Regression Subset Selection in R

For linear regression: lm() from stats package (built-in) For logistic regression: glm() from stats package For lasso and ridge regression: glmnet() from glmnet package

Load packages

```
library(glmnet)
library(QuantPsyc) # for standardized regression coefficients
library(subselect)
#library(lars)
library(tabuSearch)
```

Additionally

```
library(lavaan) # for HolzingerSwineford1939 dataset
HS <- HolzingerSwineford1939

library(elasticnet) # regularized PCA
#library(fanc) # regularized FA
#library(FAiR) # semi-exploratory factor analysis; only works on Windows
library(GA) # genetic algorithm for subset selection</pre>
```

http://www.jstatsoft.org/v53/i04/paper

You can also embed plots, for example:

```
data(diabetes)
X <- diabetes$x
Y <- diabetes$y</pre>
```

```
lm(Y ~ X)
# note: equivalent to
lm(y ~ x,data=diabetes)
# which is equivalent to
lm(diabetes$y ~ diabetes$x)
```

Note, in this dataset, x is essentially a matrix within a dataframe. This is a little unusual, where the typical format would be:

```
diabetes2 <- data.frame(cbind(Y,X))
head(diabetes2)</pre>
```

```
## 1 151 0.038075906 0.05068012 0.06169621 0.021872355 -0.044223498
## 2 75 -0.001882017 -0.04464164 -0.05147406 -0.026327835 -0.008448724
## 3 141 0.085298906 0.05068012 0.04445121 -0.005670611 -0.045599451
## 4 206 -0.089062939 -0.04464164 -0.01159501 -0.036656447 0.012190569
## 5 135 0.005383060 -0.04464164 -0.03638469 0.021872355 0.003934852
## 6 97 -0.092695478 -0.04464164 -0.04069594 -0.019442093 -0.068990650
```

```
##
                          hdl
                                       tch
                                                    ltg
## 1 -0.03482076 -0.043400846 -0.002592262 0.019908421 -0.017646125
## 2 -0.01916334 0.074411564 -0.039493383 -0.068329744 -0.092204050
## 3 -0.03419447 -0.032355932 -0.002592262 0.002863771 -0.025930339
## 4 0.02499059 -0.036037570 0.034308859 0.022692023 -0.009361911
## 5 0.01559614 0.008142084 -0.002592262 -0.031991445 -0.046640874
## 6 -0.07928784 0.041276824 -0.076394504 -0.041180385 -0.096346157
lm(Y ~ ., data=diabetes2)
##
## Call:
## lm(formula = Y ~ ., data = diabetes2)
## Coefficients:
## (Intercept)
                        age
                                     sex
                                                  bmi
                                                               map
##
       152.13
                     -10.01
                                 -239.82
                                               519.84
                                                            324.39
##
                        ldl
                                     hdl
                                                  tch
                                                               ltg
            tc
       -792.18
##
                     476.75
                                  101.04
                                               177.06
                                                            751.28
##
           glu
##
         67.63
```

Using the "." means we want to use all variables that aren't the outcome as predictors Fun Fact: Can do the same thing with a SEM package

```
library(lavaan)
lm.mod <-'
Y ~ age + sex + bmi + map + tc + ldl + hdl + tch + ltg + glu
Y ~ 1 # intercept
'
lm.sem <- sem(lm.mod,diabetes2)
#summary(lm.sem)
#parameterEstimates(lm.sem)
coef(lm.sem)</pre>
```

```
##
      Y~age
               Y~sex
                        Y~bmi
                                 Y~map
                                           Y~tc
                                                   Y~ldl
                                                            Y~hdl
                                                                     Y~tch
##
   -10.012 -239.819
                     519.840
                               324.390 -792.184 476.746 101.045 177.064
##
      Y~ltg
               Y~glu
                          Y~1
   751.279
              67.625 152.133 2859.690
```

Exact same answer.

```
lm.out <- lm(y ~ x,data=diabetes)
#summary(lm.out)

# check assumptions
#plot(lm.out)

# get standardized coefficients
lm.beta(lm.out) # from QuantPsyc</pre>
```

```
##
                                      xbmi
                                                   xmap
                                                                  xtc
           xage
                        xsex
## -0.006178065 -0.147981279
                              0.320769113
                                            0.200166344 -0.488820243
                                                   xltg
##
           xldl
                        xhdl
                                      xtch
                                                                 xglu
   0.294177828
                0.062349936
                              0.109258122
                                            0.463579756
                                                         0.041728501
##
```

