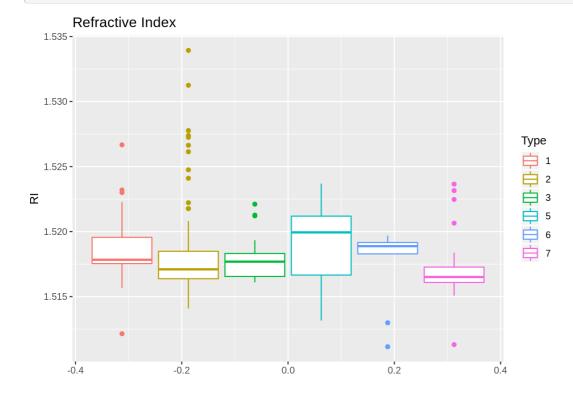
Classification

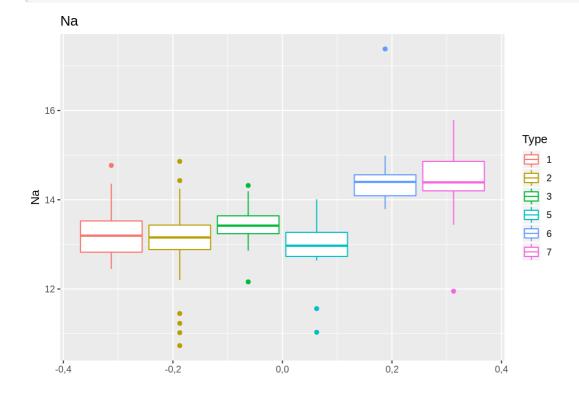
```
library(mlbench)
data(Glass)
library(ggplot2)
library(class)
library(caret)
library(e1071)
```

1. Boxplots

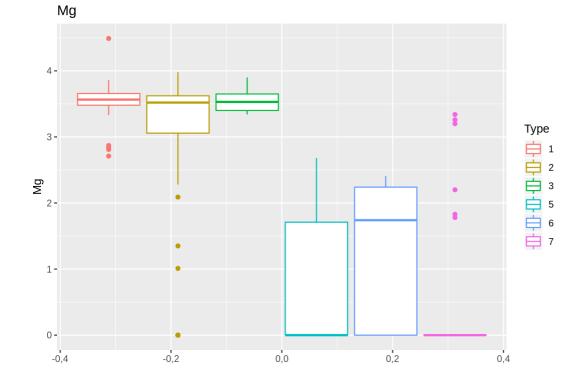
```
qplot(data = Glass, y = RI, color = Type, geom = "boxplot", main = "Refractive Index")
```



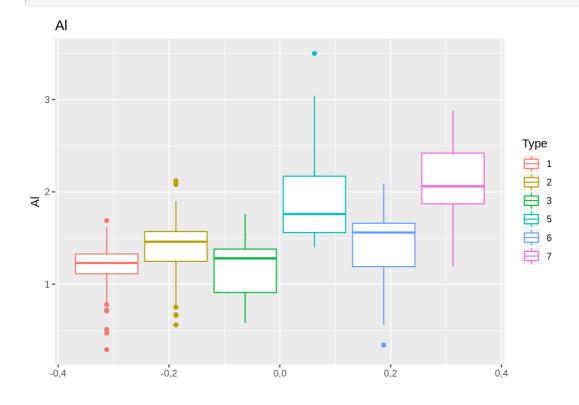
qplot(data = Glass, y = Na, color = Type, geom = "boxplot", main = "Na")



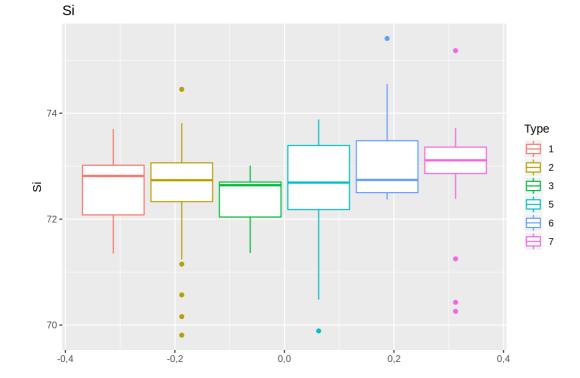
qplot(data = Glass, y = Mg, color = Type, geom = "boxplot", main = "Mg")

