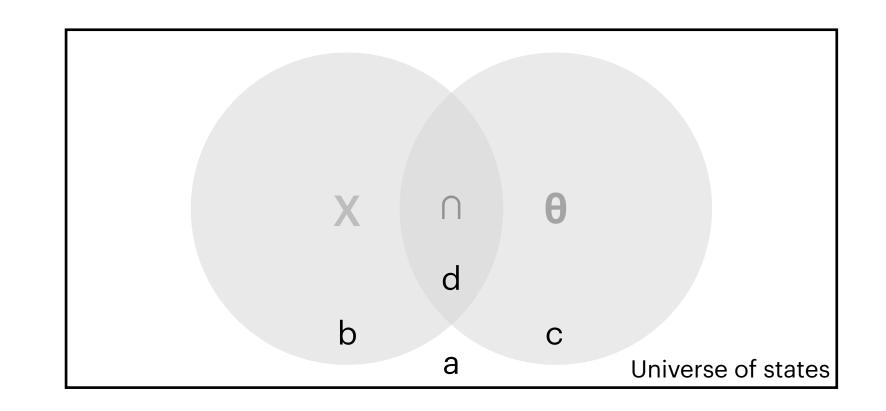
Bayes' Rule

• Intuitive statement: $P(x | \theta)P(\theta) = P(\theta | x)P(x)$

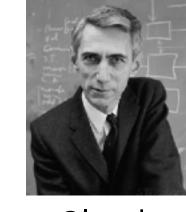
• Proof
$$\frac{d}{c} \cdot \frac{c}{a} = \frac{d}{b} \cdot \frac{b}{a} = \frac{d}{a}$$



• Bayes' Rule follows by deduction: $P(\theta|x) = \frac{P(x|\theta)P(\theta)}{P(x)}$ $posterior = \frac{likelihood \times prior}{evidence}$

• Prescription for how to update a model given new evidence (i.e., new data)

Similarity measures between distributions



Claude Shannon

- Shannon postulated that any measure of the informativeness of an event,
 x, should satisfy three conditions:
 - 1. An event with probability 1 yields no information
 - 2. The probability of an event and the information it yields vary inversely with each other
 - 3. The total information coming from independent events is purely additive
 - Which he used to define self-information: $I(x) = -\log P(x)$

• Shannon entropy: $H(P) = \mathbb{E}_{x \sim P}[I(x)] = -\mathbb{E}_{x \sim P}[\log P(x)]$

• Kullback-Leibler (KL) divergence: $D_{KL}(P | | Q) = \mathbb{E}_{x \sim P} \left| \log \frac{P(x)}{Q(x)} \right|$

• Cross entropy: $H(P,Q) = H(P) + D_{KL}(P | Q) = -\mathbb{E}_{x \sim P}[\log Q(x)]$