

Cryptography for Privacy-Preserving Machine Learning

PhD Defense · Théo Ryffel

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Paris

Your everyday life... is fueled with ML



Morning music



Route planning



Email filtering



Automatic translation

Machine Learning

Definition of Machine Learning

The process of computers changing the way they carry out tasks by **learning from new data, without** a human being needing to give **instructions in the form of a program** - *Cambridge Dictionary*

Example

Classify a skin tumor as benign or cancerous => no simple rules

ML in healthcare?

ML in Marketing
(2018)



ML in Healthcare
(2018)

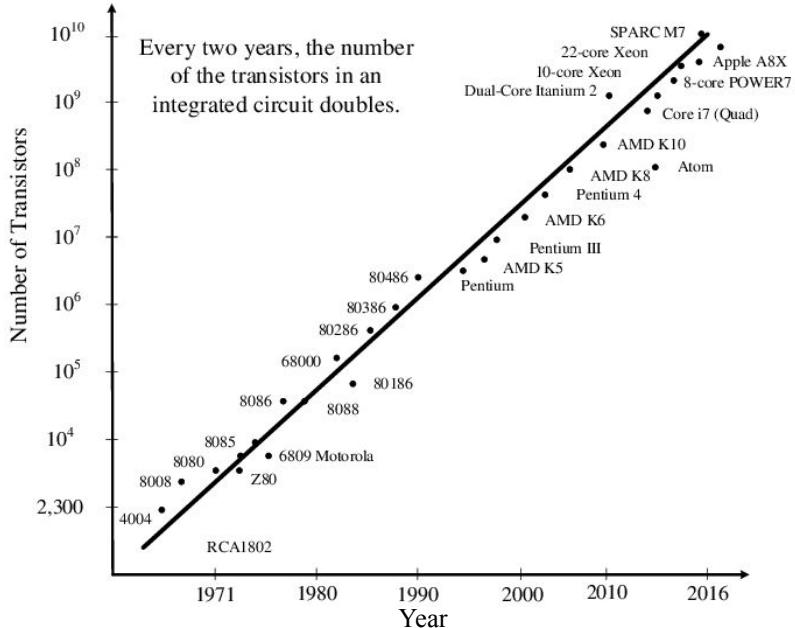


Refs. <https://www.marketresearchfuture.com/> <https://www.marketsandmarkets.com/>

Machine Learning

Machine Learning needs powerful processors and data in large quantities

Moore's Law



Imagenet (2009)



Contextual Integrity [Nis04]

Contextual Integrity (CI)

Privacy is respected when an **information flow** from one individual to another via a dedicated channel is **appropriate**, with respect to the sender, the recipient, the person concerned, the type of information and the transmission principle.

Remarks

- Not only about one's own information => not secrecy
- Positive definition: information flows => collaboration
- Ethical dimension

Contextual Integrity [Nis04]

Example which satisfies Contextual Integrity:

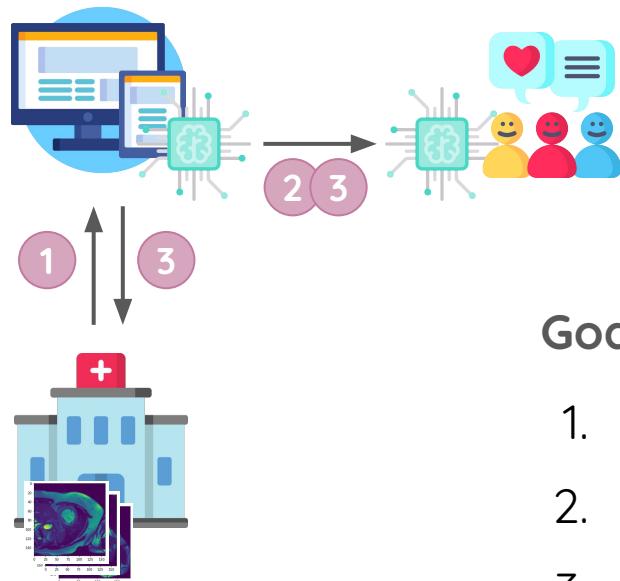
A patient sends their own medical report to their doctor via a secure messaging system



What if you replace:

- doctor *by* employer ?
- secure messaging app *by* public communication channel ?
- their own medical report *by* the one of a relative ?

Privacy-preserving ML through the prism of CI



Motivation:

Explore how privacy enhancing technologies can provide contextual integrity to machine learning workflows.

Goals:

1. Data used for training should not directly be exposed
2. ML models trained should not disclose private data
3. ML models should not be disseminated or exposed

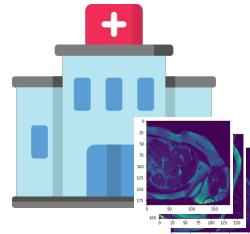
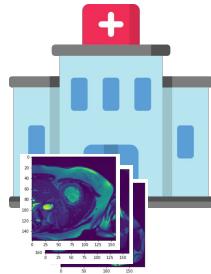
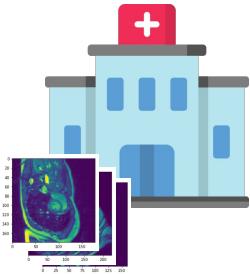
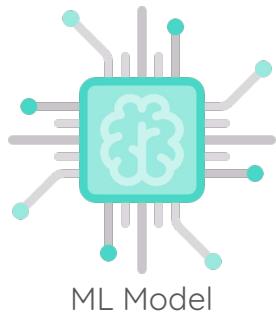
Privacy-preserving ML through the prism of CI

- 1 Federated Learning (and attacks on models)
- 2 Differential Privacy
- 3 Encrypted Computation

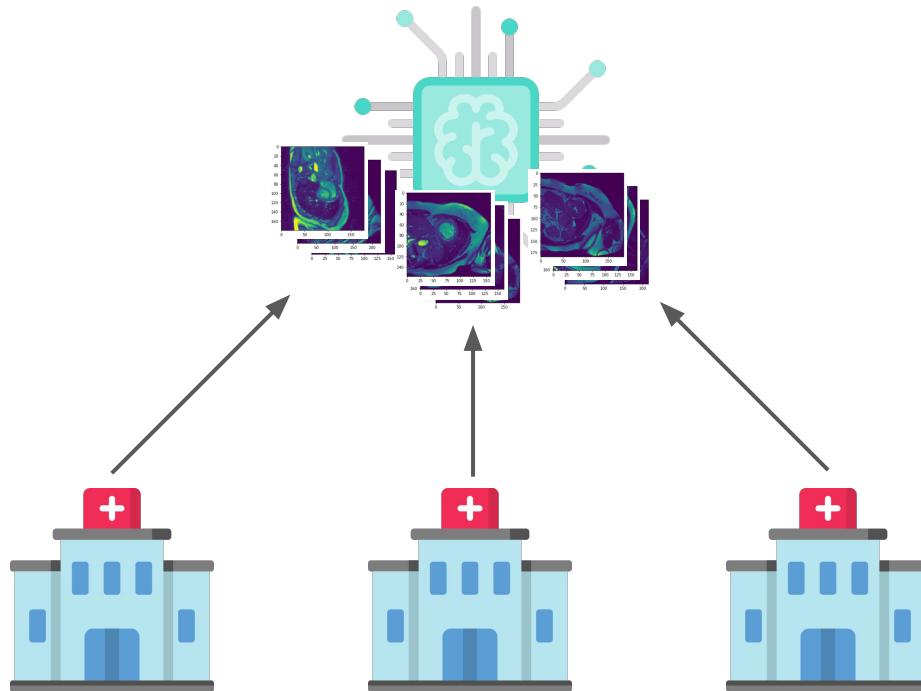
1

Federated Learning (and attacks on models)

Federated Learning [MMR+17]