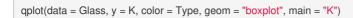


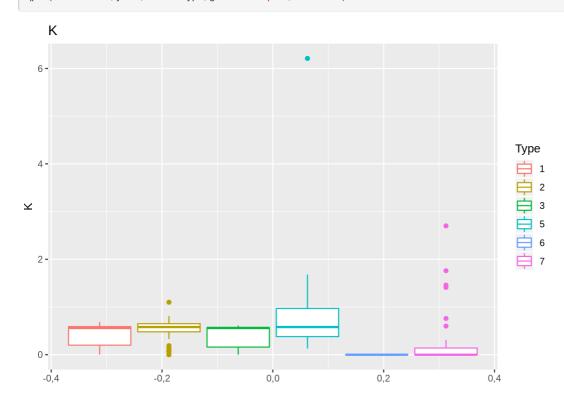
qplot(data = Glass, y = Al, color = Type, geom = "boxplot", main = "Al")



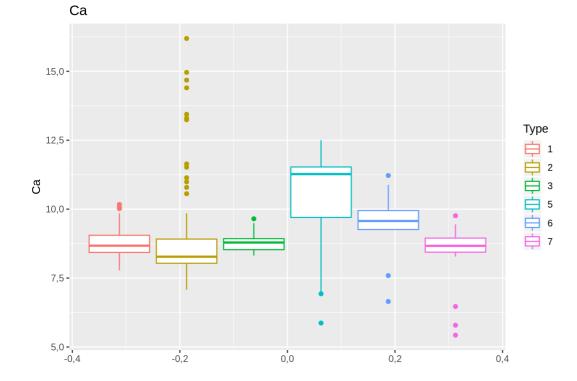
 $qplot(data = Glass, \, y = Si, \, color = Type, \, geom = \hbox{\tt "boxplot"}, \, main = \hbox{\tt "Si"})$



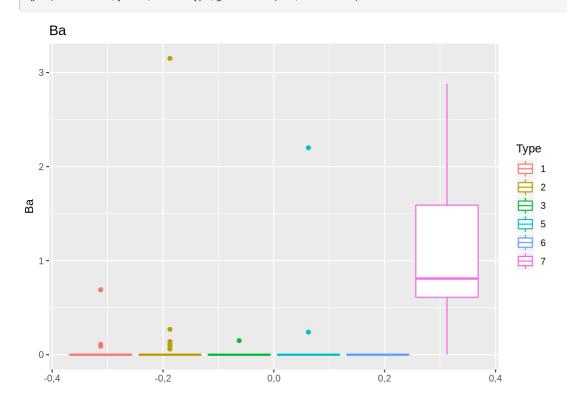




 $qplot(data = Glass, \ y = Ca, \ color = Type, \ geom = "boxplot", \ main = "Ca")$



qplot(data = Glass, y = Ba, color = Type, geom = "boxplot", main = "Ba")



qplot(data = Glass, y = Fe, color = Type, geom = "boxplot", main = "Fe")

```
Fe
  0,5 -
  0,4 -
                                                                                           Туре
                                                                                           ‡ 1
  0,3-
                                                                                           2
Fe
                                                                                           ‡ 3
                                                                                           ‡ 5
  0,2 -
                                                                                           = 6
  0,1-
  0,0 -
                         -0,2
                                             0,0
                                                                 0,2
     -0,4
```

2. KNN

a. Al

```
## Real
## pred_knn 1 2 3 5 6 7
## 111 4 3 1 1 1
## 2 4 9 2 1 2 3
## 3 3 5 0 0 0 0
## 5 0 0 0 1 0 0
## 6 0 1 0 1 0 1
## 7 0 0 0 0 0 3
```

```
mean(pred_knn == Glass[test, "Type"])
```

```
## [1] 0,4210526
```

```
set.seed(42)

pred_knn <- knn(train = Glass[-test, "Al", drop = FALSE],

test = Glass[test, "Al", drop = FALSE],

cl = Glass[-test, "Type"],

k = 10)

table(pred_knn, Real = Glass[test, "Type"])
```

```
## Real
## pred_knn 1 2 3 5 6 7

## 112 5 3 0 2 0

## 2 612 2 3 1 4

## 3 0 0 0 0 0 0

## 5 0 0 0 0 0 0

## 6 0 0 0 0 0 0

## 7 0 2 0 1 0 4
```

```
fit
```

