

# Supplementary Material for “*Unbiased and Consistent Nested Sampling via Sequential Monte Carlo*”

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## 1. INFERENCE RESULTS

We present posterior expectation and quantile results from 100 runs,  $N = 4 \cdot 10^3$  for TA-SMC and  $N = 10^3$  for NS-SMC for the Factor Analysis and ODE examples.

In brackets we report the ratio of (sample variance  $\times$  average number of evaluations of  $\mathcal{L}$ ) for the associated method to that of TA-SMC with the Random Walk Sampler. Thus, lower values indicate lower work-normalized variance.

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Table 1: Results for FA1 — Part 1 of 2

			$\widehat{\text{mean}}$	$\widehat{\text{lower}}$	$\widehat{\text{upper}}$
$\log \Lambda_{11}$	Gold standard		−0.23	−0.46	0.01
	TA-SMC	RW	−0.23(1.0)	−0.47(1.0)	0.01(1.0)
		MALA	−0.23(0.2)	−0.46(0.3)	0.01(0.4)
		SLICE	−0.23(4.5)	−0.47(1.4)	0.01(2.1)
	NS-SMC	RW	−0.23(1.3)	−0.47(0.5)	0.01(1.1)
		MALA	−0.24(3.7)	−0.47(1.3)	0.01(2.2)
		SLICE	−0.23(3.2)	−0.47(1.2)	0.01(1.7)
$\log \Lambda_{22}$	Gold standard		−0.25	−0.48	−0.00
	TA-SMC	RW	−0.25(1.0)	−0.48(1.0)	−0.00(1.0)
		MALA	−0.25(0.2)	−0.48(0.3)	−0.00(0.2)
		SLICE	−0.25(3.4)	−0.48(1.3)	−0.00(1.3)
	NS-SMC	RW	−0.24(1.3)	−0.48(0.7)	−0.00(0.7)
		MALA	−0.25(1.7)	−0.48(1.0)	−0.01(1.0)
		SLICE	−0.25(4.6)	−0.48(1.2)	−0.00(1.5)
$\log \Lambda_{33}$	Gold standard		−0.43	−0.66	−0.19
	TA-SMC	RW	−0.43(1.0)	−0.66(1.0)	−0.18(1.0)
		MALA	−0.43(0.2)	−0.66(0.3)	−0.18(0.2)
		SLICE	−0.43(3.0)	−0.66(1.6)	−0.18(1.5)
	NS-SMC	RW	−0.43(1.0)	−0.66(0.6)	−0.19(0.6)
		MALA	−0.43(3.7)	−0.66(1.7)	−0.19(1.2)
		SLICE	−0.43(4.0)	−0.66(1.4)	−0.18(1.7)
$\log \Lambda_{44}$	Gold standard		−2.65	−3.51	−2.05
	TA-SMC	RW	−2.65(1.0)	−3.51(1.0)	−2.04(1.0)
		MALA	−2.66(0.1)	−3.52(0.2)	−2.05(0.3)
		SLICE	−2.65(4.4)	−3.51(2.2)	−2.05(2.2)
	NS-SMC	RW	−2.66(1.2)	−3.52(0.9)	−2.05(0.7)
		MALA	−2.66(3.5)	−3.52(2.4)	−2.05(1.3)
		SLICE	−2.65(3.6)	−3.51(2.4)	−2.05(1.4)
$\log \Lambda_{55}$	Gold standard		−1.45	−1.73	−1.17
	TA-SMC	RW	−1.45(1.0)	−1.73(1.0)	−1.16(1.0)
		MALA	−1.45(0.2)	−1.73(0.4)	−1.16(0.3)
		SLICE	−1.45(3.1)	−1.73(1.8)	−1.16(1.9)
	NS-SMC	RW	−1.45(1.2)	−1.73(0.9)	−1.17(0.8)
		MALA	−1.45(2.6)	−1.73(1.7)	−1.16(1.1)
		SLICE	−1.45(3.4)	−1.73(1.9)	−1.16(1.4)
$\log \Lambda_{66}$	Gold standard		−1.44	−1.73	−1.16
	TA-SMC	RW	−1.43(1.0)	−1.72(1.0)	−1.15(1.0)
		MALA	−1.44(0.2)	−1.73(0.4)	−1.15(0.3)
		SLICE	−1.44(4.5)	−1.73(1.5)	−1.15(1.7)
	NS-SMC	RW	−1.44(1.5)	−1.73(1.0)	−1.15(0.8)
		MALA	−1.44(3.6)	−1.73(1.5)	−1.16(1.5)
		SLICE	−1.44(5.3)	−1.72(1.5)	−1.15(1.7)

Table 2: Results for FA1 — Part 2 of 2

			$\widehat{\text{mean}}$	$\widehat{\text{lower}}$	$\widehat{\text{upper}}$
$\log \beta_{11}$	Gold standard		−0.81	−1.24	−0.48
	TA-SMC	RW	−0.81(1.0)	−1.24(1.0)	−0.48(1.0)
		MALA	−0.81(0.2)	−1.23(0.3)	−0.48(0.3)
		SLICE	−0.81(4.1)	−1.23(2.5)	−0.48(2.0)
	NS-SMC	RW	−0.82(1.1)	−1.24(1.2)	−0.48(0.7)
		MALA	−0.81(3.2)	−1.23(2.3)	−0.48(1.3)
		SLICE	−0.81(4.2)	−1.24(2.5)	−0.48(1.3)
$\beta_{21}$	Gold standard		0.46	0.30	0.63
	TA-SMC	RW	0.46(1.0)	0.30(1.0)	0.63(1.0)
		MALA	0.46(0.3)	0.30(0.3)	0.63(0.4)
		SLICE	0.46(3.4)	0.30(1.6)	0.63(2.1)
	NS-SMC	RW	0.46(1.8)	0.30(0.8)	0.63(1.0)
		MALA	0.46(3.6)	0.30(1.1)	0.63(1.5)
		SLICE	0.46(4.5)	0.30(1.3)	0.63(2.3)
$\beta_{31}$	Gold standard		0.59	0.44	0.75
	TA-SMC	RW	0.59(1.0)	0.44(1.0)	0.75(1.0)
		MALA	0.59(0.2)	0.44(0.3)	0.75(0.3)
		SLICE	0.59(4.9)	0.44(2.2)	0.75(2.2)
	NS-SMC	RW	0.59(1.6)	0.44(0.7)	0.75(1.2)
		MALA	0.59(4.1)	0.44(1.2)	0.75(2.0)
		SLICE	0.59(7.3)	0.44(2.0)	0.75(3.2)
$\beta_{41}$	Gold standard		0.97	0.86	1.10
	TA-SMC	RW	0.97(1.0)	0.85(1.0)	1.10(1.0)
		MALA	0.97(0.2)	0.86(0.4)	1.11(0.2)
		SLICE	0.97(5.7)	0.86(2.4)	1.10(1.9)
	NS-SMC	RW	0.97(1.3)	0.86(0.8)	1.10(0.7)
		MALA	0.97(3.2)	0.86(1.4)	1.11(1.3)
		SLICE	0.97(8.4)	0.86(2.9)	1.10(2.5)
$\beta_{51}$	Gold standard		0.88	0.76	1.02
	TA-SMC	RW	0.88(1.0)	0.76(1.0)	1.02(1.0)
		MALA	0.88(0.2)	0.76(0.3)	1.02(0.3)
		SLICE	0.88(6.3)	0.76(2.5)	1.02(1.8)
	NS-SMC	RW	0.88(1.7)	0.76(0.8)	1.02(0.9)
		MALA	0.88(2.7)	0.76(1.2)	1.02(1.6)
		SLICE	0.88(8.4)	0.76(2.4)	1.02(2.7)
$\beta_{61}$	Gold standard		0.88	0.76	1.02
	TA-SMC	RW	0.88(1.0)	0.75(1.0)	1.02(1.0)
		MALA	0.88(0.2)	0.75(0.4)	1.02(0.4)
		SLICE	0.88(5.2)	0.75(2.5)	1.02(2.3)
	NS-SMC	RW	0.88(1.2)	0.75(0.9)	1.02(0.8)
		MALA	0.88(3.3)	0.76(2.0)	1.02(1.4)
		SLICE	0.88(7.6)	0.75(2.7)	1.02(3.3)