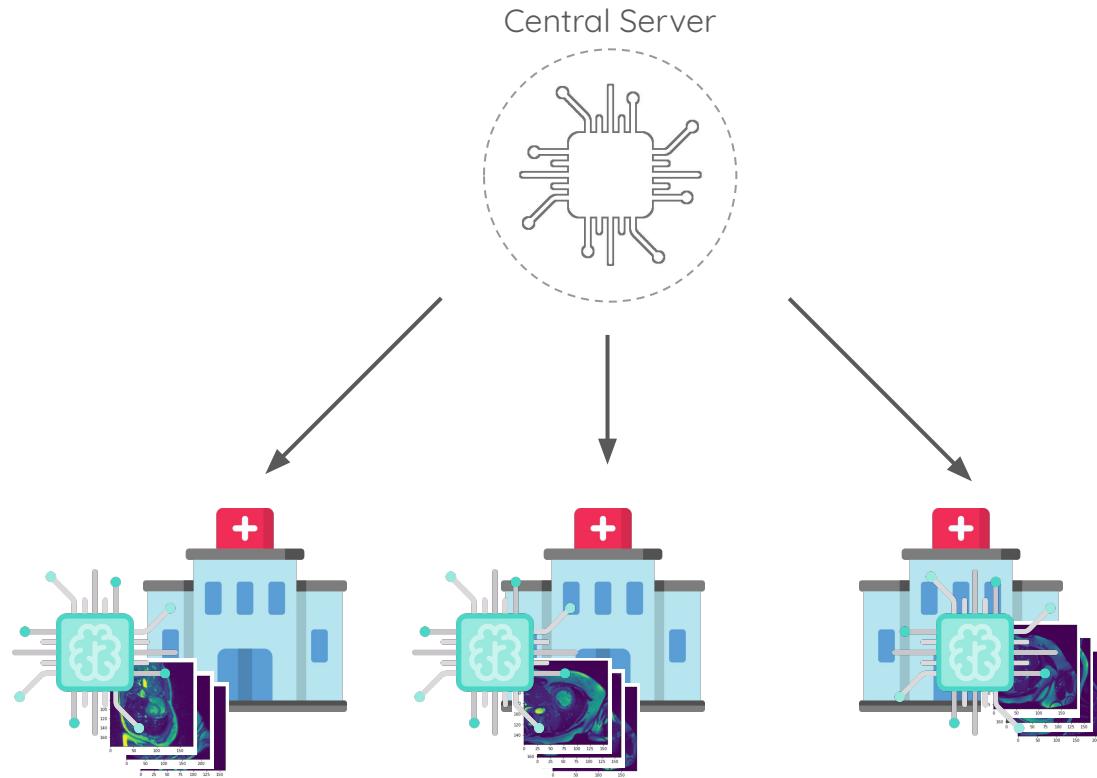
Federated Learning



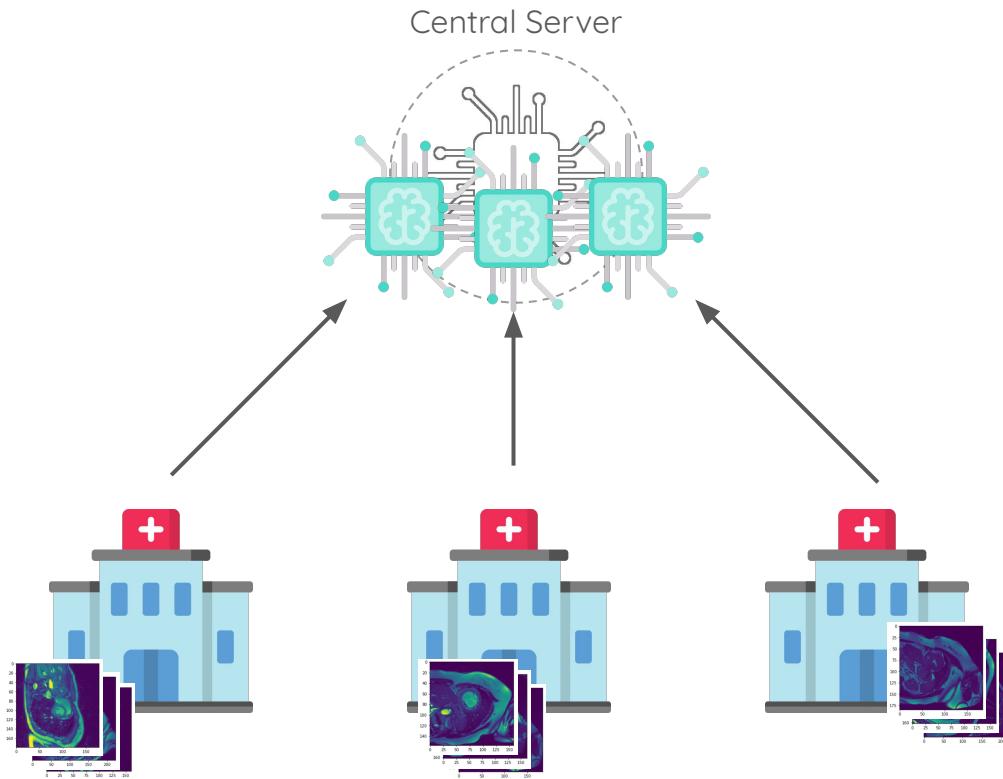
Current situation

- ! No sovereignty nor control on how data is used
- ! Important quantity of data to store

Federated Learning



Federated Learning



Benefits



Sovereignty over data



Transparency on computations

Our contribution:



PySyft [RTD+18]

Federated Learning <> Contextual Integrity



Personal data used for training should not be directly exposed



ML models should not disclose private training data



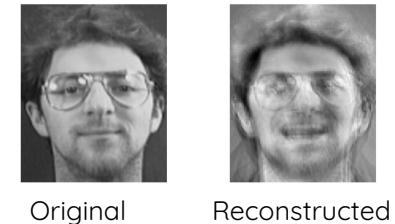
ML models should not be disseminated or exposed

Threats against ML models

Example #1: Model inversion

1. On a fully trained network [FJR15]

Black box setting



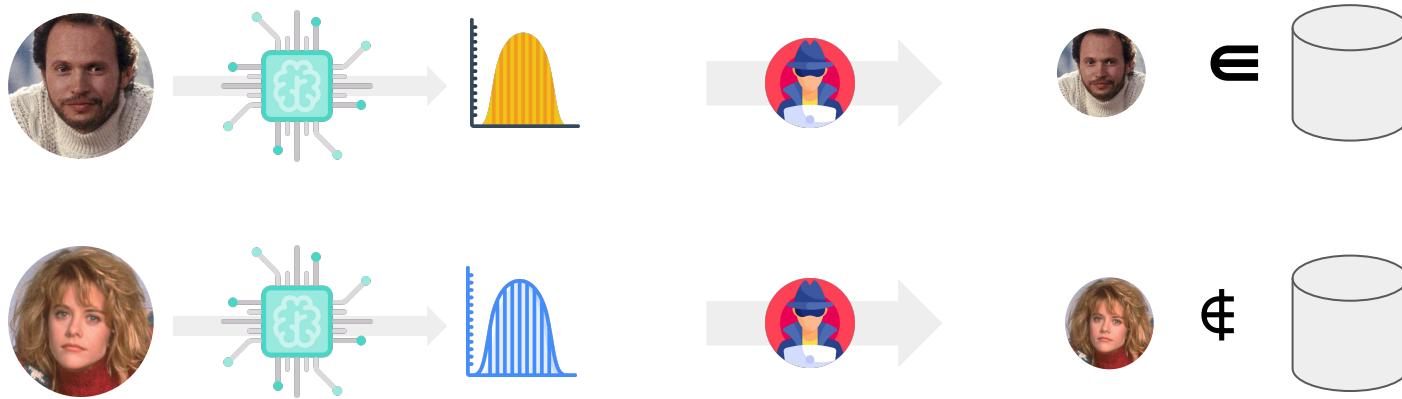
2. During a federated training [GBDM20]

