## hw4

### Valeriia

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```
library(MASS)
library(dplyr)
library(data.table)
library(ggplot2)
library(caret)
library(boot)
library(tree)
library(rpart)
library(randomForest)
library(gbm)
data(Boston)
bos <- Boston
str(bos)
## 'data.frame':
                   506 obs. of 14 variables:
## $ crim : num 0.00632 0.02731 0.02729 0.03237 0.06905 ...
            : num 18 0 0 0 0 0 12.5 12.5 12.5 12.5 ...
## $ indus : num 2.31 7.07 7.07 2.18 2.18 2.18 7.87 7.87 7.87 7.87 ...
## $ chas : int 0000000000...
           : num 0.538 0.469 0.469 0.458 0.458 0.458 0.524 0.524 0.524 0.524 ...
## $ nox
           : num 6.58 6.42 7.18 7 7.15 ...
## $ rm
## $ age
          : num 65.2 78.9 61.1 45.8 54.2 58.7 66.6 96.1 100 85.9 ...
## $ dis
          : num 4.09 4.97 4.97 6.06 6.06 ...
           : int 1223335555...
## $ rad
           : num 296 242 242 222 222 222 311 311 311 311 ...
## $ tax
## $ ptratio: num 15.3 17.8 17.8 18.7 18.7 18.7 15.2 15.2 15.2 15.2 ...
## $ black : num 397 397 393 395 397 ...
## $ lstat : num 4.98 9.14 4.03 2.94 5.33 ...
## $ medv : num 24 21.6 34.7 33.4 36.2 28.7 22.9 27.1 16.5 18.9 ...
dim(bos)
## [1] 506 14
sum(is.na(bos))
```

## [1] 0

#### summary(bos)

