HW2.1_Mary_Futey

Mary Futey

4/3/2020

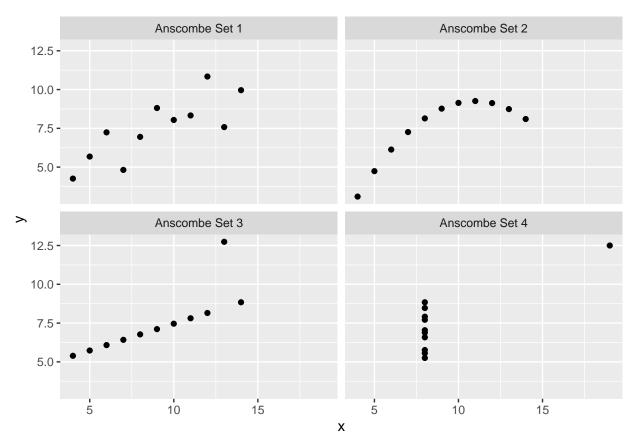
Part 1: Anscombe's dataset

*Scatter plot facetted by set

knitr::kable(anscombe)

x1	x2	х3	x4	y1	y2	у3	y4
10	10	10	8	8.04	9.14	7.46	6.58
8	8	8	8	6.95	8.14	6.77	5.76
13	13	13	8	7.58	8.74	12.74	7.71
9	9	9	8	8.81	8.77	7.11	8.84
11	11	11	8	8.33	9.26	7.81	8.47
14	14	14	8	9.96	8.10	8.84	7.04
6	6	6	8	7.24	6.13	6.08	5.25
4	4	4	19	4.26	3.10	5.39	12.50
12	12	12	8	10.84	9.13	8.15	5.56
7	7	7	8	4.82	7.26	6.42	7.91
5	5	5	8	5.68	4.74	5.73	6.89

```
anscombe.1 <- data.frame(x = anscombe[["x1"]],</pre>
                          y = anscombe[["y1"]],
                          Set = "Anscombe Set 1")
anscombe.2 <- data.frame(x =</pre>
                             anscombe[["x2"]],
                          y = anscombe[["y2"]],
                          Set = "Anscombe Set 2")
anscombe.3 <- data.frame(x = anscombe[["x3"]],</pre>
                           y = anscombe[["y3"]],
                          Set = "Anscombe Set 3")
anscombe.4 <- data.frame(x = anscombe[["x4"]],</pre>
                           y = anscombe[["y4"]],
                           Set = "Anscombe Set 4")
anscombe.data <- rbind(anscombe.1, anscombe.2, anscombe.3, anscombe.4)
ans_facet <- ggplot(anscombe.data,</pre>
                     aes(x = x,
                         y = y))+
  geom_point(color = "black")+
  facet_wrap(~Set, ncol = 2)
ans_facet
```



^{*}Summary calculation (mean, sd) grouped by set

```
aggregate(cbind(x, y) ~ Set, anscombe.data, mean)
```

```
## 1 Anscombe Set 1 9 7.500909
## 2 Anscombe Set 2 9 7.500909
## 3 Anscombe Set 3 9 7.500000
## 4 Anscombe Set 4 9 7.500909
```

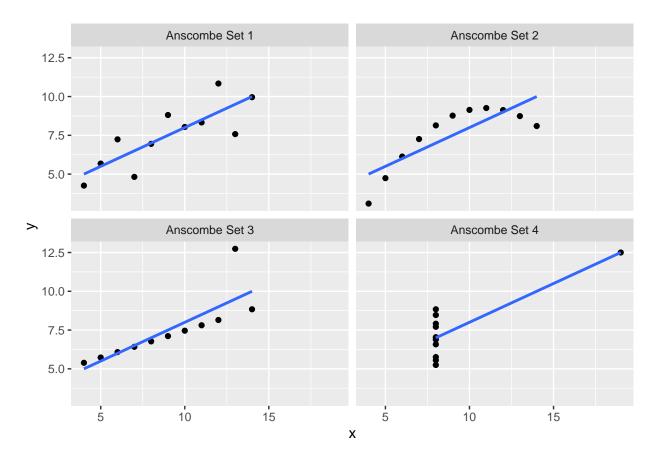
aggregate(cbind(x, y) ~ Set, anscombe.data, sd)

```
## 1 Anscombe Set 1 3.316625 2.031568
## 2 Anscombe Set 2 3.316625 2.031657
## 3 Anscombe Set 3 3.316625 2.030424
## 4 Anscombe Set 4 3.316625 2.030579
```

```
correlation <- function(data) {
    a <- data.frame(pearson = cor.test(data$x, data$y, method = "pearson")$statistic)
    b <- data.frame(p_pearson = cor.test(data$x, data$y, method = "pearson")$p.value)
    c <- data.frame(kendall = cor.test(data$x, data$y, method = "kendall")$statistic)
    d <- data.frame(p_kendall = cor.test(data$x, data$y, method = "kendall")$p.value)
    e <- data.frame(spearman = cor.test(data$x, data$y, method = "spearman")$statistic)
    f <- data.frame(p_spearman = cor.test(data$x, data$y, method = "spearman")$p.value)
    return(list(a, b, c, d, e, f))</pre>
```