Attack by the central server, white box setting



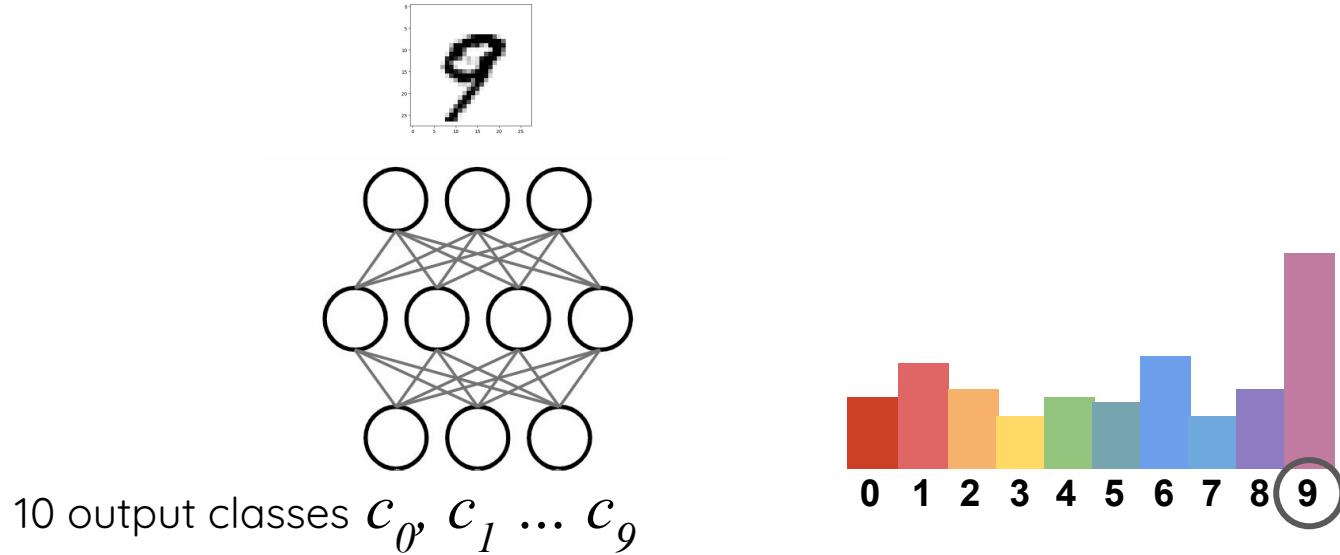
Threats against ML models

Example #2: Membership Inference [SSSS17]



Threats against ML models

Our contribution: “Collateral Learning” [RPB+19]



Collateral Learning [RPB+19]

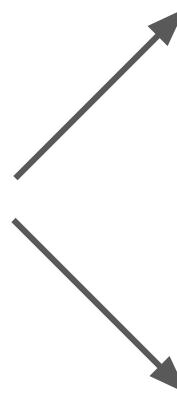
A dataset with two classification tasks

[1] (cursive) [0] (Georgia) [4] (cursive)

1 0 4

[3] (cursive) [1] (Georgia) [2] (Georgia)