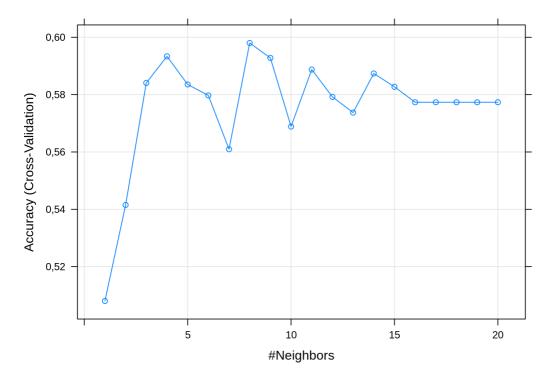
method = "knn",

trControl = trControl, metric = "Accuracy", data = Glass)

tuneGrid = expand.grid(k = 1:20),

```
## k-Nearest Neighbors
##
## 214 samples
## 1 predictor
## 6 classes: '1', '2', '3', '5', '6', '7'
## No pre-processing
## Resampling: Cross-Validated (12 fold)
## Summary of sample sizes: 198, 197, 197, 195, 196, 197, ...
## Resampling results across tuning parameters:
##
## k Accuracy Kappa
## 1 0,5080320 0,3176503
## 2 0,5415287 0,3638706
## 3 0,5841037 0,4130965
## 4 0,5933630 0,4154579
## 5 0,5835537 0,3973475
## 6 0,5797178 0,3967636
## 7 0,5609556 0,3661789
## 8 0,5980159 0,4180761
## 9 0,5928076 0,4153286
## 10 0,5688711 0,3770669
## 11 0,5887567 0,4025011
## 12 0,5792251 0,3875212
## 13 0,5737444 0,3792962
## 14 0,5873896 0,3993399
## 15 0,5827313 0,3934768
## 16 0,5773420 0,3856693
## 17 0,5773420 0,3856693
## 18 0,5773420 0,3856693
## 19 0,5773420 0,3856693
## 20 0,5773420 0,3860041
## Accuracy was used to select the optimal model using the largest value.
## The final value used for the model was k = 8.
```

plot(fit)



b. RI, AI, Si

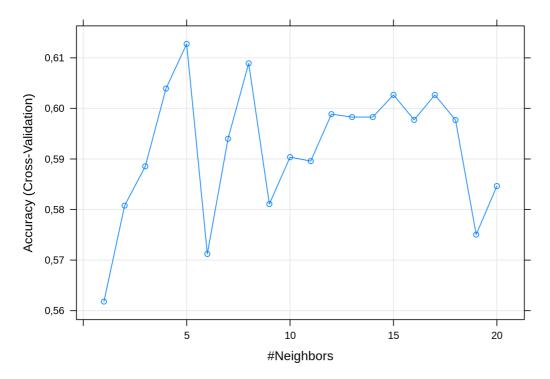
```
## Real
## pred_knn 1 2 3 5 6 7
## 1 12 1 1 1 1 1
## 2 4 14 1 2 1 3
## 3 1 3 2 0 0 0
## 5 0 1 0 1 0 0
## 6 1 0 1 0 0 0
## 7 0 0 0 0 1 4
```

```
mean(pred_knn == Glass[test, "Type"])
```