So we are doing pretty good, R^2 of 0.51, with only four significant predictors. So the question we are going to answer today is whether we can get rid of a few predictors and still do a good job of predicting the outcome. Now, there are two + reasons to do this:

- 1. In future studies, maybe time is of the essence, or each additional question costs a certain amount of money. By reducing the number of questions we have to ask participants, both money and time can be saved. The question is what is the tradeoff, can we reduce the number of scales/items/questionnaires, and still answer the questions we want?
- 2. Remember when using R^2 as a criterion, by using more variables as predictors, these can only improve are within sample predictive power. But when we become concerned with generalizability, then in some cases, a reduced number of predictors, only important ones, can generalize better than a larger set of X's. This was somewhat demonstrated in the "preprocessing" lab.

Let's try #2 on the diabetes dataset

```
ids <- sample(1:nrow(diabetes2), .5*nrow(diabetes2),replace=FALSE)
diab.train <- diabetes2[ids,]
diab.test <- diabetes2[-ids,]

lm.trainFull <- lm(Y ~ ., data= diab.train)
summary(lm.trainFull)$r.squared

## [1] 0.5030062

lm.trainSub <- lm(Y ~ sex + bmi + map + ltg, data= diab.train)
summary(lm.trainSub)$r.squared

## [1] 0.4580293

pred.full <- predict(lm.trainFull,diab.test)
pred.sub <- predict(lm.trainSub,diab.test)

cor(pred.full,diab.test$Y)**2

## [1] 0.510087</pre>
```

```
## [1] 0.508507
```

cor(pred.sub,diab.test\$Y)**2

Not in this case, but let's try some different methods specifically designed for subset selection.

Subset Selection

First off, why don't we just try out all combination of predictors – entering them all separately into lm()? Problems:

- 1. How do we choose. R^2 can only go up with added predictors (RSS can only go down).
- 2. This is usually computationally infeasible, as there are 2^p possible models, where p is the number of predictors. In our case $2^{10} = 1024$, which is a lot but not too many.

Stepwise Selection

Forward

Efficient, but not guaranteed to find best overall model.

stepFor\$anova

```
## Stepwise Model Path
## Analysis of Deviance Table
## Initial Model:
## Y ~ 1
##
## Final Model:
## Y ~ bmi + ltg + map + hdl + sex + glu
##
##
##
                Deviance Resid. Df Resid. Dev
                                                   AIC
      Step Df
## 1
                               220 1300670.2 1920.330
                                    906165.5 1842.458
## 2 + bmi 1 394504.687
                               219
## 3 + ltg
           1 143555.736
                               218
                                     762609.7 1806.341
## 4 + map 1 50917.121
                               217
                                     711692.6 1793.070
## 5 + hdl
           1 16872.125
                               216
                                     694820.5 1789.767
## 6 + sex 1
                                     668056.7 1783.086
              26763.827
                               215
               7194.799
                                     660861.9 1782.693
## 7 + glu 1
                               214
```

```
pred.for<- predict(stepFor,diab.test)
cor(pred.for,diab.test$Y)**2</pre>
```

```
## [1] 0.5192895
```

AIC (Akaike Information Criterion) induces a penalty for complexity – meaning that it will try and choose a model that balances predictive accuracy with simplicity (less predictors).

Backward

```
library(MASS)
stepBack <- stepAIC(lmFULL,direction="backward")</pre>
stepBack$anova
## Stepwise Model Path
## Analysis of Deviance Table
##
## Initial Model:
## Y \sim age + sex + bmi + map + tc + ldl + hdl + tch + ltg + glu
##
## Final Model:
## Y ~ sex + bmi + map + tc + ldl + ltg + glu
##
##
                 Deviance Resid. Df Resid. Dev
      Step Df
## 1
                                 210
                                       646425.0 1785.812
## 2 - tch 1
                 5.878708
                                 211
                                       646430.8 1783.814
## 3 - age 1
                65.659495
                                 212
                                       646496.5 1781.836
## 4 - hdl 1 1687.132174
                                 213
                                       648183.6 1780.412
```

```
## [1] 0.5171596
```

Ridge and Lasso Regression

cor(pred.back,diab.test\$Y)**2

pred.back<- predict(stepBack,diab.test)</pre>

• Including a penalty on the β parameters, and by varying the penalty we can shrink some of the β 's to zero, doing a form of "automatic" subset selection.

