

- 1.
2. A general algorithm is as follows:
  - (1) Initially, let  $l = 0$  and  $u = N$  be lower and upper bounds for the set that contains the smallest divisor of  $N$ .
  - (2) Loop: (divide and conquer – bsearch inspiration)
    - i. Let  $m = \lfloor (l + u)/2 \rfloor$ .
    - ii. If there is a divisor  $\leq m$  adjust the upper bound  $u = m$ . Otherwise adjust the lower bound  $l = m$ .
    - iii. Continue until  $u - l = 1$ , the final element is the smallest divisor.

In every loop iteration the set size is cut in half. Since  $N \leq 2^n$  we can have at most  $n$  such iterations until the set has at most one element. The time complexity of the algorithm is thus in  $O(n^4)$ .