

# IMAGE SEGMENTATION BY SUPERPIXELS

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## Key-words:

deep learning; convolutional neural networks; image segmentation

## Abstract:

In this paper, we study different options to improve the performance of a deep learning convolutional neural network

## Contents

<b>1</b>	<b>Introduction</b>	<b>3</b>
1.1	Segmentation . . . . .	3
1.2	Superpixels . . . . .	3
1.3	Ce qu'est une bonne superpixelsegmentation . . . . .	4
1.3.1	Metrics . . . . .	4
1.3.2	Autres algorithmes . . . . .	4
1.4	Motivations/ambitions . . . . .	4
<b>2</b>	<b>Dataset generation</b>	<b>5</b>
2.1	COCO dataset . . . . .	5
2.1.1	The COCO dataset . . . . .	5
2.1.2	Characteristics . . . . .	5
2.2	Eikonal . . . . .	5
2.3	Notre utilisation de eikonal . . . . .	5
<b>3</b>	<b>The model</b>	<b>5</b>
3.1	Approach . . . . .	5
3.2	Network architecture . . . . .	6
3.2.1	Layers definitions . . . . .	6
3.2.2	Chen . . . . .	7
3.2.3	UNet . . . . .	8
3.2.4	Chen + UNet . . . . .	8
3.3	Total Variation (TV) Loss . . . . .	8
3.3.1	MSE . . . . .	8
3.3.2	TV . . . . .	8
3.4	Implementation . . . . .	9
<b>4</b>	<b>Expérience et résultats</b>	<b>9</b>
4.1	Hyperparameters . . . . .	9
4.1.1	Learning rate . . . . .	9
4.1.2	Network size $d$ . . . . .	9
4.1.3	Number of epochs . . . . .	9
4.1.4	TV regularization . . . . .	10
4.1.5	Runs . . . . .	10

4.2 Results on dataset . . . . .	10
<b>5 Conclusion/Discussion</b>	<b>10</b>

## Todo

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# 1 Introduction

## 1.1 Segmentation

What it is `piche`



**Figure 1:** *An image and its segmented image*

Motivation

## 1.2 Superpixels

What it is `piche`



**Figure 2:** *A superpixel segmentation. From left to right: the original image, the original image with its calculated superpixels outlines and the resulting superpixel segmented image. Each pixel of a superpixel has only one color, the mean color of the original image over the superpixel region.*

**Applications & Motivation** `démarrer une segmentation`  
fournir un support sur lequel faire de la classification (couleur/texture moyenne, etc)

### 1.3 Ce qu'est une bonne superpixel segmentation

#### 1.3.1 Metrics

cf article <https://arxiv.org/pdf/1612.01601.pdf> let  $S = S_{j=1}^K$  and  $G = G_i$  be partitions of the same image  $I : x_n \mapsto I(x_n)$ ,  $1 \leq n \leq N$   $S$  is a segmented image  $G$  is the ground truth

**Boundary Recall** - most commonly used metric to assess boundary adherence. - Let  $TP(G, S)$  be the number of true positive boundary pixels and  $FN(G, S)$  be the number of false negative boundary pixels in the segmented image  $S$ .

$$\text{Rec}(G, S) = \frac{TP(G, S)}{TP(G, S) + FN(G, S)}$$

#### Undersegmentation Error

**Compactness** - evaluates the compactness of the superpixels.

$$\text{CO}(G, S) = \frac{1}{N} \sum_{S_j} |S_j| \frac{4\pi A(S_j)}{P(S_j)}$$

- the CO operator computes how close the area  $A(S_j)$  of each superpixel  $S_j$  is from a circle with same perimeter  $P(S_j)$ .

#### 1.3.2 Autres algorithmes

##### SLIC

**metrics** Here are the previously defined metrics of some well-known superpixel segmentation algorithms.

Algorithm	BR	UE	CO
SLIC			
Reference			

**Table 1:** Metrics for different superpixel segmentation algorithms

We use the ?? algorithm as a reference to evaluate the performances of our model.

