ~ t
and p3: pid @ s d
and p4: s ~ pid ~ t
and p5: s' = fst(statfs-by-dentry s pid de)
and p6: t' = fst(statfs-by-dentry t pid de)
shows s' ~ d ~ t'
using p6 p5 p2 statfs-by-dentry-def
by (metis fst-conv)

```

```

lemma statfs-by-dentry-wsc-e:

```

```

assumes  $p0$ : reachable0  $s$ 
  and  $p1$ : reachable0  $t$ 
  and  $p2$ :  $e = \text{SbEvt } (\text{Event-sb-statfs } pid \ de)$ 
  and  $p3$ :  $s \sim d \sim t$ 
  and  $p4$ :  $(\text{the } (\text{domain-of-event } e)) @ s \ d$ 
  and  $p5$ :  $s \sim (\text{the } (\text{domain-of-event } e)) \sim t$ 
  and  $p6$ :  $s' = \text{exec-event } s \ e$ 
  and  $p7$ :  $t' = \text{exec-event } t \ e$ 
shows  $s' \sim d \sim t'$ 
proof –
{
  have  $a0$  :  $(\text{the } (\text{domain-of-event } e)) = pid$ 
    using  $p2$  domain-of-event-def getpid-from-sb-event-def
    by force
  have  $a1$ :  $s' = \text{fst}(\text{statfs-by-dentry } s \ pid \ de)$ 
    using  $p2$   $p6$  exec-event-def by auto
  have  $a2$ :  $t' = \text{fst}(\text{statfs-by-dentry } t \ pid \ de)$ 
    using  $p2$   $p7$  exec-event-def
    by auto
  have  $a3$ :  $pid @ s \ d$ 
    using  $p4$   $a0$ 
    by blast
  have  $a4$  :  $s \sim pid \sim t$  using  $p5$   $a0$ 
    by blast
  have  $a5$ :  $s' \sim d \sim t'$ 
    using  $a1$   $a2$   $a3$   $a4$   $p0$   $p1$   $p3$   $p5$   $p4$  statfs-by-dentry-wsc
    by blast
}
then show ?thesis by auto
qed

lemma statfs-by-dentry-dwsc-e: dynamic-weakly-step-consistent-e ( SbEvt (Event-sb-statfs
 $pid \ d$ ))
  using dynamic-weakly-step-consistent-e-def statfs-by-dentry-wsc-e
  by blast

```

29.33.6 proving “do_{mount}” satisfying the “weakly step consistent” property

```

lemma do-mount-wsc:
assumes  $p0$ : reachable0  $s$ 
  and  $p1$ : reachable0  $t$ 
  and  $p2$ :  $s \sim d \sim t$ 
  and  $p3$ :  $pid @ s \ d$ 
  and  $p4$ :  $s \sim pid \sim t$ 
  and  $p5$ :  $s' = \text{fst}(\text{do-mount } s \ pid \ devname \ dirname \ tp \ f \ p)$ 
  and  $p6$ :  $t' = \text{fst}(\text{do-mount } t \ pid \ devname \ dirname \ tp \ f \ p)$ 
shows  $s' \sim d \sim t'$ 
using  $p6$   $p5$   $p2$  do-mount-def fst-conv
by (metis )

```

```

lemma do-mount-wsc-e:
  assumes  $p0$ : reachable0  $s$ 
    and  $p1$ : reachable0  $t$ 
    and  $p2$ :  $e = \text{SbEvt } (\text{Event-sb-mount } pid \text{ devname } dirname \text{ tp } f \text{ p})$ 
    and  $p3$ :  $s \sim d \sim t$ 
    and  $p4$ :  $(\text{the } (\text{domain-of-event } e)) @ s \ d$ 
    and  $p5$ :  $s \sim (\text{the } (\text{domain-of-event } e)) \sim t$ 
    and  $p6$ :  $s' = \text{exec-event } s \ e$ 
    and  $p7$ :  $t' = \text{exec-event } t \ e$ 
  shows  $s' \sim d \sim t'$ 
  proof –
    {
      have  $a0$  :  $(\text{the } (\text{domain-of-event } e)) = pid$ 
        using  $p2$  domain-of-event-def getpid-from-sb-event-def
        by force
      have  $a1$ :  $s' = \text{fst}(\text{do-mount } s \ pid \ devname \ dirname \ tp \ f \ p)$ 
        using  $p2$   $p6$  exec-event-def by auto
      have  $a2$ :  $t' = \text{fst}(\text{do-mount } t \ pid \ devname \ dirname \ tp \ f \ p)$ 
        using  $p2$   $p7$  exec-event-def
        by auto
      have  $a3$ :  $pid @ s \ d$ 
        using  $p4$   $a0$ 
        by blast
      have  $a4$  :  $s \sim pid \sim t$  using  $p5$   $a0$ 
        by blast
      have  $a5$ :  $s' \sim d \sim t'$ 
        using  $a1$   $a2$   $a3$   $a4$   $p0$   $p1$   $p3$   $p5$   $p4$  do-mount-wsc
        by blast
    }
  then show ?thesis by auto
qed

```

```

lemma do-mount-dwsc-e: dynamic-weakly-step-consistent-e (SbEvt (Event-sb-mount
   $pid \ devname \ dirname \ tp \ f \ p$ ))
  using dynamic-weakly-step-consistent-e-def do-mount-wsc-e
  by blast

```

29.33.7 proving "do_umount" satisfying the "weakly step consistent" property

```

lemma do-umount-wsc:
  assumes  $p0$ : reachable0  $s$ 
    and  $p1$ : reachable0  $t$ 
    and  $p2$ :  $s \sim d \sim t$ 
    and  $p3$ :  $pid @ s \ d$ 
    and  $p4$ :  $s \sim pid \sim t$ 
    and  $p5$ :  $s' = \text{fst } (\text{do-umount } s \ pid \ m \ i)$ 
    and  $p6$ :  $t' = \text{fst } (\text{do-umount } t \ pid \ m \ i)$ 

```

shows $s' \sim d \sim t'$
 using $p6\ p5\ p2\ do_umount_def\ fst_conv$
 by $(metis)$

lemma *do-umount-wsc-e*:
 assumes $p0$: *reachable0* s
 and $p1$: *reachable0* t
 and $p2$: $e = SbEvt\ (Event_sb_umount\ pid\ m\ i)$
 and $p3$: $s \sim d \sim t$
 and $p4$: $(the\ (domain_of_event\ e))\ @\ s\ d$
 and $p5$: $s \sim (the\ (domain_of_event\ e)) \sim t$
 and $p6$: $s' = exec_event\ s\ e$
 and $p7$: $t' = exec_event\ t\ e$
 shows $s' \sim d \sim t'$
 proof –
 {
 have $a0$: $(the\ (domain_of_event\ e)) = pid$
 using $p2\ domain_of_event_def\ getpid_from_sb_event_def$
 by *force*
 have $a1$: $s' = fst\ (do_umount\ s\ pid\ m\ i)$
 using $p2\ p6\ exec_event_def$ by *auto*
 have $a2$: $t' = fst\ (do_umount\ t\ pid\ m\ i)$
 using $p2\ p7\ exec_event_def$
 by *auto*
 have $a3$: $pid\ @\ s\ d$
 using $p4\ a0$
 by *blast*
 have $a4$: $s \sim pid \sim t$ using $p5\ a0$
 by *blast*
 have $a5$: $s' \sim d \sim t'$
 using $a1\ a2\ a3\ a4\ p0\ p1\ p3\ p5\ p4\ do_umount_wsc$
 by *blast*
 }
 then show *?thesis* by *auto*
 qed

lemma *do-umount-dwsc-e*: *dynamic-weakly-step-consistent-e* $(SbEvt\ (Event_sb_umount\ pid\ m\ i))$
 using *dynamic-weakly-step-consistent-e-def* *do-umount-wsc-e*
 by *blast*

29.33.8 proving ”pivot_{root}” satisfying the ”weakly step consistent” property

lemma *pivot-root-wsc*:
 assumes $p0$: *reachable0* s
 and $p1$: *reachable0* t
 and $p2$: $s \sim d \sim t$
 and $p3$: $pid\ @\ s\ d$
 and $p4$: $s \sim pid \sim t$

```

    and p5:  $s' = \text{fst } (\text{pivot-root } s \text{ pid})$ 
    and p6:  $t' = \text{fst } (\text{pivot-root } t \text{ pid})$ 
shows  $s' \sim d \sim t'$ 
using p6 p5 p2 pivot-root-def fst-conv
by (metis )

lemma pivot-root-wsc-e:
assumes p0: reachable0 s
    and p1: reachable0 t
    and p2:  $e = \text{SbEvt } (\text{Event-sb-pivotroot } \text{pid})$ 
    and p3:  $s \sim d \sim t$ 
    and p4:  $(\text{the } (\text{domain-of-event } e)) @ s d$ 
    and p5:  $s \sim (\text{the } (\text{domain-of-event } e)) \sim t$ 
    and p6:  $s' = \text{exec-event } s e$ 
    and p7:  $t' = \text{exec-event } t e$ 
shows  $s' \sim d \sim t'$ 
proof -
{
  have a0 :  $(\text{the } (\text{domain-of-event } e)) = \text{pid}$ 
    using p2 domain-of-event-def getpid-from-sb-event-def
    by force
  have a1:  $s' = \text{fst } (\text{pivot-root } s \text{ pid})$ 
    using p2 p6 exec-event-def by auto
  have a2:  $t' = \text{fst } (\text{pivot-root } t \text{ pid})$ 
    using p2 p7 exec-event-def
    by auto
  have a3:  $\text{pid} @ s d$ 
    using p4 a0
    by blast
  have a4 :  $s \sim \text{pid} \sim t$  using p5 a0
    by blast
  have a5:  $s' \sim d \sim t'$ 
    using a1 a2 a3 a4 p0 p1 p3 p5 p4 pivot-root-wsc
    by blast
}
then show ?thesis by auto
qed

```

```

lemma pivot-root-dwsc-e: dynamic-weakly-step-consistent-e (SbEvt (Event-sb-pivotroot
pid))
  using dynamic-weakly-step-consistent-e-def pivot-root-wsc-e
  by blast

```

29.33.9 proving "setup_{securityoptions}" satisfying the "weakly step consistent" property

```

lemma setup-security-options-wsc:
assumes p0: reachable0 s
    and p1: reachable0 t
    and p2:  $s \sim d \sim t$ 

```

```

    and p3: pid @ s d
    and p4: s ~ pid ~ t
    and p5: s' = fst(setup-security-options s pid n sb opt)
    and p6: t' = fst(setup-security-options t pid n sb opt)
  shows s' ~ d ~ t'
  using p6 p5 p2 setup-security-options-def fst-conv
  by (metis )

```

```

lemma setup-security-options-wsc-e:
  assumes p0: reachable0 s
    and p1: reachable0 t
    and p2: e = SbEvt (Event-set-mnt-opts pid n sb opt)
    and p3: s ~ d ~ t
    and p4: (the (domain-of-event e)) @ s d
    and p5: s ~ (the (domain-of-event e)) ~ t
    and p6: s' = exec-event s e
    and p7: t' = exec-event t e
  shows s' ~ d ~ t'
  proof -
    {
      have a0 : (the (domain-of-event e)) = pid
        using p2 domain-of-event-def getpid-from-sb-event-def
        by force
      have a1: s' = fst(setup-security-options s pid n sb opt)
        using p2 p6 exec-event-def by auto
      have a2: t' = fst(setup-security-options t pid n sb opt)
        using p2 p7 exec-event-def
        by auto
      have a3: pid @ s d
        using p4 a0
        by blast
      have a4 : s ~ pid ~ t using p5 a0
        by blast
      have a5: s' ~ d ~ t'
        using a1 a2 a3 a4 p0 p1 p3 p5 p4 setup-security-options-wsc
        by blast
    }
    then show ?thesis by auto
  qed

```

```

lemma setup-security-options-dwsc-e: dynamic-weakly-step-consistent-e (SbEvt (Event-set-mnt-opts
pid n sb opt))
  using dynamic-weakly-step-consistent-e-def setup-security-options-wsc-e
  by blast

```

29.33.10 proving "set_s security" satisfying the "weakly step consistent" property

```

lemma set-sb-security-wsc:
  assumes p0: reachable0 s

```

```

    and p1: reachable0 t
    and p2: s ~ d ~ t
    and p3: pid @ s d
    and p4: s ~ pid ~ t
    and p5: s' = fst(set-sb-security s pid sb de info)
    and p6: t' = fst(set-sb-security t pid sb de info)
  shows s' ~ d ~ t'
  using p6 p5 p2 set-sb-security-def fst-conv
  by (metis )

```

```

lemma set-sb-security-wsc-e:
  assumes p0: reachable0 s
  and p1: reachable0 t
  and p2: e = SbEvt (Event-set-sb-security pid sb de info)
  and p3: s ~ d ~ t
  and p4: (the (domain-of-event e)) @ s d
  and p5: s ~ (the (domain-of-event e)) ~ t
  and p6: s' = exec-event s e
  and p7: t' = exec-event t e
  shows s' ~ d ~ t'
  proof -
    {
      have a0 : (the (domain-of-event e)) = pid
        using p2 domain-of-event-def getpid-from-sb-event-def
        by force
      have a1: s' = fst(set-sb-security s pid sb de info)
        using p2 p6 exec-event-def by auto
      have a2: t' = fst(set-sb-security t pid sb de info)
        using p2 p7 exec-event-def
        by auto
      have a3: pid @ s d
        using p4 a0
        by blast
      have a4 : s ~ pid ~ t using p5 a0
        by blast
      have a5: s' ~ d ~ t'
        using a1 a2 a3 a4 p0 p1 p3 p5 p4 set-sb-security-wsc
        by blast
    }
    then show ?thesis by auto
  qed

```

```

lemma set-sb-security-dwsc-e: dynamic-weakly-step-consistent-e (SbEvt (Event-set-sb-security
pid sb d info))
  using dynamic-weakly-step-consistent-e-def set-sb-security-wsc-e
  by blast

```


29.33.11 proving "nfs_clone_sb_security" satisfying the "weakly step consistent" property

lemma *nfs-clone-sb-security-wsc*:

assumes *p0*: *reachable0 s*
and *p1*: *reachable0 t*
and *p2*: $s \sim d \sim t$
and *p3*: *pid @ s d*
and *p4*: $s \sim pid \sim t$
and *p5*: $s' = fst(nfs_clone_sb_security\ s\ pid\ sb\ de\ minfo)$
and *p6*: $t' = fst(nfs_clone_sb_security\ s\ pid\ sb\ de\ minfo)$
shows $s' \sim d \sim t'$
using *p6 p5 p2 nfs-clone-sb-security-def fst-conv*
by (*simp add: vpeq-reflexive-lemma*)

thm *nfs-clone-sb-security-def*

lemma *nfs-clone-sb-security-wsc-e*:

assumes *p0*: *reachable0 s*
and *p1*: *reachable0 t*
and *p2*: $e = SbEvt\ (Event_sb_clone_mnt_opts\ pid\ sb\ de\ minfo)$
and *p3*: $s \sim d \sim t$
and *p4*: $(the\ (domain-of-event\ e)) @ s\ d$
and *p5*: $s \sim (the\ (domain-of-event\ e)) \sim t$
and *p6*: $s' = exec-event\ s\ e$
and *p7*: $t' = exec-event\ t\ e$
shows $s' \sim d \sim t'$
proof –
{
have *a0* : $(the\ (domain-of-event\ e)) = pid$
using *p2 domain-of-event-def getpid-from-sb-event-def*
by *force*
have *a1*: $s' = fst(nfs_clone_sb_security\ s\ pid\ sb\ de\ minfo)$
using *p2 p6 exec-event-def* **by** *auto*
have *a2*: $t' = fst(nfs_clone_sb_security\ t\ pid\ sb\ de\ minfo)$
using *p2 p7 exec-event-def*
by *auto*
have *a3*: *pid @ s d*
using *p4 a0*
by *blast*
have *a4* : $s \sim pid \sim t$ **using** *p5 a0*
by *blast*
have *a5*: $result\ s\ (security_sb_clone_mnt_opts'\ s\ oldsb\ sb'\ kflags\ kflags-out) =$
True
apply(*simp add: security-sb-clone-mnt-opts'-def result-def the-run-state-def*)
by (*simp add: return-def*)
have *a6*: $s = s'$ **using** *nfs-clone-sb-security-def a5*
by (*smt a1 eq-fst-iff*)
have *a7*: $result\ t\ (security_sb_clone_mnt_opts'\ t\ oldsb\ sb'\ kflags\ kflags-out) =$
True
apply(*simp add: security-sb-clone-mnt-opts'-def result-def the-run-state-def*)

```

    by (simp add: return-def)
  have a8:  $t = t'$  using nfs-clone-sb-security-def a2 a7
    by (smt eq-fst-iff)
  have a5:  $s' \sim d \sim t'$ 
    using a1 a2 a3 a4 p0 p1 p3 p5 p4 a6 a8 set-sb-security-wsc
    by presburger
}
then show ?thesis by auto
qed

```

```

lemma nfs-clone-sb-security-dwsc-e: dynamic-weakly-step-consistent-e (SbEvt (Event-sb-clone-mnt-opts
pid sb d minfo))
  using dynamic-weakly-step-consistent-e-def nfs-clone-sb-security-wsc-e
  by blast

```

29.33.12 proving "parse_ssecurity_options" satisfying the "weaklystepconsistent" property

```

lemma parse-security-options-wsc:
  assumes p0: reachable0 s
    and p1: reachable0 t
    and p2:  $s \sim d \sim t$ 
    and p3: pid @ s d
    and p4:  $s \sim pid \sim t$ 
    and p5:  $s' = fst(parse-security-options s pid str opt)$ 
    and p6:  $t' = fst(parse-security-options t pid str opt)$ 
  shows  $s' \sim d \sim t'$ 
  using p6 p5 p2 parse-security-options-def fst-conv
  by (metis )

```

```

lemma parse-security-options-wsc-e:
  assumes p0: reachable0 s
    and p1: reachable0 t
    and p2:  $e = SbEvt (Event-sb-parse-opts-str pid str opt)$ 
    and p3:  $s \sim d \sim t$ 
    and p4: (the (domain-of-event e)) @ s d
    and p5:  $s \sim (the (domain-of-event e)) \sim t$ 
    and p6:  $s' = exec-event s e$ 
    and p7:  $t' = exec-event t e$ 
  shows  $s' \sim d \sim t'$ 
proof -
{
  have a0 : (the (domain-of-event e)) = pid
    using p2 domain-of-event-def getpid-from-sb-event-def
    by force
  have a1:  $s' = fst(parse-security-options s pid str opt)$ 
    using p2 p6 exec-event-def by auto
  have a2:  $t' = fst(parse-security-options t pid str opt)$ 
    using p2 p7 exec-event-def

```

```

    by auto
  have a3: pid @ s d
    using p4 a0
  by blast
  have a4 : s ~ pid ~ t using p5 a0
  by blast
  have a5: s' ~ d ~ t'
    using a1 a2 a3 a4 p0 p1 p3 p5 p4 parse-security-options-wsc
  by blast
}
then show ?thesis by auto
qed

```

```

lemma parse-security-options-dwsc-e: dynamic-weakly-step-consistent-e (SbEvt (Event-sb-parse-opts-str
pid str opt))
  using dynamic-weakly-step-consistent-e-def parse-security-options-wsc-e
  by blast

```

29.34 smack task hooks weakly step consistent

29.34.1 proving "prepare_{creds}" satisfying the "weakly step consistent" property

```

lemma prepare-creds-wsc:
  assumes p0: reachable0 s
    and p1: reachable0 t
    and p2: s ~ d ~ t
    and p3: pid @ s d
    and p4: s ~ pid ~ t
    and p5: s' = fst(prepare-creds s pid)
    and p6: t' = fst(prepare-creds t pid)
  shows s' ~ d ~ t'
  proof -
  {
    have a0 : s = s'
      using p5 prepare-creds-def
    by (smt fstI)
    have a1 : t = t'
      using p6 prepare-creds-def
    by (smt fst-conv)
    have a2: s' ~ d ~ t'
      using a0 a1 p2
    by blast
  }
  then show ?thesis by auto
qed

```

```

lemma prepare-creds-wsc-e:
  assumes p0: reachable0 s
    and p1: reachable0 t
    and p2: e = TskEvt ( (Event-prepare-creds pid))

```

```

and p3:  $s \sim d \sim t$ 
and p4:  $(\text{the } (\text{domain-of-event } e)) @ s d$ 
and p5:  $s \sim (\text{the } (\text{domain-of-event } e)) \sim t$ 
and p6:  $s' = \text{exec-event } s e$ 
and p7:  $t' = \text{exec-event } t e$ 
shows  $s' \sim d \sim t'$ 
proof -
{
have a0:  $(\text{the } (\text{domain-of-event } e)) = \text{pid}$ 
  using p2 domain-of-event-def getpid-from-tsk-event-def
  by force
have a1:  $s' = \text{fst}(\text{prepare-creds } s \text{ pid})$ 
  using p2 p6 exec-event-def by auto
have a2:  $t' = \text{fst}(\text{prepare-creds } t \text{ pid})$ 
  using p2 p7 exec-event-def
  by auto
have a3:  $\text{pid} @ s d$ 
  using p4 a0
  by blast
have a4:  $s \sim \text{pid} \sim t$  using p5 a0
  by blast
have a5:  $s' \sim d \sim t'$ 
  using a1 a2 a3 a4 p0 p1 p3 p5 p4 prepare-creds-wsc
  by blast
}
then show ?thesis by auto
qed

lemma prepare-creds-dwsc-e: dynamic-weakly-step-consistent-e ( $\text{TskEvt } ((\text{Event-prepare-creds } \text{pid})))$ 
  using dynamic-weakly-step-consistent-e-def prepare-creds-wsc-e
  by blast

```

29.34.2 proving "sys_setreuid" satisfying the "weakly step consistent" property

```

lemma sys-setreuid-wsc:
assumes p0: reachable0 s
and p1: reachable0 t
and p2:  $s \sim d \sim t$ 
and p3:  $\text{pid} @ s d$ 
and p4:  $s \sim \text{pid} \sim t$ 
and p5:  $s' = \text{fst}(\text{sys-setreuid } s \text{ pid kuid euid'})$ 
and p6:  $t' = \text{fst}(\text{sys-setreuid } t \text{ pid kuid euid'})$ 
shows  $s' \sim d \sim t'$ 
proof -
{
have a0:  $s = s'$ 
  using p5 sys-setreuid-def
  by (smt fstI)

```

```

    have a1 : t = t'
      using p6 sys-setreuid-def
      by (smt fst-conv)
    have a2: s' ~ d ~ t'
      using a0 a1 p2
      by blast
  }
  then show ?thesis by auto
qed

```

```

lemma sys-setreuid-wsc-e:
  assumes p0: reachable0 s
  and p1: reachable0 t
  and p2: e = TskEvt ( (Event-sys-setreuid pid kuid evid'))
  and p3: s ~ d ~ t
  and p4: (the (domain-of-event e)) @ s d
  and p5: s ~ (the (domain-of-event e)) ~ t
  and p6: s' = exec-event s e
  and p7: t' = exec-event t e
  shows s' ~ d ~ t'
  proof -
    {
      have a0 : (the (domain-of-event e)) = pid
        using p2 domain-of-event-def getpid-from-tsk-event-def
        by force
      have a1: s' = fst(sys-setreuid s pid kuid evid')
        using p2 p6 exec-event-def by auto
      have a2: t' = fst(sys-setreuid t pid kuid evid')
        using p2 p7 exec-event-def
        by auto
      have a3: pid @ s d
        using p4 a0
        by blast
      have a4 : s ~ pid ~ t using p5 a0
        by blast
      have a5: s' ~ d ~ t'
        using a1 a2 a3 a4 p0 p1 p3 p5 p4 sys-setreuid-wsc
        by blast
    }
    then show ?thesis by auto
  qed

```

```

lemma sys-setreuid-dwsc-e: dynamic-weakly-step-consistent-e (TskEvt ( (Event-sys-setreuid
pid kuid evid')))
  using dynamic-weakly-step-consistent-e-def sys-setreuid-wsc-e
  by blast

```

29.34.3 proving "setpgid" satisfying the "weakly step consistent" property

lemma *setpgid-wsc*:

```

assumes p0: reachable0 s
    and p1: reachable0 t
    and p2: s ~ d ~ t
    and p3: pid @ s d
    and p4: s ~ pid ~ t
    and p5: s' = fst(setpgid s pid i pgid)
    and p6: t' = fst(setpgid t pid i pgid)
shows s' ~ d ~ t'
proof -
{
  have a0 : s = s'
    using p5 setpgid-def
    by (smt fstI)
  have a1 : t = t'
    using p6 setpgid-def
    by (smt fst-conv)
  have a2: s' ~ d ~ t'
    using a0 a1 p2
    by blast
}
then show ?thesis by auto
qed

```

lemma *setpgid-wsc-e*:

```

assumes p0: reachable0 s
    and p1: reachable0 t
    and p2: e = TskEvt ( (Event-setpgid pid i pgid))
    and p3: s ~ d ~ t
    and p4: (the (domain-of-event e)) @ s d
    and p5: s ~ (the (domain-of-event e)) ~ t
    and p6: s' = exec-event s e
    and p7: t' = exec-event t e
shows s' ~ d ~ t'
proof -
{
  have a0 : (the (domain-of-event e)) = pid
    using p2 domain-of-event-def getpid-from-tsk-event-def
    by force
  have a1: s' = fst(setpgid s pid i pgid)
    using p2 p6 exec-event-def by auto
  have a2: t' = fst(setpgid t pid i pgid)
    using p2 p7 exec-event-def
    by auto
  have a3: pid @ s d
    using p4 a0
    by blast
}

```

```

    have a4 : s ~ pid ~ t using p5 a0
    by blast
    have a5: s' ~ d ~ t'
      using a1 a2 a3 a4 p0 p1 p3 p5 p4 setpgid-wsc
      by blast
  }
  then show ?thesis by auto
qed

```

```

lemma setpgid-dwsc-e: dynamic-weakly-step-consistent-e ( TskEvt ( (Event-setpgid
pid i pgid)))
  using dynamic-weakly-step-consistent-e-def setpgid-wsc-e
  by blast

```

29.34.4 proving "do_getpgid" satisfying the "weakly step consistent" property

```

lemma do-getpgid-wsc:
  assumes p0: reachable0 s
    and p1: reachable0 t
    and p2: s ~ d ~ t
    and p3: pid @ s d
    and p4: s ~ pid ~ t
    and p5: s' = fst(do-getpgid s pid i)
    and p6: t' = fst(do-getpgid t pid i)
  shows s' ~ d ~ t'
  proof -
  {
    have a0 : s = s'
      using p5 do-getpgid-def
      by (smt fstI)
    have a1 : t = t'
      using p6 do-getpgid-def
      by (smt fst-conv)
    have a2: s' ~ d ~ t'
      using a0 a1 p2
      by blast
  }
  then show ?thesis by auto
qed

```

```

lemma do-getpgid-wsc-e:
  assumes p0: reachable0 s
    and p1: reachable0 t
    and p2: e = TskEvt ( (Event-do-getpgid pid i))
    and p3: s ~ d ~ t
    and p4: (the (domain-of-event e)) @ s d
    and p5: s ~ (the (domain-of-event e)) ~ t
    and p6: s' = exec-event s e
    and p7: t' = exec-event t e

```

```

shows  $s' \sim d \sim t'$ 
proof -
{
  have  $a0$  :  $(the\ (domain-of-event\ e)) = pid$ 
    using  $p2\ domain-of-event-def\ getpid-from-tsk-event-def$ 
    by force
  have  $a1$  :  $s' = fst(do-getpgid\ s\ pid\ i)$ 
    using  $p2\ p6\ exec-event-def$  by auto
  have  $a2$  :  $t' = fst(do-getpgid\ t\ pid\ i)$ 
    using  $p2\ p7\ exec-event-def$ 
    by auto
  have  $a3$  :  $pid @ sd$ 
    using  $p4\ a0$ 
    by blast
  have  $a4$  :  $s \sim pid \sim t$  using  $p5\ a0$ 
    by blast
  have  $a5$  :  $s' \sim d \sim t'$ 
    using  $a1\ a2\ a3\ a4\ p0\ p1\ p3\ p5\ p4\ do-getpgid-wsc$ 
    by blast
}
then show ?thesis by auto
qed

lemma do-getpgid-dwsc-e: dynamic-weakly-step-consistent-e ( $TskEvt\ (\ (Event-do-getpgid\ pid\ i))$ )
  using dynamic-weakly-step-consistent-e-def do-getpgid-wsc-e
  by blast

```

29.34.5 proving "getsid" satisfying the "weakly step consistent" property

```

lemma getsid-wsc:
assumes  $p0$ : reachable0 s
  and  $p1$ : reachable0 t
  and  $p2$ :  $s \sim d \sim t$ 
  and  $p3$ :  $pid @ s\ d$ 
  and  $p4$ :  $s \sim pid \sim t$ 
  and  $p5$ :  $s' = fst(getsid\ s\ pid\ i)$ 
  and  $p6$ :  $t' = fst(getsid\ t\ pid\ i)$ 
shows  $s' \sim d \sim t'$ 
proof -
{
  have  $a0$  :  $s = s'$ 
    using  $p5\ getsid-def$ 
    by (smt case-prod-unfold fstI)
  have  $a1$  :  $t = t'$ 
    using  $p6\ getsid-def$ 
    by (smt fstI old.prod.case)
  have  $a2$ :  $s' \sim d \sim t'$ 

```



```

    using a0 a1 p2
    by blast
  }
  then show ?thesis by auto
qed

lemma getsid-wsc-e:
  assumes p0: reachable0 s
  and p1: reachable0 t
  and p2: e = TskEvt ( (Event-getsid pid i))
  and p3: s ~ d ~ t
  and p4: (the (domain-of-event e)) @ s d
  and p5: s ~ (the (domain-of-event e)) ~ t
  and p6: s' = exec-event s e
  and p7: t' = exec-event t e
  shows s' ~ d ~ t'
  proof -
    {
      have a0 : (the (domain-of-event e)) = pid
        using p2 domain-of-event-def getpid-from-tsk-event-def
        by force
      have a1: s' = fst(getsid s pid i)
        using p2 p6 exec-event-def by auto
      have a2: t' = fst(getsid t pid i)
        using p2 p7 exec-event-def
        by auto
      have a3: pid @ s d
        using p4 a0
        by blast
      have a4 : s ~ pid ~ t using p5 a0
        by blast
      have a5: s' ~ d ~ t'
        using a1 a2 a3 a4 p0 p1 p3 p5 p4 getsid-wsc
        by blast
    }
    then show ?thesis by auto
  qed

```

```

lemma getsid-dwsc-e: dynamic-weakly-step-consistent-e ( TskEvt ( (Event-getsid
pid i)))
  using dynamic-weakly-step-consistent-e-def getsid-wsc-e
  by blast

```

29.34.6 proving "getsecid" satisfying the "weakly step consistent" property

```

lemma getsecid-wsc:
  assumes p0: reachable0 s
  and p1: reachable0 t

```

```

and p2:  $s \sim d \sim t$ 
and p3:  $pid @ s d$ 
and p4:  $s \sim pid \sim t$ 
and p5:  $s' = fst(getsecid\ s\ pid\ p\ u)$ 
and p6:  $t' = fst(getsecid\ t\ pid\ p\ u)$ 
shows  $s' \sim d \sim t'$ 
proof -
{
  have a0 :  $s = s'$ 
    using p5 getsecid-def
    by (smt fstI)
  have a1 :  $t = t'$ 
    using p6 getsecid-def
    by (smt fst-conv)
  have a2:  $s' \sim d \sim t'$ 
    using a0 a1 p2
    by blast
}
then show ?thesis by auto
qed

```

```

lemma getsecid-wsc-e:
  assumes p0:  $reachable0\ s$ 
  and p1:  $reachable0\ t$ 
  and p2:  $e = TskEvt\ ((Event-getsecid\ pid\ p\ u))$ 
  and p3:  $s \sim d \sim t$ 
  and p4:  $(the\ (domain-of-event\ e)) @ s d$ 
  and p5:  $s \sim (the\ (domain-of-event\ e)) \sim t$ 
  and p6:  $s' = exec-event\ s\ e$ 
  and p7:  $t' = exec-event\ t\ e$ 
shows  $s' \sim d \sim t'$ 
proof -
{
  have a0 :  $(the\ (domain-of-event\ e)) = pid$ 
    using p2 domain-of-event-def getpid-from-tsk-event-def
    by force
  have a1:  $s' = fst(getsecid\ s\ pid\ p\ u)$ 
    using p2 p6 exec-event-def by auto
  have a2:  $t' = fst(getsecid\ t\ pid\ p\ u)$ 
    using p2 p7 exec-event-def
    by auto
  have a3:  $pid @ s d$ 
    using p4 a0
    by blast
  have a4 :  $s \sim pid \sim t$  using p5 a0
    by blast
  have a5:  $s' \sim d \sim t'$ 
    using a1 a2 a3 a4 p0 p1 p3 p5 p4 getsecid-wsc
    by blast
}

```

```

    }
  then show ?thesis by auto
qed

```

```

lemma getsecid-dwsc-e: dynamic-weakly-step-consistent-e (TskEvt ((Event-getsecid
pid p u)))
  using dynamic-weakly-step-consistent-e-def getsecid-wsc-e
  by blast

```

29.34.7 proving "task_setnice" satisfying the "weaklystepconsistent" property

```

lemma task-setnice-wsc:
  assumes p0: reachable0 s
    and p1: reachable0 t
    and p2: s ~ d ~ t
    and p3: pid @ s d
    and p4: s ~ pid ~ t
    and p5: s' = fst(task-setnice s pid p i)
    and p6: t' = fst(task-setnice t pid p i)
  shows s' ~ d ~ t'
  proof -
  {
    have a0 : s = s'
      using p5 task-setnice-def
      by (smt fstI)
    have a1 : t = t'
      using p6 task-setnice-def
      by (smt fst-conv)
    have a2: s' ~ d ~ t'
      using a0 a1 p2
      by blast
  }
  then show ?thesis by auto
qed

```

```

lemma task-setnice-wsc-e:
  assumes p0: reachable0 s
    and p1: reachable0 t
    and p2: e = TskEvt ((Event-task-setnice pid p i))
    and p3: s ~ d ~ t
    and p4: (the (domain-of-event e)) @ s d
    and p5: s ~ (the (domain-of-event e)) ~ t
    and p6: s' = exec-event s e
    and p7: t' = exec-event t e
  shows s' ~ d ~ t'
  proof -
  {
    have a0 : (the (domain-of-event e)) = pid
      using p2 domain-of-event-def getpid-from-tsk-event-def

```

```

    by force
  have a1:  $s' = \text{fst}(\text{task-setnice } s \text{ pid } p \ i)$ 
    using p2 p6 exec-event-def by auto
  have a2:  $t' = \text{fst}(\text{task-setnice } t \text{ pid } p \ i)$ 
    using p2 p7 exec-event-def
    by auto
  have a3:  $\text{pid} @ s d$ 
    using p4 a0
    by blast
  have a4 :  $s \sim \text{pid} \sim t$  using p5 a0
    by blast
  have a5:  $s' \sim d \sim t'$ 
    using a1 a2 a3 a4 p0 p1 p3 p5 p4 task-setnice-wsc
    by blast
}
then show ?thesis by auto
qed

```

```

lemma task-setnice-dwsc-e: dynamic-weakly-step-consistent-e (TskEvt ((Event-task-setnice
pid p i)))
  using dynamic-weakly-step-consistent-e-def task-setnice-wsc-e
  by blast

```

29.34.8 proving "set_itask_ioprio" satisfying the "weakly step consistent" property

```

lemma set-task-ioprio-wsc:
  assumes p0: reachable0 s
    and p1: reachable0 t
    and p2:  $s \sim d \sim t$ 
    and p3:  $\text{pid} @ s d$ 
    and p4:  $s \sim \text{pid} \sim t$ 
    and p5:  $s' = \text{fst}(\text{set-task-ioprio } s \text{ pid } p \ i)$ 
    and p6:  $t' = \text{fst}(\text{set-task-ioprio } t \text{ pid } p \ i)$ 
  shows  $s' \sim d \sim t'$ 
  proof -
  {
    have a0 :  $s = s'$ 
      using p5 set-task-ioprio-def
      by (smt fstI)
    have a1 :  $t = t'$ 
      using p6 set-task-ioprio-def
      by (smt fst-conv)
    have a2:  $s' \sim d \sim t'$ 
      using a0 a1 p2
      by blast
  }
  then show ?thesis by auto
qed

```

lemma *set-task-ioprio-wsc-e*:
assumes $p0$: *reachable0* s
and $p1$: *reachable0* t
and $p2$: $e = \text{TskEvt } ((\text{Event-set-task-ioprio } pid \ p \ i))$
and $p3$: $s \sim d \sim t$
and $p4$: $(\text{the } (\text{domain-of-event } e)) @ s \ d$
and $p5$: $s \sim (\text{the } (\text{domain-of-event } e)) \sim t$
and $p6$: $s' = \text{exec-event } s \ e$
and $p7$: $t' = \text{exec-event } t \ e$
shows $s' \sim d \sim t'$
proof –
{
have $a0$: $(\text{the } (\text{domain-of-event } e)) = pid$
using $p2$ *domain-of-event-def* *getpid-from-tsk-event-def*
by *force*
have $a1$: $s' = \text{fst}(\text{set-task-ioprio } s \ pid \ p \ i)$
using $p2$ $p6$ *exec-event-def* **by** *auto*
have $a2$: $t' = \text{fst}(\text{set-task-ioprio } t \ pid \ p \ i)$
using $p2$ $p7$ *exec-event-def*
by *auto*
have $a3$: $pid @ s \ d$
using $p4$ $a0$
by *blast*
have $a4$: $s \sim pid \sim t$ **using** $p5$ $a0$
by *blast*
have $a5$: $s' \sim d \sim t'$
using $a1$ $a2$ $a3$ $a4$ $p0$ $p1$ $p3$ $p5$ $p4$ *set-task-ioprio-wsc*
by *blast*
}
then show *?thesis* **by** *auto*
qed

lemma *set-task-ioprio-dwsc-e*: *dynamic-weakly-step-consistent-e* ($\text{TskEvt } ((\text{Event-set-task-ioprio } pid \ p \ i))$)
using *dynamic-weakly-step-consistent-e-def* *set-task-ioprio-wsc-e*
by *blast*

29.34.9 proving “get_iask_ioprio” satisfying the “weakly step consistent” property

lemma *get-task-ioprio-wsc*:
assumes $p0$: *reachable0* s
and $p1$: *reachable0* t
and $p2$: $s \sim d \sim t$
and $p3$: $pid @ s \ d$
and $p4$: $s \sim pid \sim t$
and $p5$: $s' = \text{fst}(\text{get-task-ioprio } s \ pid \ p)$
and $p6$: $t' = \text{fst}(\text{get-task-ioprio } t \ pid \ p)$
shows $s' \sim d \sim t'$
proof –

```

{
  have a0 : s = s'
    using p5 get-task-ioprio-def
    by (smt fstI)
  have a1 : t = t'
    using p6 get-task-ioprio-def
    by (smt fst-conv)
  have a2: s' ~ d ~ t'
    using a0 a1 p2
    by blast
}
then show ?thesis by auto
qed

```

```

lemma get-task-ioprio-wsc-e:
  assumes p0: reachable0 s
  and p1: reachable0 t
  and p2: e = TskEvt ((Event-get-task-ioprio pid p))
  and p3: s ~ d ~ t
  and p4: (the (domain-of-event e)) @ s d
  and p5: s ~ (the (domain-of-event e)) ~ t
  and p6: s' = exec-event s e
  and p7: t' = exec-event t e
  shows s' ~ d ~ t'
  proof -
    {
      have a0 : (the (domain-of-event e)) = pid
        using p2 domain-of-event-def getpid-from-tsk-event-def
        by force
      have a1: s' = fst(get-task-ioprio s pid p)
        using p2 p6 exec-event-def by auto
      have a2: t' = fst(get-task-ioprio t pid p)
        using p2 p7 exec-event-def
        by auto
      have a3: pid @ s d
        using p4 a0
        by blast
      have a4 : s ~ pid ~ t using p5 a0
        by blast
      have a5: s' ~ d ~ t'
        using a1 a2 a3 a4 p0 p1 p3 p5 p4 get-task-ioprio-wsc
        by blast
    }
    then show ?thesis by auto
  qed

```

```

lemma get-task-ioprio-dwsc-e: dynamic-weakly-step-consistent-e (TskEvt ((Event-get-task-ioprio
pid p)))
  using dynamic-weakly-step-consistent-e-def get-task-ioprio-wsc-e

```

by *blast*

29.34.10 proving "check_{prlimit}permission" satisfying the "weakly step consistent" property

lemma *check-prlimit-permission-wsc*:

```

assumes p0: reachable0 s
  and p1: reachable0 t
  and p2:  $s \sim d \sim t$ 
  and p3:  $pid @ s d$ 
  and p4:  $s \sim pid \sim t$ 
  and p5:  $s' = fst(check\_prlimit\_permission\ s\ pid\ p\ i)$ 
  and p6:  $t' = fst(check\_prlimit\_permission\ t\ pid\ p\ i)$ 
shows  $s' \sim d \sim t'$ 
proof –
{
  have a0 :  $s = s'$ 
    using p5 check-prlimit-permission-def
    by (smt fstI)
  have a1 :  $t = t'$ 
    using p6 check-prlimit-permission-def
    by (smt fst-conv)
  have a2:  $s' \sim d \sim t'$ 
    using a0 a1 p2
    by blast
}
then show ?thesis by auto
qed

```

lemma *check-prlimit-permission-wsc-e*:

```

assumes p0: reachable0 s
  and p1: reachable0 t
  and p2:  $e = TskEvt\ ((Event\_check\_prlimit\_permission\ pid\ p\ i))$ 
  and p3:  $s \sim d \sim t$ 
  and p4:  $(the\ (domain-of-event\ e)) @ s d$ 
  and p5:  $s \sim (the\ (domain-of-event\ e)) \sim t$ 
  and p6:  $s' = exec-event\ s\ e$ 
  and p7:  $t' = exec-event\ t\ e$ 
shows  $s' \sim d \sim t'$ 
proof –
{
  have a0 :  $(the\ (domain-of-event\ e)) = pid$ 
    using p2 domain-of-event-def getpid-from-tsk-event-def
    by force
  have a1:  $s' = fst(check\_prlimit\_permission\ s\ pid\ p\ i)$ 
    using p6 exec-event-def by auto
  have a2:  $t' = fst(check\_prlimit\_permission\ t\ pid\ p\ i)$ 
    using p7 exec-event-def
    by auto
  have a3:  $pid @ s d$ 

```

```

      using p4 a0
    by blast
  have a4 : s ~ pid ~ t using p5 a0
    by blast
  have a5: s' ~ d ~ t'
    using a1 a2 a3 a4 p0 p1 p3 p5 p4 check-prlimit-permission-wsc
    by blast
}
then show ?thesis by auto
qed

```

```

lemma check-prlimit-permission-dwsc-e: dynamic-weakly-step-consistent-e (TskEvt
((Event-check-prlimit-permission pid p i)))
  using dynamic-weakly-step-consistent-e-def check-prlimit-permission-wsc-e
  by blast

```

29.34.11 proving "do_{prlimit}" satisfying the "weakly step consistent" property

```

lemma do-prlimit-wsc:
  assumes p0: reachable0 s
    and p1: reachable0 t
    and p2: s ~ d ~ t
    and p3: pid @ s d
    and p4: s ~ pid ~ t
    and p5: s' = fst(do-prlimit s pid p i)
    and p6: t' = fst(do-prlimit t pid p i)
  shows s' ~ d ~ t'
  proof -
  {
    have a0 : s = s'
      using p5 do-prlimit-def
      by (smt fstI)
    have a1 : t = t'
      using p6 do-prlimit-def
      by (smt fst-conv)
    have a2: s' ~ d ~ t'
      using a0 a1 p2
      by blast
  }
  then show ?thesis by auto
qed

```

```

lemma do-prlimit-wsc-e:
  assumes p0: reachable0 s
    and p1: reachable0 t
    and p2: e = TskEvt ((Event-do-prlimit pid p i))
    and p3: s ~ d ~ t
    and p4: (the (domain-of-event e)) @ s d
    and p5: s ~ (the (domain-of-event e)) ~ t

```



```

    and p6: s' = exec-event s e
    and p7: t' = exec-event t e
shows s' ~ d ~ t'
proof -
{
  have a0 : (the (domain-of-event e)) = pid
    using p2 domain-of-event-def getpid-from-tsk-event-def
    by force
  have a1: s' = fst(do-prlimit s pid p i)
    using p2 p6 exec-event-def by auto
  have a2: t' = fst(do-prlimit t pid p i)
    using p2 p7 exec-event-def
    by auto
  have a3: pid @ s d
    using p4 a0
    by blast
  have a4 : s ~ pid ~ t using p5 a0
    by blast
  have a5: s' ~ d ~ t'
    using a1 a2 a3 a4 p0 p1 p3 p5 p4 do-prlimit-wsc
    by blast
}
then show ?thesis by auto
qed

```

```

lemma do-prlimit-dwsc-e: dynamic-weakly-step-consistent-e (TskEvt ((Event-do-prlimit
pid p i)))
  using dynamic-weakly-step-consistent-e-def do-prlimit-wsc-e
  by blast

```

29.34.12 proving "task_setscheduler" satisfying the "weaklystepconsistent" property

```

lemma task-scheduler-wsc:
assumes p0: reachable0 s
  and p1: reachable0 t
  and p2: s ~ d ~ t
  and p3: pid @ s d
  and p4: s ~ pid ~ t
  and p5: s' = fst(task-scheduler s pid p)
  and p6: t' = fst(task-scheduler t pid p)
shows s' ~ d ~ t'
proof -
{
  have a0 : s = s'
    using p5 task-scheduler-def
    by (smt fstI)
  have a1 : t = t'
    using p6 task-scheduler-def
    by (smt fst-conv)
}

```

```

    have a2:  $s' \sim d \sim t'$ 
      using a0 a1 p2
      by blast
  }
  then show ?thesis by auto
qed

```

```

lemma task-setscheduler-wsc-e:
  assumes p0: reachable0 s
  and p1: reachable0 t
  and p2:  $e = \text{TskEvt } ((\text{Event-task-setscheduler } pid \ p))$ 
  and p3:  $s \sim d \sim t$ 
  and p4:  $(\text{the } (\text{domain-of-event } e)) @ s \ d$ 
  and p5:  $s \sim (\text{the } (\text{domain-of-event } e)) \sim t$ 
  and p6:  $s' = \text{exec-event } s \ e$ 
  and p7:  $t' = \text{exec-event } t \ e$ 
  shows  $s' \sim d \sim t'$ 
  proof -
    {
      have a0 :  $(\text{the } (\text{domain-of-event } e)) = pid$ 
        using p2 domain-of-event-def getpid-from-tsk-event-def
        by force
      have a1:  $s' = \text{fst}(\text{task-setscheduler } s \ pid \ p)$ 
        using p2 p6 exec-event-def by auto
      have a2:  $t' = \text{fst}(\text{task-setscheduler } t \ pid \ p)$ 
        using p2 p7 exec-event-def
        by auto
      have a3:  $pid @ s \ d$ 
        using p4 a0
        by blast
      have a4 :  $s \sim pid \sim t$  using p5 a0
        by blast
      have a5:  $s' \sim d \sim t'$ 
        using a1 a2 a3 a4 p0 p1 p3 p5 p4 task-setscheduler-wsc
        by blast
    }
    then show ?thesis by auto
  qed

```

```

lemma task-setscheduler-dwsc-e: dynamic-weakly-step-consistent-e ( TskEvt ((Event-task-setscheduler
pid p)))
  using dynamic-weakly-step-consistent-e-def task-setscheduler-wsc-e
  by blast

```

29.34.13 proving "task_getscheduler" satisfying the "weaklystepconsistent" property

```

lemma task-getscheduler-wsc:
  assumes p0: reachable0 s
  and p1: reachable0 t

```

```

and p2:  $s \sim d \sim t$ 
and p3:  $pid @ s d$ 
and p4:  $s \sim pid \sim t$ 
and p5:  $s' = fst(task-getscheduler\ s\ pid\ p)$ 
and p6:  $t' = fst(task-getscheduler\ t\ pid\ p)$ 
shows  $s' \sim d \sim t'$ 
proof -
{
  have a0 :  $s = s'$ 
    using p5 task-getscheduler-def
    by (smt fstI)
  have a1 :  $t = t'$ 
    using p6 task-getscheduler-def
    by (smt fst-conv)
  have a2:  $s' \sim d \sim t'$ 
    using a0 a1 p2
    by blast
}
then show ?thesis by auto
qed

lemma task-getscheduler-wsc-e:
assumes p0:  $reachable0\ s$ 
and p1:  $reachable0\ t$ 
and p2:  $e = TskEvt\ ((Event-task-getscheduler\ pid\ p))$ 
and p3:  $s \sim d \sim t$ 
and p4:  $(the\ (domain-of-event\ e)) @ s\ d$ 
and p5:  $s \sim (the\ (domain-of-event\ e)) \sim t$ 
and p6:  $s' = exec-event\ s\ e$ 
and p7:  $t' = exec-event\ t\ e$ 
shows  $s' \sim d \sim t'$ 
proof -
{
  have a0 :  $(the\ (domain-of-event\ e)) = pid$ 
    using p2 domain-of-event-def getpid-from-tsk-event-def
    by force
  have a1:  $s' = fst(task-getscheduler\ s\ pid\ p)$ 
    using p2 p6 exec-event-def by auto
  have a2:  $t' = fst(task-getscheduler\ t\ pid\ p)$ 
    using p2 p7 exec-event-def
    by auto
  have a3:  $pid @ s\ d$ 
    using p4 a0
    by blast
  have a4 :  $s \sim pid \sim t$  using p5 a0
    by blast
  have a5:  $s' \sim d \sim t'$ 
    using a1 a2 a3 a4 p0 p1 p3 p5 p4 task-getscheduler-wsc
    by blast
}

```

```

    }
  then show ?thesis by auto
qed

```

```

lemma task-getscheduler-dwsc-e: dynamic-weakly-step-consistent-e ( TskEvt ((Event-task-getscheduler
pid p)))
  using dynamic-weakly-step-consistent-e-def task-getscheduler-wsc-e
  by blast

```

29.34.14 proving "task_movememory" satisfying the "weakly step consistent" property

```

lemma task-movememory-wsc:
  assumes p0: reachable0 s
    and p1: reachable0 t
    and p2: s ~ d ~ t
    and p3: pid @ s d
    and p4: s ~ pid ~ t
    and p5: s' = fst(task-movememory s pid p)
    and p6: t' = fst(task-movememory t pid p)
  shows s' ~ d ~ t'
  proof -
  {
    have a0 : s = s'
      using p5 task-movememory-def
      by (smt fstI)
    have a1 : t = t'
      using p6 task-movememory-def
      by (smt fst-conv)
    have a2: s' ~ d ~ t'
      using a0 a1 p2
      by blast
  }
  then show ?thesis by auto
qed

```

```

lemma task-movememory-wsc-e:
  assumes p0: reachable0 s
    and p1: reachable0 t
    and p2: e = TskEvt ((Event-task-movememory pid p))
    and p3: s ~ d ~ t
    and p4: (the (domain-of-event e)) @ s d
    and p5: s ~ (the (domain-of-event e)) ~ t
    and p6: s' = exec-event s e
    and p7: t' = exec-event t e
  shows s' ~ d ~ t'
  proof -
  {
    have a0 : (the (domain-of-event e)) = pid
      using p2 domain-of-event-def getpid-from-tsk-event-def

```

```

    by force
  have a1:  $s' = fst(task-movememory\ s\ pid\ p)$ 
    using p2 p6 exec-event-def by auto
  have a2:  $t' = fst(task-movememory\ t\ pid\ p)$ 
    using p2 p7 exec-event-def
    by auto
  have a3:  $pid @ s d$ 
    using p4 a0
    by blast
  have a4 :  $s \sim pid \sim t$  using p5 a0
    by blast
  have a5:  $s' \sim d \sim t'$ 
    using a1 a2 a3 a4 p0 p1 p3 p5 p4 task-movememory-wsc
    by blast
}
then show ?thesis by auto
qed

```