```
##
         crim
                                              indus
                                                                chas
                              zn
           : 0.00632
                                                                  :0.0000
##
                               :
                                  0.00
                                                 : 0.46
    Min.
                        Min.
                                          Min.
                                                           Min.
    1st Qu.: 0.08204
                        1st Qu.:
                                  0.00
                                          1st Qu.: 5.19
                                                           1st Qu.:0.00000
    Median : 0.25651
                                          Median: 9.69
##
                        Median :
                                  0.00
                                                           Median :0.00000
           : 3.61352
                                                 :11.14
##
    Mean
                        Mean
                               : 11.36
                                          Mean
                                                           Mean
                                                                  :0.06917
##
    3rd Qu.: 3.67708
                        3rd Qu.: 12.50
                                          3rd Qu.:18.10
                                                           3rd Qu.:0.00000
           :88.97620
                               :100.00
                                                 :27.74
                                                                  :1.00000
##
    Max.
                        Max.
                                          Max.
                                                           Max.
##
         nox
                            rm
                                            age
                                                              dis
                                                                : 1.130
                                                2.90
##
    Min.
           :0.3850
                      Min.
                             :3.561
                                      Min.
                                              :
                                                        Min.
                                       1st Qu.: 45.02
##
    1st Qu.:0.4490
                      1st Qu.:5.886
                                                         1st Qu.: 2.100
##
    Median :0.5380
                      Median :6.208
                                      Median : 77.50
                                                        Median : 3.207
                             :6.285
##
    Mean
           :0.5547
                      Mean
                                       Mean
                                              : 68.57
                                                        Mean
                                                               : 3.795
##
    3rd Qu.:0.6240
                      3rd Qu.:6.623
                                       3rd Qu.: 94.08
                                                         3rd Qu.: 5.188
##
    Max.
           :0.8710
                      Max.
                             :8.780
                                       Max.
                                              :100.00
                                                         Max.
                                                                :12.127
##
                                          ptratio
                                                            black
         rad
                           tax
##
    Min.
           : 1.000
                      Min.
                             :187.0
                                       Min.
                                              :12.60
                                                        Min.
                                                               : 0.32
##
    1st Qu.: 4.000
                      1st Qu.:279.0
                                       1st Qu.:17.40
                                                        1st Qu.:375.38
##
   Median : 5.000
                      Median :330.0
                                       Median :19.05
                                                        Median :391.44
##
    Mean
           : 9.549
                             :408.2
                                              :18.46
                                                               :356.67
                      Mean
                                       Mean
                                                        Mean
##
    3rd Qu.:24.000
                      3rd Qu.:666.0
                                       3rd Qu.:20.20
                                                        3rd Qu.:396.23
##
    Max.
           :24.000
                      Max.
                             :711.0
                                       Max.
                                              :22.00
                                                        Max.
                                                               :396.90
##
        lstat
                          medv
##
   Min.
           : 1.73
                            : 5.00
                     Min.
    1st Qu.: 6.95
                     1st Qu.:17.02
##
##
   Median :11.36
                    Median :21.20
##
    Mean
           :12.65
                     Mean
                            :22.53
##
    3rd Qu.:16.95
                     3rd Qu.:25.00
    Max.
           :37.97
                     Max.
                            :50.00
```

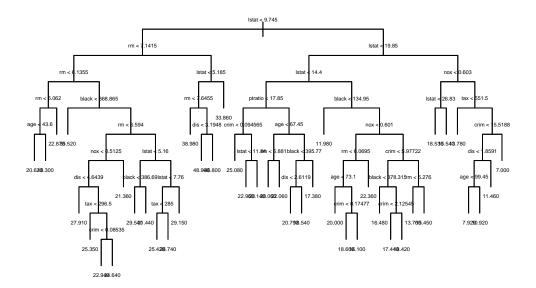
#### sum(duplicated(bos))

#### ## [1] 0

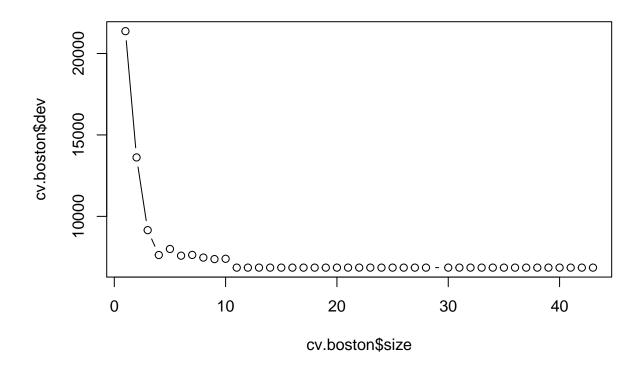
This plot shows the Error and the Number of Trees. We can easily notice that how the Error is dropping as we keep on adding more and more trees and average them.

Although the most complex tree is selected by cross-validation (the lowest error rate corresponds to the most complex tree with 6 leaves), if we wanted to prune the tree, we would do it as follows, using the prune.tree() function.

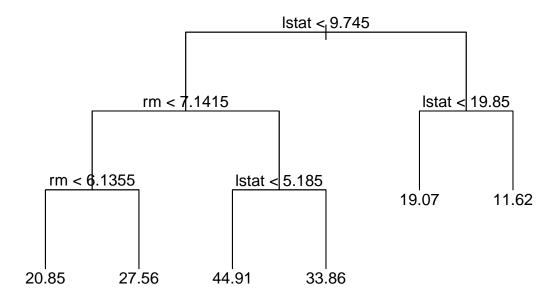
```
set.seed(3)
train <- sample(nrow(bos), 0.5*nrow(bos), replace = FALSE)
TrainSet <- bos[train,]
ValidSet <- bos[-train,]
tree.boston = tree(medv~.,Boston ,subset =train,mindev=.0001)
plot(tree.boston,type="u")
text(tree.boston,pretty=0,cex=0.3)</pre>
```