3 1 2



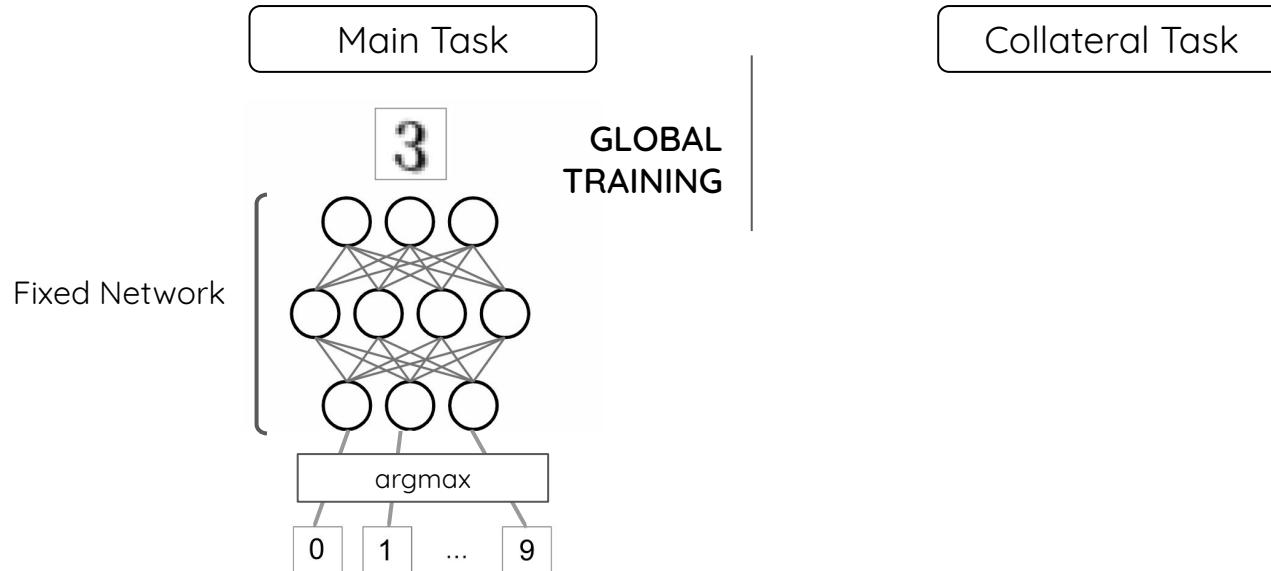
Main Task

1	0	4
3	1	2

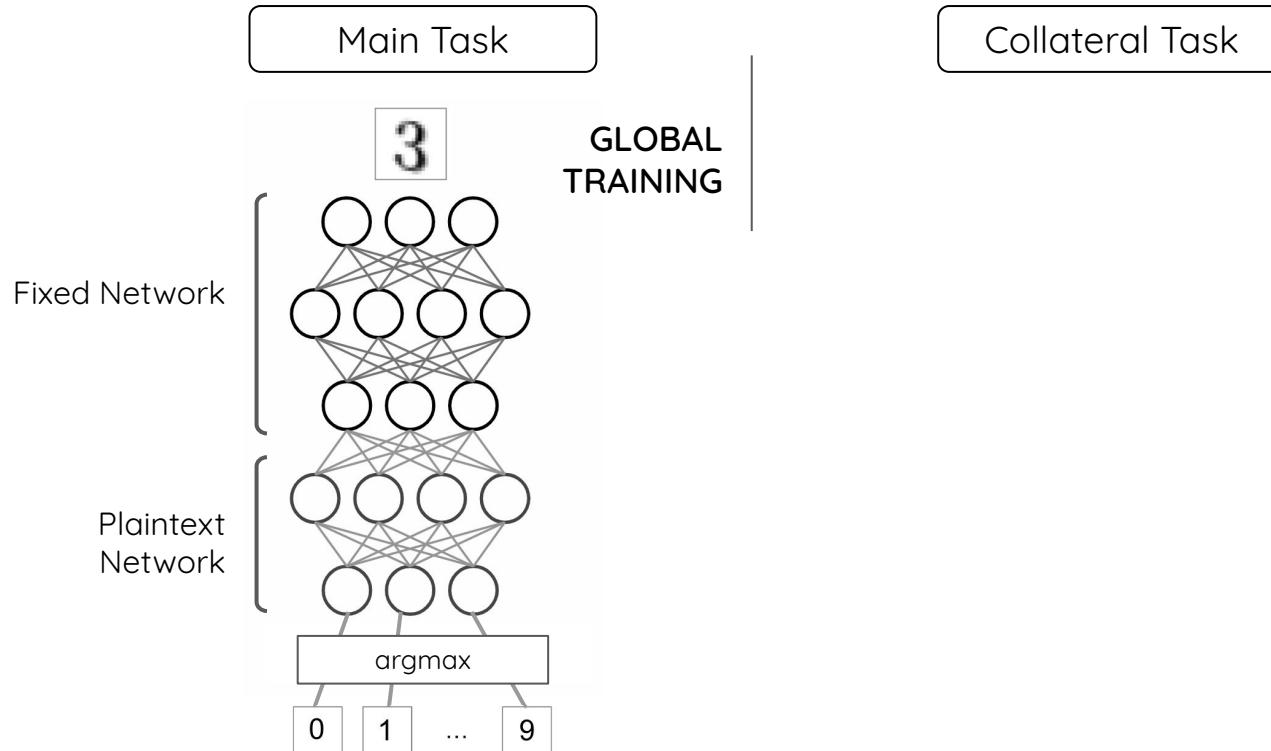
Collateral Task

cursive	georgia	cursive
cursive	georgia	georgia

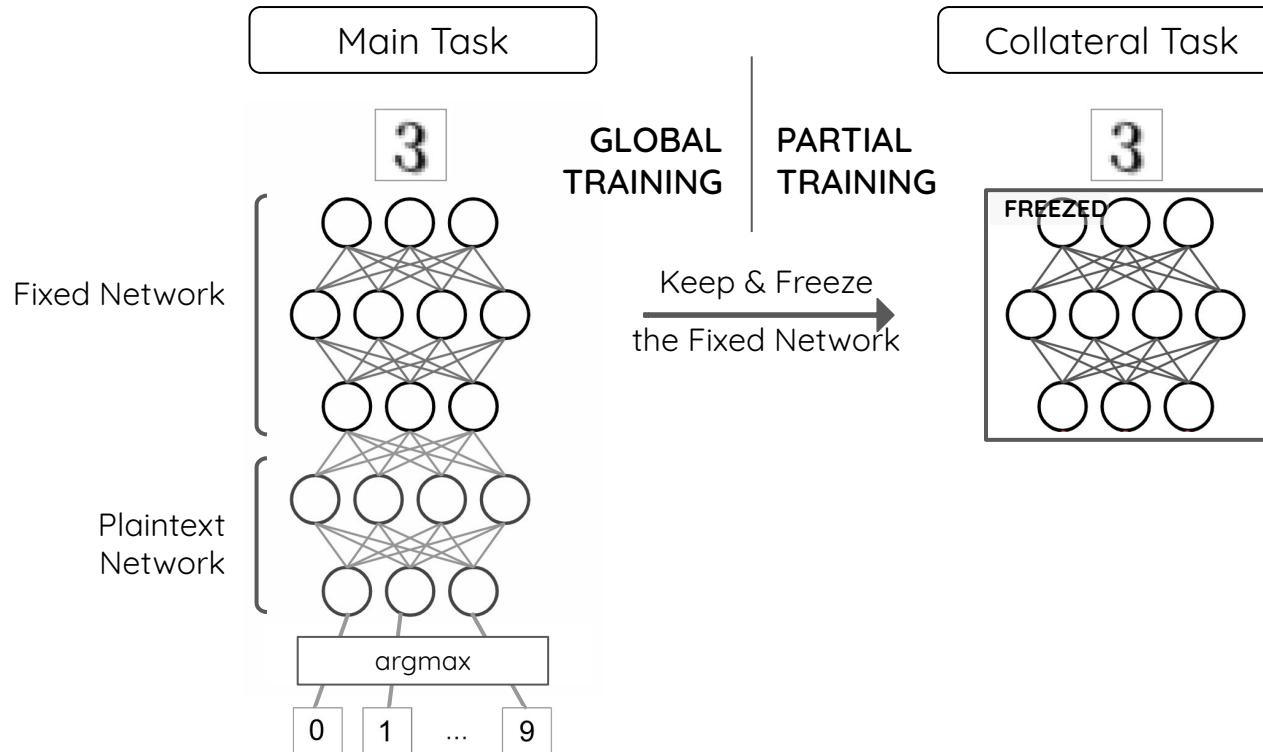
Collateral Learning [RPB+19]



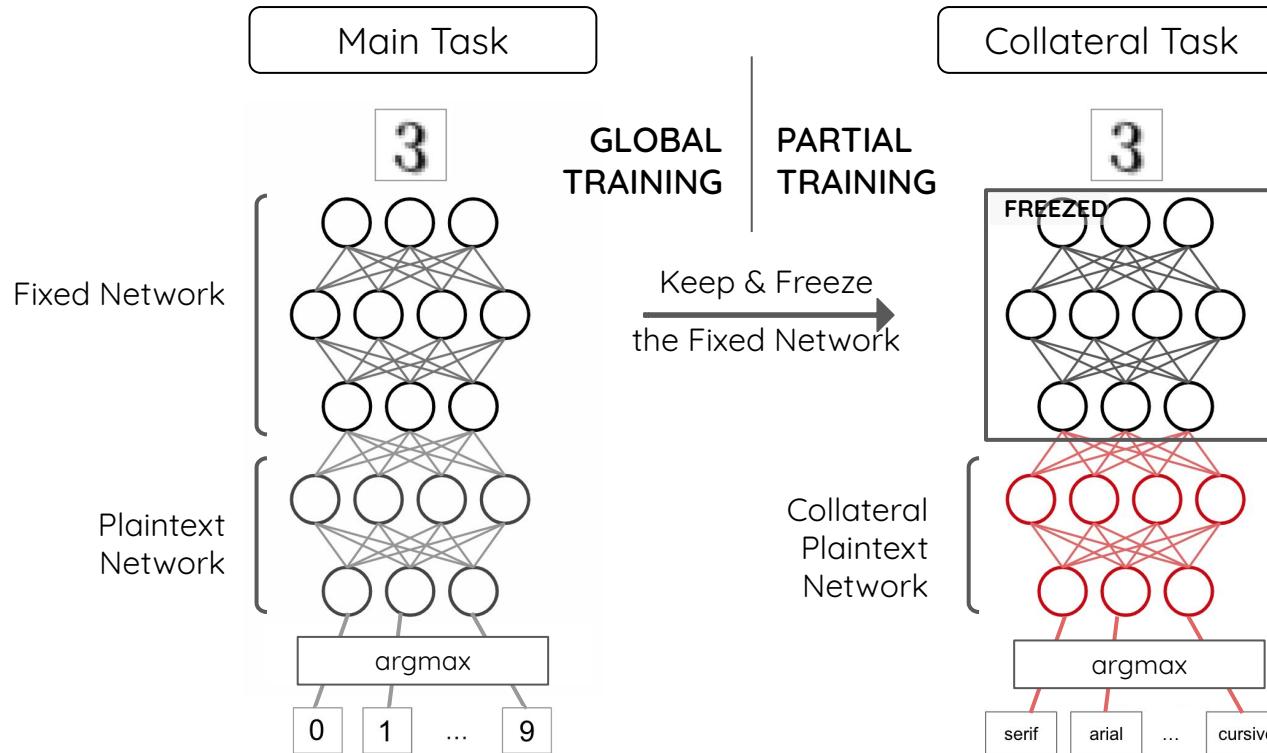
Collateral Learning [RPB+19]



Collateral Learning [RPB+19]



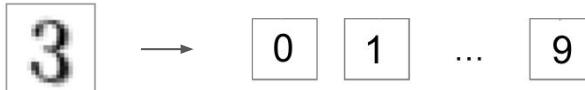
Collateral Learning [RPB+19]



Collateral Learning [RPB+19]

The collateral task achieves a high accuracy

Main Task



Collateral Task



Random baseline	10%
Accuracy with a CNN	99,1%

Random baseline	20%
Accuracy with a CNN	93.5%

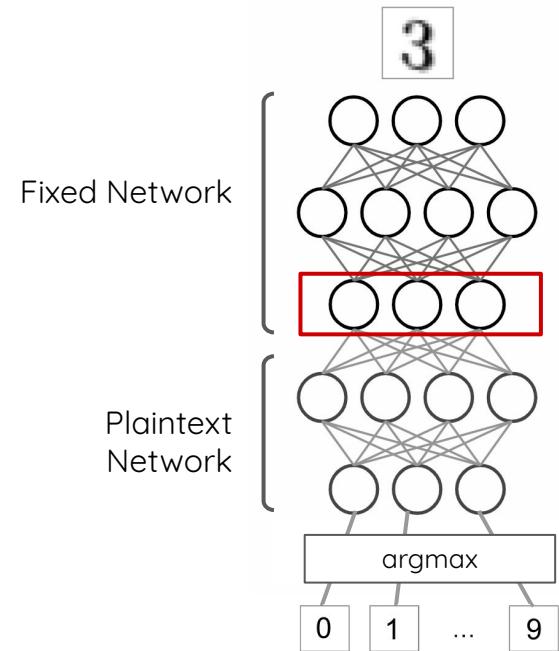
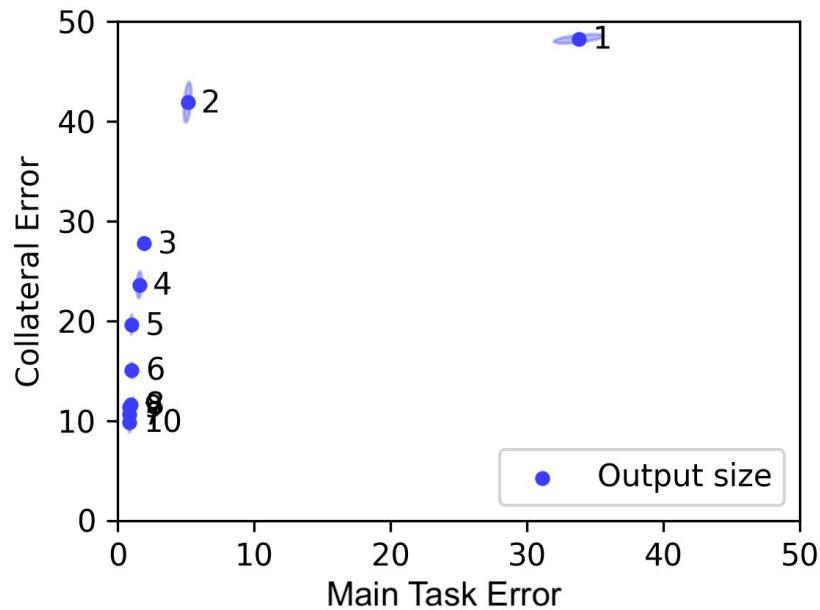
Implication of Collateral Learning