Table 3: Results for FA2 — Part 1 of 3

			$\widehat{\text{mean}}$	$\widehat{\text{lower}}$	$\widehat{\text{upper}}$
$\log \Lambda_{11}$	Gold standard		−3.08	−4.41	−1.91
	TA-SMC	RW	−3.05(1.0)	−4.38(1.0)	−1.91(1.0)
		MALA	−3.07(0.3)	−4.39(0.3)	−1.91(0.3)
		SLICE	−2.94(7.4)	−4.10(6.6)	−1.97(13.0)
	NS-SMC	RW	−3.07(0.4)	−4.41(0.4)	−1.90(0.5)
		MALA	−3.05(4.1)	−4.30(3.9)	−1.93(5.6)
		SLICE	−3.03(3.6)	−4.25(3.2)	−1.95(6.6)
$\log \Lambda_{22}$	Gold standard		−2.20	−3.50	−1.70
	TA-SMC	RW	−2.22(1.0)	−3.49(1.0)	−1.70(1.0)
		MALA	−2.21(0.2)	−3.48(0.4)	−1.70(0.3)
		SLICE	−2.29(10.8)	−3.31(5.5)	−1.73(22.6)
	NS-SMC	RW	−2.22(0.4)	−3.53(0.6)	−1.70(0.6)
		MALA	−2.23(3.5)	−3.48(5.1)	−1.71(9.4)
		SLICE	−2.23(3.5)	−3.38(3.9)	−1.72(8.0)
$\log \Lambda_{33}$	Gold standard		−0.48	−0.70	−0.24
	TA-SMC	RW	−0.48(1.0)	−0.71(1.0)	−0.24(1.0)
		MALA	−0.48(0.6)	−0.71(0.4)	−0.24(0.6)
		SLICE	−0.48(56.6)	−0.71(25.3)	−0.23(34.0)
	NS-SMC	RW	−0.48(1.3)	−0.71(1.1)	−0.24(1.4)
		MALA	−0.47(11.7)	−0.70(8.4)	−0.23(7.8)
		SLICE	−0.48(23.0)	−0.70(18.9)	−0.24(18.1)
$\log \Lambda_{44}$	Gold standard		−3.45	−4.49	−2.54
	TA-SMC	RW	−3.44(1.0)	−4.49(1.0)	−2.53(1.0)
		MALA	−3.44(0.3)	−4.47(0.4)	−2.53(0.4)
		SLICE	−3.36(16.6)	−4.26(14.8)	−2.52(22.2)
	NS-SMC	RW	−3.44(0.3)	−4.49(0.5)	−2.54(0.6)
		MALA	−3.45(7.6)	−4.43(9.7)	−2.56(7.3)
		SLICE	−3.41(7.5)	−4.38(8.7)	−2.53(9.3)
$\log \Lambda_{55}$	Gold standard		−1.39	−1.65	−1.13
	TA-SMC	RW	−1.39(1.0)	−1.65(1.0)	−1.12(1.0)
		MALA	−1.39(0.6)	−1.65(0.5)	−1.12(0.6)
		SLICE	−1.40(39.1)	−1.66(23.8)	−1.13(21.2)
	NS-SMC	RW	−1.38(1.4)	−1.64(1.3)	−1.12(1.8)
		MALA	−1.39(8.9)	−1.65(5.9)	−1.13(7.1)
		SLICE	−1.39(16.6)	−1.65(11.2)	−1.13(13.4)
$\log \Lambda_{66}$	Gold standard		−1.37	−1.63	−1.10
	TA-SMC	RW	−1.37(1.0)	−1.63(1.0)	−1.10(1.0)
		MALA	−1.37(0.4)	−1.63(0.3)	−1.11(0.6)
		SLICE	−1.37(28.0)	−1.64(18.6)	−1.11(18.3)
	NS-SMC	RW	−1.37(1.0)	−1.63(1.2)	−1.11(1.3)
		MALA	−1.37(7.1)	−1.63(4.6)	−1.10(7.0)
		SLICE	−1.37(15.2)	−1.63(10.6)	−1.11(14.4)