```
cv.boston = cv.tree(tree.boston)
plot(cv.boston$size,cv.boston$dev,type="b")
```

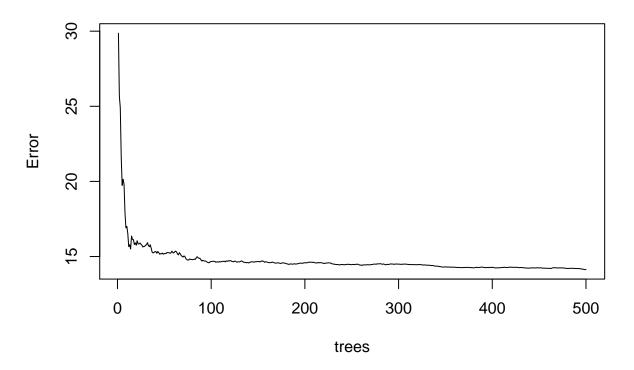


```
prune.boston = prune.tree(tree.boston,best=6)
plot(prune.boston,type="u")
text(prune.boston,pretty=0)
```

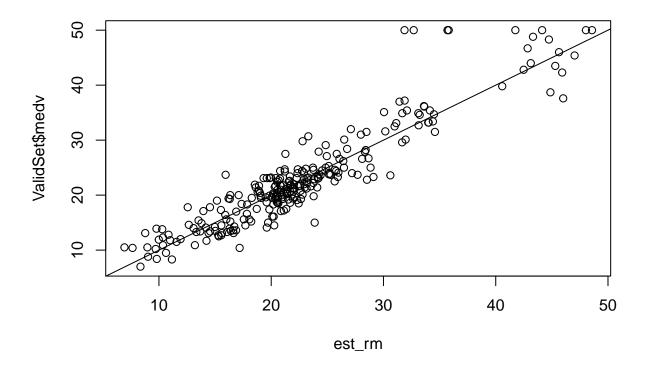


```
set.seed(13)
mod <- randomForest(medv ~ ., data = TrainSet, mtry = 13, importance = T)
plot(mod)</pre>
```

## mod



```
mod
##
## Call:
##
    randomForest(formula = medv ~ ., data = TrainSet, mtry = 13,
                                                                           importance = T)
##
                   Type of random forest: regression
##
                         Number of trees: 500
\mbox{\tt \#\#} No. of variables tried at each split: 13
##
             Mean of squared residuals: 14.1463
##
##
                        % Var explained: 83.12
est_rm <- predict(mod, newdata = ValidSet)</pre>
plot(est_rm, ValidSet$medv)
abline(0,1)
```



```
mean((est_rm - ValidSet$medv)^2)
```

## [1] 11.67461

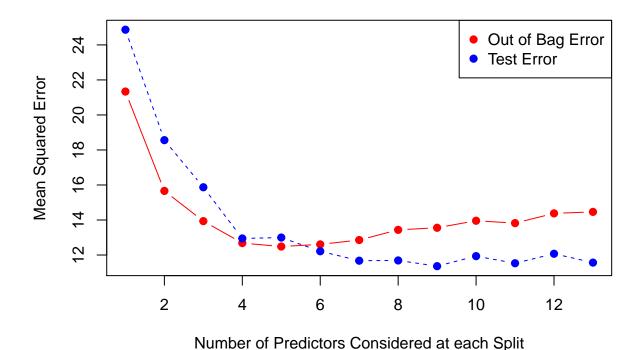
We could now try all possible 13 predictors which can be found at each split. Now what we observe is that the Red line is the Out of Bag Error Estimates and the Blue Line is the Error calculated on Test Set. Both curves are quite smooth and the error estimates are somewhat correlated too.

```
set.seed(13)
oob.err<-double(13)
test.err<-double(13)

#mtry is no of Variables randomly chosen at each split
for(mtry in 1:13)
{
    rf=randomForest(medv ~ . , data = TrainSet,mtry=mtry,ntree=400)
    oob.err[mtry] = rf$mse[400] #Error of all Trees fitted

    pred<-predict(rf,ValidSet) #Predictions on Test Set for each Tree
    test.err[mtry] = with(ValidSet, mean( (medv - pred)^2)) #Mean Squared Test Error
    cat(mtry," ")
}</pre>
```

