

concordance=TRUE

# Pol Sci 630: Problem Set 4 Solution - Regression Model Estimation

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## 1 Subset data frame

### 1.1 Download data

Download the following data from WDI and clean it as follows. Briefly comment on what each command does.

```
library(WDI)

## Loading required package: RJSONIO

d_wdi <- WDI(indicator = c("NY.GDP.PCAP.CD", "SP.DYN.IMRT.IN", "SH.MED.PHYS.ZS"),
             start = 2005, end = 2010, extra = TRUE)
d_wdi <- d_wdi[d_wdi$region != "Aggregates",
              c("country", "year", "NY.GDP.PCAP.CD", "SP.DYN.IMRT.IN", "SH.MED.PHYS.ZS")]
colnames(d_wdi)[3:5] <- c('gdppc', 'infant_mortality', 'number_of_physician')
d_wdi <- na.omit(d_wdi)
```

infant\_mortality: number of mortality per 1000 live births  
number\_of\_physician: number of physician per 1000 people

### 1.2 Subsetting

Use subsetting techniques to do the following:

1. Show the GDP per capita of Brazil across years
2. Show the country-years where infant mortality > 100 per 1000 live birth
3. Show the country-years where GDP per capita is above average
4. Show the country-years where GDP per capita is above average, but number of physician is below average

## Solution

```
library(WDI)

# Download data from WDI, specifying the indicators and start / end year
d_wdi <- WDI(indicator = c("NY.GDP.PCAP.CD", "SP.DYN.IMRT.IN", "SH.MED.PHYS.ZS"),
             start = 2008, end = 2010, extra = TRUE)

# Remove aggregates rows, selecting wanted columns by name
d_wdi <- d_wdi[d_wdi$region != "Aggregates",
              c("country", "year", "NY.GDP.PCAP.CD", "SP.DYN.IMRT.IN", "SH.MED.PHYS.ZS")]

# Rename some of the columns
colnames(d_wdi)[3:5] <- c('gdppc', 'infant_mortality', 'number_of_physician')

# Remove all rows that have missing data
d_wdi <- na.omit(d_wdi)
```

```
# 1. Show the GDP per capita of Brazil across years
d_wdi[d_wdi$country == "Brazil", c("country", "year", "gdppc")]

##      country year      gdppc
## 94  Brazil 2008  8706.819
## 95  Brazil 2009  8474.881
## 96  Brazil 2010 11121.421

# 2. Show the country-years where infant mortality > 100 per 1000 live birth
d_wdi[d_wdi$infant_mortality > 100, c("country", "year", "infant_mortality")]

##      country year infant_mortality
## 34          Angola 2009           112.2
## 119 Central African Republic 2008           105.5
## 120 Central African Republic 2009           103.6
## 568         Sierra Leone 2010           107.0
## 570         Sierra Leone 2008           116.2

# 3. Show the country-years where GDP per capita is above average
d_wdi[d_wdi$gdppc > mean(d_wdi$gdppc), c("country", "year", "gdppc")]

##      country year      gdppc
## 16          Andorra 2009  42701.45
## 17          Andorra 2010  39639.39
## 19 United Arab Emirates 2009  32905.05
## 20 United Arab Emirates 2008  45720.02
## 21 United Arab Emirates 2010  34341.91
## 44          Austria 2010  46659.84
```