Table 4: Results for FA2 — Part 2 of 3

			$\widehat{\text{mean}}$	$\widehat{\text{lower}}$	$\widehat{\text{upper}}$
$\log \beta_{11}$	Gold standard		-0.02	-0.15	0.11
		TA-SMC			
		RW	-0.02(1.0)	-0.15(1.0)	0.11(1.0)
	NS-SMC	MALA	-0.02(0.3)	-0.15(0.3)	0.11(0.5)
		SLICE	-0.02(29.2)	-0.14(16.4)	0.11(32.8)
		RW	-0.02(0.7)	-0.15(0.8)	0.11(1.6)
		MALA	-0.02(6.0)	-0.15(7.3)	0.11(7.8)
		SLICE	-0.02(14.0)	-0.14(6.8)	0.11(22.1)
$\beta_{21}$	Gold standard		0.95	0.83	1.09
		TA-SMC			
		RW	0.95(1.0)	0.83(1.0)	1.09(1.0)
	NS-SMC	MALA	0.95(0.4)	0.83(0.4)	1.09(0.4)
		SLICE	0.96(25.3)	0.84(27.1)	1.09(24.3)
		RW	0.95(0.8)	0.83(0.9)	1.09(1.2)
		MALA	0.95(4.9)	0.83(6.1)	1.09(6.3)
		SLICE	0.95(15.6)	0.83(12.5)	1.09(13.5)
$\beta_{31}$	Gold standard		0.45	0.30	0.62
		TA-SMC			
		RW	0.45(1.0)	0.30(1.0)	0.62(1.0)
	NS-SMC	MALA	0.45(0.4)	0.30(0.4)	0.62(0.4)
		SLICE	0.46(28.7)	0.30(26.3)	0.62(24.6)
		RW	0.46(0.8)	0.30(1.0)	0.62(1.2)
		MALA	0.45(8.3)	0.30(6.5)	0.62(7.2)
		SLICE	0.46(20.9)	0.30(14.1)	0.62(18.8)
$\beta_{41}$	Gold standard		0.39	0.23	0.56
		TA-SMC			
		RW	0.39(1.0)	0.23(1.0)	0.56(1.0)
	NS-SMC	MALA	0.39(0.4)	0.23(0.4)	0.56(0.3)
		SLICE	0.40(22.9)	0.23(23.0)	0.56(22.4)
		RW	0.40(0.7)	0.23(1.0)	0.56(0.9)
		MALA	0.39(5.7)	0.23(6.1)	0.56(4.9)
		SLICE	0.39(18.6)	0.24(15.3)	0.56(15.3)
$\beta_{51}$	Gold standard		0.41	0.25	0.58
		TA-SMC			
		RW	0.41(1.0)	0.25(1.0)	0.58(1.0)
	NS-SMC	MALA	0.41(0.4)	0.25(0.5)	0.58(0.3)
		SLICE	0.42(22.6)	0.25(22.3)	0.58(17.6)
		RW	0.41(0.8)	0.25(1.1)	0.58(0.8)
		MALA	0.41(5.3)	0.25(5.3)	0.58(3.2)
		SLICE	0.41(18.6)	0.26(14.4)	0.58(13.0)
$\beta_{61}$	Gold standard		0.41	0.25	0.57
		TA-SMC			
		RW	0.41(1.0)	0.25(1.0)	0.58(1.0)
	NS-SMC	MALA	0.41(0.4)	0.25(0.3)	0.57(0.4)
		SLICE	0.41(25.6)	0.25(22.4)	0.57(27.1)
		RW	0.41(0.6)	0.25(1.0)	0.58(1.0)
		MALA	0.41(5.9)	0.25(6.2)	0.57(5.3)
		SLICE	0.41(19.3)	0.25(14.9)	0.57(19.0)

Table 5: Results for FA2 — Part 3 of 3

			$\widehat{\text{mean}}$	$\widehat{\text{lower}}$	$\widehat{\text{upper}}$
$\log \beta_{22}$	Gold standard		$-3.54$	$-6.34$	$-2.21$
		TA-SMC			
		RW	$-3.57(1.0)$	$-6.06(1.0)$	$-2.23(1.0)$
	NS-SMC	MALA	$-3.53(0.3)$	$-6.17(0.6)$	$-2.22(0.3)$
		SLICE	$-3.46(6.0)$	$-5.15(2.7)$	$-2.26(11.4)$
		RW	$-3.57(0.4)$	$-6.34(1.0)$	$-2.22(0.4)$
		MALA	$-3.50(4.6)$	$-5.49(2.5)$	$-2.26(11.3)$
		SLICE	$-3.49(3.8)$	$-5.39(1.9)$	$-2.25(7.5)$
$\beta_{32}$	Gold standard		$0.25$	$-0.50$	$0.56$
		TA-SMC			
		RW	$0.22(1.0)$	$-0.47(1.0)$	$0.56(1.0)$
	NS-SMC	MALA	$0.25(0.2)$	$-0.49(0.0)$	$0.56(0.2)$
		SLICE	$0.16(3.1)$	$-0.37(6.5)$	$0.54(75.5)$
		RW	$0.22(0.5)$	$-0.49(0.4)$	$0.56(0.5)$
		MALA	$0.23(2.2)$	$-0.42(5.6)$	$0.56(4.1)$
		SLICE	$0.22(1.5)$	$-0.41(4.6)$	$0.56(1.7)$
$\beta_{42}$	Gold standard		$0.55$	$-0.97$	$1.03$
		TA-SMC			
		RW	$0.47(1.0)$	$-0.93(1.0)$	$1.03(1.0)$
	NS-SMC	MALA	$0.54(0.2)$	$-0.96(0.0)$	$1.03(0.2)$
		SLICE	$0.35(3.0)$	$-0.68(7.1)$	$0.99(658.8)$
		RW	$0.47(0.5)$	$-0.95(0.5)$	$1.03(0.3)$
		MALA	$0.49(2.2)$	$-0.80(6.1)$	$1.03(4.3)$
		SLICE	$0.46(1.5)$	$-0.77(5.1)$	$1.03(2.4)$
$\beta_{52}$	Gold standard		$0.46$	$-0.84$	$0.90$
		TA-SMC			
		RW	$0.40(1.0)$	$-0.80(1.0)$	$0.90(1.0)$
	NS-SMC	MALA	$0.46(0.2)$	$-0.83(0.0)$	$0.90(0.2)$
		SLICE	$0.29(3.1)$	$-0.60(7.0)$	$0.86(482.9)$
		RW	$0.40(0.5)$	$-0.82(0.5)$	$0.90(0.7)$
		MALA	$0.42(2.2)$	$-0.69(6.0)$	$0.90(4.9)$
		SLICE	$0.39(1.5)$	$-0.67(5.0)$	$0.90(2.4)$
$\beta_{62}$	Gold standard		$0.46$	$-0.84$	$0.90$
		TA-SMC			
		RW	$0.40(1.0)$	$-0.80(1.0)$	$0.90(1.0)$
	NS-SMC	MALA	$0.46(0.2)$	$-0.83(0.0)$	$0.90(0.2)$
		SLICE	$0.29(3.1)$	$-0.60(7.0)$	$0.86(405.4)$
		RW	$0.39(0.5)$	$-0.82(0.5)$	$0.89(0.5)$
		MALA	$0.41(2.2)$	$-0.69(6.0)$	$0.89(3.5)$
		SLICE	$0.39(1.5)$	$-0.67(5.0)$	$0.90(2.0)$