```

lemma task-movememory-dwsc-e: dynamic-weakly-step-consistent-e (TskEvt ((Event-task-movememory
pid p)))
  using dynamic-weakly-step-consistent-e-def task-movememory-wsc-e
  by blast

```

29.34.15 proving "task_{kill}" satisfying the "weakly step consistent" property

```

lemma task-kill-wsc:
  assumes p0: reachable0 s
    and p1: reachable0 t
    and p2:  $s \sim d \sim t$ 
    and p3:  $pid @ s\ d$ 
    and p4:  $s \sim pid \sim t$ 
    and p5:  $s' = fst(task-kill\ s\ pid\ p\ sinfo\ i\ c)$ 
    and p6:  $t' = fst(task-kill\ t\ pid\ p\ sinfo\ i\ c)$ 
  shows  $s' \sim d \sim t'$ 
  proof -
  {
    have a0 :  $s = s'$ 
      using p5 task-kill-def
      by (smt fstI)
    have a1 :  $t = t'$ 
      using p6 task-kill-def
      by (smt fst-conv)
    have a2:  $s' \sim d \sim t'$ 
      using a0 a1 p2
      by blast
  }
  then show ?thesis by auto
qed

```

```

lemma task-kill-wsc-e:
  assumes  $p0$ : reachable0  $s$ 
    and  $p1$ : reachable0  $t$ 
    and  $p2$ :  $e = \text{TskEvt } ((\text{Event-task-kill } \text{pid } p \text{ sinfo } i \text{ } c))$ 
    and  $p3$ :  $s \sim d \sim t$ 
    and  $p4$ :  $(\text{the } (\text{domain-of-event } e)) @ s \text{ } d$ 
    and  $p5$ :  $s \sim (\text{the } (\text{domain-of-event } e)) \sim t$ 
    and  $p6$ :  $s' = \text{exec-event } s \text{ } e$ 
    and  $p7$ :  $t' = \text{exec-event } t \text{ } e$ 
  shows  $s' \sim d \sim t'$ 
  proof –
    {
      have  $a0$  :  $(\text{the } (\text{domain-of-event } e)) = \text{pid}$ 
        using  $p2$  domain-of-event-def getpid-from-tsk-event-def
        by force
      have  $a1$ :  $s' = \text{fst}(\text{task-kill } s \text{ pid } p \text{ sinfo } i \text{ } c)$ 
        using  $p2$   $p6$  exec-event-def by auto
      have  $a2$ :  $t' = \text{fst}(\text{task-kill } t \text{ pid } p \text{ sinfo } i \text{ } c)$ 
        using  $p2$   $p7$  exec-event-def
        by auto
      have  $a3$ :  $\text{pid} @ s \text{ } d$ 
        using  $p4$   $a0$ 
        by blast
      have  $a4$  :  $s \sim \text{pid} \sim t$  using  $p5$   $a0$ 
        by blast
      have  $a5$ :  $s' \sim d \sim t'$ 
        using  $a1$   $a2$   $a3$   $a4$   $p0$   $p1$   $p3$   $p5$   $p4$  task-kill-wsc
        by blast
    }
  then show ?thesis by auto
qed

```

```

lemma task-kill-dwsc-e: dynamic-weakly-step-consistent-e ( $\text{TskEvt } ((\text{Event-task-kill } \text{pid } p \text{ sinfo } i \text{ } c)))$ 
  using dynamic-weakly-step-consistent-e-def task-kill-wsc-e
  by blast

```

29.34.16 proving "task_prctl" satisfying the "weakly step consistent" property

```

lemma task-prctl-wsc:
  assumes  $p0$ : reachable0  $s$ 
    and  $p1$ : reachable0  $t$ 
    and  $p2$ :  $s \sim d \sim t$ 
    and  $p3$ :  $\text{pid} @ s \text{ } d$ 
    and  $p4$ :  $s \sim \text{pid} \sim t$ 
    and  $p5$ :  $s' = \text{fst}(\text{task-prctl } s \text{ pid } \text{op } \text{arg2 } \text{arg3 } \text{arg4 } \text{arg5})$ 
    and  $p6$ :  $t' = \text{fst}(\text{task-prctl } t \text{ pid } \text{op } \text{arg2 } \text{arg3 } \text{arg4 } \text{arg5})$ 
  shows  $s' \sim d \sim t'$ 
  proof –

```

```

{
  have a0 : s = s'
    using p5 task-prctl-def
    by (smt fstI)
  have a1 : t = t'
    using p6 task-prctl-def
    by (smt fst-conv)
  have a2: s' ~ d ~ t'
    using a0 a1 p2
    by blast
}
then show ?thesis by auto
qed

```

```

lemma task-prctl-wsc-e:
  assumes p0: reachable0 s
    and p1: reachable0 t
    and p2: e = TskEvt ((Event-task-prctl pid op arg2 arg3 arg4 arg5))
    and p3: s ~ d ~ t
    and p4: (the (domain-of-event e)) @ s d
    and p5: s ~ (the (domain-of-event e)) ~ t
    and p6: s' = exec-event s e
    and p7: t' = exec-event t e
  shows s' ~ d ~ t'
  proof -
    {
      have a0 : (the (domain-of-event e)) = pid
        using p2 domain-of-event-def getpid-from-tsk-event-def
        by force
      have a1: s' = fst(task-prctl s pid op arg2 arg3 arg4 arg5)
        using p2 p6 exec-event-def by auto
      have a2: t' = fst(task-prctl t pid op arg2 arg3 arg4 arg5)
        using p2 p7 exec-event-def
        by auto
      have a3: pid @ s d
        using p4 a0
        by blast
      have a4 : s ~ pid ~ t using p5 a0
        by blast
      have a5: s' ~ d ~ t'
        using a1 a2 a3 a4 p0 p1 p3 p5 p4 task-prctl-wsc
        by blast
    }
    then show ?thesis by auto
  qed

```

```

lemma task-prctl-dwsc-e: dynamic-weakly-step-consistent-e (TskEvt ((Event-task-prctl
pid op arg2 arg3 arg4 arg5)))
  using dynamic-weakly-step-consistent-e-def task-prctl-wsc-e

```

by *blast*

29.35 smack ptrace hooks weakly step consistent

29.35.1 proving "ptrace_{mayaccess}" satisfying the "weakly step consistent" property

lemma *ptrace-may-access-wsc*:

```

assumes p0: reachable0 s
  and p1: reachable0 t
  and p2: s ~ d ~ t
  and p3: pid @ s d
  and p4: s ~ pid ~ t
  and p5: s' = fst(ptrace-may-access s pid p m)
  and p6: t' = fst(ptrace-may-access t pid p m)
shows s' ~ d ~ t'
proof -
{
  have a0 : s = s'
    using p5 ptrace-may-access-def
    by simp
  have a1 : t = t'
    using p6 ptrace-may-access-def
    by simp
  have a2: s' ~ d ~ t'
    using a0 a1 p2 by blast
}
then show ?thesis by auto
qed

```

lemma *ptrace-may-access-wsc-e*:

```

assumes p0: reachable0 s
  and p1: reachable0 t
  and p2: e = PtraceEvt (Event-ptrace-access-check pid p m)
  and p3: s ~ d ~ t
  and p4: (the (domain-of-event e)) @ s d
  and p5: s ~ (the (domain-of-event e)) ~ t
  and p6: s' = exec-event s e
  and p7: t' = exec-event t e
shows s' ~ d ~ t'
proof -
{
  have a0 : (the (domain-of-event e)) = pid
    using p2 domain-of-event-def getpid-from-pttrace-event-def
    by force
  have a1: s' = fst(ptrace-may-access s pid p m)
    using p2 p6 exec-event-def by auto
  have a2: t' = fst(ptrace-may-access t pid p m)
    using p2 p7 exec-event-def
    by auto
  have a3: pid @ s d

```



```

    using p4 a0
    by blast
  have a4 : s ~ pid ~ t using p5 a0
    by blast
  have a5: s' ~ d ~ t'
    using a1 a2 a3 a4 p0 p1 p3 p5 p4 ptrace-may-access-wsc
    by blast
}
then show ?thesis by auto
qed
lemma ptrace-may-access-dwsc-e: dynamic-weakly-step-consistent-e ( PtraceEvt (Event-ptrace-access-check
pid p m))
  using dynamic-weakly-step-consistent-e-def ptrace-may-access-wsc-e by blast

```

29.35.2 proving "ptrace_traceme" satisfying the "weakly step consistent" property

```

lemma ptrace-traceme-wsc:
  assumes p0: reachable0 s
    and p1: reachable0 t
    and p2: s ~ d ~ t
    and p3: pid @ s d
    and p4: s ~ pid ~ t
    and p5: s' = fst(ptrace-traceme s pid )
    and p6: t' = fst(ptrace-traceme t pid )
  shows s' ~ d ~ t'
  proof -
  {
    have a0 : s = s'
      using p5 ptrace-traceme-def
      by simp
    have a1 : t = t'
      using p6 ptrace-traceme-def
      by simp
    have a2: s' ~ d ~ t'
      using a0 a1 p2 by blast
  }
  then show ?thesis by auto
qed

```

```

lemma ptrace-traceme-wsc-e:
  assumes p0: reachable0 s
    and p1: reachable0 t
    and p2: e = PtraceEvt (Event-ptrace-traceme pid )
    and p3: s ~ d ~ t
    and p4: (the (domain-of-event e)) @ s d
    and p5: s ~ (the (domain-of-event e)) ~ t
    and p6: s' = exec-event s e
    and p7: t' = exec-event t e
  shows s' ~ d ~ t'

```

```

proof -
{
  have a0 : (the (domain-of-event e)) = pid
    using p2 domain-of-event-def getpid-from-pttrace-event-def
    by force
  have a1 : s' = fst(pttrace-traceme s pid )
    using p2 p6 exec-event-def by auto
  have a2 : t' = fst(pttrace-traceme t pid )
    using p2 p7 exec-event-def
    by auto
  have a3 : pid @ s d
    using p4 a0
    by blast
  have a4 : s ~ pid ~ t using p5 a0
    by blast
  have a5 : s' ~ d ~ t'
    using a1 a2 a3 a4 p0 p1 p3 p5 p4 pttrace-traceme-wsc
    by blast
}
then show ?thesis by auto
qed
lemma pttrace-traceme-dwsc-e: dynamic-weakly-step-consistent-e (PtraceEvt (Event-pttrace-traceme
pid))
  using dynamic-weakly-step-consistent-e-def pttrace-traceme-wsc-e by blast

```

29.35.3 proving "check_{syslog}permissions" satisfying the "weakly step consistent" property

```

lemma check-syslog-permissions-wsc:
  assumes p0: reachable0 s
    and p1: reachable0 t
    and p2: s ~ d ~ t
    and p3: pid @ s d
    and p4: s ~ pid ~ t
    and p5: s' = fst( check-syslog-permissions s pid tp)
    and p6: t' = fst( check-syslog-permissions t pid tp)
  shows s' ~ d ~ t'
  proof -
  {
    have a0 : s = s'
      using p5 check-syslog-permissions-def
      by (smt fstI)
    have a1 : t = t'
      using p6 check-syslog-permissions-def
      by (smt fst-conv)
    have a2 : s' ~ d ~ t'
      using a0 a1 p2
      by blast
  }
  then show ?thesis by auto

```

qed

lemma *check-syslog-permissions-wsc-e*:

```

assumes p0: reachable0 s
  and p1: reachable0 t
  and p2: e = SysEvt( Event-smack-syslog pid tp )
  and p3: s ~ d ~ t
  and p4: (the (domain-of-event e)) @ s d
  and p5: s ~ (the (domain-of-event e)) ~ t
  and p6: s' = exec-event s e
  and p7: t' = exec-event t e
shows s' ~ d ~ t'
proof -
  {
    have a0 : (the (domain-of-event e)) = pid
      using p2 domain-of-event-def getpid-from-sys-event-def
      by force
    have a1: s' = fst( check-syslog-permissions s pid tp )
      using p2 p6 exec-event-def by auto
    have a2: t' = fst( check-syslog-permissions t pid tp )
      using p2 p7 exec-event-def
      by auto
    have a3: pid @ s d
      using p4 a0
      by blast
    have a4 : s ~ pid ~ t using p5 a0
      by blast
    have a5: s' ~ d ~ t'
      using a1 a2 a3 a4 p0 p1 p3 p5 p4 check-syslog-permissions-wsc
      by blast
  }
  then show ?thesis by auto

```

qed

lemma *check-syslog-permissions-dwsc-e*: *dynamic-weakly-step-consistent-e* (SysEvt(Event-smack-syslog pid t))

```

using dynamic-weakly-step-consistent-e-def check-syslog-permissions-wsc-e
by blast

```

29.35.4 proving "prepare_{binprm}" satisfying the "weakly step consistent" property

lemma *prepare-binprm-wsc*:

```

assumes p0: reachable0 s
  and p1: reachable0 t
  and p2: s ~ d ~ t
  and p3: pid @ s d
  and p4: s ~ pid ~ t
  and p5: s' = fst(prepare-binprm s pid bprm)
  and p6: t' = fst(prepare-binprm t pid bprm)

```

```

shows  $s' \sim d \sim t'$ 
proof -
{
  have  $a0 : s = s'$ 
    using  $p5$  prepare-binprm-def
  proof -
    have  $s = s' \vee \text{resultValue } s \text{ (security-bprm-set-creds } s \text{ bprm)} = 0$ 
      using  $p5$  prepare-binprm-def by force
    then show ?thesis
      using  $p5$  prepare-binprm-def by fastforce
  qed
  have  $a1 : t = t'$ 
    using  $p6$  prepare-binprm-def
    by (smt fstI)
  have  $a2 : s' \sim d \sim t'$ 
    using  $a0$   $a1$   $p2$ 
    by blast
}
then show ?thesis by auto
qed

```

```

lemma prepare-binprm-wsc-e:
  assumes  $p0 : \text{reachable0 } s$ 
    and  $p1 : \text{reachable0 } t$ 
    and  $p2 : e = \text{SysEvt( Event-prepare-binprm pid bprm)}$ 
    and  $p3 : s \sim d \sim t$ 
    and  $p4 : (\text{the (domain-of-event } e)) @ s \ d$ 
    and  $p5 : s \sim (\text{the (domain-of-event } e)) \sim t$ 
    and  $p6 : s' = \text{exec-event } s \ e$ 
    and  $p7 : t' = \text{exec-event } t \ e$ 
  shows  $s' \sim d \sim t'$ 
  proof -
    {
      have  $a0 : (\text{the (domain-of-event } e)) = \text{pid}$ 
        using  $p2$  domain-of-event-def getpid-from-sys-event-def
        by force
      have  $a1 : s' = \text{fst}(\text{prepare-binprm } s \ \text{pid} \ \text{bprm})$ 
        using  $p2$   $p6$  exec-event-def by auto
      have  $a2 : t' = \text{fst}(\text{prepare-binprm } t \ \text{pid} \ \text{bprm})$ 
        using  $p2$   $p7$  exec-event-def
        by auto
      have  $a3 : \text{pid} @ s \ d$ 
        using  $p4$   $a0$ 
        by blast
      have  $a4 : s \sim \text{pid} \sim t$  using  $p5$   $a0$ 
        by blast
      have  $a5 : s' \sim d \sim t'$ 
        using  $a1$   $a2$   $a3$   $a4$   $p0$   $p1$   $p3$   $p5$   $p4$  prepare-binprm-wsc
        by blast
    }
  qed

```

```

    }
  then show ?thesis by auto
qed

```

```

lemma prepare-binprm-dwsc-e: dynamic-weakly-step-consistent-e (SysEvt( Event-prepare-binprm
pid bprm))
  using dynamic-weakly-step-consistent-e-def prepare-binprm-wsc-e
  by blast

```

29.36 smack ipc hooks weakly step consistent

29.36.1 proving "ipcperms" satisfying the "weakly step consistent" property

```

lemma ipcperms-wsc:
  assumes p0: reachable0 s
    and p1: reachable0 t
    and p2: s ~ d ~ t
    and p3: pid @ s d
    and p4: s ~ pid ~ t
    and p5: s' = fst(ipcperms s pid ipcp flg)
    and p6: t' = fst(ipcperms t pid ipcp flg)
  shows s' ~ d ~ t'
  proof -
  {
    have a0 : s = s'
      using p5 ipcperms-def
      by simp
    have a1 : t = t'
      using p6 ipcperms-def
      by (smt fstI)
    have a2: s' ~ d ~ t'
      using a0 a1 p2
      by blast
  }
  then show ?thesis by auto
qed

```

```

lemma ipcperms-wsc-e:
  assumes p0: reachable0 s
    and p1: reachable0 t
    and p2: e = KIpEvt( (Event-ipc-permission pid ipcp flg ))
    and p3: s ~ d ~ t
    and p4: (the (domain-of-event e)) @ s d
    and p5: s ~ (the (domain-of-event e)) ~ t
    and p6: s' = exec-event s e
    and p7: t' = exec-event t e
  shows s' ~ d ~ t'
  proof -
  {

```

```

have a0 : (the (domain-of-event e)) = pid
  using p2 domain-of-event-def getpid-from-kern-ipc-event-def
  by force
have a1 : s' = fst(ipcperms s pid ipcp flg)
  using p2 p6 exec-event-def by auto
have a2 : t' = fst(ipcperms t pid ipcp flg)
  using p2 p7 exec-event-def
  by auto
have a3 : pid @ s d
  using p4 a0
  by blast
have a4 : s ~ pid ~ t using p5 a0
  by blast
have a5 : s' ~ d ~ t'
  using a1 a2 a3 a4 p0 p1 p3 p5 p4 ipcperms-wsc
  by blast
}
then show ?thesis by auto
qed

```

```

lemma ipcperms-dwsc-e: dynamic-weakly-step-consistent-e (KIpEvt(( Event-ipc-permission
pid ipcp flg )))
  using dynamic-weakly-step-consistent-e-def ipcperms-wsc-e
  by blast

```

29.36.2 proving "audit_{ipc_obj}" satisfying the "weakly step consistent" property

```

lemma audit-ipc-obj-wsc:
  assumes p0: reachable0 s
    and p1: reachable0 t
    and p2: s ~ d ~ t
    and p3: pid @ s d
    and p4: s ~ pid ~ t
    and p5: s' = fst(audit-ipc-obj s pid ipcp)
    and p6: t' = fst(audit-ipc-obj t pid ipcp)
  shows s' ~ d ~ t'
  proof -
  {
    have a0 : s = s'
      using p5 audit-ipc-obj-def
      by simp
    have a1 : t = t'
      using p6 audit-ipc-obj-def
      by force
    have a2: s' ~ d ~ t'
      using a0 a1 p2
      by blast
  }
  then show ?thesis by auto

```

qed

```

lemma audit-ipc-obj-wsc-e:
  assumes p0: reachable0 s
    and p1: reachable0 t
    and p2: e = KIpEvt( (Event-ipc-getsecid pid ipcp) )
    and p3: s ~ d ~ t
    and p4: (the (domain-of-event e)) @ s d
    and p5: s ~ (the (domain-of-event e)) ~ t
    and p6: s' = exec-event s e
    and p7: t' = exec-event t e
  shows s' ~ d ~ t'
proof -
  {
    have a0 : (the (domain-of-event e)) = pid
      using p2 domain-of-event-def getpid-from-kern-ipc-event-def
      by force
    have a1: s' = fst(audit-ipc-obj s pid ipcp)
      using p2 p6 exec-event-def by auto
    have a2: t' = fst(audit-ipc-obj t pid ipcp)
      using p2 p7 exec-event-def
      by auto
    have a3: pid @ s d
      using p4 a0
      by blast
    have a4 : s ~ pid ~ t using p5 a0
      by blast
    have a5: s' ~ d ~ t'
      using a1 a2 a3 a4 p0 p1 p3 p5 p4 audit-ipc-obj-wsc
      by blast
  }
  then show ?thesis by auto
qed

```

```

lemma audit-ipc-obj-dwsc-e: dynamic-weakly-step-consistent-e (KIpEvt( (Event-ipc-getsecid
pid ipcp )))
  using dynamic-weakly-step-consistent-e-def audit-ipc-obj-wsc-e
  by blast

```

29.36.3 proving "ksys_msgget" satisfying the "weakly step consistent" property

```

lemma ksys-msgget-wsc:
  assumes p0: reachable0 s
    and p1: reachable0 t
    and p2: s ~ d ~ t
    and p3: pid @ s d
    and p4: s ~ pid ~ t
    and p5: s' = fst(ksys-msgget s pid msq msqflg)
    and p6: t' = fst(ksys-msgget t pid msq msqflg)

```

```

shows  $s' \sim d \sim t'$ 
proof -
{
  have  $a0 : s = s'$ 
    using  $p5$  ksys-msgget-def
    by simp
  have  $a1 : t = t'$ 
    using  $p6$  ksys-msgget-def
    by (smt fstI)
  have  $a2: s' \sim d \sim t'$ 
    using  $a0$   $a1$   $p2$ 
    by blast
}
then show ?thesis by auto
qed

```

```

lemma ksys-msgget-wsc-e:
assumes  $p0: \text{reachable0 } s$ 
and  $p1: \text{reachable0 } t$ 
and  $p2: e = \text{KIPCvt}(\text{Event-msg-queue-associate } pid \text{ msq msqflg })$ 
and  $p3: s \sim d \sim t$ 
and  $p4: (\text{the } (\text{domain-of-event } e)) @ s d$ 
and  $p5: s \sim (\text{the } (\text{domain-of-event } e)) \sim t$ 
and  $p6: s' = \text{exec-event } s e$ 
and  $p7: t' = \text{exec-event } t e$ 
shows  $s' \sim d \sim t'$ 
proof -
{
  have  $a0 : (\text{the } (\text{domain-of-event } e)) = pid$ 
    using  $p2$  domain-of-event-def getpid-from-kern-ipc-event-def
    by force
  have  $a1: s' = \text{fst}(\text{ksys-msgget } s \text{ pid msq msqflg})$ 
    using  $p2$   $p6$  exec-event-def by auto
  have  $a2: t' = \text{fst}(\text{ksys-msgget } t \text{ pid msq msqflg})$ 
    using  $p2$   $p7$  exec-event-def
    by auto
  have  $a3: pid @ s d$ 
    using  $p4$   $a0$ 
    by blast
  have  $a4 : s \sim pid \sim t$  using  $p5$   $a0$ 
    by blast
  have  $a5: s' \sim d \sim t'$ 
    using  $a1$   $a2$   $a3$   $a4$   $p0$   $p1$   $p3$   $p5$   $p4$  ksys-msgget-wsc
    by blast
}
then show ?thesis by auto
qed

```

```

lemma ksys-msgget-dwsc-e: dynamic-weakly-step-consistent-e (KIPCvt (Event-msg-queue-associate

```



```

pid msq msqflg )))
  using dynamic-weakly-step-consistent-e-def ksys-msgget-wsc-e
  by blast

```

29.36.4 proving "msg_{queue}msgctl" satisfying the "weakly step consistent" property

```

lemma msg-queue-msgctl-wsc:
  assumes p0: reachable0 s
    and p1: reachable0 t
    and p2: s ~ d ~ t
    and p3: pid @ s d
    and p4: s ~ pid ~ t
    and p5: s' = fst(msg-queue-msgctl s pid msq cmd)
    and p6: t' = fst(msg-queue-msgctl t pid msq cmd)
  shows s' ~ d ~ t'
  proof -
  {
    have a0 : s = s'
      using p5 msg-queue-msgctl-def
      by simp
    have a1 : t = t'
      using p6 msg-queue-msgctl-def
      by auto
    have a2: s' ~ d ~ t'
      using a0 a1 p2
      by blast
  }
  then show ?thesis by auto
qed

```

```

lemma msg-queue-msgctl-wsc-e:
  assumes p0: reachable0 s
    and p1: reachable0 t
    and p2: e = KIpEvt( (Event-msg-queue-msgctl pid msq cmd) )
    and p3: s ~ d ~ t
    and p4: (the (domain-of-event e)) @ s d
    and p5: s ~ (the (domain-of-event e)) ~ t
    and p6: s' = exec-event s e
    and p7: t' = exec-event t e
  shows s' ~ d ~ t'
  proof -
  {
    have a0 : (the (domain-of-event e)) = pid
      using p2 domain-of-event-def getpid-from-kern-ipc-event-def
      by force
    have a1: s' = fst(msg-queue-msgctl s pid msq cmd)
      using p2 p6 exec-event-def by auto
    have a2: t' = fst(msg-queue-msgctl t pid msq cmd)
      using p2 p7 exec-event-def

```

```

    by auto
  have a3: pid @ s d
    using p4 a0
  by blast
  have a4 : s ~ pid ~ t using p5 a0
  by blast
  have a5: s' ~ d ~ t'
    using a1 a2 a3 a4 p0 p1 p3 p5 p4 msg-queue-msgctl-wsc
  by blast
}
then show ?thesis by auto
qed

```

```

lemma msg-queue-msgctl-dwsc-e: dynamic-weakly-step-consistent-e ( KIpEvt((Event-msg-queue-msgctl
pid msq cmd )))
  using dynamic-weakly-step-consistent-e-def msg-queue-msgctl-wsc-e
  by blast

```

29.36.5 proving "do_msgsnd" satisfying the "weakly step consistent" property

```

lemma do-msgsnd-wsc:
  assumes p0: reachable0 s
    and p1: reachable0 t
    and p2: s ~ d ~ t
    and p3: pid @ s d
    and p4: s ~ pid ~ t
    and p5: s' = fst(do-msgsnd s pid msq msg msgflg)
    and p6: t' = fst(do-msgsnd t pid msq msg msgflg)
  shows s' ~ d ~ t'
  proof -
  {
    have a0 : s = s'
      using p5 do-msgsnd-def
      by (smt do-msgsnd-def fst-conv p5)
    have a1 : t = t'
      using p6 do-msgsnd-def
      by (smt fstI)
    have a2: s' ~ d ~ t'
      using a0 a1 p2
      by blast
  }
  then show ?thesis by auto
qed

```

```

lemma do-msgsnd-wsc-e:
  assumes p0: reachable0 s
    and p1: reachable0 t
    and p2: e = KIpEvt( (Event-msg-queue-msgsnd pid msq msg msgflg))
    and p3: s ~ d ~ t

```

```

and p4: (the (domain-of-event e)) @ s d
and p5: s ~ (the (domain-of-event e)) ~ t
and p6: s' = exec-event s e
and p7: t' = exec-event t e
shows s' ~ d ~ t'
proof -
{
have a0: (the (domain-of-event e)) = pid
  using p2 domain-of-event-def getpid-from-kern-ipc-event-def
  by force
have a1: s' = fst(do-msgsnd s pid msq msg msgflg)
  using p2 p6 exec-event-def by auto
have a2: t' = fst(do-msgsnd t pid msq msg msgflg)
  using p2 p7 exec-event-def
  by auto
have a3: pid @ s d
  using p4 a0
  by blast
have a4: s ~ pid ~ t using p5 a0
  by blast
have a5: s' ~ d ~ t'
  using a1 a2 a3 a4 p0 p1 p3 p5 p4 do-msgsnd-wsc
  by blast
}
then show ?thesis by auto
qed

```

```

lemma do-msgsnd-dwsc-e: dynamic-weakly-step-consistent-e ( KIpEvt( (Event-msg-queue-msgsnd
pid msq msg msgflg)))
  using dynamic-weakly-step-consistent-e-def do-msgsnd-wsc-e
  by blast

```

29.36.6 proving "msg_{queue}_msgrcv" satisfying the "weakly step consistent" property

```

lemma msg-queue-msgrcv-wsc:
assumes p0: reachable0 s
and p1: reachable0 t
and p2: s ~ d ~ t
and p3: pid @ s d
and p4: s ~ pid ~ t
and p5: s' = fst(msg-queue-msgrcv s pid isp msq p long msgflg)
and p6: t' = fst(msg-queue-msgrcv t pid isp msq p long msgflg)
shows s' ~ d ~ t'
proof -
{
have a0: s = s'
  using p5 msg-queue-msgrcv-def
  by simp
have a1: t = t'

```

```

    using p6 msg-queue-msgrcv-def
    by auto
  have a2:  $s' \sim d \sim t'$ 
    using a0 a1 p2
    by blast
}
then show ?thesis by auto
qed

```

```

lemma msg-queue-msgrcv-wsc-e:
  assumes p0: reachable0 s
  and p1: reachable0 t
  and p2:  $e = KIpEvt( (Event\text{-}msg\text{-}queue\text{-}msgrcv\ pid\ isp\ msq\ p\ long\ msgflg))$ 
  and p3:  $s \sim d \sim t$ 
  and p4:  $(the\ (domain\text{-}of\text{-}event\ e)) @ s\ d$ 
  and p5:  $s \sim (the\ (domain\text{-}of\text{-}event\ e)) \sim t$ 
  and p6:  $s' = exec\text{-}event\ s\ e$ 
  and p7:  $t' = exec\text{-}event\ t\ e$ 
  shows  $s' \sim d \sim t'$ 
  proof -
  {
    have a0 :  $(the\ (domain\text{-}of\text{-}event\ e)) = pid$ 
      using p2 domain-of-event-def getpid-from-kern-ipc-event-def
      by force
    have a1:  $s' = fst(msg\text{-}queue\text{-}msgrcv\ s\ pid\ isp\ msq\ p\ long\ msgflg)$ 
      using p2 p6 exec-event-def by auto
    have a2:  $t' = fst(msg\text{-}queue\text{-}msgrcv\ t\ pid\ isp\ msq\ p\ long\ msgflg)$ 
      using p2 p7 exec-event-def
      by auto
    have a3:  $pid @ s\ d$ 
      using p4 a0
      by blast
    have a4 :  $s \sim pid \sim t$  using p5 a0
      by blast
    have a5:  $s' \sim d \sim t'$ 
      using a1 a2 a3 a4 p0 p1 p3 p5 p4 msg-queue-msgrcv-wsc
      by blast
  }
  then show ?thesis by auto
qed

```

```

lemma msg-queue-msgrcv-dwsc-e: dynamic-weakly-step-consistent-e ( $KIpEvt( (Event\text{-}msg\text{-}queue\text{-}msgrcv\ pid\ isp\ msq\ p\ long\ msgflg))$ )
  using dynamic-weakly-step-consistent-e-def msg-queue-msgrcv-wsc-e
  by blast

```

29.36.7 proving "ksys_{shmget}" satisfying the "weakly step consistent" property

```

lemma ksys-shmget-wsc:

```

```

assumes p0: reachable0 s
  and p1: reachable0 t
  and p2:  $s \sim d \sim t$ 
  and p3:  $\text{pid} @ s d$ 
  and p4:  $s \sim \text{pid} \sim t$ 
  and p5:  $s' = \text{fst}(\text{ksys-shmget } s \text{ pid shm shmflg})$ 
  and p6:  $t' = \text{fst}(\text{ksys-shmget } t \text{ pid shm shmflg})$ 
shows  $s' \sim d \sim t'$ 
proof –
{
  have a0 :  $s = s'$ 
    using p5 ksys-shmget-def
    by simp
  have a1 :  $t = t'$ 
    using p6 ksys-shmget-def
    by auto
  have a2:  $s' \sim d \sim t'$ 
    using a0 a1 p2
    by blast
}
then show ?thesis by auto
qed

```

```

lemma ksys-shmget-wsc-e:
assumes p0: reachable0 s
  and p1: reachable0 t
  and p2:  $e = \text{KIpEvt}(\text{Event-shm-associate pid shm shmflg})$ 
  and p3:  $s \sim d \sim t$ 
  and p4:  $(\text{the}(\text{domain-of-event } e)) @ s d$ 
  and p5:  $s \sim (\text{the}(\text{domain-of-event } e)) \sim t$ 
  and p6:  $s' = \text{exec-event } s e$ 
  and p7:  $t' = \text{exec-event } t e$ 
shows  $s' \sim d \sim t'$ 
proof –
{
  have a0 :  $(\text{the}(\text{domain-of-event } e)) = \text{pid}$ 
    using p2 domain-of-event-def getpid-from-kern-ipc-event-def
    by force
  have a1:  $s' = \text{fst}(\text{ksys-shmget } s \text{ pid shm shmflg})$ 
    using p2 p6 exec-event-def by auto
  have a2:  $t' = \text{fst}(\text{ksys-shmget } t \text{ pid shm shmflg})$ 
    using p2 p7 exec-event-def
    by auto
  have a3:  $\text{pid} @ s d$ 
    using p4 a0
    by blast
  have a4 :  $s \sim \text{pid} \sim t$  using p5 a0
    by blast
  have a5:  $s' \sim d \sim t'$ 

```

```

      using a1 a2 a3 a4 p0 p1 p3 p4 p5 ksys-shmget-wsc
      by blast
    }
  then show ?thesis by auto
qed

```

```

lemma ksys-shmget-dwsc-e: dynamic-weakly-step-consistent-e (KIpcEvt( (Event-shm-associate
pid shm shmflg)))
  using dynamic-weakly-step-consistent-e-def ksys-shmget-wsc-e
  by blast

```

29.36.8 proving "shm_msgctl" satisfying the "weakly step consistent" property

```

lemma shm-msgctl-wsc:
  assumes p0: reachable0 s
    and p1: reachable0 t
    and p2: s ~ d ~ t
    and p3: pid @ s d
    and p4: s ~ pid ~ t
    and p5: s' = fst(shm-msgctl s pid shm cmd)
    and p6: t' = fst(shm-msgctl t pid shm cmd)
  shows s' ~ d ~ t'
  proof -
  {
    have a0 : s = s'
      using p5 shm-msgctl-def
      by simp
    have a1 : t = t'
      using p6 shm-msgctl-def
      by auto
    have a2: s' ~ d ~ t'
      using a0 a1 p2
      by blast
  }
  then show ?thesis by auto
qed

```

```

lemma shm-msgctl-wsc-e:
  assumes p0: reachable0 s
    and p1: reachable0 t
    and p2: e = KIpcEvt( (Event-shm-shmctl pid shm cmd ))
    and p3: s ~ d ~ t
    and p4: (the (domain-of-event e)) @ s d
    and p5: s ~ (the (domain-of-event e)) ~ t
    and p6: s' = exec-event s e
    and p7: t' = exec-event t e
  shows s' ~ d ~ t'
  proof -
  {

```

```

have a0 : (the (domain-of-event e)) = pid
  using p2 domain-of-event-def getpid-from-kern-ipc-event-def
  by force
have a1: s' = fst(shm-msgctl s pid shm cmd)
  using p2 p6 exec-event-def by auto
have a2: t' = fst(shm-msgctl t pid shm cmd)
  using p2 p7 exec-event-def
  by auto
have a3: pid @ s d
  using p4 a0
  by blast
have a4 : s ~ pid ~ t using p5 a0
  by blast
have a5: s' ~ d ~ t'
  using a1 a2 a3 a4 p0 p1 p3 shm-msgctl-wsc
  by blast
}
then show ?thesis by auto
qed

```

```

lemma shm-msgctl-dwsc-e: dynamic-weakly-step-consistent-e (KIpEvt(( Event-shm-shmctl
pid shm cmd )))
  using dynamic-weakly-step-consistent-e-def shm-msgctl-wsc-e
  by blast

```

29.36.9 proving "do_shmat" satisfying the "weakly step consistent" property

```

lemma do-shmat-wsc:
  assumes p0: reachable0 s
    and p1: reachable0 t
    and p2: s ~ d ~ t
    and p3: pid @ s d
    and p4: s ~ pid ~ t
    and p5: s' = fst(do-shmat s pid shp shmaddr shmflg)
    and p6: t' = fst(do-shmat t pid shp shmaddr shmflg)
  shows s' ~ d ~ t'
  proof -
  {
    have a0 : s = s'
      using p5
      apply(simp add: do-shmat-def)
      apply auto[1]
      apply (smt fst-conv)
      by (smt eq-fst-iff)
    have a1 : t = t'
      using p6
      apply(simp add: do-shmat-def)
      apply auto[1]
      apply (smt fst-conv)

```

```

    by (smt eq-fst-iff)
  have a2:  $s' \sim d \sim t'$ 
    using a0 a1 p2
    by blast
}
then show ?thesis by auto
qed

```

```

lemma do-shmat-wsc-e:
  assumes p0: reachable0 s
  and p1: reachable0 t
  and p2:  $e = KIpEvt( (Event-shm-shmat\ pid\ shp\ shmaddr\ shmflg) )$ 
  and p3:  $s \sim d \sim t$ 
  and p4:  $(the\ (domain-of-event\ e)) @ s\ d$ 
  and p5:  $s \sim (the\ (domain-of-event\ e)) \sim t$ 
  and p6:  $s' = exec-event\ s\ e$ 
  and p7:  $t' = exec-event\ t\ e$ 
  shows  $s' \sim d \sim t'$ 
  proof -
  {
    have a0 :  $(the\ (domain-of-event\ e)) = pid$ 
      using p2 domain-of-event-def getpid-from-kern-ipc-event-def
      by force
    have a1:  $s' = fst(do-shmat\ s\ pid\ shp\ shmaddr\ shmflg)$ 
      using p2 p6 exec-event-def by auto
    have a2:  $t' = fst(do-shmat\ t\ pid\ shp\ shmaddr\ shmflg)$ 
      using p2 p7 exec-event-def
      by auto
    have a3:  $pid @ s\ d$ 
      using p4 a0
      by blast
    have a4 :  $s \sim pid \sim t$  using p5 a0
      by blast
    have a5:  $s' \sim d \sim t'$ 
      using a1 a2 a3 a4 p0 p1 p3 p5 p4 do-shmat-wsc
      by blast
  }
  then show ?thesis by auto
qed

```

```

lemma do-shmat-dwsc-e: dynamic-weakly-step-consistent-e ( $KIpEvt( (Event-shm-shmat\ pid\ shp\ shmaddr\ shmflg) )$ )
  using dynamic-weakly-step-consistent-e-def do-shmat-wsc-e
  by blast

```

29.36.10 proving "ksys_semget" satisfying the "weakly step consistent" property

```

lemma ksys-semget-wsc:
  assumes p0: reachable0 s

```



```

and p1: reachable0 t
and p2: s ~ d ~ t
and p3: pid @ s d
and p4: s ~ pid ~ t
and p5: s' = fst(ksys-semget s pid sem semflg)
and p6: t' = fst(ksys-semget t pid sem semflg)
shows s' ~ d ~ t'
proof -
{
  have a0 : s = s'
    using p5 ksys-semget-def
    by simp
  have a1 : t = t'
    using p6 ksys-semget-def
    by auto
  have a2: s' ~ d ~ t'
    using a0 a1 p2
    by blast
}
then show ?thesis by auto
qed

lemma ksys-semget-wsc-e:
assumes p0: reachable0 s
and p1: reachable0 t
and p2: e = KIpEvt( (Event-sem-associate pid sem semflg ))
and p3: s ~ d ~ t
and p4: (the (domain-of-event e)) @ s d
and p5: s ~ (the (domain-of-event e)) ~ t
and p6: s' = exec-event s e
and p7: t' = exec-event t e
shows s' ~ d ~ t'
proof -
{
  have a0 : (the (domain-of-event e)) = pid
    using p2 domain-of-event-def getpid-from-kern-ipc-event-def
    by force
  have a1: s' = fst(ksys-semget s pid sem semflg)
    using p2 p6 exec-event-def by auto
  have a2: t' = fst(ksys-semget t pid sem semflg)
    using p2 p7 exec-event-def
    by auto
  have a3: pid @ s d
    using p4 a0
    by blast
  have a4 : s ~ pid ~ t using p5 a0
    by blast
  have a5: s' ~ d ~ t'
    using a1 a2 a3 a4 p0 p1 p3 p4 p5 ksys-semget-wsc

```

```

      by blast
    }
  then show ?thesis by auto
qed

```

```

lemma ksys-semget-dwsc-e: dynamic-weakly-step-consistent-e ( KIpEvt( (Event-sem-associate
pid sem semflg )))
  using dynamic-weakly-step-consistent-e-def ksys-semget-wsc-e
  by blast

```

29.36.11 proving "sem_msgctl" satisfying the "weakly step consistent" property

```

lemma sem-msgctl-wsc:
  assumes p0: reachable0 s
    and p1: reachable0 t
    and p2: s ~ d ~ t
    and p3: pid @ s d
    and p4: s ~ pid ~ t
    and p5: s' = fst(sem-msgctl s pid sem cmd)
    and p6: t' = fst(sem-msgctl t pid sem cmd)
  shows s' ~ d ~ t'
  proof -
  {
    have a0 : s = s'
      using p5 sem-msgctl-def
      by simp
    have a1 : t = t'
      using p6 sem-msgctl-def
      by auto
    have a2: s' ~ d ~ t'
      using a0 a1 p2
      by blast
  }
  then show ?thesis by auto
qed

```

```

lemma sem-msgctl-wsc-e:
  assumes p0: reachable0 s
    and p1: reachable0 t
    and p2: e = KIpEvt( (Event-sem-semctl pid sem cmd ))
    and p3: s ~ d ~ t
    and p4: (the (domain-of-event e)) @ s d
    and p5: s ~ (the (domain-of-event e)) ~ t
    and p6: s' = exec-event s e
    and p7: t' = exec-event t e
  shows s' ~ d ~ t'
  proof -
  {
    have a0 : (the (domain-of-event e)) = pid

```

```

    using p2 domain-of-event-def getpid-from-kern-ipc-event-def
    by force
  have a1:  $s' = fst(sem\text{-}msgctl\ s\ pid\ sem\ cmd)$ 
    using p2 p6 exec-event-def by auto
  have a2:  $t' = fst(sem\text{-}msgctl\ t\ pid\ sem\ cmd)$ 
    using p2 p7 exec-event-def
    by auto
  have a3:  $pid @ sd$ 
    using p4 a0
    by blast
  have a4 :  $s \sim pid \sim t$  using p5 a0
    by blast
  have a5:  $s' \sim d \sim t'$ 
    using a1 a2 a3 a4 p0 p1 p3 p4 p5 sem-msgctl-wsc
    by blast
}
then show ?thesis by auto
qed

```

```

lemma sem-msgctl-dwsc-e: dynamic-weakly-step-consistent-e (KIpEvt((Event-sem-semctl
pid sem cmd )))
  using dynamic-weakly-step-consistent-e-def sem-msgctl-wsc-e
  by blast

```

29.36.12 proving "do_{semtimedop}" satisfying the "weakly step consistent" property

```

lemma do-semtimedop-wsc:
  assumes p0: reachable0 s
    and p1: reachable0 t
    and p2:  $s \sim d \sim t$ 
    and p3:  $pid @ s\ d$ 
    and p4:  $s \sim pid \sim t$ 
    and p5:  $s' = fst(do\text{-}semtimedop\ s\ pid\ sma\ sops\ nsops\ alter')$ 
    and p6:  $t' = fst(do\text{-}semtimedop\ t\ pid\ sma\ sops\ nsops\ alter')$ 
  shows  $s' \sim d \sim t'$ 
  proof -
  {
    have a0 :  $s = s'$ 
      using p5 do-semtimedop-def
      by (smt fstI)
    have a1 :  $t = t'$ 
      using p6 do-semtimedop-def
      by (smt fstI)
    have a2:  $s' \sim d \sim t'$ 
      using a0 a1 p2
      by blast
  }
  then show ?thesis by auto
qed

```

lemma *do-semtimedop-wsc-e*:

```

assumes p0: reachable0 s
  and p1: reachable0 t
  and p2: e = KIpEvt( (Event-sem-semop pid sma sops nsops alter' ) )
  and p3: s ~ d ~ t
  and p4: (the (domain-of-event e)) @ s d
  and p5: s ~ (the (domain-of-event e)) ~ t
  and p6: s' = exec-event s e
  and p7: t' = exec-event t e
shows s' ~ d ~ t'
proof –
  {
    have a0 : (the (domain-of-event e)) = pid
      using p2 domain-of-event-def getpid-from-kern-ipc-event-def
      by force
    have a1: s' = fst(do-semtimedop s pid sma sops nsops alter')
      using p2 p6 exec-event-def by auto
    have a2: t' = fst(do-semtimedop t pid sma sops nsops alter')
      using p2 p7 exec-event-def
      by auto
    have a3: pid @ s d
      using p4 a0
      by blast
    have a4 : s ~ pid ~ t using p5 a0
      by blast
    have a5: s' ~ d ~ t'
      using a1 a2 a3 a4 p0 p1 p3 p4 p5 do-semtimedop-wsc
      by blast
  }
  then show ?thesis by auto
qed

```

```

lemma do-semtimedop-dwsc-e: dynamic-weakly-step-consistent-e (KIpEvt( (Event-sem-semop
pid sma sops nsops alter' ) ) )
  using dynamic-weakly-step-consistent-e-def do-semtimedop-wsc-e
  by blast

```

29.37 smack file hooks weakly step consistent

29.37.1 proving ”do_{ioctl}” satisfying the ”weakly step consistent” property

lemma *do-ioctl-wsc*:

```

assumes p0: reachable0 s
  and p1: reachable0 t
  and p2: s ~ d ~ t
  and p3: pid @ s d
  and p4: s ~ pid ~ t
  and p5: s' = fst(do-ioctl s pid file cmd arg)
  and p6: t' = fst(do-ioctl t pid file cmd arg)

```

```

shows  $s' \sim d \sim t'$ 
proof -
{
  have  $a0 : s = s'$ 
    using  $p5$  do-ioctl-def do-ioctl-detstate fst-conv funcState-def
    security-file-ioctl-notchgstate
    by smt
  have  $a1 : t = t'$ 
    using  $p6$  do-ioctl-def do-ioctl-detstate fst-conv funcState-def
    security-file-ioctl-notchgstate
    by smt
  have  $a2 : s' \sim d \sim t'$ 
    using  $a0$   $a1$   $p2$ 
    by blast
}
then show ?thesis by auto
qed

```

```

lemma do-ioctl-wsc-e:
assumes  $p0$ : reachable0 s
and  $p1$ : reachable0 t
and  $p2$ :  $e = \text{FileEvt}(\text{Event-do-ioctl } pid \text{ file cmd arg})$ 
and  $p3$ :  $s \sim d \sim t$ 
and  $p4$ :  $(\text{the}(\text{domain-of-event } e)) @ s d$ 
and  $p5$ :  $s \sim (\text{the}(\text{domain-of-event } e)) \sim t$ 
and  $p6$ :  $s' = \text{exec-event } s e$ 
and  $p7$ :  $t' = \text{exec-event } t e$ 
shows  $s' \sim d \sim t'$ 
proof -
{
  have  $a0 : (\text{the}(\text{domain-of-event } e)) = pid$ 
    using  $p2$  domain-of-event-def getpid-from-file-event-def
    by force
  have  $a1 : s' = \text{fst}(\text{do-ioctl } s \text{ pid file cmd arg})$ 
    using  $p2$   $p6$  exec-event-def by auto
  have  $a2 : t' = \text{fst}(\text{do-ioctl } t \text{ pid file cmd arg})$ 
    using  $p2$   $p7$  exec-event-def
    by auto
  have  $a3 : pid @ s d$ 
    using  $p4$   $a0$ 
    by blast
  have  $a4 : s \sim pid \sim t$  using  $p5$   $a0$ 
    by blast
  have  $a5 : s' \sim d \sim t'$ 
    using  $a1$   $a2$   $a3$   $a4$   $p0$   $p1$   $p3$   $p5$   $p4$  do-ioctl-wsc
    by blast
}
then show ?thesis by auto
qed

```

```

lemma do-ioctl-dwsc-e: dynamic-weakly-step-consistent-e (FileEvt( Event-do-ioctl
pid file cmd arg ))
  using dynamic-weakly-step-consistent-e-def do-ioctl-wsc-e
  by blast

```

29.37.2 proving "syscall_iioctl" satisfying the "weakly step consistent" property

```

lemma syscall-ioctl-wsc:
  assumes p0: reachable0 s
    and p1: reachable0 t
    and p2: s ~ d ~ t
    and p3: pid @ s d
    and p4: s ~ pid ~ t
    and p5: s' = fst(syscall-ioctl s pid fd cmd arg)
    and p6: t' = fst(syscall-ioctl t pid fd cmd arg)
  shows s' ~ d ~ t'
  proof –
  {
    have a0 : s = s'
      using p5 syscall-ioctl-def
      by (smt fstI)
    have a1 : t = t'
      using p6 syscall-ioctl-def
      by (smt fst-conv)
    have a2: s' ~ d ~ t'
      using a0 a1 p2
      by blast
  }
  then show ?thesis by auto
qed

```

```

lemma syscall-ioctl-wsc-e:
  assumes p0: reachable0 s
    and p1: reachable0 t
    and p2: e = FileEvt( Event-syscall-ioctl pid fd cmd arg )
    and p3: s ~ d ~ t
    and p4: (the (domain-of-event e)) @ s d
    and p5: s ~ (the (domain-of-event e)) ~ t
    and p6: s' = exec-event s e
    and p7: t' = exec-event t e
  shows s' ~ d ~ t'
  proof –
  {
    have a0 : (the (domain-of-event e)) = pid
      using p2 domain-of-event-def getpid-from-file-event-def
      by force
    have a1: s' = fst(syscall-ioctl s pid fd cmd arg)
      using p2 p6 exec-event-def by auto

```

```

    have a2:  $t' = \text{fst}(\text{syscall-ioctl } t \text{ pid } fd \text{ cmd } arg)$ 
      using p2 p7 exec-event-def
      by auto
    have a3:  $pid @ s d$ 
      using p4 a0
      by blast
    have a4 :  $s \sim pid \sim t$  using p5 a0
      by blast
    have a5:  $s' \sim d \sim t'$ 
      using a1 a2 a3 a4 p0 p1 p3 p5 p4 syscall-ioctl-wsc
      by blast
  }
  then show ?thesis by auto
qed

lemma syscall-ioctl-dwsc-e: dynamic-weakly-step-consistent-e (FileEvt( Event-syscall-ioctl
pid fd cmd arg ))
  using dynamic-weakly-step-consistent-e-def syscall-ioctl-wsc-e
  by blast

```

29.37.3 proving "ksys_iioctl" satisfying the "weakly step consistent" property

```

lemma ksys-ioctl-wsc:
  assumes p0: reachable0 s
    and p1: reachable0 t
    and p2:  $s \sim d \sim t$ 
    and p3:  $pid @ s d$ 
    and p4:  $s \sim pid \sim t$ 
    and p5:  $s' = \text{fst}(\text{ksys-ioctl } s \text{ pid } fd \text{ cmd } arg)$ 
    and p6:  $t' = \text{fst}(\text{ksys-ioctl } t \text{ pid } fd \text{ cmd } arg)$ 
  shows  $s' \sim d \sim t'$ 
  proof -
  {
    have a0 :  $s = s'$ 
      using p5 ksys-ioctl-def
      by (smt fstI)
    have a1 :  $t = t'$ 
      using p6 ksys-ioctl-def
      by (smt fst-conv)
    have a2:  $s' \sim d \sim t'$ 
      using a0 a1 p2
      by blast
  }
  then show ?thesis by auto
qed

```

```

lemma ksys-ioctl-wsc-e:
  assumes p0: reachable0 s
    and p1: reachable0 t

```

```

and p2: e = FileEvt( Event-ksys-ioctl pid fd cmd arg )
and p3: s ~ d ~ t
and p4: (the (domain-of-event e)) @ s d
and p5: s ~ (the (domain-of-event e)) ~ t
and p6: s' = exec-event s e
and p7: t' = exec-event t e
shows s' ~ d ~ t'
proof -
{
have a0 : (the (domain-of-event e)) = pid
  using p2 domain-of-event-def getpid-from-file-event-def
  by force
have a1: s' = fst(ksys-ioctl s pid fd cmd arg)
  using p2 p6 exec-event-def by auto
have a2: t' = fst(ksys-ioctl t pid fd cmd arg)
  using p2 p7 exec-event-def
  by auto
have a3: pid @ s d
  using p4 a0
  by blast
have a4 : s ~ pid ~ t using p5 a0
  by blast
have a5: s' ~ d ~ t'
  using a1 a2 a3 a4 p0 p1 p3 p5 p4 ksys-ioctl-wsc
  by blast
}
then show ?thesis by auto
qed

```

