



**MAULANA ABUL KALAM AZAD UNIVERSITY OF  
TECHNOLOGY, WESTBENGAL  
Odd Semester Examinations 2023-24**

**Paper Code: PCC-CS503**

**Paper Name: Formal Language & Automata Theory**

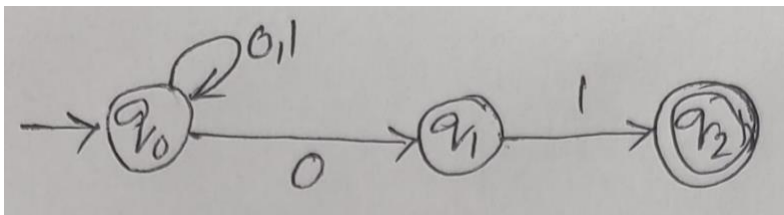
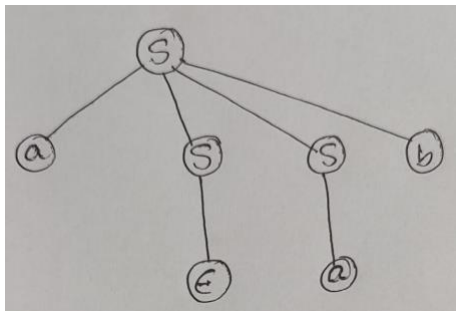
**Time Allotted: 3 Hours**

**Full Marks: 70**

Answer all questions.

**Special Instructions :( If any)**

SI	Questions	Marks	Mapped CO	Mapped PO	Bloom' s
<b>Group A</b>					
1.(a)	To simplify CFG's following operations are performed. I. Remove useless symbols II. Remove epsilon-productions/lambda-productions III. Remove unit productions The order to perform these operations is (a) I, II, III (b) II, I, III (c) II, III, I (d) III, II, I	1	CO4		L1
1.(b)	Consider the following grammar: $S \rightarrow AE \mid SB$ $A \rightarrow bSEa$ $B \rightarrow aSB \mid bBE$ $E \rightarrow aBE \mid ad$ Which of the following is/are non-generating symbol(s)? (a) S (b) A (c) E (d) B	1	CO4		L3
1.(c)	Pumping lemma for regular languages is used to check whether a given regular language is finite or not. (a) TRUE (b) FALSE	1	CO3		L1
1.(d)	CFL's are closed under complement. (a) TRUE (b) FALSE	1	CO3		L1
1.(e)	LBA's are same as TM. (a) TRUE (b) FALSE	1	CO3		L1
1.(f)	$S \rightarrow aBc$ $aB \rightarrow cA$ $Ac \rightarrow d$ The above grammar is (a) Unrestricted (b) Context free (c) Regular (d) Context sensitive	1	CO2		L3

1.(g)	Determining whether a string $w$ belongs to $L(M)$ , where $M$ is a TM, is undecidable. (a) TRUE (b) FALSE	1	C O 1	L1
1.(h)	$L(ab^*ba^*) \cup L(ba^*ab^*) = \epsilon$ (epsilon). (a) TRUE (b) FALSE	1	C O 1	L3
1.(i)	Turing machines (TM) are "hardwired" i.e., they execute only one program. (a) TRUE (b) FALSE	1	C O 1	L1
1.(j)	Consider the following CFG $X \rightarrow XY$ $X \rightarrow zX \mid bX \mid a$ $Y \rightarrow Ya \mid Yb \mid b$ Any string of terminals, which can be generated by the CFG (a) Has at least one $b$ (b) Ends with $a$ (c) Has no consecutive $a$ 's or $b$ 's (d) Has at least two $a$ 's	1	C O 1	L3
<b>Group B</b>				
2	a) Compute $\delta^*(q_0, 00101)$ by using recursive formula for $\delta^*$ [show each step clearly].  	5	C O 3	L3
OR	b) Convert the following regular expression into an $\epsilon$ -NFA. By using Ken Thompson method. Show each step clearly. $a^* \mid b^* \mid c^*$	5	C O 3	L3
3	a) Consider the following derivation tree:    Find a simple grammar $G$ for which this is the derivation tree of the string $aab$ . Then find two more sentences of $L(G)$ .	5	C O 1	L3
OR	b) Consider the grammar $S \rightarrow aaB$ $B \rightarrow Aa$ $A \rightarrow bBb \mid \epsilon$ Show that the string $aabbabba$ is not in the language generated by this grammar.	5	C O 1	L3
4	a) Convert the following CFG into CNF. $E \rightarrow (E) \mid E + E \mid EE \mid -E \mid 0 \mid 1$	5	C O 5	L3
OR	b) Convert the following CFG $G$ into a PDA $M$ with no final states such that $L(M) = L(G)$ . $S \rightarrow aBAa \mid aBB$ $A \rightarrow bA \mid Bb$ $B \rightarrow dB \mid d$	5	C O 5	L3

Group C					
5A	a) Give the complete hierarchy of grammars with their recognizers as well as the form of production rules.	7	C O 2		L1
	b) Design a TM to add two numbers $x$ and $y$ .	8	C O 6		L6
OR 5B	a) Using Chomsky hierarchy, find the highest type number (Type-0/Type-1/Type-2/Type-3 grammar) which can be applied on the following grammars. Justify your answer. i) $S \rightarrow Aa, A \rightarrow d \mid Ba, B \rightarrow abd$ ii) $S \rightarrow ASB \mid d, A \rightarrow aA$ iii) $AAbdD \rightarrow abdDbdD$ iv) $A \rightarrow abA$	7	C O 2		L3
	b) Design a TM to compute $f(x) = 2x$ .	8	C O 6		L6
6A	Draw an NFA which accepts a string containing "the" anywhere in a string of $\{a-z\}$ e.g., "there" but not "those". Convert the NFA to a minimized DFA by using the concept of distinguishability states.	3+ 6+ 6	C O 3 , C O 4		L2
OR 6B	a) Differentiate between PDA and LBA.	2	C O 3		L1
	b) Prove that the language $\{1^n0^n \mid n \geq 1\}$ is not regular using pumping lemma.	8	C O 4		L4
	c) Given a PDA $M_1$ having final states. Describe how to construct an equivalent PDA $M_2$ (without any final state) such that $N(M_2) = L(M_1)$ .	5	C O 3		L3
7A	a) Explain with a neat diagram, the working of a Turing model.	5	C O 6		L1
	b) Consider the following grammar G: $S \rightarrow AB$ $A \rightarrow BB \mid a$ $B \rightarrow AB \mid b$ Use CYK algorithm to check whether the string $aab$ is in $L(G)$ .	10	C O 4		L3
OR 7B	a) Explain various types of Turing machines.	5	C O 6		L1
	b) Convert the following grammar into GNF. $S \rightarrow Abb \mid a$ $A \rightarrow aaA \mid B$ $B \rightarrow bAb$	10	C O 4		L3