^{*}Pearson's correlation by set, and non-parametric, and p-value

```
}
res <- correlation(anscombe.data)</pre>
## Warning in cor.test.default(data$x, data$y, method = "kendall"): Cannot compute
## exact p-value with ties
## Warning in cor.test.default(data$x, data$y, method = "kendall"): Cannot compute
## exact p-value with ties
## Warning in cor.test.default(data$x, data$y, method = "spearman"): Cannot compute
## exact p-value with ties
## Warning in cor.test.default(data$x, data$y, method = "spearman"): Cannot compute
## exact p-value with ties
ldply(res)
##
                 p_pearson kendall
                                       p_kendall spearman
                                                             p_spearman
      pearson
## 1 9.160764
                                              NA
## 2
           NA 1.436505e-11
                                 NA
                                              NA
                                                                     NA
                                                        NA
## 3
           NA
                        NA 6.05286
                                              NA
                                                        NA
                                                                     NA
## 4
           NA
                        NA
                                 NA 1.422967e-09
                                                        NA
                                                                     NA
## 5
           NA
                         NA
                                 NA
                                              NA 2598.395
                                                                     NA
## 6
           NA
                         NA
                                              NA
                                                        NA 1.360916e-11
                                 NA
*Add geom_smooth()totheplot
ans_smooth <- ans_facet +</pre>
  geom_smooth(formula = y ~ x, method = "lm", se = FALSE, data = anscombe.data)
ans_smooth
```



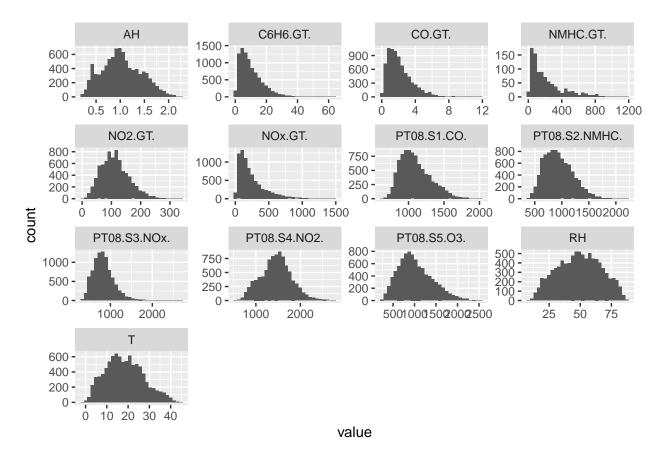
Air Quality dataset

- Explore data set, clean if needed: convert date and time to factor, check for NAs, switch comma to decimal
- Explore each variable independently: remove "-200" values as they are not possible / erroneous

```
Time CO.GT. PT08.S1.CO. NMHC.GT. C6H6.GT. PT08.S2.NMHC.
           Date
## 1 10/03/2004 18.00.00
                                                    150
                             2.6
                                         1360
                                                             11.9
                                                                            1046
## 2 10/03/2004 19.00.00
                             2.0
                                         1292
                                                    112
                                                              9.4
                                                                             955
## 3 10/03/2004 20.00.00
                             2.2
                                         1402
                                                     88
                                                              9.0
                                                                             939
## 4 10/03/2004 21.00.00
                             2.2
                                         1376
                                                     80
                                                              9.2
                                                                             948
## 5 10/03/2004 22.00.00
                             1.6
                                         1272
                                                     51
                                                              6.5
                                                                             836
                                                                             750
## 6 10/03/2004 23.00.00
                             1.2
                                         1197
                                                     38
                                                              4.7
     NOx.GT. PT08.S3.NOx. NO2.GT. PT08.S4.NO2. PT08.S5.O3.
                                                                      RH
                                                         1268 13.6 48.9 0.7578
## 1
         166
                      1056
                                113
                                             1692
## 2
         103
                      1174
                                 92
                                             1559
                                                          972 13.3 47.7 0.7255
## 3
         131
                                             1555
                                                         1074 11.9 54.0 0.7502
                      1140
                                114
## 4
         172
                                                         1203 11.0 60.0 0.7867
                      1092
                                122
                                             1584
                                                         1110 11.2 59.6 0.7888
## 5
         131
                      1205
                                116
                                             1490
## 6
          89
                      1337
                                 96
                                             1393
                                                          949 11.2 59.2 0.7848
```

airq_long <- gather(airq, key="measurement", value="value", -c(Date,Time))</pre>

```
airq_long$Date <- as.factor(airq_long$Date)</pre>
airq_long$Time <- as.factor(airq_long$Time)</pre>
airq_long$measurement <- as.factor(airq_long$measurement)</pre>
airq_fil <- airq_long %>%
  filter_all(all_vars(. != -200))
head(airq_fil)
##
                    Time measurement value
           Date
## 1 10/03/2004 18.00.00
                              CO.GT.
                                       2.6
## 2 10/03/2004 19.00.00
                              CO.GT. 2.0
## 3 10/03/2004 20.00.00
                              CO.GT.
                                       2.2
## 4 10/03/2004 21.00.00
                              CO.GT.
                                       2.2
## 5 10/03/2004 22.00.00
                              CO.GT.
                                       1.6
## 6 10/03/2004 23.00.00
                              CO.GT.
                                       1.2
colSums(is.na(airq_fil))
##
          Date
                      Time measurement
                                              value
##
p1 <- airq_fil %>% ggplot(aes(x = value)) +
  geom_histogram() +
  facet_wrap(~measurement, scales = "free")
p1
## `stat_bin()` using `bins = 30`. Pick better value with `binwidth`.
```