```

lemma ksys-ioctl-dwsc-e: dynamic-weakly-step-consistent-e (FileEvt( Event-ksys-ioctl
pid fd cmd arg ))
  using dynamic-weakly-step-consistent-e-def ksys-ioctl-wsc-e
  by blast

```

29.37.4 proving "vm_mmap_{pgoff}" satisfying the "weaklystepconsistent" property

```

lemma vm-mmap-pgoff-wsc:
assumes p0: reachable0 s
and p1: reachable0 t
and p2: s ~ d ~ t
and p3: pid @ s d
and p4: s ~ pid ~ t
and p5: s' = fst(vm-mmap-pgoff s pid file addr len' prot flag pgoff)
and p6: t' = fst(vm-mmap-pgoff t pid file addr len' prot flag pgoff)
shows s' ~ d ~ t'
proof -
{
have a0 : s = s'
  using p5 vm-mmap-pgoff-def

```



```

    by (smt fstI)
  have a1 : t = t'
    using p6 vm-mmap-pgoff-def
    by (smt fst-conv)
  have a2: s' ~ d ~ t'
    using a0 a1 p2
    by blast
}
then show ?thesis by auto
qed

```

lemma *vm-mmap-pgoff-wsc-e*:

```

assumes p0: reachable0 s
and p1: reachable0 t
and p2: e = FileEvt( Event-vm-mmap-pgoff pid file addr len' prot flag pgoff )
and p3: s ~ d ~ t
and p4: (the (domain-of-event e)) @ s d
and p5: s ~ (the (domain-of-event e)) ~ t
and p6: s' = exec-event s e
and p7: t' = exec-event t e
shows s' ~ d ~ t'

```

proof –

```

{
  have a0 : (the (domain-of-event e)) = pid
    using p2 domain-of-event-def getpid-from-file-event-def
    by force
  have a1: s' = fst(vm-mmap-pgoff s pid file addr len' prot flag pgoff)
    using p2 p6 exec-event-def by auto
  have a2: t' = fst(vm-mmap-pgoff t pid file addr len' prot flag pgoff)
    using p2 p7 exec-event-def
    by auto
  have a3: pid @ s d
    using p4 a0
    by blast
  have a4 : s ~ pid ~ t using p5 a0
    by blast
  have a5: s' ~ d ~ t'
    using a1 a2 a3 a4 p0 p1 p3 p5 p4 vm-mmap-pgoff-wsc
    by blast
}

```

then show ?thesis **by** auto

qed

lemma *vm-mmap-pgoff-dwsc-e*: *dynamic-weakly-step-consistent-e* (*FileEvt*(*Event-vm-mmap-pgoff* *pid file addr len' prot flag pgoff*))

```

using dynamic-weakly-step-consistent-e-def vm-mmap-pgoff-wsc-e
by blast

```

29.37.5 proving "do_{sysvm86}" satisfying the "weakly step consistent" property

lemma *do-sys-vm86-wsc*:

```

assumes p0: reachable0 s
  and p1: reachable0 t
  and p2: s ~ d ~ t
  and p3: pid @ s d
  and p4: s ~ pid ~ t
  and p5: s' = fst(do-sys-vm86 s pid)
  and p6: t' = fst(do-sys-vm86 t pid)
shows s' ~ d ~ t'
proof -
{
  have a0 : s = s'
    using p5 do-sys-vm86-def
    by (smt fstI)
  have a1 : t = t'
    using p6 do-sys-vm86-def
    by (smt fst-conv)
  have a2: s' ~ d ~ t'
    using a0 a1 p2
    by blast
}
then show ?thesis by auto
qed

```

lemma *do-sys-vm86-wsc-e*:

```

assumes p0: reachable0 s
  and p1: reachable0 t
  and p2: e = FileEvt( Event-do-sys-vm86 pid )
  and p3: s ~ d ~ t
  and p4: (the (domain-of-event e)) @ s d
  and p5: s ~ (the (domain-of-event e)) ~ t
  and p6: s' = exec-event s e
  and p7: t' = exec-event t e
shows s' ~ d ~ t'
proof -
{
  have a0 : (the (domain-of-event e)) = pid
    using p2 domain-of-event-def getpid-from-file-event-def
    by force
  have a1: s' = fst(do-sys-vm86 s pid)
    using p2 p6 exec-event-def by auto
  have a2: t' = fst(do-sys-vm86 t pid)
    using p2 p7 exec-event-def
    by auto
  have a3: pid @ s d
    using p4 a0
    by blast
  have a4 : s ~ pid ~ t using p5 a0

```

```

    by blast
  have a5:  $s' \sim d \sim t'$ 
    using a1 a2 a3 a4 p0 p1 p3 p5 p4 do-sys-vm86-wsc
    by blast
}
then show ?thesis by auto
qed

```

```

lemma do-sys-vm86-dwsc-e: dynamic-weakly-step-consistent-e ( FileEvt( Event-do-sys-vm86
pid ))
  using dynamic-weakly-step-consistent-e-def do-sys-vm86-wsc-e
  by blast

```

29.37.6 proving "get_{unmapped}area" satisfying the "weakly step consistent" property

```

lemma get-unmapped-area-wsc:
  assumes p0: reachable0 s
    and p1: reachable0 t
    and p2:  $s \sim d \sim t$ 
    and p3: pid @ s d
    and p4:  $s \sim pid \sim t$ 
    and p5:  $s' = fst(get-unmapped-area s pid file addr)$ 
    and p6:  $t' = fst(get-unmapped-area t pid file addr)$ 
  shows  $s' \sim d \sim t'$ 
  proof -
  {
    have a0 :  $s = s'$ 
      using p5 get-unmapped-area-def
    proof -
      have  $s = s' \vee resultValue s (security-mmap-addr s addr) = 0$ 
        using get-unmapped-area-def p5 by fastforce
      then show ?thesis
        using get-unmapped-area-def p5 by force
    qed
  }
  have a1 :  $t = t'$ 
    using p6 get-unmapped-area-def
  proof -
    have  $t = t' \vee resultValue t (security-mmap-addr t addr) = 0$ 
      using get-unmapped-area-def p6 by force
    then show ?thesis
      using get-unmapped-area-def p6 by force
  qed
  have a2:  $s' \sim d \sim t'$ 
    using a0 a1 p2
    by blast
}
then show ?thesis by auto
qed

```

```

lemma get-unmapped-area-wsc-e:
  assumes  $p0$ : reachable0  $s$ 
    and  $p1$ : reachable0  $t$ 
    and  $p2$ :  $e = \text{FileEvt}(\text{Event-get-unmapped-area } pid \text{ file } addr)$ 
    and  $p3$ :  $s \sim d \sim t$ 
    and  $p4$ :  $(\text{the } (\text{domain-of-event } e)) @ s d$ 
    and  $p5$ :  $s \sim (\text{the } (\text{domain-of-event } e)) \sim t$ 
    and  $p6$ :  $s' = \text{exec-event } s e$ 
    and  $p7$ :  $t' = \text{exec-event } t e$ 
  shows  $s' \sim d \sim t'$ 
  proof –
    {
      have  $a0$  :  $(\text{the } (\text{domain-of-event } e)) = pid$ 
        using  $p2$  domain-of-event-def getpid-from-file-event-def
        by force
      have  $a1$ :  $s' = \text{fst}(\text{get-unmapped-area } s \text{ pid } \text{file } \text{addr})$ 
        using  $p2$   $p6$  exec-event-def by auto
      have  $a2$ :  $t' = \text{fst}(\text{get-unmapped-area } t \text{ pid } \text{file } \text{addr})$ 
        using  $p2$   $p7$  exec-event-def
        by auto
      have  $a3$ :  $pid @ s d$ 
        using  $p4$   $a0$ 
        by blast
      have  $a4$  :  $s \sim pid \sim t$  using  $p5$   $a0$ 
        by blast
      have  $a5$ :  $s' \sim d \sim t'$ 
        using  $a1$   $a2$   $a3$   $a4$   $p0$   $p1$   $p3$   $p5$   $p4$  get-unmapped-area-wsc
        by blast
    }
  then show ?thesis by auto
qed

```

```

lemma get-unmapped-area-dwsc-e: dynamic-weakly-step-consistent-e ( $\text{FileEvt}(\text{Event-get-unmapped-area } pid \text{ file } \text{addr})$ )
  using dynamic-weakly-step-consistent-e-def get-unmapped-area-wsc-e
  by blast

```

29.37.7 proving “ $\text{validate}_{mmap_request}$ ” satisfying the “weakly step consistent” property

```

lemma validate-mmap-request-wsc:
  assumes  $p0$ : reachable0  $s$ 
    and  $p1$ : reachable0  $t$ 
    and  $p2$ :  $s \sim d \sim t$ 
    and  $p3$ :  $pid @ s d$ 
    and  $p4$ :  $s \sim pid \sim t$ 
    and  $p5$ :  $s' = \text{fst}(\text{validate-mmap-request } s \text{ pid } \text{file } \text{addr})$ 
    and  $p6$ :  $t' = \text{fst}(\text{validate-mmap-request } t \text{ pid } \text{file } \text{addr})$ 
  shows  $s' \sim d \sim t'$ 

```

```

proof -
{
  have  $a0 : s = s'$ 
    using  $p5$  validate-mmap-request-def
    by ( $smt$   $fstI$ )
  have  $a1 : t = t'$ 
    using  $p6$  validate-mmap-request-def
  proof -
    { assume  $t \neq t'$ 
      then have  $\neg 0 \leq resultValue\ t$  (security-mmap-addr  $t$   $addr$ )
        using  $p6$  validate-mmap-request-def by force
      then have  $?thesis$ 
        using  $p6$  validate-mmap-request-def by auto }
    then show  $?thesis$ 
      by metis
  qed
  have  $a2 : s' \sim d \sim t'$ 
    using  $a0$   $a1$   $p2$ 
    by blast
}
then show  $?thesis$  by auto
qed

```

lemma *validate-mmap-request-wsc-e*:

```

assumes  $p0 : reachable0\ s$ 
and  $p1 : reachable0\ t$ 
and  $p2 : e = FileEvt(\ Event-validate-mmap-request\ pid\ file\ addr)$ 
and  $p3 : s \sim d \sim t$ 
and  $p4 : (the\ (domain-of-event\ e)) @ s\ d$ 
and  $p5 : s \sim (the\ (domain-of-event\ e)) \sim t$ 
and  $p6 : s' = exec-event\ s\ e$ 
and  $p7 : t' = exec-event\ t\ e$ 

```

shows $s' \sim d \sim t'$

```

proof -
{
  have  $a0 : (the\ (domain-of-event\ e)) = pid$ 
    using  $p2$  domain-of-event-def getpid-from-file-event-def
    by force
  have  $a1 : s' = fst(validate-mmap-request\ s\ pid\ file\ addr)$ 
    using  $p2$   $p6$  exec-event-def by auto
  have  $a2 : t' = fst(validate-mmap-request\ t\ pid\ file\ addr)$ 
    using  $p2$   $p7$  exec-event-def
    by auto
  have  $a3 : pid @ s\ d$ 
    using  $p4$   $a0$ 
    by blast
  have  $a4 : s \sim pid \sim t$  using  $p5$   $a0$ 
    by blast
  have  $a5 : s' \sim d \sim t'$ 

```

```

      using a1 a2 a3 a4 p0 p1 p3 p5 p4 validate-mmap-request-wsc
    by blast
  }
  then show ?thesis by auto
qed

```

```

lemma validate-mmap-request-dwsc-e: dynamic-weakly-step-consistent-e (FileEvt(
Event-validate-mmap-request pid file addr))
  using dynamic-weakly-step-consistent-e-def validate-mmap-request-wsc-e
  by blast

```

29.37.8 proving "generic_ssetlease" satisfying the "weaklystepconsistent" property

```

lemma generic-setlease-wsc:
  assumes p0: reachable0 s
    and p1: reachable0 t
    and p2: s ~ d ~ t
    and p3: pid @ s d
    and p4: s ~ pid ~ t
    and p5: s' = fst(generic-setlease s pid file arg)
    and p6: t' = fst(generic-setlease t pid file arg)
  shows s' ~ d ~ t'
  proof -
  {
    have a0 : s = s'
      using p5 generic-setlease-def
      by (smt fst-conv)
    have a1 : t = t'
      using p6 generic-setlease-def
    proof -
      { assume t ≠ t'
        then have resultValue t (security-file-lock t file (nat arg)) ≠ 0
          using generic-setlease-def p6 by force
        then have ?thesis
          by (simp add: generic-setlease-def p6) }
      then show ?thesis
        by metis
    qed
    have a2: s' ~ d ~ t'
      using a0 a1 p2
      by blast
  }
  then show ?thesis by auto
qed

```

```

lemma generic-setlease-wsc-e:
  assumes p0: reachable0 s
    and p1: reachable0 t
    and p2: e = FileEvt( Event-generic-setlease pid file arg )

```

```

and p3: s ~ d ~ t
and p4: (the (domain-of-event e)) @ s d
and p5: s ~ (the (domain-of-event e)) ~ t
and p6: s' = exec-event s e
and p7: t' = exec-event t e
shows s' ~ d ~ t'
proof -
{
have a0 : (the (domain-of-event e)) = pid
  using p2 domain-of-event-def getpid-from-file-event-def
  by force
have a1: s' = fst(generic-setlease s pid file arg)
  using p2 p6 exec-event-def by auto
have a2: t' = fst(generic-setlease t pid file arg)
  using p2 p7 exec-event-def
  by auto
have a3: pid @ s d
  using p4 a0
  by blast
have a4 : s ~ pid ~ t using p5 a0
  by blast
have a5: s' ~ d ~ t'
  using a1 a2 a3 a4 p0 p1 p3 p5 p4 generic-setlease-wsc
  by blast
}
then show ?thesis by auto
qed

```

```

lemma generic-setlease-dwsc-e: dynamic-weakly-step-consistent-e ( FileEvt( Event-generic-setlease
pid file arg ))
  using dynamic-weakly-step-consistent-e-def generic-setlease-wsc-e
  by blast

```

29.37.9 proving "syscall_{lock}" satisfying the "weakly step consistent" property

```

lemma syscall-lock-wsc:
assumes p0: reachable0 s
and p1: reachable0 t
and p2: s ~ d ~ t
and p3: pid @ s d
and p4: s ~ pid ~ t
and p5: s' = fst(syscall-lock s pid fd cmd )
and p6: t' = fst(syscall-lock t pid fd cmd )
shows s' ~ d ~ t'
proof -
{
have a0 : s = s'
  by (simp add: p5 syscall-lock-def)
have a1 : t = t'

```

```

    using p6
    by (simp add: syscall-lock-def)
  have a2:  $s' \sim d \sim t'$ 
    using a0 a1 p2
    by blast
}
then show ?thesis by auto
qed

lemma syscall-lock-wsc-e:
  assumes p0: reachable0 s
  and p1: reachable0 t
  and p2:  $e = \text{FileEvt}(\text{Event-syscall-lock } pid \text{ fd cmd})$ 
  and p3:  $s \sim d \sim t$ 
  and p4:  $(\text{the } (\text{domain-of-event } e)) @ s d$ 
  and p5:  $s \sim (\text{the } (\text{domain-of-event } e)) \sim t$ 
  and p6:  $s' = \text{exec-event } s e$ 
  and p7:  $t' = \text{exec-event } t e$ 
shows  $s' \sim d \sim t'$ 
proof -
{
  have a0 :  $(\text{the } (\text{domain-of-event } e)) = pid$ 
    using p2 domain-of-event-def getpid-from-file-event-def
    by force
  have a1:  $s' = \text{fst}(\text{syscall-lock } s \text{ pid fd cmd})$ 
    using p2 p6 exec-event-def by auto
  have a2:  $t' = \text{fst}(\text{syscall-lock } t \text{ pid fd cmd})$ 
    using p2 p7 exec-event-def
    by auto
  have a3:  $pid @ s d$ 
    using p4 a0
    by blast
  have a4 :  $s \sim pid \sim t$  using p5 a0
    by blast
  have a5:  $s' \sim d \sim t'$ 
    using a1 a2 a3 a4 p0 p1 p3 p5 p4 syscall-lock-wsc
    by blast
}
then show ?thesis by auto
qed

```

```

lemma syscall-lock-dwsc-e: dynamic-weakly-step-consistent-e (  $\text{FileEvt}(\text{Event-syscall-lock } pid \text{ fd cmd})$  )
  using dynamic-weakly-step-consistent-e-def syscall-lock-wsc-e
  by blast

```

29.37.10 proving “do_{lock_file_wait}” satisfying the “weakly step consistent” property

```

lemma do-lock-file-wait-wsc:

```



```

assumes  $p0$ : reachable0  $s$ 
  and  $p1$ : reachable0  $t$ 
  and  $p2$ :  $s \sim d \sim t$ 
  and  $p3$ :  $pid @ s d$ 
  and  $p4$ :  $s \sim pid \sim t$ 
  and  $p5$ :  $s' = fst(do-lock-file-wait\ s\ pid\ file\ cmd\ fl)$ 
  and  $p6$ :  $t' = fst(do-lock-file-wait\ t\ pid\ file\ cmd\ fl)$ 
shows  $s' \sim d \sim t'$ 
proof –
{
  have  $a0$  :  $s = s'$ 
    using  $p5$ 
    by (smt do-lock-file-wait-def fst-conv)
  have  $a1$  :  $t = t'$ 
    using  $p6$  do-lock-file-wait-def
  proof –
    have  $\forall s\ n\ f\ i\ fa. do-lock-file-wait\ s\ n\ f\ i\ fa =$ 
      (if resultValue  $s$  (security-file-lock  $s\ f$  (nat (of-char (fl-type  $fa$ )))) = 0
        then ( $s, 0$ )
        else ( $s, resultValue\ s$  (security-file-lock  $s\ f$  (nat (of-char (fl-type  $fa$ ))))))
      using do-lock-file-wait-def by presburger
    then show ?thesis
      by (metis fstI p6)
  qed
  have  $a2$ :  $s' \sim d \sim t'$ 
    using  $a0\ a1\ p2$ 
    by blast
}
then show ?thesis by auto
qed

```

```

lemma do-lock-file-wait-wsc-e:
assumes  $p0$ : reachable0  $s$ 
  and  $p1$ : reachable0  $t$ 
  and  $p2$ :  $e = FileEvt( Event-do-lock-file-wait\ pid\ file\ cmd\ fl )$ 
  and  $p3$ :  $s \sim d \sim t$ 
  and  $p4$ : (the (domain-of-event  $e$ ))  $@ s\ d$ 
  and  $p5$ :  $s \sim (the\ (domain-of-event\ e)) \sim t$ 
  and  $p6$ :  $s' = exec-event\ s\ e$ 
  and  $p7$ :  $t' = exec-event\ t\ e$ 
shows  $s' \sim d \sim t'$ 
proof –
{
  have  $a0$  : (the (domain-of-event  $e$ )) =  $pid$ 
    using  $p2$  domain-of-event-def getpid-from-file-event-def
    by force
  have  $a1$ :  $s' = fst(do-lock-file-wait\ s\ pid\ file\ cmd\ fl)$ 
    using  $p2\ p6$  exec-event-def by auto
  have  $a2$ :  $t' = fst(do-lock-file-wait\ t\ pid\ file\ cmd\ fl)$ 

```

```

    using p2 p7 exec-event-def
  by auto
have a3: pid @ s d
  using p4 a0
  by blast
have a4 : s ~ pid ~ t using p5 a0
  by blast
have a5: s' ~ d ~ t'
  using a1 a2 a3 a4 p0 p1 p3 p5 p4 do-lock-file-wait-wsc
  by blast
}
then show ?thesis by auto
qed

```

```

lemma do-lock-file-wait-dwsc-e: dynamic-weakly-step-consistent-e (FileEvt( Event-do-lock-file-wait
pid file cmd fl))
  using dynamic-weakly-step-consistent-e-def do-lock-file-wait-wsc-e
  by blast

```

29.37.11 proving "file_{fcntl}" satisfying the "weakly step consistent" property

```

lemma file-fcntl-wsc:
  assumes p0: reachable0 s
    and p1: reachable0 t
    and p2: s ~ d ~ t
    and p3: pid @ s d
    and p4: s ~ pid ~ t
    and p5: s' = fst(file-fcntl s pid file cmd arg)
    and p6: t' = fst(file-fcntl t pid file cmd arg)
  shows s' ~ d ~ t'
  proof -
  {
    have a0 : s = s'
      using p5 file-fcntl-def
      by (smt fstI)
    have a1 : t = t'
      using p6 file-fcntl-def
    proof -
      have  $\forall s n f na nb. \text{file-fcntl } s n f na nb =$ 
        (if resultValue s (security-file-fcntl s f na nb) = 0
          then (s, 0)
          else (s, resultValue s (security-file-fcntl s f na nb)))
        using file-fcntl-def by presburger
      then have file-fcntl t pid file cmd arg = (t, resultValue t (security-file-fcntl t
file cmd arg))
        by auto
      then show ?thesis
        using p6 by auto
    qed
  }

```

```

    have a2:  $s' \sim d \sim t'$ 
      using a0 a1 p2
      by blast
  }
  then show ?thesis by auto
qed

```

```

lemma file-fcntl-wsc-e:
  assumes p0: reachable0 s
  and p1: reachable0 t
  and p2:  $e = \text{FileEvt}(\text{Event-file-fcntl pid file cmd arg})$ 
  and p3:  $s \sim d \sim t$ 
  and p4:  $(\text{the}(\text{domain-of-event } e)) @ s d$ 
  and p5:  $s \sim (\text{the}(\text{domain-of-event } e)) \sim t$ 
  and p6:  $s' = \text{exec-event } s e$ 
  and p7:  $t' = \text{exec-event } t e$ 
  shows  $s' \sim d \sim t'$ 
  proof -
    {
      have a0:  $(\text{the}(\text{domain-of-event } e)) = \text{pid}$ 
        using p2 domain-of-event-def getpid-from-file-event-def
        by force
      have a1:  $s' = \text{fst}(\text{file-fcntl } s \text{ pid file cmd arg})$ 
        using p2 p6 exec-event-def by auto
      have a2:  $t' = \text{fst}(\text{file-fcntl } t \text{ pid file cmd arg})$ 
        using p2 p7 exec-event-def
        by auto
      have a3:  $\text{pid} @ s d$ 
        using p4 a0
        by blast
      have a4:  $s \sim \text{pid} \sim t$  using p5 a0
        by blast
      have a5:  $s' \sim d \sim t'$ 
        using a1 a2 a3 a4 p0 p1 p3 p5 p4 file-fcntl-wsc
        by blast
    }
    then show ?thesis by auto
  qed

```

```

lemma file-fcntl-dwsc-e: dynamic-weakly-step-consistent-e ( $\text{FileEvt}(\text{Event-file-fcntl}$ 
 $\text{pid file cmd arg})$ )
  using dynamic-weakly-step-consistent-e-def file-fcntl-wsc-e
  by blast

```

29.37.12 proving "file_send_ssigiotask" satisfying the "weaklystepconsistent" property

```

lemma file-send-sigiotask-wsc:
  assumes p0: reachable0 s
  and p1: reachable0 t

```

```

and p2: s ~ d ~ t
and p3: pid @ s d
and p4: s ~ pid ~ t
and p5: s' = fst(file-send-sigiotask s pid ty fown sig)
and p6: t' = fst(file-send-sigiotask t pid ty fown sig)
shows s' ~ d ~ t'
proof -
{
  have a0 : s = s'
    using p5 file-send-sigiotask-def
    by simp
  have a1 : t = t'
    using p6 file-send-sigiotask-def
    by simp
  have a2: s' ~ d ~ t'
    using a0 a1 p2
    by blast
}
then show ?thesis by auto
qed

```

lemma file-send-sigiotask-wsc-e:

```

assumes p0: reachable0 s
and p1: reachable0 t
and p2: e = FileEvt( Event-file-send-sigiotask pid ty fown sig )
and p3: s ~ d ~ t
and p4: (the (domain-of-event e)) @ s d
and p5: s ~ (the (domain-of-event e)) ~ t
and p6: s' = exec-event s e
and p7: t' = exec-event t e
shows s' ~ d ~ t'
proof -
{
  have a0 : (the (domain-of-event e)) = pid
    using p2 domain-of-event-def getpid-from-file-event-def
    by force
  have a1: s' = fst(file-send-sigiotask s pid ty fown sig)
    using p2 p6 exec-event-def by auto
  have a2: t' = fst(file-send-sigiotask t pid ty fown sig)
    using p2 p7 exec-event-def
    by auto
  have a3: pid @ s d
    using p4 a0
    by blast
  have a4 : s ~ pid ~ t using p5 a0
    by blast
  have a5: s' ~ d ~ t'
    using a1 a2 a3 a4 p0 p1 p3 p5 p4 file-send-sigiotask-wsc
    by blast
}

```

```

    }
  then show ?thesis by auto
qed

```

```

lemma file-send-sigiotask-dwsc-e: dynamic-weakly-step-consistent-e (FileEvt( Event-file-send-sigiotask
pid ty fown sig ))
  using dynamic-weakly-step-consistent-e-def file-send-sigiotask-wsc-e
  by blast

```

29.37.13 proving "file_rreceive" satisfying the "weakly step consistent" property

```

lemma file-receive-wsc:
  assumes p0: reachable0 s
    and p1: reachable0 t
    and p2: s ~ d ~ t
    and p3: pid @ s d
    and p4: s ~ pid ~ t
    and p5: s' = fst(file-receive s pid f)
    and p6: t' = fst(file-receive t pid f)
  shows s' ~ d ~ t'
  proof -
  {
    have a0 : s = s'
      using p5 file-receive-def
      by auto
    have a1 : t = t'
      using p6 file-receive-def
      by simp
    have a2: s' ~ d ~ t'
      using a0 a1 p2
      by blast
  }
  then show ?thesis by auto
qed

```

```

lemma file-receive-wsc-e:
  assumes p0: reachable0 s
    and p1: reachable0 t
    and p2: e = FileEvt( Event-file-receive pid f)
    and p3: s ~ d ~ t
    and p4: (the (domain-of-event e)) @ s d
    and p5: s ~ (the (domain-of-event e)) ~ t
    and p6: s' = exec-event s e
    and p7: t' = exec-event t e
  shows s' ~ d ~ t'
  proof -
  {
    have a0 : (the (domain-of-event e)) = pid
      using p2 domain-of-event-def getpid-from-file-event-def

```

```

    by force
  have a1:  $s' = fst(file-receive\ s\ pid\ f)$ 
    using p2 p6 exec-event-def by auto
  have a2:  $t' = fst(file-receive\ t\ pid\ f)$ 
    using p2 p7 exec-event-def
    by auto
  have a3:  $pid @ s d$ 
    using p4 a0
    by blast
  have a4 :  $s \sim pid \sim t$  using p5 a0
    by blast
  have a5:  $s' \sim d \sim t'$ 
    using a1 a2 a3 a4 p0 p1 p3 p5 p4 file-receive-wsc
    by blast
}
then show ?thesis by auto
qed

```

```

lemma file-receive-dwsc-e: dynamic-weakly-step-consistent-e (FileEvt( Event-file-receive
pid f))
  using dynamic-weakly-step-consistent-e-def file-receive-wsc-e
  by blast

```

29.37.14 proving "do_{dentry_oopen}" satisfying the "weakly step consistent" property

```

lemma do-dentry-open-wsc:
  assumes p0: reachable0 s
    and p1: reachable0 t
    and p2:  $s \sim d \sim t$ 
    and p3:  $pid @ s\ d$ 
    and p4:  $s \sim pid \sim t$ 
    and p5:  $s' = fst(do-dentry-open\ s\ pid\ f)$ 
    and p6:  $t' = fst(do-dentry-open\ t\ pid\ f)$ 
  shows  $s' \sim d \sim t'$ 
  proof -
  {
    have a0 :  $s = s'$ 
      using p5 do-dentry-open-def by simp
    have a1 :  $t = t'$ 
      using p6 do-dentry-open-def by auto
    have a2:  $s' \sim d \sim t'$ 
      using a0 a1 p2
      by blast
  }
  then show ?thesis by auto
qed

```

```

lemma do-dentry-open-wsc-e:

```

```

assumes  $p0$ : reachable0  $s$ 
and  $p1$ : reachable0  $t$ 
and  $p2$ :  $e = \text{FileEvt}(\text{Event-do-dentry-open } pid\ f)$ 
and  $p3$ :  $s \sim d \sim t$ 
and  $p4$ :  $(\text{the } (\text{domain-of-event } e)) @ s\ d$ 
and  $p5$ :  $s \sim (\text{the } (\text{domain-of-event } e)) \sim t$ 
and  $p6$ :  $s' = \text{exec-event } s\ e$ 
and  $p7$ :  $t' = \text{exec-event } t\ e$ 
shows  $s' \sim d \sim t'$ 
proof –
{
  have  $a0$  :  $(\text{the } (\text{domain-of-event } e)) = pid$ 
    using  $p2$  domain-of-event-def getpid-from-file-event-def
    by force
  have  $a1$ :  $s' = \text{fst}(\text{do-dentry-open } s\ pid\ f)$ 
    using  $p2\ p6$  exec-event-def by auto
  have  $a2$ :  $t' = \text{fst}(\text{do-dentry-open } t\ pid\ f)$ 
    using  $p2\ p7$  exec-event-def
    by auto
  have  $a3$ :  $pid @ s\ d$ 
    using  $p4\ a0$ 
    by blast
  have  $a4$  :  $s \sim pid \sim t$  using  $p5\ a0$ 
    by blast
  have  $a5$ :  $s' \sim d \sim t'$ 
    using  $a1\ a2\ a3\ a4\ p0\ p1\ p3\ p5\ p4$  do-dentry-open-wsc
    by blast
}
then show ?thesis by auto
qed

```

```

lemma do-dentry-open-dwsc-e: dynamic-weakly-step-consistent-e ( $\text{FileEvt}(\text{Event-do-dentry-open } pid\ f)$ )
  using dynamic-weakly-step-consistent-e-def do-dentry-open-wsc-e
  by blast

```

29.38 smack key hooks weakly step consistent

29.38.1 proving "key_{task_ppermission}" satisfying the "weakly step consistent" property

```

lemma key-task-permission-wsc:
assumes  $p0$ : reachable0  $s$ 
and  $p1$ : reachable0  $t$ 
and  $p2$ :  $s \sim d \sim t$ 
and  $p3$ :  $pid @ s\ d$ 
and  $p4$ :  $s \sim pid \sim t$ 
and  $p5$ :  $s' = \text{fst}(\text{key-task-permission } s\ pid\ \text{key-ref } cred'\ perm)$ 
and  $p6$ :  $t' = \text{fst}(\text{key-task-permission } t\ pid\ \text{key-ref } cred'\ perm)$ 
shows  $s' \sim d \sim t'$ 
proof –

```

```

{
  have a0 : s = s'
    using p5 key-task-permission-def
    by simp
  have a1 : t = t'
    using p6
    using key-task-permission-def by auto
  have a2: s' ~ d ~ t'
    using a0 a1 p2
    by blast
}
then show ?thesis by auto
qed

```

```

lemma key-task-permission-wsc-e:
  assumes p0: reachable0 s
    and p1: reachable0 t
    and p2: e = KeyEvt( Event-key-permission pid key-ref cred' perm )
    and p3: s ~ d ~ t
    and p4: (the (domain-of-event e)) @ s d
    and p5: s ~ (the (domain-of-event e)) ~ t
    and p6: s' = exec-event s e
    and p7: t' = exec-event t e
  shows s' ~ d ~ t'
  proof -
    {
      have a0 : (the (domain-of-event e)) = pid
        using p2 domain-of-event-def getpid-from-key-event-def
        by force
      have a1: s' = fst(key-task-permission s pid key-ref cred' perm)
        using p2 p6 exec-event-def by auto
      have a2: t' = fst(key-task-permission t pid key-ref cred' perm)
        using p2 p7 exec-event-def
        by auto
      have a3: pid @ s d
        using p4 a0
        by blast
      have a4 : s ~ pid ~ t using p5 a0
        by blast
      have a5: s' ~ d ~ t'
        using a1 a2 a3 a4 p0 p1 p3 p5 p4 key-task-permission-wsc
        by blast
    }
    then show ?thesis by auto
  qed

```

```

lemma key-task-permission-dwsc-e: dynamic-weakly-step-consistent-e (KeyEvt( Event-key-permission
pid key-ref cred' perm ))
  using dynamic-weakly-step-consistent-e-def key-task-permission-wsc-e

```


by *blast*

29.38.2 proving "keyctl_{get}security" satisfying the "weakly step consistent" property

lemma *keyctl-get-security-wsc*:

```

assumes p0: reachable0 s
  and p1: reachable0 t
  and p2: s ~ d ~ t
  and p3: pid @ s d
  and p4: s ~ pid ~ t
  and p5: s' = fst(keyctl-get-security s pid keyid' buffer buflen)
  and p6: t' = fst(keyctl-get-security t pid keyid' buffer buflen)
shows s' ~ d ~ t'
proof -
{
  have a0 : s = s'
    using p5 keyctl-get-security-def
    by auto
  have a1 : t = t'
    using p6 keyctl-get-security-def
    by simp
  have a2: s' ~ d ~ t'
    using a0 a1 p2
    by blast
}
then show ?thesis by auto
qed

```

lemma *keyctl-get-security-wsc-e*:

```

assumes p0: reachable0 s
  and p1: reachable0 t
  and p2: e = KeyEvt( Event-key-getsecurity pid keyid' buffer buflen)
  and p3: s ~ d ~ t
  and p4: (the (domain-of-event e)) @ s d
  and p5: s ~ (the (domain-of-event e)) ~ t
  and p6: s' = exec-event s e
  and p7: t' = exec-event t e
shows s' ~ d ~ t'
proof -
{
  have a0 : (the (domain-of-event e)) = pid
    using p2 domain-of-event-def getpid-from-key-evevt-def
    by force
  have a1: s' = fst(keyctl-get-security s pid keyid' buffer buflen)
    using p2 p6 exec-event-def by auto
  have a2: t' = fst(keyctl-get-security t pid keyid' buffer buflen)
    using p2 p7 exec-event-def
    by auto
  have a3: pid @ s d

```

```

    using p4 a0
    by blast
  have a4 : s ~ pid ~ t using p5 a0
    by blast
  have a5: s' ~ d ~ t'
    using a1 a2 a3 a4 p0 p1 p3 p5 p4 keyctl-get-security-wsc
    by blast
}
then show ?thesis by auto
qed

```

```

lemma keyctl-get-security-dwsc-e: dynamic-weakly-step-consistent-e (KeyEvt( Event-key-getsecurity
pid keyid' buffer buflen))
  using dynamic-weakly-step-consistent-e-def keyctl-get-security-wsc-e
  by blast

```

29.39 smack audit hooks weakly step consistent

29.39.1 proving "audit_{data}_t_o_eentry" satisfying the "weakly step consistent" property

```

lemma audit-data-to-entry-wsc:
  assumes p0: reachable0 s
    and p1: reachable0 t
    and p2: s ~ d ~ t
    and p3: pid @ s d
    and p4: s ~ pid ~ t
    and p5: s' = fst(audit-data-to-entry s pid )
    and p6: t' = fst(audit-data-to-entry t pid )
  shows s' ~ d ~ t'
  proof -
  {
    have a0 : s = s'
      using p5 audit-data-to-entry-def
      by (smt fstI)
    have a1 : t = t'
      using p6 audit-data-to-entry-def
      by (smt fst-conv)
    have a2: s' ~ d ~ t'
      using a0 a1 p2
      by blast
  }
  then show ?thesis by auto
qed

```

```

lemma audit-data-to-entry-wsc-e:
  assumes p0: reachable0 s
    and p1: reachable0 t
    and p2: e = AuditEvt( Event-audit-data-to-entry pid)
    and p3: s ~ d ~ t
    and p4: (the (domain-of-event e)) @ s d

```

```

    and p5: s ~ (the (domain-of-event e)) ~ t
    and p6: s' = exec-event s e
    and p7: t' = exec-event t e
  shows s' ~ d ~ t'
  proof -
    {
      have a0 : (the (domain-of-event e)) = pid
        using p2 domain-of-event-def getpid-from-aduit-evevt-def
        by force
      have a1: s' = fst(audit-data-to-entry s pid )
        using p2 p6 exec-event-def by auto
      have a2: t' = fst(audit-data-to-entry t pid )
        using p2 p7 exec-event-def
        by auto
      have a3: pid @ s d
        using p4 a0
        by blast
      have a4 : s ~ pid ~ t using p5 a0
        by blast
      have a5: s' ~ d ~ t'
        using a1 a2 a3 a4 p0 p1 p3 p5 p4 audit-data-to-entry-wsc
        by blast
    }
    then show ?thesis by auto
  qed

```

```

lemma audit-data-to-entry-dwsc-e: dynamic-weakly-step-consistent-e (AuditEvt( Event-audit-data-to-entry
pid))
  using dynamic-weakly-step-consistent-e-def audit-data-to-entry-wsc-e
  by blast

```

29.39.2 proving "audit_{dupe_{lsm}field}" satisfying the "weakly step consistent" property

lemma audit-dupe-lsm-field-wsc:

```

assumes p0: reachable0 s
    and p1: reachable0 t
    and p2: s ~ d ~ t
    and p3: pid @ s d
    and p4: s ~ pid ~ t
    and p5: s' = fst(audit-dupe-lsm-field s pid df sf)
    and p6: t' = fst(audit-dupe-lsm-field t pid df sf)
  shows s' ~ d ~ t'
  proof -
    {
      have a0 : s = s'
        using p5 audit-dupe-lsm-field-def
        by (smt fstI)
      have a1 : t = t'
        using p6 audit-dupe-lsm-field-def

```

```

    by (smt fst-conv)
  have a2:  $s' \sim d \sim t'$ 
    using a0 a1 p2
    by blast
}
then show ?thesis by auto
qed

```

```

lemma audit-dupe-lsm-field-wsc-e:
  assumes p0: reachable0 s
  and p1: reachable0 t
  and p2:  $e = \text{AuditEvt}(\text{Event-audit-dupe-lsm-field pid df sf})$ 
  and p3:  $s \sim d \sim t$ 
  and p4:  $(\text{the}(\text{domain-of-event } e)) @ s d$ 
  and p5:  $s \sim (\text{the}(\text{domain-of-event } e)) \sim t$ 
  and p6:  $s' = \text{exec-event } s e$ 
  and p7:  $t' = \text{exec-event } t e$ 
  shows  $s' \sim d \sim t'$ 
  proof -
  {
    have a0 :  $(\text{the}(\text{domain-of-event } e)) = \text{pid}$ 
      using p2 domain-of-event-def getpid-from-aduit-evevt-def
      by force
    have a1:  $s' = \text{fst}(\text{audit-dupe-lsm-field } s \text{ pid df sf})$ 
      using p2 p6 exec-event-def by auto
    have a2:  $t' = \text{fst}(\text{audit-dupe-lsm-field } t \text{ pid df sf})$ 
      using p2 p7 exec-event-def
      by auto
    have a3:  $\text{pid} @ s d$ 
      using p4 a0
      by blast
    have a4 :  $s \sim \text{pid} \sim t$  using p5 a0
      by blast
    have a5:  $s' \sim d \sim t'$ 
      using a1 a2 a3 a4 p0 p1 p3 p5 p4 audit-dupe-lsm-field-wsc
      by blast
  }
  then show ?thesis by auto
qed

```

```

lemma audit-dupe-lsm-field-dwsc-e: dynamic-weakly-step-consistent-e ( $\text{AuditEvt}(\text{Event-audit-dupe-lsm-field pid df sf})$ )
  using dynamic-weakly-step-consistent-e-def audit-dupe-lsm-field-wsc-e
  by blast

```

29.39.3 proving "update_{lsm}-rule" satisfying the "weakly step consistent" property

```

lemma update-lsm-rule-wsc:
  assumes p0: reachable0 s

```

```

and p1: reachable0 t
and p2: s ~ d ~ t
and p3: pid @ s d
and p4: s ~ pid ~ t
and p5: s' = fst(update-lsm-rule s pid krule)
and p6: t' = fst(update-lsm-rule t pid krule)
shows s' ~ d ~ t'
proof -
{
  have a0 : s = s'
    using p5 update-lsm-rule-def
    by simp
  have a1 : t = t'
    using p6 update-lsm-rule-def
    by auto
  have a2: s' ~ d ~ t'
    using a0 a1 p2
    by blast
}
then show ?thesis by auto
qed

lemma update-lsm-rule-wsc-e:
assumes p0: reachable0 s
and p1: reachable0 t
and p2: e = AuditEvt( Event-audit-rule-known pid krule)
and p3: s ~ d ~ t
and p4: (the (domain-of-event e)) @ s d
and p5: s ~ (the (domain-of-event e)) ~ t
and p6: s' = exec-event s e
and p7: t' = exec-event t e
shows s' ~ d ~ t'
proof -
{
  have a0 : (the (domain-of-event e)) = pid
    using p2 domain-of-event-def getpid-from-aduit-evevt-def
    by force
  have a1: s' = fst(update-lsm-rule s pid krule)
    using p2 p6 exec-event-def by auto
  have a2: t' = fst(update-lsm-rule t pid krule)
    using p2 p7 exec-event-def
    by auto
  have a3: pid @ s d
    using p4 a0
    by blast
  have a4 : s ~ pid ~ t using p5 a0
    by blast
  have a5: s' ~ d ~ t'
    using a1 a2 a3 a4 p0 p1 p3 p5 p4 update-lsm-rule-wsc

```

```

      by blast
    }
  then show ?thesis by auto
qed

```

```

lemma update-lsm-rule-dwsc-e: dynamic-weakly-step-consistent-e ( AuditEvt( Event-audit-rule-known
pid krule))
  using dynamic-weakly-step-consistent-e-def update-lsm-rule-wsc-e
  by blast

```

29.39.4 proving "audit_{rule_m}match" satisfying the "weakly step consistent" property

```

lemma audit-rule-match-wsc:
  assumes p0: reachable0 s
    and p1: reachable0 t
    and p2: s ~ d ~ t
    and p3: pid @ s d
    and p4: s ~ pid ~ t
    and p5: s' = fst(audit-rule-match s pid sid)
    and p6: t' = fst(audit-rule-match t pid sid)
  shows s' ~ d ~ t'
  proof -
  {
    have a0 : s = s'
      using p5 audit-rule-match-def
      by (metis fstI)
    have a1 : t = t'
      using p6 audit-rule-match-def
      by (smt fst-conv)
    have a2: s' ~ d ~ t'
      using a0 a1 p2
      by blast
  }
  then show ?thesis by auto
qed

```

```

lemma audit-rule-match-wsc-e:
  assumes p0: reachable0 s
    and p1: reachable0 t
    and p2: e = AuditEvt( Event-audit-rule-match pid sid)
    and p3: s ~ d ~ t
    and p4: (the (domain-of-event e)) @ s d
    and p5: s ~ (the (domain-of-event e)) ~ t
    and p6: s' = exec-event s e
    and p7: t' = exec-event t e
  shows s' ~ d ~ t'
  proof -
  {
    have a0 : (the (domain-of-event e)) = pid

```

```

    using p2 domain-of-event-def getpid-from-aduit-evevt-def
    by force
  have a1:  $s' = \text{fst}(\text{audit-rule-match } s \text{ pid sid})$ 
    using p2 p6 exec-event-def by auto
  have a2:  $t' = \text{fst}(\text{audit-rule-match } t \text{ pid sid})$ 
    using p2 p7 exec-event-def
    by auto
  have a3:  $\text{pid} @ s d$ 
    using p4 a0
    by blast
  have a4 :  $s \sim \text{pid} \sim t$  using p5 a0
    by blast
  have a5:  $s' \sim d \sim t'$ 
    using a1 a2 a3 a4 p0 p1 p3 p5 p4 audit-rule-match-wsc
    by blast
}
then show ?thesis by auto
qed

```

lemma *audit-rule-match-dwsc-e: dynamic-weakly-step-consistent-e* (*AuditEvt* (*Event-audit-rule-match* *pid sid*))
 using *dynamic-weakly-step-consistent-e-def* *audit-rule-match-wsc-e*
 by *blast*

29.39.5 proving "audit_{free_lsm_field}" satisfying the "weakly step consistent" property

lemma *audit-free-lsm-field-wsc:*
assumes *p0: reachable0 s*
 and *p1: reachable0 t*
 and *p2: $s \sim d \sim t$*
 and *p3: $\text{pid} @ s d$*
 and *p4: $s \sim \text{pid} \sim t$*
 and *p5: $s' = \text{fst}(\text{audit-free-lsm-field } s \text{ pid } f)$*
 and *p6: $t' = \text{fst}(\text{audit-free-lsm-field } t \text{ pid } f)$*
shows $s' \sim d \sim t'$
proof –
{
 have *a0* : $s = s'$
 using *p5* *audit-free-lsm-field-def*
 by *simp*
 have *a1* : $t = t'$
 using *p6* *audit-free-lsm-field-def*
 by *auto*
 have *a2*: $s' \sim d \sim t'$
 using *a0 a1 p2*
 by *blast*
}
 then show ?thesis by *auto*
qed

```

lemma audit-free-lsm-field-wsc-e:
  assumes  $p0$ : reachable0  $s$ 
    and  $p1$ : reachable0  $t$ 
    and  $p2$ :  $e = \text{AuditEvt}(\text{Event-audit-rule-free } pid\ f)$ 
    and  $p3$ :  $s \sim d \sim t$ 
    and  $p4$ :  $(\text{the } (\text{domain-of-event } e)) @ s\ d$ 
    and  $p5$ :  $s \sim (\text{the } (\text{domain-of-event } e)) \sim t$ 
    and  $p6$ :  $s' = \text{exec-event } s\ e$ 
    and  $p7$ :  $t' = \text{exec-event } t\ e$ 
  shows  $s' \sim d \sim t'$ 
  proof –
    {
      have  $a0$  :  $(\text{the } (\text{domain-of-event } e)) = pid$ 
        using  $p2$  domain-of-event-def getpid-from-aduit-evevt-def
        by force
      have  $a1$ :  $s' = \text{fst}(\text{audit-free-lsm-field } s\ pid\ f)$ 
        using  $p2\ p6$  exec-event-def by auto
      have  $a2$ :  $t' = \text{fst}(\text{audit-free-lsm-field } t\ pid\ f)$ 
        using  $p2\ p7$  exec-event-def
        by auto
      have  $a3$ :  $pid @ s\ d$ 
        using  $p4\ a0$ 
        by blast
      have  $a4$  :  $s \sim pid \sim t$  using  $p5\ a0$ 
        by blast
      have  $a5$ :  $s' \sim d \sim t'$ 
        using  $a1\ a2\ a3\ a4\ p0\ p1\ p3\ p5\ p4$  audit-free-lsm-field-wsc
        by blast
    }
  then show ?thesis by auto
qed

```

```

lemma audit-free-lsm-field-dwsc-e: dynamic-weakly-step-consistent-e ( $\text{AuditEvt}(\text{Event-audit-rule-free } pid\ f)$ )
  using dynamic-weakly-step-consistent-e-def audit-free-lsm-field-wsc-e
  by blast

```

29.40 smack sock hooks weakly step consistent

29.40.1 proving "unix_sstream_cconnect" satisfying the "weakly step consistent" property

```

lemma unix-stream-connect-wsc:
  assumes  $p0$ : reachable0  $s$ 
    and  $p1$ : reachable0  $t$ 
    and  $p2$ :  $s \sim d \sim t$ 
    and  $p3$ :  $pid @ s\ d$ 
    and  $p4$ :  $s \sim pid \sim t$ 
    and  $p5$ :  $s' = \text{fst}(\text{unix-stream-connect } s\ pid\ sock\ uaddr\ addr-len\ flags')$ 
    and  $p6$ :  $t' = \text{fst}(\text{unix-stream-connect } t\ pid\ sock\ uaddr\ addr-len\ flags')$ 

```



```

shows  $s' \sim d \sim t'$ 
proof -
{
  have  $a0 : s = s'$ 
    using  $p5$  unix-stream-connect-def
    by (smt fstI)
  have  $a1 : t = t'$ 
    using  $p6$  unix-stream-connect-def
    by (smt fst-conv)
  have  $a2 : s' \sim d \sim t'$ 
    using  $a0$   $a1$   $p2$ 
    by blast
}
then show ?thesis by auto
qed

lemma unix-stream-connect-wsc-e:
  assumes  $p0 : \text{reachable0 } s$ 
  and  $p1 : \text{reachable0 } t$ 
  and  $p2 : e = \text{SocketEvt}(\text{Event-unix-stream-connect } pid \text{ sock } uaddr \text{ addr-len } flags')$ 
  and  $p3 : s \sim d \sim t$ 
  and  $p4 : (\text{the } (\text{domain-of-event } e)) @ s d$ 
  and  $p5 : s \sim (\text{the } (\text{domain-of-event } e)) \sim t$ 
  and  $p6 : s' = \text{exec-event } s e$ 
  and  $p7 : t' = \text{exec-event } t e$ 
shows  $s' \sim d \sim t'$ 
proof -
{
  have  $a0 : (\text{the } (\text{domain-of-event } e)) = pid$ 
    using  $p2$  domain-of-event-def getpid-from-socket-event-def
    by force
  have  $a1 : s' = \text{fst}(\text{unix-stream-connect } s \text{ pid sock } uaddr \text{ addr-len } flags')$ 
    using  $p2$   $p6$  exec-event-def by auto
  have  $a2 : t' = \text{fst}(\text{unix-stream-connect } t \text{ pid sock } uaddr \text{ addr-len } flags')$ 
    using  $p2$   $p7$  exec-event-def
    by auto
  have  $a3 : pid @ s d$ 
    using  $p4$   $a0$ 
    by blast
  have  $a4 : s \sim pid \sim t$  using  $p5$   $a0$ 
    by blast
  have  $a5 : s' \sim d \sim t'$ 
    using  $a1$   $a2$   $a3$   $a4$   $p0$   $p1$   $p3$  unix-stream-connect-wsc
    by blast
}
then show ?thesis by auto
qed

```

```

lemma unix-stream-connect-dwsc-e: dynamic-weakly-step-consistent-e (SocketEvt(
Event-unix-stream-connect pid sock uaddr addr-len flags' ))
  using dynamic-weakly-step-consistent-e-def unix-stream-connect-wsc-e
  by blast

```

29.40.2 proving "unix_{dgram}connect" satisfying the "weakly step consistent" property

```

lemma unix-dgram-connect-wsc:

```

```

  assumes p0: reachable0 s
    and p1: reachable0 t
    and p2: s ~ d ~ t
    and p3: pid @ s d
    and p4: s ~ pid ~ t
    and p5: s' = fst(unix-dgram-connect s pid sock uaddr alen flags')
    and p6: t' = fst(unix-dgram-connect t pid sock uaddr alen flags')
  shows s' ~ d ~ t'
  proof –
  {
    have a0 : s = s'
      using p5 unix-dgram-connect-def
      by (smt fstI)
    have a1 : t = t'
      using p6 unix-dgram-connect-def
      by (smt fst-conv)
    have a2: s' ~ d ~ t'
      using a0 a1 p2
      by blast
  }
  then show ?thesis by auto
qed

```

```

lemma unix-dgram-connect-wsc-e:

```

```

  assumes p0: reachable0 s
    and p1: reachable0 t
    and p2: e = SocketEvt( Event-unix-dgram-connect pid sock uaddr alen flags'
  )
    and p3: s ~ d ~ t
    and p4: (the (domain-of-event e)) @ s d
    and p5: s ~ (the (domain-of-event e)) ~ t
    and p6: s' = exec-event s e
    and p7: t' = exec-event t e
  shows s' ~ d ~ t'
  proof –
  {
    have a0 : (the (domain-of-event e)) = pid
      using p2 domain-of-event-def getpid-from-socket-event-def
      by force
    have a1: s' = fst(unix-dgram-connect s pid sock uaddr alen flags')
      using p2 p6 exec-event-def by auto

```