## 46	Australia 2009	42715.13
## 47	Australia 2010	51845.65
## 63	Barbados 2010	15901.43
## 67	Belgium 2010	44382.88
## 68	Belgium 2008	48424.59
## 76	Bahrain 2010	20386.02
## 77	Bahrain 2008	23043.03
## 78	Bahrain 2009	19166.71
## 88	Brunei Darussalam 2009	27726.48
## 89	Brunei Darussalam 2010	31453.22
## 90	Brunei Darussalam 2008	37798.39
## 99	Bahamas, The 2008	23657.37
## 112	Canada 2008	46596.34
## 114	Canada 2010	47445.76
## 124	Switzerland 2010	74277.12
## 154	Cyprus 2008	34950.35
## 155	Cyprus 2009	31673.46
## 156	Cyprus 2010	30438.90
## 157	Czech Republic 2010	19763.96
## 158	Czech Republic 2008	22649.38
## 160	Germany 2010	41788.04
## 162	Germany 2008	45699.20
## 166	Denmark 2010	57647.67
## 167	Denmark 2009	57895.50
## 168	Denmark 2008	64181.99
## 181	Estonia 2008	18094.55
## 183	Estonia 2010	14641.40
## 190	Spain 2009	32333.47
## 191	Spain 2010	30737.83
## 192	Spain 2008	35578.74
## 202	Finland 2010	46205.17
## 203	Finland 2008	53401.31
## 204	Finland 2009	47107.16
## 214	France 2008	45413.07
## 215	France 2010	40705.77
## 222	United Kingdom 2010	38292.87
## 247	Greece 2010	26919.36
## 248	Greece 2008	31997.28
## 268	Croatia 2008	15893.86
## 275	Hungary 2008	15649.72
## 280	Ireland 2008	61189.73
## 282	Ireland 2010	48260.67
## 283	Israel 2010	30736.36
## 298	Iceland 2010	41620.07
## 299	Iceland 2008	55229.61

## 300	Iceland	2009	40362.04
## 301	Italy	2009	36976.85
## 302	Italy	2010	35851.51
## 303	Italy	2008	40640.18
## 313	Japan	2010	42935.25
## 315	Japan	2008	37865.62
## 337	Korea, Rep.	2008	20474.89
## 338	Korea, Rep.	2010	22151.21
## 339	Korea, Rep.	2009	18338.71
## 340	Kuwait	2009	36754.95
## 341	Kuwait	2008	54484.30
## 342	Kuwait	2010	37725.14
## 371	Lithuania	2008	14961.57
## 373	Luxembourg	2010	103267.28
## 377	Latvia	2008	16323.77
## 381	Libya	2008	14231.60
## 425	Malta	2010	19694.08
## 426	Malta	2009	19636.01
## 460	Netherlands	2010	50341.25
## 462	Netherlands	2008	56928.82
## 463	Norway	2010	87646.27
## 464	Norway	2009	80017.78
## 465	Norway	2008	96880.51
## 472	New Zealand	2009	28200.94
## 473	New Zealand	2008	31287.61
## 474	New Zealand	2010	33692.17
## 478	Oman	2009	17518.83
## 479	Oman	2010	19920.65
## 480	Oman	2008	22963.38
## 501	Poland	2008	13906.22
## 508	Portugal	2008	24815.61
## 509	Portugal	2010	22540.00
## 510	Portugal	2009	23063.97
## 517	Qatar	2008	82990.07
## 518	Qatar	2010	70870.23
## 519	Qatar	2009	61463.90
## 544	Saudi Arabia	2008	19436.86
## 545	Saudi Arabia	2009	15655.08
## 546	Saudi Arabia	2010	18753.98
## 556	Sweden	2008	55746.84
## 557	Sweden	2010	52076.43
## 558	Sweden	2009	46207.06
## 559	Singapore	2009	38577.56
## 560	Singapore	2010	46569.68
## 561	Singapore	2008	39721.05

```
## 562          Slovenia 2010 23438.85
## 564          Slovenia 2008 27501.82
## 565      Slovak Republic 2009 16460.22
## 566      Slovak Republic 2010 16554.88
## 650  Trinidad and Tobago 2010 15840.44
## 664          United States 2010 48374.09
## 665          United States 2009 47001.56
## 666          United States 2008 48401.43

# 4. Show the country-years where GDP per capita is above average,
# but number of physician is below average
d_wdi[d_wdi$gdppc > mean(d_wdi$gdppc) &
      d_wdi$number_of_physician < mean(d_wdi$number_of_physician),
      c("country", "year", "gdppc")]

##          country year   gdppc
## 76          Bahrain 2010 20386.02
## 77          Bahrain 2008 23043.03
## 78          Bahrain 2009 19166.71
## 88  Brunei Darussalam 2009 27726.48
## 89  Brunei Darussalam 2010 31453.22
## 90  Brunei Darussalam 2008 37798.39
## 341           Kuwait 2008 54484.30
## 561          Singapore 2008 39721.05
## 650  Trinidad and Tobago 2010 15840.44
```