```
matplot(1:mtry , cbind(oob.err,test.err), pch=19 , col=c("red","blue"),type="b",ylab="Mean Squared Error
legend("topright",legend=c("Out of Bag Error","Test Error"),pch=19, col=c("red","blue"))
```

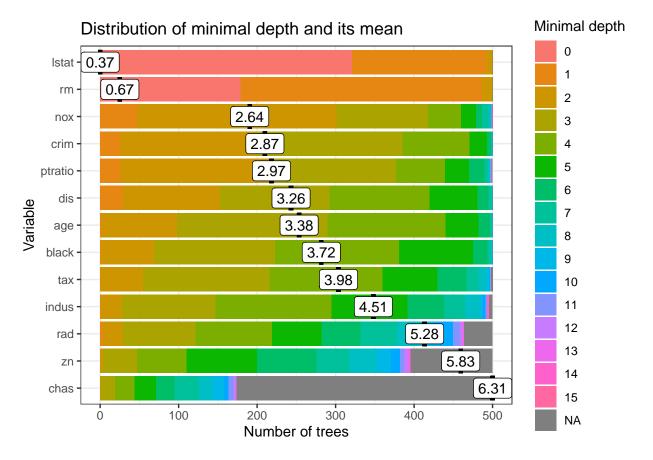


Next, we pass it to the function plot\_min\_depth\_distribution and under default settings obtain obtain a plot of the distribution of minimal depth for top ten variables according to mean minimal depth calculated using top trees (mean\_sample = "top\_trees"). We could also pass our forest directly to the plotting function but if we want to make more than one plot of the minimal depth distribution is more efficient to pass the min\_depth\_frame to the plotting function so that it will not be calculated again for each plot (this works similarly for other plotting functions of randomForestExplainer).

#### library(randomForestExplainer)

```
## Registered S3 method overwritten by 'GGally':
## method from
## +.gg ggplot2

min_depth_frame <- min_depth_distribution(mod)
plot_min_depth_distribution(min_depth_frame, mean_sample = "relevant_trees", k = 15)</pre>
```



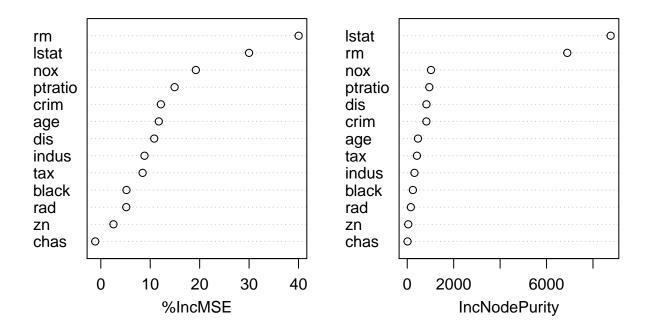
```
set.seed(13)
bag.boston=randomForest(medv~.,data=TrainSet,mtry=9, importance=TRUE)
yhat.bag = predict(bag.boston,newdata=ValidSet)
mean((yhat.bag-ValidSet$medv)^2)
```

#### ## [1] 11.61344

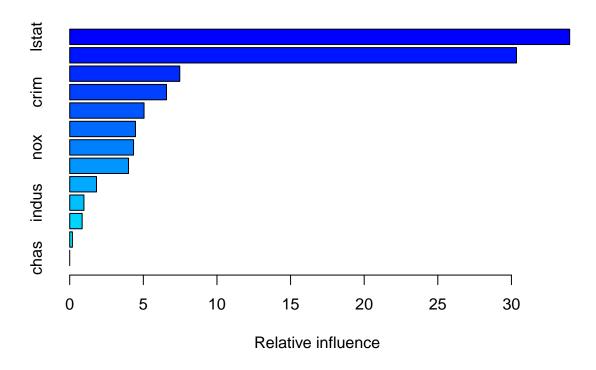
### importance(bag.boston)