```

have a2:  $t' = fst(\text{unix-dgram-connect } t \text{ pid sock uaddr alen flags'})$ 
  using p2 p7 exec-event-def
  by auto
have a3:  $pid @ s d$ 
  using p4 a0
  by blast
have a4 :  $s \sim pid \sim t$  using p5 a0
  by blast
have a5:  $s' \sim d \sim t'$ 
  using a1 a2 a3 a4 p0 p1 p3 unix-dgram-connect-wsc
  by blast
}
then show ?thesis by auto
qed

```

```

lemma unix-dgram-connect-dwsc-e: dynamic-weakly-step-consistent-e (SocketEvt(
Event-unix-dgram-connect pid sock uaddr alen flags' ))
  using dynamic-weakly-step-consistent-e-def unix-dgram-connect-wsc-e
  by blast

```

29.40.3 proving "unix_{dgram}sendmsg" satisfying the "weakly step consistent" property

```

lemma unix-dgram-sendmsg-wsc:
  assumes p0: reachable0 s
    and p1: reachable0 t
    and p2:  $s \sim d \sim t$ 
    and p3:  $pid @ s d$ 
    and p4:  $s \sim pid \sim t$ 
    and p5:  $s' = fst(\text{unix-dgram-sendmsg } s \text{ pid sock uaddr alen})$ 
    and p6:  $t' = fst(\text{unix-dgram-sendmsg } t \text{ pid sock uaddr alen})$ 
  shows  $s' \sim d \sim t'$ 
  proof -
  {
    have a0 :  $s = s'$ 
      using p5 unix-dgram-sendmsg-def
      by (smt fstI)
    have a1 :  $t = t'$ 
      using p6 unix-dgram-sendmsg-def
      by (smt fst-conv)
    have a2:  $s' \sim d \sim t'$ 
      using a0 a1 p2
      by blast
  }
  then show ?thesis by auto
qed

```

```

lemma unix-dgram-sendmsg-wsc-e:
  assumes p0: reachable0 s
    and p1: reachable0 t

```

```

and p2: e = SocketEvt( Event-unix-dgram-sendmsg pid sock uaddr alen)
and p3: s ~ d ~ t
and p4: (the (domain-of-event e)) @ s d
and p5: s ~ (the (domain-of-event e)) ~ t
and p6: s' = exec-event s e
and p7: t' = exec-event t e
shows s' ~ d ~ t'
proof -
{
have a0 : (the (domain-of-event e)) = pid
  using p2 domain-of-event-def getpid-from-socket-event-def
  by force
have a1: s' = fst(unix-dgram-sendmsg s pid sock uaddr alen)
  using p2 p6 exec-event-def by auto
have a2: t' = fst(unix-dgram-sendmsg t pid sock uaddr alen)
  using p2 p7 exec-event-def
  by auto
have a3: pid @ s d
  using p4 a0
  by blast
have a4 : s ~ pid ~ t using p5 a0
  by blast
have a5: s' ~ d ~ t'
  using a1 a2 a3 a4 p0 p1 p3 unix-dgram-sendmsg-wsc
  by blast
}
then show ?thesis by auto
qed

```

```

lemma unix-dgram-sendmsg-dwsc-e: dynamic-weakly-step-consistent-e (SocketEvt(
Event-unix-dgram-sendmsg pid sock uaddr alen))
  using dynamic-weakly-step-consistent-e-def unix-dgram-sendmsg-wsc-e
  by blast

```

29.40.4 proving "sys_{bind}" satisfying the "weakly step consistent" property

```

lemma sys-bind'-wsc:
assumes p0: reachable0 s
and p1: reachable0 t
and p2: s ~ d ~ t
and p3: pid @ s d
and p4: s ~ pid ~ t
and p5: s' = fst(sys-bind' s pid fd umyaddr addrlen)
and p6: t' = fst(sys-bind' t pid fd umyaddr addrlen)
shows s' ~ d ~ t'
proof -
{
have a0 : s = s'
  using p5 sys-bind'-def

```

```

    by (smt fstI)
  have a1 : t = t'
    using p6 sys-bind'-def
    by (smt fst-conv)
  have a2: s' ~ d ~ t'
    using a0 a1 p2
    by blast
}
then show ?thesis by auto
qed

```

```

lemma sys-bind'-wsc-e:
  assumes p0: reachable0 s
    and p1: reachable0 t
    and p2: e = SocketEvt( Event-sys-bind' pid fd umyaddr addrlen )
    and p3: s ~ d ~ t
    and p4: (the (domain-of-event e)) @ s d
    and p5: s ~ (the (domain-of-event e)) ~ t
    and p6: s' = exec-event s e
    and p7: t' = exec-event t e
  shows s' ~ d ~ t'
  proof -
    {
      have a0 : (the (domain-of-event e)) = pid
        using p2 domain-of-event-def getpid-from-socket-event-def
        by force
      have a1: s' = fst(sys-bind' s pid fd umyaddr addrlen)
        using p2 p6 exec-event-def by auto
      have a2: t' = fst(sys-bind' t pid fd umyaddr addrlen)
        using p2 p7 exec-event-def
        by auto
      have a3: pid @ s d
        using p4 a0
        by blast
      have a4 : s ~ pid ~ t using p5 a0
        by blast
      have a5: s' ~ d ~ t'
        using a1 a2 a3 a4 p0 p1 p3 sys-bind'-wsc
        by blast
    }
  then show ?thesis by auto
qed

```

```

lemma sys-bind'-dwsc-e: dynamic-weakly-step-consistent-e (SocketEvt( Event-sys-bind'
pid fd umyaddr addrlen ))
  using dynamic-weakly-step-consistent-e-def sys-bind'-wsc-e
  by blast

```

29.40.5 proving "sys_cconnect'" satisfying the "weakly step consistent" property

```

lemma sys-connect'-wsc:
  assumes p0: reachable0 s
    and p1: reachable0 t
    and p2: s ~ d ~ t
    and p3: pid @ s d
    and p4: s ~ pid ~ t
    and p5: s' = fst(sys-connect' s pid fd servaddr addrlen)
    and p6: t' = fst(sys-connect' t pid fd servaddr addrlen)
  shows s' ~ d ~ t'
  proof -
  {
    have a0 : s = s'
      using p5 sys-connect'-def
      by (smt fstI)
    have a1 : t = t'
      using p6 sys-connect'-def
      by (smt fst-conv)
    have a2: s' ~ d ~ t'
      using a0 a1 p2
      by blast
  }
  then show ?thesis by auto
qed

lemma sys-connect'-wsc-e:
  assumes p0: reachable0 s
    and p1: reachable0 t
    and p2: e = SocketEvt( Event-sys-connect' pid fd servaddr addrlen)
    and p3: s ~ d ~ t
    and p4: (the (domain-of-event e)) @ s d
    and p5: s ~ (the (domain-of-event e)) ~ t
    and p6: s' = exec-event s e
    and p7: t' = exec-event t e
  shows s' ~ d ~ t'
  proof -
  {
    have a0 : (the (domain-of-event e)) = pid
      using p2 domain-of-event-def getpid-from-socket-event-def
      by force
    have a1: s' = fst(sys-connect' s pid fd servaddr addrlen)
      using p2 p6 exec-event-def by auto
    have a2: t' = fst(sys-connect' t pid fd servaddr addrlen)
      using p2 p7 exec-event-def
      by auto
    have a3: pid @ s d
      using p4 a0
      by blast
    have a4 : s ~ pid ~ t using p5 a0

```

```

    by blast
  have a5:  $s' \sim d \sim t'$ 
    using a1 a2 a3 a4 p0 p1 p3 sys-connect'-wsc
    by blast
}
then show ?thesis by auto
qed

```

```

lemma sys-connect'-dwsc-e: dynamic-weakly-step-consistent-e (SocketEvt( Event-sys-connect'
pid fd useraddr addrlen))
  using dynamic-weakly-step-consistent-e-def sys-connect'-wsc-e
  by blast

```

29.40.6 proving "sock_sendmsg" satisfying the "weakly step consistent" property

```

lemma sock-sendmsg-wsc:
  assumes p0: reachable0 s
    and p1: reachable0 t
    and p2:  $s \sim d \sim t$ 
    and p3: pid @ s d
    and p4:  $s \sim pid \sim t$ 
    and p5:  $s' = fst(sock-sendmsg s pid sock msg)$ 
    and p6:  $t' = fst(sock-sendmsg t pid sock msg)$ 
  shows  $s' \sim d \sim t'$ 
  proof -
  {
    have a0 :  $s = s'$ 
      using p5 sock-sendmsg-def
      by (smt fstI)
    have a1 :  $t = t'$ 
      using p6 sock-sendmsg-def
      by (smt fst-conv)
    have a2:  $s' \sim d \sim t'$ 
      using a0 a1 p2
      by blast
  }
  then show ?thesis by auto
qed

```

```

lemma sock-sendmsg-wsc-e:
  assumes p0: reachable0 s
    and p1: reachable0 t
    and p2:  $e = SocketEvt( Event-sock-sendmsg pid sock msg)$ 
    and p3:  $s \sim d \sim t$ 
    and p4: (the (domain-of-event e)) @ s d
    and p5:  $s \sim (the (domain-of-event e)) \sim t$ 
    and p6:  $s' = exec-event s e$ 
    and p7:  $t' = exec-event t e$ 
  shows  $s' \sim d \sim t'$ 

```

```

proof –
{
  have  $a0$  : (the (domain-of-event  $e$ )) =  $pid$ 
    using  $p2$  domain-of-event-def getpid-from-socket-event-def
    by force
  have  $a1$  :  $s' = fst(sock-sendmsg\ s\ pid\ sock\ msg)$ 
    using  $p2\ p6$  exec-event-def by auto
  have  $a2$  :  $t' = fst(sock-sendmsg\ t\ pid\ sock\ msg)$ 
    using  $p2\ p7$  exec-event-def
    by auto
  have  $a3$  :  $pid @ sd$ 
    using  $p4\ a0$ 
    by blast
  have  $a4$  :  $s \sim pid \sim t$  using  $p5\ a0$ 
    by blast
  have  $a5$  :  $s' \sim d \sim t'$ 
    using  $a1\ a2\ a3\ a4\ p0\ p1\ p3$  sock-sendmsg-wsc
    by blast
}
then show ?thesis by auto
qed

```

```

lemma sock-sendmsg-dwsc-e: dynamic-weakly-step-consistent-e (SocketEvt( Event-sock-sendmsg
 $pid\ sock\ msg$  ))
  using dynamic-weakly-step-consistent-e-def sock-sendmsg-wsc-e
  by blast

```

29.40.7 proving "sock_recvmsg" satisfying the "weakly step consistent" property

```

lemma sock-recvmsg-wsc:
assumes  $p0$ : reachable0  $s$ 
  and  $p1$ : reachable0  $t$ 
  and  $p2$ :  $s \sim d \sim t$ 
  and  $p3$ :  $pid @ s\ d$ 
  and  $p4$ :  $s \sim pid \sim t$ 
  and  $p5$ :  $s' = fst(sock-recvmsg\ s\ pid\ sock\ msg\ flags')$ 
  and  $p6$ :  $t' = fst(sock-recvmsg\ t\ pid\ sock\ msg\ flags')$ 
shows  $s' \sim d \sim t'$ 
proof –
{
  have  $a0$  :  $s = s'$ 
    using  $p5$  sock-recvmsg-def
    by simp
  have  $a1$  :  $t = t'$ 
    using  $p6$  sock-recvmsg-def
    by auto
  have  $a2$ :  $s' \sim d \sim t'$ 
    using  $a0\ a1\ p2$ 
    by blast
}

```



```

}
then show ?thesis by auto
qed

```

```

lemma sock-recvmmsg-wsc-e:
  assumes p0: reachable0 s
  and p1: reachable0 t
  and p2: e = SocketEvt( Event-sock-recvmmsg pid sock msg flags' )
  and p3: s ~ d ~ t
  and p4: (the (domain-of-event e)) @ s d
  and p5: s ~ (the (domain-of-event e)) ~ t
  and p6: s' = exec-event s e
  and p7: t' = exec-event t e
shows s' ~ d ~ t'
proof -
  {
    have a0 : (the (domain-of-event e)) = pid
      using p2 domain-of-event-def getpid-from-socket-event-def
      by force
    have a1: s' = fst(sock-recvmmsg s pid sock msg flags')
      using p2 p6 exec-event-def by auto
    have a2: t' = fst(sock-recvmmsg t pid sock msg flags')
      using p2 p7 exec-event-def
      by auto
    have a3: pid @ s d
      using p4 a0
      by blast
    have a4 : s ~ pid ~ t using p5 a0
      by blast
    have a5: s' ~ d ~ t'
      using a1 a2 a3 a4 p0 p1 p3 sock-recvmmsg-wsc
      by blast
  }
  then show ?thesis by auto
qed

```

```

lemma sock-recvmmsg-dwsc-e: dynamic-weakly-step-consistent-e (SocketEvt( Event-sock-recvmmsg
pid sock msg flags'))
  using dynamic-weakly-step-consistent-e-def sock-recvmmsg-wsc-e
  by blast

```

29.40.8 proving "sk_{filter}trim_{cap}" satisfying the "weakly step consistent" property

```

lemma sk-filter-trim-cap-wsc:
  assumes p0: reachable0 s
  and p1: reachable0 t
  and p2: s ~ d ~ t
  and p3: pid @ s d
  and p4: s ~ pid ~ t

```

```

    and p5:  $s' = fst(sk-filter-trim-cap\ s\ pid\ sk'\ skb\ cap)$ 
    and p6:  $t' = fst(sk-filter-trim-cap\ t\ pid\ sk'\ skb\ cap)$ 
shows  $s' \sim d \sim t'$ 
proof -
{
  have a0:  $s = s'$ 
    using p5 sk-filter-trim-cap-def
    by (smt fstI)
  have a1:  $t = t'$ 
    using p6 sk-filter-trim-cap-def
    by (smt fst-conv)
  have a2:  $s' \sim d \sim t'$ 
    using a0 a1 p2
    by blast
}
then show ?thesis by auto
qed

lemma sk-filter-trim-cap-wsc-e:
assumes p0: reachable0 s
  and p1: reachable0 t
  and p2:  $e = SocketEvt( Event-sk-filter-trim-cap\ pid\ sk'\ skb\ cap )$ 
  and p3:  $s \sim d \sim t$ 
  and p4:  $(the\ (domain-of-event\ e)) @ s\ d$ 
  and p5:  $s \sim (the\ (domain-of-event\ e)) \sim t$ 
  and p6:  $s' = exec-event\ s\ e$ 
  and p7:  $t' = exec-event\ t\ e$ 
shows  $s' \sim d \sim t'$ 
proof -
{
  have a0:  $(the\ (domain-of-event\ e)) = pid$ 
    using p2 domain-of-event-def getpid-from-socket-event-def
    by force
  have a1:  $s' = fst(sk-filter-trim-cap\ s\ pid\ sk'\ skb\ cap)$ 
    using p2 p6 exec-event-def by auto
  have a2:  $t' = fst(sk-filter-trim-cap\ t\ pid\ sk'\ skb\ cap)$ 
    using p2 p7 exec-event-def
    by auto
  have a3:  $pid @ s\ d$ 
    using p4 a0
    by blast
  have a4:  $s \sim pid \sim t$  using p5 a0
    by blast
  have a5:  $s' \sim d \sim t'$ 
    using a1 a2 a3 a4 p0 p1 p3 sk-filter-trim-cap-wsc
    by blast
}
then show ?thesis by auto
qed

```

```

lemma sk-filter-trim-cap-dwsc-e: dynamic-weakly-step-consistent-e (SocketEvt( Event-sk-filter-trim-cap
pid sk' skb cap ))
  using dynamic-weakly-step-consistent-e-def sk-filter-trim-cap-wsc-e
  by blast

```

29.40.9 proving "sock_ggetsockopt" satisfying the "weaklystepconsistent" property

```

lemma sock-getsockopt-cap-wsc:
  assumes p0: reachable0 s
    and p1: reachable0 t
    and p2: s ~ d ~ t
    and p3: pid @ s d
    and p4: s ~ pid ~ t
    and p5: s' = fst(sock-getsockopt s pid sock level' optname optval optlen)
    and p6: t' = fst(sock-getsockopt t pid sock level' optname optval optlen)
  shows s' ~ d ~ t'
  proof –
  {
    have a0 : s = s'
      using p5 sock-getsockopt-def
      by (smt fstI)
    have a1 : t = t'
      using p6 sock-getsockopt-def
      by (smt fst-conv)
    have a2: s' ~ d ~ t'
      using a0 a1 p2
      by blast
  }
  then show ?thesis by auto
qed

```

```

lemma sock-getsockopt-wsc-e:
  assumes p0: reachable0 s
    and p1: reachable0 t
    and p2: e = SocketEvt( Event-sock-getsockopt pid sock level' optname optval
optlen )
    and p3: s ~ d ~ t
    and p4: (the (domain-of-event e)) @ s d
    and p5: s ~ (the (domain-of-event e)) ~ t
    and p6: s' = exec-event s e
    and p7: t' = exec-event t e
  shows s' ~ d ~ t'
  proof –
  {
    have a0 : (the (domain-of-event e)) = pid
      using p2 domain-of-event-def getpid-from-socket-event-def
      by force
    have a1: s' = fst(sock-getsockopt s pid sock level' optname optval optlen)

```

```

    using p2 p6 exec-event-def by auto
  have a2:  $t' = \text{fst}(\text{sock-getsockopt } t \text{ pid sock level' optname optval optlen})$ 
    using p2 p7 exec-event-def
    by auto
  have a3:  $\text{pid} @ s d$ 
    using p4 a0
    by blast
  have a4 :  $s \sim \text{pid} \sim t$  using p5 a0
    by blast
  have a5:  $s' \sim d \sim t'$ 
    using a1 a2 a3 a4 p0 p1 p3 sock-getsockopt-cap-wsc
    by blast
}
then show ?thesis by auto
qed

```

```

lemma sock-getsockopt-dwsc-e: dynamic-weakly-step-consistent-e ( SocketEvt( Event-sock-getsockopt
pid sock level' optname optval optlen ))
  using dynamic-weakly-step-consistent-e-def sock-getsockopt-wsc-e
  by blast

```

29.40.10 proving "unix_{getpeersec}dgram" satisfying the "weaklystepconsistent" property

```

lemma unix-get-peersec-dgram-wsc:
  assumes p0: reachable0 s
    and p1: reachable0 t
    and p2:  $s \sim d \sim t$ 
    and p3:  $\text{pid} @ s d$ 
    and p4:  $s \sim \text{pid} \sim t$ 
    and p5:  $s' = \text{fst}(\text{unix-get-peersec-dgram } s \text{ pid sock scm } )$ 
    and p6:  $t' = \text{fst}(\text{unix-get-peersec-dgram } t \text{ pid sock scm } )$ 
  shows  $s' \sim d \sim t'$ 
  proof -
  {
    have a0 :  $s = s'$ 
      using p5 unix-get-peersec-dgram-def
      by (smt fstI)
    have a1 :  $t = t'$ 
      using p6 unix-get-peersec-dgram-def
      by (smt fst-conv)
    have a2:  $s' \sim d \sim t'$ 
      using a0 a1 p2
      by blast
  }
  then show ?thesis by auto
qed

```

```

lemma unix-get-peersec-dgram-wsc-e:
  assumes p0: reachable0 s

```

```

and p1: reachable0 t
and p2: e = SocketEvt( Event-unix-get-peersec-dgram pid sock scm )
and p3: s ~ d ~ t
and p4: (the (domain-of-event e)) @ s d
and p5: s ~ (the (domain-of-event e)) ~ t
and p6: s' = exec-event s e
and p7: t' = exec-event t e
shows s' ~ d ~ t'
proof -
{
have a0 : (the (domain-of-event e)) = pid
  using p2 domain-of-event-def getpid-from-socket-event-def
  by force
have a1: s' = fst(unix-get-peersec-dgram s pid sock scm )
  using p2 p6 exec-event-def by auto
have a2: t' = fst(unix-get-peersec-dgram t pid sock scm )
  using p2 p7 exec-event-def
  by auto
have a3: pid @ s d
  using p4 a0
  by blast
have a4 : s ~ pid ~ t using p5 a0
  by blast
have a5: s' ~ d ~ t'
  using a1 a2 a3 a4 p0 p1 p3 unix-get-peersec-dgram-wsc
  by blast
}
then show ?thesis by auto
qed

lemma unix-get-peersec-dgram-dwsc-e: dynamic-weakly-step-consistent-e (SocketEvt(
Event-unix-get-peersec-dgram pid sock scm))
  using dynamic-weakly-step-consistent-e-def unix-get-peersec-dgram-wsc-e
  by blast

```

29.41 smack inodes hooks weakly step consistent

29.41.1 proving "vfs_{link}" satisfying the "weakly step consistent" property

lemma *vfs-link-wsc*:

```

assumes p0: reachable0 s
and p1: reachable0 t
and p2: s ~ d ~ t
and p3: pid @ s d
and p4: s ~ pid ~ t
and p5: s' = fst(vfs-link s pid old-dentry dir new-dentry delegated-inode)
and p6: t' = fst(vfs-link t pid old-dentry dir new-dentry delegated-inode)
shows s' ~ d ~ t'
proof -
{

```

```

    have a0 : s = s'
      using p5 vfs-link-def
      by (smt fstI)
    have a1 : t = t'
      using p6 vfs-link-def
      by (smt fst-conv)
    have a2: s' ~ d ~ t'
      using a0 a1 p2
      by blast
  }
  then show ?thesis by auto
qed

lemma vfs-link-wsc-e:
  assumes p0: reachable0 s
    and p1: reachable0 t
    and p2: e = InodeEvt( Event-vfs-link pid old-dentry dir new-dentry delegated-inode
  )
    and p3: s ~ d ~ t
    and p4: (the (domain-of-event e)) @ s d
    and p5: s ~ (the (domain-of-event e)) ~ t
    and p6: s' = exec-event s e
    and p7: t' = exec-event t e
  shows s' ~ d ~ t'
  proof -
    {
      have a0 : (the (domain-of-event e)) = pid
        using p2 domain-of-event-def getpid-from-inode-evevt-def
        by force
      have a1: s' = fst(vfs-link s pid old-dentry dir new-dentry delegated-inode)
        using p2 p6 exec-event-def by auto
      have a2: t' = fst(vfs-link t pid old-dentry dir new-dentry delegated-inode)
        using p2 p7 exec-event-def
        by auto
      have a3: pid @ s d
        using p4 a0
        by blast
      have a4 : s ~ pid ~ t using p5 a0
        by blast
      have a5: s' ~ d ~ t'
        using a1 a2 a3 a4 p0 p1 p3 vfs-link-wsc
        by blast
    }
    then show ?thesis by auto
  qed

lemma vfs-link-dwsc-e: dynamic-weakly-step-consistent-e (InodeEvt( Event-vfs-link
pid old-dentry dir new-dentry delegated-inode ))
  using dynamic-weakly-step-consistent-e-def vfs-link-wsc-e

```

by *blast*

29.41.2 proving "*vfs_uunlink*" satisfying the "weakly step consistent" property

lemma *vfs-unlink-wsc*:

```

assumes p0: reachable0 s
  and p1: reachable0 t
  and p2: s ~ d ~ t
  and p3: pid @ s d
  and p4: s ~ pid ~ t
  and p5: s' = fst(vfs-unlink s pid dir dentry delegated-inode)
  and p6: t' = fst(vfs-unlink t pid dir dentry delegated-inode)
shows s' ~ d ~ t'
proof –
{
  have a0 : s = s'
    using p5 vfs-unlink-def
    by (smt fstI)
  have a1 : t = t'
    using p6 vfs-unlink-def
    by (smt fst-conv)
  have a2: s' ~ d ~ t'
    using a0 a1 p2
    by blast
}
then show ?thesis by auto
qed

```

lemma *vfs-unlink-wsc-e*:

```

assumes p0: reachable0 s
  and p1: reachable0 t
  and p2: e = InodeEvt( Event-vfs-unlink pid dir dentry delegated-inode)
  and p3: s ~ d ~ t
  and p4: (the (domain-of-event e)) @ s d
  and p5: s ~ (the (domain-of-event e)) ~ t
  and p6: s' = exec-event s e
  and p7: t' = exec-event t e
shows s' ~ d ~ t'
proof –
{
  have a0 : (the (domain-of-event e)) = pid
    using p2 domain-of-event-def getpid-from-inode-event-def
    by force
  have a1: s' = fst(vfs-unlink s pid dir dentry delegated-inode)
    using p2 p6 exec-event-def by auto
  have a2: t' = fst(vfs-unlink t pid dir dentry delegated-inode)
    using p2 p7 exec-event-def
    by auto
  have a3: pid @ s d

```

```

    using p4 a0
  by blast
have a4 : s ~ pid ~ t using p5 a0
  by blast
have a5: s' ~ d ~ t'
  using a1 a2 a3 a4 p0 p1 p3 vfs-unlink-wsc
  by blast
}
then show ?thesis by auto
qed

```

lemma *vfs-unlink-dwsc-e: dynamic-weakly-step-consistent-e* (*InodeEvt*(*Event-vfs-unlink* *pid dir dentry delegated-inode*))
 using *dynamic-weakly-step-consistent-e-def* *vfs-unlink-wsc-e*
 by blast

29.41.3 proving "vfs_{rmdir}" satisfying the "weakly step consistent" property

lemma *vfs-rmdir-wsc:*
assumes *p0: reachable0 s*
 and *p1: reachable0 t*
 and *p2: s ~ d ~ t*
 and *p3: pid @ s d*
 and *p4: s ~ pid ~ t*
 and *p5: s' = fst(vfs-rmdir s pid dir dentry)*
 and *p6: t' = fst(vfs-rmdir t pid dir dentry)*
shows *s' ~ d ~ t'*
proof –
{
 have *a0 : s = s'*
 using *p5 vfs-rmdir-def*
 by (*smt fstI*)
 have *a1 : t = t'*
 using *p6 vfs-rmdir-def*
 by (*smt fst-conv*)
 have *a2: s' ~ d ~ t'*
 using *a0 a1 p2*
 by blast
}
then show ?thesis by auto
qed

lemma *vfs-rmdir-wsc-e:*
assumes *p0: reachable0 s*
 and *p1: reachable0 t*
 and *p2: e = InodeEvt(Event-vfs-rmdir pid dir dentry)*
 and *p3: s ~ d ~ t*
 and *p4: (the (domain-of-event e)) @ s d*
 and *p5: s ~ (the (domain-of-event e)) ~ t*


```

    and p6: s' = exec-event s e
    and p7: t' = exec-event t e
shows s' ~ d ~ t'
proof -
{
  have a0 : (the (domain-of-event e)) = pid
    using p2 domain-of-event-def getpid-from-inode-event-def
    by force
  have a1: s' = fst(vfs-rmdir s pid dir dentry )
    using p2 p6 exec-event-def by auto
  have a2: t' = fst(vfs-rmdir t pid dir dentry )
    using p2 p7 exec-event-def
    by auto
  have a3: pid @ s d
    using p4 a0
    by blast
  have a4 : s ~ pid ~ t using p5 a0
    by blast
  have a5: s' ~ d ~ t'
    using a1 a2 a3 a4 p0 p1 p3 vfs-rmdir-wsc
    by blast
}
then show ?thesis by auto
qed

```

```

lemma vfs-rmdir-dwsc-e: dynamic-weakly-step-consistent-e ( InodeEvt( Event-vfs-rmdir
pid dir dentry))
  using dynamic-weakly-step-consistent-e-def vfs-rmdir-wsc-e
  by blast

```

29.41.4 proving "vfs_rrename" satisfying the "weaklystepconsistent" property

```

lemma vfs-rename-wsc:
assumes p0: reachable0 s
  and p1: reachable0 t
  and p2: s ~ d ~ t
  and p3: pid @ s d
  and p4: s ~ pid ~ t
  and p5: s' = fst(vfs-rename s pid old-dir old-dentry new-dir new-dentry
delegated-inode flgs)
  and p6: t' = fst(vfs-rename t pid old-dir old-dentry new-dir new-dentry
delegated-inode flgs)
shows s' ~ d ~ t'
proof -
{
  have a0 : s = s'
    using p5 vfs-rename-def
    by (smt fstI)
  have a1 : t = t'

```

```

    using p6 vfs-rename-def
    by (smt fst-conv)
    have a2:  $s' \sim d \sim t'$ 
    using a0 a1 p2
    by blast
  }
  then show ?thesis by auto
qed

```

```

lemma vfs-rename-wsc-e:
  assumes p0: reachable0 s
  and p1: reachable0 t
  and p2:  $e = \text{InodeEvt}(\text{Event-vfs-rename pid old-dir old-dentry new-dir}$ 
     $\text{new-dentry delegated-inode flgs})$ 
  and p3:  $s \sim d \sim t$ 
  and p4:  $(\text{the}(\text{domain-of-event } e)) @ s d$ 
  and p5:  $s \sim (\text{the}(\text{domain-of-event } e)) \sim t$ 
  and p6:  $s' = \text{exec-event } s e$ 
  and p7:  $t' = \text{exec-event } t e$ 
  shows  $s' \sim d \sim t'$ 
  proof -
    {
      have a0 :  $(\text{the}(\text{domain-of-event } e)) = \text{pid}$ 
      using p2 domain-of-event-def getpid-from-inode-evevt-def
      by force
      have a1:  $s' = \text{fst}(\text{vfs-rename } s \text{ pid old-dir old-dentry new-dir new-dentry}$ 
         $\text{delegated-inode flgs})$ 
      using p2 p6 exec-event-def by auto
      have a2:  $t' = \text{fst}(\text{vfs-rename } t \text{ pid old-dir old-dentry new-dir new-dentry}$ 
         $\text{delegated-inode flgs})$ 
      using p2 p7 exec-event-def
      by auto
      have a3:  $\text{pid} @ s d$ 
      using p4 a0
      by blast
      have a4 :  $s \sim \text{pid} \sim t$  using p5 a0
      by blast
      have a5:  $s' \sim d \sim t'$ 
      using a1 a2 a3 a4 p0 p1 p3 vfs-rename-wsc
      by blast
    }
    then show ?thesis by auto
  qed

```

```

lemma vfs-rename-dwsc-e: dynamic-weakly-step-consistent-e ( $\text{InodeEvt}(\text{Event-vfs-rename}$ 
   $\text{pid old-dir old-dentry new-dir new-dentry delegated-inode flgs})$ )
  using dynamic-weakly-step-consistent-e-def vfs-rename-wsc-e
  by blast

```

29.41.5 proving "inode_{permission}" satisfying the "weakly step consistent" property

lemma *inode-permission-wsc*:

```

assumes p0: reachable0 s
  and p1: reachable0 t
  and p2: s ~ d ~ t
  and p3: pid @ s d
  and p4: s ~ pid ~ t
  and p5: s' = fst(inode-permission s pid inode mask')
  and p6: t' = fst(inode-permission t pid inode mask')
shows s' ~ d ~ t'
proof -
{
  have a0 : s = s'
    using p5 inode-permission-def
    by (smt fstI)
  have a1 : t = t'
    using p6 inode-permission-def
    by (smt fst-conv)
  have a2: s' ~ d ~ t'
    using a0 a1 p2
    by blast
}
then show ?thesis by auto
qed

```

lemma *inode-permission-wsc-e*:

```

assumes p0: reachable0 s
  and p1: reachable0 t
  and p2: e = InodeEvt( Event-inode-permission pid inode mask' )
  and p3: s ~ d ~ t
  and p4: (the (domain-of-event e)) @ s d
  and p5: s ~ (the (domain-of-event e)) ~ t
  and p6: s' = exec-event s e
  and p7: t' = exec-event t e
shows s' ~ d ~ t'
proof -
{
  have a0 : (the (domain-of-event e)) = pid
    using p2 domain-of-event-def getpid-from-inode-event-def
    by force
  have a1: s' = fst(inode-permission s pid inode mask')
    using p2 p6 exec-event-def by auto
  have a2: t' = fst(inode-permission t pid inode mask')
    using p2 p7 exec-event-def
    by auto
  have a3: pid @ s d
    using p4 a0
    by blast
  have a4 : s ~ pid ~ t using p5 a0

```

```

    by blast
  have a5:  $s' \sim d \sim t'$ 
    using a1 a2 a3 a4 p0 p1 p3 inode-permission-wsc
    by blast
}
then show ?thesis by auto
qed

```

```

lemma inode-permission-dwsc-e: dynamic-weakly-step-consistent-e (InodeEvt( Event-inode-permission
pid inode mask' ))
  using dynamic-weakly-step-consistent-e-def inode-permission-wsc-e
  by blast

```

29.41.6 proving "notify_{change}" satisfying the "weakly step consistent" property

```

lemma notify-change-wsc:
  assumes p0: reachable0 s
    and p1: reachable0 t
    and p2:  $s \sim d \sim t$ 
    and p3: pid @ s d
    and p4:  $s \sim pid \sim t$ 
    and p5:  $s' = fst(notify-change\ s\ pid\ dentry\ attr'\ delegated-inode\ )$ 
    and p6:  $t' = fst(notify-change\ t\ pid\ dentry\ attr'\ delegated-inode\ )$ 
  shows  $s' \sim d \sim t'$ 
  proof -
  {
    have a0 :  $s = s'$ 
      using p5 notify-change-def
      by (smt fstI)
    have a1 :  $t = t'$ 
      using p6 notify-change-def
      by (smt fst-conv)
    have a2:  $s' \sim d \sim t'$ 
      using a0 a1 p2
      by blast
  }
  then show ?thesis by auto
qed

```

```

lemma notify-change-wsc-e:
  assumes p0: reachable0 s
    and p1: reachable0 t
    and p2:  $e = InodeEvt( Event-notify-change\ pid\ dentry\ attr'\ delegated-inode\ )$ 
  )
    and p3:  $s \sim d \sim t$ 
    and p4:  $(the\ (domain-of-event\ e)) @ s\ d$ 
    and p5:  $s \sim (the\ (domain-of-event\ e)) \sim t$ 
    and p6:  $s' = exec-event\ s\ e$ 
    and p7:  $t' = exec-event\ t\ e$ 

```

```

shows  $s' \sim d \sim t'$ 
proof -
{
  have  $a0 : (the (domain-of-event e)) = pid$ 
    using  $p2$  domain-of-event-def getpid-from-inode-event-def
    by force
  have  $a1 : s' = fst(notify-change s pid dentry attr' delegated-inode )$ 
    using  $p2$   $p6$  exec-event-def by auto
  have  $a2 : t' = fst(notify-change t pid dentry attr' delegated-inode )$ 
    using  $p2$   $p7$  exec-event-def
    by auto
  have  $a3 : pid @ sd$ 
    using  $p4$   $a0$ 
    by blast
  have  $a4 : s \sim pid \sim t$  using  $p5$   $a0$ 
    by blast
  have  $a5 : s' \sim d \sim t'$ 
    using  $a1$   $a2$   $a3$   $a4$   $p0$   $p1$   $p3$  notify-change-wsc
    by blast
}
then show ?thesis by auto
qed

```

```

lemma notify-change-dwsc-e: dynamic-weakly-step-consistent-e (InodeEvt (Event-notify-change
pid dentry attr' delegated-inode ))
using dynamic-weakly-step-consistent-e-def notify-change-wsc-e
by blast

```

29.41.7 proving "fat_{ioctl_set_aattributes}" satisfying the "weakly step consistent" property

```

lemma fat-ioctl-set-attributes-wsc:
assumes  $p0 : reachable0 s$ 
and  $p1 : reachable0 t$ 
and  $p2 : s \sim d \sim t$ 
and  $p3 : pid @ s d$ 
and  $p4 : s \sim pid \sim t$ 
and  $p5 : s' = fst(fat-ioctl-set-attributes s pid f)$ 
and  $p6 : t' = fst(fat-ioctl-set-attributes t pid f)$ 
shows  $s' \sim d \sim t'$ 
proof -
{
  have  $a0 : s = s'$ 
    using  $p5$  fat-ioctl-set-attributes-def
    by (smt fstI)
  have  $a1 : t = t'$ 
    using  $p6$  fat-ioctl-set-attributes-def
    by (smt fst-conv)
  have  $a2 : s' \sim d \sim t'$ 
    using  $a0$   $a1$   $p2$ 

```

```

    by blast
  }
  then show ?thesis by auto
qed

```

```

lemma fat-iocctl-set-attributes-wsc-e:
  assumes p0: reachable0 s
    and p1: reachable0 t
    and p2: e = InodeEvt( Event-fat-iocctl-set-attributes pid f)
    and p3: s ~ d ~ t
    and p4: (the (domain-of-event e)) @ s d
    and p5: s ~ (the (domain-of-event e)) ~ t
    and p6: s' = exec-event s e
    and p7: t' = exec-event t e
  shows s' ~ d ~ t'
  proof -
    {
      have a0 : (the (domain-of-event e)) = pid
        using p2 domain-of-event-def getpid-from-inode-evevt-def
        by force
      have a1: s' = fst(fat-iocctl-set-attributes s pid f)
        using p2 p6 exec-event-def by auto
      have a2: t' = fst(fat-iocctl-set-attributes t pid f)
        using p2 p7 exec-event-def
        by auto
      have a3: pid @ s d
        using p4 a0
        by blast
      have a4 : s ~ pid ~ t using p5 a0
        by blast
      have a5: s' ~ d ~ t'
        using a1 a2 a3 a4 p0 p1 p3 fat-iocctl-set-attributes-wsc
        by blast
    }
    then show ?thesis by auto
  qed

```

```

lemma fat-iocctl-set-attributes-dwsc-e: dynamic-weakly-step-consistent-e (InodeEvt(
  Event-fat-iocctl-set-attributes pid f ))
  using dynamic-weakly-step-consistent-e-def fat-iocctl-set-attributes-wsc-e
  by blast

```

29.41.8 proving "vfs_getattr" satisfying the "weaklystepconsistent" property

```

lemma vfs-getattr-wsc:
  assumes p0: reachable0 s
    and p1: reachable0 t
    and p2: s ~ d ~ t
    and p3: pid @ s d

```

```

    and p4:  $s \sim pid \sim t$ 
    and p5:  $s' = fst(vfs-getattr\ s\ pid\ path)$ 
    and p6:  $t' = fst(vfs-getattr\ t\ pid\ path)$ 
  shows  $s' \sim d \sim t'$ 
  proof -
  {
    have a0:  $s = s'$ 
      using p5 vfs-getattr-def
      by (smt fstI)
    have a1:  $t = t'$ 
      using p6 vfs-getattr-def
      by (smt fst-conv)
    have a2:  $s' \sim d \sim t'$ 
      using a0 a1 p2
      by blast
  }
  then show ?thesis by auto
qed

lemma vfs-getattr-wsc-e:
  assumes p0: reachable0 s
  and p1: reachable0 t
  and p2:  $e = InodeEvt(\ Event-vfs-getattr\ pid\ path\ )$ 
  and p3:  $s \sim d \sim t$ 
  and p4:  $(the\ (domain-of-event\ e)) @ s\ d$ 
  and p5:  $s \sim (the\ (domain-of-event\ e)) \sim t$ 
  and p6:  $s' = exec-event\ s\ e$ 
  and p7:  $t' = exec-event\ t\ e$ 
  shows  $s' \sim d \sim t'$ 
  proof -
  {
    have a0:  $(the\ (domain-of-event\ e)) = pid$ 
      using p2 domain-of-event-def getpid-from-inode-evevt-def
      by force
    have a1:  $s' = fst(vfs-getattr\ s\ pid\ path)$ 
      using p2 p6 exec-event-def by auto
    have a2:  $t' = fst(vfs-getattr\ t\ pid\ path)$ 
      using p2 p7 exec-event-def
      by auto
    have a3:  $pid @ s\ d$ 
      using p4 a0
      by blast
    have a4:  $s \sim pid \sim t$  using p5 a0
      by blast
    have a5:  $s' \sim d \sim t'$ 
      using a1 a2 a3 a4 p0 p1 p3 vfs-getattr-wsc
      by blast
  }
  then show ?thesis by auto

```

qed

lemma *vfs-getattr-dwsc-e: dynamic-weakly-step-consistent-e* (*InodeEvt*(*Event-vfs-getattr* *pid path*))
 using *dynamic-weakly-step-consistent-e-def* *vfs-getattr-wsc-e*
 by *blast*

29.41.9 proving "vfs_setxattr" satisfying the "weakly step consistent" property

lemma *vfs-setxattr-wsc:*
assumes *p0: reachable0 s*
 and *p1: reachable0 t*
 and *p2: s ~ d ~ t*
 and *p3: pid @ s d*
 and *p4: s ~ pid ~ t*
 and *p5: s' = fst(vfs-setxattr s pid dentry name value size' flgs)*
 and *p6: t' = fst(vfs-setxattr t pid dentry name value size' flgs)*
shows *s' ~ d ~ t'*
proof –
 {
 have *a0 : s = s'*
 using *p5 vfs-setxattr-def*
 by (*smt fstI*)
 have *a1 : t = t'*
 using *p6 vfs-setxattr-def*
 by (*smt fst-conv*)
 have *a2: s' ~ d ~ t'*
 using *a0 a1 p2*
 by *blast*
 }
then show *?thesis* by *auto*
 qed

lemma *vfs-setxattr-wsc-e:*
assumes *p0: reachable0 s*
 and *p1: reachable0 t*
 and *p2: e = InodeEvt(Event-vfs-setxattr pid dentry name value size' flgs)*
 and *p3: s ~ d ~ t*
 and *p4: (the (domain-of-event e)) @ s d*
 and *p5: s ~ (the (domain-of-event e)) ~ t*
 and *p6: s' = exec-event s e*
 and *p7: t' = exec-event t e*
shows *s' ~ d ~ t'*
proof –
 {
 have *a0 : (the (domain-of-event e)) = pid*
 using *p2 domain-of-event-def getpid-from-inode-event-def*
 by *force*
 have *a1: s' = fst(vfs-setxattr s pid dentry name value size' flgs)*


```

    using p2 p6 exec-event-def by auto
  have a2:  $t' = \text{fst}(\text{vfs-setxattr } t \text{ pid dentry name value size' flgs})$ 
    using p2 p7 exec-event-def
    by auto
  have a3:  $\text{pid} @ s d$ 
    using p4 a0
    by blast
  have a4 :  $s \sim \text{pid} \sim t$  using p5 a0
    by blast
  have a5:  $s' \sim d \sim t'$ 
    using a1 a2 a3 a4 p0 p1 p3 vfs-setxattr-wsc
    by blast
}
then show ?thesis by auto
qed

```

```

lemma vfs-setxattr-dwsc-e: dynamic-weakly-step-consistent-e (InodeEvt( Event-vfs-setxattr
pid dentry name value size' flgs))
  using dynamic-weakly-step-consistent-e-def vfs-setxattr-wsc-e
  by blast

```

29.41.10 proving "vfs_getxattr" satisfying the "weakly step consistent" property

```

lemma vfs-getxattr-wsc:
  assumes p0: reachable0 s
    and p1: reachable0 t
    and p2:  $s \sim d \sim t$ 
    and p3:  $\text{pid} @ s d$ 
    and p4:  $s \sim \text{pid} \sim t$ 
    and p5:  $s' = \text{fst}(\text{vfs-getxattr } s \text{ pid dentry name value size' })$ 
    and p6:  $t' = \text{fst}(\text{vfs-getxattr } t \text{ pid dentry name value size' })$ 
  shows  $s' \sim d \sim t'$ 
  proof -
  {
    have a0 :  $s = s'$ 
      using p5 vfs-getxattr-def
      by (smt fstI)
    have a1 :  $t = t'$ 
      using p6 vfs-getxattr-def
      by (smt fst-conv)
    have a2:  $s' \sim d \sim t'$ 
      using a0 a1 p2
      by blast
  }
  then show ?thesis by auto
qed

```

```

lemma vfs-getxattr-wsc-e:
  assumes p0: reachable0 s

```

```

and p1: reachable0 t
and p2: e = InodeEvt( Event-vfs-getxattr pid dentry name value size' )
and p3: s ~ d ~ t
and p4: (the (domain-of-event e)) @ s d
and p5: s ~ (the (domain-of-event e)) ~ t
and p6: s' = exec-event s e
and p7: t' = exec-event t e
shows s' ~ d ~ t'
proof -
{
  have a0 : (the (domain-of-event e)) = pid
    using p2 domain-of-event-def getpid-from-inode-event-def
    by force
  have a1: s' = fst(vfs-getxattr s pid dentry name value size' )
    using p2 p6 exec-event-def by auto
  have a2: t' = fst(vfs-getxattr t pid dentry name value size' )
    using p2 p7 exec-event-def
    by auto
  have a3: pid @ s d
    using p4 a0
    by blast
  have a4 : s ~ pid ~ t using p5 a0
    by blast
  have a5: s' ~ d ~ t'
    using a1 a2 a3 a4 p0 p1 p3 vfs-getxattr-wsc
    by blast
}
then show ?thesis by auto
qed

```

```

lemma vfs-getxattr-dwsc-e: dynamic-weakly-step-consistent-e (InodeEvt( Event-vfs-getxattr
pid dentry name value size'))
  using dynamic-weakly-step-consistent-e-def vfs-getxattr-wsc-e
  by blast

```

29.41.11 proving "vfs_removeattr" satisfying the "weakly step consistent" property

```

lemma vfs-removeattr-wsc:
assumes p0: reachable0 s
and p1: reachable0 t
and p2: s ~ d ~ t
and p3: pid @ s d
and p4: s ~ pid ~ t
and p5: s' = fst(vfs-removeattr s pid dentry name)
and p6: t' = fst(vfs-removeattr t pid dentry name)
shows s' ~ d ~ t'
proof -
{
  have a0 : s = s'

```

```

    using p5 vfs-removeattr-def
    by (smt fstI)
  have a1 : t = t'
    using p6 vfs-removeattr-def
    by (smt fst-conv)
  have a2: s' ~ d ~ t'
    using a0 a1 p2
    by blast
}
then show ?thesis by auto
qed

```

```

lemma vfs-removeattr-wsc-e:
  assumes p0: reachable0 s
  and p1: reachable0 t
  and p2: e = InodeEvt( Event-vfs-removeattr pid dentry name)
  and p3: s ~ d ~ t
  and p4: (the (domain-of-event e)) @ s d
  and p5: s ~ (the (domain-of-event e)) ~ t
  and p6: s' = exec-event s e
  and p7: t' = exec-event t e
shows s' ~ d ~ t'
proof -
  {
    have a0 : (the (domain-of-event e)) = pid
      using p2 domain-of-event-def getpid-from-inode-evevt-def
      by force
    have a1: s' = fst(vfs-removeattr s pid dentry name)
      using p2 p6 exec-event-def by auto
    have a2: t' = fst(vfs-removeattr t pid dentry name)
      using p2 p7 exec-event-def
      by auto
    have a3: pid @ s d
      using p4 a0
      by blast
    have a4 : s ~ pid ~ t using p5 a0
      by blast
    have a5: s' ~ d ~ t'
      using a1 a2 a3 a4 p0 p1 p3 vfs-removeattr-wsc
      by blast
  }
  then show ?thesis by auto
qed

```

```

lemma vfs-removeattr-dwsc-e: dynamic-weakly-step-consistent-e (InodeEvt( Event-vfs-removeattr
pid dentry name))
  using dynamic-weakly-step-consistent-e-def vfs-removeattr-wsc-e
  by blast

```

29.41.12 proving "xattr_{getsecurity}" satisfying the "weakly step consistent" property

lemma xattr-getsecurity-wsc:

```

assumes p0: reachable0 s
  and p1: reachable0 t
  and p2: s ~ d ~ t
  and p3: pid @ s d
  and p4: s ~ pid ~ t
  and p5: s' = fst(xattr-getsecurity s pid inode name value size')
  and p6: t' = fst(xattr-getsecurity t pid inode name value size')
shows s' ~ d ~ t'
proof -
{
  have a0 : s = s'
    using p5 xattr-getsecurity-def
    by (smt fstI)
  have a1 : t = t'
    using p6 xattr-getsecurity-def
    by (smt fst-conv)
  have a2: s' ~ d ~ t'
    using a0 a1 p2
    by blast
}
then show ?thesis by auto
qed

```

lemma xattr-getsecurity-wsc-e:

```

assumes p0: reachable0 s
  and p1: reachable0 t
  and p2: e = InodeEvt( Event-xattr-getsecurity pid inode name value size')
  and p3: s ~ d ~ t
  and p4: (the (domain-of-event e)) @ s d
  and p5: s ~ (the (domain-of-event e)) ~ t
  and p6: s' = exec-event s e
  and p7: t' = exec-event t e
shows s' ~ d ~ t'
proof -
{
  have a0 : (the (domain-of-event e)) = pid
    using p2 domain-of-event-def getpid-from-inode-event-def
    by force
  have a1: s' = fst(xattr-getsecurity s pid inode name value size')
    using p2 p6 exec-event-def by auto
  have a2: t' = fst(xattr-getsecurity t pid inode name value size')
    using p2 p7 exec-event-def
    by auto
  have a3: pid @ s d
    using p4 a0
    by blast
  have a4 : s ~ pid ~ t using p5 a0

```

```

    by blast
  have a5:  $s' \sim d \sim t'$ 
    using a1 a2 a3 a4 p0 p1 p3 xattr-getsecurity-wsc
    by blast
}
then show ?thesis by auto
qed

```

```

lemma xattr-getsecurity-dwsc-e: dynamic-weakly-step-consistent-e (InodeEvt( Event-xattr-getsecurity
pid inode name value size'))
  using dynamic-weakly-step-consistent-e-def xattr-getsecurity-wsc-e
  by blast

```

29.41.13 proving "nfs4_llistxattr_nfs4_llabel" satisfying the "weakly step consistent" property

```

lemma nfs4-listxattr-nfs4-label-wsc:
  assumes p0: reachable0 s
    and p1: reachable0 t
    and p2:  $s \sim d \sim t$ 
    and p3:  $pid @ s d$ 
    and p4:  $s \sim pid \sim t$ 
    and p5:  $s' = fst(nfs4-listxattr-nfs4-label s pid inode name size')$ 
    and p6:  $t' = fst(nfs4-listxattr-nfs4-label t pid inode name size')$ 
  shows  $s' \sim d \sim t'$ 
  proof -
  {
    have a0 :  $s = s'$ 
      using p5 nfs4-listxattr-nfs4-label-def
      by (smt fstI)
    have a1 :  $t = t'$ 
      using p6 nfs4-listxattr-nfs4-label-def
      by (smt fst-conv)
    have a2:  $s' \sim d \sim t'$ 
      using a0 a1 p2
      by blast
  }
  then show ?thesis by auto
qed

```

```

lemma nfs4-listxattr-nfs4-label-wsc-e:
  assumes p0: reachable0 s
    and p1: reachable0 t
    and p2:  $e = InodeEvt( Event-nfs4-listxattr-nfs4-label pid inode name size')$ 
    and p3:  $s \sim d \sim t$ 
    and p4:  $(the (domain-of-event e)) @ s d$ 
    and p5:  $s \sim (the (domain-of-event e)) \sim t$ 
    and p6:  $s' = exec-event s e$ 
    and p7:  $t' = exec-event t e$ 
  shows  $s' \sim d \sim t'$ 

```

```

proof -
{
  have a0 : (the (domain-of-event e)) = pid
    using p2 domain-of-event-def getpid-from-inode-event-def
    by force
  have a1: s' = fst(nfs4-listxattr-nfs4-label s pid inode name size')
    using p2 p6 exec-event-def by auto
  have a2: t' = fst(nfs4-listxattr-nfs4-label t pid inode name size')
    using p2 p7 exec-event-def
    by auto
  have a3: pid @ s d
    using p4 a0
    by blast
  have a4 : s ~ pid ~ t using p5 a0
    by blast
  have a5: s' ~ d ~ t'
    using a1 a2 a3 a4 p0 p1 p3 nfs4-listxattr-nfs4-label-wsc
    by blast
}
then show ?thesis by auto
qed

```

```

lemma nfs4-listxattr-nfs4-label-dwsc-e: dynamic-weakly-step-consistent-e (InodeEvt(
  Event-nfs4-listxattr-nfs4-label pid inode name size'))
  using dynamic-weakly-step-consistent-e-def nfs4-listxattr-nfs4-label-wsc-e
  by blast

```

29.41.14 proving "sockfs_{listxattr}" satisfying the "weakly step consistent" property