Althought there a number of packages to do this, maybe the best is glmnet

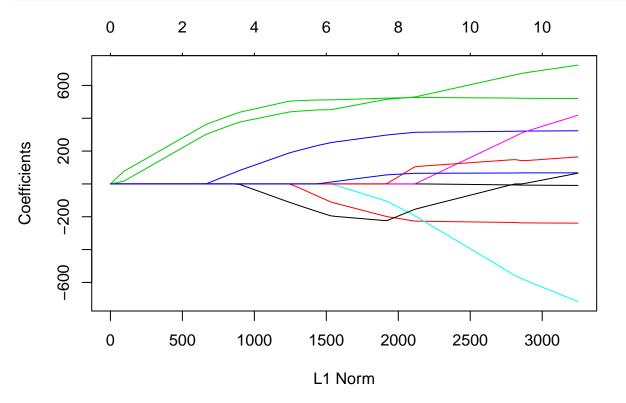
Note, for glmnet, your data has to be set up in two separate matrices. Doing this can be accomplished by:

```
YY <- as.matrix(diabetes2$Y)
XX <- as.matrix(diabetes2[,2:11])
# or
XX <- as.matrix(diabetes2[,c("age","sex","bmi","map","tc","ldl","hdl","tch","ltg","glu")])</pre>
```

Two things to note: 1. Because we are doing regression with a continuous outcome, we specify the family(distribution) as "gaussian" 2. Shrinkage in lasso and ridge is sensitive to the scale of the variables, therefore, it is best to standardize the predictors before entering. glmnet does this by default (look at ?glmnet).

Lasso

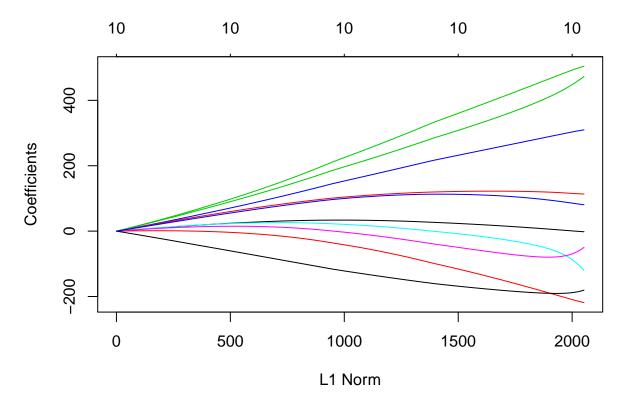
```
?glmnet
lasso.out <- glmnet(XX,YY,family="gaussian",alpha=1)
plot(lasso.out)</pre>
```



#gaussian for continuous outcomes, "binomial" for categorical
alpha=1 is lasso, alpha=0 is ridge

Ridge

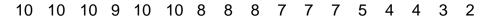
```
ridge.out <- glmnet(XX,YY,family="gaussian",alpha=0)
#plot(ridge.out,type.coef="2norm")
plot(ridge.out)</pre>
```

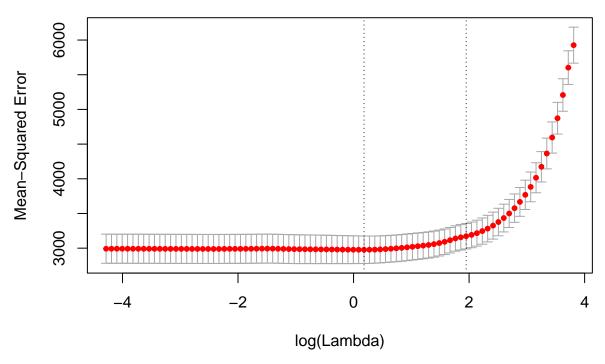


Since ridge regression does not shrink the β coefficients to 0 with increase penalization, it does not do an "automatic" form of subset selection