### 1.4 Motivations/ambitions

**Difficultés que l'on cherche à résoudre**

**Pas de vraie approche DL pour segmentation avec superpixels**

**Ambitions** améliorer les métriques

## 2 Dataset generation

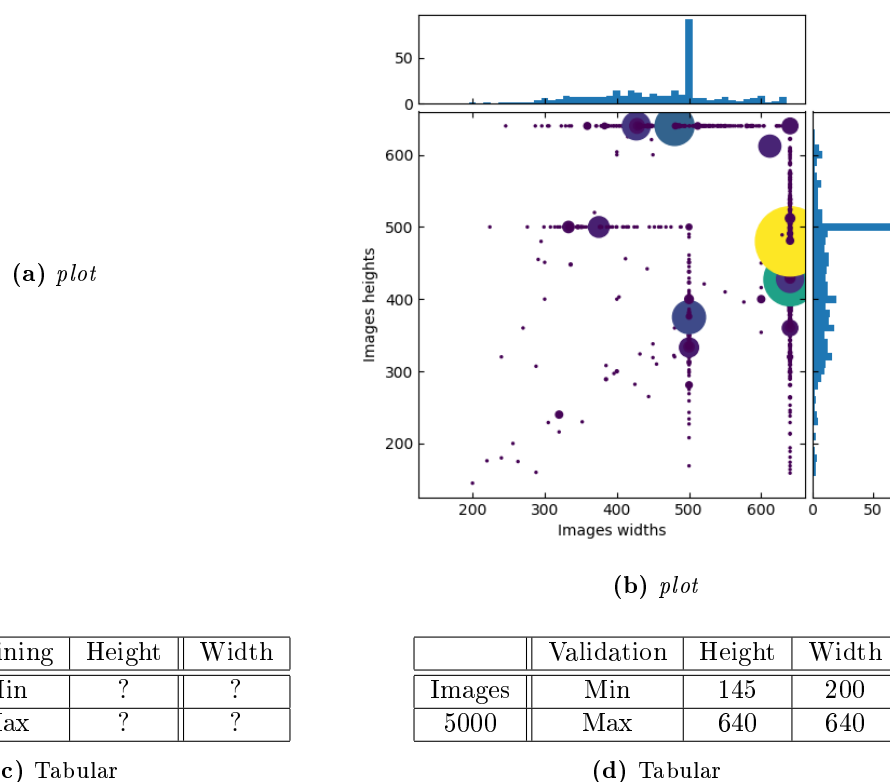
### 2.1 COCO dataset

#### 2.1.1 The COCO dataset

COCO dataset<sup>1</sup>, nb of images, examples

#### 2.1.2 Characteristics

Piche



**Figure 3:** *Training and validation sets characterization*

### 2.2 Eikonal

### 2.3 Notre utilisation de eikonal

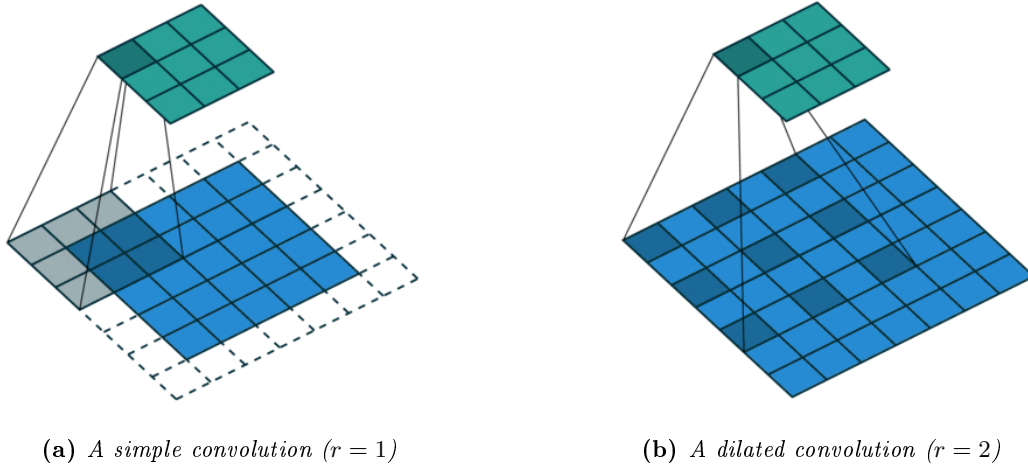
en plus réutilisé derrière sur image qui sort du réseau  
faire un petit résumé