Table 6: FA3 Inference Results — Part 1 of 4

			$\widehat{\text{mean}}$	$\widehat{\text{lower}}$	$\widehat{\text{upper}}$	
$\log \Lambda_{11}$	Gold standard		-2.89	-4.31	-1.86	
		TA-SMC	RW	-2.89(1.0)	-4.25(1.0)	-1.86(1.0)
			MALA	-2.88(0.1)	-4.28(0.1)	-1.86(0.1)
	SLICE		-2.84(5.0)	-4.14(3.4)	-1.89(11.0)	
	NS-SMC	RW	-2.88(0.4)	-4.30(0.5)	-1.86(0.6)	
		MALA	-2.87(0.9)	-4.28(0.8)	-1.86(1.1)	
		SLICE	-2.87(2.6)	-4.23(2.0)	-1.86(4.0)	
$\log \Lambda_{22}$	Gold standard		-2.38	-3.88	-1.73	
		TA-SMC	RW	-2.38(1.0)	-3.82(1.0)	-1.73(1.0)
			MALA	-2.38(0.1)	-3.84(0.1)	-1.73(0.1)
	SLICE		-2.43(6.8)	-3.71(4.7)	-1.76(10.7)	
	NS-SMC	RW	-2.39(0.5)	-3.85(0.8)	-1.73(0.4)	
		MALA	-2.41(1.1)	-3.84(1.1)	-1.74(1.0)	
		SLICE	-2.40(3.2)	-3.84(3.4)	-1.74(3.9)	
$\log \Lambda_{33}$	Gold standard		-1.08	-3.84	-0.27	
		TA-SMC	RW	-1.15(1.0)	-3.63(1.0)	-0.28(1.0)
			MALA	-1.12(0.1)	-3.81(0.1)	-0.27(0.1)
	SLICE		-1.09(2.3)	-3.21(3.4)	-0.28(4.9)	
	NS-SMC	RW	-1.10(0.4)	-3.75(0.4)	-0.27(0.3)	
		MALA	-1.11(0.6)	-3.63(1.1)	-0.28(1.1)	
		SLICE	-1.11(1.0)	-3.68(1.2)	-0.27(1.0)	
$\log \Lambda_{44}$	Gold standard		-3.17	-4.42	-1.96	
		TA-SMC	RW	-3.19(1.0)	-4.41(1.0)	-2.01(1.0)
			MALA	-3.18(0.1)	-4.41(0.1)	-1.99(0.1)
	SLICE		-3.13(4.9)	-4.28(6.6)	-2.05(4.2)	
	NS-SMC	RW	-3.18(0.5)	-4.42(0.9)	-1.99(0.4)	
		MALA	-3.20(1.0)	-4.43(0.8)	-2.05(2.1)	
		SLICE	-3.16(2.1)	-4.37(4.1)	-2.00(1.8)	
$\log \Lambda_{55}$	Gold standard		-1.77	-3.80	-1.16	
		TA-SMC	RW	-1.77(1.0)	-3.68(1.0)	-1.16(1.0)
			MALA	-1.76(0.1)	-3.74(0.1)	-1.16(0.1)
	SLICE		-1.80(4.6)	-3.40(3.7)	-1.17(6.0)	
	NS-SMC	RW	-1.75(0.4)	-3.69(0.5)	-1.16(0.3)	
		MALA	-1.73(1.6)	-3.35(2.7)	-1.16(2.3)	
		SLICE	-1.77(2.1)	-3.62(2.1)	-1.16(2.1)	
$\log \Lambda_{66}$	Gold standard		-1.75	-3.73	-1.14	
		TA-SMC	RW	-1.74(1.0)	-3.56(1.0)	-1.14(1.0)
			MALA	-1.73(0.1)	-3.64(0.1)	-1.15(0.1)
	SLICE		-1.75(3.9)	-3.28(3.3)	-1.15(5.5)	
	NS-SMC	RW	-1.74(0.5)	-3.64(0.5)	-1.14(0.5)	
		MALA	-1.74(1.7)	-3.47(2.5)	-1.14(1.6)	
		SLICE	-1.74(1.8)	-3.45(2.0)	-1.15(1.7)	

Table 7: Results for FA3 — Part 2 of 4

$\log \beta_{11}$	Gold standard		$\widehat{\text{mean}}$	$\widehat{\text{lower}}$	$\widehat{\text{upper}}$	
			−0.02	−0.16	0.11	
	TA-SMC	RW	−0.02(1.0)	−0.16(1.0)	0.11(1.0)	
		MALA	−0.02(0.1)	−0.16(0.1)	0.11(0.2)	
		SLICE	−0.03(10.7)	−0.16(7.5)	0.10(11.9)	
	NS-SMC	RW	−0.02(1.0)	−0.16(1.3)	0.11(1.4)	
		MALA	−0.02(1.3)	−0.16(1.4)	0.11(1.3)	
		SLICE	−0.03(7.3)	−0.16(6.7)	0.10(8.2)	
$\beta_{21}$	Gold standard		0.96	0.83	1.10	
		TA-SMC	RW	0.96(1.0)	0.83(1.0)	1.09(1.0)
			MALA	0.96(0.1)	0.83(0.2)	1.09(0.2)
	SLICE		0.96(10.2)	0.84(9.2)	1.09(10.5)	
	NS-SMC	RW	0.96(1.0)	0.83(1.4)	1.10(1.6)	
		MALA	0.96(1.0)	0.83(1.4)	1.10(1.2)	
SLICE		0.96(5.4)	0.83(6.6)	1.09(9.6)		
$\beta_{31}$	Gold standard		0.46	0.30	0.63	
		TA-SMC	RW	0.46(1.0)	0.30(1.0)	0.63(1.0)
			MALA	0.46(0.1)	0.30(0.2)	0.63(0.2)
	SLICE		0.46(15.0)	0.30(11.0)	0.62(10.3)	
	NS-SMC	RW	0.46(1.6)	0.30(2.1)	0.63(1.9)	
		MALA	0.46(1.3)	0.30(1.5)	0.63(1.2)	
SLICE		0.46(8.3)	0.30(8.4)	0.62(7.9)		
$\beta_{41}$	Gold standard		0.40	0.23	0.57	
		TA-SMC	RW	0.40(1.0)	0.23(1.0)	0.57(1.0)
			MALA	0.40(0.1)	0.23(0.2)	0.57(0.2)
	SLICE		0.40(16.9)	0.23(17.7)	0.56(12.6)	
	NS-SMC	RW	0.40(1.1)	0.23(1.9)	0.57(1.3)	
		MALA	0.40(1.0)	0.23(1.5)	0.57(1.4)	
SLICE		0.40(8.0)	0.23(13.2)	0.56(7.3)		
$\beta_{51}$	Gold standard		0.42	0.25	0.58	
		TA-SMC	RW	0.42(1.0)	0.25(1.0)	0.58(1.0)
			MALA	0.41(0.1)	0.25(0.2)	0.58(0.2)
	SLICE		0.41(18.3)	0.25(16.2)	0.58(12.3)	
	NS-SMC	RW	0.41(1.5)	0.25(1.9)	0.58(1.5)	
		MALA	0.42(1.1)	0.25(1.2)	0.58(1.7)	
SLICE		0.41(8.3)	0.25(11.8)	0.58(7.7)		
$\beta_{61}$	Gold standard		0.41	0.25	0.58	
		TA-SMC	RW	0.41(1.0)	0.25(1.0)	0.58(1.0)
			MALA	0.41(0.1)	0.25(0.2)	0.58(0.3)
	SLICE		0.41(16.1)	0.25(14.8)	0.58(14.1)	
	NS-SMC	RW	0.41(1.1)	0.25(1.4)	0.58(1.8)	
		MALA	0.41(0.8)	0.25(0.9)	0.58(1.2)	
SLICE		0.41(8.3)	0.25(11.7)	0.58(9.3)		



