



STAT 453: Introduction to Deep Learning and Generative Models

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Lecture 06: Automatic Differentiation with PyTorch

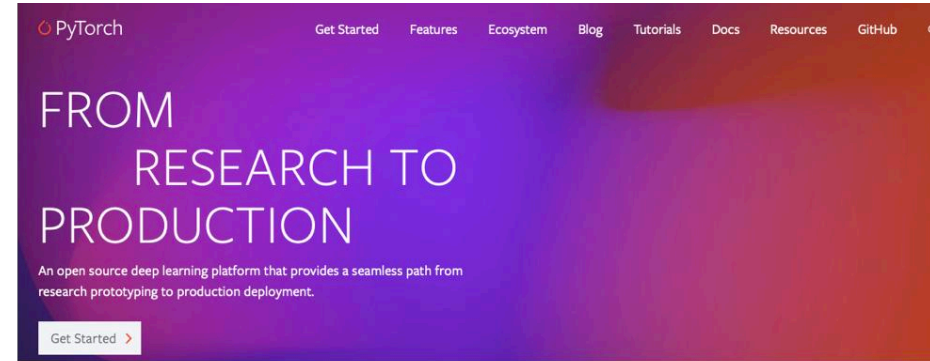
September 22, 2025



Today: Computing partial derivatives with PyTorch

1. **PyTorch Resources**
2. Computation Graphs
3. Automatic Differentiation in PyTorch
4. A Closer Look at the PyTorch API

PyTorch



<https://pytorch.org/>

At a Glance:

- Based on Torch 7, which was based on Lua and inspired by Lush
- PyTorch started in 2016
- Focuses on flexibility and minimizing cognitive overhead
- Dynamic nature of autograd API inspired by Chainer
- Core features
 - **Automatic differentiation**
 - **Dynamic computation graphs**
 - NumPy integration
- written in C++ and CUDA (CUDA is like C++ for the GPU)
- Python is the usability glue



Installing PyTorch

Recommendation for Laptop (e.g., MacBook)

PyTorch Build	Stable (1.7.1)		Preview (Nightly)	
Your OS	Linux	Mac	Windows	
Package	Conda	Pip	LibTorch	Source
Language	Python		C++ / Java	
CUDA	9.2	10.1	10.2	11.0
				None
Run this Command:	NOTE: Python 3.9 users will need to add '-c=conda-forge' for installation <code>conda install pytorch torchvision torchaudio -c pytorch</code>			

Recommendation for Desktop (Linux) with GPU

PyTorch Build	Stable (1.7.1)		Preview (Nightly)	
Your OS	Linux	Mac	Windows	
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<https://pytorch.org/>

And don't forget that you import PyTorch as "import torch," not "import pytorch" :)

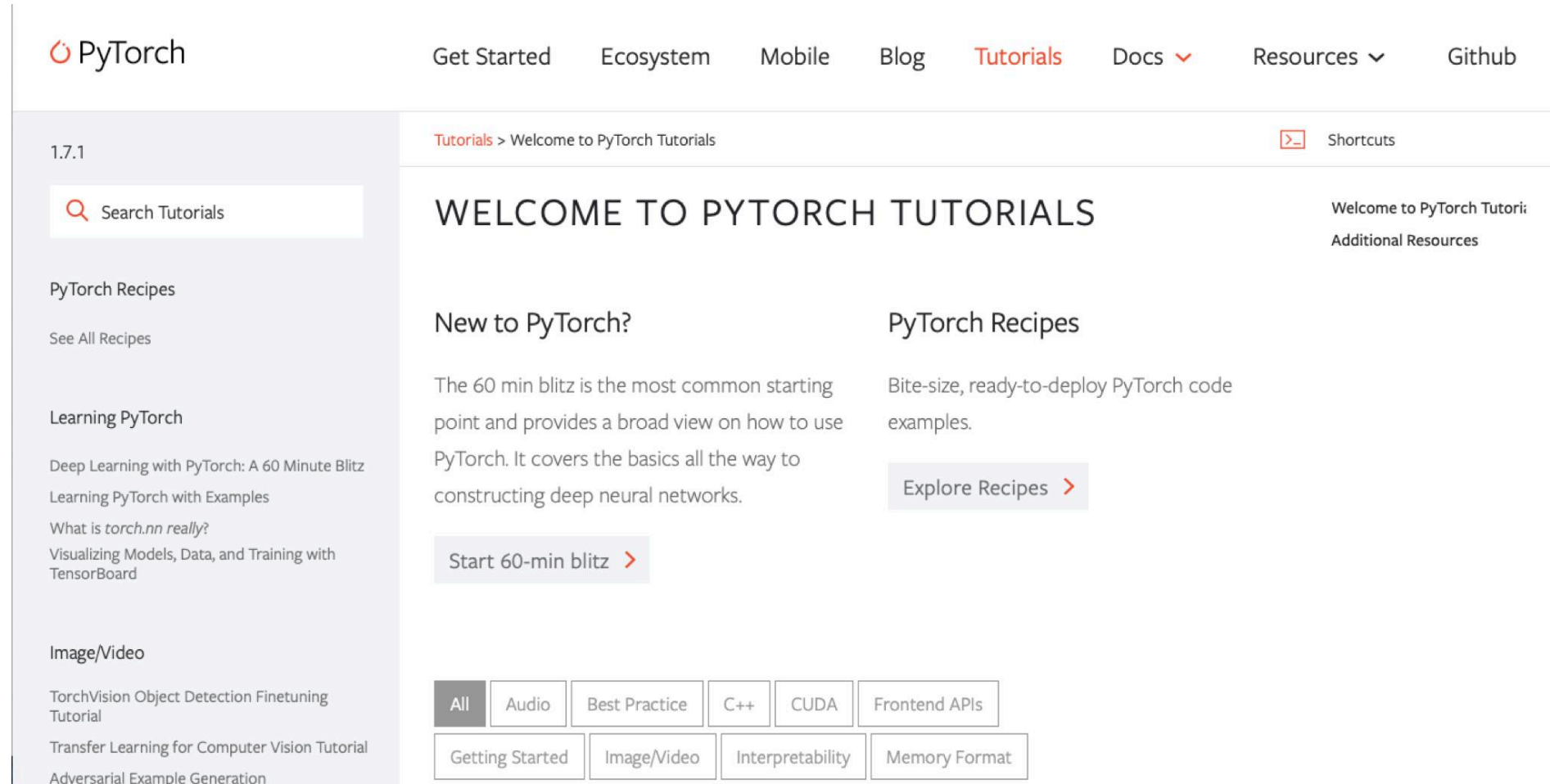
```
[In [1]: import torch

[In [2]: torch.__version__
Out[2]: '1.7.0'

In [3]:
```



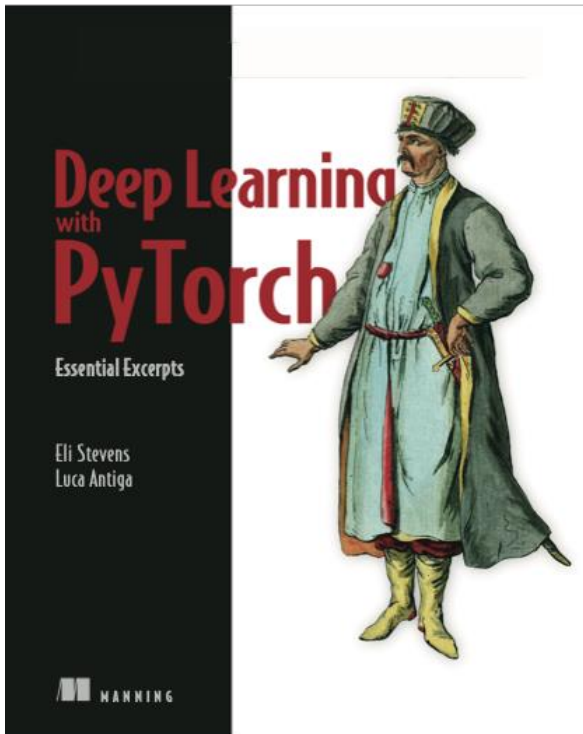
Many useful tutorials (recommend you read some)



The screenshot shows the PyTorch Tutorials page. The header includes the PyTorch logo and navigation links: Get Started, Ecosystem, Mobile, Blog, Tutorials (highlighted), Docs, Resources, and Github. The left sidebar contains a search bar, a version selector (1.7.1), and sections for PyTorch Recipes, Learning PyTorch (with links to a 60-minute blitz, examples, and torch.nn), and Image/Video (with links to object detection and transfer learning). The main content area is titled 'WELCOME TO PYTORCH TUTORIALS' and features a 'New to PyTorch?' section with a 'Start 60-min blitz' button. To the right, there's a 'PyTorch Recipes' section with an 'Explore Recipes' button. A filter bar at the bottom allows selection by category (All, Audio, Best Practice, C++, CUDA, Frontend APIs) and topic (Getting Started, Image/Video, Interpretability, Memory Format).