• Need to normalize data

```
airq_wide <- spread(airq_fil, key = "measurement" ,value = "value")
airq_wide <- na.omit(airq_wide)

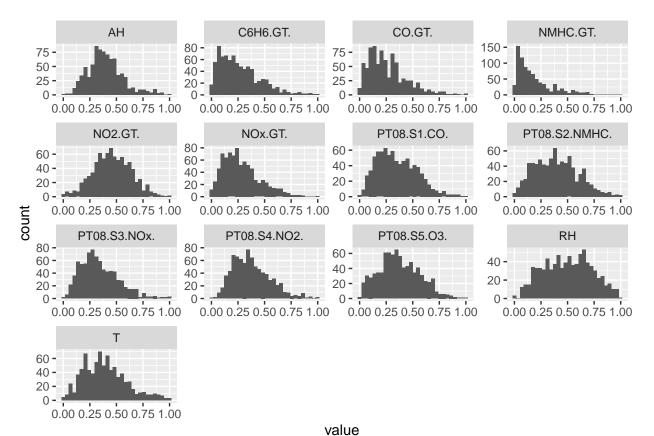
norm <- function(x) {
        (x - min(x)) / (max(x) - min(x))
}

airq_norm <- as.data.frame(lapply(airq_wide[3:15], norm))
airq_norm$Date <- airq_wide$Date
airq_norm$Time <- airq_wide$Time

airq_norm_long <- gather(airq_norm, key = "measurement", value = "value", -c(Date, Time))

p2 <- airq_norm_long %>% ggplot(aes(x = value)) +
        geom_histogram() +
        facet_wrap(~measurement, scales = "free")
```

`stat_bin()` using `bins = 30`. Pick better value with `binwidth`.

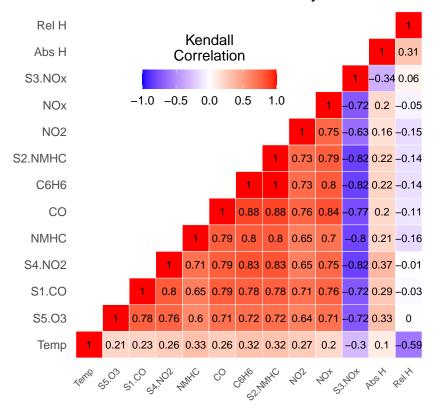


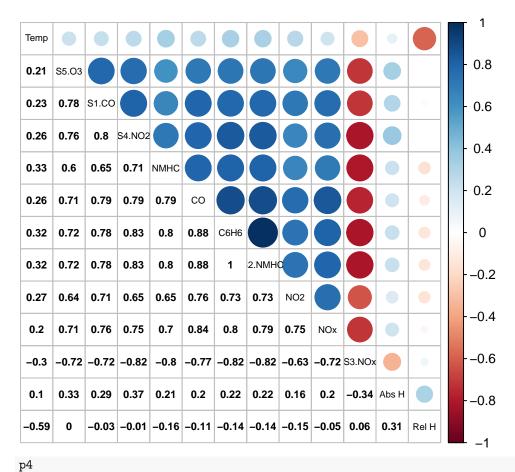
• Cross correlations

```
airq_sub <- airq_norm[, 1:13]
colnames(airq_sub) <- c(</pre>
  "Abs H",
  "C6H6",
  "CO",
  "NMHC",
  "NO2",
  "NOx",
  "S1.CO",
  "S2.NMHC",
  "S3.NOx",
  "S4.NO2",
  "S5.03",
  "Rel H",
  "Temp"
)
airq_cor <- round(cor(airq_sub, method = "kendall"),2)</pre>
#reorder, create upper triangle
reorder_airq_cor <- function(airq_cor){</pre>
  # Use correlation between variables as distance
  dd <- as.dist((1-airg cor)/2)</pre>
  hc <- hclust(dd)
  airq_cor <-airq_cor[hc$order, hc$order]</pre>
}
```

```
get_upper_tri <- function(airq_cor){</pre>
  airq_cor[lower.tri(airq_cor)] <- NA
 return(airq cor)
airq_cor <- reorder_airq_cor(airq_cor)</pre>
upper_tri <- get_upper_tri(airq_cor)</pre>
melt_uppertri <- melt(upper_tri, na.rm = TRUE)</pre>
## Warning in melt(upper_tri, na.rm = TRUE): The melt generic in data.table has
## been passed a matrix and will attempt to redirect to the relevant reshape2
## method; please note that reshape2 is deprecated, and this redirection is now
## deprecated as well. To continue using melt methods from reshape2 while both
## libraries are attached, e.g. melt.list, you can prepend the namespace like
## reshape2::melt(upper_tri). In the next version, this warning will become an
p3 <- ggplot(melt_uppertri,
             aes(Var2, Var1,
                 fill = value)) +
  geom_tile(color = "white") +
  scale_fill_gradient2(low = "blue", high = "red", mid = "white",
                       midpoint = 0, limit = c(-1,1), space = "Lab",
                       name="Kendall\nCorrelation") +
  ggtitle("Correlation Matrix for Air Quality Dataset") +
  theme minimal() +
  theme(axis.text.x = element_text(angle = 45, vjust = 1,
                                    size = 7, hjust = 1)) +
  coord fixed() +
  geom_text(aes(Var2,
                label = value),
            color = "black", size = 2.8) +
  theme(
    axis.title.x = element_blank(),
   axis.title.y = element_blank(),
   panel.grid.major = element_blank(),
   panel.border = element_blank(),
   panel.background = element_blank(),
   axis.ticks = element_blank(),
   legend. justification = c(1, 0),
   legend.position = c(0.6, 0.7),
   legend.direction = "horizontal")+
  guides(fill = guide_colorbar(barwidth = 7, barheight = 1,
                               title.position = "top", title.hjust = 0.5))
рЗ
```