Table 8: Results for FA3 — Part 3 of 4

			$\widehat{\text{mean}}$	$\widehat{\text{lower}}$	$\widehat{\text{upper}}$
$\log \beta_{22}$	Gold standard		$-3.23$	$-6.06$	$-1.63$
	TA-SMC	RW	$-3.22(1.0)$	$-5.83(1.0)$	$-1.67(1.0)$
		MALA	$-3.23(0.1)$	$-5.99(0.3)$	$-1.65(0.1)$
		SLICE	$-3.20(5.7)$	$-5.42(2.8)$	$-1.73(2.5)$
	NS-SMC	RW	$-3.24(0.6)$	$-6.01(0.8)$	$-1.64(0.6)$
		MALA	$-3.10(2.5)$	$-5.19(2.1)$	$-1.64(1.2)$
		SLICE	$-3.22(1.8)$	$-5.74(2.1)$	$-1.68(1.3)$
$\beta_{32}$	Gold standard		$-0.06$	$-0.83$	$0.58$
	TA-SMC	RW	$-0.06(1.0)$	$-0.79(1.0)$	$0.57(1.0)$
		MALA	$-0.06(0.1)$	$-0.83(0.1)$	$0.59(0.2)$
		SLICE	$-0.06(4.0)$	$-0.69(4.8)$	$0.55(3.5)$
	NS-SMC	RW	$-0.06(0.6)$	$-0.81(0.7)$	$0.58(0.9)$
		MALA	$-0.08(1.2)$	$-0.76(1.8)$	$0.56(1.6)$
		SLICE	$-0.06(1.9)$	$-0.77(2.5)$	$0.56(1.9)$
$\beta_{42}$	Gold standard		$0.23$	$-0.87$	$0.94$
	TA-SMC	RW	$0.23(1.0)$	$-0.82(1.0)$	$0.93(1.0)$
		MALA	$0.24(0.1)$	$-0.86(0.1)$	$0.94(0.1)$
		SLICE	$0.19(5.4)$	$-0.72(6.7)$	$0.88(29.9)$
	NS-SMC	RW	$0.23(0.6)$	$-0.85(0.3)$	$0.94(0.5)$
		MALA	$0.22(1.9)$	$-0.78(2.2)$	$0.92(2.6)$
		SLICE	$0.22(2.1)$	$-0.81(2.2)$	$0.93(4.2)$
$\beta_{52}$	Gold standard		$0.23$	$-0.79$	$0.89$
	TA-SMC	RW	$0.23(1.0)$	$-0.74(1.0)$	$0.87(1.0)$
		MALA	$0.24(0.1)$	$-0.78(0.1)$	$0.88(0.1)$
		SLICE	$0.20(5.7)$	$-0.65(5.7)$	$0.82(15.4)$
	NS-SMC	RW	$0.23(0.7)$	$-0.77(0.3)$	$0.88(0.6)$
		MALA	$0.22(1.9)$	$-0.70(1.9)$	$0.86(2.6)$
		SLICE	$0.22(2.2)$	$-0.74(2.3)$	$0.87(2.9)$
$\beta_{62}$	Gold standard		$0.15$	$-0.81$	$0.86$
	TA-SMC	RW	$0.15(1.0)$	$-0.77(1.0)$	$0.84(1.0)$
		MALA	$0.16(0.1)$	$-0.80(0.1)$	$0.86(0.1)$
		SLICE	$0.12(4.9)$	$-0.70(6.0)$	$0.79(16.8)$
	NS-SMC	RW	$0.15(0.5)$	$-0.80(0.4)$	$0.86(0.5)$
		MALA	$0.13(1.8)$	$-0.74(2.2)$	$0.82(1.9)$
		SLICE	$0.14(1.9)$	$-0.76(1.9)$	$0.84(3.0)$
$\log \beta_{33}$	Gold standard		$-1.21$	$-3.63$	$-0.16$
	TA-SMC	RW	$-1.16(1.0)$	$-3.30(1.0)$	$-0.19(1.0)$
		MALA	$-1.23(0.2)$	$-3.71(0.3)$	$-0.17(0.1)$
		SLICE	$-1.23(6.7)$	$-2.98(2.1)$	$-0.28(4.2)$
	NS-SMC	RW	$-1.22(0.7)$	$-3.69(1.3)$	$-0.18(0.5)$
		MALA	$-1.17(2.8)$	$-3.00(2.5)$	$-0.21(1.6)$
		SLICE	$-1.23(3.8)$	$-3.50(3.4)$	$-0.20(1.6)$

Table 9: Results for FA3 — Part 4 of 4.

			$\widehat{\text{mean}}$	$\widehat{\text{lower}}$	$\widehat{\text{upper}}$
$\beta_{43}$	Gold standard		0.57	−0.54	0.97
	TA-SMC	RW	0.57(1.0)	−0.40(1.0)	0.97(1.0)
		MALA	0.56(0.1)	−0.49(0.1)	0.97(0.1)
		SLICE	0.55(5.6)	−0.24(2.3)	0.96(13.1)
	NS-SMC	RW	0.56(0.5)	−0.50(0.7)	0.97(0.5)
		MALA	0.57(1.7)	−0.35(1.2)	0.97(2.0)
		SLICE	0.57(1.7)	−0.38(1.6)	0.97(2.7)
$\beta_{53}$	Gold standard		0.47	−0.53	0.89
	TA-SMC	RW	0.47(1.0)	−0.45(1.0)	0.89(1.0)
		MALA	0.46(0.1)	−0.52(0.1)	0.89(0.1)
		SLICE	0.44(5.5)	−0.32(3.6)	0.87(6.7)
	NS-SMC	RW	0.46(0.5)	−0.51(0.6)	0.89(0.6)
		MALA	0.47(1.8)	−0.40(1.6)	0.88(2.0)
		SLICE	0.47(1.5)	−0.43(1.7)	0.88(1.9)
$\beta_{63}$	Gold standard		0.53	−0.44	0.90
	TA-SMC	RW	0.53(1.0)	−0.33(1.0)	0.90(1.0)
		MALA	0.51(0.1)	−0.41(0.1)	0.90(0.1)
		SLICE	0.51(6.2)	−0.19(2.6)	0.88(5.5)
	NS-SMC	RW	0.51(0.6)	−0.40(0.8)	0.90(0.6)
		MALA	0.53(1.9)	−0.27(1.4)	0.89(1.3)
		SLICE	0.53(2.1)	−0.30(1.9)	0.90(2.1)