<https://pytorch.org/tutorials/>

Other resources



PyTorch

Do you want live notifications when people reply to your posts? [Enable Notifications](#)

all categories all Latest New (47) Unread (104) Top Categories + New Topic

Topic	Replies	Views	Activity
Using MSELoss instead of CrossEntropy for Ordinal Regression/Classification vision	2	83	1h
Optimizer.load_state_dict() weird behaviour with Adam optimizer vision	7	2.0k	1h
Is there a way to train 3 dataloaders using multiprocessing?	0	11	2h
Getting different feature vectors from frozen layers after training vision	5	86	2h
Libtorch_cuda.so is too large (>2GB) deployment	22	346	2h
Undo pruning - How to 'unmask' pruned weights vision	0	8	2h
If input.dim() == 2 and bias is not None: AttributeError: 'tuple' object has no attribute 'dim'	3	41	2h
Export unsupported/compound ops to ONNX deployment	0	9	2h

<https://discuss.pytorch.org>

And...

Ask ChatGPT/Claude if your PyTorch code is not working 😊



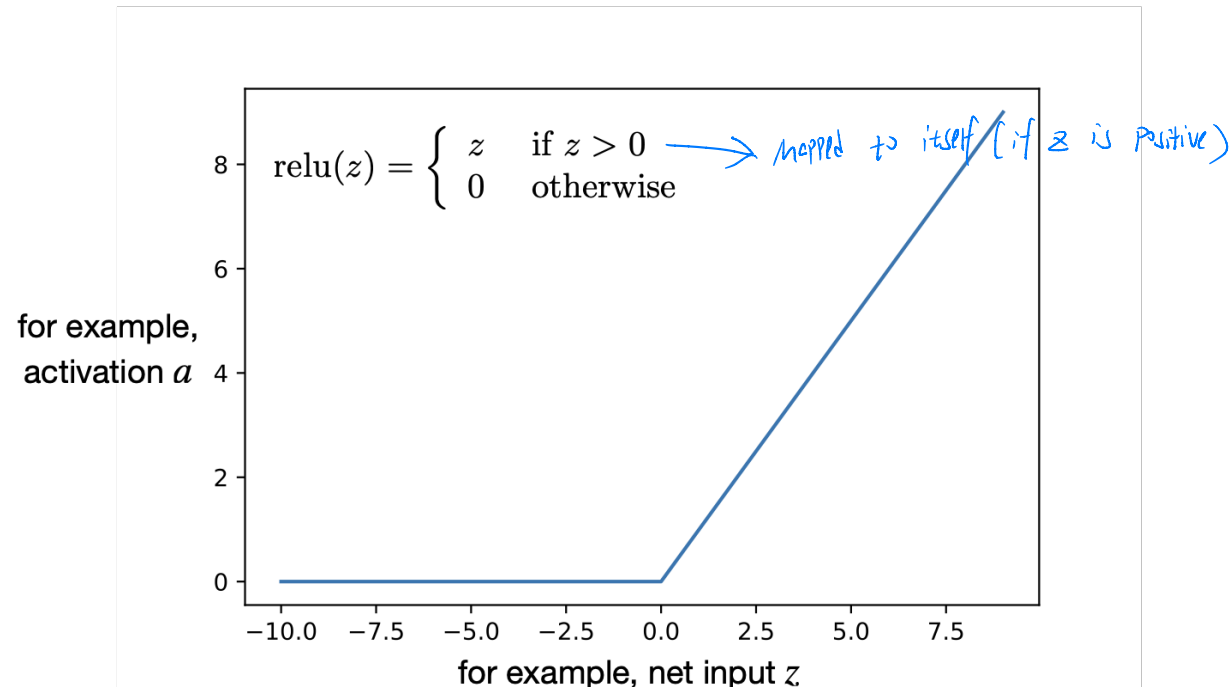
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Computation graphs: ReLU

Suppose we have the following activation function:

$$a(x, w, b) = \text{relu}(w \cdot x + b)$$



ReLU = Rectified Linear Unit

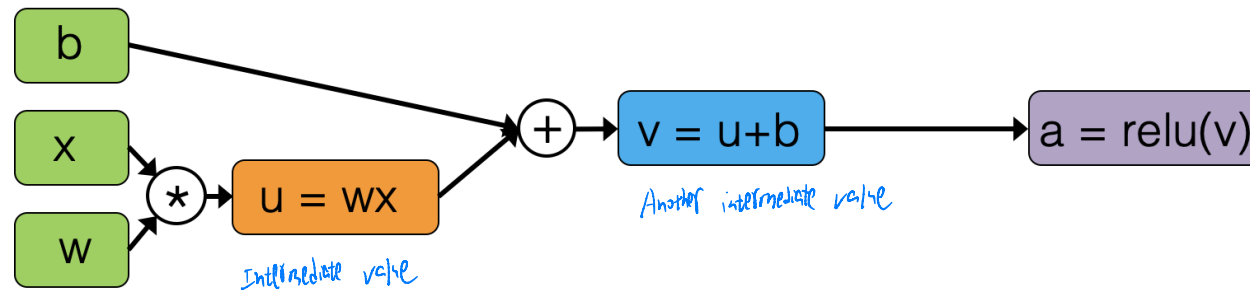
(prob. the most commonly used activation function in DL)