Correlation Matrix for Air Quality Dataset





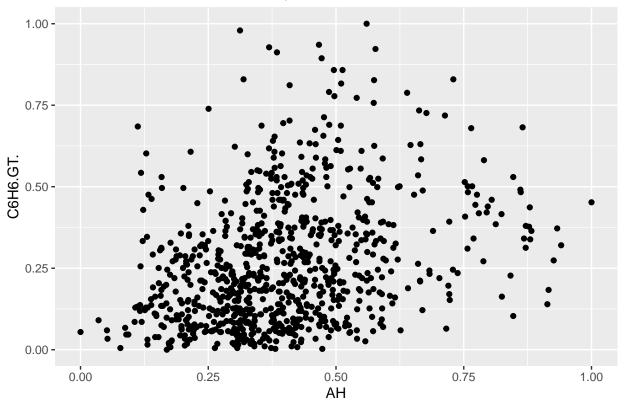
```
Temp S5.03 S1.C0 S4.N02 NMHC
                                                  C6H6 S2.NMHC
                                                                 NO2
                                                                       NOx S3.NOx
##
                                              CO
## Temp
            1.00
                  0.21 0.23
                               0.26
                                     0.33
                                            0.26
                                                  0.32
                                                          0.32
                                                                0.27
                                                                      0.20
                                                                           -0.30
                                                                      0.71 - 0.72
## S5.03
            0.21
                  1.00
                        0.78
                               0.76
                                     0.60
                                            0.71
                                                  0.72
                                                          0.72
                                                                0.64
## S1.CO
            0.23
                  0.78
                        1.00
                               0.80
                                     0.65
                                            0.79
                                                  0.78
                                                          0.78
                                                                0.71
                                                                      0.76
                                                                            -0.72
## S4.NO2
            0.26
                  0.76
                        0.80
                               1.00
                                     0.71
                                            0.79
                                                  0.83
                                                          0.83
                                                                0.65
                                                                      0.75
                                                                            -0.82
## NMHC
                                                          0.80
                                                                0.65
                                                                      0.70
                                                                            -0.80
            0.33
                  0.60
                        0.65
                               0.71
                                     1.00
                                            0.79
                                                  0.80
## CO
                                                                0.76 0.84
                                                                            -0.77
            0.26
                  0.71
                        0.79
                               0.79
                                     0.79
                                            1.00
                                                  0.88
                                                          0.88
## C6H6
            0.32
                  0.72
                        0.78
                               0.83
                                     0.80
                                            0.88
                                                  1.00
                                                          1.00
                                                                0.73 0.80
                                                                            -0.82
## S2.NMHC
           0.32
                  0.72
                        0.78
                               0.83
                                     0.80
                                            0.88
                                                 1.00
                                                          1.00 0.73 0.79
                                                                            -0.82
                                                                1.00 0.75
## NO2
            0.27
                  0.64
                        0.71
                               0.65
                                     0.65
                                            0.76
                                                  0.73
                                                          0.73
                                                                            -0.63
                  0.71
## NOx
            0.20
                        0.76
                               0.75
                                     0.70
                                            0.84
                                                  0.80
                                                          0.79
                                                                0.75
                                                                      1.00
                                                                            -0.72
## S3.NOx
           -0.30 -0.72 -0.72
                              -0.82 -0.80 -0.77 -0.82
                                                         -0.82 -0.63 -0.72
                                                                             1.00
                  0.33
                       0.29
                               0.37 0.21
                                            0.20 0.22
                                                          0.22 0.16
                                                                     0.20
                                                                            -0.34
## Abs H
            0.10
## Rel H
           -0.59 0.00 -0.03 -0.01 -0.16 -0.11 -0.14
                                                         -0.14 -0.15 -0.05
                                                                             0.06
           Abs H Rel H
##
## Temp
            0.10 - 0.59
## S5.03
            0.33 0.00
## S1.CO
            0.29 -0.03
## S4.NO2
            0.37 -0.01
## NMHC
            0.21 -0.16
## CO
            0.20 - 0.11
            0.22 -0.14
## C6H6
## S2.NMHC 0.22 -0.14
## NO2
            0.16 -0.15
## NOx
            0.20 -0.05
```

```
## S3.NOx -0.34 0.06
## Abs H 1.00 0.31
## Rel H 0.31 1.00
```

 $\bullet\,$ Build simple linear models with each predictor, check assumptions, response C6H6