```

lemma sockfs-listxattr-wsc:
  assumes p0: reachable0 s
    and p1: reachable0 t
    and p2: s ~ d ~ t
    and p3: pid @ s d
    and p4: s ~ pid ~ t
    and p5: s' = fst(sockfs-listxattr s pid dentry buffer size')
    and p6: t' = fst(sockfs-listxattr t pid dentry buffer size')
  shows s' ~ d ~ t'
  proof -
  {
    have a0 : s = s'
      using p5 sockfs-listxattr-def
      by (smt fstI)
    have a1 : t = t'
      using p6 sockfs-listxattr-def
      by (smt fst-conv)
    have a2: s' ~ d ~ t'
      using a0 a1 p2
      by blast
  }

```

```

}
then show ?thesis by auto
qed

```

```

lemma sockfs-listxattr-wsc-e:
  assumes p0: reachable0 s
    and p1: reachable0 t
    and p2: e = InodeEvt( Event-sockfs-listxattr pid dentry buffer size')
    and p3: s ~ d ~ t
    and p4: (the (domain-of-event e)) @ s d
    and p5: s ~ (the (domain-of-event e)) ~ t
    and p6: s' = exec-event s e
    and p7: t' = exec-event t e
  shows s' ~ d ~ t'
  proof -
    {
      have a0 : (the (domain-of-event e)) = pid
        using p2 domain-of-event-def getpid-from-inode-event-def
        by force
      have a1: s' = fst(sockfs-listxattr s pid dentry buffer size')
        using p2 p6 exec-event-def by auto
      have a2: t' = fst(sockfs-listxattr t pid dentry buffer size')
        using p2 p7 exec-event-def
        by auto
      have a3: pid @ s d
        using p4 a0
        by blast
      have a4 : s ~ pid ~ t using p5 a0
        by blast
      have a5: s' ~ d ~ t'
        using a1 a2 a3 a4 p0 p1 p3 sockfs-listxattr-wsc
        by blast
    }
  then show ?thesis by auto
qed

```

```

lemma sockfs-listxattr-dwsc-e: dynamic-weakly-step-consistent-e ( InodeEvt( Event-sockfs-listxattr
pid dentry buffer size'))
  using dynamic-weakly-step-consistent-e-def sockfs-listxattr-wsc-e
  by blast

```

29.41.15 proving the "dynamic step consistent" property

```

theorem dynamic-weakly-step-consistent:dynamic-weakly-step-consistent
proof -
  {
    fix e
    have dynamic-weakly-step-consistent-e e
      apply(induct e)

```

```

        using sb-copy-data-dwsc-e do-remount-dwsc-e show-sb-opts-dwsc-e
        statfs-by-dentry-dwsc-e do-mount-dwsc-e do-umount-dwsc-e pivot-root-dwsc-e
setup-security-options-dwsc-e
        set-sb-security-dwsc-e nfs-clone-sb-security-dwsc-e parse-security-options-dwsc-e
mount-fs-dwsc-e
        apply (metis Event-sb.exhaust)
    using prepare-creds-dwsc-e
        sys-setreuid-dwsc-e setpgid-dwsc-e do-getpgid-dwsc-e
        getsid-dwsc-e getsecid-dwsc-e task-setnice-dwsc-e
        set-task-ioprio-dwsc-e
        get-task-ioprio-dwsc-e
        check-prlimit-permission-dwsc-e
        do-prlimit-dwsc-e
        task-setscheduler-dwsc-e
        task-getscheduler-dwsc-e
        task-movememory-dwsc-e
        task-kill-dwsc-e
        task-prctl-dwsc-e
    apply (metis Event-tsk.exhaust)
using ptrace-may-access-dwsc-e ptrace-traceme-dwsc-e Event-Ptrace.exhaust
    apply metis
    using check-syslog-permissions-dwsc-e prepare-binprm-dwsc-e
    apply (metis Event-sys.exhaust)
    using do-iocctl-dwsc-e syscall-iocctl-dwsc-e
ksys-iocctl-dwsc-e vm-mmap-pgoff-dwsc-e do-sys-vm86-dwsc-e get-unmapped-area-dwsc-e
    validate-mmap-request-dwsc-e generic-setlease-dwsc-e syscall-lock-dwsc-e
    do-lock-file-wait-dwsc-e file-fcntl-dwsc-e
    file-send-sigiotask-dwsc-e file-receive-dwsc-e do-dentry-open-dwsc-e
    apply (metis Event-file.exhaust)
using ipcperms-dwsc-e audit-ipc-obj-dwsc-e
    msg-queue-msgctl-dwsc-e do-msgsnd-dwsc-e msg-queue-msgrcv-dwsc-e
ksys-shmget-dwsc-e sem-msgctl-dwsc-e do-semtimedop-dwsc-e do-shmat-dwsc-e

    ksys-semget-dwsc-e shm-msgctl-dwsc-e ksys-msgget-dwsc-e
    apply (metis Event-ipc.exhaust)
    using key-task-permission-dwsc-e
        keyctl-get-security-dwsc-e apply (metis Event-Key.exhaust)
using audit-data-to-entry-dwsc-e audit-dupe-lsm-field-dwsc-e update-lsm-rule-dwsc-e
    audit-rule-match-dwsc-e audit-free-lsm-field-dwsc-e
    using Event-audit.exhaust apply metis

using unix-stream-connect-dwsc-e unix-dgram-connect-dwsc-e unix-dgram-sendmsg-dwsc-e

    sys-bind'-dwsc-e
sys-connect'-dwsc-e sock-sendmsg-dwsc-e sock-recvmsg-dwsc-e sk-filter-trim-cap-dwsc-e

    sock-getsockopt-dwsc-e unix-get-peersec-dgram-dwsc-e
    apply (metis Event-network-sock.exhaust)
using vfs-link-dwsc-e

```



```

    vfs-unlink-dwsc-e
    vfs-rmdir-dwsc-e
    vfs-rename-dwsc-e
    inode-permission-dwsc-e
    notify-change-dwsc-e
    fat-iocctl-set-attributes-dwsc-e
    vfs-getattr-dwsc-e
    vfs-setxattr-dwsc-e
    vfs-getxattr-dwsc-e
    vfs-removexattr-dwsc-e
    xattr-getsecurity-dwsc-e
    nfs4-listxattr-nfs4-label-dwsc-e
    sockfs-listxattr-dwsc-e
  by (metis Event-inode.exhaust)
}
then show ?thesis
  using dynamic-weakly-step-consistent-all-evt by blast
qed

```

29.42 Information flow security of linux LSM specification

theorem *noninfluence-sat: noninfluence*
using *dynamic-local-respect uc-eq-noninf dynamic-weakly-step-consistent weak-with-step-cons*
by *blast*

theorem *weak-noninfluence-sat: weak-noninfluence* **using** *noninf-impl-weak noninfluence-sat*
by *blast*

theorem *nonleakage-sat: nonleakage*
using *noninf-impl-nonlk noninfluence-sat* **by** *blast*

theorem *noninterference-r-sat: noninterference-r*
using *noninf-impl-nonintf-r noninfluence-sat* **by** *blast*

theorem *noninterference-sat: noninterference*
using *noninterference-r-sat nonintf-r-impl-noninterf* **by** *blast*

theorem *weak-noninterference-r-sat: weak-noninterference-r*
using *noninterference-r-sat nonintf-r-impl-wk-nonintf-r* **by** *blast*

theorem *weak-noninterference-sat: weak-noninterference*
using *noninterference-sat nonintf-impl-weak* **by** *blast*

end
end

29.43 smack_h

theory *smack-h*
imports

```

    Main
    HOL.Real
    HOL.String
    ../../LSM/Element
begin
typedecl mutex
typedecl list-head
typedecl hlist-node

* Use IPv6 port labeling if IPv6 is enabled and secmarks * are not being
used.

definition SMACK-IPV6-PORT-LABELING ≡ 1

definition SMACK-IPV6-SECMARK-LABELING ≡ 1
definition SMK-LABELLEN ≡ 24
definition SMK-CIPSOLEN ≡ 24
definition SMK-LOGLABEL ≡ 256

record smack-known =
    smack-known :: string
    smack-secid :: nat
    smack-rules :: list-head
    smack-netlabel :: netlbl-lsm-secattr

record superblock-smack = smack-root :: smack-known
    smack-floor :: smack-known
    smack-hat :: smack-known
    smack-default :: smack-known
    smack-flags :: int

definition SMK-SB-INITIALIZED ≡ 0x01
definition SMK-SB-UNTRUSTED ≡ 0x02

record socket-smack = smack-out :: smack-known
    smack-in :: smack-known
    smack-packet :: smack-known option

record inode-smack = smack-inode :: smack-known
    smack-itask :: smack-known option
    smack-mmap :: smack-known option
    smack-lock :: mutex
    smack-iflags :: int
    smack-rcu :: rcu-head

record task-smack = smack-task :: smack-known
    smack-forked :: smack-known
    smack-rule :: list-head

```

```

smk-rules-lock :: mutex
smk-relabel :: smack-known list

record smack-rule =
    smk-subject :: smack-known
    smk-object :: smack-known
    smk-access :: int

record smk-net4addr = net4-list :: list-head
    net4-smk-host :: in-addr
    net4-smk-mask :: in-addr
    net4-smk-masks :: int
    net4-smk-label :: smack-known

record smk-net6addr = list :: list-head
    smk-host :: in6-addr
    smk-mask :: in6-addr
    smk-masks :: int
    smk-label :: smack-known

typedecl short
record smk-port-label = list :: list-head
    smk-sock :: sock
    smk-port :: nat
    lsmk-in :: smack-known
    l-smk-out :: smack-known
    smk-sock-type :: short
    smk-can-reuse :: short

record smack-known-list-elem = list :: list-head
    smk-label :: smack-known

record Config-SECURITY-SMACK = SECURITY-SMACK :: bool
    SECURITY-SMACK-BRINGUP :: bool
    SECURITY-SMACK-NETFILTER :: bool
    SECURITY-SMACK-APPEND-SIGNALS :: bool
    SMACK-IPV6-SECMARK-LABELING :: bool
    SMACK-IPV6-PORT-LABELING :: bool
    CONFIG-IPV6 :: bool
    CONFIG-SECURITY-SMACK-NETFILTER :: bool
    CONFIG-SECURITY-SMACK-APPEND-SIGNALS :: bool

consts conf :: Config-SECURITY-SMACK

```

definition *FSDEFAULT-MNT* $\equiv 0x01$
definition *FSFLOOR-MNT* $\equiv 0x02$
definition *FSHAT-MNT* $\equiv 0x04$
definition *FSROOT-MNT* $\equiv 0x08$
definition *FSTRANS-MNT* $\equiv 0x10$
definition *NUM-SMK-MNT-OPTS* $\equiv 5$

definition *SMK-FSDEFAULT* $\equiv \text{"smackfsdef="}$
definition *SMK-FSFLOOR* $\equiv \text{"smackfsfloor="}$
definition *SMK-FSHAT* $\equiv \text{"smackfshat="}$
definition *SMK-FSROOT* $\equiv \text{"smackfsroot="}$
definition *SMK-FSTRANS* $\equiv \text{"smackfstransmute="}$

definition *SMACK-DELETE-OPTION* $\equiv \text{"-DELETE"}$
definition *SMACK-CIPSO-OPTION* $\equiv \text{"-CIPSO"}$

definition *SMACK-UNLABELED-SOCKET* $\equiv 0$
definition *SMACK-CIPSO-SOCKET* $\equiv 1$

definition *SMACK-CIPSO-DOI-DEFAULT* $\equiv 3$
definition *SMACK-CIPSO-DOI-INVALID* $\equiv -1$
definition *SMACK-CIPSO-DIRECT-DEFAULT* $\equiv 250$
definition *SMACK-CIPSO-MAPPED-DEFAULT* $\equiv 251$
definition *SMACK-CIPSO-MAXLEVEL* $\equiv 255$
definition *SMACK-CIPSO-MAXCATNUM* $\equiv 184$

definition *SMACK-PTRACE-DEFAULT* $\equiv 0$
definition *SMACK-PTRACE-EXACT* $\equiv 1$
definition *SMACK-PTRACE-DRACONIAN* $\equiv 2$
definition *SMACK-PTRACE-MAX* $\equiv \text{SMACK-PTRACE-DRACONIAN}$

definition *MAY-TRANSMUTE* $\equiv 0x00001000$
definition *MAY-LOCK* $\equiv 0x00002000$
definition *MAY-BRINGUP* $\equiv 0x00004000$
definition *MAY-DELIVER* $\equiv \text{if CONFIG-SECURITY-SMACK-APPEND-SIGNALS}$
conf then MAY-APPEND else MAY-WRITE

definition *MAY-ANYREAD* $\equiv \text{bitOR MAY-READ MAY-EXEC}$
definition *MAY-NOT* $\equiv 0$
definition *MAY-READWRITE* $\equiv \text{bitOR MAY-READ MAY-WRITE}$

definition *SMACK-BRINGUP-ALLOW* $\equiv 1$
definition *SMACK-UNCONFINED-SUBJECT* $\equiv 2$

definition *SMACK-UNCONFINED-OBJECT* $\equiv 3$

definition *SMK-INODE-INSTANT* $\equiv 1$

definition *SMK-INODE-TRANSMUTE* $\equiv 2$

definition *SMK-INODE-CHANGED* $\equiv 4$

definition *SMK-INODE-IMPURE* $\equiv 8$

definition *TRANS-TRUE-SIZE* $\equiv 4$

definition *SMK-CONNECTING* $\equiv 0$

definition *SMK-RECEIVING* $\equiv 1$

definition *SMK-SENDING* $\equiv 2$

consts *smack-known-list* :: *smack-known list*

record *smack-audit-data* = *func* :: *string*

subject :: *string*

object :: *string*

request :: *string*

result :: *int*

typedecl *common-audit-data*

record *smk-audit-info* = *smk-a* :: *common-audit-data*

sad :: *smack-audit-data*

definition *smk-of-task* :: *task-smack* \Rightarrow *smack-known*

where *smk-of-task tsp* = *smk-task tsp*

definition *smk-of-forked* :: *task-smack* \Rightarrow *smack-known*

where *smk-of-forked tsp* = *smk-forked tsp*

definition *SMACK-AUDIT-DENIED* $\equiv 0x1$

definition *SMACK-AUDIT-ACCEPT* $\equiv 0x2$

end

29.44 smack hooks

theory *SmackHooks*

imports

../.. / LSM / Element

../.. / LSM / Linux-LSM-Model

../.. / LSM / LSM-Cap

../FSP / smack-h

Main

HOL.Real

HOL.String

HOL- Word. Word-Bitwise

../.. / lib / Monad-WP / NonDetMonadVCG

begin

```

record smack-parsed-rule = smk-subject :: smack-known
                        smk-object :: smack-known
                        smk-access1 :: int
                        smk-access2 :: int

record netlbl-audit = secid :: u32
                        loginuid :: kuid
                        sessionid :: nat

typedecl smk-audit-info
consts rules :: list-head
consts nlabel :: netlbl-lsm-secattr

consts smk-net4addr-list :: smk-net4addr list
consts smk-net6addr-list :: smk-net6addr list

definition smack-known-floor  $\equiv$  ( $\lfloor$ smk-known = "- ",
                        smk-secid = 5,
                        smk-rules = rules,
                        smk-netlabel = nlabel $\rfloor$ )

definition smack-known-hat  $\equiv$  ( $\lfloor$ smk-known = "^ ",
                        smk-secid = 3,
                        smk-rules = rules,
                        smk-netlabel = nlabel  $\rfloor$ )

definition smack-known-huh  $\equiv$  ( $\lfloor$ smk-known = "? ",
                        smk-secid = 2,
                        smk-rules = rules,
                        smk-netlabel = nlabel  $\rfloor$ )

definition smack-known-star  $\equiv$  ( $\lfloor$ smk-known = "* ",
                        smk-secid = 4,
                        smk-rules = rules ,
                        smk-netlabel = nlabel $\rfloor$ )

definition smack-known-web  $\equiv$  ( $\lfloor$ smk-known = "@ ",
                        smk-secid = 7 ,
                        smk-rules = rules,
                        smk-netlabel = nlabel $\rfloor$ )

axiomatization smack-unconfined :: smack-known
  where assumes-unconfined : smack-unconfined  $\neq$  smack-known-floor  $\wedge$ 
                        smack-unconfined  $\neq$  smack-known-hat  $\wedge$ 
                        smack-unconfined  $\neq$  smack-known-huh  $\wedge$ 
                        smack-unconfined  $\neq$  smack-known-star  $\wedge$ 
                        smack-unconfined  $\neq$  smack-known-web

```

```

record State' = current :: process-id
  tasks :: process-id  $\rightarrow$  Task
  k-superblock :: t-sb  $\rightarrow$  super-block
  inodes :: inum  $\rightarrow$  inode
  sdentry :: dname  $\rightarrow$  dentry
  files :: fname  $\rightarrow$  Files
  msg-msgs :: msg-mid  $\rightarrow$  msg-msg
  msg-queues :: msg-qid  $\rightarrow$  kern-ipc-perm
  keys :: keyid  $\rightarrow$  key
  sockets :: socketdesp  $\rightarrow$  socket
  opts :: opts

  t-security :: Cred  $\Rightarrow$  task-smack option
  sb-security :: super-block  $\Rightarrow$  superblock-smack option
  msg-security :: msg-msg  $\Rightarrow$  smack-known option
  ipc-security :: kern-ipc-perm  $\Rightarrow$  smack-known option
  i-security :: inode  $\Rightarrow$  inode-smack option
  f-security :: Files  $\Rightarrow$  smack-known option
  sk-security :: sock  $\Rightarrow$  socket-smack option
  key-security :: key  $\Rightarrow$  smack-known option
  subj-l :: Subj  $\Rightarrow$  Label
  obj-l :: Obj  $\Rightarrow$  Label
  Subjs :: Subj set
  Objs :: Obj set
  pol-tab :: (Subj, Obj) policy-table

```

```

definition get-current s  $\equiv$  (current s)
definition get-cur-task s = the(tasks s (get-current s))

```

```

definition current-cred :: Task  $\Rightarrow$  Cred
  where current-cred task = cred task

```

```

definition current-real-cred :: Task  $\Rightarrow$  Cred
  where current-real-cred task = real-cred task

```

```

definition task-cred task  $\equiv$  cred task

```

```

definition task-real-cred task  $\equiv$  real-cred task

```

```

record Shared = smack-enabled :: int
  smack-cipso-direct :: int
  smack-cipso-mapped :: int

```

```

smack-net-ambient :: smack-known
smack-syslog-label :: smack-known
smack-pttrace-rule :: int
smack-known-lock :: mutex
smack-onlycap-lock :: mutex

```

consts *shared* :: *Shared*

definition *string-to-label* :: *string* \Rightarrow *Label*
where *string-to-label str* \equiv *if str = "?" then Huh*
else if str = "^" then Hat
else if str = "-" then Floor
else if str = "" then Star*
else if str = "@" then Web
else Normal str

definition *smk-of-subjlabel* :: *State'* \Rightarrow *process-id* \Rightarrow *Label*
where *smk-of-subjlabel s pid* \equiv *let*
subjlabel = (t-security s) (cred(the(tasks s pid))) in
if subjlabel = None then UNDEFINED
else
string-to-label (smk-known(smk-of-task(the(t-security s (task-cred (the((tasks
s) pid))))))))

definition *smk-of-subjlabel-real* :: *State'* \Rightarrow *process-id* \Rightarrow *Label*
where *smk-of-subjlabel-real s pid* \equiv
string-to-label (smk-known(smk-of-task(the(t-security s (task-real-cred (the((tasks
s) pid))))))))

definition *smk-of-filelabel* :: *State'* \Rightarrow *Files* \Rightarrow *Label*
where *smk-of-filelabel s file* \equiv *let flabel = (f-security s file) in*
if flabel = None then UNDEFINED
else
string-to-label(smk-known (the flabel))

definition *smk-of-ipclabel* :: *State'* \Rightarrow *kern-ipc-perm* \Rightarrow *Label*
where *smk-of-ipclabel s ipc'* \equiv *let flabel = (ipc-security s ipc') in*
if flabel = None then UNDEFINED
else
string-to-label(smk-known (the flabel))

definition *smk-of-msglable* :: *State'* \Rightarrow *msg-msg* \Rightarrow *Label*
where *smk-of-msglable s msg'* \equiv *let label = (msg-security s msg') in*
if label = None then UNDEFINED
else
string-to-label(smk-known (the label))

definition *smk-of-keylabel* :: *State'* \Rightarrow *key* \Rightarrow *Label*
where *smk-of-keylabel s k* \equiv *let label = (key-security s k) in*

if label = None then UNDEFINED
else
string-to-label(smk-known (the label))

definition *smk-of-sklable :: State' \Rightarrow sock \Rightarrow Label*
where *smk-of-sklable s k \equiv let label = (sk-security s k) in*
if label = None then UNDEFINED
else
string-to-label(smk-known(smk-in (the label)))

definition *smk-of-inodelable :: State' \Rightarrow inode \Rightarrow Label*
where *smk-of-inodelable s i \equiv let label = (i-security s i) in*
if label = None then UNDEFINED
else
string-to-label(smk-known(smk-inode (the label)))

definition *smk-of-superblocklabel :: State' \Rightarrow super-block \Rightarrow Label*
where *smk-of-superblocklabel s t \equiv let slabel = (sb-security s t)*
in if slabel = None then UNDEFINED
else
string-to-label(smk-known (smk-default (the slabel)))

primrec *smk-of-objectlabel :: State' \Rightarrow Obj \Rightarrow Label*
where *smk-of-objectlabel s (File obj) = smk-of-filelabel s obj |*
smk-of-objectlabel s (Sb obj) = smk-of-superblocklabel s obj |
smk-of-objectlabel s (Process obj) = smk-of-subjlabel-real s obj |
smk-of-objectlabel s (IPC obj) = smk-of-ipclabel s obj |
smk-of-objectlabel s (Msg obj) = smk-of-msglabel s obj |
smk-of-objectlabel s (ObjInode obj) = smk-of-inodelable s obj |
smk-of-objectlabel s (ObjSock obj) = smk-of-sklable s obj |
smk-of-objectlabel s (ObjKey obj) = smk-of-keylabel s obj

definition *objlabelAccess :: Label \Rightarrow access set*
where *objlabelAccess obj \equiv case obj of Floor \Rightarrow {READ,EXECUTE} |*
Star \Rightarrow {READ,EXECUTE,WRITE,APPEND,T,
LOCK } |
- \Rightarrow {}

definition *smk-access-rules' :: State' \Rightarrow Label \Rightarrow Label \Rightarrow access set*
where *smk-access-rules' s subj obj \equiv*
case subj of Star \Rightarrow {} |
Hat \Rightarrow {READ,EXECUTE} |
Floor \Rightarrow objlabelAccess obj |
Huh \Rightarrow objlabelAccess obj |
Web \Rightarrow objlabelAccess obj |
Normal x \Rightarrow if obj = Floor then objlabelAccess obj
else if obj = Star then objlabelAccess obj

$\text{else if } \text{obj} = \text{Normal } x \text{ then } \{\text{READ}, \text{EXECUTE}, \text{WRITE}, \text{APPEND}, T, \text{LOCK}\}$
 $\text{else } \{\}$

definition *Label-to-string* :: *Label* \Rightarrow *string*
where *Label-to-string* *label'* \equiv *SOME* *x*. *Normal* *x* = *label'*

fun *user-define-rule* :: *string* \Rightarrow *string* \Rightarrow *access set*
where *user-define-rule* - - = $\{\}$

definition *smk-access-rules* :: *Label* \Rightarrow *Label* \Rightarrow *access set*
where *smk-access-rules* *subj* *obj* \equiv
 $\text{if } \text{obj} = \text{UNDEFINED} \text{ then } \{\}$
 else
 $\text{if } \text{subj} = \text{Star} \text{ then } \{\}$
 else
 $\text{if } \text{obj} = \text{Web} \vee \text{subj} = \text{Web} \text{ then } \{\text{READ}, \text{EXECUTE}, \text{WRITE}, \text{APPEND}, T, \text{LOCK}\}$
 else
 $\text{if } \text{obj} = \text{Star} \text{ then } \{\text{READ}, \text{EXECUTE}, \text{WRITE}, \text{APPEND}, T, \text{LOCK}\}$
 else
 $\text{if } \text{subj} = \text{obj} \text{ then } \{\text{READ}, \text{EXECUTE}, \text{WRITE}, \text{APPEND}, T, \text{LOCK}\}$
 else
 $\text{if } \text{obj} = \text{Floor} \vee \text{subj} = \text{Hat} \text{ then } \{\text{READ}, \text{LOCK}, \text{EXECUTE}\}$
 $\text{else } \text{user-define-rule } (\text{Label-to-string } \text{subj}) (\text{Label-to-string } \text{obj})$

definition *ReferenceMonitor* :: *State'* \Rightarrow *Subj* \Rightarrow *Obj* \Rightarrow *Request* \Rightarrow *decision*
where *ReferenceMonitor* *s* *subj* *obj* *r* \equiv
 $\text{if } (\text{access-rl } r) \in (\text{smk-access-rules}) (\text{smk-of-subjlabel } s \text{ subj}) (\text{smk-of-objectlabel } s \text{ obj})$
 then allow
 else deny

definition *task-security* *s* *t* \equiv *the* (*t-security* *s* (*cred* *t*))

definition *task-real-security* *s* *t* \equiv *the* (*t-security* *s* (*real-cred* *t*))

definition *inode-security* *s* *inode* = *the*(*i-security* *s* *inode*)

definition *get-pid* *s* *task* \equiv *SOME* *pid* . (*tasks* *s*) *pid* = *Some* *task*

definition *get-inum* *s* *inode* \equiv *SOME* *inum* . (*inodes* *s*) *inum* = *Some* *inode*

definition *get-sbnum* *s* *sb* \equiv *SOME* *i* . (*k-superblock* *s*) *i* = *Some* *sb*

definition *smk-of-task-struct* :: *State'* \Rightarrow *Task* \Rightarrow *smack-known*
where *smk-of-task-struct* *s* *t* \equiv *smk-of-task* (*task-security* *s* *t*)

definition *current-task* $s = \text{the}(\text{tasks } s)(\text{current } s)$

definition *current-security* $s = \text{task-security } s(\text{current-task } s)$

definition *smk-of-current* $:: \text{State}' \Rightarrow \text{smack-known}$
where *smk-of-current* $s \equiv \text{smk-of-task}(\text{task-security } s(\text{current-task } s))$

definition *smk-inode-transmutable* $:: \text{State}' \Rightarrow \text{inode} \Rightarrow \text{int}$
where *smk-inode-transmutable* $s \text{ is } p \equiv$
 $\text{let } sip = (\text{the}(\text{i-security } s \text{ is } p)) \text{ in}$
 $\text{if } (\text{smk-flags } sip \text{ AND } \text{SMK-INODE-TRANSMUTE}) \neq 0 \text{ then } 1$
 $\text{else } 0$

definition *smk-of-inode* $:: \text{State}' \Rightarrow \text{inode} \Rightarrow \text{smack-known}$
where *smk-of-inode* $s \text{ inode} \equiv \text{smk-inode}(\text{inode-security } s \text{ inode})$

definition *smk-bu-note* $:: \text{State}' \Rightarrow \text{string} \Rightarrow \text{smack-known} \Rightarrow \text{smack-known} \Rightarrow \text{int}$
 $\Rightarrow \text{int} \Rightarrow \text{int}$
where *smk-bu-note* $s \text{ note } sskp \text{ oskp } m \text{ rc} \equiv$
 $\text{if } (\text{SECURITY-SMACK-BRINGUP } \text{conf}) \text{ then } 0$
 $\text{else if } rc \leq 0 \text{ then } rc \text{ else } 0$

definition *smk-bu-current* $:: \text{State}' \Rightarrow \text{string} \Rightarrow \text{smack-known} \Rightarrow \text{int} \Rightarrow \text{int} \Rightarrow \text{int}$
where *smk-bu-current* $s \text{ note } oskp \text{ m } rc \equiv$
 $\text{if } (\text{SECURITY-SMACK-BRINGUP } \text{conf}) \text{ then } 0$
 $\text{else if } rc \leq 0 \text{ then } rc \text{ else } 0$

definition *smk-bu-task* $:: \text{State}' \Rightarrow \text{Task} \Rightarrow \text{int} \Rightarrow \text{int} \Rightarrow \text{int}$
where *smk-bu-task* $s \text{ otp } m \text{ rc} \equiv$
 $\text{if } (\text{SECURITY-SMACK-BRINGUP } \text{conf}) \text{ then}$
 $\text{if } rc \leq 0 \text{ then } rc$
 else
 $\text{if } rc > \text{SMACK-UNCONFINED-OBJECT} \text{ then } 0$
 $\text{else } rc$
 $\text{else } rc$

definition *smk-bu-inode* $:: \text{State}' \Rightarrow \text{inode} \Rightarrow \text{int} \Rightarrow \text{int} \Rightarrow \text{int}$
where *smk-bu-inode* $s \text{ inode } m \text{ rc} \equiv \text{if } (\text{SECURITY-SMACK-BRINGUP } \text{conf})$
 $\text{then } 0 \text{ else } rc$

definition *smk-bu-file* $:: \text{State}' \Rightarrow \text{Files} \Rightarrow \text{int} \Rightarrow \text{int} \Rightarrow \text{int}$
where *smk-bu-file* $s \text{ f } m \text{ rc} \equiv \text{if } (\text{SECURITY-SMACK-BRINGUP } \text{conf}) \text{ then } 0$
 $\text{else } rc$

definition *smk-bu-credfile* $:: \text{State}' \Rightarrow \text{Cred} \Rightarrow \text{Files} \Rightarrow \text{int} \Rightarrow \text{int} \Rightarrow \text{int}$
where *smk-bu-credfile* $s \text{ cred' } f \text{ m } rc \equiv \text{if } (\text{SECURITY-SMACK-BRINGUP } \text{conf}) \text{ then } 0 \text{ else } rc$

definition *smack-privileged-cred* :: *int* \Rightarrow *Cred* \Rightarrow *bool*
where *smack-privileged-cred cap c* \equiv *False*

term *the*((*tasks s*) (*current s*))

definition *smack-privileged* :: *State'* \Rightarrow *int* \Rightarrow *bool*

where *smack-privileged s cap* \equiv
if flags (the((tasks s) (current s))) = PF-KTHREAD then True
else smack-privileged-cred cap (current-cred (the((tasks s) (current s))))

definition *d-backing-inode* :: *State'* \Rightarrow *dentry* \Rightarrow *inode option*
where *d-backing-inode s upper* \equiv ((*inodes s*)(*d-inode upper*))

definition *get-inode s inum* = *inodes s inum*

definition *get-dentry s dname* \equiv *sdentry s dname*

definition *file-inode* :: *Files* \Rightarrow *inode*
where *file-inode f* \equiv *f-inode f*

type-synonym *word32* = 32 *word*

type-synonym *word8* = 8 *word*

type-synonym *byte* = *word8*

lemma (*PTRACE-MODE-READ AND PTRACE-MODE-ATTACH*) = (0x00 ::
byte)
apply(*simp add:PTRACE-MODE-READ-def PTRACE-MODE-ATTACH-def*)
done

term (*PTRACE-MODE-READ AND PTRACE-MODE-ATTACH*::'a::len *word*

term *sint* (*PTRACE-MODE-READ AND PTRACE-MODE-ATTACH*)

lemma *sint* (*PTRACE-MODE-READ AND PTRACE-MODE-ATTACH*) = 0
by(*simp add:PTRACE-MODE-READ-def PTRACE-MODE-ATTACH-def*)

consts *smack-rules* :: *smack-rule list*

definition *smk-access-entry* :: *State'* \Rightarrow *string* \Rightarrow *string* \Rightarrow *list-head* \Rightarrow (*State'*, *int*)
nondet-monad

where *smk-access-entry s subj obj r* = *do*
may \leftarrow *return*(-ENOENT);
may \leftarrow *return*((*if* ((*may AND MAY-WRITE*) = *MAY-WRITE*) *then* (*may*
OR MAY-LOCK)
else ((*may*)))));
return may

od

definition *smk-access-out-audit* :: *smack-known* \Rightarrow *smack-known* \Rightarrow *int* \Rightarrow *int*
where *smk-access-out-audit* subj obj rc \equiv
 if (*SECURITY-SMACK-BRINGUP* conf) \wedge rc < 0 then
 let rc = if obj = *smack-unconfined* then *SMACK-UNCONFINED-OBJECT*
 else rc;
 rc = if subj = *smack-unconfined* then *SMACK-UNCONFINED-SUBJECT*
 else rc
 in rc
 else rc

definition *smk-access* :: *State'* \Rightarrow *smack-known* \Rightarrow *smack-known* \Rightarrow *int*
 \Rightarrow *smk-audit-info* option \Rightarrow (*State'*, *int*) nondet-monad
where *smk-access* s subj obj requests a \equiv
 do

rc \leftarrow (if subj = *smack-known-star* then
 let rc = *-EACCES*
 in return(*smk-access-out-audit* subj obj rc)
 else
 if obj = *smack-known-web* \vee subj = *smack-known-web*
 then return(*smk-access-out-audit* subj obj 0)
 else
 if obj = *smack-known-star* then
 return(*smk-access-out-audit* subj obj 0)
 else
 if *smk-known* subj = *smk-known* obj then
 return(*smk-access-out-audit* subj obj 0)
 else if (requests AND *MAY-ANYREAD* = requests) \vee (requests AND
MAY-LOCK = requests)
 then return(*smk-access-out-audit* subj obj 0)
 else do
 may \leftarrow *smk-access-entry* s (*smk-known* subj) (*smk-known* obj)
 (*smk-rules* subj);
 if may \leq 0 \vee (requests AND may) \neq requests then
 return(*smk-access-out-audit* subj obj (*-EACCES*))
 else if (*SECURITY-SMACK-BRINGUP* conf) \wedge (may AND
MAY-BRINGUP \neq 0) then
 return(*smk-access-out-audit* subj obj *SMACK-BRINGUP-ALLOW*)
)
 else
 return(*smk-access-out-audit* subj obj 0)
 od);
 return rc
 od

definition $smk\text{-}tskacc :: State' \Rightarrow task\text{-}smack \Rightarrow smack\text{-}known \Rightarrow int$
 $\Rightarrow smk\text{-}audit\text{-}info \Rightarrow (State', int) \text{ nondet-monad}$

where $smk\text{-}tskacc\ s\ tsp\ obj\ m\ a \equiv$

```

do
  sbj-known ← return (smk-of-task tsp);
  ad ← return (Some a);
  rc ← smk-access s sbj-known obj m ad;
  rc ← (if rc ≥ 0 then
    do may ← smk-access-entry s (smk-known sbj-known) (smk-known obj)
    (smk-rule tsp) ;
    rc' ← (if may < 0 ∨ (m AND may) = m then return rc
      else return(−EACCES)
    );
    return rc'
  od
  else return rc);
rc ← (if rc ≠ 0 ∧ (smack-privileged s CAP-MAC-OVERRIDE) then return
0
  else return rc
);
return rc
od

```

definition $smk\text{-}curacc :: State' \Rightarrow smack\text{-}known \Rightarrow int \Rightarrow smk\text{-}audit\text{-}info \Rightarrow (State', int) \text{ nondet-monad}$

where $smk\text{-}curacc\ s\ obj\ m\ a \equiv$

```

do
  rc ← smk-tskacc s (current-security s) obj m a;
  return rc
od

```

definition $new\text{-}task\text{-}smack :: smack\text{-}known \Rightarrow smack\text{-}known \Rightarrow nat \Rightarrow task\text{-}smack \text{ option}$

where $new\text{-}task\text{-}smack\ task\ forked\ gfp' \equiv$

```

(SOME t. ∀ rule m label .if t = None then t = None
  else t = Some (⊔ smk-task = task,
    smk-forked = forked,
    smk-rule = rule,
    smk-rules-lock = m,
    smk-relabel = label⊔ ))

```

definition $new\text{-}inode\text{-}smack :: smack\text{-}known \Rightarrow inode\text{-}smack \text{ option}$

where $new\text{-}inode\text{-}smack\ skip \equiv$

```

(SOME t. ∃ mp lock forked rcu .if t = None then t = None
  else t = Some (⊔ smk-inode = skip,

```

```

smk-itask = forked,
smk-mmap = mp,
smk-lock = lock,
smk-iflags = 0,
smk-rcu = rcu) ))

```

definition *smk-copy-rules* :: *State'* \Rightarrow *list-head* \Rightarrow *list-head* \Rightarrow *nat* \Rightarrow (*State'*, *int*)
nondet-monad

```

where smk-copy-rules s nhead ohead g  $\equiv$ 
  do
    rc  $\leftarrow$  return( 0);
    return rc
  od

```

definition *smk-copy-relabel* :: *State'* \Rightarrow *smack-known list* \Rightarrow *smack-known list*
 \Rightarrow *nat* \Rightarrow (*State'*, *int*) *nondet-monad*

```

where smk-copy-relabel s nhead ohead g  $\equiv$ 
  do
    rc  $\leftarrow$  return( 0);
    return rc
  od

```

definition *smack-from-secid* :: *u32* \Rightarrow (*State'*, *smack-known option*) *nondet-monad*

```

where smack-from-secid secid'  $\equiv$ 
  do
    a'  $\leftarrow$  return(0);
    (a', result)  $\leftarrow$  whileLoop
      ( $\lambda(a', result)$  secid'. a' < length(smack-known-list))
      ( $\lambda(a', result)$  . ((if smk-secid (smack-known-list ! a') = secid'
        then return (a' + 1, Some ( (smack-known-list ! a')))
        else return (a' + 1, Some smack-known-huh))))
      (a', Some smack-known-huh);
    return result
  od

```

consts *smack-known-hash* :: *smack-known list*

definition *smk-find-entry* :: *string* \Rightarrow (*State'*, *smack-known option*) *nondet-monad*

```

where smk-find-entry str  $\equiv$ 
  do
    a'  $\leftarrow$  return(0);
    (a', result)  $\leftarrow$  whileLoop
      ( $\lambda(a', result)$  b'. a' < length(smack-known-list))
      ( $\lambda(a', result)$  . ((if smk-known (smack-known-hash ! a') = str
        then return (a' + 1, Some ( (smack-known-list ! a')))
        else return (a' + 1, None))))
      (a', None);

```

```

return result
od

```

definition *SOCKET-I'* :: *inode* \Rightarrow *socket-alloc*
where *SOCKET-I'* *i* \equiv *SOME* *sk*. *skvfs-inode* *sk* = *i*

definition *SOCKET-I* :: *inode* \Rightarrow *socket*
where *SOCKET-I* *i* \equiv *socket* (*SOCKET-I'* *i*)

definition *smk-pttrace-mode* :: *mode* \Rightarrow *int*
where *smk-pttrace-mode* *m* \equiv
 if (*m* AND *PTRACE-MODE-ATTACH*) \neq 0
 then *MAY-READWRITE*
 else
 if (*m* AND *PTRACE-MODE-READ*) \neq 0
 then *MAY-READ*
 else 0

definition *smk-pttrace-rule-check* :: *State'* \Rightarrow *Task* \Rightarrow *smack-known* \Rightarrow *nat* \Rightarrow *string*
 \Rightarrow (*State'*, *int*) *nondet-monad*
where *smk-pttrace-rule-check* *s* *tracer* *tracee-known* *m* *func'* \equiv *do*
tracercrd \leftarrow *return*(*task-cred* *tracer*);
tsp \leftarrow *return*(*the*(*t-security* *s* *tracercrd*));
tracer-known \leftarrow *return*(*smk-of-task* *tsp*);
saip \leftarrow (if (*int* *m* AND *PTRACE-MODE-NOAUDIT*) \neq 0 then
 return (*SOME* *x*::*smk-audit-info* *option* . *True*)
 else
 return (*None*)
);
rc \leftarrow (if (((*int* *m*) AND *PTRACE-MODE-ATTACH*) \neq 0) \wedge (
 ((*smack-pttrace-rule* *shared*) = *SMACK-PTRACE-EXACT*) \vee
 ((*smack-pttrace-rule* *shared*) = *SMACK-PTRACE-DRACONIAN*))
 then
 if *smk-known* *tracer-known* = *smk-known* *tracee-known*
 then *return* 0
 else
 if (*smack-pttrace-rule* *shared*) = *SMACK-PTRACE-DRACONIAN*
 then *return* (\neg *EACCES*)
 else
 if *smack-privileged-cred* *CAP-SYS-PTRACE* *tracercrd*
 then *return* 0
 else *return* (\neg *EACCES*)
 else *do*
 rc \leftarrow *smk-nskacc* *s* *tsp* *tracee-known* (*smk-pttrace-mode* *m*)


```

(the saip);
                                return rc
                                od
                                );
                                return rc
                                od

```

definition *smack-pttrace-access-check* :: $State' \Rightarrow Task \Rightarrow nat \Rightarrow (State', int) nondet-monad$
where *smack-pttrace-access-check* $s\ ctp\ m \equiv$
do
 $skp \leftarrow return(sm\text{-}of\text{-}task\text{-}struct\ s\ ctp);$
 $r \leftarrow sm\text{-}pttrace\text{-}rule\text{-}check\ s\ (current\text{-}task\ s)\ skp\ m\ "smack\text{-}pttrace\text{-}access\text{-}check";$
 $return(r)$
od

definition *smack-pttrace-traceme* :: $State' \Rightarrow Task \Rightarrow (State', int) nondet-monad$
where *smack-pttrace-traceme* $s\ ptp \equiv$
do
 $rc \leftarrow return(SOME\ x::int.\ True);$
 $skp \leftarrow return\ (sm\text{-}of\text{-}current\ s);$
 $rc \leftarrow sm\text{-}pttrace\text{-}rule\text{-}check\ s\ ptp\ skp\ PTRACE\text{-}MODE\text{-}ATTACH\ "smack\text{-}pttrace\text{-}traceme";$
 $return\ (rc)$
od

definition *smack-syslog* :: $State' \Rightarrow int \Rightarrow (State', int) nondet-monad$
where *smack-syslog* $s\ type\ from \equiv$
do
 $skp \leftarrow return(sm\text{-}of\text{-}current\ s);$
 $slabel \leftarrow return(smack\text{-}syslog\text{-}label\ shared);$
 $rc \leftarrow (\text{ if } smack\text{-}privileged\ s\ CAP\text{-}MAC\text{-}OVERRIDE$
 then return 0
 else
 if $slabel \neq skp$
 then return (uminus EACCES)
 else return 0
);
 $return(rc)$
od

term *pol-tab* s

term $(pol\text{-}tab\ s\ c)((c,t) := a)$

term *sorted-list-of-set*

term $SOME\ ta.\ \forall p\ obj.\ p \in taskset \wedge tab = tab((p,obj) := \{\}) \wedge ta = ta(p := tab)$

term $ta(p := SOME\ tab.\ \forall p\ obj.\ p \in taskset \wedge tab = tab((p,obj) := \{\}))$

definition *cursp* :: *State'* \Rightarrow *process-id list*
where *cursp* *s* \equiv *sorted-list-of-set* $\{t \cdot \forall p \cdot \text{tasks } s = (\text{tasks } s)(t := \text{Some } p) \}$

definition *createObjChgTab* :: *State'* \Rightarrow *Subj* \Rightarrow *Obj* \Rightarrow (*Subj*, *Obj*) *policy-table*
where *createObjChgTab* *s subj object'* \equiv
 $\text{let taskset} = \{t \cdot \forall sb \cdot \text{tasks } s = (\text{tasks } s)(t := \text{Some } sb) \};$
 $\text{subjlabel} = \text{smk-of-subjlabel } s \text{ subj};$
 $\text{objlabel} = \text{smk-of-objectlabel } s \text{ object'};$
 $\text{right} = \text{smk-access-rules } \text{subjlabel } \text{objlabel};$
 $\text{tab} = \text{SOME } \text{tab} \cdot \forall p \cdot p \in \text{taskset} \wedge \text{tab} = \text{tab}((p, \text{object}') := \text{right})$
in
 $\text{SOME } \text{ta} \cdot \forall p \cdot p \in \text{taskset} \wedge \text{ta} = \text{ta}(p := \text{tab})$

definition *update-access-tab* :: *State'* \Rightarrow *process-id* \Rightarrow *Obj* \Rightarrow *State'*
where *update-access-tab* *s subj obj* \equiv
 $\text{let tab} = (\text{pol-tab } s);$
 $\text{subjlabel} = (\text{smk-of-subjlabel } s \text{ subj});$
 $\text{objectlabel} = (\text{smk-of-objectlabel } s \text{ obj});$
 $\text{right} = (\text{smk-access-rules } \text{subjlabel } \text{objectlabel});$
 $\text{access} = ((\text{pol-tab } s \text{ subj})(\text{subj}, \text{obj}) := \text{right})$
 $\text{in } s(\text{pol-tab} := (\text{pol-tab } s)(\text{subj} := \text{access}))$

definition *update* :: *State'* \Rightarrow *Obj* \Rightarrow (*State'*, *nat*) *nondet-monad*
where *update* *s obj* \equiv
do
 $a' \leftarrow \text{return}(0);$
 $(a', \text{result}) \leftarrow \text{whileLoop}$
 $(\lambda(a', \text{result}) \text{ s. } a' < \text{length}(\text{cursp } s))$
 $(\lambda(a', \text{result}) \cdot (\text{return } (a'+1, \text{update-access-tab } s (\text{cursp } s ! a') \text{ obj})))$
 $(a', \text{result});$
 $\text{return } a'$
od

29.45 Superblock Hooks

definition *smack-sb-alloc-security* :: *State'* \Rightarrow *super-block* \Rightarrow (*State'*, *int*) *nondet-monad*
where *smack-sb-alloc-security* *s sb* \equiv
do
 $\text{sbsp} \leftarrow \text{return}(\text{SOME } x :: \text{superblock-smack option. True});$
 $\text{rc} \leftarrow (\text{if } \text{sbsp} = \text{None}$
 $\text{then return } (\text{uminus } \text{ENOMEM})$
 else do
 $\text{sbsp} \leftarrow \text{return}(\text{!smk-root} = \text{smack-known-floor},$
 $\text{smk-floor} = \text{smack-known-floor},$

```

        smk-hat = smack-known-hat,
        smk-default = smack-known-floor,
        smk-flags = 0
    );
    modify( $\lambda s$  .s(|sb-security := (sb-security s)(sb := Some sb-sp)|));
    return 0
  od);
return(rc)
od

```

definition *smack-sb-free-security* :: $State' \Rightarrow super-block \Rightarrow (State', unit) nondet-monad$
where *smack-sb-free-security* s $sb \equiv do$
 $modify(\lambda s$.s(|sb-security := (sb-security s)(sb := None)|));
 $return()$
 od

definition *smack-sb-copy-data* :: $State' \Rightarrow string \Rightarrow string \Rightarrow (State', int) nondet-monad$
where *smack-sb-copy-data* s $orig$ $smackopts \equiv do$
 $otheropts \leftarrow return(SOME\ x :: string.\ True);$
 $r \leftarrow (if\ length(otheropts) = 0$
 then $return\ (uminus\ ENOMEM)$
 else $return\ 0$);
 $return(r)$
 od

definition *smack-parse-opts-str* :: $State' \Rightarrow string \Rightarrow opts \Rightarrow (State', int) nondet-monad$
where *smack-parse-opts-str* s $options$ $opt \equiv do$
 $r \leftarrow (if\ length(options) = 0$ then $return\ 0$ else $return(uminus\ ENOMEM)$);
 $return(r)$
 od

definition *smack-set-mnt-opts* :: $State' \Rightarrow super-block \Rightarrow opts \Rightarrow nat \Rightarrow nat \Rightarrow (State', int) nondet-monad$
where *smack-set-mnt-opts* s sb opt $kern-flags$ $set-kern-flags \equiv do$

```

    root  $\leftarrow return(s-root\ sb);$ 
    inode  $\leftarrow return(d-backing-inode\ s\ (the((sentry\ s)\ root)));$ 
    sp  $\leftarrow return(the(sb-security\ s\ sb));$ 
    num-opts  $\leftarrow return\ (num-mnt-opts\ opt);$ 
    rc  $\leftarrow (if\ (smk-flags\ sp\ AND\ SMK-SB-INITIALIZED) \neq 0$ 
        then  $return\ 0$ 
        else if  $\neg(smack-privileged\ s\ CAP-MAC-ADMIN) \wedge num-opts \neq 0$ 
            then  $return\ (-EPERM)$ 
            else  $return\ 0$ 
    );
    return(rc)
  od

```

definition *get-ret* $s\ m = \text{fst}(\text{the-run-state } m\ s)$

definition *get-security-mnt-opts* $:: \text{State}' \Rightarrow \text{opts}$
where *get-security-mnt-opts* $s \equiv \text{opts } s$

definition *smack-sb-kern-mount* $:: \text{State}' \Rightarrow \text{super-block} \Rightarrow \text{int} \Rightarrow \text{string} \Rightarrow (\text{State}', \text{int}) \text{ nondet-monad}$
where *smack-sb-kern-mount* $s\ sb\ f\ data \equiv \text{do}$
 options $\leftarrow (\text{return } data);$
 rc $\leftarrow (\text{if length}(data) = 0 \text{ then } (\text{smack-set-mnt-opts } s\ sb\ (\text{get-security-mnt-opts } s)\ 0\ 0)$
 else do
 rc $\leftarrow \text{smack-parse-opts-str } s\ \text{options } (\text{opts } s);$
 rc $\leftarrow (\text{if } rc = 0 \text{ then return } rc$
 else } (\text{smack-set-mnt-opts } s\ sb\ (\text{get-security-mnt-opts } s)\ 0\ 0)
);
 return rc
 od
);
 return(rc)
 od

definition *smack-sb-statfs* $:: \text{State}' \Rightarrow \text{dentry} \Rightarrow (\text{State}', \text{int}) \text{ nondet-monad}$
where *smack-sb-statfs* $s\ d \equiv \text{do}$
 sbp $\leftarrow \text{return}(\text{the } (sb\text{-security } s\ (d\text{-sb } d)));$
 ad $\leftarrow \text{return } (\text{SOME } x :: \text{smk-audit-info } .\text{True});$
 rc $\leftarrow \text{smk-curacc } s\ (\text{smk-floor } sbp)\ \text{MAY-READ } ad;$
 rc $\leftarrow \text{return}(\text{smk-bu-current } s\ \text{"statfs"}\ (\text{smk-floor } sbp)\ \text{MAY-READ } rc\);$
 return(rc)
 od

29.46 BPRM hooks

definition *ptrace-parent* $:: \text{State}' \Rightarrow \text{Task} \Rightarrow \text{Task option}$
where *ptrace-parent* $s\ tsk' \equiv \text{if unlikely } (\text{ptrace } tsk') \text{ then Some } (\text{the}((\text{tasks } s)\ (\text{parent } tsk')))) \text{ else None}$

definition *smack-bprm-set-creds* $:: \text{State}' \Rightarrow \text{linux-binprm} \Rightarrow (\text{State}', \text{int}) \text{ nondet-monad}$
where *smack-bprm-set-creds* $s\ bprm \equiv \text{do}$
 inode $\leftarrow \text{return}(\text{file-inode}(\text{lfiles } bprm));$
 bsp $\leftarrow \text{return } (\text{the}((\text{t-security } s)\ (\text{lcred } bprm)));$
 rc $\leftarrow (\text{if called-set-creds } bprm \neq 0 \text{ then return } 0 \text{ else}$
 do
 isp $\leftarrow \text{return } (\text{the}(\text{i-security } s\ \text{inode}));$
 if } (\text{the}(\text{smk-itask } isp)) = (\text{smk-task } bsp) \text{ then return } 0 \text{ else}
 do
 sbsp $\leftarrow \text{return}(\text{the}((\text{sb-security } s)\ (\text{i-sb } \text{inode})));$
 if } ((\text{smk-flags } sbsp)\ \text{AND } \text{SMK-SB-UNTRUSTED}) \neq 0 \wedge
 return 0
 od
 od
 rc
 od