Computation graphs: ReLU

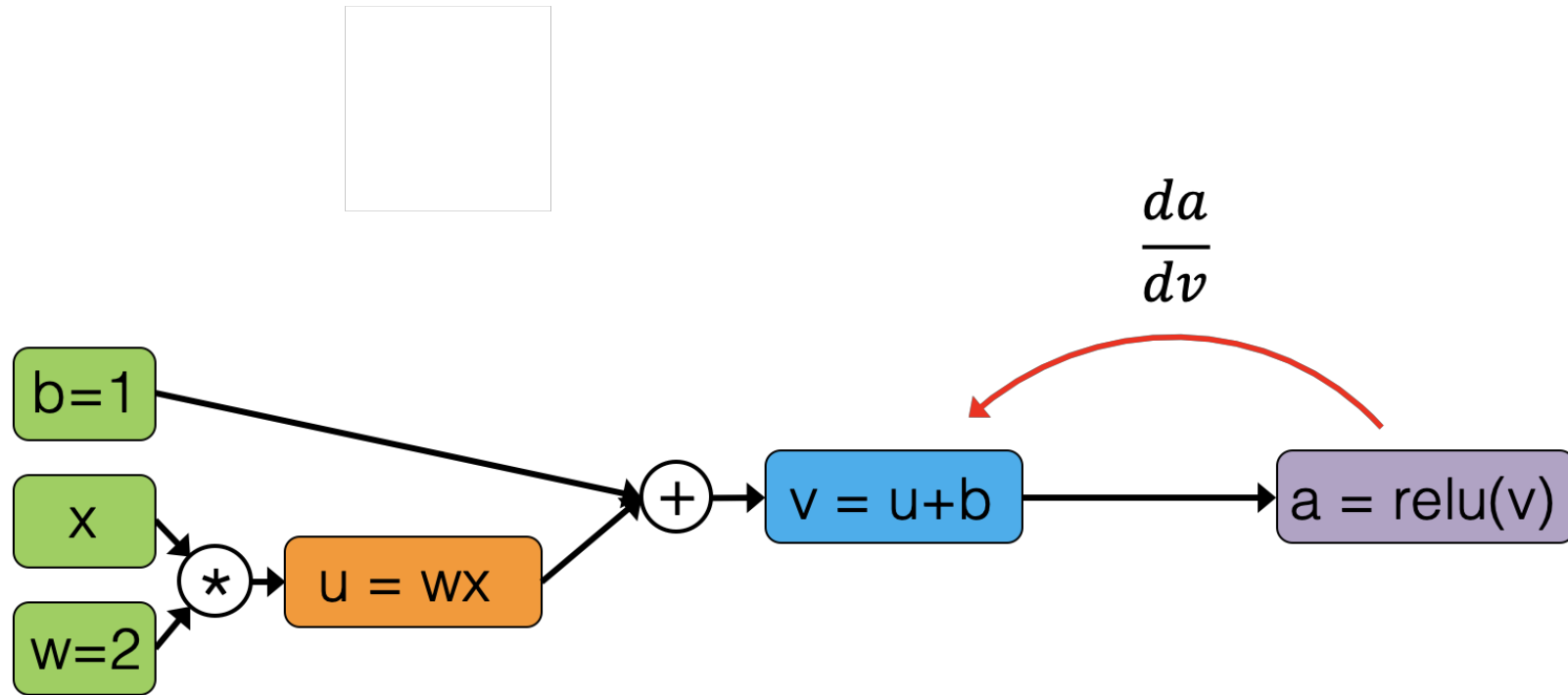
↓
Directed

$$a(x, w, b) = \text{relu}(\underbrace{w \cdot x}_{u} + b)$$

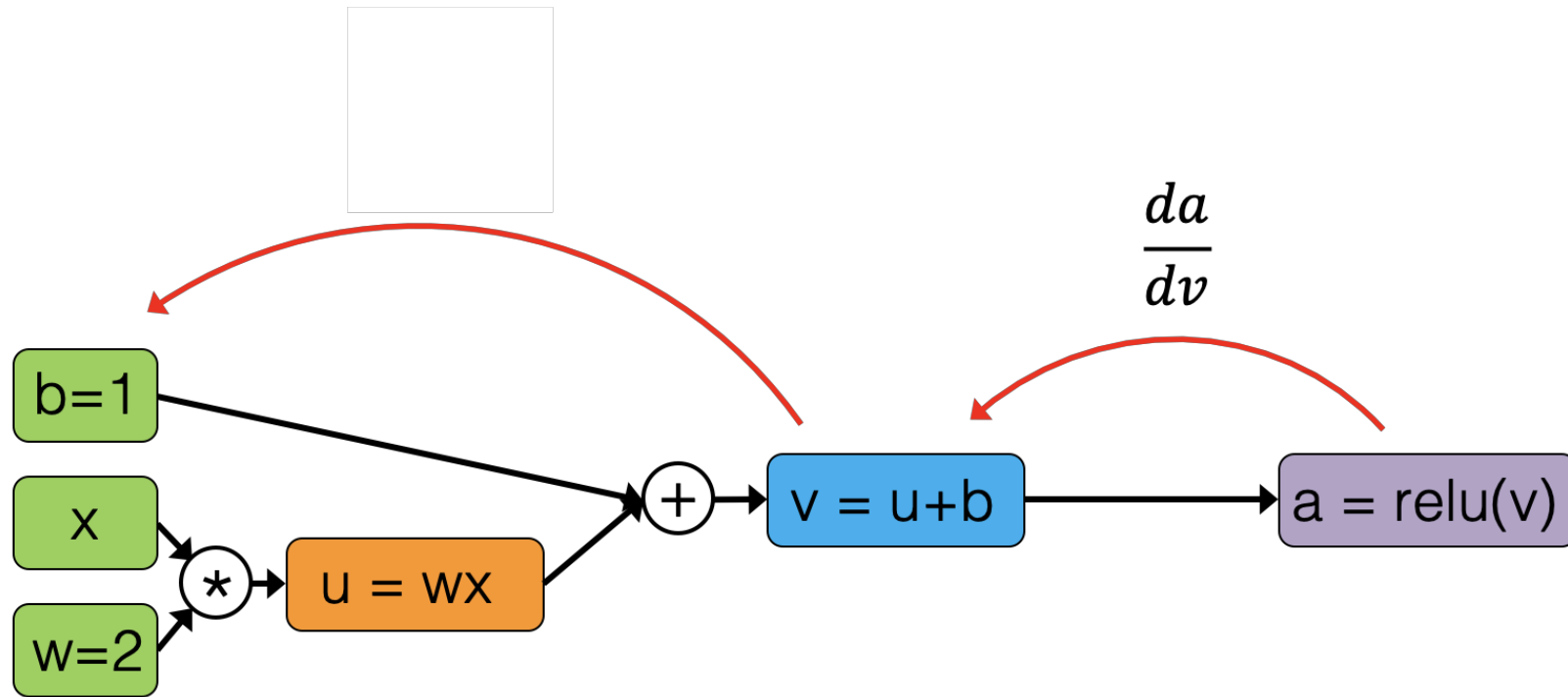
v



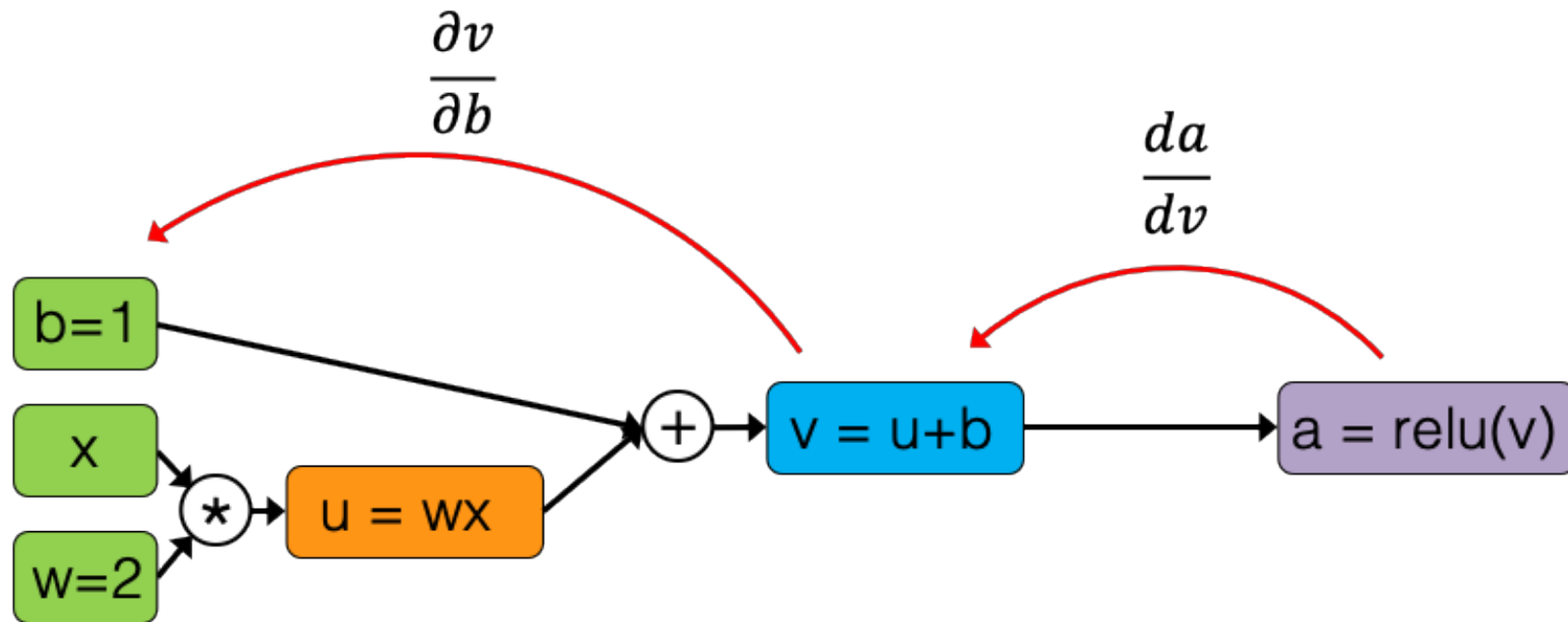