## 3 The model

### 3.1 Approach

description générale de l'approche (NN puis eikonal)

<sup>1</sup>site de COCO



**Figure 4:** Illustration of two types of convolutions

## 3.2 Network architecture

### 3.2.1 Layers definitions

**Dilated convolution** We consider a layer  $L = (L_j)_{j \in \llbracket 1, w \rrbracket}$ ,  $w$  being the number of feature maps  $L_j$  of  $L$ . We also consider  $K = (K_{i,j})_{i,j}$ , each  $K_{i,j}$  being a  $3 \times 3$  convolutional kernel. The dilated convolution operation of  $K_{i,j}$  on  $L_j$  is denoted by  $L_j *_r K_{i,j}$ ,  $r$  being the dilation parameter. The output  $C(x)$  of a pixel  $x$  is:

$$\begin{aligned}
 C(x) &:= (L_j *_r K_{i,j})(x) \\
 &= \sum_{a+rb=x} L_j(a) K_{i,j}(b) \\
 &= \sum_b L_j(x - rb) K_{i,j}(b)
 \end{aligned}$$

and we recognize the simple convolution when  $r = 1$ .

A dilated convolution enables the network getting larger receptive fields while preserving the input resolution<sup>2</sup>

**Adaptive Batch Normalization (ABN)** As we have seen in (2.1.2), page 5, we need to normalize the data. We define the *adaptive normalization function*  $\Psi$  as:

$$\Psi(x) = a x + b \text{BN}(x),$$

where  $\text{BN}$  is the classic batch normalization<sup>3</sup>, defined as:

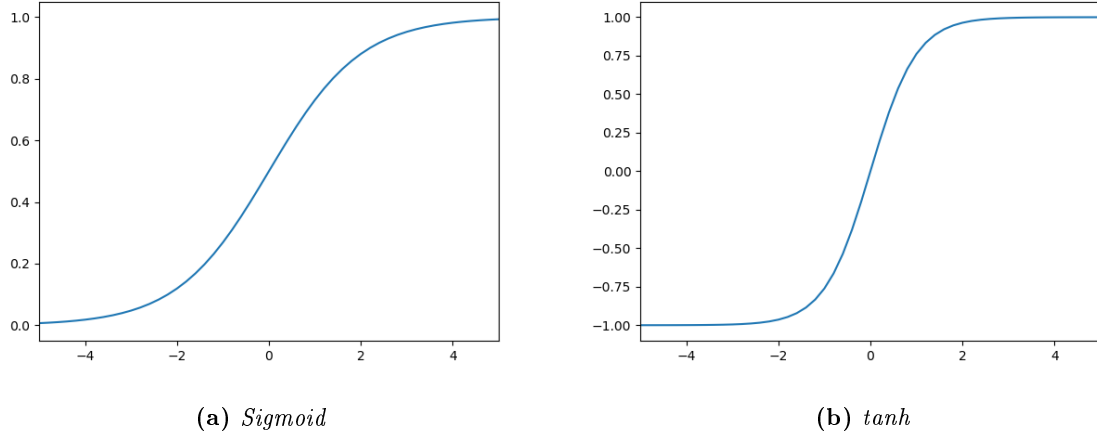
$$\text{BN}(x) = \frac{x - \mathbb{E}[x]}{\sqrt{\text{Var}[x] + \epsilon}} * \gamma + \beta.$$

As such,  $\Psi$  combines identity mapping and batch normalization.  $a$ ,  $b$ ,  $\gamma$  and  $\beta$  are learned parameters<sup>4</sup> by backpropagation. It allows the model to adapt to each dataset, choosing whether or not giving a big importance to the identity term and the normalization term.