```
%IncMSE IncNodePurity
##
           12.147639
                         824.80963
## crim
                          43.48682
            2.557948
## zn
## indus
            8.840377
                         311.06503
## chas
           -1.128566
                          12.92043
## nox
           19.228600
                        1022.46314
           40.028419
                        6892.82790
## rm
           11.733696
                         463.31816
## age
## dis
           10.805116
                         826.29924
            5.149959
                         155.78841
## rad
## tax
            8.457679
                         417.46830
## ptratio 14.929554
                         950.81755
## black
            5.188529
                         243.23221
## lstat
           29.990160
                        8761.13215
```

## bag.boston



set.seed(13)
boost.boston=gbm(medv~.,data=TrainSet,distribution="gaussian",n.trees=5000,interaction.depth=4)
summary(boost.boston)



```
##
                        rel.inf
               var
## lstat
             lstat 3.395648e+01
## rm
                rm 3.034449e+01
## dis
               dis 7.473351e+00
              crim 6.574485e+00
## crim
## ptratio ptratio 5.047400e+00
## age
               age 4.464963e+00
## nox
               nox 4.335555e+00
             black 3.993297e+00
## black
## tax
               tax 1.819489e+00
             indus 9.649379e-01
## indus
               rad 8.443563e-01
## rad
                zn 1.811841e-01
## zn
## chas
              chas 6.817918e-06
```

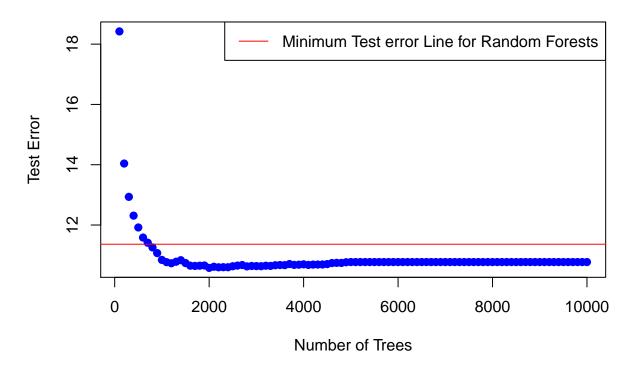
boost.boston=gbm(medv~.,data=TrainSet,distribution="gaussian",n.trees=5000,interaction.depth=4,shrinkag
yhat.boost=predict(boost.boston,newdata=ValidSet,n.trees=5000)
mean((yhat.boost-ValidSet\$medv)^2)

```
## [1] 10.77138
```

```
n.trees = seq(from=100 ,to=10000, by=100) #no of trees-a vector of 100 values
#Generating a Prediction matrix for each Tree
```

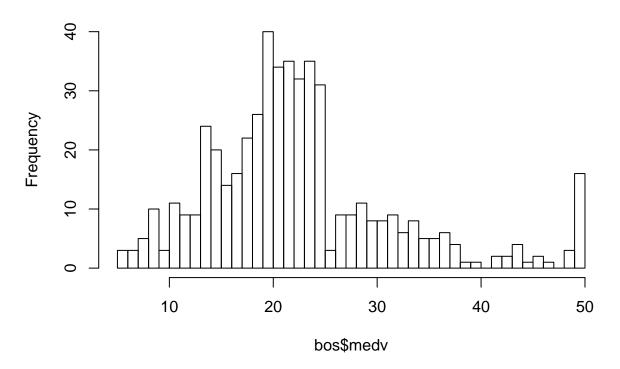
```
predmatrix<-predict(boost.boston,Boston[-train,],n.trees = n.trees)</pre>
dim(predmatrix) #dimentions of the Prediction Matrix
## [1] 253 100
#Calculating The Mean squared Test Error
test.error<-with(Boston[-train,],apply( (predmatrix-medv)^2,2,mean))</pre>
head(test.error) #contains the Mean squared test error for each of the 100 trees averaged
##
        100
                 200
                          300
                                   400
                                             500
## 18.42201 14.03957 12.93418 12.31029 11.91826 11.58359
#Plotting the test error vs number of trees
plot(n.trees , test.error , pch=19,col="blue",xlab="Number of Trees",ylab="Test Error", main = "Perfoma
#adding the RandomForests Minimum Error line trained on same data and similar parameters
abline(h = min(test.err),col="red") #test.err is the test error of a Random forest fitted on same data
legend("topright",c("Minimum Test error Line for Random Forests"),col="red",lty=1,lwd=1)
```

## **Perfomance of Boosting on Test Set**

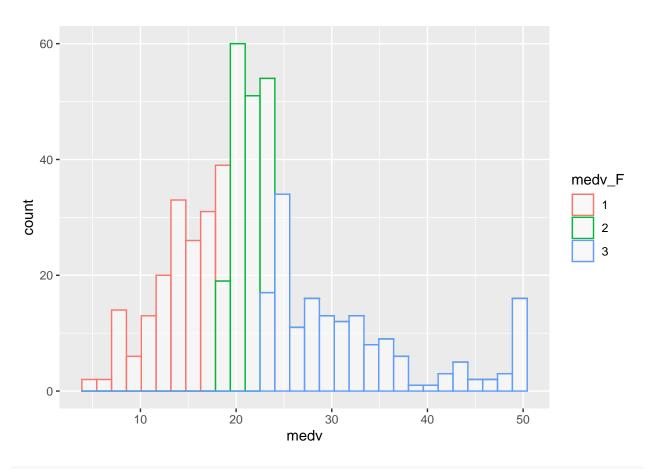