Computation graphs: ReLU



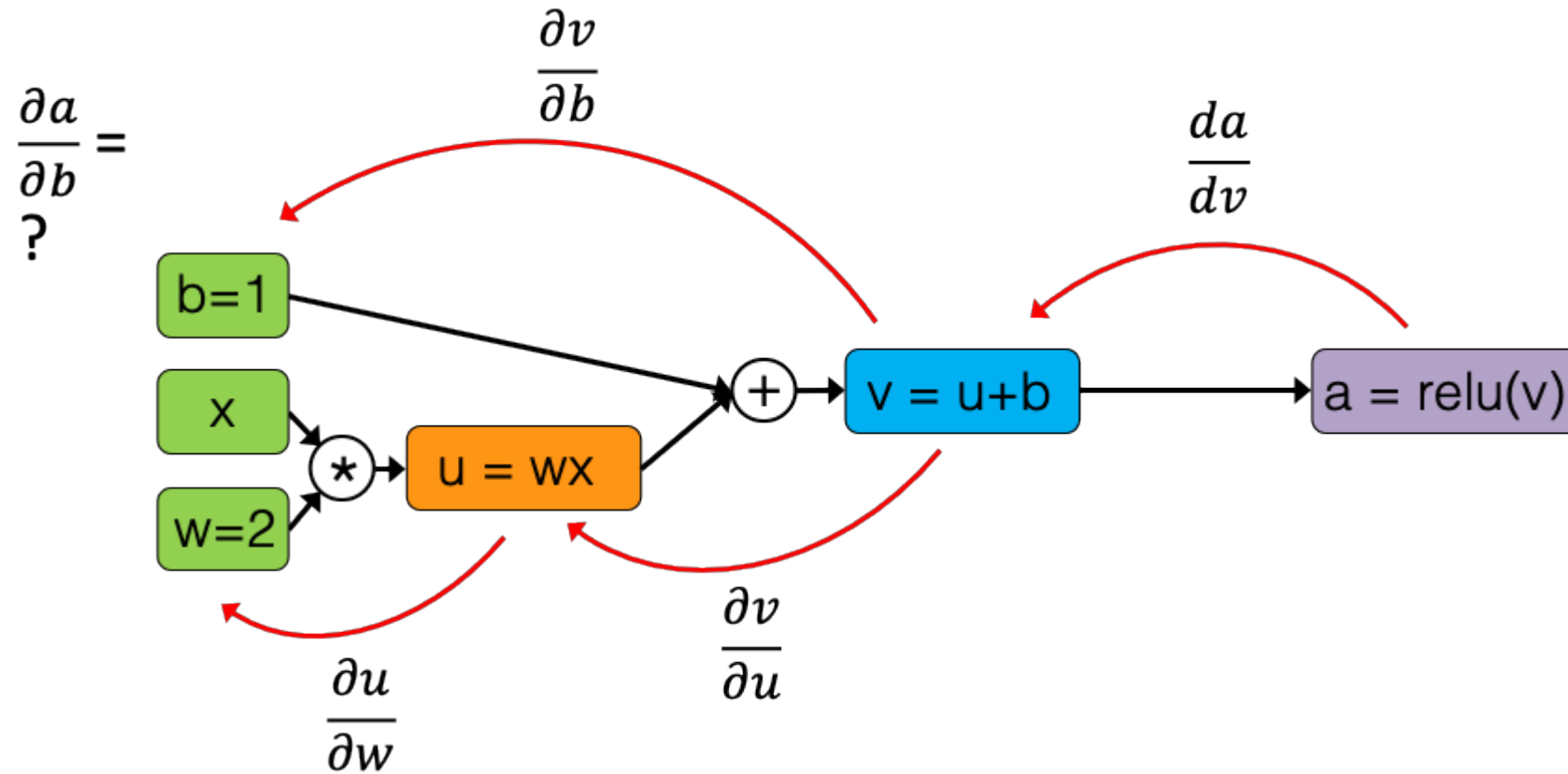
Computation graphs: ReLU



Computation graphs: ReLU

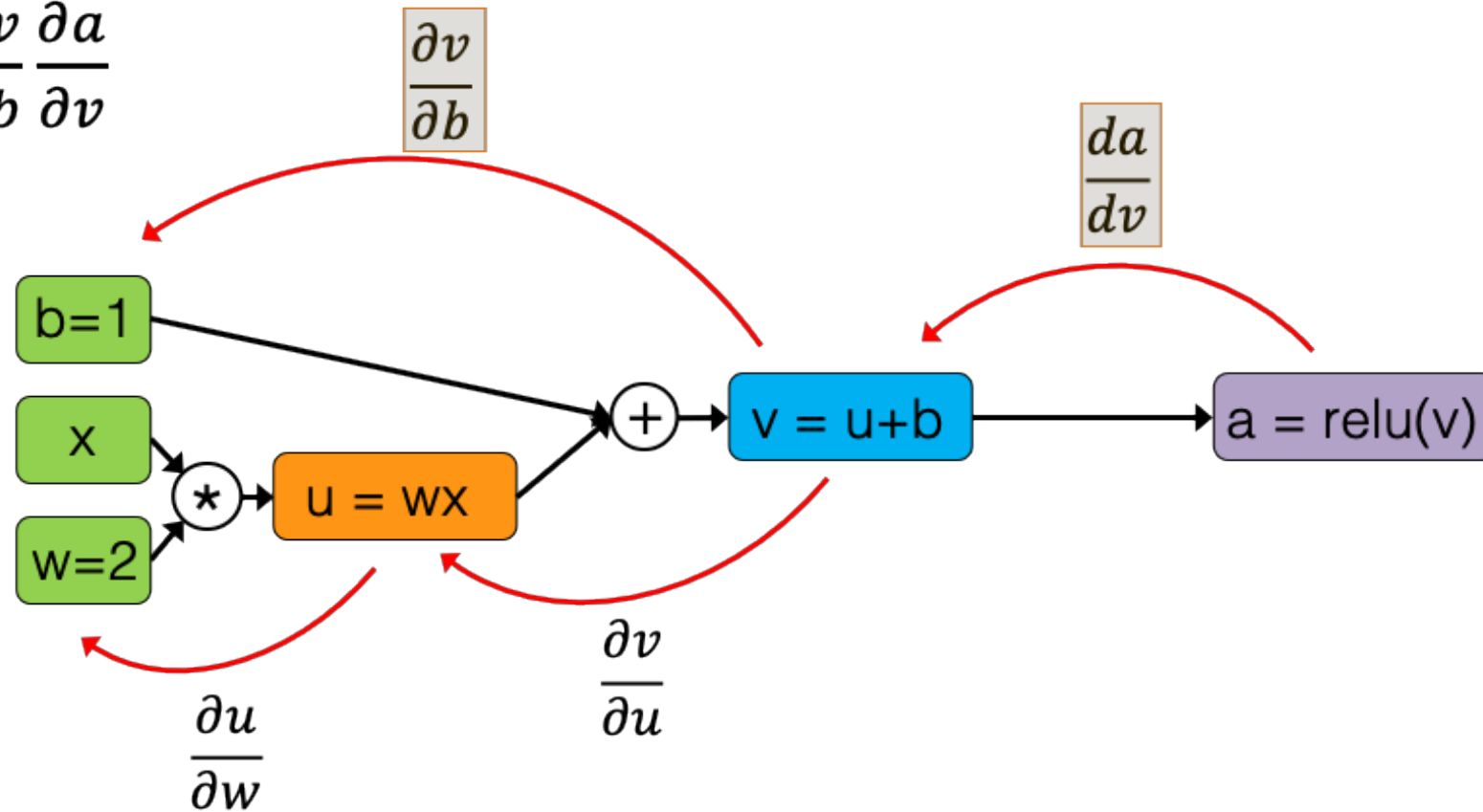


Computation graphs: ReLU

