

Information gain is the reduction in entropy or surprise by transforming a data set and is used in training decision trees.

$H(Y|X)$ means;

- I know x
- It tells the uncertainty in Y after knowing x

$H(Y|X) = H(Y) \rightarrow x$ and Y are statistically independent

If x and Y are dependent, and I know x , for this if Y 's uncertainty is decreased, then it is called information gain

$$IG(Y, x) = H(Y) - H(Y|x) = 0$$

where,

$$x = 0, \text{ when } H(Y|x) = H(Y) = Y \perp x$$

$$x = +ve, \text{ when } H(Y) > H(Y|x)$$

$$x = -ve \text{ when } H(Y) < H(Y|x)$$

This is where the math starts; -

$$P(\text{Play Golf} = Y) = 9/14 = 0.64$$

$$P(\text{Play Golf} = N) = 5/14 = 1 - 0.64 = 0.36$$

$$H(\text{Play Golf}) = - \sum_{a \in A} P(a) \log_2 P(a)$$

$$= - \left[0.64 \log_2 (0.64) + 0.36 \log_2 (0.36) \right]$$

$$= - \left[-0.64 \times 0.644 + (-1.474 \times 0.36) \right]$$

$$= 0.9428$$

$$P(\text{outlook} = \text{rainy}) = \frac{5}{14} = 0.35 \quad P(\text{outlook} = \text{Sunny}) = \frac{5}{14} = 0.35$$

$$P(\text{outlook} = \text{overcast}) = \frac{4}{14} = 0.30$$

$$H(\text{Play Golf} | \text{outlook} = \text{rainy}) = - \sum_{a \in A} \left[P(\text{Play Golf} | \text{outlook} = \text{rainy}) \times \log_2 P(\text{Play Golf} | \text{outlook} = \text{rainy}) \right]$$

$$= - \sum_{a \in A} \left[P(\text{Play Golf} = Y | \text{outlook} = \text{rainy}) \times \log_2 P(\text{Play Golf} = Y | \text{outlook} = \text{rainy}) \right. \\ \left. + P(\text{Play Golf} = N | \text{outlook} = \text{rainy}) \times \log_2 P(\text{Play Golf} = N | \text{outlook} = \text{rainy}) \right]$$

$$P(P=Y | O=r) = \frac{P(P=Y, O=r)}{P(O=r)}$$

$$= \frac{\frac{2}{14}}{0.35} = \frac{1}{20} = \frac{2}{40}$$

$$P(P=N | O=r) = \frac{P(P=N, O=r)}{P(O=r)} = \frac{\frac{3}{14}}{0.35} = \frac{3}{40}$$

$$P(P=Y | O=s) = \frac{P(P=Y, O=s)}{P(O=s)} = \frac{\frac{3}{14}}{0.35} = \frac{3}{40}$$

$$P(P=N | O=s) = \frac{P(P=N, O=s)}{P(O=s)} = \frac{\frac{2}{14}}{0.35} = \frac{2}{40}$$

$$P(P=Y | O=\emptyset) = \frac{P(P=Y, O=\emptyset)}{P(O=\emptyset)} = \frac{\frac{4}{14}}{0.3} = \frac{20}{21}$$

$$P(P=N | O=\emptyset) = \frac{P(P=N, O=\emptyset)}{P(O=\emptyset)} = \frac{4}{14} = \frac{2}{7}$$

in WL
chopped

$$\begin{aligned}
 H(\text{Play Golf} | \text{Outlook} = r) &= - \left[\frac{2}{40} \log_2 \frac{2}{40} + \frac{3}{40} \log_2 \frac{3}{40} \right] \\
 &= - \left[\frac{2}{40} \times (-4.32) + \frac{3}{40} \times (-3.74) \right] \\
 &= - (-0.216 - 0.2801)
 \end{aligned}$$

$$\begin{aligned}
 H(\text{Play Golf} | \text{Outlook} = s) &\stackrel{=}{=} 0.497 \\
 &= - \left[\frac{3}{40} \log_2 \frac{3}{40} + \frac{2}{40} \log_2 \frac{2}{40} \right] \\
 &= \left[-3.74 \times \frac{3}{40} + \frac{2}{40} \times (-4.32) \right] \\
 &= 0.497
 \end{aligned}$$

$$\begin{aligned}
 H(\text{Play Golf} | \text{Outlook} = 0) &= \left[\frac{20}{21} \log_2 \left(\frac{20}{21} \right) \right] \\
 &= 0.070
 \end{aligned}$$

This is where ⁽²⁾ started -
conditional entropy

$$\begin{aligned}
 H(\text{Play Golf} | \text{Outlook}) &= \sum_{a \in A} P(a) H(\text{Play Golf} | \text{Outlook} = a) \\
 &= \frac{5}{14} \times 0.497 + \frac{5}{14} \times 0.497 \\
 &\quad + \frac{4}{14} \times 0.070 \\
 &= 0.1775 + 0.1775 + 0.02 \\
 &= 0.375
 \end{aligned}$$

$$\begin{aligned}
 E_H(\text{Play Golf} | \text{Outlook}) &= 0.9428 - 0.375 \\
 &= 0.5678
 \end{aligned}$$

Answer according to Question No 2

AI

✓ AI (Artificial Intelligence) is defined as acquisition of knowledge and ability to apply knowledge

✓ The aim is to simulate natural intelligence to solve tough issues

ML

✓ It is practice of getting machines to make decisions without being programmed

✓ ML is a subset of AI and data science

DL

✓ In deep learning, it implements an Artificial Neural Network (ANN) which has multiple layers between its input and output layers

DS

✓ Data Science is a broad field that spans to collection, management and analysis of large amounts of data with a wide range of applications.

✓ It integrates all terms above and more to summarize ~~from~~ insights from data and make predictions from large data sets.

Answer according to Question No 3

Cross validation is a resampling procedure used to evaluate machine learning models on limited data sample and it can divide data into 2 segments :

- ✓ one can used to learn or train a model
- ✓ one is used to validate the model.

* Overfitting is an error that occurs in data modelling as result of a particular function aligning too closely to a minimal set of data points.

* ~~financial~~ prob when a model has been compromised by overfitting, the model may lose its value as a predictive tool for investing

* Overfitting is more frequent problem than underfitting and typically occurs as result of trying to avoid floccing.

We can remove the problem by :-

1. model must be linear $y = ax + b$ (too simple)
2. model can be quadratic $y = ax^2 + bx + c$
 $= ax_1 + bx_2 + cx_0$
 (good)

* To prevent it from cross-validation, in which data being used for training model is chopped into folds and model is used for each fold.