

Question: Q3. A bit stream 10011101 is transmitted using the... | Chegg.c...

Q3. A bit stream 10011101 is transmitted using the standard CRC method. The generator polynomial is $x^3 + 1$.

- Show the actual bit string transmitted.
- Suppose that the third bit from the left is inverted during transmission. Show that this error is detected at the receiver's end.
- Give an example of bit errors in the bit string transmitted that will not be detected by the receiver.

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Expert Answer

(a) Given bit stream : 10011101

CRC generator polynomial : $x^3 + 1 = 1001$

K is the length of CRC generator polynomial : 4

Step 1: Append 'K-1' zeroes to given bit stream.

Message : 10011101000

Step 2: Compute code word for given bit stream using generator polynomial.

$$\begin{array}{r}
 1001 \overline{) 10011101000} \quad (10001100) \\
 \underline{1001} \\
 0001 \\
 \underline{0000} \\
 0011 \\
 \underline{0000} \\
 0110 \\
 \underline{0000} \\
 1101 \\
 \underline{1001} \\
 1000 \\
 \underline{1001} \\
 0010 \\
 \underline{0000} \\
 0100 \\
 \underline{0000} \\
 100 \rightarrow \text{Remainder}
 \end{array}$$

Step 3: Append the remainder to bit stream which is the
bit string transmitted:

Bit string transmitted: 1001110100

- ① Actual bit stream to be transmitted: 1001110100
Invert third bit from left, then we get: 1011110100
- To know that received message is error free or not, following steps need to be followed:
- ① Calculate remainder to received message using same generator polynomial
 - ② If we get remainder as all zeroes, then there is no error in received message
 - ③ Else we can just say that there exists errors in received message but we can't say how many errors, what are the errors.
- Eg: message (corrupted): ~~100~~ 1011110100
3rd bit from left is inverted.
- So, apply CRC algorithm on message using same generator polynomial '1001'.

$$\begin{array}{r}
 1001 \overline{) 10111101100} \quad (10101000) \\
 \underline{1001} \\
 0101 \\
 \underline{0000} \\
 1011 \\
 \underline{1001} \\
 0100 \\
 \underline{0000} \\
 1001 \\
 \underline{1001} \\
 0001 \\
 \underline{0000} \\
 0000 \\
 \underline{0010} \\
 0000 \\
 \underline{0100} \\
 0000 \\
 \underline{100} \rightarrow \text{Remainder}
 \end{array}$$

→ Since remainder is not all zeroes, we can say that there exists some errors in message, but can't say what are these errors.

© Let's take an example with multiple errors:
 Message: 11001010100
 2nd, 4th, 6th, 7th, 8th bits of original message are inverted.

① Calculate remainder.

$$\begin{array}{r}
 1001 \overline{) 11001010100} \quad (11010000) \\
 \underline{1001} \\
 1011 \\
 \underline{1001} \\
 0100 \\
 \underline{0000} \\
 1001 \\
 \underline{1001} \\
 0000 \\
 \underline{0000} \\
 0001 \\
 \underline{0000} \\
 0010 \\
 \underline{0000} \\
 0100 \\
 \underline{0000} \\
 100 \rightarrow \text{remainder}
 \end{array}$$

→ We totally have 5 errors, but remainder is 100, so by looking at remainder, we just can say whether the bit stream is corrupted or not but we can't say what are those corrupted bit.