Statistics in R: Task 0

```
library(ggplot2)
library(ggpubr)
```

1. Measures of center

```
x <- c(175, 176, 182, 165, 167, 172, 175, 196, 158, 172)
```

Mode

```
mode_my <- function(sample) {
  tab <- table(sample)
   as.numeric(names(tab)[tab == max(tab)])
}
mode_my_x <- mode_my(x)
mode_my_x</pre>
```

[1] 172 175

Median

```
median_my <- function(sample) {
   sorted <- sort(sample)
   (sorted[length(sample) / 2] + sorted[length(sample) / 2 + 1]) / 2
}
median_my_x <- median_my(x)
median_builtin_x <- median(x)</pre>
median_builtin_x
```

```
## [1] 173.5
median_my_x
```

[1] 173.5

Mean

```
mean_my <- function(sample) {
    sum(sample) / length(sample)
}
mean_my_x <- mean_my(x)

mean_builtin_x <- mean(x)
mean_trim_x <- mean(x, trim = 0.1)

mean_builtin_x

## [1] 173.8

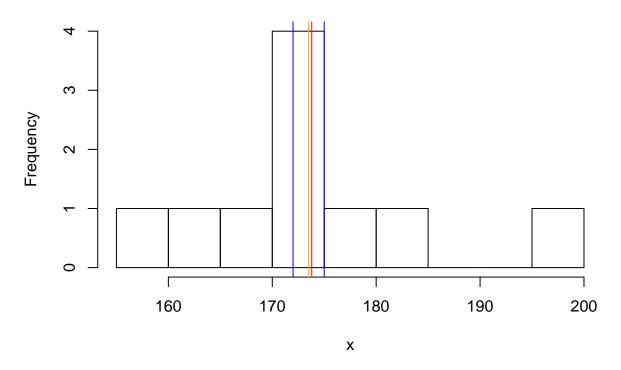
mean_my_x

## [1] 173.8</pre>
```

${\bf Histogram}$

```
hist(x, breaks=10)
abline(v = mode_my_x, col="blue")
abline(v = median_my_x, col="orange")
abline(v = mean_my_x, col="red")
```

Histogram of x



Sample with an outlier

```
x_outl <- c(x, 2)

mode_my_outl <- mode_my(x_outl)

median_builtin_outl <- median(x_outl)

median_my_outl <- median_my(x_outl)

mean_builtin_outl <- mean(x_outl)

mean_my_outl <- mean_my(x_outl)

mean_trim_outl <- mean(x_outl, trim = 0.1)

mode_my_outl</pre>
```

[1] 172 175

median_builtin_outl

[1] 172

```
median_my_outl

## [1] 172

mean_builtin_outl

## [1] 158.1818

mean_my_outl

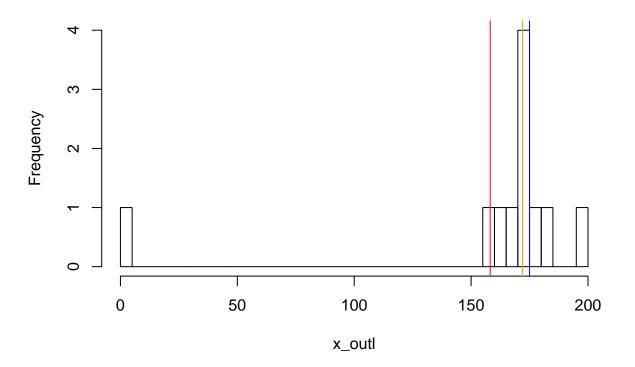
## [1] 158.1818

mean_trim_outl

## [1] 171.3333

hist(x_outl, breaks=30)
abline(v = mode_my_outl, col="blue")
```

Histogram of x_outl



One of the modes and the median are overlapping.

abline(v = median_my_outl, col="orange")
abline(v = mean_my_outl, col="red")