```

    (the(smkn-task isp) ≠ smkn-root sbp)
  then return 0 else
    if (unsafe bprm AND LSM-UNSAFE-PTRACE) ≠ 0 then
      do
        rc ← return 0;
        tracer ← return(ptrace-parent s (get-cur-task s));
        rc ← (if tracer ≠ None then
          do
            rc ← smkn-pttrace-rule-check s (the tracer) (the(smkn-task
isp)))
            PTRACE-MODE-ATTACH "smack-bprm-set-creds";
            return rc
          od
        else return rc;
        if rc ≠ 0 then return rc
        else do
          modify(λs .s(|t-security :=
            (t-security s)((lcred bprm) :=
              Some(bsp(|smkn-task:= the(smkn-task isp))))))
          );
          return 0
        od
      od
    else if (unsafe bprm) ≠ 0 then return (-EPERM)
    else
      return 0
    od
  od
);
return(rc)
od

```

29.47 inode hooks

definition *smack-inode-alloc-security* :: $State' \Rightarrow inode \Rightarrow (State', int)$ nondet-monad

```

where smack-inode-alloc-security s inode ≡ do
  skp ← (return (smkn-of-current s));
  i-s ← return(new-inode-smack skp);
  modify(λs .s(|i-security := (i-security s)(inode := i-s )));
  rc ← (if (i-security s inode) = None
    then return (uminus ENOMEM)
    else return 0
  );
  return(rc)
od

```

definition *smack-inode-free-security* :: $State' \Rightarrow inode \Rightarrow (State', unit)$ nondet-monad

```

where smack-inode-free-security s inode ≡ do
  modify(λs .s(|i-security := (i-security s)(inode := None )));

```

```

    return ()
  od

```

definition *smack-inode-init-security* :: $State' \Rightarrow inode \Rightarrow inode \Rightarrow string \Rightarrow string \Rightarrow string \Rightarrow int \Rightarrow (State', int)$ nondet-monad

where *smack-inode-init-security* *s inode dir qstr name value len'* \equiv do

```

  skip  $\leftarrow$  (return (smk-of-current s));
  issp  $\leftarrow$  (return (the(i-security s inode)));
  isp  $\leftarrow$  return(smk-of-inode s inode);
  dsp  $\leftarrow$  return(smk-of-inode s dir);
  rc  $\leftarrow$  (if length(value)  $\neq$  0  $\wedge$  len'  $\neq$  0 then
    do
      may  $\leftarrow$  smk-access-entry s (smk-known skip) (smk-known dsp)
(smk-rules skip);
      rc  $\leftarrow$  (if ((may > 0  $\wedge$  (may AND MAY-TRANSMUTE)  $\neq$  0)  $\wedge$ 
(smk-inode-transmutable s dir)  $\neq$  0)
        then do
          f  $\leftarrow$  return (bitOR (smk-flags issp) SMK-INODE-CHANGED
);
          modify( $\lambda s. s \langle i\text{-security} := (i\text{-security } s)(inode := \text{Some}$ 
(issp( $\langle smk\text{-flags} := f \rangle$ ))));
          value  $\leftarrow$  return(smk-known dsp);
          if length(value) = 0
            then return (uminus ENOMEM)
            else return 0
          od
        else
          if length(smk-known isp) = 0
            then return (uminus ENOMEM)
            else return 0
          od
      );
    return (rc)
  od
  else return 0);
return(rc)
od

```

definition *smack-inode-link* :: $State' \Rightarrow dentry \Rightarrow inode \Rightarrow dentry \Rightarrow (State', int)$ nondet-monad

where *smack-inode-link* *s old dir new* \equiv do

```

  isp  $\leftarrow$  (return (smk-of-inode s (the(d-backing-inode s old))));
  ad  $\leftarrow$  return (SOME x :: smk-audit-info .True);
  rc  $\leftarrow$  return (smk-bu-inode s (the(d-backing-inode s old)) MAY-WRITE
((get-ret s (smk-curacc s isp MAY-WRITE ad))));
  rc  $\leftarrow$  (if rc = 0  $\wedge$  d-is-positive new
    then return (smk-bu-inode s (the(d-backing-inode s new)) MAY-WRITE

```

```

((get-ret s (smk-curacc s isp MAY-WRITE ad))))
    else return rc);
return(rc)
od

```

definition *smack-inode-unlink* :: $State' \Rightarrow inode \Rightarrow dentry \Rightarrow (State', int) nondet-monad$

```

where smack-inode-unlink s dir d  $\equiv$  do
  ip  $\leftarrow$  return(the(d-backing-inode s d));
  ad  $\leftarrow$  return (SOME x :: smk-audit-info .True);
  rc  $\leftarrow$  smk-curacc s (smk-of-inode s ip) MAY-WRITE ad;
  rc  $\leftarrow$  return(smk-bu-inode s ip MAY-WRITE rc );
  rc  $\leftarrow$  (if rc = 0
    then do
      rc  $\leftarrow$  smk-curacc s (smk-of-inode s dir) MAY-WRITE ad;
      return(smk-bu-inode s dir MAY-WRITE rc )
    od
    else return rc);
return(rc)
od

```

definition *smack-inode-rmdir* :: $State' \Rightarrow inode \Rightarrow dentry \Rightarrow (State', int) nondet-monad$

```

where smack-inode-rmdir s dir d  $\equiv$  do
  ip  $\leftarrow$  return(the(d-backing-inode s d));
  ad  $\leftarrow$  return (SOME x :: smk-audit-info .True);
  rc  $\leftarrow$  smk-curacc s (smk-of-inode s ip) MAY-WRITE ad;
  rc  $\leftarrow$  return(smk-bu-inode s ip MAY-WRITE rc );
  rc  $\leftarrow$  (if rc = 0
    then do
      rc  $\leftarrow$  smk-curacc s (smk-of-inode s dir) MAY-WRITE ad;
      return(smk-bu-inode s dir MAY-WRITE rc )
    od
    else return rc);
return(rc)
od

```

definition *smack-inode-rename* :: $State' \Rightarrow inode \Rightarrow dentry \Rightarrow inode \Rightarrow dentry \Rightarrow (State', int) nondet-monad$

```

where smack-inode-rename s old-inode old-dentry new-inode new-dentry  $\equiv$  do
  isp  $\leftarrow$  return(the(d-backing-inode s old-dentry));
  ad  $\leftarrow$  return (SOME x :: smk-audit-info .True);
  rc  $\leftarrow$  smk-curacc s (smk-of-inode s isp) MAY-READWRITE ad;
  rc  $\leftarrow$  return(smk-bu-inode s isp MAY-READWRITE rc );
  rc  $\leftarrow$  (if rc = 0  $\wedge$  d-is-positive(new-dentry)
    then do
      rc  $\leftarrow$  smk-curacc s (smk-of-inode s isp) MAY-READWRITE ad;
      return(smk-bu-inode s (the(d-backing-inode s new-dentry))
MAY-READWRITE rc )
    od
    else return rc);

```

```

    return(rc)
  od

```

definition *smack-inode-permission* :: $State' \Rightarrow inode \Rightarrow int \Rightarrow (State', int)$ nondet-monad

```

where smack-inode-permission s i fmask  $\equiv$  do
  sbsp  $\leftarrow$  (return (the(sb-security s (i-sb i))));
  no-block  $\leftarrow$  return(fmask AND MAY-NOT-BLOCK);
  f  $\leftarrow$  return (fmask AND 15);
  rc  $\leftarrow$  (if f = 0 then
    return 0
  else if ((smk-flags sbsp) AND SMK-SB-UNTRUSTED)  $\neq$  0  $\wedge$ 
    (smk-of-inode s i)  $\neq$  (smk-root sbsp) then return (uminus(EACCES))
    else if no-block  $\neq$  0 then return (−ECHILD) else
    do
      ad  $\leftarrow$  return (SOME x :: smk-audit-info .True);
      mask  $\leftarrow$  return (nat f);
      rc  $\leftarrow$  smk-curacc s (smk-of-inode s i) mask ad;
      rc  $\leftarrow$  return(smk-bu-inode s i mask rc ); return rc
    od
  );
  return(rc)
od

```

definition *smack-inode-setattr* :: $State' \Rightarrow dentry \Rightarrow iattr \Rightarrow (State', int)$ nondet-monad

```

where smack-inode-setattr s d attrs  $\equiv$  do
  ad  $\leftarrow$  return (SOME x :: smk-audit-info .True);
  rc  $\leftarrow$  (if ((ia-valid attrs) AND ATTR-FORCE)  $\neq$  0 then
    return 0
  else do
    rc  $\leftarrow$  smk-curacc s (smk-of-inode s (the(d-backing-inode s d)))
    MAY-WRITE ad;
    return(smk-bu-inode s (the(d-backing-inode s d)) MAY-WRITE
    rc )
  od);
  return(rc)
od

```

definition *smack-inode-getattr* :: $State' \Rightarrow path \Rightarrow (State', int)$ nondet-monad

```

where smack-inode-getattr s p  $\equiv$  do
  ad  $\leftarrow$  return (SOME x :: smk-audit-info .True);
  inode  $\leftarrow$  return (the(d-backing-inode s (p-dentry p)));
  rc  $\leftarrow$  smk-curacc s (smk-of-inode s inode) MAY-READ ad;
  rc  $\leftarrow$  return(smk-bu-inode s inode MAY-READ rc );
  return(rc)
od

```

definition *xattr-ret* :: $State' \Rightarrow dentry \Rightarrow xattr \Rightarrow string \Rightarrow int \Rightarrow int \Rightarrow (State',$


```

int) nondet-monad
  where xattr-ret s dentry name value size' flags'  $\equiv$  do
    ns  $\leftarrow$  return (s-user-ns (d-sb dentry));
    rc  $\leftarrow$  (if name = XATTR-NAME-SMACKTRANSMUTE  $\wedge$  value  $\neq$  "true"
      then return (-EINVAL)
      else
        cap-inode-setxattr s dentry name value size' flags'
    );
    return(rc)
  od

```

definition *set-check-priv* :: *xattr* \Rightarrow *int*

where *set-check-priv* name \equiv case name of XATTR-NAME-SMACK \Rightarrow 1 |
 XATTR-NAME-SMACKIPIN \Rightarrow 1 |
 XATTR-NAME-SMACKIPOUT \Rightarrow 1 |
 XATTR-NAME-SMACKEXEC \Rightarrow 1 |
 XATTR-NAME-SMACKMMAP \Rightarrow 1 |
 XATTR-NAME-SMACKTRANSMUTE \Rightarrow 1 |
 - \Rightarrow 0

definition *set-check-import* :: *xattr* \Rightarrow *int*

where *set-check-import* name \equiv case name of XATTR-NAME-SMACK \Rightarrow 1 |
 XATTR-NAME-SMACKIPIN \Rightarrow 1 |
 XATTR-NAME-SMACKIPOUT \Rightarrow 1 |
 XATTR-NAME-SMACKEXEC \Rightarrow 1 |
 XATTR-NAME-SMACKMMAP \Rightarrow 1 |
 - \Rightarrow 0

definition *set-check-star* :: *xattr* \Rightarrow *int*

where *set-check-star* name \equiv case name of XATTR-NAME-SMACKEXEC \Rightarrow
 1 |
 XATTR-NAME-SMACKMMAP \Rightarrow 1 |
 - \Rightarrow 0

definition *smk-import-entry* :: *State'* \Rightarrow *string* \Rightarrow *int* \Rightarrow (*State'*, *smack-known option*) *nondet-monad*

where *smk-import-entry* s str len' \equiv do
 rc \leftarrow return (Some(SOME x :: smack-known .True));

 return(rc)
od

definition *smack-inode-setxattr* :: *State'* \Rightarrow *dentry* \Rightarrow *xattr* \Rightarrow *string* \Rightarrow *int* \Rightarrow *int*
 \Rightarrow (*State'*, *int*) *nondet-monad*

where *smack-inode-setxattr* s dentry name value size' flags' \equiv do
 ad \leftarrow return (SOME x :: smk-audit-info .True);

```

    skip ← return (SOME x :: smack-known option. True);
    check-priv ← return (set-check-priv name);
    check-import ← return (set-check-import name);
    check-star ← return (set-check-star name);
    rc ← xattr-ret s dentry name value size' flags';
    rc ← (if (rc = 0) ∧ check-import ≠ 0 then
        do
            skip ← (
                if size' > 0 then smk-import-entry s value size'
                else return None
            );
            if (skip = None) ∨
                (check-star ≠ 0 ∧ ((the(skip) = smack-known-star) ∨ (the(skip)
= smack-known-web))))
                then return (−EINVAL)
            else return 0
        od
    else
        return rc
    );
    inode ← return (the(d-backing-inode s dentry));
    rc ← smk-curacc s (smk-of-inode s inode) MAY-WRITE ad;
    rc ← return (smk-bu-inode s inode MAY-WRITE rc );
    return(rc)
od

```

definition *smack-inode-post-setxattr* :: *State'* ⇒ *dentry* ⇒ *xattr* ⇒ *string* ⇒ *int* ⇒ *int* ⇒ (*State'*, *unit*) *nondet-monad*

```

where smack-inode-post-setxattr s dentry name value size' flags' ≡ do
    skip ← return (SOME x :: smack-known .True);
    inode ← return (the(d-backing-inode s dentry));
    isp ← return (the(i-security s inode));
    if name = XATTR-NAME-SMACKTRANSMUTE then
        do
            modify(λs .s[i-security := (i-security s)
                (inode := Some(isp[i smk-iflags :=
                (bitOR (smk-iflags isp) SMK-INODE-TRANSMUTE))] )]);
            return()
        od
    else
        case name of XATTR-NAME-SMACK ⇒
            do
                skip ← smk-import-entry s value size';
                if skip ≠ None then
                    do modify(λs .s[i-security := (i-security s)(inode := Some(isp[
smk-inode := the skip))] )]);
                    return()
                od
            else return ()

```

```

    od |
      XATTR-NAME-SMACKEXEC  $\Rightarrow$ 
    do
       $skp \leftarrow smk\text{-import-entry } s \text{ value size'}$ ;
      if  $skp \neq None$  then
        do modify( $\lambda s . s[i\text{-security} := (i\text{-security } s)(inode := Some(isp($ 
smk-itask :=  $skp)) )$ ));
        return()
      od else return ()
    od |
      XATTR-NAME-SMACKMMAP  $\Rightarrow$ 
    do
       $skp \leftarrow smk\text{-import-entry } s \text{ value size'}$ ;
      if  $skp \neq None$  then
        do modify( $\lambda s . s[i\text{-security} := (i\text{-security } s)(inode := Some(isp($ 
smk-mmap :=  $skp)) )$ ));
        return()
      od else return ()
    od
  od

```

definition *smack-inode-getxattr* :: $State' \Rightarrow dentry \Rightarrow xattr \Rightarrow (State', int) \text{ nondet-monad}$
where *smack-inode-getxattr* $s \text{ dentry name} \equiv$ do
 $ad \leftarrow \text{return } (SOME \ x :: smk\text{-audit-info} . True)$;
 $inode \leftarrow \text{return } (the(d\text{-backing-inode } s \text{ dentry}))$;
 $rc \leftarrow smk\text{-curacc } s \ (smk\text{-of-inode } s \ inode) \ MAY\text{-READ } ad$;
 $rc \leftarrow \text{return}(smk\text{-bu-inode } s \ inode \ MAY\text{-READ } rc)$;
 $\text{return}(rc)$
 od

definition *xattr-remove* :: $xattr \Rightarrow bool$
where *xattr-remove* $name \equiv$ case $name$ of $XATTR\text{-NAME-SMACK} \Rightarrow True \mid$
 $XATTR\text{-NAME-SMACKIPIN} \Rightarrow True \mid$
 $XATTR\text{-NAME-SMACKIPOUT} \Rightarrow True \mid$
 $XATTR\text{-NAME-SMACKEXEC} \Rightarrow True \mid$
 $XATTR\text{-NAME-SMACKMMAP} \Rightarrow True \mid$
 $XATTR\text{-NAME-SMACKTRANSMUTE} \Rightarrow$
 $True \mid$
 $- \Rightarrow False$

record *sysConfig* = $CONFIG\text{-USER-NS} :: bool$

definition *privileged-wrt-inode-uidgid* :: $ns \Rightarrow inode \Rightarrow bool$
where *privileged-wrt-inode-uidgid* $ns \ i \equiv True$

definition *capable-wrt-inode-uidgid* :: $State' \Rightarrow inode \Rightarrow int \Rightarrow bool$
where *capable-wrt-inode-uidgid* $s \ i \ cap \equiv$ let $ns = user\text{-ns } (current\text{-cred } (get\text{-cur-task } s))$ in
 $(ns\text{-capable } ns \ cap) \wedge privileged\text{-wrt-inode-uidgid } ns \ i$

definition *cap-inode-removexattr* :: *State'* \Rightarrow *dentry* \Rightarrow *xattr* \Rightarrow (*State'*, *int*) *nondet-monad*

where *cap-inode-removexattr* *s dentry name* \equiv *do*

ns \leftarrow *return* (*s-user-ns* (*d-sb dentry*));

rc \leftarrow (*if name* \neq *XATTR-SECURITY-PREFIX* *then return 0 else*

if name = *XATTR-NAME-CAPS* *then*

do

inode \leftarrow *return* (*d-backing-inode s dentry*);

if inode = *None* *then return* ($-EINVAL$) *else*

if \neg (*capable-wrt-inode-widgid s* (*the inode*) *CAP-SETFCAP*) *then*

return ($-EPERM$)

else

return 0

od

else

if \neg (*ns-capable ns CAP-SYS-ADMIN*) *then return* ($-EPERM$)

else

return 0

);

return(rc)

od

definition *smack-inode-removexattr* :: *State'* \Rightarrow *dentry* \Rightarrow *xattr* \Rightarrow (*State'*, *int*) *nondet-monad*

where *smack-inode-removexattr* *s dentry name* \equiv *do*

ad \leftarrow *return* (*SOME x* :: *smk-audit-info* .*True*);

rc \leftarrow (*if xattr-remove name* *then if* \neg (*smack-privileged s CAP-MAC-ADMIN*)

then return ($-EPERM$)

else return 0

else cap-inode-removexattr s dentry name);

rc \leftarrow (*if rc* $\neq 0$ *then return rc else*

do

inode \leftarrow *return* (*the(d-backing-inode s dentry)*);

rc \leftarrow *smk-curacc s* (*smk-of-inode s inode*) *MAY-READ ad*;

rc \leftarrow *return*(*smk-bu-inode s inode MAY-READ rc*);

if rc $\neq 0$ *then return rc*

else

do

inode \leftarrow *return*(*the(d-backing-inode s dentry)*);

isp \leftarrow *return* (*the(i-security s inode)*);

if name = *XATTR-NAME-SMACK* *then*

do

sbp \leftarrow *return*(*d-sb dentry*);

sbsp \leftarrow *return*(*the(sb-security s sbp)*);

modify($\lambda s . s \setminus i\text{-security} := (i\text{-security } s)(inode := \text{Some}(isp \setminus$

smk-inode := *smk-default sbsp*))

return 0

od

od

```

      else
      if name = XATTR-NAME-SMACKEXEC then do
        modify( $\lambda s . s \langle i\text{-security} := (i\text{-security } s) \rangle$ )(inode := Some( $\langle i\text{-security} := (i\text{-security } s) \rangle$ )));
smk-itask := None));
      return 0
    od
  else
  if name = XATTR-NAME-SMACKMMAP then do
    modify( $\lambda s . s \langle i\text{-security} := (i\text{-security } s) \rangle$ )(inode := Some( $\langle i\text{-security} := (i\text{-security } s) \rangle$ )));
smk-mmap := None));
    return 0
  od
  else if name = XATTR-NAME-SMACKTRANSMUTE then do
    iflags  $\leftarrow$  return( $\langle i\text{-security} := (i\text{-security } s) \rangle$  AND (NOT
SMK-INODE-TRANSMUTE));
    modify( $\lambda s . s \langle i\text{-security} := (i\text{-security } s) \rangle$ )(inode := Some( $\langle i\text{-security} := (i\text{-security } s) \rangle$ )));
smk-iflags := iflags));
    return 0
  od
  else return 0
od
od);
return(rc)
od

```

definition $kstrdup \text{ str} \equiv \text{if length(str) = 0 then None else Some str}$

definition $\text{smack-inode-getsecurity} :: \text{State}' \Rightarrow \text{inode} \Rightarrow \text{xattr} \Rightarrow \text{Void} \Rightarrow \text{bool} \Rightarrow (\text{State}', \text{int}) \text{ nondet-monad}$

```

where  $\text{smack-inode-getsecurity } s \text{ inode name buffer alloc} \equiv \text{do}$ 
  ad  $\leftarrow$  return (SOME  $x :: \text{smk-audit-info} . \text{True}$ );
  isp  $\leftarrow$  return (SOME  $x :: \text{smack-known} . \text{True}$ );
  ip  $\leftarrow$  return (inode);
  rc  $\leftarrow$  (if name = XATTR-SMACK-SUFFIX then
do
  isp  $\leftarrow$  return( $\text{smk-of-inode } s \text{ inode}$ );
  return (length( $\text{smk-known } isp$ ))
od
else do
  sbp  $\leftarrow$  return( $i\text{-sb } ip$ );
  if ( $s\text{-magic sbp} \neq \text{SOCKFS-MAGIC}$ ) then return( $-EOPNOTSUPP$ )
  else do
    sock  $\leftarrow$  return (SOCKET-I ip);
    ssp  $\leftarrow$  return ( $\text{the}(sk\text{-security } s \text{ (the}(sk \text{ sock} \text{ )})))$ );
    rc  $\leftarrow$  ( if name = XATTR-SMACK-IPIN then
do isp  $\leftarrow$  return( $\text{smk-in } ssp$ );
if alloc then do buffer  $\leftarrow$  return( $kstrdup (\text{smk-known } s \text{ (the}(sk \text{ sock} \text{ )})))$ )
else return 0
od
else return 0
od

```

```

isp));
                                if buffer = None then return
(ENOMEM)                                else return(int (length(smkn-known
isp)))                                od else return(int (length(smkn-known
isp)))
                                od else
                                if name = XATTR-SMACK-IPOUT then
                                do isp ← return(smkn-out ssp);
                                if alloc then do buffer ← return(kstrdup (smkn-known
isp));
                                if buffer = None then return
(−ENOMEM)                                else return(int (length(smkn-known
isp)))                                od else return(int (length(smkn-known
isp)))
                                od
                                else return ( −EOPNOTSUPP)
                                ); return rc
                                od

                                od
                                );
                                return(rc)
                                od

```

term $s \llbracket i\text{-security} := (i\text{-security } s)(inode := \text{Some}(nsp \llbracket smkn\text{-inode} := (\text{the}(skp)),$
 $smkn\text{-iflags} := (\text{bitOR } (smkn\text{-iflags } nsp)$
 $SMK\text{-INODE-INSTANT } \rrbracket) \rrbracket \rrbracket$

definition $smkn\text{-inode-setsecurity} :: \text{State}' \Rightarrow inode \Rightarrow xattr \Rightarrow \text{Void} \Rightarrow nat \Rightarrow in-$
 $t \Rightarrow (\text{State}', int) \text{ nondet-monad}$

```

where smkn-inode-setsecurity s inode name value size' flg  ≡ do
  nsp ← return (the ((i-security s) inode));
  value ← return(SOME x. String x = value);
  skp ← return (SOME x :: smkn-known .True);
  rc ← (if length(value) = 0 ∨ size' > SMK-LONGLABEL ∨ size' = 0 then

    return (−EINVAL)
  else do
    skp ← smkn-import-entry s value size';
    if skp = None then return (−ENOMEM) else
    if (name = XATTR-SMACK-SUFFIX) then
      do
        modify(λs . s ⧸ i-security := (i-security s)(inode :=
Some(nsp ⧸ smkn-inode := (the(skp)),

```

```

smk-iflags :=(bitOR (smk-iflags nsp)
SMK-INODE-INSTANT ))) ));
      return 0
    od

      else if (s-magic (i-sb inode) ≠ SOCKFS-MAGIC) then
return(-EOPNOTSUPP)
      else do
        sock ← return (SOCKET-I inode);
        ssp ← return (the(sk-security s (the(sk sock) )));
        rc ←( if name = XATTR-SMACK-IPIN then
          do isp← return(smk-in ssp);
            modify(λs .s);
            return 0
          od else
            if name = XATTR-SMACK-IPOUT then
              do isp← return(smk-out ssp);
                return 0
              od
            else return ( -EOPNOTSUPP)
          ); return rc
        od
      od
    );
  return(rc)
od

```

definition *smack-inode-listsecurity* :: $State' \Rightarrow inode \Rightarrow Void \Rightarrow int \Rightarrow (State', int)$ *nondet-monad*

where *smack-inode-listsecurity* *s inode buffer buffer-size* \equiv *do*

```

  ad ← return (SOME x :: smk-audit-info .True);
  len ← return(17);
  return(len)
od

```

definition *smack-inode-getsecid* :: $State' \Rightarrow inode \Rightarrow int \Rightarrow (State', unit)$ *nondet-monad*

where *smack-inode-getsecid* *s inode secid'* \equiv *do*

```

  skp ← return (smk-of-inode s inode);
  secid ← return(smk-secid skp);
  return()
od

```

29.48 file hooks

definition *get-file-name* *s f* \equiv *SOME n . files s n = Some f*

type-synonym *smackfile* = *Files*

definition *smack-file-alloc-security* :: *State'* \Rightarrow *smackfile* \Rightarrow (*State'*, *int*) *nondet-monad*
where *smack-file-alloc-security* *s* *file'* \equiv *do*
 f \leftarrow *return* (*smk-of-current* *s*);
 fsp \leftarrow *return* (*f-security* *s* *file'*);
 if *fsp* \neq *None* *then* *return* (\neg *EEXIST*)
 else do
 modify($\lambda s . s(|f-security := (f-security\ s)(file' := Some\ f)|)$);
 rc \leftarrow *return*(0);
 return(*rc*)
 od
 od

definition *smack-file-free-security* :: *State'* \Rightarrow *smackfile* \Rightarrow (*State'*, *unit*) *nondet-monad*
where *smack-file-free-security* *s* *file'* \equiv *do*
 fsp \leftarrow *return* (*f-security* *s* *file'*);
 if *fsp* = *None* *then* *return* ()
 else do
 modify($\lambda s . s(|f-security := (f-security\ s)(file' := None)|)$);
 return() *od*
 od

definition *smack-file-iocctl* :: *State'* \Rightarrow *smackfile* \Rightarrow *IOC-DIR* \Rightarrow *nat* \Rightarrow (*State'*, *int*) *nondet-monad*
where *smack-file-iocctl* *s* *file'* *cmd* *arg* \equiv *do*
 ad \leftarrow *return* (*SOME* *x* :: *smk-audit-info* .*True*);
 inode \leftarrow *return*(*file-inode* *file'*);

 rc \leftarrow (*if unlikely*(*IS-PRIVATE*(*inode*)) *then* *return* 0 *else*
 do
 rc \leftarrow (*case* *cmd* *of* *IOC-WRITE* \Rightarrow
 do
 rc \leftarrow *smk-curacc* *s* (*smk-of-inode* *s* *inode*) *MAY-WRITE*
 ad;
 return(*smk-bu-file* *s* *file'* *MAY-WRITE* *rc*)
 od |
 IOC-READ \Rightarrow
 do
 rc \leftarrow *smk-curacc* *s* (*smk-of-inode* *s* *inode*) *MAY-READ*
 ad;
 return(*smk-bu-file* *s* *file'* *MAY-READ* *rc*)
 od | - \Rightarrow *return* 0);
 return *rc*
 od);
 return(*rc*)
 od

definition *smack-file-lock* :: *State'* \Rightarrow *smackfile* \Rightarrow *nat* \Rightarrow (*State'*, *int*) *nondet-monad*
where *smack-file-lock* *s* *file'* *cmd* \equiv *do*
 ad \leftarrow *return* (*SOME* *x* :: *smk-audit-info* .*True*);
 inode \leftarrow *return*(*file-inode*(*file'*));
 rc \leftarrow (if unlikely(*IS-PRIVATE*(*inode*)) then *return* 0 else
 do
 rc \leftarrow *smk-curacc* *s* (*smk-of-inode* *s* *inode*) *MAY-LOCK* *ad*;
 return(*smk-bu-file* *s* *file'* *MAY-LOCK* *rc*)
 od);
 return(*rc*)
od

definition *smack-file-fcntl* :: *State'* \Rightarrow *smackfile* \Rightarrow *nat* \Rightarrow *nat* \Rightarrow (*State'*, *int*) *nondet-monad*
where *smack-file-fcntl* *s* *file'* *cmd* *arg* \equiv *do*
 ad \leftarrow *return* (*SOME* *x* :: *smk-audit-info* .*True*);
 inode \leftarrow *return*(*file-inode*(*file'*));
 rc \leftarrow (if unlikely(*IS-PRIVATE*(*inode*)) then *return* 0 else
 if *cmd* = *F-SETLK* \vee *cmd* = *F-SETLKW* then
 do
 rc \leftarrow *smk-curacc* *s* (*smk-of-inode* *s* *inode*) *MAY-LOCK* *ad*;
 return(*smk-bu-file* *s* *file'* *MAY-LOCK* *rc*)
 od
 else if *cmd* = *F-SETOWN* \vee *cmd* = *F-SETSIG* then
 do
 rc \leftarrow *smk-curacc* *s* (*smk-of-inode* *s* *inode*) *MAY-WRITE* *ad*;
 return(*smk-bu-file* *s* *file'* *MAY-WRITE* *rc*)
 od
 else
 return 0
);
 return(*rc*)
od

definition *smack-mmap-file* :: *State'* \Rightarrow *smackfile* *option* \Rightarrow *nat* \Rightarrow *nat* \Rightarrow *nat* \Rightarrow (*State'*, *int*) *nondet-monad*
where *smack-mmap-file* *s* *file'* *reqprot* *prot* *flags'* \equiv *do*
 ad \leftarrow *return* (*SOME* *x* :: *smk-audit-info* .*True*);
 rc \leftarrow (if *file'* = *None* \vee (unlikely(*IS-PRIVATE*(*file-inode*(*the*(*file'*)))))
 then *return* 0
 else *do*
 isp \leftarrow *return*(*the*(*i-security* *s* (*file-inode*(*the*(*file'*)))))
 if *smk-mmap* *isp* = *None* then *return* 0 else
 do
 sbsp \leftarrow *return*(*the*(*sb-security* *s*) (*i-sb* (*file-inode*(*the*
 (*file'*)))))
 if (*smk-flags* *sbsp* AND *SMK-SB-UNTRUSTED*) \neq 0 \wedge
 (*the*(*smk-mmap* *isp*) \neq *smk-root* *sbsp*)
 then *return* (\neg *EACCES*)

```

        else do
            mkp ← return(the(smknmap isp));
            tsp ← return(current-security s);
            skp ← return(smkn-of-current s);
            return 0
        od
    od
od
);
return(rc)
od

consts dac-mmap-min-addr :: nat
consts init-user-ns :: ns

definition cap-capable-boby :: State' ⇒ Cred ⇒ ns ⇒ int ⇒ int ⇒ (State', int)
nondet-monad
    where cap-capable-boby s c ns cap audit ≡ do
        rc ← (if ns = user-ns c then
            if (cap-raised (cap-effective c) cap) ≠ 0 then return 0 else return
            (−EPERM)
        else
            if ns-level ns ≤ ns-level (user-ns c) then return (−EPERM)
            else if uid-eq (owner ns) (euid c)
                then return 0 else return (−EPERM)
        );
        return rc
    od

definition cap-capable :: State' ⇒ Cred ⇒ ns ⇒ int ⇒ int ⇒ (State', int) nondet-monad
    where cap-capable s c targ-ns cap audit ≡ do
        ns ← return(targ-ns);
        return(0)
    od

definition cap-mmap-addr :: State' ⇒ nat ⇒ (State', int) nondet-monad
    where cap-mmap-addr s addr ≡ do
        ret ← return (0);
        ret ← (if addr < dac-mmap-min-addr then do
            ret ← cap-capable s (current-cred (get-cur-task s)) init-user-ns
            CAP-SYS-RAWIO SECURITY-CAP-AUDIT;
            return ret
        od
        else return ret);
        return(ret)
    od

```

definition *smack-file-set-fowner* :: *State'* \Rightarrow *smackfile* \Rightarrow (*State'*, *unit*) *nondet-monad*
where *smack-file-set-fowner* *s* *file'* \equiv *do*
 f \leftarrow *return* (*smk-of-current* *s*);
 modify($\lambda s . s \backslash f\text{-security} := (f\text{-security } s)(file' := \text{Some } f)$);
 return()
od

definition *container-of-smack* :: *fown-struct* \Rightarrow *smackfile*
where *container-of-smack* *fown* \equiv *SOME* *f* . *fown* = *f-owner* *f*

definition *smack-file-send-sigiotask* :: *State'* \Rightarrow *Task* \Rightarrow *fown-struct* \Rightarrow *int* \Rightarrow (*State'*, *int*) *nondet-monad*
where *smack-file-send-sigiotask* *s* *tsk'* *fown* *signum* \equiv *do*
 skp \leftarrow *return* (*SOME* *x* :: *smack-known* . *True*);
 tkp \leftarrow *return* (*smk-of-task* (*the*((*t-security* *s*) (*current-cred* *tsk'*))));
 file' \leftarrow *return* (*container-of-smack* *fown*);
 skp \leftarrow *return*(*the*(*f-security* *s* *file'*));
 rc \leftarrow *smk-access* *s* *skp* *tkp* *MAY-DELIVER* *None*;
 rc \leftarrow *return*(*smk-bu-note* *s* "sigiotask" *skp* *tkp* *MAY-DELIVER* *rc*);
 tcred \leftarrow *return*(*task-cred*(*tsk'*));
 rc \leftarrow (*if* *rc* \neq 0 \wedge (*smack-privileged-cred* *CAP-MAC-OVERRIDE* *tcred*)
 then return 0
 else return *rc*);
 return(*rc*)
od

definition *smack-file-receive* :: *State'* \Rightarrow *smackfile* \Rightarrow (*State'*, *int*) *nondet-monad*
where *smack-file-receive* *s* *file'* \equiv *do*
 ad \leftarrow *return* (*SOME* *x* :: *smk-audit-info* . *True*);
 may \leftarrow *return* 0;
 inode \leftarrow *return*(*file-inode*(*file'*));
 rc \leftarrow (*if unlikely*(*IS-PRIVATE*(*inode*)) *then return* 0 *else*
 do
 rc \leftarrow (*if* (*s-magic* (*i-sb* *inode*)) = *nat* *SOCKFS-MAGIC* *then*
 do
 sock \leftarrow *return*(*SOCKET-I* *inode*);
 ssp \leftarrow *return*(*the*(*sk-security* *s* (*the*(*sk* *sock*)))));
 tsp \leftarrow *return*(*current-security* *s*);
 rc \leftarrow *smk-access* *s* (*smk-task* *tsp*) (*smk-out* *ssp*) *MAY-WRITE*
 (*Some* *ad*) ;
 rc \leftarrow *return*(*smk-bu-file* *s* *file'* *may* *rc*);
 rc \leftarrow (*if* *rc* < 0 *then return* *rc*
 else
 do
 rc \leftarrow *smk-access* *s* (*smk-in* *ssp*) (*smk-task* *tsp*)
 MAY-WRITE (*Some* *ad*) ;
 rc \leftarrow *return*(*smk-bu-file* *s* *file'* *may* *rc*); *return* *rc*
 od
);
);

```

    return rc
  od else if (f-mode file' AND FMODE-READ) ≠ 0 then
    do
      may ← return (MAY-READ);
      rc ← smk-curacc s (smk-of-inode s inode) may ad;
      rc ← return(smk-bu-file s file' MAY-LOCK rc );
      return rc

    od else if (f-mode file' AND FMODE-WRITE) ≠ 0 then
      do
        may ← return (bitOR may MAY-READ);
        rc ← smk-curacc s (smk-of-inode s inode) may ad;
        rc ← return(smk-bu-file s file' MAY-LOCK rc );
        return rc

      od else
        do
          rc ← smk-curacc s (smk-of-inode s inode) may ad;
          rc ← return(smk-bu-file s file' MAY-LOCK rc );
          return rc
        od
    );

  return(rc)
od);
return(rc)
od

```

definition *smack-file-open* :: $State' \Rightarrow smackfile \Rightarrow (State', int) \text{ nondet-monad}$

where *smack-file-open* s file' \equiv do
 ad ← return (SOME x :: smk-audit-info .True);
 inode ← return(file-inode(file'));
 tsp ← return(the(t-security s (f-cred file')));
 rc ← (
 do
 rc ← smk-tskacc s tsp (smk-of-inode s inode) MAY-READ ad;
 return(smk-bu-credfile s (f-cred file') file' MAY-READ rc)
 od);
 return(rc)
od

29.49 task hooks

definition *smack-cred-alloc-blank* :: $State' \Rightarrow Cred \Rightarrow nat \Rightarrow (State', int) \text{ nondet-monad}$

where *smack-cred-alloc-blank* s cred' gfp' \equiv do
 tsp ← return (SOME x :: task-smack .True);
 t ← return (SOME x :: smack-known .True);
 tsp ← return(new-task-smack t t gfp');

```

rc ← ( if tsp = None then return (−ENOMEM)
      else
      do
        modify(λs .s(t-security := (t-security s)(cred' := tsp )));
        return 0
      od
    );
return(rc)
od

```

definition *smack-cred-free* :: $State' \Rightarrow Cred \Rightarrow (State', unit) \text{ nondet-monad}$
where *smack-cred-free* *s cred'* \equiv do
 tsp ← return (SOME *x* :: task-smack .True);
 modify(λs .s(t-security := (t-security s)(cred' := None)));
 return()
od

definition *smack-cred-prepare* :: $State' \Rightarrow Cred \Rightarrow Cred \Rightarrow nat \Rightarrow (State', int) \text{ nondet-monad}$
where *smack-cred-prepare* *s new old g* \equiv do
 old-tsp ← return (the ((t-security s) old));
 new-tsp ← return (SOME *x* :: task-smack .True);
 new-tsp ← return(new-task-smack (smk-task old-tsp) (smk-task old-tsp) *g*);
 rc ← (if new-tsp = None then return (−ENOMEM)
 else do
 new-tsp' ← return(the(new-task-smack (smk-task old-tsp) (smk-task old-tsp) *g*));
 modify(λs .s(t-security := (t-security s)(new := new-tsp)));
 rc ← (smk-copy-rules *s* (smk-rule new-tsp') (smk-rule old-tsp) *g*);
 rc ← (if rc ≠ 0 then return rc else
 do
 rc ← (smk-copy-relabel *s* (smk-relabel new-tsp') (smk-relabel old-tsp) *g*);
 if rc ≠ 0 then return rc
 else
 return 0
 od);
 return rc
 od
);
 return(rc)
od

definition *smack-cred-getsecid* :: $State' \Rightarrow Cred \Rightarrow u32 \Rightarrow (State', unit) \text{ nondet-monad}$
where *smack-cred-getsecid* *s c seci* \equiv do
 skip ← return (SOME *x* :: smack-known. True);

```

    skip ← return (smk-of-task (the (t-security s c)));
    seci ← return (smk-secid skip);
    return()
  od

```

definition *smack-kernel-act-as* :: $State' \Rightarrow Cred \Rightarrow u32 \Rightarrow (State', int)$ *nondet-monad*

where *smack-kernel-act-as* *s cred' seci* \equiv *do*

```

  new-tsp ← return (the(t-security s cred'));
  i ← smack-from-secid seci;
  modify(λs .s(t-security := (t-security s)(cred' := Some (new-tsp(smk-task
:= the i))) ));
  return(0)
od

```

definition *smack-kernel-create-files-as* :: $State' \Rightarrow Cred \Rightarrow inode \Rightarrow (State', int)$ *nondet-monad*

where *smack-kernel-create-files-as* *s new inode'* \equiv *do*

```

  isp ← return (the(i-security s inode'));
  tsp ← return (the(t-security s new));
  modify(λs .s(t-security := (t-security s)(new := Some (tsp(smk-forked
:= smk-inode isp,smk-task := smk-forked tsp))) ));
  return(0)
od

```

definition *smack-cred-transfer* :: $State' \Rightarrow Cred \Rightarrow Cred \Rightarrow (State', unit)$ *nondet-monad*

where *smack-cred-transfer* *s new old* \equiv *do*

```

  old-tsp ← return (the(t-security s old));
  new-tsp ← return (the(t-security s new));
  modify(λs .s(t-security := (t-security s)
    (new := Some (new-tsp(smk-forked := smk-task old-tsp,
    smk-task :=smk-task old-tsp )) ));
  return()
od

```

definition *smk-curacc-on-task* :: $State' \Rightarrow Task \Rightarrow int \Rightarrow string \Rightarrow (State', int)$ *nondet-monad*

where *smk-curacc-on-task* *s p access' caller'* \equiv *do*

```

  ad ← return (SOME x :: smk-audit-info .True);
  skip ← return (smk-of-task-struct s p);
  rc ← ( do
    rc ← smk-curacc s skip access' ad;
    return (smk-bu-task s p access' rc )
  od);
  return(rc)

```

od

definition *smack-task-setpgid* :: $State' \Rightarrow Task \Rightarrow int \Rightarrow (State', int) nondet-monad$
where *smack-task-setpgid* *s p pgid* $\equiv do$
 $rc \leftarrow smk-curacc-on-task\ s\ p\ MAY-WRITE\ "smack-task-setpgid";$
 $return(rc)od$

definition *smack-task-getpgid* :: $State' \Rightarrow Task \Rightarrow (State', int) nondet-monad$
where *smack-task-getpgid* *s p* $\equiv do$
 $rc \leftarrow smk-curacc-on-task\ s\ p\ MAY-READ\ "smack-task-getpgid";$
 $return(rc)od$

definition *smack-task-getsid* :: $State' \Rightarrow Task \Rightarrow (State', int) nondet-monad$
where *smack-task-getsid* *s p* $\equiv do$
 $rc \leftarrow smk-curacc-on-task\ s\ p\ MAY-READ\ "smack-task-getsid";$
 $return(rc)od$

definition *smack-task-getsecid* :: $State' \Rightarrow Task \Rightarrow nat \Rightarrow (State', unit) nondet-monad$
where *smack-task-getsecid* *s p secid'* $\equiv do$
 $skp \leftarrow return(smkn-of-task-struct\ s\ p);$
 $secid' \leftarrow return(smkn-secid\ skp);$
 $return()od$

definition *smack-task-setnice* :: $State' \Rightarrow Task \Rightarrow int \Rightarrow (State', int) nondet-monad$
where *smack-task-setnice* *s p nice* $\equiv do$
 $rc \leftarrow smk-curacc-on-task\ s\ p\ MAY-WRITE\ "smack-task-setnice";$
 $return(rc)od$

definition *smack-task-setioprio* :: $State' \Rightarrow Task \Rightarrow int \Rightarrow (State', int) nondet-monad$
where *smack-task-setioprio* *s p ioprio* $\equiv do$
 $rc \leftarrow smk-curacc-on-task\ s\ p\ MAY-WRITE\ "smack-task-setioprio";$
 $return(rc)od$

definition *smack-task-getioprio* :: $State' \Rightarrow Task \Rightarrow (State', int) nondet-monad$
where *smack-task-getioprio* *s p* $\equiv do$
 $rc \leftarrow smk-curacc-on-task\ s\ p\ MAY-READ\ "smack-task-getioprio";$
 $return(rc)od$

definition *smack-task-setscheduler* :: $State' \Rightarrow Task \Rightarrow (State', int) nondet-monad$
where *smack-task-setscheduler* *s p* $\equiv do$
 $rc \leftarrow smk-curacc-on-task\ s\ p\ MAY-WRITE\ "smack-task-setscheduler";$

```

    return(rc)
  od

```

definition *smack-task-getscheduler* :: *State'* \Rightarrow *Task* \Rightarrow (*State'*, *int*) *nondet-monad*
where *smack-task-getscheduler* *s p* \equiv *do*
 rc \leftarrow *smk-curacc-on-task* *s p* *MAY-READ* "smack-task-setscheduler";
 return(*rc*)
 od

definition *smack-task-movememory* :: *State'* \Rightarrow *Task* \Rightarrow (*State'*, *int*) *nondet-monad*
where *smack-task-movememory* *s p* \equiv *do*
 rc \leftarrow *smk-curacc-on-task* *s p* *MAY-WRITE* "smack-task-movememory";
 return(*rc*)
 od

definition *smack-task-kill* :: *State'* \Rightarrow *Task* \Rightarrow *siginfo* \Rightarrow *int* \Rightarrow *Cred option* \Rightarrow (*State'*, *int*) *nondet-monad*
where *smack-task-kill* *s p info sig cred'* \equiv *do*
 ad \leftarrow return (*SOME* *x* :: *smk-audit-info* .*True*);
 skp \leftarrow return (*SOME* *x* :: *smack-known* .*True*);
 tkp \leftarrow return(*smk-of-task-struct* *s p*);
 rc \leftarrow (if *sig* = 0 then return 0 else if *cred'* = *None* then
 do *rc* \leftarrow (*smk-curacc* *s tkp* *MAY-DELIVER* *ad*);
 return(*smk-bu-task* *s p* *MAY-DELIVER* *rc*) od
 else do
 ad \leftarrow return (*Some* *ad*);
 skp \leftarrow return (*smk-of-task* (*current-security* *s*));
 rc \leftarrow *smk-access* *s skp tkp* *MAY-DELIVER* *ad*;
 rc \leftarrow return (*smk-bu-note* *s* "USB signal" *skp tkp*
 MAY-DELIVER *rc*) ;
 return *rc*
 od
);
 return(*rc*)
od

definition *smack-task-to-inode* :: *State'* \Rightarrow *Task* \Rightarrow *inode* \Rightarrow (*State'*, *unit*) *nondet-monad*
where *smack-task-to-inode* *s p i* \equiv *do*
 isp \leftarrow return (*the*(*i-security* *s i*));
 skp \leftarrow return(*smk-of-task-struct* *s p*);
 f \leftarrow return(*bitOR* (*smk-iflags* *isp*) *SMK-INODE-INSTANT*);
 modify($\lambda s . s(i\text{-security} := (i\text{-security } s) (i := \text{Some } (isp \sqcap \text{smk-inode} :=$
 skp, smk-iflags := f))))
 return()
 od

where *smack-ipc-getsecid* *s ipp flag* \equiv *do*
 iskp \leftarrow *return* (*get-ipc-security s ipp*);
 secid \leftarrow *return*(*smk-secid iskp*);
 return()*od*

definition *smack-msg-msg-alloc-security* :: *State'* \Rightarrow *msg-msg* \Rightarrow (*State'*, *int*)
nondet-monad

where *smack-msg-msg-alloc-security s msg* \equiv *do*
 skp \leftarrow *return* (*smk-of-current s*);
 msgs \leftarrow *return* (*msg-security s msg*);
 if *msgs* \neq *None* *then* *return*(\neg *EEXIST*)
 else do
 modify($\lambda s . s(|msg-security := (msg-security s)(msg := Some skp)|)$);
 return(0)
 od
od

definition *smack-msg-msg-free-security* :: *State'* \Rightarrow *msg-msg* \Rightarrow (*State'*, *unit*)
nondet-monad

where *smack-msg-msg-free-security s msg* \equiv *do*
 msgs \leftarrow *return* (*msg-security s msg*);
 if *msgs* = *None* *then* *return* ()
 else do
 modify($\lambda s . s(|msg-security := (msg-security s)(msg := None)|)$);
 return()
 od
od

definition *smack-of-ipc* :: *State'* \Rightarrow *kern-ipc-perm* \Rightarrow *smack-known*
where *smack-of-ipc s isp* \equiv *get-ipc-security s isp*

definition *smack-ipc-alloc-security* :: *State'* \Rightarrow *kern-ipc-perm* \Rightarrow (*State'*, *int*)
nondet-monad

where *smack-ipc-alloc-security s isp* \equiv *do*
 skp \leftarrow *return* (*smk-of-current s*);
 modify($\lambda s . s(|ipc-security := (ipc-security s)(isp := Some skp)|)$);
 return(0)
od

definition *smack-ipc-free-security* :: *State'* \Rightarrow *kern-ipc-perm* \Rightarrow (*State'*, *unit*)
nondet-monad

where *smack-ipc-free-security s isp* \equiv *do*
 modify($\lambda s . s(|ipc-security := (ipc-security s)(isp := None)|)$);
 return()
od

definition *smk-curacc-shm* :: *State'* \Rightarrow *kern-ipc-perm* \Rightarrow *int* \Rightarrow (*State'*, *int*)
nondet-monad

where *smk-curacc-shm s isp access* \equiv *do*
 ssp \leftarrow *return(smack-of-ipc s isp);*
 ad \leftarrow *return(SOME x :: smk-audit-info .True);*
 rc \leftarrow *smk-curacc s ssp access ad ;*
 rc \leftarrow *return(smk-bu-current s "shm" ssp access*
rc);
 return rc
od

definition *smack-shm-associate* :: *State'* \Rightarrow *kern-ipc-perm* \Rightarrow *int* \Rightarrow (*State'*, *int*)
nondet-monad

where *smack-shm-associate s isp shmflg* \equiv *do*
 may \leftarrow *return(smack-flags-to-may shmflg);*
 rc \leftarrow *smk-curacc-shm s isp may;*
 return rc
od

definition *smack-shm-shmctl* :: *State'* \Rightarrow *kern-ipc-perm* \Rightarrow *IPC-CMD* \Rightarrow (*State'*, *int*) *nondet-monad*

where *smack-shm-shmctl s isp cmd* \equiv
 do
 rc \leftarrow (case *cmd* of *SHM-STAT* \Rightarrow *smk-curacc-shm s isp MAY-READ* |
 SHM-STAT-ANY \Rightarrow *smk-curacc-shm s isp MAY-READ* |

 IPC-STAT \Rightarrow *smk-curacc-shm s isp MAY-READ* |
 SHM-LOCK \Rightarrow *smk-curacc-shm s isp MAY-READWRITE* |
 SHM-UNLOCK \Rightarrow *smk-curacc-shm s isp MAY-READWRITE*
 |
 IPC-SET \Rightarrow *smk-curacc-shm s isp MAY-READWRITE* |
 IPC-RMID \Rightarrow *smk-curacc-shm s isp MAY-READWRITE* |
 IPC-INFO \Rightarrow *return 0* |
 MSG-INFO \Rightarrow *return 0* |
 - \Rightarrow *return (-EINVAL)*
);
 return rc
od

definition *smack-shm-shmat* :: *State'* \Rightarrow *kern-ipc-perm* \Rightarrow *string* \Rightarrow *int* \Rightarrow (*State'*, *int*) *nondet-monad*

where *smack-shm-shmat s ipc' shmaddr shmflg* \equiv *do*
 may \leftarrow *return(smack-flags-to-may shmflg);*
 rc \leftarrow *smk-curacc-shm s ipc' may;*
 return rc

od

definition *smk-curacc-sem* :: *State'* \Rightarrow *kern-ipc-perm* \Rightarrow *int* \Rightarrow (*State'*, *int*)
nondet-monad

where *smk-curacc-sem s isp access* \equiv do
 ssp \leftarrow return(*smack-of-ipc s isp*);
 ad \leftarrow return(*SOME x* :: *smk-audit-info* .*True*);
 rc \leftarrow *smk-curacc s ssp access ad* ;
 rc \leftarrow return(*smk-bu-current s "sem" ssp access*
rc);
 return *rc*
 od

definition *smack-sem-associate* :: *State'* \Rightarrow *kern-ipc-perm* \Rightarrow *int* \Rightarrow (*State'*, *int*)
nondet-monad

where *smack-sem-associate s isp shmflg* \equiv do
 may \leftarrow return(*smack-flags-to-may shmflg*);
 rc \leftarrow *smk-curacc-sem s isp may*;
 return *rc*
 od

definition *smack-sem-semctl* :: *State'* \Rightarrow *kern-ipc-perm* \Rightarrow *IPC-CMD* \Rightarrow (*State'*,
int) *nondet-monad*

where *smack-sem-semctl s isp cmd* \equiv
 do
 rc \leftarrow (case *cmd* of *GETPID* \Rightarrow *smk-curacc-sem s isp MAY-READ* |
 GETNCNT \Rightarrow *smk-curacc-sem s isp MAY-READ* |
 GETZCNT \Rightarrow *smk-curacc-sem s isp MAY-READ* |
 GETVAL \Rightarrow *smk-curacc-sem s isp MAY-READ* |
 GETALL \Rightarrow *smk-curacc-sem s isp MAY-READ* |
 SEM-STAT \Rightarrow *smk-curacc-sem s isp MAY-READ* |
 SEM-STAT-ANY \Rightarrow *smk-curacc-sem s isp MAY-READ* |
 IPC-STAT \Rightarrow *smk-curacc-sem s isp MAY-READ* |
 SETVAL \Rightarrow *smk-curacc-sem s isp MAY-READWRITE* |
 SETALL \Rightarrow *smk-curacc-sem s isp MAY-READWRITE* |
 IPC-SET \Rightarrow *smk-curacc-sem s isp MAY-READWRITE* |
 IPC-RMID \Rightarrow *smk-curacc-sem s isp MAY-READWRITE* |
 IPC-INFO \Rightarrow return 0 |
 MSG-INFO \Rightarrow return 0 |
 - \Rightarrow return (-*EINVAL*)
);
 return *rc*
 od

definition *smack-sem-semop* :: *State'* \Rightarrow *kern-ipc-perm* \Rightarrow *sembuf* \Rightarrow *nat* \Rightarrow *int* \Rightarrow (*State'*, *int*) *nondet-monad*

where *smack-sem-semop* *s isp sops nsops alter* \equiv *do*
 rc \leftarrow *smk-curacc-sem s isp MAY-READWRITE*;
 return rc
od

definition *smk-curacc-msq* :: *State'* \Rightarrow *kern-ipc-perm* \Rightarrow *int* \Rightarrow (*State'*, *int*) *nondet-monad*

where *smk-curacc-msq s isp access* \equiv *do*
 msp \leftarrow *return(smack-of-ipc s isp)*;
 ad \leftarrow *return(SOME x :: smk-audit-info .True)*;
 rc \leftarrow *smk-curacc s msp access ad* ;
 rc \leftarrow *return(smk-bu-current s "msq" msp access*
rc);
 return rc
od

definition *smack-msg-queue-associate* :: *State'* \Rightarrow *kern-ipc-perm* \Rightarrow *int* \Rightarrow (*State'*, *int*) *nondet-monad*

where *smack-msg-queue-associate s isp msgflg* \equiv *do*
 may \leftarrow *return(smack-flags-to-may msgflg)*;
 rc \leftarrow *smk-curacc-msq s isp may*;
 return rc
od

definition *smack-msg-queue-msgctl* :: *State'* \Rightarrow *kern-ipc-perm* \Rightarrow *IPC-CMD* \Rightarrow (*State'*, *int*) *nondet-monad*

where *smack-msg-queue-msgctl s isp cmd* \equiv *do*
 rc \leftarrow (*case cmd of* *IPC-STAT* \Rightarrow *smk-curacc-msq s isp MAY-READ* |
 MSG-STAT \Rightarrow *smk-curacc-msq s isp MAY-READ* |
 MSG-STAT-ANY \Rightarrow *smk-curacc-msq s isp MAY-READ* |
 IPC-SET \Rightarrow *smk-curacc-msq s isp MAY-READWRITE* |
 IPC-RMID \Rightarrow *smk-curacc-msq s isp MAY-READWRITE* |
 IPC-INFO \Rightarrow *return 0* |
 MSG-INFO \Rightarrow *return 0* |
 - \Rightarrow *return (-EINVAL)*
);
 return rc
od

definition *smack-msg-queue-msgsnd* :: *State'* \Rightarrow *kern-ipc-perm* \Rightarrow *msg-msg* \Rightarrow *int* \Rightarrow (*State'*, *int*) *nondet-monad*

where *smack-msg-queue-msgsnd s isp msg msgflg* \equiv *do*
 may \leftarrow *return(smack-flags-to-may msgflg)*;