The problem now becomes, which value of λ (amount of shrinkage) do we choose? Using cross-validation is one of the better ways, and is implemented the glmnet package

```
cv.lasso <- cv.glmnet(XX,YY,family="gaussian",alpha=1)
plot(cv.lasso)</pre>
```





Two-strategies for selecting λ : either pick the lowest CV error, or the best solution within 1 standard error. I don't think that there is a clear best choice. The one advantage of using the 1SE rule is that you need fewer predictors. In our example 4 instead of 7.

```
#str(cv.lasso)
(lmin <- cv.lasso$lambda.min)</pre>
## [1] 1.19949
(lminSE <- cv.lasso$lambda.1se)</pre>
## [1] 7.025438
lasso.out2 = glmnet(XX,YY,family="gaussian",alpha=1,lambda=lminSE)
lasso.out2
##
## Call: glmnet(x = XX, y = YY, family = "gaussian", alpha = 1, lambda = lminSE)
##
##
        Df
              %Dev Lambda
## [1,] 4 0.4753 7.025
Note that Df correspond to the number of non-zero \beta's
So how are we doing?
```

?predict.glmnet

cor(pred.1se,YY)**2

pred.1se <- predict(lasso.out2,XX)</pre>

```
## [,1]
## s0 0.4891983
```

So with only 4 predictors entered into the model, we only lose 2-3% of our predicted variance (R^2). With the lasso, there are two recommended strategies for using the results. 1. Taking the predictors with non-zero $\beta's$, and just using that subset in linear regression. 2. Or, bypass this all together and use least angle regression.

"One approach for reducing this bias is to run the lasso to identify the set of non-zero coefficients, and then fit an un-restricted linear model to the selected set of features." p. 91 Hastie et al., 2009

In our case, we will take the predictors with non-zero $\beta's$ and use them with lm() to get our final model. This will probably be our most realistic estimate of R^2 when caring about generalization, as we are using the test dataset to derive the estimate.

```
coef(lasso.out2)
```

```
## 11 x 1 sparse Matrix of class "dgCMatrix"
##
## (Intercept) 152.1335
## age
## sex
## bmi
                 498.9887
                 180.6668
## map
## tc
## ldl
## hdl
                -103.2937
## tch
                 433.5503
## ltg
## glu
lm.lasso <- lm(Y ~ bmi + map + hdl + ltg,diab.train)</pre>
lmLas.pred <- predict(lm.lasso,diab.test)</pre>
```

```
## [1] 0.5102243
```

Try Elastic Net - from caret

cor(lmLas.pred,diab.test\$Y)**2

This optimizes both the λ and mixing percentage

```
library(caret)
XX <- as.matrix(diab.train[,-1])
YY <- diab.train$Y # important to change class of variable
enet.out <- train(XX,YY,method="glmnet",tuneLength=8)

row.result <- best(enet.out$results,"Rsquared",maximize=T)
enet.out$results[row.result,]</pre>
```

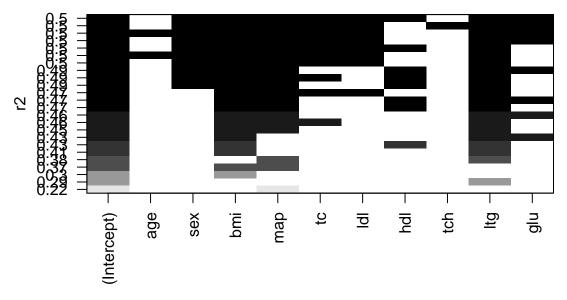
Stochastic Search

Use 3 packages: "tabuSearch" "leaps" "GA" (genetic algorithm, note there is also "genalg")

```
library(leaps)
```

```
##
## Attaching package: 'leaps'
##
## The following object is masked from 'package:subselect':
##
## leaps

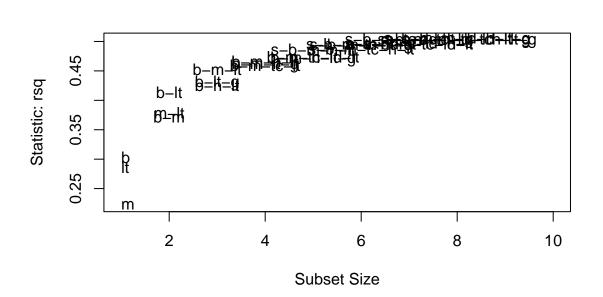
# leaps
# leaps <- regsubsets(Y ~.,,data=diab.train,nbest=3)
#summary(leaps)
# plot a table of models showing variables in each model.
# models are ordered by the selection statistic.
plot(leaps,scale="r2")</pre>
```