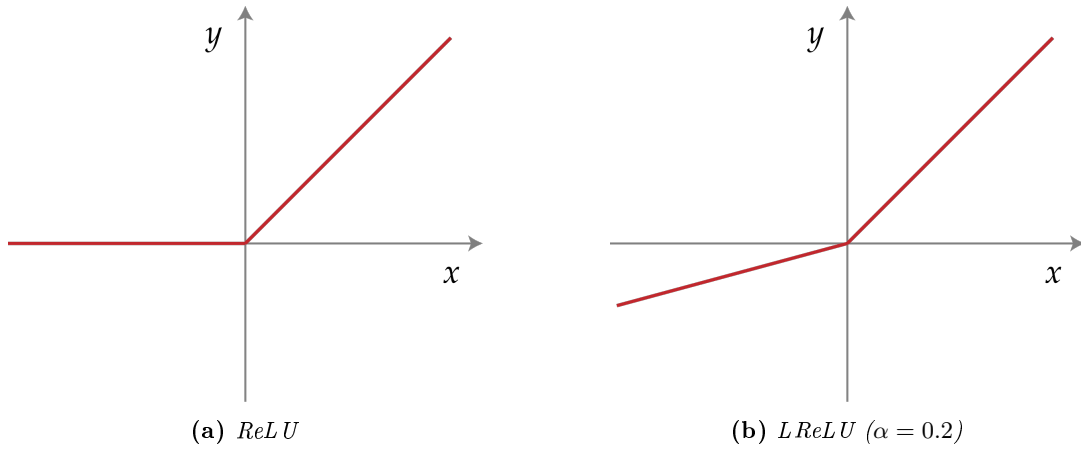
<sup>2</sup>ref ?

<sup>3</sup>reference ?

<sup>4</sup>ref : [https://pytorch.org/docs/stable/\\_modules/torch/nn/modules/batchnorm.html](https://pytorch.org/docs/stable/_modules/torch/nn/modules/batchnorm.html)



**Figure 5:** *Illustration of two bounded rectifiers*



**Figure 6:** *Illustration of two unbounded rectifiers*

**Leaky rectifier (LReLU)** In order to let our neural network model complex patterns in the data, we have to add a non-linear property to the model. It often is an activation function, such as a sigmoid or a tanh (Figure 5).

The problem with these activation functions is that they are bounded and their gradient is very low on the edges. Because we want to be able to manipulate high scalar values, we have to use an unbounded activation function, such as ReLU,  $\Phi(x) = \max(0, x)$  (Figure 6a). But the issue with ReLU is that all the negative values become zero immediately, which decreases the ability of our model to train from the data. Hence the implementation of a *leaky rectifier*, LReLU:

$$\Phi(x) = \max(\alpha x, x), \text{ with } 0 < \alpha < 1.$$

By implementing a Leaky Rectifier, we are able to take into account the negative valued pixels.

### 3.2.2 Chen

**Context Aggregation Network (CAN)** <sup>5</sup> blabla sur le RGB en entrée, RGB en sortie I -> f(I)

---

<sup>5</sup>reference

input $I$	$\longrightarrow$	$L^1$	$\longrightarrow$	$\dots$	$\longrightarrow$	$L^s$	$\longrightarrow$	$\dots$	$\longrightarrow$	output ( $L^d$ )
$m \times n \times 3$		$m \times n \times w_1$				$m \times n \times w_s$				$m \times n \times 3$

**Table 2:** *Layers*

**Architecture of a block** Each block  $L_s$  is made of 3 layers:

1. *A dilated convolution,  $r_s = 2^s$*
2. *An adaptative batch normalization*
3. *A leaky rectifier (ReLU)*

so that the content of an intermediate layer  $L^s$  can be computed from the content of the previous layer  $L^{s-1}$ :

$$L_i^s = \Phi \left( \Psi^s \left( b_i^s + \sum_j L_j^{s-1} *_{r_s} K_{i,j}^s \right) \right). \quad (1)$$

where ... is ...

and

$$L_j^{s-1} *_{r_s} K_{i,j}^s = \sum_{a+r_s b=x} L_j^{s-1}(a) K_{i,j}^s(b) \quad (2)$$

because of 3.2.1, page 6.