[1] 0,5789474

```
## k-Nearest Neighbors
## 214 samples
   3 predictor
##
   6 classes: '1', '2', '3', '5', '6', '7'
## No pre-processing
## Resampling: Cross-Validated (12 fold)
## Summary of sample sizes: 198, 197, 197, 195, 196, 197, ...
## Resampling results across tuning parameters:
##
##
   k Accuracy Kappa
    1 0,5617995 0,4099565
##
    2 0,5807784 0,4319915
##
    3 0,5885470 0,4304192
##
   4 0,6039212 0,4436183
## 5 0,6127558 0,4529520
## 6 0,5712128 0,3939731
## 7 0,5939937 0,4269579
## 8 0,6089145 0,4416142
## 9 0,5810794 0,4011413
## 10 0,5903674 0,4070353
## 11 0,5895790 0,4017001
## 12 0,5988670 0,4161133
## 13 0,5982883 0,4151980
   14 0,5982883 0,4118151
##
   15 0,6026742 0,4161983
##
   16 0,5977382 0,4114154
   17 0,6026742 0,4163846
##
   18 0,5977096 0,4096108
##
   19 0,5750487 0,3750827
##
   20 0,5846430 0,3874747
##
## Accuracy was used to select the optimal model using the largest value.
## The final value used for the model was k = 5.
```

plot(fit)



c. All possible predictors

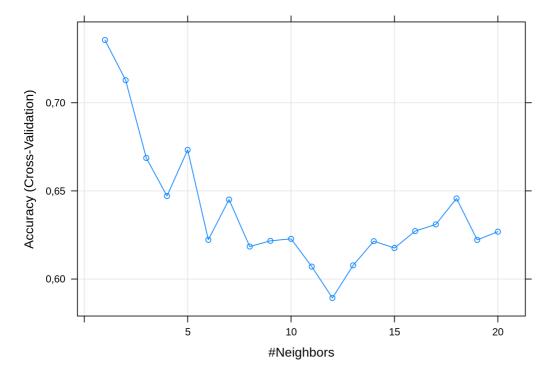
```
## Pred_knn 1 2 3 5 6 7
## 113 4 2 0 0 0
## 2 114 2 0 1 0
## 3 4 0 1 0 0 1
## 5 0 1 0 3 0 0
## 6 0 0 0 0 1 1
## 7 0 0 0 1 1 6
```

```
mean(pred_knn == Glass[test, "Type"])
```

```
## [1] 0,6666667
```

```
## k-Nearest Neighbors
## 214 samples
## 9 predictor
## 6 classes: '1', '2', '3', '5', '6', '7'
##
## No pre-processing
## Resampling: Cross-Validated (12 fold)
## Summary of sample sizes: 198, 197, 197, 195, 196, 197, ...
## Resampling results across tuning parameters:
##
## k Accuracy Kappa
## 1 0,7355790 0,6420605
## 2 0,7127928 0,6096557
## 3 0,6686697 0,5452538
## 4 0,6471090 0,5079293
## 5 0,6732707 0,5469701
## 6 0,6222588 0,4758995
## 7 0,6451005 0,5044083
## 8 0,6184461 0,4674469
## 9 0,6216801 0,4692021
## 10 0,6228034 0,4705830
## 11 0,6070656 0,4486693
## 12 0,5892780 0,4252646
## 13 0,6077625 0,4479702
## 14 0,6214704 0,4634332
## 15 0,6176005 0,4598108
## 16 0,6271948 0,4715813
## 17 0,6310020 0,4759820
## 18 0,6457133 0,4969750
## 19 0,6222301 0,4598929
## 20 0,6268597 0,4668207
## Accuracy was used to select the optimal model using the largest value.
## The final value used for the model was k = 1.
```

plot(fit)



d. with PCA

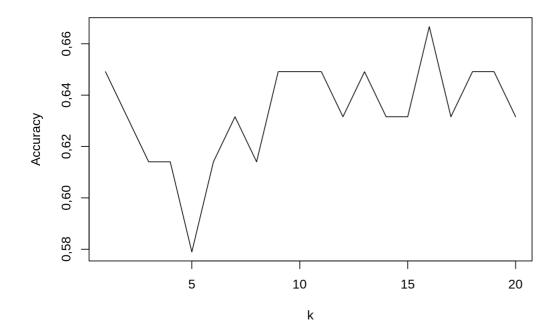
```
pca.result <- prcomp(Glass[-test,-c(10:11)], scale=T)
train.pca <- pca.result$x
test.pca <- predict(pca.result, Glass[test,-c(10:11)])

k <- NULL
accuracy <- NULL
set.seed(42)
for (i in 1:20){
    pred_knn <- knn(train.pca, test.pca, Glass[-test, "Type"], k=i)
    accuracy <- c(accuracy, mean(pred_knn == Glass[test, "Type"]))
    k <- c(k, i)
}
result <- data.frame('k' = k, 'Accuracy' = accuracy)
```