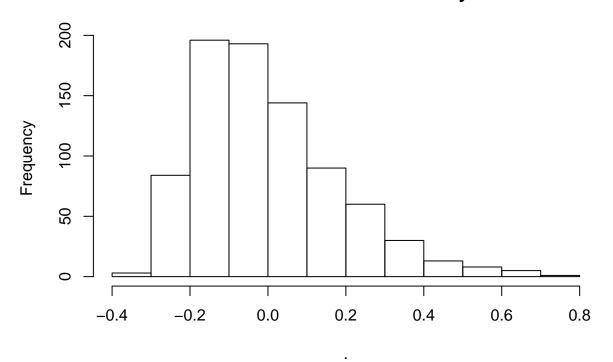
Absolute humidity - data not linear

C6H6.GT. vs absolute humidity



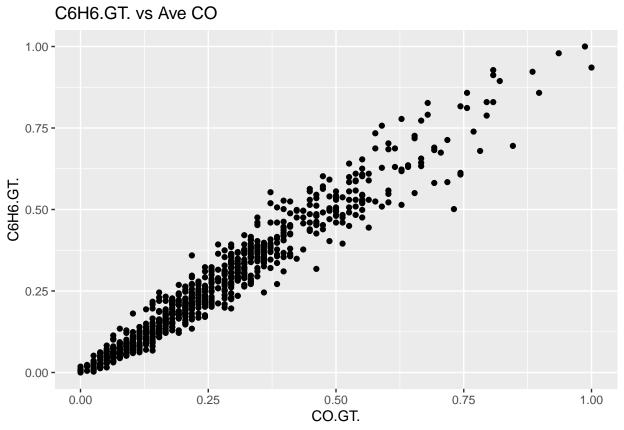
```
AH <- lm(C6H6.GT. ~ AH, airq_norm)
residuals(AH) %>% hist(main = "residuals absolute humidity")
```

residuals absolute humidity



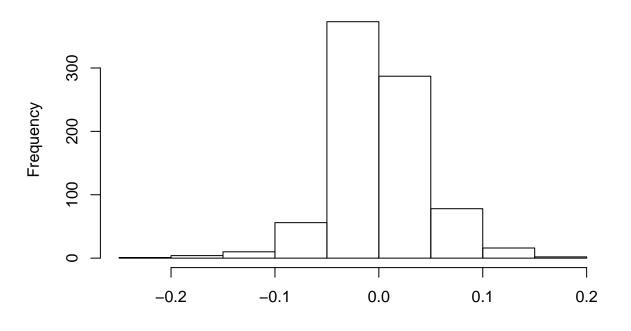
summary(AH)

```
##
## Call:
## lm(formula = C6H6.GT. ~ AH, data = airq_norm)
##
## Residuals:
##
        Min
                  1Q
                      Median
                                    ЗQ
                                            Max
## -0.32613 -0.13882 -0.03953 0.09949 0.74474
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) 0.12084
                           0.01651
                                    7.318 5.99e-13 ***
                0.36445
                           0.03845
                                     9.480 < 2e-16 ***
## AH
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.1821 on 825 degrees of freedom
## Multiple R-squared: 0.09823,
                                   Adjusted R-squared: 0.09714
## F-statistic: 89.87 on 1 and 825 DF, p-value: < 2.2e-16
#Ave CO (CO.GT.)
ggplot(airq_norm, aes(x = CO.GT.,
                   y = C6H6.GT.)) +
  geom_point() +
 ggtitle("C6H6.GT. vs Ave CO")
```



CO <- lm(C6H6.GT. ~ CO.GT., airq_norm)
residuals(CO) %>% hist(main = "residuals ave CO")

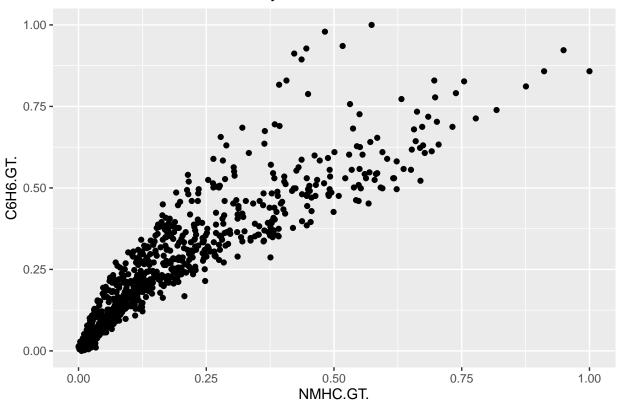
residuals ave CO



summary(CO)

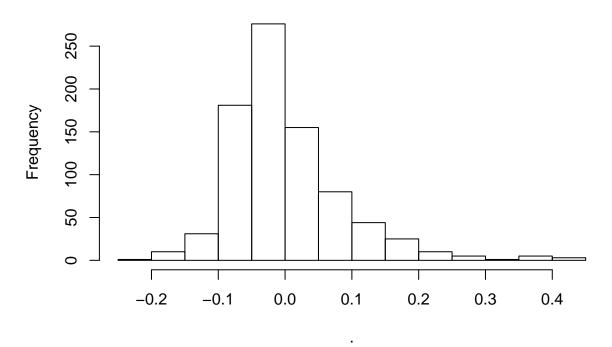
```
##
## Call:
## lm(formula = C6H6.GT. ~ CO.GT., data = airq_norm)
## Residuals:
##
        Min
                   1Q
                         Median
  -0.246446 -0.024653 -0.002748 0.021429 0.175606
##
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) -0.006234
                          0.002738 -2.277
                                             0.0231 *
                         0.008577 120.298
## CO.GT.
               1.031752
                                             <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.04454 on 825 degrees of freedom
## Multiple R-squared: 0.9461, Adjusted R-squared: 0.946
## F-statistic: 1.447e+04 on 1 and 825 DF, p-value: < 2.2e-16
#Non Metanic HydroCarbons (NMHC.GT.)
ggplot(airq_norm, aes(x = NMHC.GT.,
                  y = C6H6.GT.) +
 geom_point() +
 ggtitle("C6H6.GT. vs Non Metanic HydroCarbons")
```

C6H6.GT. vs Non Metanic HydroCarbons



```
NMHC <- lm(C6H6.GT. ~ NMHC.GT., airq_norm)
residuals(NMHC) %>% hist(main = "residuals Non Metanic HydroCarbons")
```