Layer	1	2	3	4	5	6	7
Convolution	$3 \times 3$						
Dilation	1						
Batch Normalization	Yes						
LReLU	Yes						

**Table 3:** *Chen*

### 3.2.3 UNet

### 3.2.4 Chen + UNet

## 3.3 Total Variation (TV) Loss

### 3.3.1 MSE

$$L_{MSE} = \frac{1}{N} \sum_{i=1}^N |\hat{f}(I)_i - f(I)_i|^2$$

### 3.3.2 TV

**Formula**

$$L_{TV} = \frac{1}{N} \sum_{i=1}^N |\hat{f}(I)_i - f(I)_i|^2 + \frac{1}{N}$$

**Why**



$lr_0$	decay?	saturation?	$d$	TV?
0.001	No	No	7	No
0.01	No	No	7	No
0.01	$\times 0.5$ every 2 epochs	$10^{-4}$	7	No
0.001	$\times 0.5$ every 2 epochs	$10^{-4}$	7	No

**Table 4:** Runs for learning rate tuning

### 3.4 Implementation

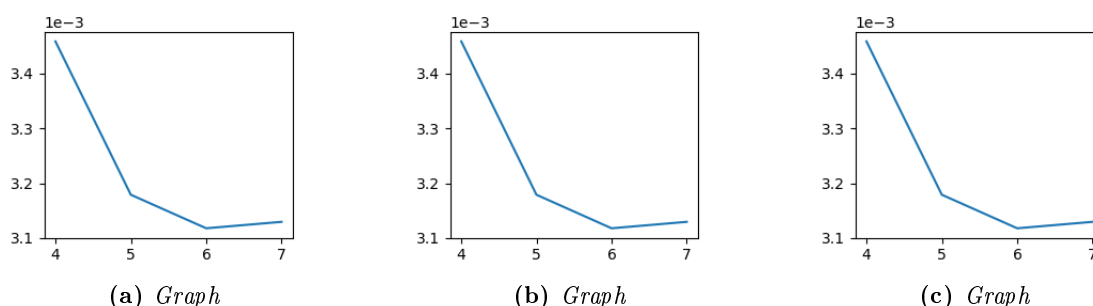
The network was implemented with PyTorch<sup>6</sup> and we used GPU acceleration [...] (pytorch), se renseigner (section assez courante) GPU acceleraation code sur github

## 4 Expérience et résultats

### 4.1 Hyperparameters

petit bilan des valeurs choisies évolution des paramètres a et b ?

#### 4.1.1 Learning rate

**Figure 7:** Tuning of learning rate

**Constant value** entraînement (lr, alpha) -> courbes de loss, et loss qui sature (cluster) d'où changement de lr au cours des epochs

**Non constant value**

#### 4.1.2 Network size $d$

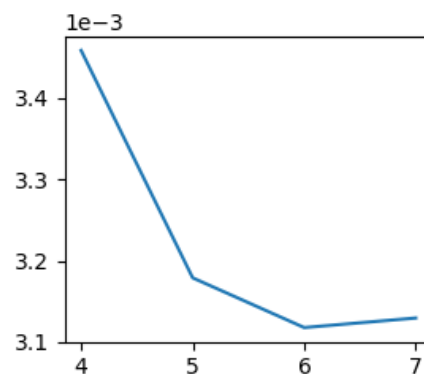
- Learning rate initialisé à 0.01, divisé par 2 toutes les 2 époques, saturation à  $10^{-4}$  - Pas de régularisation TV CONCLUSION des run 3 à 5: Il est préférable de laisser  $d=7$ . Entre  $d=6$  et  $d=7$ , l'amélioration semble relativement faible. bon intermédiaire entre temps de calcul et performances

#### 4.1.3 Number of epochs

nb epochs: on le sélectionne en prenant le minimum de la validation loss

<sup>6</sup>Repository can be found at <https://github.com/theodumont/superpixels-segmentation>.

$d$	4	5	6	7	8
$\text{loss} \times 10^3$	3.46	3.18	3.12	3.13	???

(a) *Loss values on validation set*(b) *Graph***Figure 8:** *Tuning of network size*

#### 4.1.4 TV regularization

#### 4.1.5 Runs

tableaux et graphes

### 4.2 Results on dataset

image originale  $\rightarrow$  CNN  $\rightarrow$  résultat du filtre dans eikonal  $\rightarrow$  superpixels sans couleurs + couleur moyenne pour chaque spp de l'image originale cf results/images

## 5 Conclusion/Discussion

On a présenté un nouveau...

On a prouvé...

Il reste à faire...

relire tous les mails pour avoir toutes les infos sur performances etc

## Special thanks

## Sources

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