What solution can we propose?

Collateral learning [RPB+19]

Mitigation #1: reducing the fixed network output

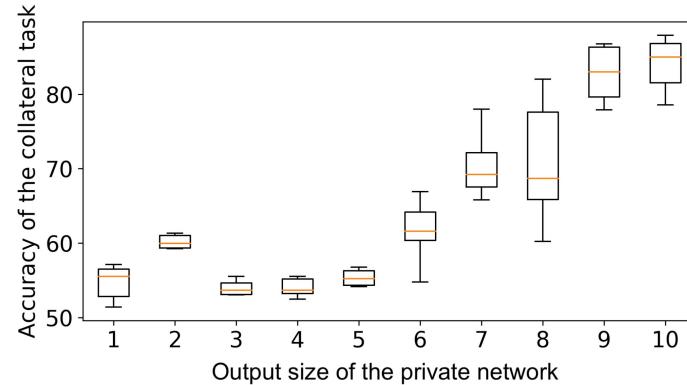
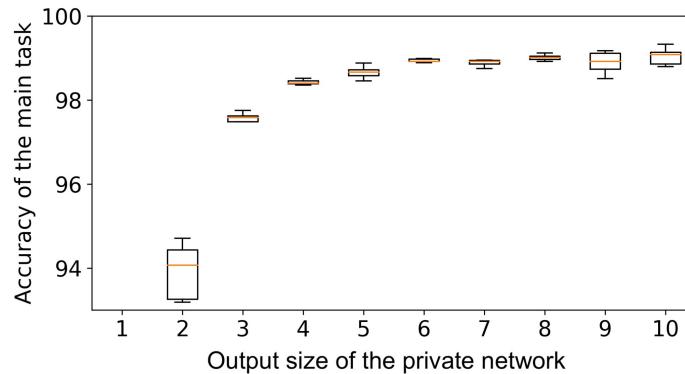


Collateral learning [RPB+19]

Mitigation #2: Adversarial learning [DDSV04] against a simulated adversary

Perform a joint optimisation using the loss that we imagine an adversary would try to optimize:

$$L_{joint} = L_{main} - \alpha \cdot L_{collateral}$$



Collateral learning [RPB+19]

Mitigation #2: Adversarial learning against a simulated adversary

Accuracy of an attacker to distinguish between 2 fonts, using different classifiers.

Linear Ridge Regression	$53.5 \pm 0.5\%$
Logistic Regression	$52.5 \pm 0.6\%$
Quad. Discriminant Analysis	$54.9 \pm 0.3\%$
SVM (RBF kernel)	$57.9 \pm 0.4\%$
Gaussian Process Classifier	$53.8 \pm 0.3\%$
Gaussian Naive Bayes	$53.2 \pm 0.5\%$
K-Neighbors Classifier	$58.1 \pm 0.7\%$
Decision Tree Classifier	$56.8 \pm 0.4\%$
Random Forest Classifier	$58.9 \pm 0.2\%$
Gradient Boosting Classifier	$58.9 \pm 0.2\%$

(Baseline: 50%)

2

Differential Privacy

Intuition



Mean with bob: 1567

Mean without bob: 1620

Deduction of bob's salary: $1567 * 6 - 1620 * 5 = 1300$

Objective: to ensure that statistical analysis does not compromise the privacy of individuals

Analyse: function(data) *example : mean of salaries*

Perfect confidentiality: the result of the query is indistinguishable if you add or remove a single individual in the dataset



If you add noise to the calculation, it becomes difficult to determine Bob's salary or even if Bob is part of the dataset

(ϵ, δ) -Differential Privacy [DMNS06]

A randomized algorithm \mathcal{A} satisfies (ϵ, δ) -differential privacy if for any datasets \mathcal{D} and \mathcal{D}' only differing in one item, we have:

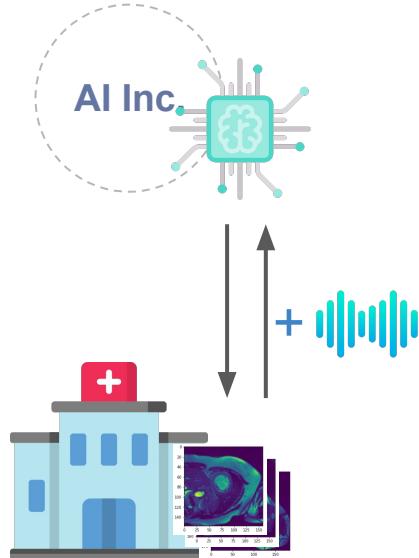
$$P[\mathcal{A}(\mathcal{D}) \in S] \leq e^\epsilon P[\mathcal{A}(\mathcal{D}') \in S] + \delta$$



Privacy budget (ϵ, δ) “small” => increased privacy

Differential Privacy

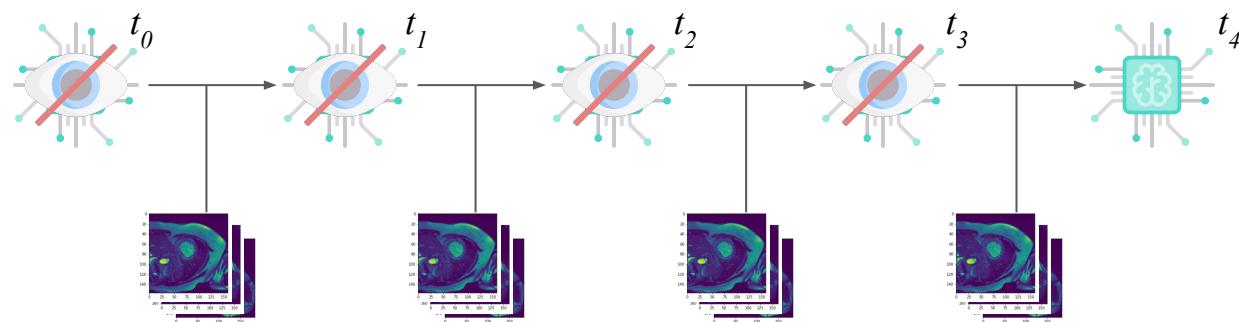
Differentially Private Stochastic Gradient Descent (DP-SGD) [BST14]



- Works by adding Gaussian noise on the model updates
- Limited access to data for a given privacy budget
- More noise: better privacy budget but worse model utility => **trade-off**

Stochastic Gradient Langevin Dynamics [RBP22]

Our working hypothesis: DP-SGD assumes that the model is public at each iteration. If we can hide the model during training and only disclose it at the end, less information should leak.