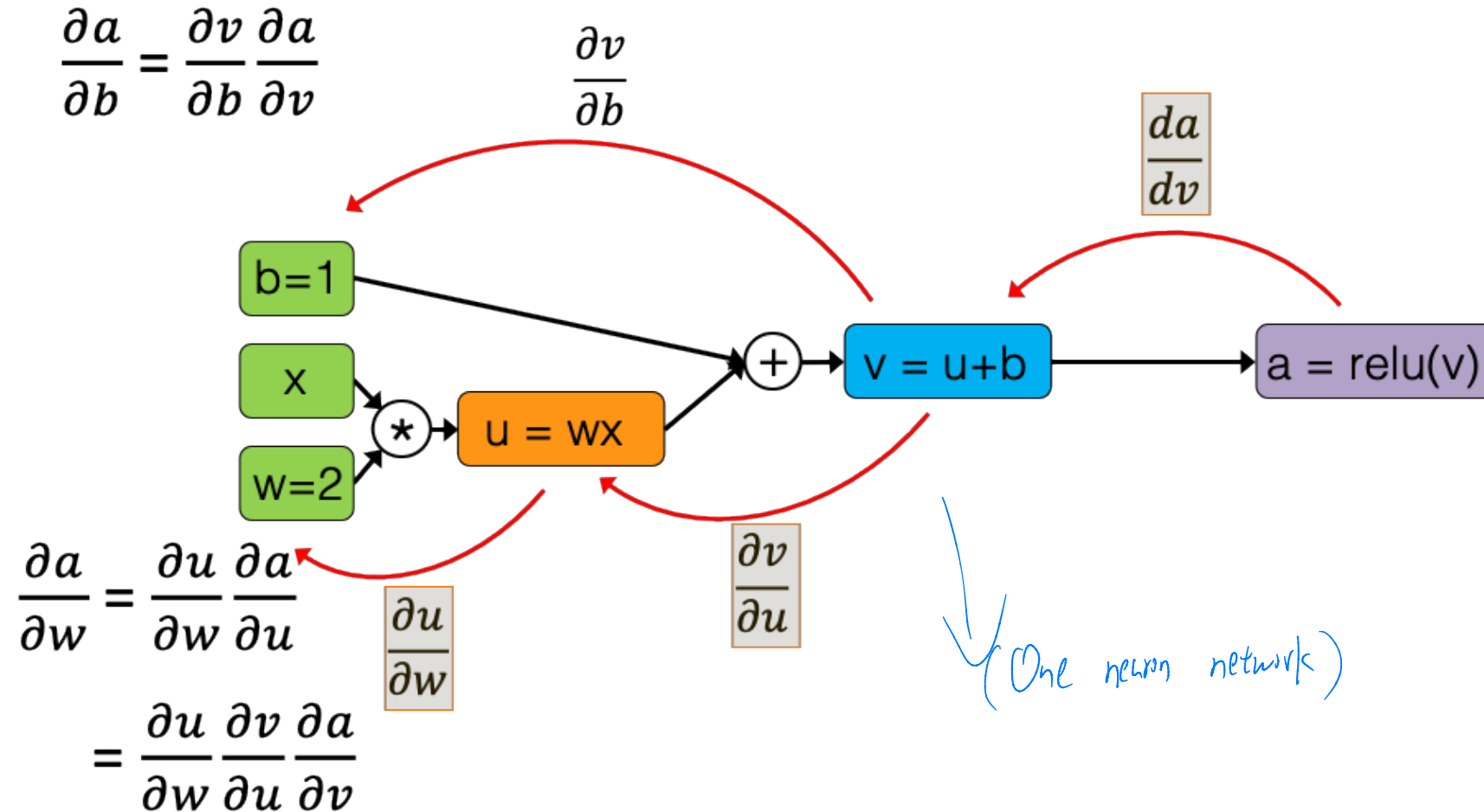


Computation graphs: ReLU

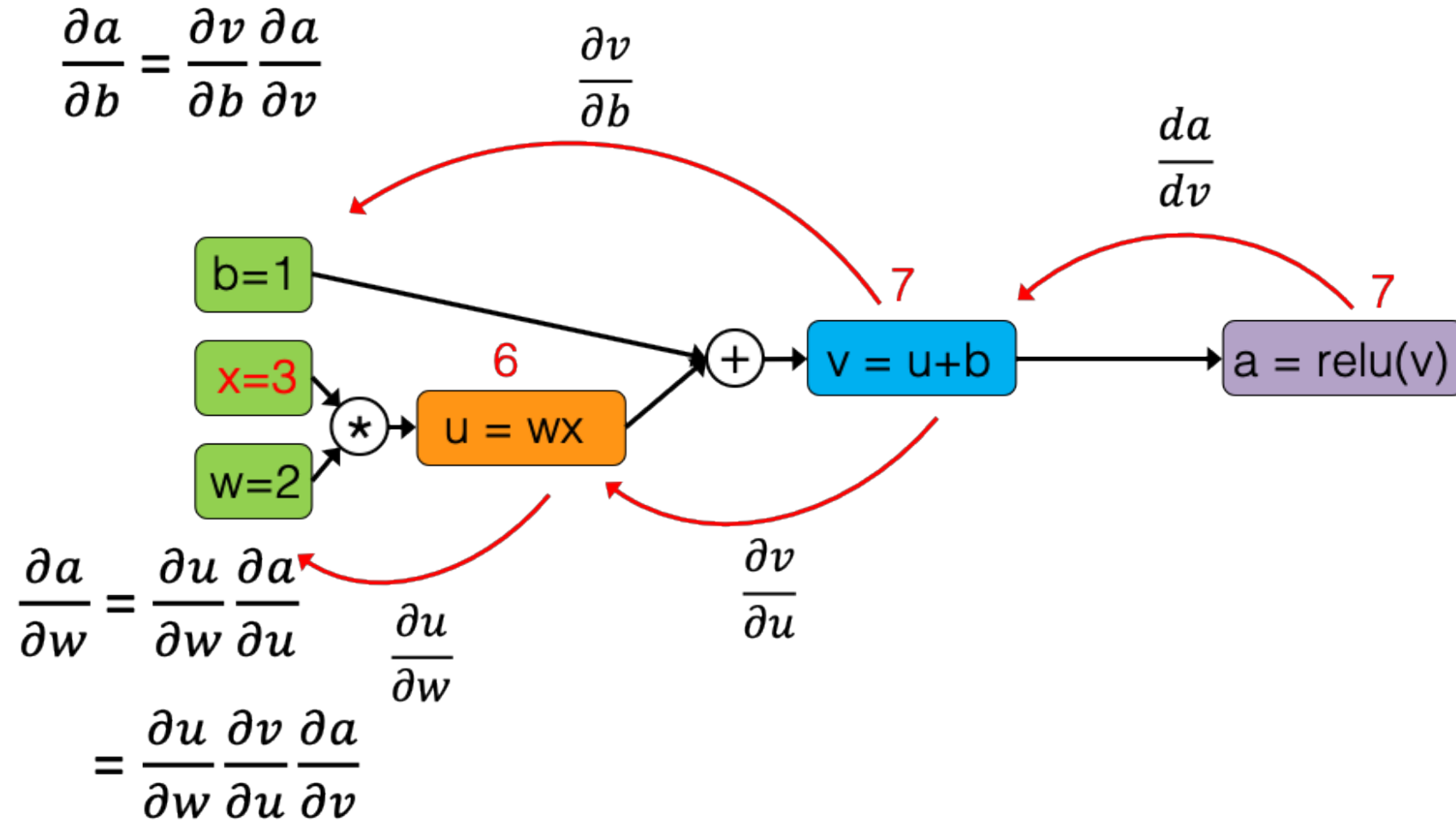
$$\frac{\partial a}{\partial b} = \frac{\partial v}{\partial b} \frac{\partial a}{\partial v}$$