Table 10: Results for ODE model – Part 1 of 2

			$\widehat{\text{mean}}$	$\widehat{\text{lower}}$	$\widehat{\text{upper}}$
$\log k_1$	Gold standard		−3.40	−4.46	−2.71
		TA-SMC			
		RW	−3.33(1.0)	−4.06(1.0)	−2.71(1.0)
	NS-SMC	MALA	−3.18(1.3)	−3.67(0.4)	−2.66(4.2)
		SLICE	−3.36(8.3)	−4.09(6.8)	−2.71(7.3)
		RW	−3.34(4.2)	−4.10(3.4)	−2.71(2.5)
		MALA	−3.36(2.7)	−4.06(1.7)	−2.72(2.0)
$\log V_1$	Gold standard		−0.98	−2.02	0.19
		TA-SMC			
		RW	−1.03(1.0)	−2.02(1.0)	0.04(1.0)
	NS-SMC	MALA	−1.09(3.2)	−2.03(4.2)	−0.09(2.2)
		SLICE	−1.00(6.7)	−1.98(12.0)	0.00(6.8)
		RW	−1.03(1.7)	−2.03(2.9)	0.06(2.4)
		MALA	−0.96(1.3)	−1.95(3.9)	0.15(1.4)
$\log K_{m1}$	Gold standard		−1.01	−4.12	1.04
		TA-SMC			
		RW	−0.98(1.0)	−3.69(1.0)	0.95(1.0)
	NS-SMC	MALA	−1.00(3.2)	−3.57(2.0)	0.79(2.2)
		SLICE	−0.98(6.8)	−3.56(4.7)	0.93(4.3)
		RW	−0.96(2.2)	−3.62(2.9)	0.95(2.6)
		MALA	−0.90(2.8)	−3.43(2.0)	0.94(2.2)
$\log K_{m2}$	Gold standard		−2.86	−4.38	−1.79
		TA-SMC			
		RW	−2.77(1.0)	−3.92(1.0)	−1.81(1.0)
	NS-SMC	MALA	−2.58(1.9)	−3.46(1.0)	−1.76(3.2)
		SLICE	−2.80(7.0)	−3.93(4.8)	−1.82(5.6)
		RW	−2.79(3.9)	−3.97(3.3)	−1.81(2.3)
		MALA	−2.81(2.1)	−3.93(1.4)	−1.81(1.6)
$\log V_2$	Gold standard		−2.05	−2.64	−1.07
		TA-SMC			
		RW	−2.11(1.0)	−2.65(1.0)	−1.47(1.0)
	NS-SMC	MALA	−2.24(1.1)	−2.70(4.7)	−1.82(0.3)
		SLICE	−2.09(9.0)	−2.64(8.8)	−1.43(6.6)
		RW	−2.10(4.6)	−2.65(2.7)	−1.42(3.3)
		MALA	−2.09(3.0)	−2.64(2.2)	−1.46(1.6)
$\log V_2$	Gold standard		−2.10(10.4)	−2.65(8.0)	−1.52(4.4)
		TA-SMC			
		RW	−2.11(1.0)	−2.65(1.0)	−1.47(1.0)
	NS-SMC	MALA	−2.24(1.1)	−2.70(4.7)	−1.82(0.3)
		SLICE	−2.09(9.0)	−2.64(8.8)	−1.43(6.6)
		RW	−2.10(4.6)	−2.65(2.7)	−1.42(3.3)
		MALA	−2.09(3.0)	−2.64(2.2)	−1.46(1.6)
		SLICE	−2.10(10.4)	−2.65(8.0)	−1.52(4.4)

Table 11: Results for ODE model – Part 2 of 2

			$\widehat{\text{mean}}$	$\widehat{\text{lower}}$	$\widehat{\text{upper}}$
$\log S(0)$	Gold standard		−0.23	−1.24	0.61
		TA-SMC			
		RW	−0.22(1.0)	−1.18(1.0)	0.59(1.0)
	NS-SMC	MALA	−0.24(3.0)	−1.15(2.9)	0.56(2.6)
		SLICE	−0.23(7.8)	−1.14(10.0)	0.56(9.5)
		RW	−0.21(1.6)	−1.17(2.5)	0.61(1.6)
		MALA	−0.26(1.6)	−1.22(2.3)	0.55(2.8)
$\log D(0)$	Gold standard		−2.88	−6.05	−1.02
		TA-SMC			
		RW	−2.85(1.0)	−5.76(1.0)	−1.01(1.0)
	NS-SMC	MALA	−2.85(2.5)	−5.49(1.2)	−1.06(4.4)
		SLICE	−2.84(6.0)	−5.53(5.3)	−1.04(14.5)
		RW	−2.89(2.7)	−5.84(3.3)	−1.02(5.0)
		MALA	−2.90(1.1)	−5.75(1.0)	−1.02(2.1)
$\log R(0)$	Gold standard		0.31	−0.28	0.83
		TA-SMC			
		RW	0.30(1.0)	−0.24(1.0)	0.80(1.0)
	NS-SMC	MALA	0.30(2.1)	−0.22(1.7)	0.77(2.2)
		SLICE	0.31(7.2)	−0.21(5.3)	0.79(8.2)
		RW	0.31(1.9)	−0.24(2.6)	0.81(2.6)
		MALA	0.32(2.1)	−0.20(1.9)	0.82(2.4)
$\log R_{pp}(0)$	Gold standard		−4.17	−6.89	−2.90
		TA-SMC			
		RW	−4.14(1.0)	−6.60(1.0)	−2.91(1.0)
	NS-SMC	MALA	−4.09(1.1)	−6.25(0.9)	−2.93(3.7)
		SLICE	−4.14(4.3)	−6.32(2.6)	−2.93(6.6)
		RW	−4.19(6.9)	−6.50(2.1)	−2.93(2.8)
		MALA	−4.15(1.6)	−6.40(1.0)	−2.93(2.3)
$\log R_{pp}(0)$	Gold standard		−4.10	−6.27	−2.92
		TA-SMC			
		RW	−4.10(2.8)	−6.27(2.3)	−2.92(3.9)
	NS-SMC	MALA	−4.10(2.8)	−6.27(2.3)	−2.92(3.9)
		SLICE	−4.10(2.8)	−6.27(2.3)	−2.92(3.9)
		RW	−4.10(2.8)	−6.27(2.3)	−2.92(3.9)
		MALA	−4.10(2.8)	−6.27(2.3)	−2.92(3.9)

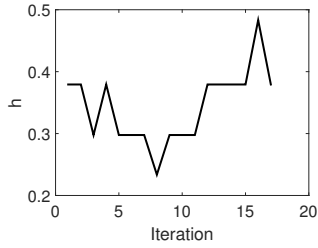
## 2. CALIBRATION PLOTS

The following plots display the evolution of the automated choice of MCMC kernel parameters  $h$  (for RW/MALA) and  $w$  (for Slice Sampling), as well as the evolution of the choice of MCMC iterations (repeats) chosen by the Calibration methods described in Section 5 of the paper. We use a range of twenty possible values for  $h$  that are logarithmically spaced on the interval  $[0.01,1]$ , and ten possible values for  $w$  that are linearly spaced on the interval  $[0.02,2]$ .

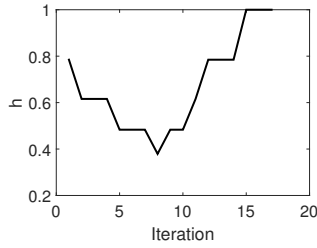
Note here that iteration on the  $x$ -axis refers not to MCMC iteration, but instead the time step of the SMC sampler.