result

```
##
    k Accuracy
## 1 1 0,6491228
## 2 2 0,6315789
## 3 3 0,6140351
## 4 4 0,6140351
## 5 5 0,5789474
## 6 6 0,6140351
## 7 7 0,6315789
## 8 8 0,6140351
## 9 9 0,6491228
## 10 10 0,6491228
## 11 11 0,6491228
## 12 12 0,6315789
## 13 13 0,6491228
## 14 14 0,6315789
## 15 15 0,6315789
## 16 16 0,6666667
## 17 17 0,6315789
## 18 18 0,6491228
## 19 19 0,6491228
## 20 20 0,6315789
```

```
plot(result, type = 'l')
```



result[which.max(result\$Accuracy),]

```
## k Accuracy
## 16 16 0,6666667
```

e. Comparing all the models

```
## Model Accuracy
## 1 Al 0,5919404
## 2 Rl + Al + Si 0,6233678
## 3 All predictors 0,7400707
## 4 PCA 0,6842105
```

3. Logistic regression

"RI"

```
glm_fit_ri <- glm(Type ~ RI, data = Glass, family = "binomial")
summary(glm_fit_ri)
```

```
##
## Call:
## glm(formula = Type ~ RI, family = "binomial", data = Glass)
##
## Deviance Residuals:
## Min 1Q Median 3Q Max
## -1,6522 -1,4544 0,8472 0,8865 1,2360
##
## Coefficients:
```

```
## Warning in printCoefmat(coefs, digits = digits, signif.stars = signif.stars, : в
## результате преобразования созданы NA
```

```
## Estimate Std. Error z value Pr(>|z|)
## (Intercept) 84,85 71,45 1,188 0,235
## RI -55,40 47,05 -1,178 0,239
##
## (Dispersion parameter for binomial family taken to be 1)
##
## Null deviance: 270,54 on 213 degrees of freedom
## Residual deviance: 269,16 on 212 degrees of freedom
## AIC: 273,16
##
## Number of Fisher Scoring iterations: 4
```

```
glm_fit_na <- glm(Type ~ Na, data = Glass,
           family = "binomial")
 summary(glm_fit_na)
 ## Call:
 ## glm(formula = Type ~ Na, family = "binomial", data = Glass)
 ## Deviance Residuals:
 ## Min 1Q Median 3Q Max
 ## -1,7436 -1,3976 0,7987 0,9139 1,3125
 ## Coefficients:
 ## Warning in printCoefmat(coefs, digits = digits, signif.stars = signif.stars, : B
 ## результате преобразования созданы NA
           Estimate Std. Error z value Pr(>|z|)
 ## (Intercept) -4,5226 2,5630 -1,765 0,0776.
 ## Na
             0,3924 0,1921 2,043 0,0411 *
 ## ---
 ## Signif. codes: 0 '*** 0,001 '** 0,01 '* 0,05 '.' 0,1 ' 1
 ## (Dispersion parameter for binomial family taken to be 1)
 ##
     Null deviance: 270,54 on 213 degrees of freedom
 ##
 ## Residual deviance: 266,10 on 212 degrees of freedom
 ## AIC: 270,1
 ##
 ## Number of Fisher Scoring iterations: 4
"Mg"
 glm_fit_mg <- glm(Type ~ Mg, data = Glass,
           family = "binomial")
 summary(glm_fit_mg)
 ## Call:
 ## glm(formula = Type ~ Mg, family = "binomial", data = Glass)
 ## Deviance Residuals:
 ## Min 1Q Median 3Q Max
 ## -1,85959 -1,17969 0,07464 1,05855 1,39758
 ## Coefficients:
 ## Warning in printCoefmat(coefs, digits = digits, signif.stars = signif.stars, : B
 ## результате преобразования созданы NA
           Estimate Std. Error z value Pr(>|z|)
 ## (Intercept) 5,8820 1,4769 3,983 6,81e-05 ***
 ## Mg
             -1,6045 0,4201 -3,820 0,000134 ***
 ## ---
 ## Signif. codes: 0 '*** 0,001 '** 0,01 '* 0,05 '.' 0,1 ' 1
 ##
 ## (Dispersion parameter for binomial family taken to be 1)
 ##
     Null deviance: 270,54 on 213 degrees of freedom
 ##
 ## Residual deviance: 214,97 on 212 degrees of freedom
 ## AIC: 218,97
 ##
 ## Number of Fisher Scoring iterations: 7
"Al"
```