Stochastic Gradient Langevin Dynamics [RBP22]

Extension of [CYS21] which leverages Langevin diffusion to achieve:

- Exponentially fast convergence of the privacy (instead of \sqrt{K})
- Under smooth and strongly convex objectives
- For full gradient descent

Our contribution: a stochastic version more practical for ML users [RBP22]

Differential Privacy <> Contextual Integrity



Personal data used for training should not be directly exposed



ML models should not disclose private training data

The model is sanitized to prevent attacks like model inversion or membership attack

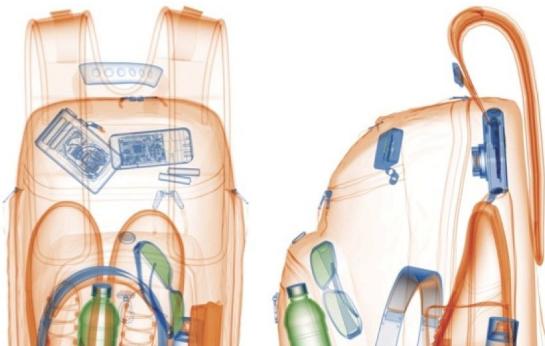


ML models should not be disseminated or exposed

The model is still shared directly to the data owners => IP issue

Differential Privacy <> Contextual Integrity

Example of risk on the model: Airport X-ray security scan



3

Encrypted Computation

Overview of available methods

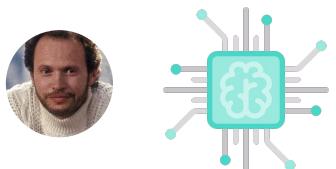
The ML model should be “encrypted”, meaning **usable but not visible**

Several methods:

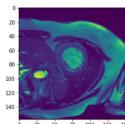
- Homomorphic Encryption
- Functional Encryption
- Secure Multi-Party Computation

Homomorphic Encryption

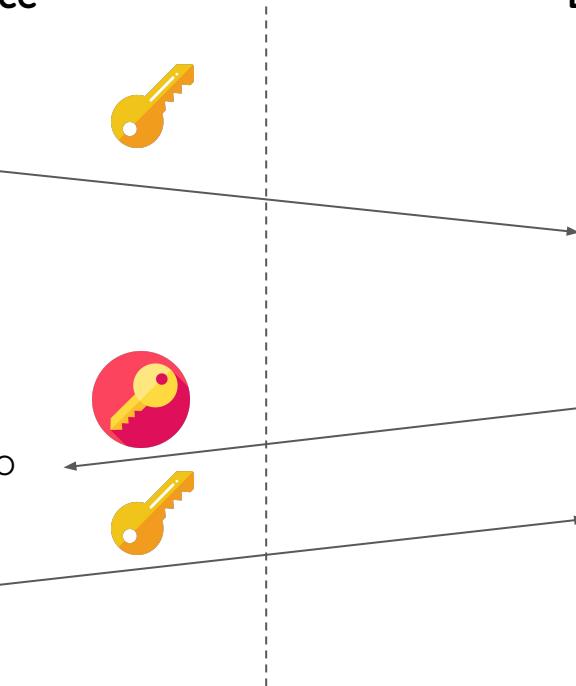
Non-encrypted space



Encrypted space

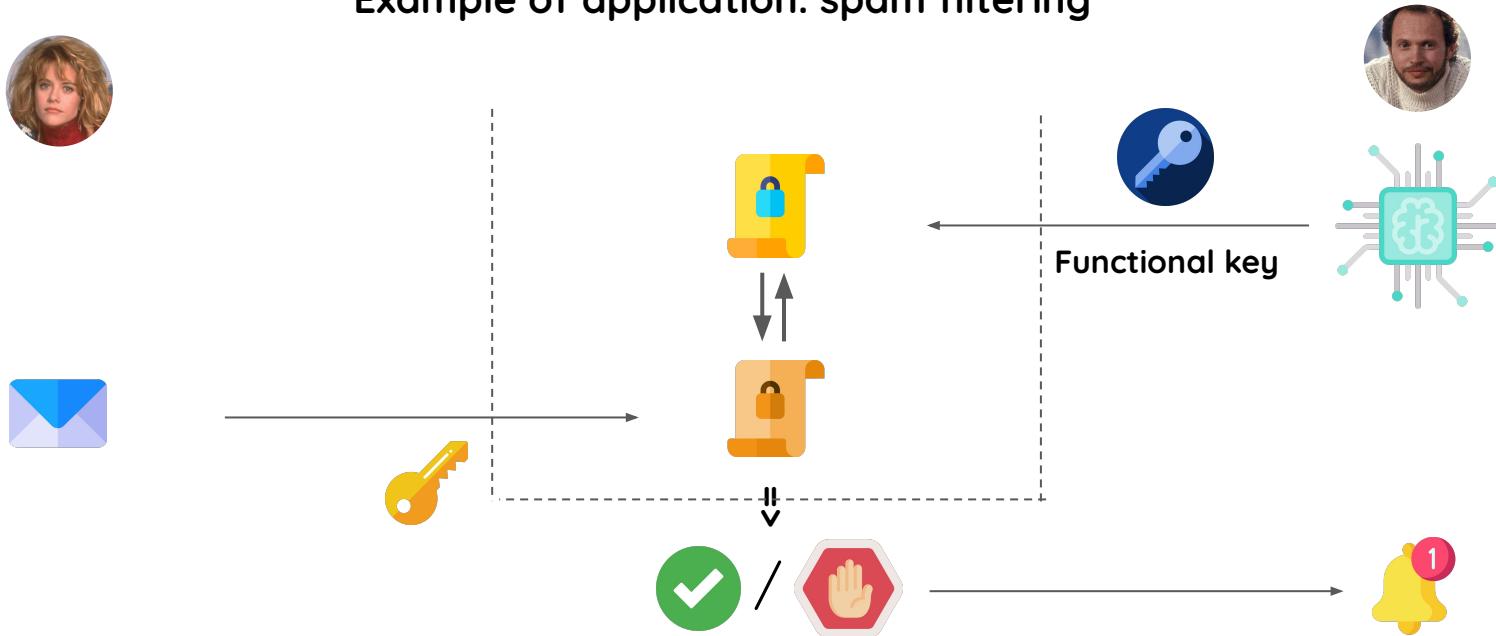


Yes/No



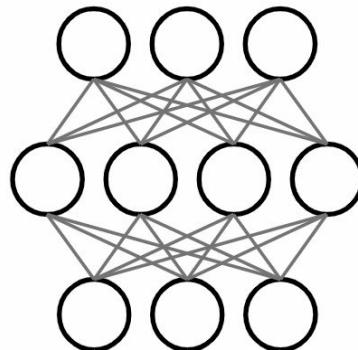
Functional Encryption

Example of application: spam filtering



A Quadratic Functional Encryption Scheme

Our contribution: Extension of [DGP18], the functional scheme can be viewed as a neural network with one hidden layer and a square activation. [RPB+19]



[1] (cursive) [0] (Georgia) [4] (cursive)



[3] (cursive) [1] (Georgia) [2] (Georgia)