## 2 Build linear model

### 2.1 Download

Download 2 variables of interest and build a linear model of their relationship using `lm()`. Show the `summary()` of results.

### 2.2 Calculate the regression coefficients WITHOUT using ‘lm’

Use the mathematical formula of the regression coefficients you saw in class and implement it in R. Is this result the same as the result output by ‘lm’?

### 2.3 Model output

Show the result with `stargazer`, customizing:

- The labels of the independent variables (i.e. the covariate)

- The label of the dependent variable
- Make the model name (i.e. OLS) show up

Hint: The options to do those things are in `help(stargazer)`. I have worded the task in a way that should help you find the relevant options.

### Solution

Build the linear model

```
m1 <- lm(infant_mortality ~ gdppc, data = d_wdi)
summary(m1)

##
## Call:
## lm(formula = infant_mortality ~ gdppc, data = d_wdi)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -27.697 -16.248  -6.166   11.606   80.199
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  3.633e+01  1.384e+00   26.25  <2e-16 ***
## gdppc        -7.307e-04  5.933e-05  -12.32  <2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 20.9 on 350 degrees of freedom
## Multiple R-squared:  0.3024, Adjusted R-squared:  0.3004
## F-statistic: 151.7 on 1 and 350 DF, p-value: < 2.2e-16
```

Calculate the regression coef by hand, using covariance and variance:

```
cov(d_wdi$infant_mortality, d_wdi$gdppc) / var(d_wdi$gdppc)

## [1] -0.00073073
```

or fully by hand (the result will be slightly different because R's 'cov' and 'var' divided by 'n - 1' while 'mean' divides by 'n') (read more at [http://nebula.deanza.edu/~bloom/math10/m10divideby\\_nminus1.pdf](http://nebula.deanza.edu/~bloom/math10/m10divideby_nminus1.pdf)):

```
mean((d_wdi$infant_mortality - mean(d_wdi$infant_mortality)) *
      d_wdi$gdppc - mean(d_wdi$gdppc)) /
mean((d_wdi$gdppc - mean(d_wdi$gdppc))**2)

## [1] -0.0007699624
```

```
library(stargazer)

##
## Please cite as:
## Hlavac, Marek (2015). stargazer: Well-Formatted Regression and
## Summary Statistics Tables.
## R package version 5.2. http://CRAN.R-project.org/package=stargazer

stargazer(m1,
  covariate.labels = c("GDP per capita"),
  dep.var.labels = c("Infant Mortality (per 1000 births)"),
  model.names = TRUE)
```

Table 1:

	<i>Dependent variable:</i>
	Infant Mortality (per 1000 births)
	<i>OLS</i>
GDP per capita	−0.001*** (0.0001)
Constant	36.332*** (1.384)
Observations	352
R <sup>2</sup>	0.302
Adjusted R <sup>2</sup>	0.300
Residual Std. Error	20.905 (df = 350)
F Statistic	151.705*** (df = 1; 350)
<i>Note:</i>	*p<0.1; **p<0.05; ***p<0.01

### 3 Calculate sum of squares and RMSE

1. Extract the residuals and predicted values (fitted values) from the model object (from the linear model built above)
2. Calculate three “sum of squares” (TSS, RegSS, RSS)
3. Calculate the root mean square error and compare with R. (In R and stargazer, RMSE is called “Residual standard error”.)