plot statistic by subset size library(car)

```
##
## Attaching package: 'car'
##
## The following object is masked from 'package:boot':
##
## logit

subsets(leaps, statistic="rsq",legend=F)
```



```
##
       Abbreviation
## age
## sex
                    S
                    b
## bmi
## map
                   m
## tc
                   tc
## ldl
                  ld
## hdl
                   h
## tch
                 tch
## ltg
                  lt
## glu
                    g
```

have to press ESC to exit

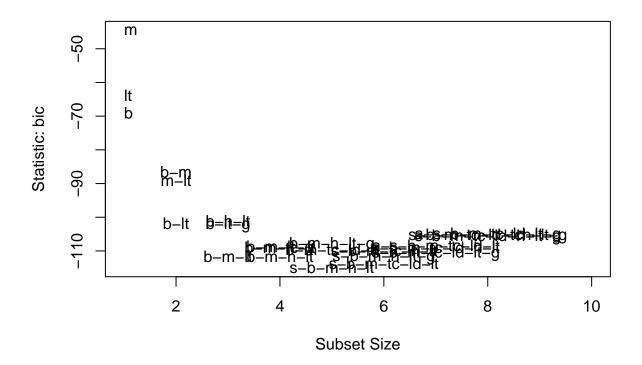
Based on this, looks like a subset size of 5 might be best, as we get pretty close to an R^2 of 0.5

Maybe R^2 isn't the best, as this doesn't penalize for complexity and will probably not generalize well. In regsubsets() we can use BIC which may help.

summary(leaps)\$bic

```
## [1] -69.07594 -63.82772 -44.68232 -101.79487 -89.03482 -86.47742
## [7] -111.66788 -102.34958 -101.00919 -111.57207 -109.11731 -108.98023
## [13] -114.85491 -109.53601 -108.13102 -113.72715 -111.84977 -109.87648
## [19] -110.73256 -108.88665 -108.35441 -105.91037 -105.50404 -105.34391

subsets(leaps, statistic="bic",legend=F)
```



```
##
       Abbreviation
## age
## sex
                    s
## bmi
                    b
## map
                    m
                   tc
## ldl
                   ld
## hdl
                    h
## tch
                  tch
## ltg
                   lt
## glu
                    g
```

Looks like we get a similar answer, but seem to also have a "clearer" best model The

Genetic Algorithm

An example using the "GA" package to do this: http://www.jstatsoft.org/v53/i04/paper But there is an easier way:

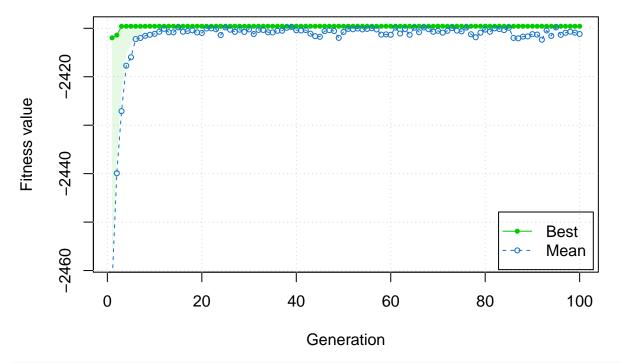
```
library(glmulti)

## Loading required package: rJava

Using "GA"

mod <- lm(Y ~ ., diab.train)

x <- model.matrix(mod)[, -1]
y <- model.response(model.frame(mod))</pre>
```



summary(GA)

```
Genetic Algorithm
##
## GA settings:
## Type
                            binary
## Population size
                            50
## Number of generations = 100
## Elitism
## Crossover probability = 0.8
## Mutation probability = 0.1
##
## GA results:
## Iterations
## Fitness function value = -2409.583
##
       age sex bmi map tc ldl hdl tch ltg glu
```

```
summary(GA)$solution
```

```
## age sex bmi map tc ldl hdl tch ltg glu
## [1,] 0 1 1 1 1 1 0 0 1 1
```

