

Unit-I

b (a) Inverse, converse and contrapositive of $A \rightarrow B$

→ Define an inverse function with a suitable example

→ Define set

→ Types of Quantifiers

→ Show that $(\forall x)(H(x) \rightarrow M(x)) \wedge H(s) \Rightarrow M(s)$

→ If the universe of the discourse is the set $\{a, b, c\}$

Eliminate the quantifier from $(\forall x)R(x)$

→ Draw Venn diagram of $A \cap B^c$

→ Implication; modus Ponens; modus Tollens

→ Define contrapositive statement

→ Define Venn diagram with the help of an example

→ Define cardinality of set

→ Different types of sets definitions

→ Laws; Domain & range; 6 types of relations

→ Equivalence relation

→ Function; one-one; onto; Bijective; inverse

→ Propositional logic

→ 4 types of fundamental logic

→ Tautology, Contradiction, Contingency

→ Subject; predicate; Quantifiers & their types

→ What are the 9 methods of proof of an implication

Unit-2

- Sum rule, Product rule
- Permutation, combination differences
- Principle of inclusion, exclusion & Pigeonhole principle
- Problems on Permutation & combination

1. Compute the no. of subcommittees of 3 members each that can be formed from a committee with 25 members: $25C_3$

2. There are 15 married couples in a party. In how many ways we can select a man & woman such that they are unmarried together: $15C_1 = 15$

(ii) Not married together: 15×14

3. In how many ways can 10 people arrange themselves in a ring: $(10-1)! = 9!$

4. Find the no. of arrangements of TALLAHASSEE = $\frac{11!}{3! 2! 2! 2!}$

5. How many elements are there in $A_1 \cup A_2$ if $|A_1| = 12$,

$|A_2| = 18$ & $A_1 \subseteq A_2$?

$$n(A_1 \cup A_2) = n(A_1) + n(A_2) - n(A_1 \cap A_2) = 12 + 18 - 12 = 18$$

Formulas:

$$n(A_1 \cup A_2) = n(A_1) + n(A_2) - n(A_1 \cap A_2)$$

$$n(A_1 \cup A_2 \cup A_3) = n(A_1) + n(A_2) + n(A_3) - n(A_1 \cap A_2) - n(A_1 \cap A_3) - n(A_2 \cap A_3) + n(A_1 \cap A_2 \cap A_3)$$

Unit-3

→ Define recurrence relation & explain its types

→ Define generating function.

→ Examples for General form of second order linear homogeneous recurrence relation.

$$C_0(n) a_{n-0} + C_1(n) a_{n-1} + C_2(n) a_{n-2} = 0 ; n \geq 2$$

→ Coefficient of x^{12} in $x^3(1-2x)^{10}$

Sol: Binomial $(x+y)^n = \sum_{r=0}^n {}^nC_r \cdot x^{n-r} y^r$

$$x^3(1-2x)^{10} = x^3(1+(-2x))^{10}$$

$$x=1, y=-2x, n=10$$

$$\Rightarrow x^3 \sum_{r=0}^{10} {}^{10}C_r \cdot (-2x)^r$$

$$\text{At } r=9$$

$$\Rightarrow x^3 {}^{10}C_9 (-2x)^9 \Rightarrow -2^9 {}^{10}C_9 x^{12}$$

$$\therefore \text{Coefficient of } x^{12} = -2^9 {}^{10}C_9$$

→ Generating function for $e_1 + e_2 + \dots + e_n = r ; 0 \leq e_i \leq 1$

$$A(x) = (1+x)^n$$

→ Explain divide & conquer recurrence relation

& All formulas in Unit-3