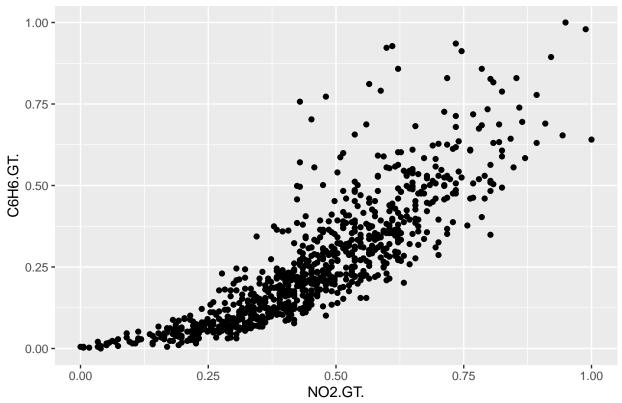
residuals Non Metanic HydroCarbons



summary(NMHC)

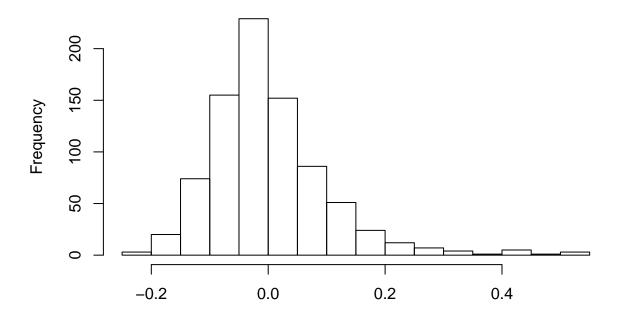
```
##
## Call:
## lm(formula = C6H6.GT. ~ NMHC.GT., data = airq_norm)
##
## Residuals:
       Min
                  1Q
                      Median
                                            Max
## -0.21156 -0.05312 -0.01712 0.03570 0.42827
##
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 0.080435
                          0.004311
                                     18.66
                                             <2e-16 ***
## NMHC.GT.
              0.975924
                         0.016655
                                     58.60
                                             <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.08442 on 825 degrees of freedom
## Multiple R-squared: 0.8063, Adjusted R-squared: 0.806
## F-statistic: 3434 on 1 and 825 DF, p-value: < 2.2e-16
#ave NO2 (NO2.GT.)
ggplot(airq_norm, aes(x = NO2.GT.,
                  y = C6H6.GT.) +
  geom_point() +
 ggtitle("C6H6.GT. vs averaged NO2")
```

C6H6.GT. vs averaged NO2



NO2 <- lm(C6H6.GT. ~ NO2.GT., airq_norm)
residuals(NO2) %>% hist(main = "residuals ave NO2")

residuals ave NO2

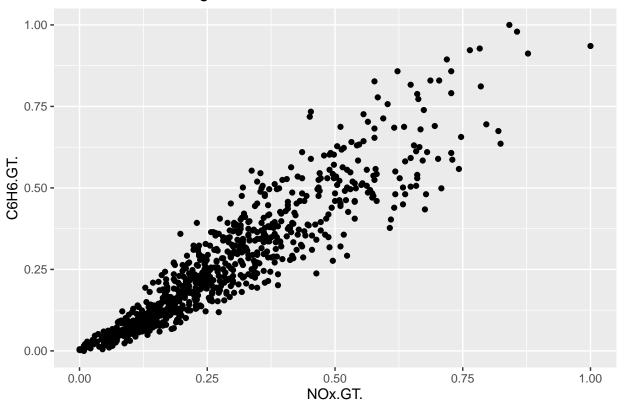


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summary(NO2)

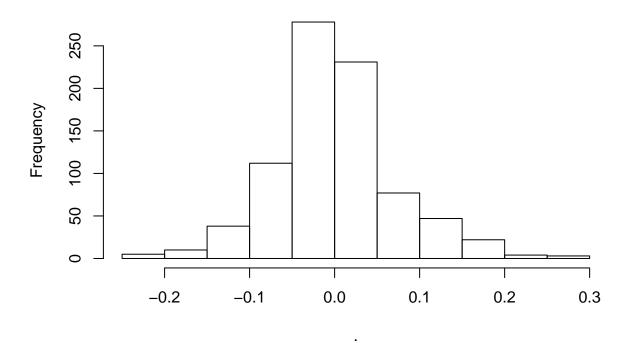
```
##
## Call:
## lm(formula = C6H6.GT. ~ NO2.GT., data = airq_norm)
## Residuals:
       Min
##
                 1Q
                     Median
## -0.22960 -0.06523 -0.01512 0.04535 0.52958
##
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) -0.153377
                          0.009824 -15.61
                                             <2e-16 ***
                                     45.72
                                             <2e-16 ***
## NO2.GT.
               0.912185
                          0.019953
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
\#\# Residual standard error: 0.102 on 825 degrees of freedom
## Multiple R-squared: 0.717, Adjusted R-squared: 0.7166
## F-statistic: 2090 on 1 and 825 DF, p-value: < 2.2e-16
#ave NOx (NO2.GT.)
ggplot(airq_norm, aes(x = NOx.GT.,
                  y = C6H6.GT.) +
 geom_point() +
 ggtitle("C6H6.GT. vs averaged NOx")
```

C6H6.GT. vs averaged NOx



```
NOx <- lm(C6H6.GT. ~ NOx.GT., airq_norm)
residuals(NOx) %>% hist(main = "residuals ave NOx")
```