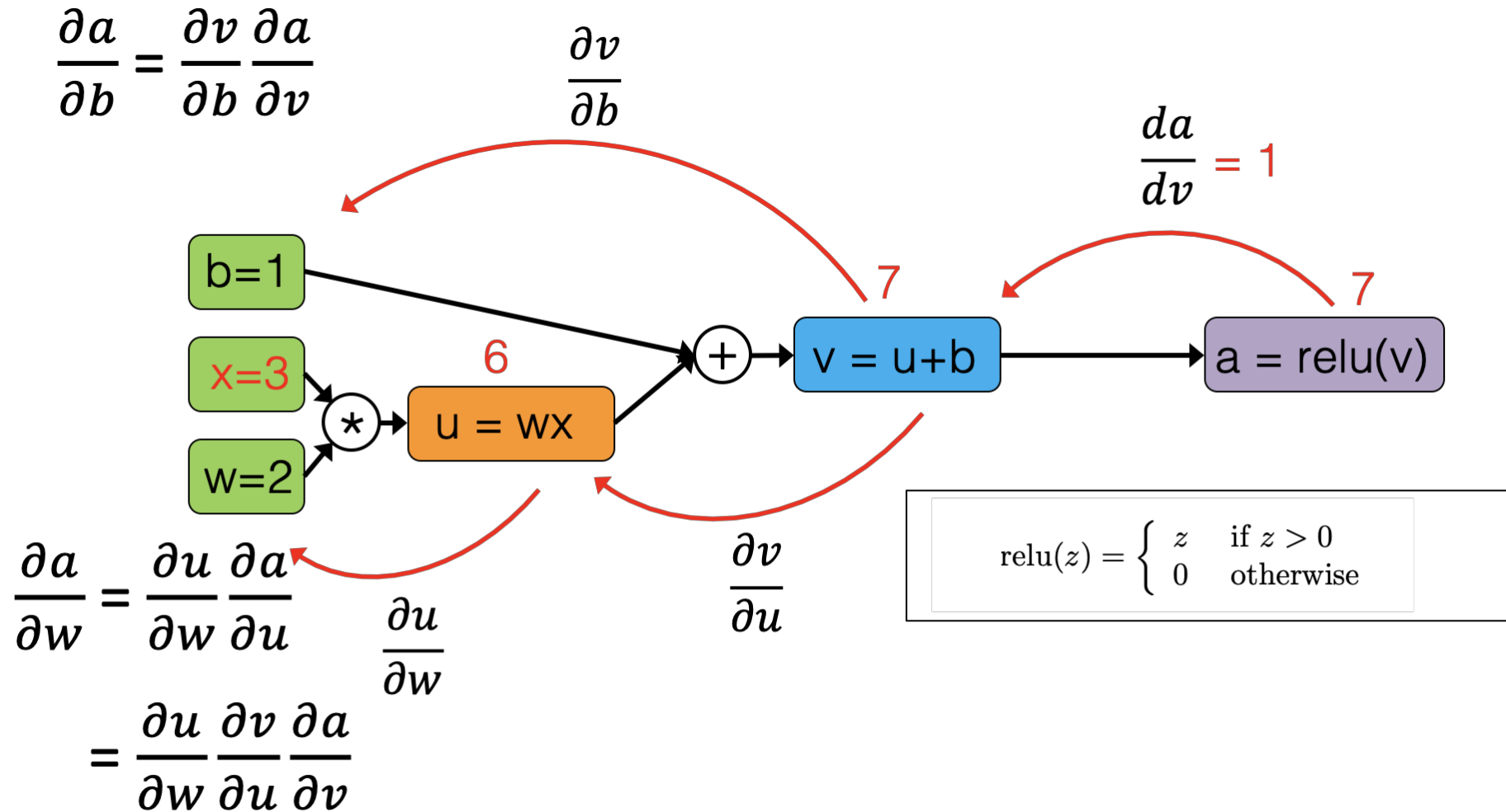
Computation graphs: ReLU



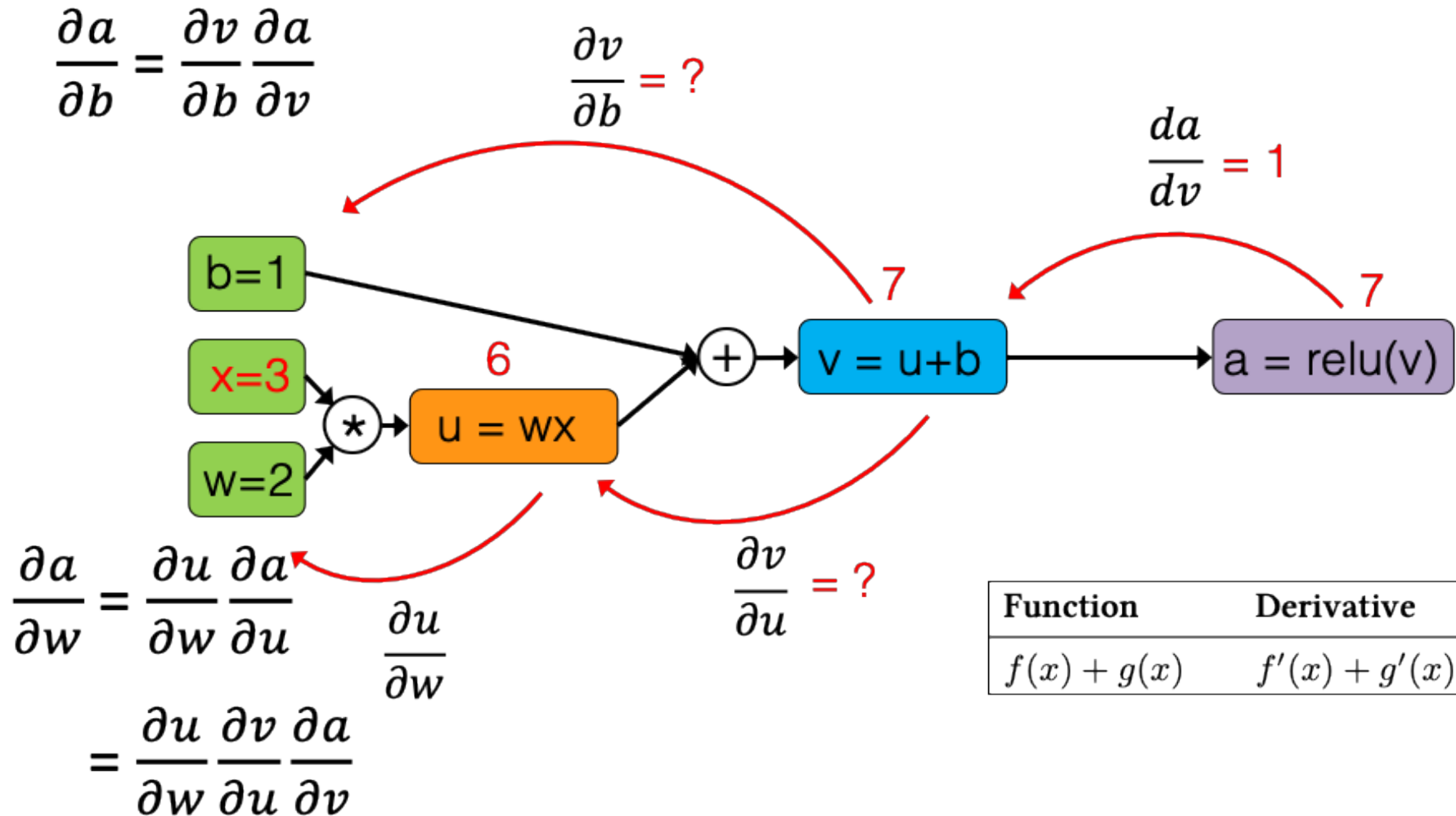
Computation graphs: ReLU



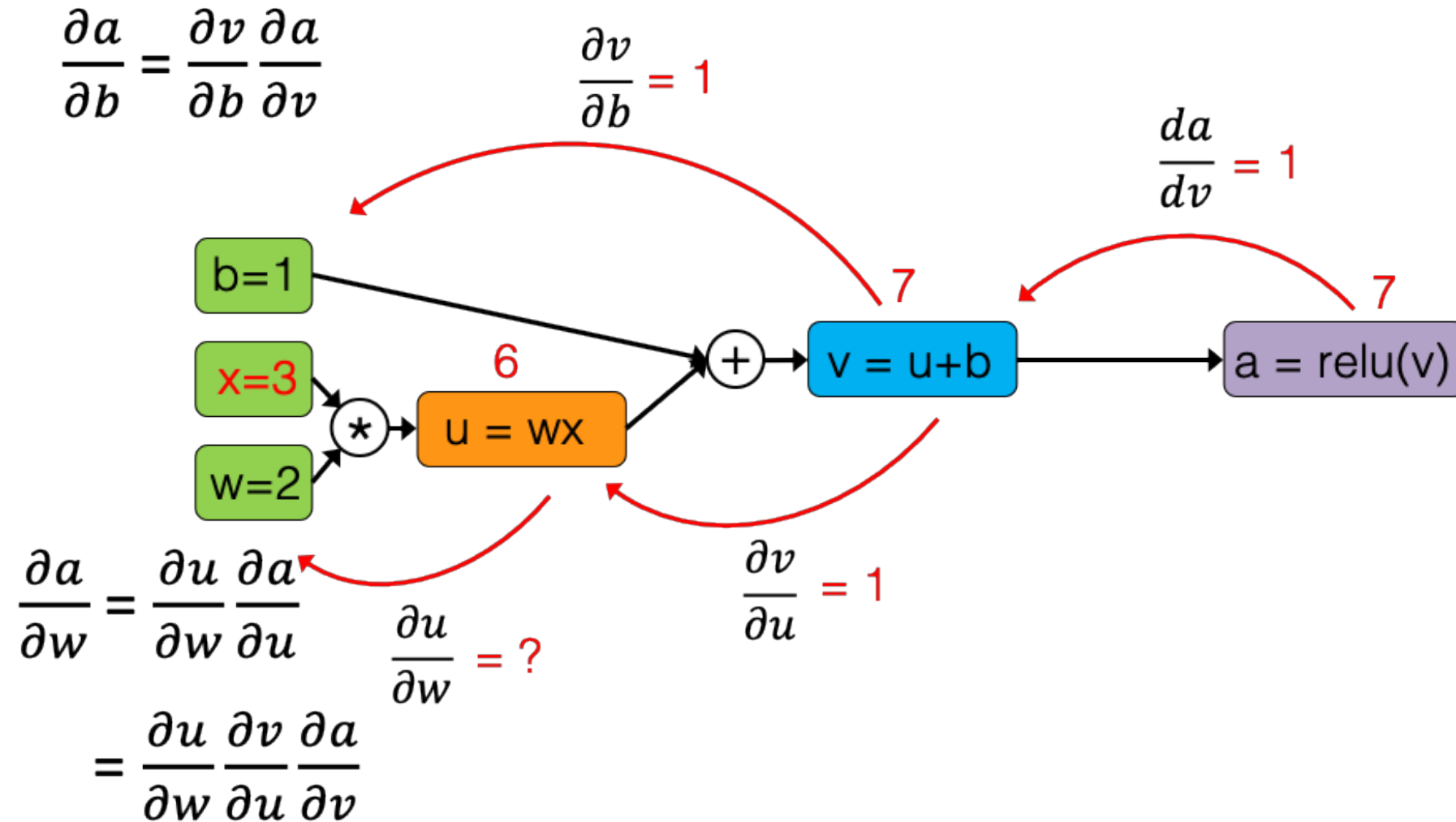
Computation graphs: ReLU



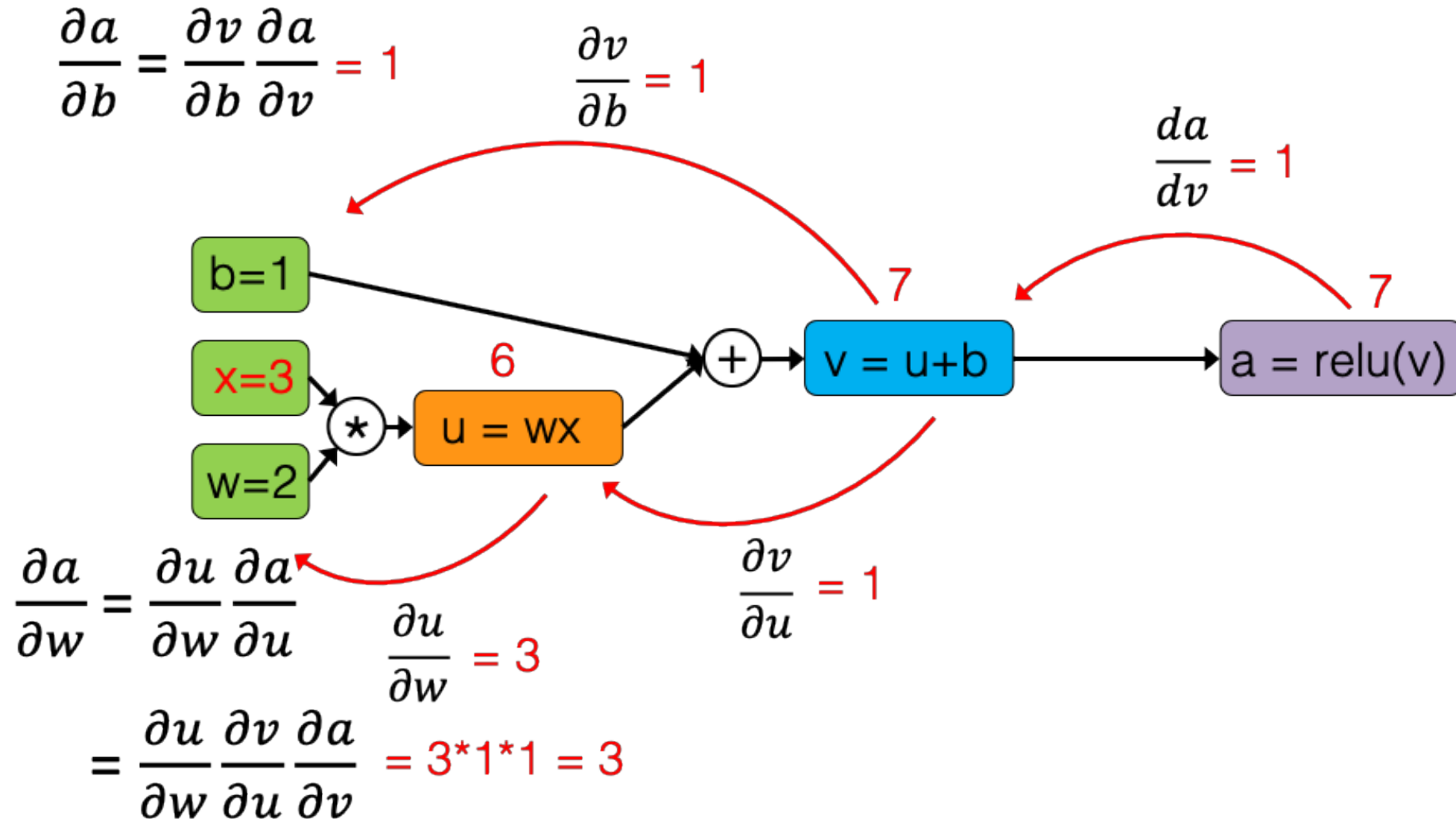
Computation graphs: ReLU



Computation graphs: ReLU



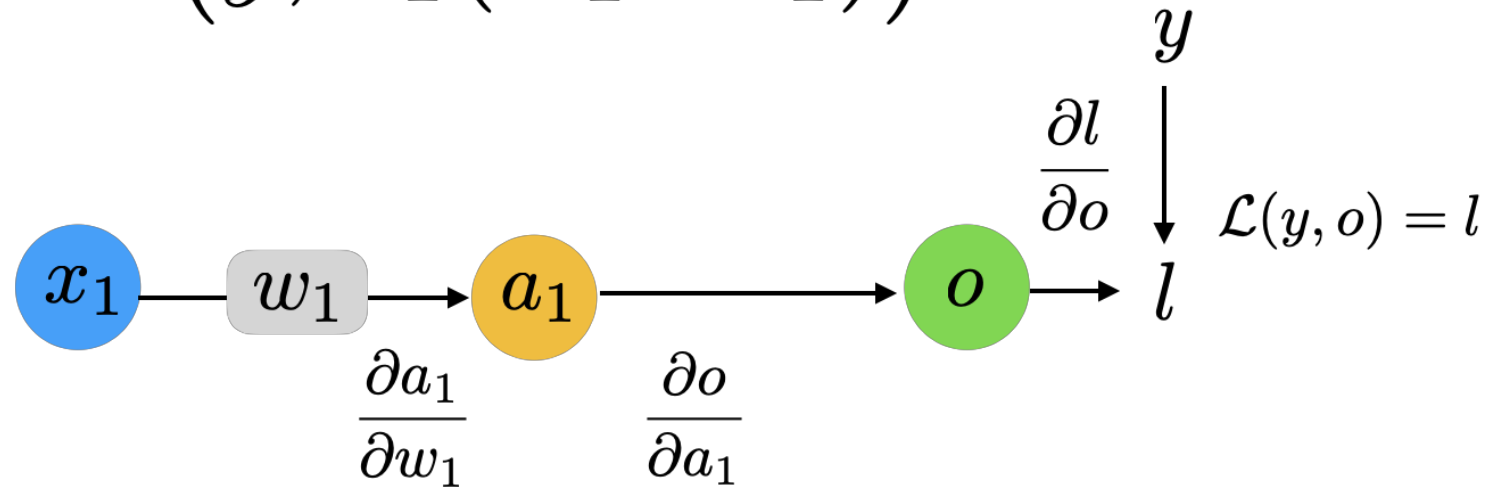