```

      rc ← smk-curacc-msq s isp may;
      return rc
    od

```

definition *smack-msg-queue-msgrcv* :: *State'* ⇒ *kern-ipc-perm* ⇒ *msg-msg* ⇒ *Task* ⇒ *int* ⇒ *int* ⇒ (*State'*, *int*) *nondet-monad*
where *smack-msg-queue-msgrcv* *s isp msg p long msgflg* ≡ *do*
 rc ← *smk-curacc-msq s isp MAY-READWRITE*;
 return rc
od

29.51 key

definition *get-key-id* :: *State'* ⇒ *key* ⇒ *int*
where *get-key-id s k* ≡ *SOME id . (keys s) id = Some k*

definition *smack-key-alloc* :: *State'* ⇒ *key* ⇒ *Cred* ⇒ *nat* ⇒ (*State'*, *int*) *nondet-monad*
where *smack-key-alloc s k c flg* ≡ *do*
 skp ← *return(smk-of-task (the((t-security s) c)))*;
 modify(λs .s[key-security := (key-security s)(k := Some skp
)]);
 return 0
od

definition *smack-key-free* :: *State'* ⇒ *key* ⇒ (*State'*, *unit*) *nondet-monad*
where *smack-key-free s k* ≡ *do*
 modify(λs .s[key-security := (key-security s)(k := None)]);
 return ()
od

definition *KEY-NEED-ALL* ≡ 63

definition *key-ref-to-ptr* :: *State'* ⇒ *key-ref-t* ⇒ *key option*
where *key-ref-to-ptr s key-ref* ≡ (*keys s*) *key-ref*

definition *smack-key-permission* :: *State'* ⇒ *key-ref-t* ⇒ *Cred* ⇒ *nat* ⇒ (*State'*, *int*) *nondet-monad*
where *smack-key-permission s key-ref c perm* ≡ *do*
 tkp ← *return(Some(smk-of-task (the((t-security s) c)))*);
 ad ← *return(SOME x :: smk-audit-info .True)*;
 request ← *return 0*;
 rc ← (*if (int perm) AND (NOT KEY-NEED-ALL) ≠ 0*
 then return (−EINVAL)
 else
 do
 keyp ← *return(key-ref-to-ptr s key-ref)*;
 rc ← (*if keyp = None then return (−EINVAL)*

```

else if (key-security s)(the keyp) = None then
  return 0
else if tkp = None then
  return (-EACCES)
else
  if smack-privileged-cred CAP-MAC-OVERRIDE
c then
  return 0 else
do
  request ← (if ((int perm) AND 11) ≠ 0
    then return (bitOR request
MAY-READ )
    else if ((int perm) AND 30) ≠ 0
    then return (bitOR
request MAY-WRITE )
    else
      return 0
  );
  rc ← smk-access s (the tkp) (the
((key-security s)(the keyp))) request (Some ad);
  rc ← return(smk-bu-note s "key access"
(the tkp) (the ((key-security s)(the keyp))) request rc);
  return rc
od
);
return rc
od
);
return rc
od

```

definition *smack-key-getsecurity* :: $State' \Rightarrow key \Rightarrow string \Rightarrow (State', int) nondet-monad$
where *smack-key-getsecurity* s k buffer \equiv do
 skip ← return(key-security s k);
 rc ← (if skip = None then return 0 else
 do
 skip ← return (the skip);
 copy ← return (kstrdup (smk-known skip));
 if copy = None then return (-ENOMEM) else
 return (length(the(copy))+1)
 od
);
 return rc
od

29.52 sock

type-synonym *smacksock* = *sock*

type-synonym *smacksocket* = *socket*

definition *get-socket-id* :: *State'* \Rightarrow *smacksocket* \Rightarrow *int*

where *get-socket-id* *s sock* \equiv *SOME id . (sockets s) id = Some sock*

definition *smack-unix-stream-connect* :: *State'* \Rightarrow *smacksock* \Rightarrow *smacksock* \Rightarrow *s-macksock* \Rightarrow (*State'*, *int*) *nondet-monad*

where *smack-unix-stream-connect* *s sock other newsk* \equiv *do*
 ssp \leftarrow *return(the(sk-security s sock))*;
 osp \leftarrow *return(the(sk-security s other))*;
 nsp \leftarrow *return(the(sk-security s newsk))*;
 ad \leftarrow *return(SOME x :: smk-audit-info .True)*;
 ad \leftarrow *return(Some ad)*;
 rc \leftarrow (*if* \neg (*smack-privileged s CAP-MAC-OVERRIDE*) *then*
 do
 skp \leftarrow *return (smk-out ssp)*;
 okp \leftarrow *return (smk-in osp)*;
 rc \leftarrow *smk-access s skp okp MAY-WRITE ad*;
 rc \leftarrow *return(smk-bu-note s "UDS connect" skp okp*
 MAY-WRITE rc);
 if *rc = 0 then*
 do
 okp \leftarrow *return (smk-out osp)*;
 skp \leftarrow *return (smk-in ssp)*;
 rc \leftarrow *smk-access s okp skp MAY-WRITE ad*;
 rc \leftarrow *return(smk-bu-note s "UDS connect" okp*
 skp MAY-WRITE rc);
 return rc
 od else
 return rc
 od
 else
 return 0
);
 return rc
 od

definition *smack-unix-may-send* :: *State'* \Rightarrow *socket* \Rightarrow *socket* \Rightarrow (*State'*, *int*) *nondet-monad*

where *smack-unix-may-send* *s sock other* \equiv *do*
 ssp \leftarrow *return(the(sk-security s (the(sk sock))))*;
 osp \leftarrow *return(the(sk-security s (the(sk other))))*;
 ad \leftarrow *return(SOME x :: smk-audit-info .True)*;
 ad \leftarrow *return(Some ad)*;
 rc \leftarrow (*if* (*smack-privileged s CAP-MAC-OVERRIDE*) *then*
 do
 skp \leftarrow *return (smk-out ssp)*;
 okp \leftarrow *return (smk-in osp)*;
 rc \leftarrow *smk-access s skp okp MAY-WRITE ad*;
 rc \leftarrow *return(smk-bu-note s "UDS connect" skp okp*
 MAY-WRITE rc);
 if *rc = 0 then*
 do
 okp \leftarrow *return (smk-out osp)*;
 skp \leftarrow *return (smk-in ssp)*;
 rc \leftarrow *smk-access s okp skp MAY-WRITE ad*;
 rc \leftarrow *return(smk-bu-note s "UDS connect" okp*
 skp MAY-WRITE rc);
 return rc
 od else
 return rc
 od
 else
 return 0
);
 return rc
 od


```

      skip ← return (smk-out ssp);
      okp ← return (smk-in osp);
      rc ← smk-access s skip okp MAY-WRITE ad;
      rc ← return(smk-bu-note s "UDS send" skip okp
MAY-WRITE rc);
      return rc
    od
  );
  return rc
od

```

definition *netlbl-sock-setattr* :: *sock* \Rightarrow *Sk-Family* \Rightarrow *netlbl-lsm-secattr* \Rightarrow *int*
where *netlbl-sock-setattr* *sk'* *family* *secattr* \equiv $-ENOSYS$

definition *smack-netlabel* :: *State'* \Rightarrow *sock* \Rightarrow *int* \Rightarrow (*State'*, *int*) *nondet-monad*
where *smack-netlabel* *s* *sock* *labeled* \equiv *do*
 ssp ← *return*(*the*(*sk-security* *s* *sock*));
 skip ← *return*(*SOME* *x* :: *smack-known* .*True*);
 ad ← *return*(*SOME* *x* :: *smk-audit-info* .*True*);
 ad ← *return*(*Some* *ad*);
 rc ← (if (*smk-out* *ssp* = (*smack-net-ambient* *shared*)
 \vee *labeled* = *SMACK-UNLABELED-SOCKET*
)
 then return 0 else
 do
 skip ← *return* (*smk-out* *ssp*);
 rc ← *return*(*netlbl-sock-setattr* *sock* (*sk-family* *sock*)
 (*smk-netlabel* *skip*));
 return rc
 od
);
return rc
od

definition *smack-socket-post-create* :: *State'* \Rightarrow *smacksocket* \Rightarrow *Sk-Family*
 \Rightarrow *int* \Rightarrow *int* \Rightarrow *int* \Rightarrow (*State'*, *int*)
nondet-monad
where *smack-socket-post-create* *s* *sock* *family* *type'* *protocols* *kern* \equiv *do*
 ssp ← *return*(*sk* *sock*);
 rc ← (if *sk* *sock* = *None* *then return 0*
 else
 if *family* \neq *PF-INET* *then*
 return 0
 else
 smack-netlabel *s* (*the*(*sk* *sock*)) *SMACK-CIPSO-SOCKET*
);
 return rc
 od

definition *smack-socket-socketpair* :: *State'* \Rightarrow *smacksocket* \Rightarrow *smacksocket* \Rightarrow (*State'*, *int*) *nondet-monad*

where *smack-socket-socketpair* *s socka sockb* \equiv *do*
 asp \leftarrow *return*(*the*(*sk-security* *s* (*the*(*sk socka*))));
 bsp \leftarrow *return*(*the*(*sk-security* *s* (*the*(*sk sockb*))));
 ask \leftarrow *return*(*the*(*sk socka*));
 bsk \leftarrow *return*(*the*(*sk sockb*));
 modify($\lambda s . s(\text{sk-security} := (\text{sk-security } s)(ask :=$
Some(asp(*smk-packet* := *Some*(*smk-out* *bsp*)))));
 modify($\lambda s . s(\text{sk-security} := (\text{sk-security } s)(bsk :=$
Some(bsp(*smk-packet* := *Some*(*smk-out* *asp*)))));
 rc \leftarrow *return*(0);
 return rc
od

definition *smk-ipv6-port-label* :: *State'* \Rightarrow *smacksocket* \Rightarrow *sockaddr* \Rightarrow (*State'*, *unit*) *nondet-monad*

where *smk-ipv6-port-label* *s sock address* \equiv *return* ()

definition *smack-socket-bind* :: *State'* \Rightarrow *socket* \Rightarrow *sockaddr* \Rightarrow *int* \Rightarrow (*State'*, *int*) *nondet-monad*

where *smack-socket-bind* *s sock address addrlen* \equiv *do*
 socka \leftarrow *return*(*sk sock*);
 if *socka* \neq *None* \wedge (*sk-family* (*the*(*sk sock*))) = *PF-INET6*
then
 do
 smk-ipv6-port-label *s sock address*;
 return 0
 od
 else
 return 0
 od

definition *ipv4host-label-find* :: *nat* \Rightarrow *in-addr* \Rightarrow (*State'*, *smack-known option*) *nondet-monad*

where *ipv4host-label-find* *a'* *siap* \equiv
do (*a'*, *result*) \leftarrow *whileLoop*
 ($\lambda(a', \text{result}) \text{ siap. } a' < \text{length}(\text{smk-net4addr-list})$)
 ($\lambda(a', \text{result}) . ((\text{if } (\text{int } (s\text{-addr } (\text{net4-smk-host } (\text{smk-net4addr-list } ! a')))) =$
 ($\text{int}(s\text{-addr } \text{siap}) \text{ AND } (\text{int}(s\text{-addr } (\text{net4-smk-mask}$
 ($\text{smk-net4addr-list } ! a'))))$)
 then return (*a'* + 1, *Some* (*net4-smk-label* (*smk-net4addr-list* !
 a')))
 else return (*a'* + 1, *None*))))
 (*a'*, *None*);
return result

od

definition *smack-ipv4host-label* :: *State'* \Rightarrow *sockaddr-in* \Rightarrow (*State'*, *smack-known option*) *nondet-monad*

where *smack-ipv4host-label s sip* \equiv *do*
 siap \leftarrow *return(sin-addr sip)*;
 rc \leftarrow *ipv4host-label-find 0 siap*;
 return rc
od

definition *smack-netlabel-send* :: *State'* \Rightarrow *sock* \Rightarrow *sockaddr-in* \Rightarrow (*State'*, *int*) *nondet-monad*

where *smack-netlabel-send s sock sap* \equiv *do*
 skp \leftarrow *return (SOME x :: smack-known .True)*;
 hkp \leftarrow *return (SOME x :: smack-known .True)*;
 ssp \leftarrow *return(the(sk-security s sock))*;
 ad \leftarrow *return (SOME x :: smk-audit-info .True)*;
 hkp \leftarrow *smack-ipv4host-label s sap*;
 rc \leftarrow (if *hkp* \neq *None* then
 do
 sk-lbl \leftarrow *return SMACK-UNLABELED-SOCKET*;
 skp \leftarrow *return (smk-out ssp)*;
 rc \leftarrow *smk-access s skp (the hkp) MAY-WRITE*
 (*Some ad*);
 rc \leftarrow *return(smk-bu-note s "IPv4 host check" skp*
 (*the hkp*) *MAY-WRITE rc)*;
 if *rc* \neq 0 then *return rc*
 else *smack-netlabel s sock sk-lbl*
 od
 else *do*
 sk-lbl \leftarrow *return SMACK-CIPSO-SOCKET*;
 smack-netlabel s sock sk-lbl
 od
);
 return rc
od

definition *smk-ipv6-localhost* :: *sockaddr-in6* \Rightarrow *bool*

where *smk-ipv6-localhost sip* \equiv *True*

definition *smack-ipv6host-label* :: *State'* \Rightarrow *sockaddr-in6* \Rightarrow (*State'*, *smack-known option*) *nondet-monad*

where *smack-ipv6host-label s sip* \equiv *do*
 rc \leftarrow *return (SOME x :: smack-known option .True)*;
 rc \leftarrow (if *smk-ipv6-localhost sip* then *return (None)*
 else *return rc*);
 return rc

od

definition *smk-ipv6-check* :: *State'* \Rightarrow *smack-known* \Rightarrow *smack-known*
 \Rightarrow *sockaddr-in6* \Rightarrow *int* \Rightarrow (*State'*, *int*) *nondet-monad*
where *smk-ipv6-check* *s subj obj addr act* \equiv *do*
ad \leftarrow *return*(*SOME* *x* :: *smk-audit-info* .*True*);
rc \leftarrow *smk-access* *s subj obj MAY-WRITE* (*Some ad*);
rc \leftarrow *return*(*smk-bu-note* *s "IPv6 check" subj obj MAY-WRITE*
rc);
return rc
od

definition *smk-ipv6-port-check* :: *State'* \Rightarrow *sock* \Rightarrow *sockaddr-in6* \Rightarrow *int* \Rightarrow (*State'*,
int) *nondet-monad*
where *smk-ipv6-port-check* *s sock addr act* \equiv *do*
ad \leftarrow *return*(*SOME* *x* :: *smk-audit-info* .*True*);
ssp \leftarrow *return*(*the*(*sk-security* *s sock*));
skp \leftarrow (*if* *act* = *SMK-RECEIVING* *then smack-ipv6host-label*
s addr
else return (*Some*(*smk-out* *ssp*)));
obj \leftarrow (*if* *act* = *SMK-RECEIVING* *then return* (*Some*(*smk-in*
ssp))
else smack-ipv6host-label *s addr*);
rc \leftarrow (*if* *skp* = *None* \wedge *obj* = *None*
then smk-ipv6-check *s* (*the skp*) (*the obj*) *addr act*
else
do
skp \leftarrow (*if* *skp* = *None* *then*
return (*smack-net-ambient* *shared*)
else
return (*the skp*)
);
obj \leftarrow (*if* *obj* = *None* *then*
return (*smack-net-ambient* *shared*)
else
return (*the obj*));
rc \leftarrow (*if* (\neg (*smk-ipv6-localhost* *addr*)) *then*
smk-ipv6-check *s* (*skp*) (*obj*) *addr act*
else if *act* = *SMK-RECEIVING*
then return 0
else
smk-ipv6-check *s skp obj addr act*
);
return rc
od
);
return rc

od

definition *sockaddr-to-sockaddr-in* :: *sockaddr* \Rightarrow *sockaddr-in*
where *sockaddr-to-sockaddr-in sap* \equiv (*SOME x* :: *sockaddr-in .True*)

definition *smack-socket-connect* :: *State'* \Rightarrow *smacksocket* \Rightarrow *sockaddr* \Rightarrow *int* \Rightarrow (*State'*, *int*) *nondet-monad*

where *smack-socket-connect s sock sap addrlen* \equiv do
 rc \leftarrow *return*(0);
 sk \leftarrow *return* (*sk sock*);
 ssp \leftarrow *return*(*the*(*sk-security s*(*the*(*sk*))));
 sap \leftarrow *return*(*SOME x* :: *sockaddr-in .True*);
 sip \leftarrow *return*(*SOME x* :: *sockaddr-in6 .True*);
 rc \leftarrow (if *sk* = *None* then *return 0* else do
 sk-family \leftarrow *return*(*sk-family* (*the*(*sk*)));
 case sk-family of PF-INET \Rightarrow
 do
 ret \leftarrow *smack-netlabel-send s* (*the sk*) *sap*;
 return ret
 od | *PF-INET6* \Rightarrow
 do
 rsp \leftarrow *smack-ipv6host-label s sip*;
 ret \leftarrow *smk-ipv6-check s* (*smk-out ssp*) (*the rsp*)
 sip SMK-CONNECTING;
 return ret
 od | - \Rightarrow *return rc*
 od);
 return rc
 od

definition *getSockaddr-in* :: *Msghdr-name option* \Rightarrow *sockaddr-in option*
where *getSockaddr-in name* \equiv let *e* = *SOME e*. *Sockaddr-in e* = *the name in Some e*

definition *getSockaddr-in6 name* \equiv let *e* = *SOME e*. *Sockaddr-in6 e* = *the name in Some e*

term *getSockaddr-in* (*msg-name msg*)

definition *smack-socket-sendmsg* :: *State'* \Rightarrow *smacksocket* \Rightarrow *msghdr* \Rightarrow *int* \Rightarrow (*State'*, *int*) *nondet-monad*

where *smack-socket-sendmsg s sock msg size'* \equiv do
 rc \leftarrow *return*(0);
 sip \leftarrow *return*(*getSockaddr-in* (*msg-name msg*));
 sap \leftarrow *return* (*getSockaddr-in6* (*msg-name msg*));
 sk \leftarrow *return* (*the*(*sk sock*));
 ssp \leftarrow *return*(*the*(*sk-security s*(*sk*)));

```

    sk-family ← return(sk-family sk);
    rc ← (if sip = None then return 0 else

        case sk-family of PF-INET ⇒
            do
                ret ← smack-netlabel-send s sk (the sip);
                return ret
            od | PF-INET6 ⇒
            do
                rc ← (if SMACK-IPV6-SECMARK-LABELING
                    (the sap) SMK-CONNECTING;
                    return ret od else return rc
                od
                else return rc);
                rc ← (if SMACK-IPV6-PORT-LABELING conf
                    then
                        do
                            ret ← smk-ipv6-port-check s sk (the sap)
                        od
                        return ret
                    else
                        return rc
                );
                return rc
            od | - ⇒ return rc

    );
    return rc

od

```

definition *netlbl-skbuff-getattr* :: *sk-buff* ⇒ *Sk-Family* ⇒ *netlbl-lsm-secattr* ⇒ *int*
where *netlbl-skbuff-getattr* *skb* *family* *secattr* ≡ (−ENOSYS)

definition *smack-socket-sock-rcv-skb* :: *State'* ⇒ *sock* ⇒ *sk-buff* ⇒ (*State'*, *int*)
nondet-monad

where *smack-socket-sock-rcv-skb* *s* *sock* *skb* ≡ do
 rc ← return(0);
 ssp ← return(the(sk-security s sock));
 sk-family ← return(sk-family sock);

```

        ad ← return( SOME x :: smk-audit-info .True);
        sadd ← return( SOME x :: sockaddr-in6 .True);
        secattr ← return( SOME x :: netlbl-lsm-secattr .True);
        family ← (if sk-family = PF-INET6 ∧ protocol skb = ETH-P-IP

                    then return(PF-INET)
                    else return sk-family
                );
        rc ← (
            case family of PF-INET ⇒
                if CONFIG-SECURITY-SMACK-NETFILTER
                    if secmark skb ≠ 0 then
                        do
                            skip ← smack-from-secid (secmark skb);
                            rc ← smk-access s (the skip) (smk-in ssp)
                                MAY-WRITE (Some ad);
                            rc ← return(smk-bu-note s "IPv4 delivery"
                                (the skip) (smk-in ssp) MAY-WRITE rc);
                            return rc
                        od
                    else
                        return (netlbl-skbuff-getattr skb family secattr)
                else
                    return (netlbl-skbuff-getattr skb family secattr)

            | PF-INET6 ⇒
                do
                    skip ← (if SMACK-IPV6-SECMARK-LABELING
                                if (secmark skb) ≠ 0 then smack-from-secid
                                    else
                                        smack-ipv6host-label s sadd
                                    else return( None));
                    skip ← (if skip = None then return (smack-net-ambient
                                shared)
                            else return (the skip));
                    rc ← (if SMACK-IPV6-SECMARK-LABELING
                                do
                                    rc ← smk-access s ( skip) (smk-in ssp)
                                        MAY-WRITE (Some ad);
                                    rc ← return(smk-bu-note s "IPv6 delivery"
                                        ( skip) (smk-in ssp) MAY-WRITE rc);
                                    return rc
                                od
                            else if SMACK-IPV6-PORT-LABELING conf

```

```

SMK-RECEIVING
    then smk-ipv6-port-check s sock sadd
    else return rc
    );
    return rc
od | - => return rc

);
return rc
od

```

definition *smack-copy-to-user* :: *string* => *string* => *nat* => *int*
where *smack-copy-to-user from to n* ≡ *let to = take n from in if (length to) = 0*
then 1 else 0

definition *smack-put-user* :: *int* => *int* => *int*
where *smack-put-user x ptr* ≡ *let x = ptr in 0*

definition *smack-socket-getpeersec-stream* :: *State'* => *socket* => *string* => *int* => *nat*
=> (*State'*, *int*) *nondet-monad*

```

where smack-socket-getpeersec-stream s sock optval optlen len' ≡ do
    ssp ← return (the (sk-security s (the (sk sock))));
    rcp ← return ("" );
    slen ← return (1);
    rc ← return (0);
    sk ← return (sk sock);
    sk-family ← return (sk-family (the sk));
    rcp ← (if (smk-packet ssp) ≠ None
        then return (smk-known (the (smk-packet ssp)))
        else return rcp);
    slen ← (if (smk-packet ssp) ≠ None
        then return (length ((smk-known (the (smk-packet
ssp)))) + 1)
        else return slen);
    rc ← (if slen > len' then return (-ERANGE)
        else if (smack-copy-to-user optval rcp slen) ≠ 0
            then return (-EFAULT)
            else if (smack-put-user slen optlen ≠ 0)
                then return (-EFAULT)
            else return rc
        );
    return rc
od

```

definition *smack-from-secattr* :: *State'* => *netlbl-lsm-secattr* => *socket-smack* =>

(*State'*, *smack-known*) *nondet-monad*

where *smack-from-secattr s sap ssp* \equiv *do*
 rc \leftarrow *return*(*SOME x* :: *smack-known .True*);
 return rc
od

definition *smack-socket-getpeersec-stream-t* ::

State' \Rightarrow socket \Rightarrow Sk-Family \Rightarrow netlbl-lsm-secattr \Rightarrow sk-buff \Rightarrow (State', int)
nondet-monad

where *smack-socket-getpeersec-stream-t s sock family secattr skb* \equiv *do*
 sid \leftarrow (if *sk sock* \neq *None* then
 do
 ssp \leftarrow *return*(*the*(*sk-security s* (*the*(*sk sock*))));

 rc \leftarrow *return* (*netlbl-skbuff-getattr skb family secattr*);
 if *rc* = 0 then *do skp* \leftarrow *smack-from-secattr s secattr*
ssp;

 return (*smk-secid skp*) *od* else *return 0*
 od
 else *return* (0);
 return sid
od

definition *smack-socket-getpeersec-dgram* :: *State' \Rightarrow socket \Rightarrow sk-buff option \Rightarrow u32*
 \Rightarrow (State', int) nondet-monad

where *smack-socket-getpeersec-dgram s sock skb secid'* \equiv *do*
 ssp \leftarrow *return*(*the*(*sk-security s* (*the*(*sk sock*))));
 family \leftarrow *return*(*PF-UNSPEC*);
 skb \leftarrow *return* (*the skb*);
 family \leftarrow (if (protocol *skb*) = *ETH-P-IP* then *return PF-INET*

 else if (*CONFIG-IPV6 conf* \wedge (protocol *skb*) =
ETH-P-IPV6)

 then *return PF-INET6*
 else if (*family* = *PF-UNSPEC*) then
 return (*sk-family* (*the*(*sk sock*)))
 else *return family*
);
 secattr \leftarrow *return* (*SOME x* :: *netlbl-lsm-secattr .True*);
 sid \leftarrow (case *family* of *PF-UNIX* \Rightarrow *return*(*smk-secid* (*smk-out*
ssp)) |

 PF-INET \Rightarrow
 (if *CONFIG-SECURITY-SMACK-NETFILTER conf*

 then

 do
 sid \leftarrow *return*(*secmark skb*);
 if (*sid* \neq 0) then *return sid*
 else *smack-socket-getpeersec-stream-t s sock family*

```

secattr skb
    od
    else
    smack-socket-getpeersec-stream-t s sock family secattr
skb)|
    PF-INET6  $\Rightarrow$  if SMACK-IPV6-SECMARK-LABELING
conf then return (secmark skb)
    else return 0
);
secid  $\leftarrow$  return sid;
rc  $\leftarrow$  if sid = 0 then return(-EINVAL)
    else return (0);
return rc
od

```

definition *smack-sk-alloc-security* :: $State' \Rightarrow sock \Rightarrow int \Rightarrow gfp-t \Rightarrow (State', int)$
nondet-monad

```

where smack-sk-alloc-security s sock family flgs  $\equiv$  do
    skp  $\leftarrow$  return(smkn-of-current s);
    ssp  $\leftarrow$  return(sk-security s ( sock));
    rc  $\leftarrow$  return (0);
    f  $\leftarrow$  return ( flags (get-cur-task s) );
    rc  $\leftarrow$  (if ssp = None then return (-ENOMEM)
    else if (f = PF-KTHREAD) then
    do

        modify( $\lambda s . s(|sk-security := (sk-security s)(sock :=$ 
            Some( $(|smkn-out = smack-known-web,$ 
                smkn-in = smack-known-web,
                smkn-packet = None  $|))|)$ );

        return rc
    od
    else
    do

        modify( $\lambda s . s(|sk-security := (sk-security s)(sock :=$ 
            Some( $(|smkn-out = smack-known-web,$ 
                smkn-in = smack-known-web,
                smkn-packet = None  $|))|)$ );

        return rc
    od
);

return rc
od

```

definition *smack-sk-free-security* :: $State' \Rightarrow sock \Rightarrow (State', unit)$ *nondet-monad*

```

where smack-sk-free-security s sock  $\equiv$  do
    modify( $\lambda s . s(|sk-security := (sk-security s)(sock :=$  None $|))$ );

```

```

    return()
  od

definition smack-sock-graft :: State' ⇒ sock ⇒ socket ⇒ (State', unit) nondet-monad
  where smack-sock-graft s sock parent' ≡ do
    ssp ← return(the(sk-security s ( sock)));
    skp ← return(smkn-of-current s);
    rc ← ( if sk-family sock ≠ PF-INET ∧ sk-family sock ≠
PF-INET6
          then return()
          else do
            modify(λs .s(sk-security := (sk-security s)(sock :=
Some(ssp(smkn-in := skp,smkn-out :=
skp ))))));
            return()
          od
    );
    return rc
  od

```

definition netlbl-req-setattr :: request-sock ⇒ netlbl-lsm-secattr ⇒ int
where netlbl-req-setattr req secattr ≡ (−ENOSYS)

definition smack-inet-conn-request :: State' ⇒ sock ⇒ sk-buff ⇒ request-sock ⇒ (State', int) nondet-monad
where smack-inet-conn-request s sock skb req ≡ do
 family ← return(sk-family sock);
 ssp ← return(the(sk-security s (sock)));
 ad ← return(SOME x :: smkn-audit-info .True);
 secattr ← return(SOME x :: netlbl-lsm-secattr .True);
 family ← (if CONFIG-IPV6 conf ∧ family = PF-INET6 ∧
protocol skb = ETH-P-IP
 then return(PF-INET) else return family);
 rc ← (if ¬(CONFIG-IPV6 conf ∧ family = PF-INET6 ∧
protocol skb = ETH-P-IP)
 then return(0)
 else
 if CONFIG-SECURITY-SMACK-NETFILTER
 conf then do
 skp ← (if secmark skb ≠ 0 then
smack-from-secid (secmark skb)
 else return (None));
 rc ← smkn-access s (the skp) (smkn-in ssp)
MAY-WRITE (Some ad);
 rc ← return(smkn-bu-note s "IPv4 connect"
(the skp) (smkn-in ssp) MAY-WRITE rc);
 else
 return(rc)
)
);
 return rc

```

rc ← (if rc ≠ 0 then return rc else
do
addr ← return(SOME x:: sockaddr-in.
True);

hskp ← smack-ipv4host-label s addr ;
if hskp = None
then
return(netlbl-req-setattr req

(smkn-netlabel (the skp)))

else
return rc
od
);
return rc
od
else
return 0
);

return rc
od

```

definition *smack-inet-csk-clone* :: *State'* ⇒ *sock* ⇒ *request-sock* ⇒ (*State'*, *unit*) *nondet-monad*

where *smack-inet-csk-clone* *s sock req* ≡ *do*

```

ssp ← return(the(sk-security s ( sock)));
skp ← return(smkn-of-current s);
(if peer-secid req ≠ 0
then do skp ← smack-from-secid (peer-secid req);
modify(λs .s(sk-security := (sk-security s)(sock
:=
Some(ssp(smkn-packet := skp )))) od
else
modify(λs .s(sk-security := (sk-security s)(sock :=
Some(ssp(smkn-packet := None )))) od
);
return ()
od

```

29.53 audit hook

definition *smack-audit-rule-init* ::

State' ⇒ *u32* ⇒ *enum-audit* ⇒ *string* ⇒ *string* ⇒ (*State'*, *int*) *nondet-monad*

where *smack-audit-rule-init* *s field op rulestr vrule* ≡ *do*

```

skp ← smkn-import-entry s rulestr 0;

```

```

rc ← (if field ≠ AUDIT-SUBJ-USER ∧ field ≠ AUDIT-OBJ-USER
      then return (−EINVAL)
      else if op ≠ Audit-equal ∧ op ≠ Audit-not-equal then return
(−EINVAL)
      else if skip = None then return (−ENOMEM)
      else do rule ← return(smknknown (the(skip)));
      return 0
      od
);
return rc
od

```

definition *smack-audit-rule-known* :: $State' \Rightarrow audit-krule \Rightarrow (State', int) nondet-monad$
where *smack-audit-rule-known* *s* *krule* \equiv
do
a' ← return(0);
(*a'*, *result*) ← whileLoop
($\lambda(a', result) \text{ secid}'. a' < (field-count \text{ krule})$)
($\lambda(a', result) \cdot ((if \text{ atype } (afields \text{ krule}) ! a' = AUDIT-SUBJ-USER \vee$
 $\text{ atype } (afields \text{ krule}) ! a' = AUDIT-OBJ-USER$
then return (*a'* + 1, 1)
else return (*a'* + 1, 0))))
(*a'*, 0);
return *result*
od

definition *smack-audit-rule-match* ::
 $State' \Rightarrow u32 \Rightarrow u32 \Rightarrow enum-audit \Rightarrow string \Rightarrow audit-context \Rightarrow (State', int)$
nondet-monad
where *smack-audit-rule-match* *s* *secid'* *field* *op* *vrule* *actx* \equiv do
rule ← return(*vrule*);
rc ← (if unlikely (length(rule)) then return(−ENOENT) else
if field ≠ AUDIT-SUBJ-USER ∧ field ≠ AUDIT-OBJ-USER
then return 0
else do
skip ← smack-from-secid *secid'*;
if op = Audit-equal then if rule = smknknown (the
skip)
then return 1
else return 0
else if op = Audit-not-equal then if rule ≠ smknknown
(the skip)
then return 1 else return 0
else return 0
od
);

```

    return rc
  od

```

29.54 other

definition *smack-getprocattr* :: *State'* \Rightarrow *Task* \Rightarrow *string* \Rightarrow *string* \Rightarrow (*State'*, *int*)
nondet-monad

```

  where smack-getprocattr s p name value  $\equiv$  do
    skp  $\leftarrow$  return (smk-of-task-struct s p);
    cp  $\leftarrow$  return(kstrdup (smk-known skp));
    rc  $\leftarrow$  (if length(the cp) = 0 then return (uminus ENOMEM)
              else return (length (the cp)));
    return rc
  od

```

definition *smack-d-instantiate* :: *State'* \Rightarrow *dentry* \Rightarrow *inode option* \Rightarrow (*State'*, *unit*)
nondet-monad

```

  where smack-d-instantiate s opt-dentry inode  $\equiv$  do
    skp  $\leftarrow$  return (smk-of-current s );

    rc  $\leftarrow$  (if inode = None then return ()
              else do
                isp  $\leftarrow$  return(the(i-security s (the inode)));
                if (smk-flags isp AND SMK-INODE-INSTANT)
 $\neq$  0 then return()

                else do
                  sbp  $\leftarrow$  return(i-sb (the inode));
                  sbsp  $\leftarrow$  return(the(sb-security s sbp));
                  return()
                od
              od

    );
    return rc
  od

```

definition *smack-setprocattr-known* :: *State'* \Rightarrow *smack-known list* \Rightarrow *smack-known* \Rightarrow
(*State'*, *int*) *nondet-monad*

```

  where smack-setprocattr-known s relabellist skp  $\equiv$ 
    do
      a'  $\leftarrow$  return(0);
      (a', result)  $\leftarrow$  whileLoop
        ( $\lambda(a', result)$  secid'. a' < (length relabellist))
        ( $\lambda(a', result)$  . ((if ( relabellist ! a') = skp
                           then return (a' + 1, 0)
                           else return (a' + 1, ( $-EPERM$ ))))))
      (a', ( $-EPERM$ ));
    return result
  od

```

definition *smack-setprocattr* :: *State'* \Rightarrow *string* \Rightarrow *string* \Rightarrow *int* \Rightarrow (*State'*, *int*) *nondet-monad*

```

where smack-setprocattr s name value size'  $\equiv$  do
    tsp  $\leftarrow$  return(current-security s);
    rc  $\leftarrow$  (if  $\neg$ (smack-privileged s CAP-MAC-ADMIN)  $\wedge$ 
length(smk-relabel tsp) = 0
    then return (uminus EPERM)
    else
    if length(value) = 0  $\vee$  size' = 0  $\vee$  size'  $\geq$  SMK-LOGLABEL

    then return ( $\neg$ EINVAL)
    else if name  $\neq$  "current"
    then return ( $\neg$ EINVAL) else
    do
    skp  $\leftarrow$  smk-import-entry s value size';
    if skp = None then return ( $\neg$ ENOMEM)
    else if (the skp) = smack-known-web  $\vee$  (the skp) =
smack-known-star

    then return ( $\neg$ EINVAL)
    else if  $\neg$ (smack-privileged s CAP-MAC-ADMIN)

    then

    do
    rc  $\leftarrow$  smack-setprocattr-known s (smk-relabel
tsp) (the skp);

    return rc
    od
    else
    do
    new  $\leftarrow$  return(snd(prepare-creds s));
    if new = None then return ( $\neg$ ENOMEM)

    return size'
    od
    od
    );
    return rc
    od

```

definition *smack-ismaclabel* :: *State'* \Rightarrow *xattr* \Rightarrow (*State'*, *int*) *nondet-monad*

where *smack-ismaclabel* *s* *name* \equiv *do*

```

    rc  $\leftarrow$  (if name = XATTR-SMACK-SUFFIX then return (1)
    else return (0));
    return rc
    od

```

definition *smack-secid-to-secctx* :: *State'* \Rightarrow *u32* \Rightarrow *string* \Rightarrow *u32* \Rightarrow (*State'*, *int*)

nondet-monad

where *smack-secid-to-secctx* *s* *secid'* *secd**ata* *seclen* \equiv *do*
 skp \leftarrow *smack-from-secid* *secid'*;
 *secd**ata* \leftarrow (if *length*(*secd**ata*) \neq 0 then return (*smk-known*
 (*the skp*))
 else return *secd**ata*);
 seclen \leftarrow return (*length*(*smk-known* (*the skp*)));
 return 0
 od

definition *smack-secctx-to-secid* :: *State'* \Rightarrow *string* \Rightarrow *u32* \Rightarrow *u32* \Rightarrow (*State'*, *int*)
nondet-monad

where *smack-secctx-to-secid* *s* *secd**ata* *seclen* *secid'* \equiv *do*
 skp \leftarrow *smk-find-entry* *secd**ata*;
 secid' \leftarrow (if *skp* = *None* then return (*smk-secid* (*the skp*))
 else return (0));
 return 0
 od

definition *smack-inode-notifysecctx* :: *State'* \Rightarrow *inode* \Rightarrow *string* \Rightarrow *u32* \Rightarrow (*State'*,
int) *nondet-monad*

where *smack-inode-notifysecctx* *s* *inode* *ctx* *ctxlen* \equiv
 smack-inode-setsecurity *s* *inode* *XATTR-SMACK-SUFFIX* (*String ctx*)
 ctxlen 0

definition *vfs-setxattr* :: *State'* \Rightarrow *dentry* \Rightarrow *string* \Rightarrow *string* \Rightarrow *int* \Rightarrow *int* \Rightarrow (*State'*,
int) *nondet-monad*

where *vfs-setxattr* *s* *dentry* *name* *value* *size'* *flgs* \equiv return 0

definition *is-bad-inode* :: *inode* \Rightarrow *bool*

where *is-bad-inode* *inode* \equiv *True*

definition *vfs-setxattr-noperm'* :: *State'* \Rightarrow *dentry* \Rightarrow *string* \Rightarrow *string* \Rightarrow *int* \Rightarrow
int \Rightarrow (*State'*, *int*) *nondet-monad*

where *vfs-setxattr-noperm'* *s* *dentry* *name* *value* *size'* *flgs* \equiv *do*
 inode \leftarrow return(*get-inode* *s* (*d-inode* *dentry*));
 error \leftarrow return (\neg *EAGAIN*);
 inode \leftarrow (if *name* \neq "security." then *do*
 f \leftarrow return ((*int*(*i-flgs* (*the inode*))) AND (*NOT S-NOSEC*));
 indoe \leftarrow return((*the inode*) | *i-flgs* := (*nat f*));
 return (*inode*)
 od
 else return(*inode*));
 error \leftarrow (if (*int*(*i-opflgs* (*the inode*)) AND *IOP-XATTR*) \neq 0


```

    then
      vfs-setxattr s dentry name value size' flags

    else
      if is-bad-inode (the inode) then return(-EIO)
      else if (error = (-EAGAIN)) then
        return (-EOPNOTSUPP)
      else return error

  );
  return error
od

```

definition *smack-inode-setsecctx* :: *State'* \Rightarrow *dentry* \Rightarrow *string* \Rightarrow *u32* \Rightarrow (*State'*, *int*)
nondet-monad

where *smack-inode-setsecctx* *s dentry ctx ctxlen* \equiv
vfs-setxattr-noperm' s dentry "security.SMACK64" ctx ctxlen 0

definition *smack-inode-getsecctx* :: *State'* \Rightarrow *inode* \Rightarrow *string* \Rightarrow *u32* \Rightarrow (*State'*, *int*)
nondet-monad

where *smack-inode-getsecctx* *s inode ctx ctxlen* \equiv *do*
skp \leftarrow *return*(*smk-of-inode s inode*);
ctx \leftarrow *return*(*smk-known skp*);
ctxlen \leftarrow *return*(*length*(*smk-known skp*));
return 0
od

definition *smack-inode-copy-up* :: *State'* \Rightarrow *dentry* \Rightarrow *Cred option* \Rightarrow (*State'*, *int*)
nondet-monad

where *smack-inode-copy-up* *s dentry new* \equiv *do*
new-creds \leftarrow *return*(*new*);
rc \leftarrow (if *new-creds* = *None* then
 do
 new-creds \leftarrow *return*(*snd*(*prepare-creds s*));
 if *new-creds* = *None* then *return* (-*ENOMEM*) else
 do
 tsp \leftarrow *return*(*t-security s* (*the new-creds*));
 isp \leftarrow *return* (*i-security s* (*the*(*get-inode s* (*d-inode* (*the*(*get-dentry*
s (*d-parent dentry*))))))));
 skp \leftarrow *return*(*smk-inode* (*the isp*));
 modify($\lambda s . s \langle t\text{-security} := (t\text{-security } s) ((the\ new\ creds) :=$
Some (*the tsp* \sqcup *smk-task* := *skp* \sqcup))));
 new \leftarrow *return*(*new-creds*);
 return 0
 od
 od
)
od

```

      else
      return 0);

    return rc
  od

```

definition *smack-inode-copy-up-xattr* :: $State' \Rightarrow xattr \Rightarrow (State', int) \text{ nondet-monad}$
where *smack-inode-copy-up-xattr* *s name* \equiv if *name* = XATTR-NAME-SMACK
 then return 1
 else return ($-EOPNOTSUPP$)

definition *smack-dentry-create-files-as* :: $State' \Rightarrow dentry \Rightarrow mode \Rightarrow string \Rightarrow Cred \Rightarrow Cred \Rightarrow (State', int) \text{ nondet-monad}$
where *smack-dentry-create-files-as* *s dentry mode' name old new* \equiv do
otsp \leftarrow return(*the*(*t-security s old*));
ntsp \leftarrow return(*the*(*t-security s new*));
 modify($\lambda s . s(t\text{-security} := (t\text{-security } s)(new := \text{Some } (ntsp \sqcup \text{smk-task} := \text{smk-task } otsp \sqcup)))$);
isp \leftarrow return(*the*(*i-security s* (*the*(*get-inode s* (*d-inode* (*the*(*get-dentry s* (*d-parent dentry*))))))));
 if (*smk-flags isp AND SMK-INODE-TRANSMUTE*) \neq 0 then
 do
may \leftarrow *smk-access-entry s* (*smk-known* (*smk-task otsp*)) (*smk-known* (*smk-inode isp*)) (*smk-rules* (*smk-task otsp*));
 (if *may* > 0 \wedge ((*may AND MAY-TRANSMUTE*) \neq 0) then
 modify($\lambda s . s(t\text{-security} := (t\text{-security } s)(new := \text{Some } (ntsp \sqcup \text{smk-task} := \text{smk-task } otsp \sqcup)))$);
 else
 modify($\lambda s . s(t\text{-security} := (t\text{-security } s)(new := \text{Some } (ntsp \sqcup \text{smk-task} := \text{smk-inode } isp \sqcup)))$);
 return 0
 od
 else return 0
od

definition *smack-init* :: $State' \Rightarrow (State', int) \text{ nondet-monad}$
where *smack-init s* \equiv do
cred' \leftarrow return (*SOME x* :: *Cred . True*);
tsp \leftarrow return (*SOME x* :: *task-smack . True*);
cred' \leftarrow return (*current-cred* (*current-task s*));

 return(0)
od

end

30 Smack proof

```

theory SmackLemma
  imports
    SmackHooks
begin

```

30.1 Correctness for Smack TDS specification

lemma *smk-access-entry-not-chg-state*:

```

 $\bigwedge s'.$ 
 $\{\lambda s. s = s'\}$ 
  smk-access-entry  $s'$  subj obj  $r$ 
 $\{\lambda r s. s = s'\}$ 
apply (unfold smk-access-entry-def)
apply wpsimp
done

```

30.2 correctness lemmas of smack_ptrace_access_check

lemma *smack-ptrace-access-check-correctness*:

```

 $\{\lambda s. \text{True}\}$  smack-ptrace-access-check  $s$   $t$   $m$   $\{\lambda r s. r = 0 \vee r \neq 0\}$ 
apply (unfold smack-ptrace-access-check-def smk-ptrace-rule-check-def)
apply wpsimp
done

```

lemma *smack-ptrace-access-check-correctness1*:

```

 $\exists t m. \{\lambda s. \text{smk-known (smk-of-task (the ((t-security s) (task-cred (current-task s))))})$ 
 $= \text{smk-known (smk-of-task-struct s t)}$ 
 $\wedge (((\text{int } m) \text{ AND PTRACE-MODE-ATTACH}) \neq 0) \wedge ($ 
 $((\text{smack-ptrace-rule shared}) = \text{SMACK-PTRACE-EXACT}) \vee$ 
 $((\text{smack-ptrace-rule shared}) = \text{SMACK-PTRACE-DRACONIAN}))$ 
 $= \text{True}$ 
 $\}$ 
  smack-ptrace-access-check  $s$   $t$   $m$   $\{\lambda r s. r = 0\}$ 
apply (unfold smack-ptrace-access-check-def smk-ptrace-rule-check-def)
apply wpsimp
by (metis int-and-0 semiring-1-class.of-nat-0)

```

lemma *smack-ptrace-access-check-correctness2*:

```

 $\exists t m. \{\lambda s. \text{smk-known (smk-of-task (the ((t-security s) (task-cred (current-task s))))})$ 
 $\neq \text{smk-known (smk-of-task-struct s t)}$ 
 $\wedge (((\text{int } m) \text{ AND PTRACE-MODE-ATTACH}) \neq 0) \wedge ($ 
 $((\text{smack-ptrace-rule shared}) = \text{SMACK-PTRACE-EXACT}) \vee$ 
 $((\text{smack-ptrace-rule shared}) = \text{SMACK-PTRACE-DRACONIAN}))$ 
 $= \text{True}$ 
 $\wedge (\text{smack-ptrace-rule shared}) = \text{SMACK-PTRACE-DRACONIAN}$ 
 $\}$ 
  smack-ptrace-access-check  $s$   $t$   $m$   $\{\lambda r s. r = -\text{EACCES}\}$ 
apply (unfold smack-ptrace-access-check-def smk-ptrace-rule-check-def)

```

apply *wsimp*
by (*metis int-and-0 semiring-1-class.of-nat-0*)

lemma *smack-pttrace-access-check-correctness3*:
 $\exists t m. \{ \lambda s. \text{smk-known } (\text{smk-of-task } (\text{the } ((t\text{-security } s) (\text{task-cred } (\text{current-task } s)))))) \neq \text{smk-known } (\text{smk-of-task-struct } s t) \wedge (((\text{int } m) \text{ AND } \text{PTRACE-MODE-ATTACH}) \neq 0) \wedge ((\text{smack-pttrace-rule shared}) = \text{SMACK-PTRACE-EXACT}) \vee ((\text{smack-pttrace-rule shared}) = \text{SMACK-PTRACE-DRACONIAN})) \}$
 $= \text{True}$
 $\wedge (\text{smack-pttrace-rule shared}) \neq \text{SMACK-PTRACE-DRACONIAN}$
 $\wedge \text{smack-privileged-cred CAP-SYS-PTRACE tracercred}$
 $\}$
 $\text{smack-pttrace-access-check } s t m \{ \lambda r s. r = 0 \}$
apply (*unfold smack-pttrace-access-check-def smk-pttrace-rule-check-def*)
apply *wsimp*
by (*metis int-and-0 semiring-1-class.of-nat-0*)

lemma *smack-pttrace-access-check-correctness4*:
 $\exists t m. \{ \lambda s. \text{smk-known } (\text{smk-of-task } (\text{the } ((t\text{-security } s) (\text{task-cred } (\text{current-task } s)))))) \neq \text{smk-known } (\text{smk-of-task-struct } s t) \wedge (((\text{int } m) \text{ AND } \text{PTRACE-MODE-ATTACH}) \neq 0) \wedge ((\text{smack-pttrace-rule shared}) = \text{SMACK-PTRACE-EXACT}) \vee ((\text{smack-pttrace-rule shared}) = \text{SMACK-PTRACE-DRACONIAN})) \}$
 $= \text{True}$
 $\wedge (\text{smack-pttrace-rule shared}) \neq \text{SMACK-PTRACE-DRACONIAN}$
 $\wedge \text{smack-privileged-cred CAP-SYS-PTRACE tracercred} = \text{False}$
 $\}$
 $\text{smack-pttrace-access-check } s t m \{ \lambda r s. r = -\text{EACCES} \}$
apply (*unfold smack-pttrace-access-check-def smk-pttrace-rule-check-def*)
apply *wsimp*
by (*metis int-and-comm int-and-extra-simps(1) semiring-1-class.of-nat-0*)

30.3 correctness lemmas of $\text{smack}_p\text{trace}_t\text{raceme}$

lemma *smack-pttrace-traceme-correctness*:
 $\{ \lambda s. \text{True} \} \text{smack-pttrace-traceme } s \text{ ptp } \{ \lambda r s. r = 0 \vee r \neq 0 \}$
apply (*unfold smack-pttrace-traceme-def smk-pttrace-rule-check-def*)
apply *wsimp*
done

30.4 correctness lemmas of $\text{smack}_s\text{yslog}$

lemma *smack-syslog-correctness*:
 $\{ \lambda s. \text{True} \} \text{smack-syslog } s t \{ \lambda r s. r = 0 \vee r = \text{uminus } \text{EACCES} \}$
apply (*unfold smack-syslog-def*)
apply *wsimp*
done

lemma *smack-syslog-correctness1*:

$\exists s. \{ \lambda s. \text{smack-privileged } s \text{ CAP-MAC-OVERRIDE} = \text{True} \} \text{smack-syslog } s \ t \{ \lambda r$
 $s. r = 0 \}$
apply(*unfold smack-syslog-def*)
apply *wpsimp*
by (*metis (mono-tags, lifting) hoare-return-simp*)

lemma *smack-syslog-correctness2*:

$\exists s. \{ \lambda s. \text{smack-privileged } s \text{ CAP-MAC-OVERRIDE} = \text{False}$
 $\wedge \text{smk-of-current } s \neq \text{smack-syslog-label shared} \} \text{smack-syslog } s \ t \{ \lambda r \ s. r =$
 $-EACCES \}$
apply(*unfold smack-syslog-def*)
apply *wpsimp*
by (*metis (mono-tags, lifting) hoare-return-simp*)

lemma *smack-syslog-correctness3*:

$\exists s. \{ \lambda s. \text{smack-privileged } s \text{ CAP-MAC-OVERRIDE} = \text{False}$
 $\wedge \text{smk-of-current } s = \text{smack-syslog-label shared} \} \text{smack-syslog } s \ t \{ \lambda r \ s. r =$
 $0 \}$
apply(*unfold smack-syslog-def*)
apply *wpsimp*
by (*metis (mono-tags, lifting) hoare-return-simp*)

30.5 correctness lemmas of *smack_{sb}alloc_{security}*

lemma *smack-sb-alloc-security-correctness*:

$\{ \lambda s. \text{True} \} \text{smack-sb-alloc-security } s \ sb$
 $\{ \lambda r \ s. (r = 0) \vee r = (\text{uminus } ENOMEM) \}$
apply(*unfold smack-sb-alloc-security-def*)
apply *wpsimp*
done

30.6 correctness lemmas of *smack_{sb}free_{security}*

lemma *smack-sb-free-security-correctness*:

$\{ \lambda s. \text{True} \} \text{smack-sb-free-security } s \ sb \{ \lambda r \ s. r = \text{unit} \}$
apply(*unfold smack-sb-free-security-def get-sbnum-def*)
apply *wpsimp*
done

lemma *smack-sb-free-security-correctness1*:

$\{ \lambda s. \text{True} \} \text{smack-sb-free-security } s \ sb \{ \lambda r \ s. (r = \text{unit} \wedge \text{sb-security } s \ sb = \text{None}) \}$
apply(*unfold smack-sb-free-security-def get-sbnum-def*)
apply *wpsimp*
done

30.7 correctness lemmas of *smack_{sb}copy_{data}*

lemma *smack-sb-copy-data-correctness*:

```

 $\{\lambda s. \text{True}\}$  smack-sb-copy-data s orig smackopts
 $\{\lambda r s. r = 0 \vee r = (\text{uminus ENOMEM})\}$ 
  apply(unfold smack-sb-copy-data-def)
  apply wpsimp
done

```

30.8 correctness lemmas of $\text{smack}_{parse_opts_tr}$

30.9 correctness lemmas of $\text{smack}_{set_mnt_opts}$

lemma *smack-set-mnt-opts-correctness*:

```

 $\{\lambda s. \text{True}\}$  smack-set-mnt-opts s sb opt kern-flags set-kern-flags
 $\{\lambda r s. r = 0 \vee r = (\text{uminus EPERM})\}$ 
  apply(unfold smack-set-mnt-opts-def)
  apply wpsimp
done

```

30.10 correctness lemmas of $\text{smack}_{sb_kern_mount}$

lemma *smack-sb-kern-mount-correctness*:

```

 $\{\lambda s. \text{True}\}$  smack-sb-kern-mount s sb f data  $\{\lambda r s. (r = 0 \vee r = (\text{uminus EPERM}))\}$ 
  apply(unfold smack-sb-kern-mount-def smack-set-mnt-opts-def)
  apply wpsimp
done

```

lemma *smack-sb-kern-mount-correctness1*:

```

 $\exists \text{data}. \{\lambda s. \text{length}(\text{data}) = 0\}$  smack-sb-kern-mount s sb f data  $\{\lambda r s. r = 0\}$ 
  apply(unfold smack-sb-kern-mount-def smack-set-mnt-opts-def)
  apply wpsimp
  by blast

```

30.11 correctness lemmas of smack_{sb_statfs}

lemma *smack-sb-statfs-correctness*:

```

 $\{\lambda s. \text{True}\}$  smack-sb-statfs s sb  $\{\lambda r s. (r = 0 \vee r \neq 0)\}$ 
  apply(unfold smack-sb-statfs-def )
  apply wpsimp
done

```

30.12 correctness lemmas of $\text{smack}_{bprm_set_creds}$

lemma *smack-bprm-set-creds-correctness*:

```

 $\{\lambda s. \text{True}\}$  smack-bprm-set-creds s bprm  $\{\lambda r s. r = 0 \vee r \neq 0\}$ 
  apply(unfold smack-bprm-set-creds-def smk-pttrace-rule-check-def pttrace-parent-def
smack-privileged-cred-def )
  apply wpsimp
done

```

30.13 correctness lemmas of $\text{smack}_{\text{inode}_a\text{alloc}_s\text{security}}$

lemma *smack-inode-alloc-security-correctness*:

```
 $\{\lambda s. \text{True}\}$  smack-inode-alloc-security s a  $\{\lambda r s. r = 0 \vee r = (\text{uminus } \text{ENOMEM})\}$   
 $\}$   
  apply (unfold smack-inode-alloc-security-def)  
  apply wpsimp  
  done
```

30.14 correctness lemmas of $\text{smack}_{\text{inode}_f\text{free}_s\text{security}}$

lemma *smack-inode-free-security-correctness*:

```
 $\{\lambda s. \text{True}\}$  smack-inode-free-security s a  $\{\lambda r s. r = \text{unit}\}$   
  apply (unfold smack-inode-free-security-def)  
  apply wpsimp  
  done
```

30.15 correctness lemmas of $\text{smack}_{\text{inode}_i\text{init}_s\text{security}}$

lemma *smack-inode-init-security-correctness*:

```
 $\{\lambda s. \text{True}\}$  smack-inode-init-security s inode dir qstr name value len'  $\{\lambda r s. r = 0 \vee r \neq 0\}$   
  apply wpsimp  
  done
```

30.16 correctness lemmas of $\text{smack}_{\text{inode}_l\text{link}}$

lemma *smack-inode-link-correctness*:

```
 $\{\lambda s. \text{True}\}$  smack-inode-link s old dir new  $\{\lambda r s. r = 0 \vee r \neq 0\}$   
  apply (unfold smack-inode-link-def)  
  apply wpsimp  
  done
```

30.17 correctness lemmas of $\text{smack}_{\text{inode}_u\text{unlink}}$

lemma *smack-inode-unlink-correctness*:

```
 $\{\lambda s. \text{True}\}$  smack-inode-unlink s dir d  $\{\lambda r s. r = 0 \vee r \neq 0\}$   
  apply (unfold smack-inode-unlink-def)  
  apply wpsimp  
  done
```

30.18 correctness lemmas of $\text{smack}_{\text{inode}_r\text{mdir}}$

lemma *smack-inode-rmdir-correctness*:

```
 $\{\lambda s. \text{True}\}$  smack-inode-rmdir s dir d  $\{\lambda r s. r = 0 \vee r \neq 0\}$   
  apply (unfold smack-inode-rmdir-def)  
  apply wpsimp  
  done
```

30.19 correctness lemmas of $\text{smack}_{i\text{node}_r\text{ename}}$

lemma *smack-inode-rename-correctness*:

$\{\lambda s. \text{True}\} \text{smack-inode-rename } s \text{ oldinode oldd newinode newd } \{\lambda r s. r = 0 \vee r \neq 0\}$

apply(*unfold smack-inode-rename-def*)
apply *wpsimp*
done

30.20 correctness lemmas of $\text{smack}_{i\text{node}_p\text{ermission}}$

lemma *smack-inode-permission-correctness*:

$\{\lambda s. \text{True}\} \text{smack-inode-permission } s \text{ i mask' } \{\lambda r s. r = 0 \vee r \neq 0\}$

apply(*unfold smack-inode-permission-def*)
apply *wpsimp*
done

30.21 correctness lemmas of $\text{smack}_{i\text{node}_s\text{etattr}}$

lemma *smack-inode-setattr-correctness*:

$\{\lambda s. \text{True}\} \text{smack-inode-setattr } s \text{ d attrs } \{\lambda r s. r = 0 \vee r \neq 0\}$

apply(*unfold smack-inode-setattr-def*)
apply *wpsimp*
done

30.22 correctness lemmas of $\text{smack}_{i\text{node}_g\text{etattr}}$

lemma *smack-inode-getattr-correctness*:

$\{\lambda s. \text{True}\} \text{smack-inode-getattr } s \text{ path' } \{\lambda r s. r = 0 \vee r \neq 0\}$

apply(*unfold smack-inode-getattr-def*)
apply *wpsimp*
done

30.23 correctness lemmas of $\text{smack}_{i\text{node}_s\text{etxattr}}$

lemma *smack-inode-setxattr-correctness*:

$\{\lambda s. \text{True}\} \text{smack-inode-setxattr } s \text{ dentry name value size' flags' } \{\lambda r s. r = 0 \vee r \neq 0\}$

apply(*unfold smack-inode-setxattr-def*)
apply *wpsimp*
done

30.24 correctness lemmas of $\text{smack}_{i\text{node}_p\text{ost}_s\text{etxattr}}$

lemma *smack-inode-post-setxattr-correctness*:

$\{\lambda s. \text{True}\} \text{smack-inode-post-setxattr } s \text{ dentry name value size' flags' } \{\lambda r s. r = \text{unit}\}$

apply(*unfold smack-inode-post-setxattr-def*)
apply *wpsimp*
done

30.25 correctness lemmas of `smackinodegetxattr`

lemma *smack-inode-getxattr-correctness*:
 $\{\lambda s. \text{True}\} \text{smack-inode-getxattr } s \text{ d name } \{\lambda r \text{ s. } r = 0 \vee r \neq 0\}$
 apply (*unfold smack-inode-getxattr-def*)
 apply *wpsimp*
 done

30.26 correctness lemmas of `smackinoderemovexattr`

lemma *smack-inode-removexattr-correctness*:
 $\{\lambda s. \text{True}\} \text{smack-inode-removexattr } s \text{ dentry name } \{\lambda r \text{ s. } r = 0 \vee r \neq 0\}$
 apply (*unfold smack-inode-removexattr-def*)
 apply *wpsimp*
 done

30.27 correctness lemmas of `smackinodegetsecurity`

lemma *smack-inode-getsecurity-correctness*:
 $\{\lambda s. \text{True}\} \text{smack-inode-getsecurity } s \text{ inode name buffer alloc } \{\lambda r \text{ s. } r = 0 \vee r \neq 0\}$
 apply (*unfold smack-inode-getsecurity-def*)
 apply *wpsimp*
 done

30.28 correctness lemmas of `smackinodelistsecurity`

lemma *smack-inode-listsecurity-correctness*:
 $\{\lambda s. \text{True}\} \text{smack-inode-listsecurity } s \text{ inode buffer buffer-size } \{\lambda r \text{ s. } r = 17\}$
 apply (*unfold smack-inode-listsecurity-def*)
 apply *wpsimp*
 done

30.29 correctness lemmas of `smackinodegetsecid`

lemma *smack-inode-getsecid-correctness*:
 $\{\lambda s. \text{True}\} \text{smack-inode-getsecid } s \text{ i secid' } \{\lambda r \text{ s. } r = \text{unit}\}$
 apply (*unfold smack-inode-getsecid-def*)
 apply *wpsimp*
 done

30.30 correctness lemmas of `smackfileallocsecurity`

lemma *smack-file-alloc-security-correctness*:
 $\bigwedge s \text{ f. } \{\lambda s. \text{True}\} \text{smack-file-alloc-security } s \text{ f } \{\lambda r \text{ s. } r = 0 \vee r = -EEXIST\}$
 apply (*unfold smack-file-alloc-security-def*)
 apply *wpsimp*
 done

lemma *smack-file-alloc-security-correctness-state*:

```

 $\wedge s' f. \llbracket \lambda so. so = s' \wedge f\text{-security } so \ f = \text{None} \rrbracket$ 
   $\text{smack-file-alloc-security } s' f$ 
   $\llbracket \lambda r \ sa. sa = s' (\llbracket f\text{-security } := (f\text{-security } s') (f := \text{Some } (\text{smk-of-current } s')) \rrbracket) \rrbracket$ 
  apply (unfold smack-file-alloc-security-def bind-def return-def modify-def put-def
get-def EEXIST-def valid-def)
  apply wpsimp
  done

```

30.31 correctness lemmas of *smack_{file}free_{security}*

lemma *smack-file-free-security-correctness*:

```

 $\llbracket \lambda s. \text{True} \rrbracket \text{smack-file-free-security } s \ f \ \llbracket \lambda r \ s. r = \text{unit} \rrbracket$ 
  apply (unfold smack-file-free-security-def)
  apply wpsimp
  done

```

30.32 correctness lemmas of *smack_{mmap}file*

lemma *smack-mmap-file-correctness*:

```

 $\llbracket \lambda s. \text{True} \rrbracket \text{smack-mmap-file } s \ \text{file}' \ \text{reqprot } \text{prot} \ \text{flags}' \ \llbracket \lambda r \ s. r = 0 \vee r \neq 0 \rrbracket$ 
  apply (unfold smack-mmap-file-def)
  apply wpsimp
  done

```

30.33 correctness lemmas of *smack_{file}ioctl*

lemma *smack-file-ioctl-correctness1*:

```

 $\exists \text{file}' \ \text{inode} .$ 
   $\llbracket \lambda s. \text{inode} = \text{file-inode}(\text{file}') \wedge \text{unlikely}(\text{IS-PRIVATE}(\text{inode})) \rrbracket$ 
   $\text{smack-file-ioctl } s \ \text{file}' \ \text{cmd} \ \text{arg}$ 
   $\llbracket \lambda r \ s. r = 0 \rrbracket$ 
  apply (unfold smack-file-ioctl-def)
  apply wpsimp
  by (smt hoare-assume-pre hoare-return-simp)

```

lemma *smack-file-ioctl-correctness-ioc-write*:

```

 $\exists \text{file}' \ \text{inode} \ \text{cmd} \ \text{ret}.$ 
   $\llbracket \lambda s. \text{inode} = \text{file-inode}(\text{file}') \wedge$ 
     $\text{unlikely}(\text{IS-PRIVATE}(\text{inode})) = \text{False} \wedge$ 
     $\text{cmd} = \text{IOC-WRITE} \wedge$ 
     $\text{ret} = \text{fst}(\text{the-run-state } (\text{smk-curacc } s \ (\text{smk-of-inode } s \ \text{inode}) \ \text{MAY-WRITE}$ 
ad) s)  $\rrbracket$ 
   $\text{smack-file-ioctl } s \ \text{file}' \ \text{cmd} \ \text{arg}$ 
   $\llbracket \lambda r \ s. r = \text{ret} \rrbracket$ 
  apply (unfold smack-file-ioctl-def smk-bu-file-def bind-def return-def valid-def
the-run-state-def fstI)
  by auto

```

lemma *smack-file-ioctl-correctness-ioc-read*:

$\exists file' inode cmd ret.$
 $\{\lambda s. inode = file_inode(file') \wedge$
 $unlikely(IS-PRIVATE(inode)) = False \wedge$
 $cmd = IOC-READ \wedge$
 $ret = fst(the-run-state (smk-curacc s (smk-of-inode s inode) MAY-READ$
 $ad) s)\}$
 $smack-file-ioctl s file' cmd arg$
 $\{\lambda r s. r = ret \}$
apply(*unfold smack-file-ioctl-def smk-bu-file-def bind-def return-def valid-def*
the-run-state-def fstI)
by *auto*

lemma *smack-file-ioctl-correctness-ioc-other*:
 $\exists file' inode cmd.$
 $\{\lambda s. inode = file_inode(file') \wedge$
 $unlikely(IS-PRIVATE(inode)) = False \wedge$
 $cmd \neq IOC-READ \wedge$
 $cmd \neq IOC-WRITE\}$
 $smack-file-ioctl s file' cmd arg$
 $\{\lambda r s. r = 0 \}$
apply(*unfold smack-file-ioctl-def smk-bu-file-def bind-def return-def valid-def*
the-run-state-def fstI)
by *auto*

30.34 correctness lemmas of *smack_{filelock}*

lemma *smack-file-lock-correctness*:
 $\{\lambda s. True\} smack-file-lock s file' cmd \{\lambda r s. r = 0 \vee r \neq 0\}$
apply(*unfold smack-file-lock-def*)
apply *wsimp*
done

lemma *smack-file-lock-correctness1*:
 $\exists file' inode .$
 $\{\lambda s. inode = file_inode(file') \wedge unlikely(IS-PRIVATE(inode)) \}$
 $smack-file-lock s file' cmd$
 $\{\lambda r s. r = 0 \}$
apply(*unfold smack-file-lock-def*)
apply *wsimp*
by (*smt hoare-assume-pre hoare-return-simp*)

lemma *smack-file-lock-correctness2*:
 $\exists file' inode rc.$
 $\{\lambda s. (SECURITY-SMACK-BRINGUP conf) = True \wedge inode = file_inode(file') \wedge$
 $unlikely(IS-PRIVATE(inode)) = False \}$
 $smack-file-lock s file' cmd$
 $\{\lambda r s. r = 0 \}$
apply(*unfold smack-file-lock-def smk-bu-file-def bind-def return-def valid-def*)
by *auto*

lemma *smack-file-lock-correctness3*:

$\forall sa. \exists file' inode ret ad.$
 $\{\lambda s. (SECURITY-SMACK-BRINGUP\ conf) = False \wedge s = sa \wedge$
 $inode = file-inode(file') \wedge$
 $unlikely(IS-PRIVATE(inode)) = False \wedge$
 $ret = fst(the-run-state (smk-curacc\ s\ (smk-of-inode\ s\ inode)\ MAY-LOCK$
 $ad)\ s)\}$
 $smack-file-lock\ sa\ file'\ cmd$
 $\{\lambda r\ s. r = ret\}$
apply(*unfold smack-file-lock-def smk-bu-file-def bind-def return-def valid-def*
the-run-state-def fstI)
apply *auto*
by *blast*

30.35 correctness lemmas of *smack_{filefcntl}.def*

lemma *smack-file-fcntl-correctness*:

$\{\lambda s. True\}$ *smack-file-fcntl* *s file' cmd arg* $\{\lambda r\ s. r = 0 \vee r \neq 0\}$
apply(*unfold smack-file-fcntl-def*)
apply *wp simp*
done

lemma *smack-file-fcntl-correctness1*:

$\exists file' inode .$
 $\{\lambda s. inode = file-inode(file') \wedge unlikely(IS-PRIVATE(inode))\}$
 $smack-file-fcntl\ s\ file'\ cmd\ arg$
 $\{\lambda r\ s. r = 0\}$
apply(*unfold smack-file-fcntl-def*)
apply *wp simp*
by (*smt hoare-assume-pre hoare-return-simp*)

lemma *smack-file-fcntl-correctness-fsetlkandfsetlkw*:

$\forall sa. \exists file' inode ret ad\ cmd.$
 $\{\lambda s. (SECURITY-SMACK-BRINGUP\ conf) = False \wedge s = sa \wedge$
 $inode = file-inode(file') \wedge$
 $unlikely(IS-PRIVATE(inode)) = False \wedge$
 $(cmd = F-SETLK \vee cmd = F-SETLKW) \wedge$
 $ret = fst(the-run-state (smk-curacc\ s\ (smk-of-inode\ s\ inode)\ MAY-LOCK$
 $ad)\ s)\}$
 $smack-file-fcntl\ s\ file'\ cmd\ arg$
 $\{\lambda r\ s. r = ret\}$
apply(*unfold smack-file-fcntl-def smk-bu-file-def bind-def return-def valid-def*
the-run-state-def fstI)
apply *auto*
by *blast*

lemma *smack-file-fcntl-correctness-fsetownandsig*:

$\forall sa . \exists file' inode ret ad\ cmd.$

```

 $\{\lambda s. (SECURITY-SMACK-BRINGUP\ conf) = False \wedge s = sa \wedge$ 
 $inode = file-inode(file') \wedge$ 
 $unlikely(IS-PRIVATE(inode)) = False \wedge$ 
 $(cmd = F-SETOWN \vee cmd = F-SETSIG) \wedge$ 
 $ret = fst(the-run-state (smk-curacc\ s\ (smk-of-inode\ s\ inode)\ MAY-WRITE$ 
 $ad)\ s)\}$ 
 $smack-file-fcntl\ s\ file'\ cmd\ arg$ 
 $\{\lambda r\ s. r = ret\}$ 
apply(unfold smack-file-fcntl-def smk-bu-file-def bind-def return-def valid-def
the-run-state-def fstI)
apply auto
by blast

```

lemma *smack-file-fcntl-correctness-other*:

```

 $\forall sa. \exists file'\ inode\ ret\ ad\ cmd.$ 
 $\{\lambda s. (SECURITY-SMACK-BRINGUP\ conf) = False \wedge s = sa \wedge$ 
 $inode = file-inode(file') \wedge$ 
 $unlikely(IS-PRIVATE(inode)) = False \wedge$ 
 $(cmd \neq F-SETOWN \wedge cmd \neq F-SETSIG \wedge cmd \neq F-SETLK \wedge cmd \neq$ 
 $F-SETLKW) \wedge$ 
 $ret = fst(the-run-state (smk-curacc\ s\ (smk-of-inode\ s\ inode)\ MAY-WRITE$ 
 $ad)\ s)\}$ 
 $smack-file-fcntl\ s\ file'\ cmd\ arg$ 
 $\{\lambda r\ s. r = 0\}$ 
apply(unfold smack-file-fcntl-def smk-bu-file-def bind-def return-def valid-def
the-run-state-def fstI)
apply auto
done

```

30.36 correctness lemmas of `smackfile_set_fowner`

lemma *smack-file-set-fowner-correctness*:

```

 $\{\lambda s. True\}$  smack-file-set-fowner s file'  $\{\lambda r\ s. r = unit\}$ 
apply(unfold smack-file-set-fowner-def)
apply wsimp
done

```

lemma *smack-file-set-fowner-correctness1*:

```

 $\wedge sa. \{\lambda s. s = sa\}$  smack-file-set-fowner sa file'  $\{\lambda r\ s. f-security\ s\ file' = Some$ 
 $(smk-of-current\ sa)\}$ 
apply(unfold smack-file-set-fowner-def modify-def return-def get-def put-def bind-def
valid-def)
apply wsimp
done

```

30.37 correctness lemmas of `smackfile_send_sigiotask`

lemma *smack-file-send-sigiotask-correctness*:

```

 $\{\lambda s. True\}$  smack-file-send-sigiotask s tsk' fown signum  $\{\lambda r\ s. r = 0 \vee r \neq 0\}$ 
apply(unfold smack-file-send-sigiotask-def)

```

apply wpsimp
done

30.38 correctness lemmas of $\text{smack}_{file_receive}$

lemma *smack-file-receive-correctness*:
 $\{\lambda s. \text{True}\} \text{smack-file-receive } s \text{ file}' \{\lambda r s. r = 0 \vee r \neq 0\}$
 apply (unfold smack-file-receive-def)
 apply wpsimp
 done

30.39 correctness lemmas of smack_{file_open}

lemma *smack-file-open-correctness*:
 $\{\lambda s. \text{True}\} \text{smack-file-open } s \text{ file}' \{\lambda r s. r = 0 \vee r \neq 0\}$
 apply (unfold smack-file-open-def)
 apply wpsimp
 done

30.40 correctness lemmas of $\text{smack}_{cred_alloc_blank}$

lemma *smack-cred-alloc-blank-correctness*:
 $\{\lambda s. \text{True}\} \text{smack-cred-alloc-blank } s \text{ c g } \{\lambda r s. r = 0 \vee r = -ENOMEM\}$
 apply (unfold smack-cred-alloc-blank-def)
 apply wpsimp
 done

30.41 correctness lemmas of smack_{cred_free}

lemma *smack-cred-free-correctness*:
 $\{\lambda s. \text{True}\} \text{smack-cred-free } s \text{ c } \{\lambda r s. r = \text{unit} \wedge (t\text{-security } s) \text{ c} = \text{None}\}$
 apply (unfold smack-cred-free-def)
 apply wpsimp
 done

30.42 correctness lemmas of $\text{smack}_{cred_prepare}$

lemma *smack-cred-prepare-correctness*:
 $\{\lambda s. \text{True}\} \text{smack-cred-prepare } s \text{ new old g } \{\lambda r s. r = 0 \vee r \neq 0\}$
 apply (unfold smack-cred-prepare-def)
 apply wpsimp
 done

30.43 correctness lemmas of $\text{smack}_{cred_getsecid}$

lemma *smack-cred-getsecid-correctness*:
 $\{\lambda s. \text{True}\} \text{smack-cred-getsecid } s \text{ c i } \{\lambda r s'. r = \text{unit}\}$
 apply (unfold smack-cred-getsecid-def smk-of-task-def)
 apply wpsimp
 done

30.44 correctness lemmas of $\text{smack}_{cred_transfer}$

lemma *smack-cred-transfer-correctness*:

$\{\lambda s. \text{True}\} \text{smack-cred-transfer } s \text{ new old } \{\lambda r s'. r = \text{unit} \}$
 apply(*unfold smack-cred-transfer-def smk-of-task-def*)
 apply *wsimp*
 done

30.45 correctness lemmas of $\text{smack}_{kernel_act_as}$

lemma *smack-kernel-act-as-correctness*:

$\{\lambda s. \text{True}\} \text{smack-kernel-act-as } s \text{ c i } \{\lambda r s. r = 0 \}$
 apply(*unfold smack-kernel-act-as-def*)
 apply *wsimp*
 done

30.46 correctness lemmas of $\text{smack}_{kernel_create_files_as}$

lemma *smack-kernel-create-files-as-correctness*:

$\{\lambda s. \text{True}\} \text{smack-kernel-create-files-as } s \text{ new i } \{\lambda r s. r = 0 \}$
 apply(*unfold smack-kernel-create-files-as-def*)
 apply *wsimp*
 done

30.47 correctness lemmas of $\text{smk}_{curacc_on_task}$

lemma *smk-curacc-on-task-correctness*:

$\{\lambda s. \text{True}\} \text{smk-curacc-on-task } s \text{ p access' caller' } \{\lambda r s. r = 0 \vee r \neq 0 \}$
 apply(*unfold smk-curacc-on-task-def*)
 apply *wsimp*
 done

30.48 correctness lemmas of $\text{smack}_{task_setpgid}$

lemma *smack-task-setpgid-correctness*:

$\{\lambda s. \text{True}\} \text{smack-task-setpgid } s \text{ p pid } \{\lambda r s. r = 0 \vee r \neq 0 \}$
 apply(*unfold smack-task-setpgid-def smk-curacc-on-task-def*)
 apply *wsimp*
 done

30.49 correctness lemmas of $\text{smack}_{task_getpgid}$

lemma *smack-task-getpgid-correctness*:

$\{\lambda s. \text{True}\} \text{smack-task-getpgid } s \text{ p } \{\lambda r s. r = 0 \vee r \neq 0 \}$
 apply(*unfold smack-task-getpgid-def smk-curacc-on-task-def*)
 apply *wsimp*
 done

30.50 correctness lemmas of $\text{smack}_{task_getsid}$

lemma *smack-task-getsid-correctness*:

```

 $\{\lambda s. \text{True}\}$  smack-task-getsid s p  $\{\lambda r s. r = 0 \vee r \neq 0\}$ 
  apply(unfold smack-task-getsid-def smk-curacc-on-task-def)
  apply wpsimp
done

```

30.51 correctness lemmas of *smack_task_getsecid*

```

lemma smack-task-getsecid-correctness:
 $\{\lambda s. \text{True}\}$  smack-task-getsecid s p pid  $\{\lambda r s. r = \text{unit}\}$ 
  apply(unfold smack-task-getsecid-def smk-curacc-on-task-def)
  apply wpsimp
done

```

30.52 correctness lemmas of *smack_task_setnice*

```

lemma smack-task-setnice-correctness:
 $\{\lambda s. \text{True}\}$  smack-task-setnice s p pid  $\{\lambda r s. r = 0 \vee r \neq 0\}$ 
  apply(unfold smack-task-setnice-def smk-curacc-on-task-def)
  apply wpsimp
done

```

30.53 correctness lemmas of *smack_task_setioprio*

```

lemma smack-task-setioprio-correctness:
 $\{\lambda s. \text{True}\}$  smack-task-setioprio s p pid  $\{\lambda r s. r = 0 \vee r \neq 0\}$ 
  apply(unfold smack-task-setioprio-def smk-curacc-on-task-def)
  apply wpsimp
done

```

30.54 correctness lemmas of *smack_task_getioprio*

```

lemma smack-task-getioprio-correctness:
 $\{\lambda s. \text{True}\}$  smack-task-getioprio s p  $\{\lambda r s. r = 0 \vee r \neq 0\}$ 
  apply(unfold smack-task-getioprio-def smk-curacc-on-task-def)
  apply wpsimp
done

```

30.55 correctness lemmas of *smack_task_setscheduler*

```

lemma smack-task-setscheduler-correctness:
 $\{\lambda s. \text{True}\}$  smack-task-setscheduler s p  $\{\lambda r s. r = 0 \vee r \neq 0\}$ 
  apply(unfold smack-task-setscheduler-def smk-curacc-on-task-def)
  apply wpsimp
done

```

30.56 correctness lemmas of *smack_task_getscheduler*

```

lemma smack-task-getscheduler-correctness:
 $\{\lambda s. \text{True}\}$  smack-task-getscheduler s p  $\{\lambda r s. r = 0 \vee r \neq 0\}$ 
  apply(unfold smack-task-getscheduler-def smk-curacc-on-task-def)

```


apply wpsimp
done

30.57 correctness lemmas of $\text{smack}_{task_{move}memory}$

lemma *smack-task-movememory-correctness*:

$\{\lambda s. \text{True}\} \text{smack-task-movememory } s \ p \ \{\lambda r \ s. r = 0 \vee r \neq 0\}$
 apply (unfold smack-task-movememory-def smk-curacc-on-task-def)
 apply wpsimp
 done

30.58 correctness lemmas of $\text{smack}_{task_{kill}}$

lemma *smack-task-kill-correctness*:

$\{\lambda s. \text{True}\} \text{smack-task-kill } s \ p \ \text{info sig } c \ \{\lambda r \ s'. r = 0 \vee r \neq 0\}$
 apply (unfold smack-task-kill-def smk-curacc-on-task-def)
 apply wpsimp
 done

30.59 correctness lemmas of $\text{smack}_{task_{oinode}}$

lemma *smack-task-to-inode-correctness*:

$\forall p. \{\lambda s. \text{True}\} \text{smack-task-to-inode } s \ p \ i \ \{\lambda r \ s'. r = \text{unit}\}$
 apply (unfold smack-task-to-inode-def smk-curacc-on-task-def)
 apply wpsimp
 done

30.60 correctness lemmas of $\text{smack}_{ipc_{permission}}$

lemma *smack-ipc-permission-correctness*:

$\{\lambda s. \text{True}\} \text{smack-ipc-permission } s \ \text{ipp flag} \ \{\lambda r \ s'. r = 0 \vee r \neq 0\}$
 apply (unfold smack-ipc-permission-def)
 apply wpsimp
 done

30.61 correctness lemmas of $\text{smack}_{ipc_{getsecid}}$

lemma *smack-ipc-getsecid-correctness*:

$\{\lambda s. \text{True}\} \text{smack-ipc-getsecid } s \ \text{ipp flag} \ \{\lambda r \ s'. r = ()\}$
 apply (unfold smack-ipc-getsecid-def)
 apply wpsimp
 done

30.62 correctness lemmas of $\text{smack}_{msg_{msgalloc}security}$

lemma *smack-msg-msg-alloc-security-correctness*:

$\{\lambda s. \text{True}\} \text{smack-msg-msg-alloc-security } s \ \text{msg} \ \{\lambda r \ s'. r = 0 \vee r \neq 0\}$
 apply (unfold smack-msg-msg-alloc-security-def)
 apply wpsimp
 done

lemma *smack-msg-msg-alloc-security-correctness-state*:
 $\bigwedge sa\ msg. \{\lambda s. s = sa \wedge msg_security\ s\ msg = None\}$
 $\quad smack_msg_msg_alloc_security\ sa\ msg$
 $\quad \{\lambda r\ s. msg_security\ s\ msg = Some\ (smk_of_current\ sa)\}$
apply(*unfold smack-msg-msg-alloc-security-def*)
apply *wpsimp*
done

30.63 correctness lemmas of $smack_{msg_msg_free_security}$

lemma *smack-msg-msg-free-security-correctness*:
 $\{\lambda s. True\} smack_msg_msg_free_security\ s\ msg\ \{\lambda r\ s'. r = ()\}$
apply(*unfold smack-msg-msg-free-security-def*)
apply *wpsimp*
done

30.64 correctness lemmas of $smack_{ipc_alloc_security}$

lemma *smack-ipc-alloc-security-correctness*:
 $\{\lambda s. True\} smack_ipc_alloc_security\ s\ isp\ \{\lambda r\ s. r = 0\}$
apply(*unfold smack-ipc-alloc-security-def*)
apply *wpsimp*
done

30.65 correctness lemmas of $smack_{ipc_free_security}$

lemma *smack-ipc-free-security-correctness*:
 $\{\lambda s. True\} smack_ipc_free_security\ s\ isp\ \{\lambda r\ s. r = ()\}$
apply(*unfold smack-ipc-free-security-def*)
apply *wpsimp*
done

30.66 correctness lemmas of $smack_{shm_associate}$

lemma *smack-shm-associate-correctness*:
 $\{\lambda s. True\} smack_shm_associate\ s\ isp\ shm_flg\ \{\lambda r\ s'. r = 0 \vee r \neq 0\}$
apply(*unfold smack-shm-associate-def*)
apply *wpsimp*
done

30.67 correctness lemmas of $smack_{shm_shmctl}$

lemma *smack-shm-shmctl-correctness*:
 $\{\lambda s. True\} smack_shm_shmctl\ s\ isp\ cmd\ \{\lambda r\ s. r = 0 \vee r \neq 0\}$
apply(*unfold smack-shm-shmctl-def*)
apply *wpsimp*
done

30.68 correctness lemmas of smack_{shm_shmat}

lemma *smack-shm-shmat-correctness*:

$\{\lambda s. \text{True}\} \text{smack-shm-shmat } s \text{ ipc' shmaddr shmflg } \{\lambda r s. r = 0 \vee r \neq 0\}$
 apply (*unfold smack-shm-shmat-def*)
 apply *wp simp*
 done

30.69 correctness lemmas of smk_{curacc_sem}

lemma *smk-curacc-sem-correctness*:

$\{\lambda s. \text{True}\} \text{smk-curacc-sem } s \text{ isp access } \{\lambda r s. r = 0 \vee r \neq 0\}$
 apply (*unfold smk-curacc-sem-def*)
 apply *wp simp*
 done

30.70 correctness lemmas of $\text{smack}_{sem_associate}$

lemma *smack-sem-associate-correctness*:

$\{\lambda s. \text{True}\} \text{smack-sem-associate } s \text{ isp shmflg } \{\lambda r s. r = 0 \vee r \neq 0\}$
 apply (*unfold smack-sem-associate-def*)
 apply *wp simp*
 done

30.71 correctness lemmas of $\text{smack}_{sem_semctl}$

lemma *smack-sem-semctl-correctness*:

$\{\lambda s. \text{True}\} \text{smack-sem-semctl } s \text{ isp cmd } \{\lambda r s. r = 0 \vee r \neq 0\}$
 apply (*unfold smack-sem-semctl-def*)
 apply *wp simp*
 done

30.72 correctness lemmas of smack_{sem_semop}

lemma *smack-sem-semop-correctness*:

$\{\lambda s. \text{True}\} \text{smack-sem-semop } s \text{ isp sops nsops alter } \{\lambda r s. r = 0 \vee r \neq 0\}$
 apply (*unfold smack-sem-semop-def*)
 apply *wp simp*
 done

30.73 correctness lemmas of smk_{curacc_msq}

lemma *smk-curacc-msq-correctness*:

$\{\lambda s. \text{True}\} \text{smk-curacc-msq } s \text{ isp acces } \{\lambda r s. r = 0 \vee r \neq 0\}$
 apply (*unfold smk-curacc-msq-def*)
 apply *wp simp*
 done

30.74 correctness lemmas of $\text{smack}_{msg_queue_associate}$

lemma *smack-msg-associate-correctness*:

```

 $\{\lambda s. \text{True}\}$  smack-msg-queue-associate s isp shmflg  $\{\lambda r s. r = 0 \vee r \neq 0\}$ 
  apply(unfold smack-msg-queue-associate-def )
  apply wpsimp
done

```

30.75 correctness lemmas of *smack_{msgqueuemsgctl}*

```

lemma smack-msg-queue-msgctl-correctness:
 $\{\lambda s. \text{True}\}$  smack-msg-queue-msgctl s isp cmd  $\{\lambda r s. r = 0 \vee r \neq 0\}$ 
  apply(unfold smack-msg-queue-msgctl-def )
  apply wpsimp
done

```

30.76 correctness lemmas of *smack_{msgqueuemsgsnd}*

```

lemma smack-msg-queue-msgsnd-correctness:
 $\{\lambda s. \text{True}\}$  smack-msg-queue-msgsnd s isp msg msgflg  $\{\lambda r s. r = 0 \vee r \neq 0\}$ 
  apply(unfold smack-msg-queue-msgsnd-def )
  apply wpsimp
done

```

30.77 correctness lemmas of *smack_{msgqueuemsgrcv}*

```

lemma smack-msg-queue-msgrcv-correctness:
 $\{\lambda s. \text{True}\}$  smack-msg-queue-msgrcv s isp msg p long msgflg  $\{\lambda r s. r = 0 \vee r \neq 0\}$ 
  apply(unfold smack-msg-queue-msgrcv-def )
  apply wpsimp
done

```

30.78 correctness lemmas of *smack_{keyalloc}*

```

lemma smack-key-alloc-correctness:
 $\{\lambda s. \text{True}\}$  smack-key-alloc s k c flg  $\{\lambda r s. r = 0\}$ 
  apply(unfold smack-key-alloc-def )
  apply wpsimp
done

```

30.79 correctness lemmas of *smack_{keyfree}*

```

lemma smack-key-free-correctness:
 $\{\lambda s. \text{True}\}$  smack-key-free s k  $\{\lambda r s. r = \text{unit}\}$ 
  apply(unfold smack-key-free-def )
  apply wpsimp
done

```

30.80 correctness lemmas of *smack_{keypermission}*

```

lemma smack-key-permission-correctness:
 $\{\lambda s. \text{True}\}$  smack-key-permission s key-ref c perm  $\{\lambda r s. r = 0 \vee r \neq 0\}$ 

```

```

apply(unfold smack-key-permission-def )
apply wpsimp
done

```

30.81 correctness lemmas of $\text{smack}_{key_getsecurity}$

```

lemma smack-key-getsecurity-correctness:
 $\llbracket \lambda s. \text{True} \rrbracket \text{smack-key-getsecurity } s \text{ } k \text{ } buffer \llbracket \lambda r \text{ } s. r = 0 \vee r \neq 0 \rrbracket$ 
apply(unfold smack-key-getsecurity-def )
apply wpsimp
done

```

30.82 correctness lemmas of $\text{smack}_{unix_stream_connect}$

```

lemma smack-unix-stream-connect-correctness:
 $\llbracket \lambda s. \text{True} \rrbracket \text{smack-unix-stream-connect } s \text{ } sock \text{ } other \text{ } newsk \llbracket \lambda r \text{ } s. r = 0 \vee r \neq 0 \rrbracket$ 
apply(unfold smack-unix-stream-connect-def )
apply wpsimp
done

```

30.83 correctness lemmas of $\text{smack}_{unix_may_send}$

```

lemma smack-unix-may-send-correctness:
 $\llbracket \lambda s. \text{True} \rrbracket \text{smack-unix-may-send } s \text{ } sock \text{ } other \llbracket \lambda r \text{ } s. r = 0 \vee r \neq 0 \rrbracket$ 
apply(unfold smack-unix-may-send-def )
apply wpsimp
done

```

30.84 correctness lemmas of $\text{smack}_{socket_post_create}$

```

lemma smack-socket-post-create-correctness:
 $\llbracket \lambda s. \text{True} \rrbracket \text{smack-socket-post-create } s \text{ } sock \text{ } family \text{ } type' \text{ } protocols \text{ } kern \llbracket \lambda r \text{ } s'. r = 0 \vee r \neq 0 \rrbracket$ 
apply(unfold smack-socket-post-create-def )
apply wpsimp
done

```

30.85 correctness lemmas of $\text{smack}_{socket_socketpair}$

```

lemma smack-socket-socketpair-correctness:
 $\llbracket \lambda s. \text{True} \rrbracket \text{smack-socket-socketpair } s \text{ } socka \text{ } sockb \llbracket \lambda r \text{ } s'. r = 0 \rrbracket$ 
apply(unfold smack-socket-socketpair-def )
apply wpsimp
done

```

30.86 correctness lemmas of $\text{smack}_{socket_bind}$

```

lemma smack-socket-bind-correctness:
 $\llbracket \lambda s. \text{True} \rrbracket \text{smack-socket-bind } s \text{ } sock \text{ } address \text{ } addrlen \llbracket \lambda r \text{ } s'. r = 0 \rrbracket$ 
apply(unfold smack-socket-bind-def )

```

apply wpsimp
done

30.87 correctness lemmas of $\text{smack}_{\text{socket_connect}}$

lemma *smack-socket-connect-correctness*:
 $\{\lambda s. \text{True}\} \text{smack-socket-connect } s \text{ sock sap addrlen } \{\lambda r s'. r = 0 \vee r \neq 0\}$
 apply (unfold smack-socket-connect-def)
 apply wpsimp
 done

30.88 correctness lemmas of $\text{smack}_{\text{socket_sendmsg}}$

lemma *smack-socket-sendmsg-correctness*:
 $\{\lambda s. \text{True}\} \text{smack-socket-sendmsg } s \text{ sock msg size' } \{\lambda r s'. r = 0 \vee r \neq 0\}$
 apply (unfold smack-socket-sendmsg-def)
 apply wpsimp
 done

30.89 correctness lemmas of $\text{smack}_{\text{socket_sock_rcv_skb}}$

lemma *smack-socket-sock-rcv-skb-correctness*:
 $\{\lambda s. \text{True}\} \text{smack-socket-sock-rcv-skb } s \text{ sock skb } \{\lambda r s'. r = 0 \vee r \neq 0\}$
 apply (unfold smack-socket-sock-rcv-skb-def)
 apply wpsimp
 done

30.90 correctness lemmas of $\text{smack}_{\text{socket_getpeersec_stream}}$

lemma *smack-socket-getpeersec-stream-correctness*:
 $\{\lambda s. \text{True}\} \text{smack-socket-getpeersec-stream } s \text{ sock optval optlen len' } \{\lambda r s'. r = 0 \vee r \neq 0\}$
 apply (unfold smack-socket-getpeersec-stream-def)
 apply wpsimp
 done

30.91 correctness lemmas of $\text{smack}_{\text{socket_getpeersec_dgram}}$

lemma *smack-socket-getpeersec-dgram-correctness*:
 $\{\lambda s. \text{True}\} \text{smack-socket-getpeersec-dgram } s \text{ sock skb secid' } \{\lambda r s'. r = 0 \vee r \neq 0\}$
 apply (unfold smack-socket-getpeersec-dgram-def)
 apply wpsimp
 done

30.92 correctness lemmas of $\text{smack}_{\text{sk_alloc_security}}$

lemma *smack-sk-alloc-security-correctness*:
 $\{\lambda s. \text{True}\} \text{smack-sk-alloc-security } s \text{ sock family flgs } \{\lambda r s'. r = 0 \vee r \neq 0\}$
 apply (unfold smack-sk-alloc-security-def)

```

apply wpsimp
done

```

30.93 correctness lemmas of $\text{smack}_{sk_free_security}$

```

lemma smack-sk-free-security-correctness:
 $\llbracket \lambda s. \text{True} \rrbracket \text{smack-sk-free-security } s \text{ sock } \llbracket \lambda r \ s'. r = \text{unit} \rrbracket$ 
  apply (unfold smack-sk-free-security-def )
  apply wpsimp
done

```

30.94 correctness lemmas of $\text{smack}_{sock_graft}$

```

lemma smack-sock-graft-correctness:
 $\llbracket \lambda s. \text{True} \rrbracket \text{smack-sock-graft } s \text{ sock parent' } \llbracket \lambda r \ s'. r = \text{unit} \rrbracket$ 
  apply (unfold smack-sock-graft-def )
  apply wpsimp
done

```

30.95 correctness lemmas of $\text{smack}_{inet_conn_request}$

```

lemma smack-inet-conn-request-correctness:
 $\llbracket \lambda s. \text{True} \rrbracket \text{smack-inet-conn-request } s \text{ sock skb req } \llbracket \lambda r \ s'. r = 0 \vee r \neq 0 \rrbracket$ 
  apply (unfold smack-inet-conn-request-def )
  apply wpsimp
done

```

30.96 correctness lemmas of $\text{smack}_{inet_csk_clone}$

```

lemma smack-inet-csk-clone-correctness:
 $\llbracket \lambda s. \text{True} \rrbracket \text{smack-inet-csk-clone } s \text{ sock req } \llbracket \lambda r \ s'. r = \text{unit} \rrbracket$ 
  apply (unfold smack-inet-csk-clone-def )
  apply wpsimp
done

```

30.97 correctness lemmas of $\text{smack}_{audit_rule_init}$

```

lemma smack-audit-rule-init-correctness:
 $\llbracket \lambda s. \text{True} \rrbracket \text{smack-audit-rule-init } s \text{ field op rulestr vrule } \llbracket \lambda r \ s'. r = 0 \vee r \neq 0 \rrbracket$ 
  apply wpsimp
done

```

30.98 correctness lemmas of $\text{smack}_{audit_rule_known}$

```

lemma smack-audit-rule-known-correctness:
 $\llbracket \lambda s. \text{True} \rrbracket \text{smack-audit-rule-known } s \text{ krule } \llbracket \lambda r \ s'. r = 0 \vee r \neq 0 \rrbracket$ 
  apply wpsimp
done

```

30.99 correctness lemmas of $\text{smack}_{audit_rule_match}$

lemma *smack-audit-rule-match-correctness*:

$\{\lambda s. \text{True}\}$ *smack-audit-rule-match* s *secid'* *field op vrule actx* $\{\lambda r s'. r = 0 \vee r \neq 0\}$
 apply *wpsimp*
 done

30.100 correctness lemmas of $\text{smack}_i\text{smaclabel}$

lemma *smack-ismaclabel-correctness*:

$\{\lambda s. \text{True}\}$ *smack-ismaclabel* s *name* $\{\lambda r s'. r = 0 \vee r \neq 0\}$
 apply *wpsimp*
 done

30.101 correctness lemmas of $\text{smack}_s\text{ecid}_t\text{o}_s\text{ecctx}$

lemma *smack-secid-to-secctx-correctness*:

$\{\lambda s. \text{True}\}$ *smack-secid-to-secctx* s *secid'* *secddata seclen* $\{\lambda r s. r = 0\}$
 apply(*unfold smack-secid-to-secctx-def*)
 apply *wpsimp*
 done

30.102 correctness lemmas of $\text{smack}_s\text{ecctx}_t\text{o}_s\text{ecid}$

lemma *smack-secctx-to-secid-correctness*:

$\{\lambda s. \text{True}\}$ *smack-secctx-to-secid* s *secddata seclen* *secid'* $\{\lambda r s. r = 0\}$
 apply(*unfold smack-secctx-to-secid-def*)
 apply *wpsimp*
 done

30.103 correctness lemmas of $\text{smack}_i\text{node}_n\text{otifysecctx}$

lemma *smack-inode-notifysecctx-correctness*:

$\{\lambda s. \text{True}\}$ *smack-inode-notifysecctx* s *inode ctx ctxlen* $\{\lambda r s'. r = 0 \vee r \neq 0\}$
 apply(*unfold smack-inode-notifysecctx-def*)
 apply *wpsimp*
 done

30.104 correctness lemmas of $\text{smack}_i\text{node}_s\text{etsecctx}$

lemma *smack-inode-setsecctx-correctness*:

$\{\lambda s. \text{True}\}$ *smack-inode-setsecctx* s *dentry ctx ctxlen* $\{\lambda r s'. r = 0 \vee r \neq 0\}$
 apply(*unfold smack-inode-setsecctx-def*)
 apply *wpsimp*
 done

30.105 correctness lemmas of $\text{smack}_i\text{node}_g\text{etsecctx}$

lemma *smack-inode-getsecctx-correctness*:

$\{\lambda s. \text{True}\}$ *smack-inode-getsecctx* s *inode ctx ctxlen* $\{\lambda r s. r = 0\}$


```

apply(unfold smack-inode-getsecctx-def)
apply wpsimp
done

```

30.106 correctness lemmas of $\text{smack}_{\text{inode_copy_up}}$

```

lemma smack-inode-copy-up-correctness:
 $\{\lambda s. \text{True}\} \text{smack-inode-copy-up } s \text{ dentry new } \{\lambda r s'. r = 0 \vee r \neq 0\}$ 
apply wpsimp
done

```

30.107 correctness lemmas of $\text{smack}_{\text{inode_copy_up_xattr}}$

```

lemma smack-inode-copy-up-xattr-correctness:
 $\{\lambda s. \text{True}\} \text{smack-inode-copy-up-xattr } s \text{ name } \{\lambda r s. r = -EOPNOTSUPP \vee r = 1\}$ 
apply(unfold smack-inode-copy-up-xattr-def)
apply wpsimp
done

```

```

lemma smack-inode-copy-up-xattr-correctness1:
 $\{\lambda s. \text{name} = \text{XATTR-NAME-SMACK}\} \text{smack-inode-copy-up-xattr } s \text{ name } \{\lambda r s. r = 1\}$ 
apply(unfold smack-inode-copy-up-xattr-def)
apply wpsimp
done

```

```

lemma smack-inode-copy-up-xattr-correctness2:
 $\{\lambda s. \text{name} \neq \text{XATTR-NAME-SMACK}\} \text{smack-inode-copy-up-xattr } s \text{ name } \{\lambda r s. r = -EOPNOTSUPP\}$ 
apply(unfold smack-inode-copy-up-xattr-def)
apply wpsimp
done

```

30.108 correctness lemmas of $\text{smack}_{\text{dentry_create_files_as}}$

```

lemma smack-dentry-create-files-as-correctness:
 $\{\lambda s. \text{True}\} \text{smack-dentry-create-files-as } s \text{ dentry mode' name old new } \{\lambda r s. r = 0\}$ 
apply(unfold smack-dentry-create-files-as-def)
apply wpsimp
done
end

```