## 2.1 Factor Analysis – One Factor

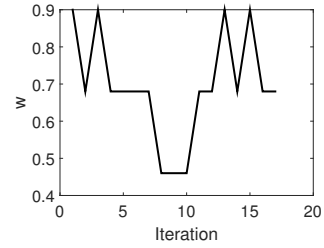
### MCMC Parameters



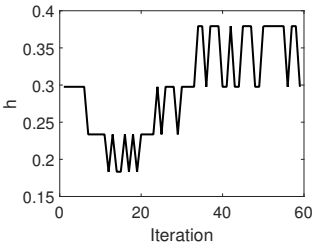
(a) TA-SMC RW



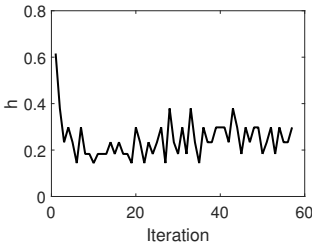
(b) TA-SMC MALA



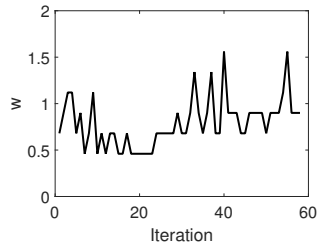
(c) TA-SMC SLICE



(d) NS-SMC RW

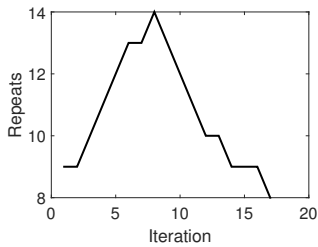


(e) NS-SMC MALA

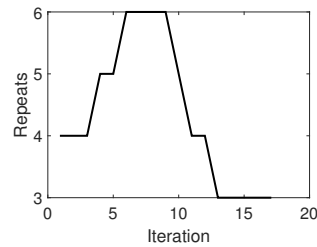


(f) NS-SMC SLICE

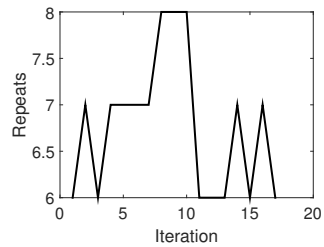
### MCMC Repeats



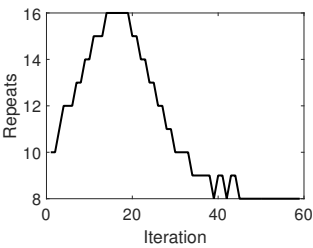
(g) TA-SMC RW



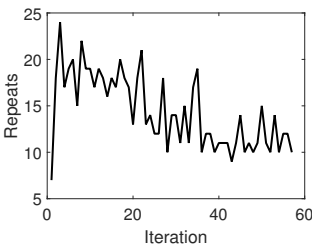
(h) TA-SMC MALA



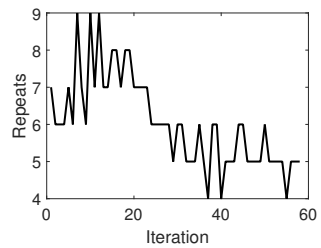
(i) TA-SMC SLICE



(j) NS-SMC RW



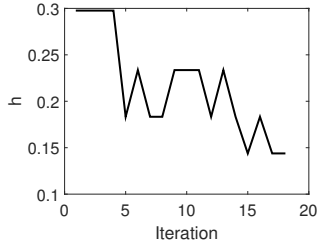
(k) NS-SMC MALA



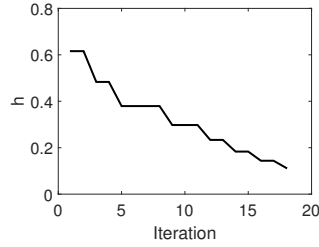
(l) NS-SMC SLICE

## 2.2 Factor Analysis – Two Factors

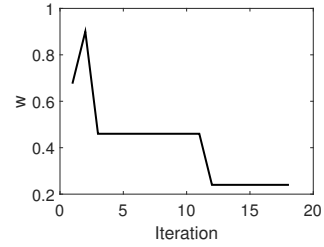
### MCMC Parameters



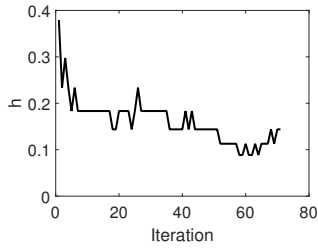
(a) TA-SMC RW



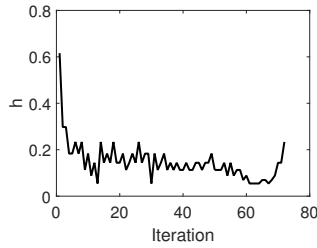
(b) TA-SMC MALA



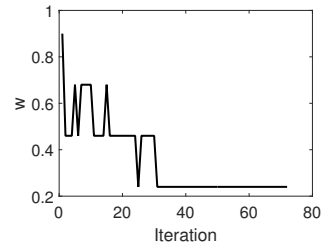
(c) TA-SMC SLICE



(d) NS-SMC RW

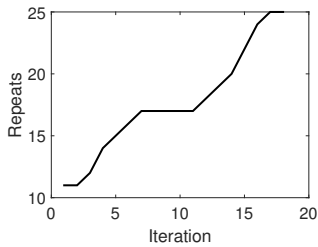


(e) NS-SMC MALA

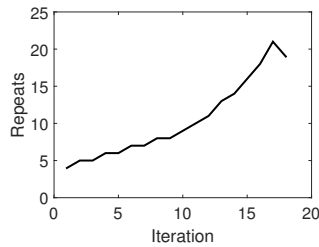


(f) NS-SMC SLICE

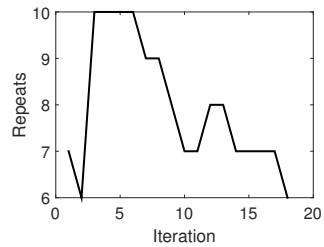
### MCMC Repeats



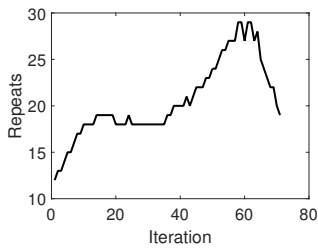
(g) TA-SMC RW



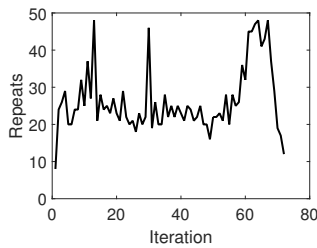
(h) TA-SMC MALA



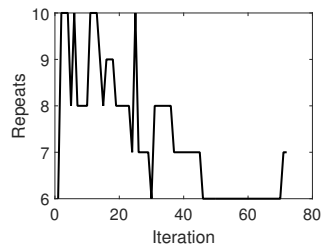
(i) TA-SMC SLICE



(j) NS-SMC RW



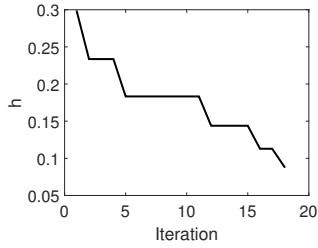
(k) NS-SMC MALA