2. Measures of spread

Variance

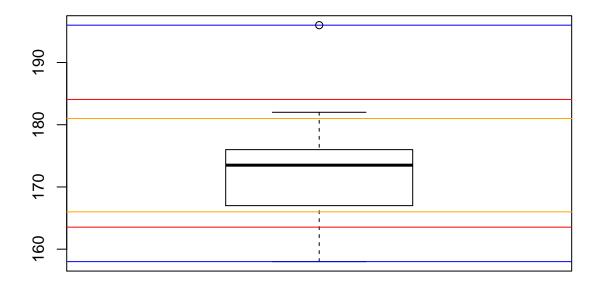
```
var_builtin_x <- var(x)</pre>
var_my <- function(sample) {</pre>
  sum <- 0
  for (i in 1:length(sample)) {
    sum = sum + (sample[i] - mean_builtin_x)^2
  sum / (length(sample) - 1)
var_my_x <- var_my(x)</pre>
var_builtin_x
## [1] 105.2889
var_my_x
## [1] 105.2889
```

SD

```
sd_builtin_x \leftarrow sd(x)
sd_my_x <- sqrt(var_my_x)</pre>
sd_builtin_x
## [1] 10.26104
sd_my_x
## [1] 10.26104
```

Boxplot

```
iqr_x \leftarrow IQR(x)
boxplot(x)
abline(h = range(x), col="blue")
abline(h = median_builtin_x + iqr_x, col="orange")
abline(h = median_builtin_x - iqr_x, col="orange")
abline(h = mean_builtin_x + sd_builtin_x, col="red")
abline(h = mean_builtin_x - sd_builtin_x, col="red")
```



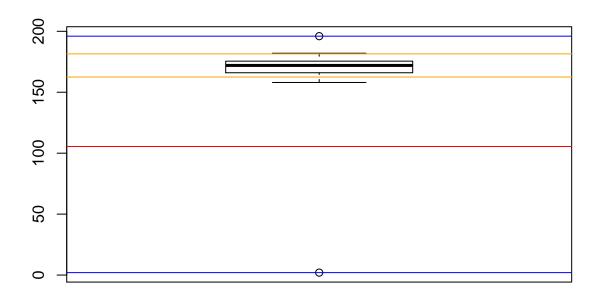
Sample with an outlier

```
iqr_outl <- IQR(x_outl)

sd_outl <- sd(x_outl)

boxplot(x_outl)

abline(h = range(x_outl), col="blue")
abline(h = median_builtin_outl + iqr_outl, col="orange")
abline(h = median_builtin_outl - iqr_outl, col="orange")
abline(h = mean_builtin_outl + sd_outl, col="red")
abline(h = mean_builtin_outl - sd_outl, col="red")</pre>
```



 $(mean_builtin_outl + sd_outl)$ is outside of the plot.

3. Properties

Checking

```
sub <- x - 100
div <- x / 100
all.equal(mean(sub), mean(x) - 100)

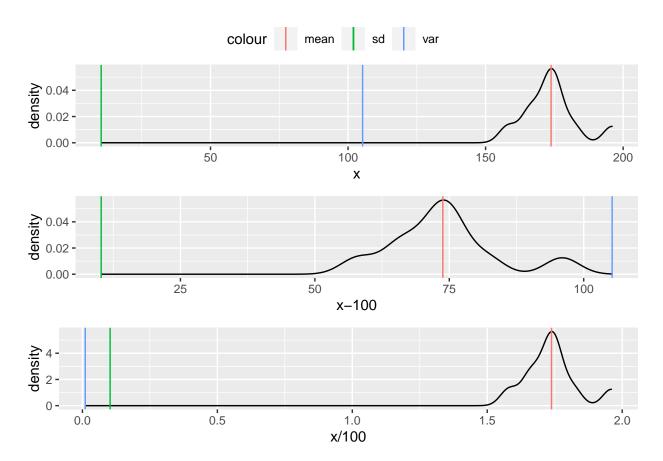
## [1] TRUE
all.equal(mean(div), mean(x) / 100)

## [1] TRUE
abs(sum(x - mean(x)) - 0) < 0.000000001</pre>
```

```
all.equal(var(sub), var(x))
## [1] TRUE
all.equal(var(div), var(x) / 10000)
## [1] TRUE
all.equal(sd(div), sd(x) / 100)
## [1] TRUE
Visualization
Table
prop_df <- matrix(c(mean(x), mean(sub), mean(div),</pre>
                        var(x), var(sub), var(div),
                         sd(x), sd(sub), sd(div)), ncol=3,byrow=TRUE)
colnames(prop_df) <- c('x', 'x-100', 'x/100')</pre>
rownames(prop_df) <- c("mean", "var", "sd")</pre>
prop_df <- as.data.frame(prop_df)</pre>
prop_df
##
                       x-100
                                   x/100
## mean 173.80000 73.80000 1.73800000
## var 105.28889 105.28889 0.01052889
## sd
         10.26104 10.26104 0.10261037
Plot
data_df <- cbind(x, sub, div)</pre>
samples_ids <- c('x', 'x-100', 'x/100')
colnames(data_df) <- samples_ids</pre>
prop_df <- rbind(prop_df, data_df)</pre>
plot <- function(sample_id) {</pre>
  info <- prop_df[[sample_id]]</pre>
  ggplot() +
    aes(info[4:13]) +
    geom_density() +
    geom_vline(aes(xintercept=info[[1]], color="mean")) +
    geom_vline(aes(xintercept=info[[2]], color="var")) +
    geom_vline(aes(xintercept=info[[3]], color="sd")) +
    xlab(sample_id)
```