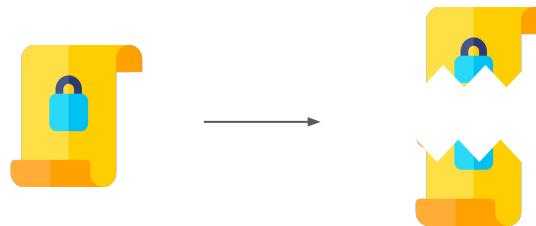


Secure Multi-Party Computation

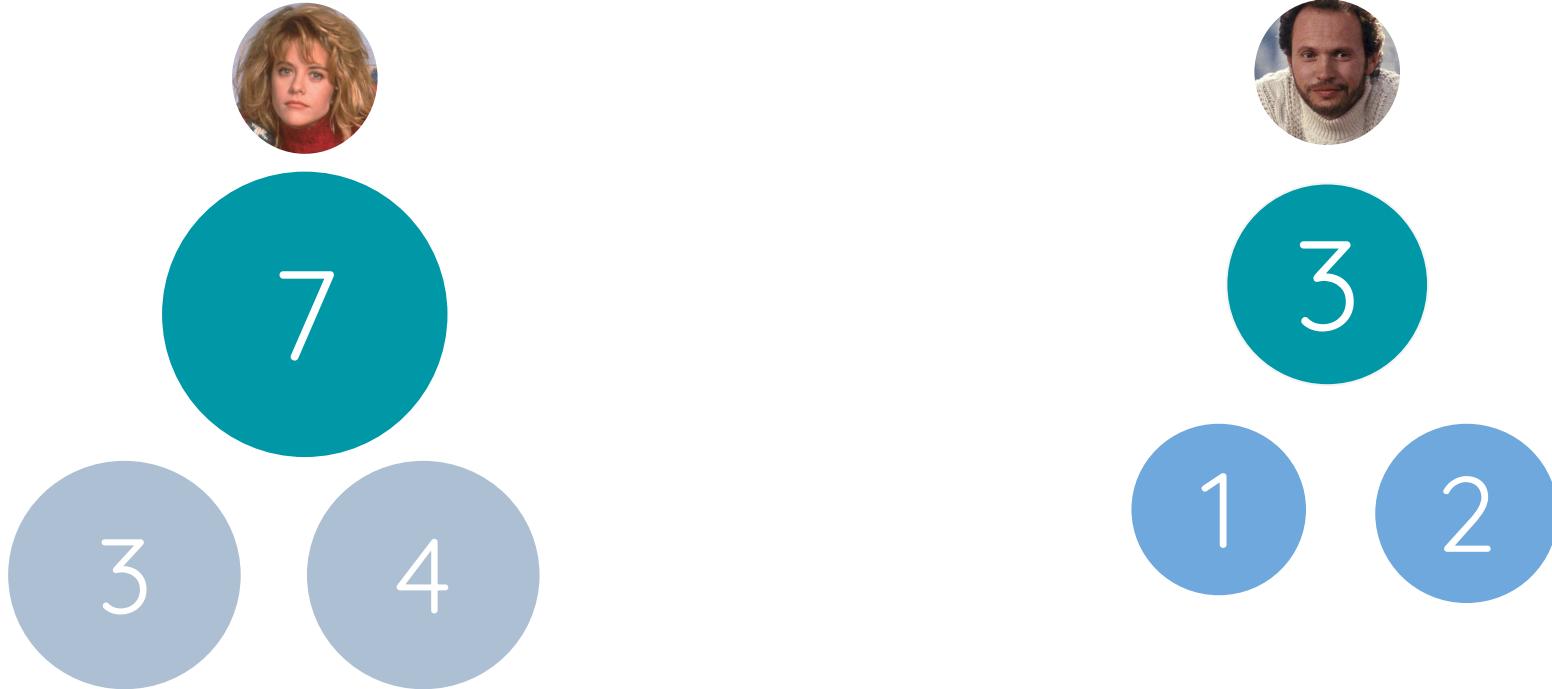
Definition

The set of methods for parties to jointly compute a function over their inputs while keeping those inputs private.

Focus on additive secret-sharing:



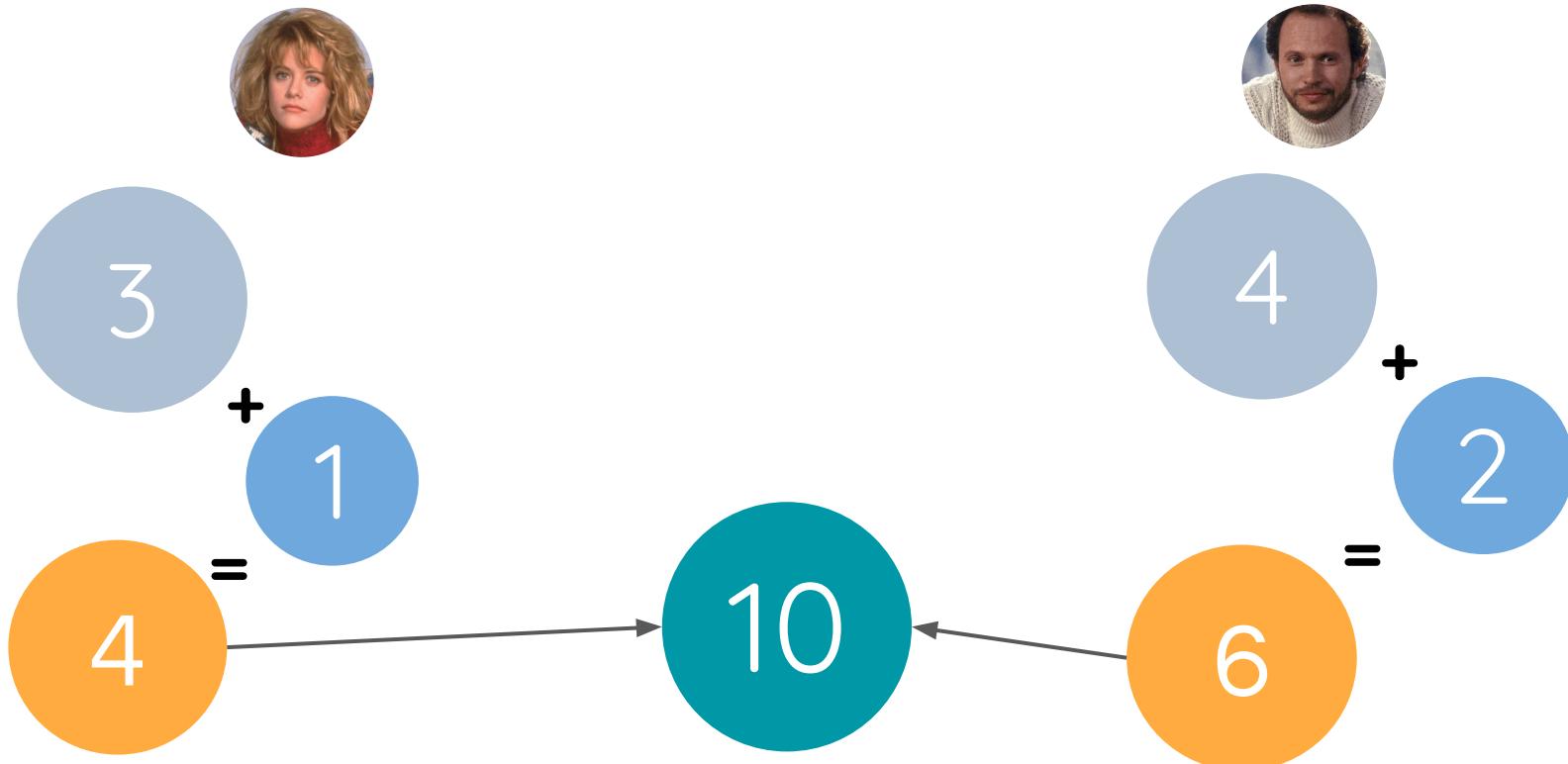
Additive Secret Sharing



Additive Secret Sharing



Additive Secret Sharing



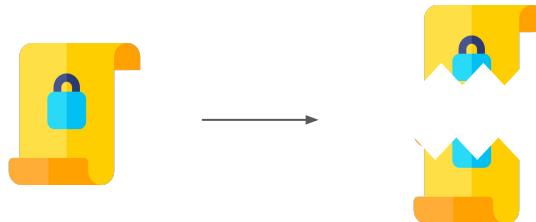
Additive Secret Sharing

Secret sharing: no single party can reconstruct sensitive data alone

Shared governance: data can only be used or decrypted if everyone agrees

Additive Secret Sharing

Data and models can be secret shared in the same way



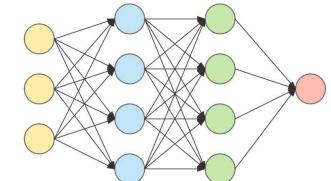
Operations needed for ML models

- Addition (already seen)
- Multiplication & matrix multiplication (not very difficult)
- **Comparisons**

Additive Secret Sharing

$$x \quad f \longrightarrow f(x)$$

Example $f: x \mapsto x \geq 0$



Function Secret Sharing [BGI15]