Tabu Search

An example: http://www.r-bloggers.com/finding-the-best-subset-of-a-gam-using-tabu-search-and-visualizing-it-in-r/

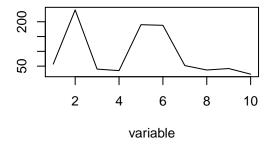
```
library(tabuSearch)
mod <- lm(Y ~ ., diab.train)

x <- model.matrix(mod)[, -1]
y <- model.response(model.frame(mod))

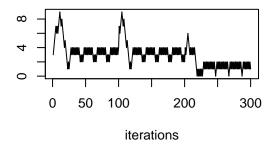
fitness2 <- function(string) {
  inc <- which(string == 1)
  X <- cbind(1, x[,inc])
  mod <- lm.fit(X, y)
  class(mod) <- "lm"
  -AIC(mod) + 100000 # won't take negative
}

result <- tabuSearch(size = 10, iters = 100,objFunc = fitness2)
plot(result) #fit margins too large</pre>
```

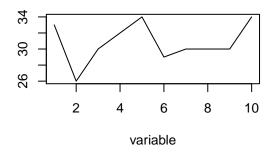
No of times selected



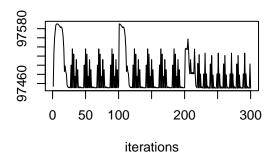
Sum of included variables



Most frequent moves



Objective Function



```
summary(result,verbose=T) # 6 predictors
```

```
## Tabu Settings
                                             = binary configuration
##
    Type
##
    No of algorithm repeats
##
    No of iterations at each prelim search
                                             = 100
    Total no of iterations
                                             = 300
##
    No of unique best configurations
                                             = 55
    Tabu list size
                                             = 9
##
    Configuration length
                                             = 10
    No of neighbours visited at each iteration = 10
##
## Results:
    Highest value of objective fn = 97590.41675
    Occurs # of times
##
##
   Optimum number of variables
                                 = c(7, 7)
## Optimum configuration:
       [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8] [,9] [,10]
              1
                 1 1
                            1
                                 1
                                    0
## [2,]
       0
            1 1
                      1
                            1
                                  1
                                      0
                                           0
```

glmulti

Looks for interactions as well

Now we can take the output and test it out in lm()

eq = summary(multi.out)\$bestmodel
lm.multi = lm(eq,data=diab.train)

summary(lm.multi)

```
library(glmulti)
\# method = "g" for genetic algorithm
# default fitfunction = "glm"
multi.out = glmulti(Y ~., data=diab.train,method="g",plotty=F,
                    report=F,fitfunction="lm",crit="aic")
## TASK: Genetic algorithm in the candidate set.
## Initialization...
## Algorithm started...
## Improvements in best and average IC have bebingo en below the specified goals.
## Algorithm is declared to have converged.
## Completed.
#summary(multi.out)
summary(multi.out)$bestmodel
## [1] "Y ~ 1 + sex + bmi + map + tc + ldl + ltg + glu + bmi:age + map:bmi + "
## [2] "
          tc:age + tc:sex + ldl:sex + hdl:bmi + tch:tc + tch:ldl + "
## [3] "
           ltg:ldl + glu:ldl + glu:hdl + glu:tch"
```

```
##
## Call:
## lm(formula = eq, data = diab.train)
##
## Residuals:
##
        Min
                       Median
                                     3Q
                  1Q
                                             Max
                       -2.658
  -120.674 -33.210
                                33.217
                                        164.897
##
## Coefficients:
##
                 Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                  150.061
                               4.617
                                       32.504 < 2e-16 ***
## sex
                 -238.517
                              88.912
                                      -2.683 0.007913 **
                  376.726
                             101.401
                                        3.715 0.000263 ***
## bmi
## map
                  419.511
                              88.825
                                        4.723 4.36e-06 ***
## tc
                 -795.669
                              251.984
                                       -3.158 0.001836 **
## ldl
                  640.827
                             241.715
                                        2.651 0.008661 **
                  766.361
                             119.785
                                        6.398 1.09e-09 ***
## ltg
                  169.310
                              90.562
                                        1.870 0.063001 .
## glu
                 3466.129
                            1987.275
                                        1.744 0.082660
## bmi:age
## bmi:map
                 5201.707
                            1698.231
                                        3.063 0.002491 **
## tc:age
                -3239.013
                            1760.440
                                      -1.840 0.067259 .
                 9457.575
                            4462.404
                                        2.119 0.035285 *
## sex:tc
## sex:ldl
                -7335.897
                            4734.103
                                      -1.550 0.122814
## bmi:hdl
                 3153.680
                            2036.078
                                        1.549 0.122979
## tc:tch
               -14489.322
                            4342.291
                                      -3.337 0.001010 **
## ldl:tch
                 8392.404
                            3740.014
                                        2.244 0.025926 *
## ldl:ltg
                 5924.064
                                        2.720 0.007108 **
                            2178.279
## ldl:glu
                -6070.442
                            2964.496
                                      -2.048 0.041889 *
## glu:hdl
                 8444.079
                                        2.201 0.028879 *
                            3836.584
## glu:tch
                12578.225
                            4238.164
                                        2.968 0.003363 **
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 51.81 on 201 degrees of freedom
## Multiple R-squared: 0.5852, Adjusted R-squared:
## F-statistic: 14.92 on 19 and 201 DF, p-value: < 2.2e-16
```