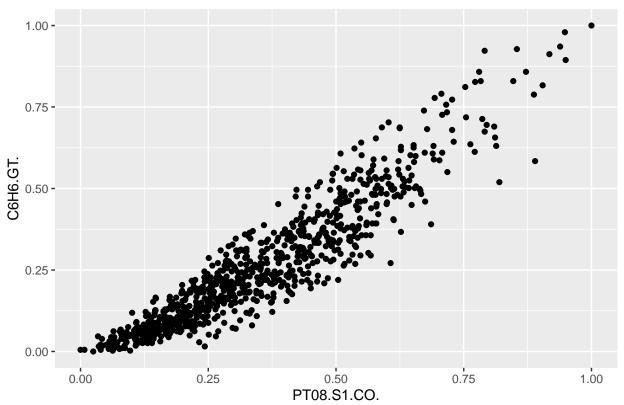
residuals ave NOx



summary(NOx)

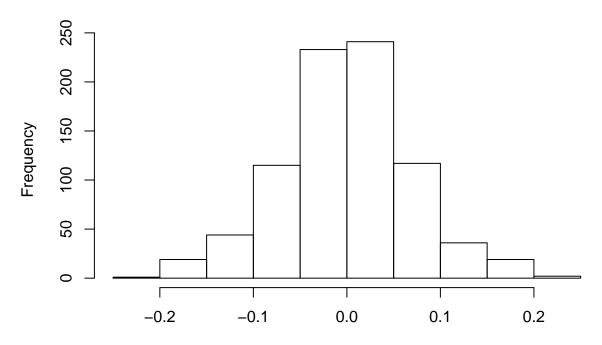
```
##
## Call:
## lm(formula = C6H6.GT. ~ NOx.GT., data = airq_norm)
## Residuals:
        Min
                   1Q
                         Median
                                       3Q
                                                Max
## -0.229885 -0.039333 -0.004928 0.032293 0.295763
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) -0.020242
                          0.004727 -4.282 2.07e-05 ***
## NOx.GT.
               1.012233
                          0.014225 71.157 < 2e-16 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.07179 on 825 degrees of freedom
## Multiple R-squared: 0.8599, Adjusted R-squared: 0.8597
## F-statistic: 5063 on 1 and 825 DF, p-value: < 2.2e-16
#ave tin oxide (PT08.S1.CO.)
ggplot(airq_norm, aes(x = PT08.S1.C0.,
                  y = C6H6.GT.) +
  geom_point() +
 ggtitle("C6H6.GT. vs tin oxide / PT08.S1.CO.")
```

C6H6.GT. vs tin oxide / PT08.S1.CO.



PT08.S1 <- lm(C6H6.GT. ~ PT08.S1.CO., airq_norm)
residuals(PT08.S1) %>% hist(main = "residuals tin oxide")

residuals tin oxide

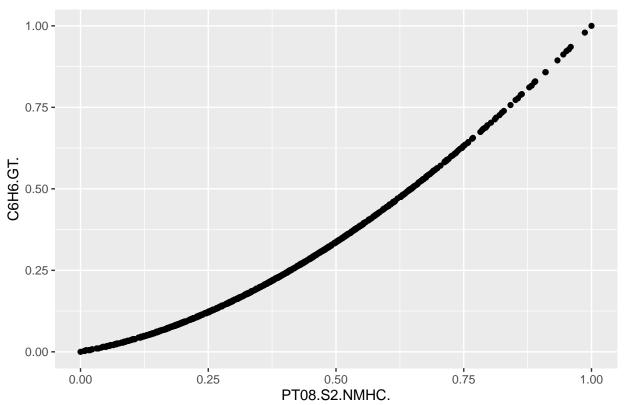


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```
summary(PT08.S1)
```

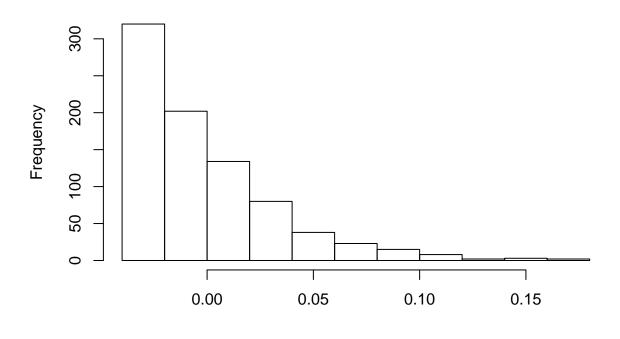
```
##
## Call:
## lm(formula = C6H6.GT. ~ PT08.S1.CO., data = airq_norm)
## Residuals:
##
        Min
                   1Q
                         Median
## -0.234852 -0.041978  0.000656  0.042554  0.241339
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) -0.070423
                          0.005175 -13.61
                                             <2e-16 ***
## PT08.S1.CO. 0.950160
                         0.012931
                                     73.48
                                             <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.06983 on 825 degrees of freedom
## Multiple R-squared: 0.8674, Adjusted R-squared: 0.8673
## F-statistic: 5399 on 1 and 825 DF, p-value: < 2.2e-16
#ave titania (PT08.S2.NMHC)
ggplot(airq_norm, aes(x = PT08.S2.NMHC.,
                  y = C6H6.GT.) +
 geom_point() +
 ggtitle("C6H6.GT. vs titania / PT08.S2.NMHC")
```

C6H6.GT. vs titania / PT08.S2.NMHC