```
hist(bos$medv, breaks = 50)
```

# Histogram of bos\$medv



## `stat\_bin()` using `bins = 30`. Pick better value with `binwidth`.



```
## ntree
              00B
                       1
                              2
           31.77% 32.84% 38.33% 24.62%
##
       2:
           26.25% 29.07% 29.17% 20.73%
##
##
           28.23% 29.89% 35.53% 20.00%
           25.50% 22.99% 34.62% 19.77%
##
       8:
           25.79% 20.45% 37.18% 20.93%
##
      10:
##
      12:
           26.09% 22.47% 34.62% 22.09%
           23.72% 20.22% 33.33% 18.60%
##
      16: 23.72% 19.10% 33.33% 19.77%
##
           23.72% 20.22% 33.33% 18.60%
##
      18:
##
      20: 22.53% 17.98% 30.77% 19.77%
##
      22: 23.72% 19.10% 34.62% 18.60%
      24: 24.51% 17.98% 35.90% 20.93%
##
```

```
26: 22.13% 17.98% 30.77% 18.60%
##
      28: 22.92% 19.10% 32.05% 18.60%
##
      30: 22.53% 19.10% 33.33% 16.28%
##
##
      32: 22.53% 19.10% 32.05% 17.44%
      34: 21.74% 19.10% 29.49% 17.44%
##
##
      36: 22.13% 17.98% 32.05% 17.44%
##
      38: 22.92% 17.98% 34.62% 17.44%
      40: 22.92% 17.98% 34.62% 17.44%
##
      42: 22.92% 19.10% 33.33% 17.44%
##
##
      44: 23.32% 19.10% 34.62% 17.44%
      46: 23.72% 17.98% 35.90% 18.60%
      48: 23.72% 17.98% 35.90% 18.60%
##
      50: 22.92% 17.98% 35.90% 16.28%
set.seed(3)
rf <- randomForest(medv_F ~ ., data=bos,</pre>
                   subset = train,
                   ntree = 30,
                   mtry = mtry,
                   sampsize = sampsize,
                   importance = TRUE)
rf
##
## Call:
## randomForest(formula = medv_F ~ ., data = bos, ntree = 30, mtry = mtry,
                                                                                 sampsize = sampsize, i
##
                  Type of random forest: classification
                        Number of trees: 30
##
## No. of variables tried at each split: 3
##
##
           OOB estimate of error rate: 22.53%
## Confusion matrix:
     1 2 3 class.error
## 1 72 16 1 0.1910112
## 2 14 52 12 0.3333333
## 3 2 12 72
              0.1627907
pred <- predict(rf, newdata = bos[-train,])</pre>
mean(pred!=bos$medv_F[-train])
## [1] 0.2134387
varImpPlot(rf)
```