The addition of interactions increases our R^2 even though our criterion for glmulti was AIC.

simulated annealing

http://topepo.github.io/caret/SA.html

part of this, other options including GA available: http://topepo.github.io/caret/featureselection.html To do, have to install most current version of caret from github. CRAN version doesn't include functions The great thing about this function is that we can use it for all of the methods in caret (100+).

```
library(devtools)
devtools::install_github("cran/caret")
library(caret)
```

Use with genetic algorithm: http://topepo.github.io/caret/GA.html

Pretty slow

Classification

All of the methods used previously will also work in the classification context in using forms of logistic regression.

Logistic Regression

```
Ybin <- ifelse(diab.train$Y > mean(diab.train$Y),1,0)
diab.train2 <- diab.train
diab.train2$Y <- Ybin

# logistic
glm.out <- glm(Y ~ ., diab.train2,family="binomial")
#summary(glm.out)</pre>
```

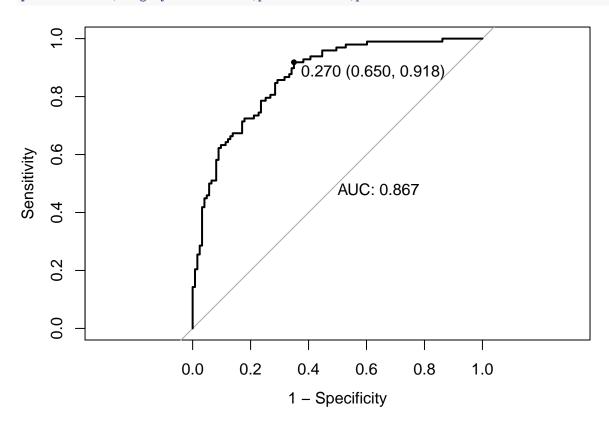
So how well did we do? I like using receive operating characteristic (ROC) curves and the area under the curve (AUC) to evaluate results in classification.

For binary outcomes, my favorite way to assess how well I did is using the confusionMatrix() function from caret