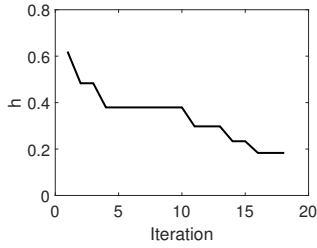
(l) NS-SMC SLICE

## 2.3 Factor Analysis – Three Factors

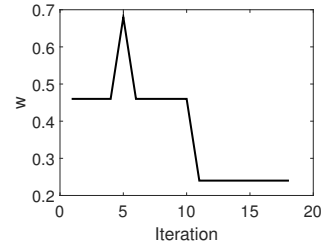
### MCMC Parameters



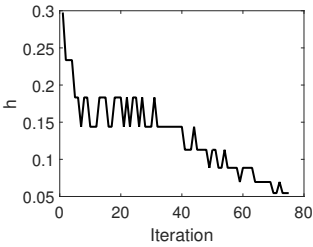
(a) TA-SMC RW



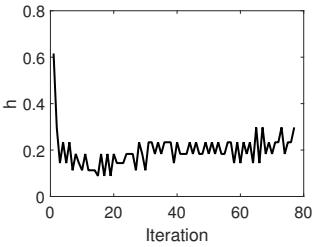
(b) TA-SMC MALA



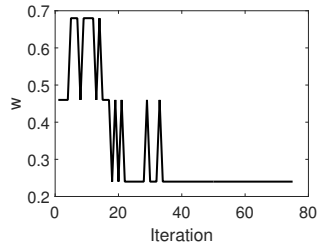
(c) TA-SMC SLICE



(d) NS-SMC RW

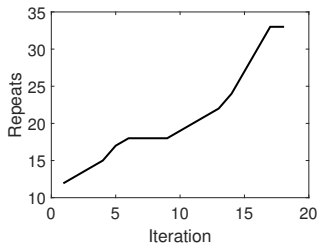


(e) NS-SMC MALA

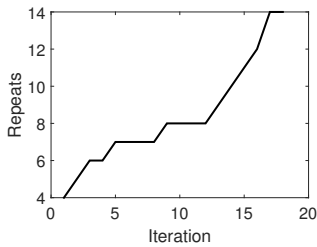


(f) NS-SMC SLICE

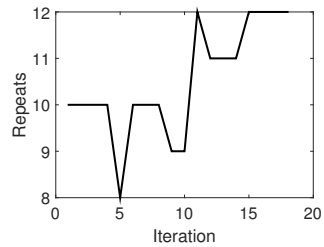
### MCMC Repeats



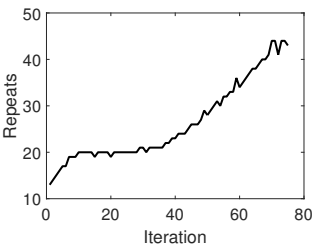
(g) TA-SMC RW



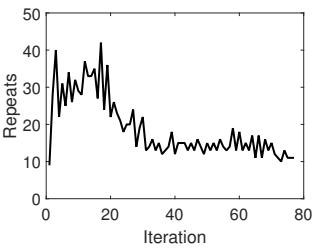
(h) TA-SMC MALA



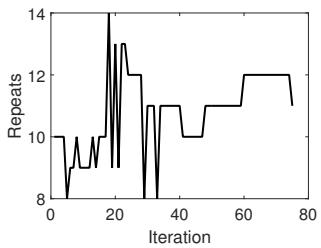
(i) TA-SMC SLICE



(j) NS-SMC RW



(k) NS-SMC MALA

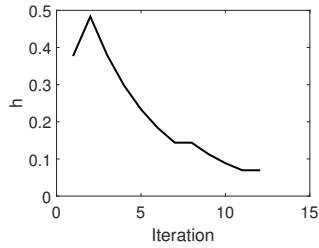


(l) NS-SMC SLICE

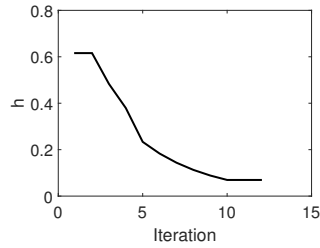


## 2.4 ODE

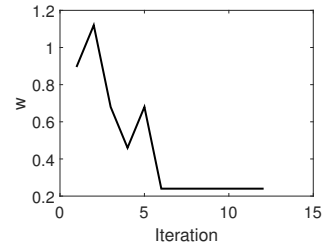
### MCMC Parameters



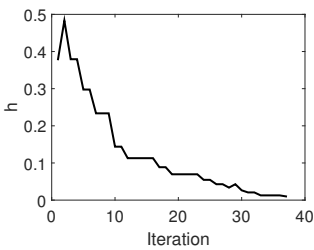
(a) TA-SMC RW



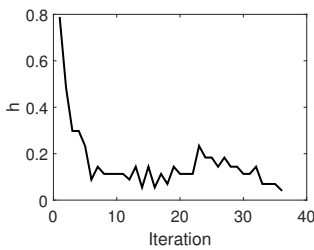
(b) TA-SMC MALA



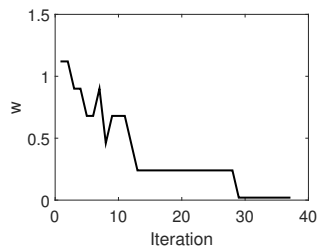
(c) TA-SMC SLICE



(d) NS-SMC RW

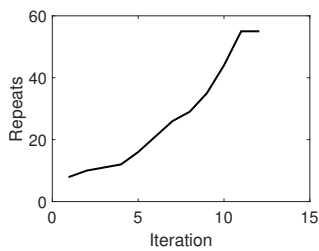


(e) NS-SMC MALA

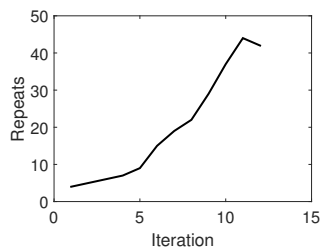


(f) NS-SMC SLICE

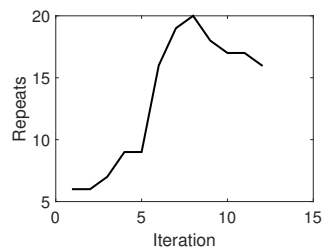
### MCMC Repeats



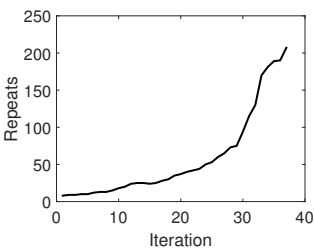
(g) TA-SMC RW



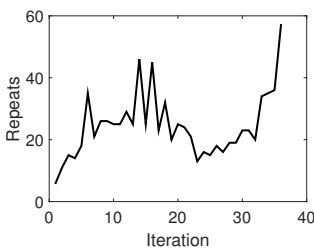
(h) TA-SMC MALA



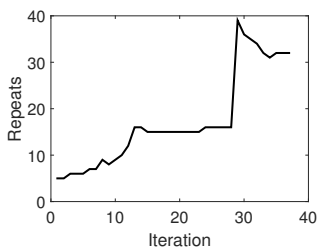
(i) TA-SMC SLICE



(j) NS-SMC RW



(k) NS-SMC MALA



(l) NS-SMC SLICE