

# Pseudocode of ADDT

$\mathbf{x}_0$  is image from training dataset,  $\mathbf{y}$  is the class label of the image,  $\mathbf{C}$  is the classifier,  $P$  is one-step diffusion reverse process and  $\theta$  is it's parameter,  $L$  is CrossEntropy Loss.

Here, we take DDPM for example, The training process is as follows:

- for  $\mathbf{x}_0, \mathbf{y}$  in the training dataset do:
  - $t \sim \text{Uniform}(\{1, \dots, T\})$
  - $\lambda_t = \text{clip}(\gamma_t \lambda_{\text{unit}}, \lambda_{\min}, \lambda_{\max})$ , where  $\gamma_t = \frac{\sqrt{\alpha_t}}{\sqrt{1 - \bar{\alpha}_t}}$
  - $\delta = 0$
  - for 1 to  $\text{ADDT}_{\text{iterations}}$  do:
    - $\epsilon \sim \mathcal{N}(0, I)$
    - $\epsilon_\delta = \text{RBGM}(\delta)$
    - $\mathbf{x}_t = \sqrt{\bar{\alpha}_t} \mathbf{x}_0 + \lambda_t \sqrt{1 - \bar{\alpha}_t} \epsilon + \sqrt{1 - \lambda_t^2} \sqrt{1 - \bar{\alpha}_t} \epsilon_\delta$
    - $\delta+ = \nabla_{\epsilon_\delta} L(\mathbf{C}(P(\mathbf{x}_t, t), \mathbf{y}))$
  - $\epsilon \sim \mathcal{N}(0, I)$
  - $\epsilon_\delta = \text{RBGM}(\delta)$
  - $\mathbf{x}_t = \sqrt{\bar{\alpha}_t} \mathbf{x}_0 + \lambda_t \sqrt{1 - \bar{\alpha}_t} \epsilon + \sqrt{1 - \lambda_t^2} \sqrt{1 - \bar{\alpha}_t} \epsilon_\delta$
  - Take a gradient descent step on:
    - $\nabla_\theta \left\| \frac{\sqrt{\alpha_t}}{\sqrt{1 - \bar{\alpha}_t}} (\mathbf{x}_0 - P(\mathbf{x}_t, t)) \right\|_2^2$

In DDPM, the unet  $\epsilon_\theta$  predicts the Gaussian noise added to the image, adopting equation (3) in the paper, we have  $P(\mathbf{x}_t, t) = (\mathbf{x}_t - \sqrt{1 - \bar{\alpha}_t} \epsilon_\theta(\mathbf{x}_t, t)) / \sqrt{\bar{\alpha}_t}$