sensitivity = true positive – with event AND predicted to have event / having the event people who respondend AND people predicted to respond / people who respondend specificity = samples w/o event AND predicted as non-event / samples w/o event actual non-response AND predicted non-response/ actual non-response false-positive = 1-specificity

```
library(pROC)
library(caret)
glm.probs=predict(glm.out,type="response")
glm.pred=ifelse(glm.probs>0.5,1,0)
table(diab.train2$Y,glm.pred)
##
      glm.pred
##
        0 1
##
     0 99 24
##
     1 27 71
confusionMatrix(diab.train2$Y,glm.pred,positive="1") # from caret package
## Confusion Matrix and Statistics
##
             Reference
## Prediction 0 1
##
            0 99 24
            1 27 71
##
##
##
                  Accuracy : 0.7692
##
                    95% CI: (0.708, 0.8231)
       No Information Rate : 0.5701
##
##
       P-Value [Acc > NIR] : 4.809e-10
##
##
                     Kappa : 0.531
   Mcnemar's Test P-Value: 0.7794
##
##
##
               Sensitivity: 0.7474
##
               Specificity: 0.7857
            Pos Pred Value: 0.7245
##
##
            Neg Pred Value: 0.8049
##
                Prevalence: 0.4299
##
            Detection Rate: 0.3213
##
      Detection Prevalence : 0.4434
##
         Balanced Accuracy: 0.7665
##
          'Positive' Class : 1
##
rocCurve <- roc(diab.train2$Y,glm.probs)</pre>
auc(rocCurve)
## Area under the curve: 0.8672
ci.roc(rocCurve)
## 95% CI: 0.821-0.9134 (DeLong)
```

```
plot(rocCurve, legacy.axes = TRUE,print.thres=T,print.auc=T)
```

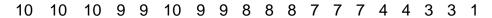


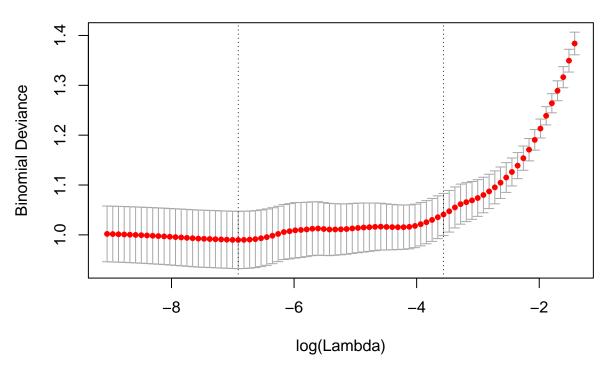
```
##
## Call:
## roc.default(response = diab.train2$Y, predictor = glm.probs)
##
## Data: glm.probs in 123 controls (diab.train2$Y 0) < 98 cases (diab.train2$Y 1).
## Area under the curve: 0.8672</pre>
```

Try also with elastic net

Regularization in caret package: http://topepo.github.io/caret/L1_Regularization.html

```
XX <- as.matrix(diab.train2[,-1])
YY <- diab.train2$Y
lasLog <- cv.glmnet(XX,YY,family="binomial")
plot(lasLog)</pre>
```





```
pred.lasLog <- predict(lasLog, XX, s="lambda.1se",type="response")</pre>
```

How did we do?

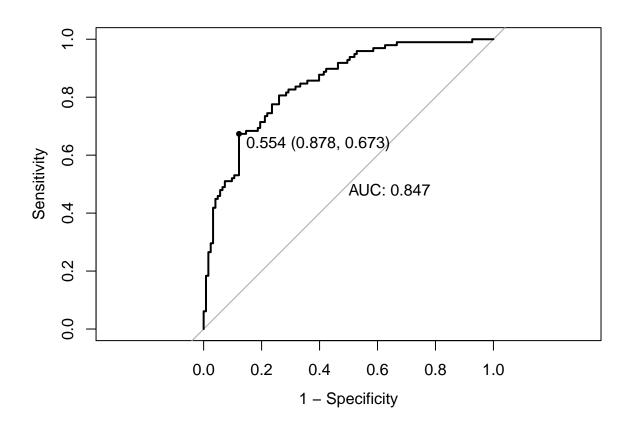
ci.roc(rocCurve2)

```
rocCurve2 <- roc(diab.train2$Y,pred.lasLog)
auc(rocCurve2)</pre>
```

Area under the curve: 0.8474

95% CI: 0.7972-0.8977 (DeLong)

```
plot(rocCurve2, legacy.axes = TRUE,print.thres=T,print.auc=T)
```



```
##
## Call:
## roc.default(response = diab.train2$Y, predictor = pred.lasLog)
##
## Data: pred.lasLog in 123 controls (diab.train2$Y 0) < 98 cases (diab.train2$Y 1).
## Area under the curve: 0.8474</pre>
```

We got rid of 6 predictors and only lost 0.01 in the AUC