A different perspective

 $\llbracket x \rrbracket_0$ \prod_f  $\llbracket x \rrbracket_1$

Additive Secret Sharing



$$[\![x]\!]_0 \quad \prod_f$$



$$[\![x]\!]_1 \quad \prod_f$$

Additive Secret Sharing



$$\begin{array}{ccc} \llbracket x \rrbracket_0 & \prod_{f \in \Sigma} & \longrightarrow & \llbracket f(x) \rrbracket_0 \\ & & & & \Sigma \quad f(x) \end{array}$$



$$\begin{array}{ccc} \llbracket x \rrbracket_1 & \prod_{f \in \Sigma} & \longrightarrow & \llbracket f(x) \rrbracket_1 \end{array}$$

Function Secret Sharing

A different perspective



$$[\![f]\!]_0$$

x



$$[\![f]\!]_1$$

Function Secret Sharing

A different perspective



$$\begin{array}{ccc} x & \xrightarrow{\quad \llbracket f \rrbracket_0 \quad} & \llbracket f \rrbracket_0(x) \\ x \nearrow & & \\ x & \xrightarrow{\quad \llbracket f \rrbracket_1 \quad} & \Sigma f(x) \\ \searrow & & \\ & & \llbracket f \rrbracket_1(x) \end{array}$$

Example $f: x \mapsto x \geq \alpha$

Function Secret Sharing

A different perspective

$$\begin{array}{ccc} \llbracket y \rrbracket_0 + \llbracket \alpha \rrbracket_0 & \xrightarrow{x} & \llbracket f \rrbracket_0 \longrightarrow \llbracket f \rrbracket_0(x) \\ \Sigma \quad x \quad \swarrow \quad \searrow & & \Sigma \quad f(x) \\ \llbracket y \rrbracket_1 + \llbracket \alpha \rrbracket_1 & \xrightarrow{x} & \llbracket f \rrbracket_1 \longrightarrow \llbracket f \rrbracket_1(x) \end{array}$$
$$x \geq \alpha \Rightarrow y \geq 0 \text{ with } x = y + \alpha$$

Secure Comparison with Function Secret Sharing

[RTPB22]

Reminder on the binary notation:

$$x = x_1 x_2 \dots x_n = \sum 2^{n-k} \cdot x^k$$

Example:

$$n = 3, \quad x = 010_2 = 4 \cdot 0 + 2 \cdot 1 + 1 \cdot 0 = \\ 2$$

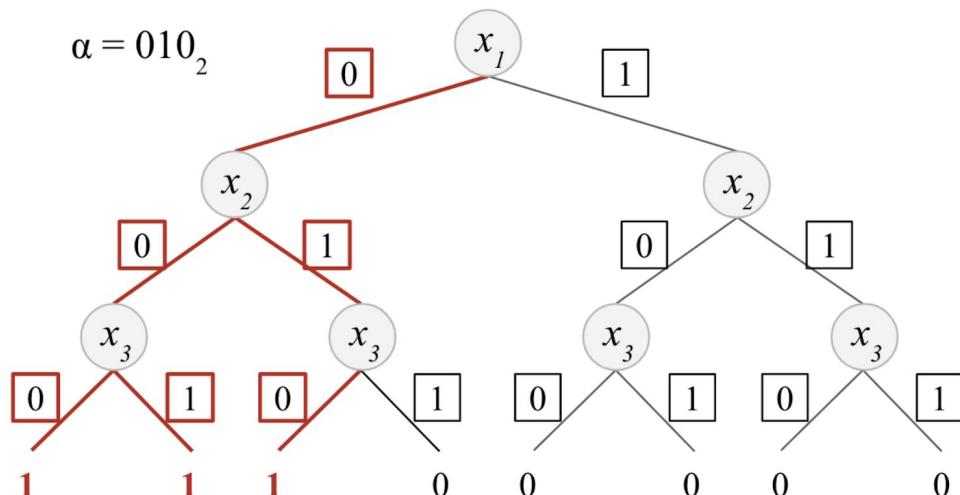
Using the bit notation, x and α write:

$$x = x_1 x_2 \dots x_n, \quad \alpha = \alpha_1 \alpha_2 \dots \alpha_n$$

Secure Comparison with Function Secret Sharing

Example with $n = 3$ of $x \leq \alpha$

[RTPB22]



Bit per bit private comparison

For each k from 1 to n

- if $x_k > \alpha_k$, then $x \leq \alpha$ is false
- if $x_k < \alpha_k$, then $x \leq \alpha$ is true
- if $x_k = \alpha_k$, then we need to compare the bit $k + 1$ to decide

Secure Comparison with Function Secret Sharing

Correctness & Security of our protocol [RTPB22]

- Honest but curious, 2 party computation with trusted dealer
- Small error rate (that can be avoided with extra computation) => [BCG+21]

Secure Comparison with Function Secret Sharing [RTPB22]

Why FSS is promising for private ML

Pros

- Enjoys the efficiency of MPC protocols (only light cryptographic primitives)
- Can be run on GPUs
- Considerably reduces the number of communication rounds compared to other MPC protocols: 1 for private comparison

Cons

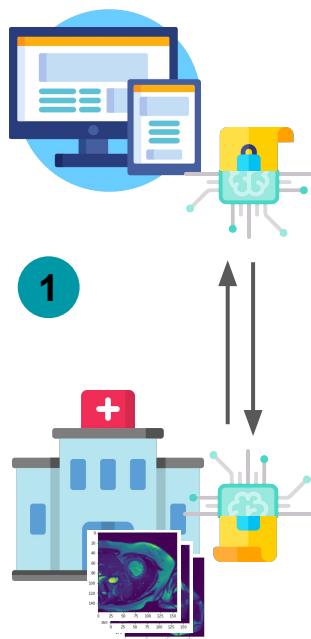
- Requires big preprocessing keys (correlated random strings)
size of key of a 32 bits integer comparison $\sim 32 \lambda$ bits

Example: 224x224 image through ResNet-18

3311620 comparisons $\Rightarrow \sim 1.7$ Go per key

Machine Learning with Function Secret Sharing

AriaNN - Private training using Function Secret Sharing [RTPB22]



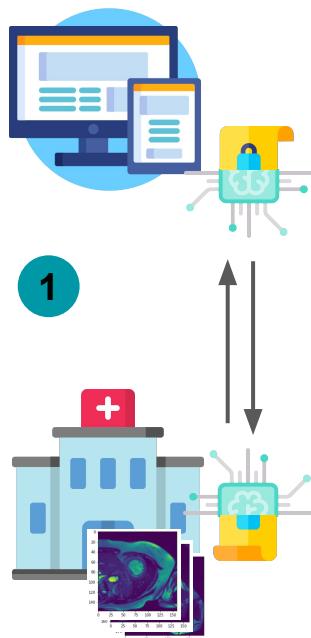
Dataset	Model	Accuracy (%)	Time / epoch (h)
28x28 MNIST	Linear	98.0	0.8
28x28 MNIST	LeNet	99.2	4.2



github.com/OpenMined/sycret

Machine Learning with Function Secret Sharing

AriaNN - Private evaluation using Function Secret Sharing [RTPB22]



Dataset	Model	Time over LAN using CPU (s)	Time over LAN using GPU (s)
32x32 CIFAR10	AlexNet	0.15	0.078
32x32 CIFAR10	VGG16	1.75	1.55
224x224 Imagenet	ResNet18	19.9	13.9



github.com/OpenMined/sycret

Machine Learning with Function Secret Sharing

Study using AriaNN for private evaluation [KZPR+21]



End-to-end privacy preserving deep learning on multi-institutional medical imaging



Function Secret Sharing used for Secure inference-as-a-service, a scenario where latency matters



To evaluate privately a neural network at expert level accuracy

Function Secret Sharing <> Contextual Integrity



Personal data used for training should not be directly exposed



ML models should not disclose private training data

If differential privacy is used



ML models should not be disseminated or exposed

Additional remarks

- Only honest but curious security
- Model not visible during training: condition for the DP methods exposed
=> allows powerful combinations

4

Conclusion

Conclusions & Perspectives

- Impact on the run-time or accuracy: the use of PETs depends on the context, hence the concept of contextual integrity
- Cross domain research: a challenge and an opportunity
- Need for user-friendly open-source implementations to accelerate awareness
- Real life data needs intensive cleaning and structuration to be useable, this can't be done once data is encrypted
- Also a social, political, legal and economic challenge

Acknowledgments

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Bibliography (our contributions)

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