}

```
# not working with cycle; with cycle through samples_ids instead of apply
# it will use the last sample_id in all plots, so all plots will be the same
plots <- lapply(samples_ids, plot)
ggarrange(plotlist=plots, ncol=1, common.legend = TRUE)</pre>
```



4. Normal distribution

```
set.seed(42)

# p(x < 156)
pnorm(156, mean=175, sd=10)

## [1] 0.02871656

# p(x > 198)
pnorm(198, mean=175, sd=10, lower=FALSE)
```

[1] 0.01072411

```
# p(168 < x < 172)
obs <- 1e5
sample <- rnorm(obs, mean=175, sd=10)
sum(sample > 168 & sample < 172) / obs

## [1] 0.13851

Standard normal distribution</pre>
```

```
# mean = 0, sd = 1
sample <- rnorm(obs)
# +/- 1 sd: 68%
sum(sample > -1 & sample < 1) / obs

## [1] 0.68135

# +/- 2 sd: 95%
sum(sample > -2 & sample < 2) / obs

## [1] 0.95408

# +/- 3 sd: 99.7%
sum(sample > -3 & sample < 3) / obs

## [1] 0.99679</pre>
```

Standardization

[1] 1

```
sample <- rnorm(obs, mean=175, sd=10)
mean(sample)

## [1] 174.992

sd(sample)

## [1] 10.00118

sample <- scale(sample, center=TRUE, scale=TRUE)
mean(sample)

## [1] 1.44957e-15

sd(sample)</pre>
```

5. Central Limit Theorem

```
stat_by_k <- function(population, k) {</pre>
  samples <- replicate(n, sample(population, k))</pre>
  means <- colMeans(samples)</pre>
  c(k, mean(means), sd(means), sd(means)/sqrt(n), means)
obs <- 1e6
population <- rnorm(obs)</pre>
ks \leftarrow c(10, 50, 100, 500)
n <- 30
stat <- data.frame()</pre>
distr <- vector(mode="list", length=length(ks))</pre>
names(distr) <- ks</pre>
for (k in ks) {
  stat_temp <- stat_by_k(population, k)</pre>
  stat <- rbind(stat, stat_temp[1:4])</pre>
  distr[[as.character(k)]] <- stat_temp[5:n+4]</pre>
colnames(stat) <- c('k', 'mean', 'sd', 'SE')</pre>
stat
##
                 mean
                                sd
## 1 10 0.134680648 0.34136140 0.06232378
## 2 50 0.002981947 0.13294629 0.02427256
## 3 100 0.022223126 0.08261959 0.01508420
## 4 500 0.002207400 0.04512560 0.00823877
plot <- function(k) {</pre>
  ggplot() +
    aes(distr[[as.character(k)]]) +
    geom_histogram() +
    geom_vline(aes(xintercept=stat[stat$k == k, 2], color="mean")) +
    geom_vline(aes(xintercept=stat[stat$k == k, 4], color="SE")) +
    xlab(paste(k, " observations")) +
    xlim(-0.5, 0.5)
}
plots <- lapply(ks, plot)</pre>
ggarrange(plotlist=plots, common.legend = TRUE)
```