glm_fit_al <- glm(Type ~ Al, data = Glass, family = "binomial")

summary(glm_fit_al)

```
##
 ## Call:
 ## glm(formula = Type ~ Al, family = "binomial", data = Glass)
 ## Deviance Residuals:
            1Q Median
                            3Q
 ## -1,8816 -1,1959 0,5304 0,8195 2,0056
 ##
 ## Coefficients:
 ## Warning in printCoefmat(coefs, digits = digits, signif.stars = signif.stars, : B
 ## результате преобразования созданы NA
           Estimate Std. Error z value Pr(>|z|)
 ## (Intercept) -2,7368 0,6500 -4,210 2,55e-05 ***
             2,5563 0,4857 5,263 1,41e-07 ***
 ## AI
 ## ---
 ## Signif. codes: 0 '*** 0,001 '** 0,01 '* 0,05 '.' 0,1 ' 1
 ## (Dispersion parameter for binomial family taken to be 1)
      Null deviance: 270,54 on 213 degrees of freedom
 ## Residual deviance: 228,87 on 212 degrees of freedom
 ## AIC: 232,87
 ## Number of Fisher Scoring iterations: 5
"Si"
 glm_fit_si <- glm(Type ~ Si, data = Glass,
            family = "binomial")
 summary(glm_fit_si)
 ##
 ## Call:
 ## glm(formula = Type ~ Si, family = "binomial", data = Glass)
 ## Deviance Residuals:
 ## Min 1Q Median
                              3Q
 ## -1,5324 -1,4729 0,8768 0,8911 0,9743
 ##
 ## Coefficients:
 ## Warning in printCoefmat(coefs, digits = digits, signif.stars = signif.stars, : B
 ## результате преобразования созданы NA
           Estimate Std. Error z value Pr(>|z|)
 ## (Intercept) -4,99094 13,62203 -0,366 0,714
 ## Si
            0,07863 0,18753 0,419 0,675
 ##
 ## (Dispersion parameter for binomial family taken to be 1)
     Null deviance: 270,54 on 213 degrees of freedom
 ## Residual deviance: 270,37 on 212 degrees of freedom
```

AIC: 274,37

summary(glm_fit_k)