Computation graphs: ReLU



- Some more computation graphs

Computation graphs: Single-path

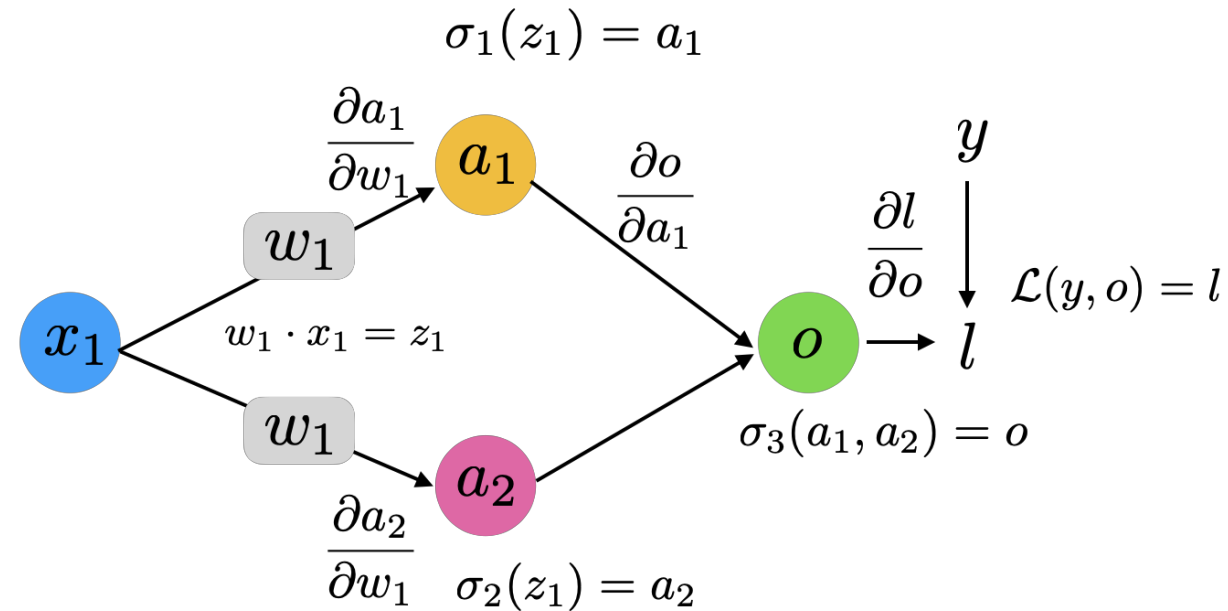
$$\mathcal{L}(y, \sigma_1(w_1 \cdot x_1))$$



$$\frac{\partial l}{\partial w_1} = \frac{\partial l}{\partial o} \cdot \frac{\partial o}{\partial a_1} \cdot \frac{\partial a_1}{\partial w_1} \quad (\text{univariate chain rule})$$