Note: the data you feed to `lm()` may have missing data, so R has to modify the data a little before using it. To extract the data that are actually used by `lm()`, use `my_model$model`. Use this data to calculate  $\bar{y}$  in the sum of squares.

#### Solution

```
res <- m1$residuals # Residuals
pred <- m1$fitted.values # Predicted values
y <- m1$model$infant_mortality # Data of Y that is used by lm()

# Calculate 3 sum of squares
TSS <- sum( (y - mean(y)) ** 2)
RegSS <- sum( (pred - mean(y)) ** 2)
RSS <- sum( res ** 2 )

# Calculate root mean square error
N <- nrow(d_wdi)
k <- 1 # We only have 1 predictor, which is log_gdppc
rmse <- sqrt(RSS / (N - k - 1))
```

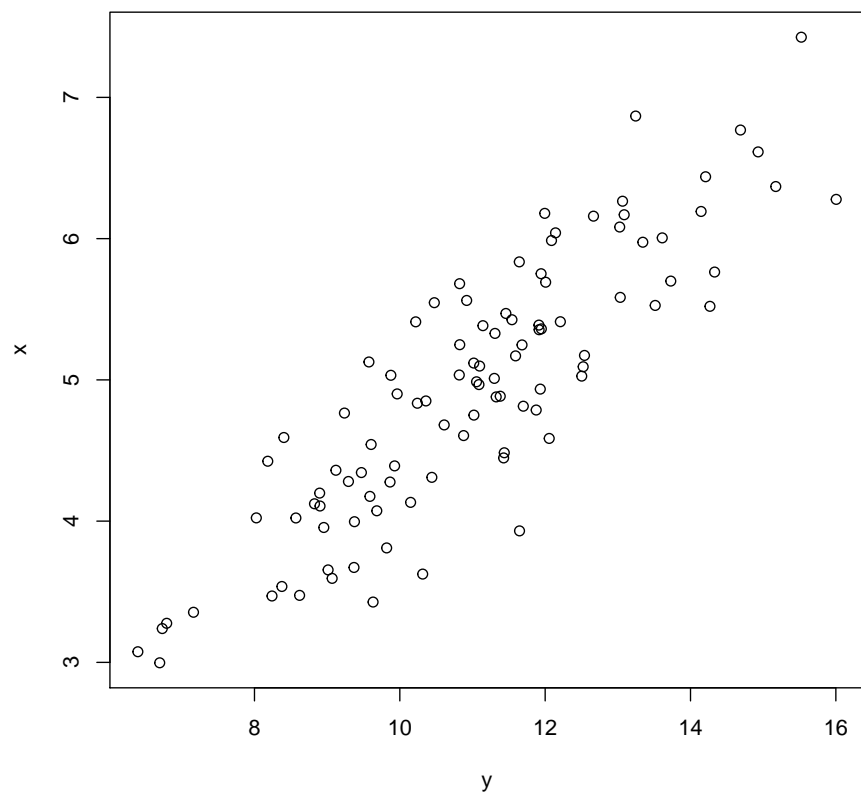
The calculated root mean square error is 20.9048032, the same as reported by R in `summary(m1)`.

## 4 Explore why we have standard errors

```
x <- rnorm(mean = 5, 100)
y <- 1 + 2 * x + rnorm(100)
plot(y, x)

c_nsim <- 100
model_data <- vector("list", length = c_nsim)
model_results <- vector("list", length = c_nsim)
for (i in 1:c_nsim) {
  sample_index <- sample(100, 10, replace = TRUE)
  sample_x <- x[sample_index]
  sample_y <- y[sample_index]
  model_data[[i]] <- list(sample_x, sample_y)
  model_results[[i]] <- lm(sample_y ~ sample_x)
}

plot(y, x)
```



```
for (i in 1:c_nsim) {  
  }  
}
```