Number of Fisher Scoring iterations: 4

 $glm_fit_k \leftarrow glm(Type \sim K, data = Glass, family = "binomial")$

##

"K"

```
##
 ## Call:
 ## glm(formula = Type ~ K, family = "binomial", data = Glass)
 ## Deviance Residuals:
            1Q Median
                            3Q
                                   Max
 ## -1,5153 -1,4669 0,8791 0,8999 0,9283
 ##
 ## Coefficients:
 ## Warning in printCoefmat(coefs, digits = digits, signif.stars = signif.stars, : B
 ## результате преобразования созданы NA
           Estimate Std. Error z value Pr(>|z|)
 ## (Intercept) 0,6187 0,1960 3,157 0,0016 **
            0,2142 0,2838 0,755 0,4504
 ## K
 ## ---
 ## Signif. codes: 0 '*** 0,001 '** 0,01 '* 0,05 '.' 0,1 ' 1
 ## (Dispersion parameter for binomial family taken to be 1)
 ##
      Null deviance: 270,54 on 213 degrees of freedom
 ## Residual deviance: 269,86 on 212 degrees of freedom
 ## AIC: 273,86
 ## Number of Fisher Scoring iterations: 4
"Ca"
 glm_fit_ca <- glm(Type ~ Ca, data = Glass,
            family = "binomial")
 summary(glm_fit_ca)
 ##
 ## Call:
 ## glm(formula = Type ~ Ca, family = "binomial", data = Glass)
 ## Deviance Residuals:
 ## Min 1Q Median
                              3Q
 ## -1,5675 -1,4670 0,8724 0,9152 1,0621
 ##
 ## Coefficients:
 ## Warning in printCoefmat(coefs, digits = digits, signif.stars = signif.stars, : B
```

```
## результате преобразования созданы NA
```

```
Estimate Std. Error z value Pr(>|z|)
## (Intercept) -0,4157 1,0055 -0,413 0,679
## Ca
            0,1276 0,1123 1,137 0,256
##
## (Dispersion parameter for binomial family taken to be 1)
    Null deviance: 270,54 on 213 degrees of freedom
## Residual deviance: 269,16 on 212 degrees of freedom
## AIC: 273,16
##
## Number of Fisher Scoring iterations: 4
```

"Ba"

```
glm_fit_ba <- glm(Type ~ Ba, data = Glass,
          family = "binomial")
summary(glm_fit_ba)
```

```
##
 ## Call:
 ## glm(formula = Type ~ Ba, family = "binomial", data = Glass)
 ##
 ## Deviance Residuals:
            1Q Median
                              3Q
                                   Max
 ## -2,4432 -1,3938 0,9755 0,9755 0,9755
 ##
 ## Coefficients:
 ## Warning in printCoefmat(coefs, digits = digits, signif.stars = signif.stars, : B
 ## результате преобразования созданы NA
           Estimate Std. Error z value Pr(>|z|)
 ## (Intercept) 0,4955 0,1532 3,234 0,00122 **
              3,5323 1,5720 2,247 0,02464 *
 ## Ba
 ## ---
 ## Signif. codes: 0 '***' 0,001 '**' 0,01 '*' 0,05 '.' 0,1 ' ' 1
 ## (Dispersion parameter for binomial family taken to be 1)
 ##
      Null deviance: 270,54 on 213 degrees of freedom
 ## Residual deviance: 250,79 on 212 degrees of freedom
 ## AIC: 254,79
 ## Number of Fisher Scoring iterations: 7
"Fe"
 glm_fit_fe <- glm(Type ~ Fe, data = Glass,
            family = "binomial")
 summary(glm_fit_fe)
 ##
 ## Call:
 ## glm(formula = Type ~ Fe, family = "binomial", data = Glass)
 ##
 ## Deviance Residuals:
 ## Min 1Q Median
                              3Q
 ## -1,4951 -1,4949 0,8901 0,8902 0,8902
```

```
##
## Coefficients:
```

```
## Warning in printCoefmat(coefs, digits = digits, signif.stars = signif.stars, : B
## результате преобразования созданы NA
```

```
Estimate Std. Error z value Pr(>|z|)
## (Intercept) 0,72123 0,16891 4,270 1,96e-05 ***
## Fe
           0,00147 1,49893 0,001 0,999
## ---
## Signif. codes: 0 '***' 0,001 '**' 0,01 '*' 0,05 '.' 0,1 ' ' 1
## (Dispersion parameter for binomial family taken to be 1)
    Null deviance: 270,54 on 213 degrees of freedom
##
## Residual deviance: 270,54 on 212 degrees of freedom
## AIC: 274,54
## Number of Fisher Scoring iterations: 4
```