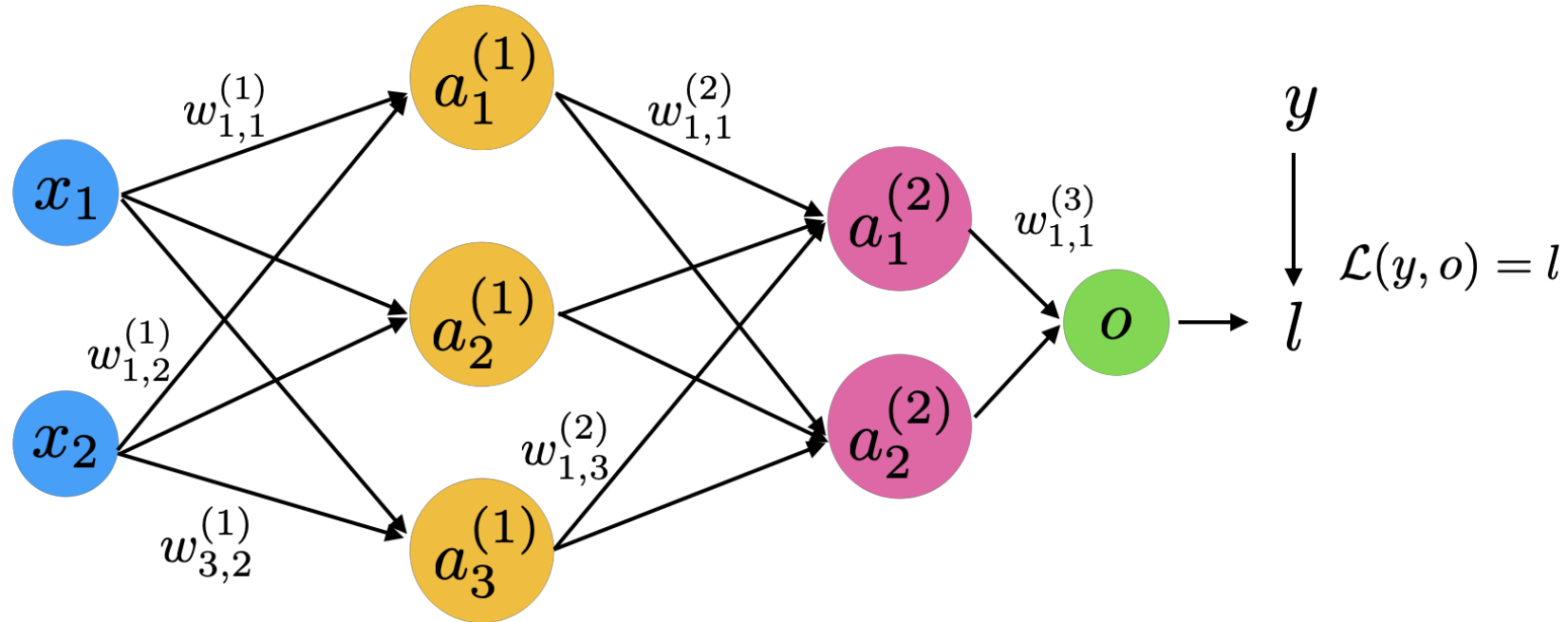
Computation graphs: **Weight-Sharing**

$$\mathcal{L}(y, \sigma_3[\sigma_1(w_1 \cdot x_1), \sigma_2(w_1 \cdot x_1)])$$



$$\frac{\partial l}{\partial w_1} = \underbrace{\frac{\partial l}{\partial o} \cdot \frac{\partial o}{\partial a_1} \cdot \frac{\partial a_1}{\partial w_1}}_{\text{Upper path}} + \underbrace{\frac{\partial l}{\partial o} \cdot \frac{\partial o}{\partial a_2} \cdot \frac{\partial a_2}{\partial w_1}}_{\text{Lower path}} \quad (\text{multivariable chain rule})$$

Computation graphs: Fully-Connected Layer



$$\begin{aligned} \frac{\partial l}{\partial w_{1,1}^{(1)}} &= \frac{\partial l}{\partial o} \cdot \frac{\partial o}{\partial a_1^{(2)}} \cdot \frac{\partial a_1^{(2)}}{\partial a_1^{(1)}} \cdot \frac{\partial a_1^{(1)}}{\partial w_{1,1}^{(1)}} \\ &\quad + \frac{\partial l}{\partial o} \cdot \frac{\partial o}{\partial a_2^{(2)}} \cdot \frac{\partial a_2^{(2)}}{\partial a_1^{(1)}} \cdot \frac{\partial a_1^{(1)}}{\partial w_{1,1}^{(1)}} \end{aligned}$$



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Automatic Differentiation in PyTorch

- An example:
<https://github.com/rasbt/stat453-deep-learning-ss21/tree/master/L06/code/pytorch-autograd.ipynb>



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PyTorch Usage: Step 1 (Definition)

```
class MultilayerPerceptron(torch.nn.Module):  
  
    def __init__(self, num_features, num_classes):  
        super(MultilayerPerceptron, self).__init__()  
  
        ### 1st hidden layer  
        self.linear_1 = torch.nn.Linear(num_feat, num_h1)  
  
        ### 2nd hidden layer  
        self.linear_2 = torch.nn.Linear(num_h1, num_h2)  
  
        ### Output layer  
        self.linear_out = torch.nn.Linear(num_h2, num_classes)  
  
    def forward(self, x):  
        out = self.linear_1(x)  
        out = F.relu(out)  
        out = self.linear_2(out)  
        out = F.relu(out)  
        logits = self.linear_out(out)  
        probas = F.log_softmax(logits, dim=1)  
        return logits, probas
```

Backward will be inferred automatically if we use the nn.Module class!

Define model parameters that will be instantiated when created an object of this class

Define how and in what order the model parameters should be used in the forward pass

PyTorch Usage: Step 2 (Creation)

```
torch.manual_seed(random_seed)
model = MultilayerPerceptron(num_features=num_features,
                             num_classes=num_classes)
```

Instantiate model
(creates the model parameters)

```
model = model.to(device)
```

```
optimizer = torch.optim.SGD(model.parameters(),
                             lr=learning_rate)
```

Define an optimization method

PyTorch Usage: Step 3 (Training)

```

for epoch in range(num_epochs):
    model.train()
    for batch_idx, (features, targets) in enumerate(train_loader):

        features = features.view(-1, 28*28).to(device)
        targets = targets.to(device)

        ### FORWARD AND BACK PROP
        logits, probas = model(features)
        cost = F.cross_entropy(probas, targets)
        optimizer.zero_grad()

        cost.backward()

        ### UPDATE MODEL PARAMETERS
        optimizer.step()

    model.eval()
    with torch.no_grad():
        # compute accuracy

```

Run for a specified number of epochs

Iterate over minibatches in epoch

If your model is on the GPU, data should also be on the GPU

`y = model(x)` calls `__call__` and then `.forward()`, where some extra stuff is done in `__call__`;
don't run `y = model.forward(x)` directly

Gradients at each leaf node are accumulated under the `.grad` attribute, not just stored. This is why we have to zero them before each backward pass

PyTorch Usage: Step 3 (Training)

```
for epoch in range(num_epochs):  
    model.train()  
    for batch_idx, (features, targets) in enumerate(train_loader):
```

```
        features = features.view(-1, 28*28).to(device)  
        targets = targets.to(device)
```

```
        ### FORWARD AND BACK PROP
```

```
        logits, probas = model(features)
```

```
        loss = F.cross_entropy(logits, targets)
```

```
        optimizer.zero_grad()
```

```
        loss.backward()
```

```
        ### UPDATE MODEL PARAMETERS
```

```
        optimizer.step()
```

```
    model.eval()
```

```
    with torch.no_grad():  
        # compute accuracy
```

← This will run the forward() method

← Define a loss function to optimize

← Set the gradient to zero

(could be non-zero from a previous forward pass)

← Compute the gradients, the backward is automatically constructed by "autograd" based on the forward() method and the loss function

← Use the gradients to update the weights according to the optimization method (defined on the previous slide)

E.g., for SGD, $w := w + \text{learning_rate} \times \text{gradient}$

PyTorch Usage: Step 3 (Training)

```
for epoch in range(num_epochs):  
    model.train()  
    for batch_idx, (features, targets) in enumerate(train_loader):
```

```
        features = features.view(-1, 28*28).to(device)  
        targets = targets.to(device)
```

```
        ### FORWARD AND BACK PROP  
        logits, probas = model(features)  
        loss = F.cross_entropy(logits, targets)  
        optimizer.zero_grad()
```

```
        loss.backward()
```

```
        ### UPDATE MODEL PARAMETERS  
        optimizer.step()
```

```
    model.eval()  
    with torch.no_grad():  
        # compute accuracy
```

For evaluation, set the model to eval mode (will be relevant later when we use Dropout or BatchNorm)

This prevents the computation graph for backpropagation from automatically being build in the background to save memory

Simple “print” statements don’t work for debugging

```
[7]: model.net

[7]: Sequential(
  (0): Linear(in_features=784, out_features=128, bias=True)
  (1): ReLU(inplace)
  (2): Linear(in_features=128, out_features=256, bias=True)
  (3): ReLU(inplace)
  (4): Linear(in_features=256, out_features=10, bias=True)
)

[ ]: If we want to get the output from the 2nd layer during the forward pass, we can register a hook as follows:

[8]: outputs = []
def hook(module, input, output):
    outputs.append(output)

model.net[2].register_forward_hook(hook)

[8]: <torch.utils.hooks.RemovableHandle at 0x7f659c6685c0>

Now, if we call the model on some inputs, it will save the intermediate results in the "outputs" list:

[9]: _ = model(features)

print(outputs)

[tensor([[0.5341, 1.0513, 2.3542, ..., 0.0000, 0.0000, 0.0000],
        [0.0000, 0.6676, 0.6620, ..., 0.0000, 0.0000, 2.4056],
        [1.1520, 0.0000, 0.0000, ..., 2.5860, 0.8992, 0.9642],
        ...,
        [0.0000, 0.1076, 0.0000, ..., 1.8367, 0.0000, 2.5203],
        [0.5415, 0.0000, 0.0000, ..., 2.7968, 0.8244, 1.6335],
        [1.0710, 0.9805, 3.0103, ..., 0.0000, 0.0000, 0.0000]],
        device='cuda:3', grad_fn=<ThresholdBackward1>)]
```

Questions?