"All predictors"

```
glm_fit_all <- glm(Type ~ RI + Na + Mg + AI + Si + K + Ca + Ba + Fe , data = Glass,
          family = "binomial")
summary(glm_fit_all)
```

```
##
 ## Call:
 ## glm(formula = Type \sim RI + Na + Mg + AI + Si + K + Ca + Ba + Fe,
      family = "binomial", data = Glass)
 ##
 ##
 ## Deviance Residuals:
 ## Min 1Q Median 3Q Max
 ## -1,82235 -0,75017 0,04975 0,72806 2,19096
 ##
 ## Coefficients:
 ## Warning in printCoefmat(coefs, digits = digits, signif.stars = signif.stars, : B
 ## результате преобразования созданы NA
           Estimate Std. Error z value Pr(>|z|)
 ## (Intercept) 575,3570 341,4893 1,685 0,09202.
 ## RI
           -67,1196 192,6359 -0,348 0,72752
 ## Na
            -3,5201 2,0937 -1,681 0,09271 .
 ## Mg
            -6,1380 2,2075 -2,780 0,00543 **
           -1,4019 2,3365 -0,600 0,54850
-5,0003 2,0758 -2,409 0,01600 *
 ## Al
 ## Si
           -4,4712 2,4649 -1,814 0,06969.
 ## K
           -4,3862 2,1879 -2,005 0,04499 *
 ## Ca
            -4,9974 2,5373 -1,970 0,04889 *
 ## Ba
 ## Fe
           0,9779 2,0595 0,475 0,63489
 ## Signif. codes: 0 '***' 0,001 '**' 0,01 '*' 0,05 '.' 0,1 ' ' 1
 ## (Dispersion parameter for binomial family taken to be 1)
 ##
 ## Null deviance: 270,54 on 213 degrees of freedom
 ## Residual deviance: 178,67 on 204 degrees of freedom
 ## AIC: 198,67
 ## Number of Fisher Scoring iterations: 7
"Best"
 glm_fit_best \leftarrow glm(Type \sim Mg + Al + Si, data = Glass,
           family = "binomial")
 summary(glm_fit_best)
 ##
 ## Call:
 ## glm(formula = Type ~ Mg + Al + Si, family = "binomial", data = Glass)
 ## Deviance Residuals:
 ## Min 1Q Median 3Q
                                      Max
 ## -1,79584 -0,88280 0,06546 0,83801 2,15389
 ## Coefficients:
 ## Warning in printCoefmat(coefs, digits = digits, signif.stars = signif.stars, : в
 ## результате преобразования созданы NA
           Estimate Std. Error z value Pr(>|z|)
 ## (Intercept) 56,5629 26,6852 2,120 0,034036 *
 ## Mg
          -1,5989 0,4144 -3,858 0,000114 ***
 ## AI
            3,1030 0,6993 4,437 9,11e-06 ***
 ## Si
           -0,7529 0,3602 -2,090 0,036610 *
 ## ---
 ## Signif. codes: 0 '***' 0,001 '**' 0,01 '*' 0,05 '.' 0,1 ' ' 1
 ## (Dispersion parameter for binomial family taken to be 1)
 ##
     Null deviance: 270,54 on 213 degrees of freedom
 ## Residual deviance: 189,31 on 210 degrees of freedom
 ## AIC: 197,31
 ## Number of Fisher Scoring iterations: 7
```

```
## Call:
## glm(formula = Type ~ one + two + three, family = "binomial",
## data = Glass)
##
## Deviance Residuals:
## Min 1Q Median 3Q Max
## -1,95507 -0,84954 0,06482 0,77752 2,08106
##
## Coefficients:
```

Warning in printCoefmat(coefs, digits = digits, signif.stars = signif.stars, : в ## результате преобразования созданы NA

```
## Estimate Std. Error z value Pr(>|z|)
## (Intercept) 2,082e+01 9,388e+00 2,218 0,026538 *
## one -1,507e+00 4,055e-01 -3,717 0,000202 ***
## two 1,410e+00 3,077e-01 4,581 4,63e-06 ***
## three -4,617e-05 2,278e-05 -2,027 0,042648 *
## ---
## Signif. codes: 0 '***' 0,001 '**' 0,01 '*' 0,05 '.' 0,1 '' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
## Null deviance: 270,54 on 213 degrees of freedom
## Residual deviance: 185,78 on 210 degrees of freedom
## AIC: 193,78
##
## Number of Fisher Scoring iterations: 7
```

```
## Real
## pred_glm 1 2 3 5 6 7
## FALSE 10 3 0 0 0 0
## TRUE 8 16 5 4 3 8
```

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[1] 0,8