```
PT08.S2 <- lm(C6H6.GT. ~ PT08.S2.NMHC., airq_norm)
residuals(PT08.S2) %>% hist(main = "residuals ave titania")
```

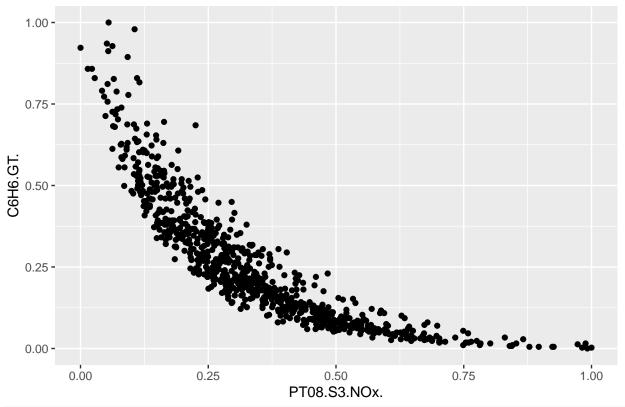
residuals ave titania



```
summary(PT08.S2)
```

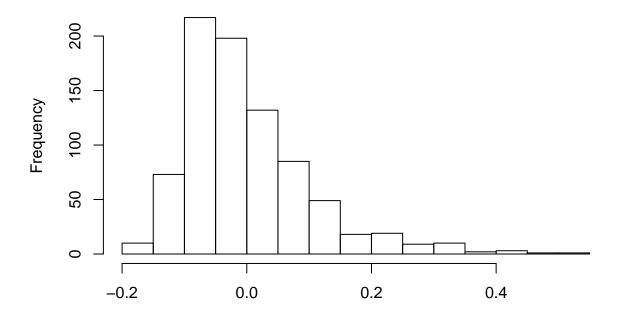
```
##
## Call:
## lm(formula = C6H6.GT. ~ PT08.S2.NMHC., data = airq_norm)
## Residuals:
       Min
                 1Q
                      Median
                                   3Q
                                            Max
## -0.02964 -0.02476 -0.01192 0.01419 0.17634
##
## Coefficients:
##
                 Estimate Std. Error t value Pr(>|t|)
                            0.002532 -40.18
## (Intercept)
                -0.101710
                                                <2e-16 ***
## PT08.S2.NMHC. 0.925371
                            0.005676 163.04
                                                <2e-16 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.03328 on 825 degrees of freedom
## Multiple R-squared: 0.9699, Adjusted R-squared: 0.9699
## F-statistic: 2.658e+04 on 1 and 825 DF, p-value: < 2.2e-16
#ave tungsten oxide NOx targeted (PT08.S3.NOx.) - data not linear
ggplot(airq_norm, aes(x = PT08.S3.N0x.,
                  y = C6H6.GT.) +
  geom_point() +
  ggtitle("C6H6.GT. vs tungsten oxide NOx / PT08.S3.NOx.")
```

C6H6.GT. vs tungsten oxide NOx / PT08.S3.NOx.



PT08.S3 <- lm(C6H6.GT. ~ PT08.S3.NOx., airq_norm)
residuals(PT08.S3) %>% hist(main = " residuals tungsten oxide NOx")

residuals tungsten oxide NOx



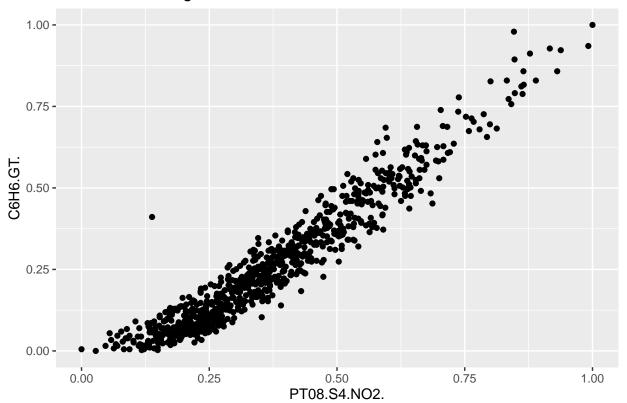
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summary(PT08.S3) ## ## Call: ## lm(formula = C6H6.GT. ~ PT08.S3.N0x., data = airq_norm) ## Residuals: ## Min 1Q Median ## -0.16861 -0.06947 -0.02396 0.04462 0.50203 ## ## Coefficients: ## Estimate Std. Error t value Pr(>|t|) ## (Intercept) 0.572754 0.007539 75.97 <2e-16 *** ## PT08.S3.NOx. -0.901926 0.019555 -46.12 <2e-16 *** ## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1 ## Residual standard error: 0.1014 on 825 degrees of freedom

#ave tungsten oxide NO2 targeted (PT08.S4.NO2.)

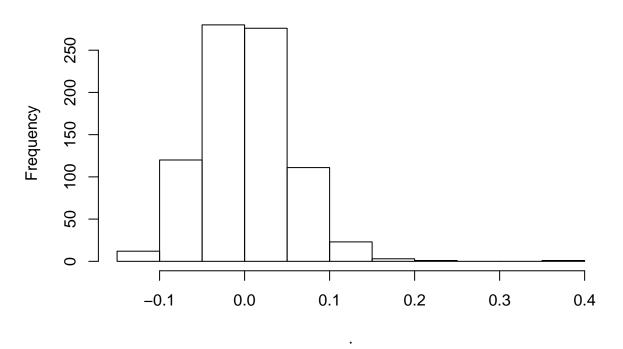
C6H6.GT. vs tungsten oxide NO2 / PT08.S4.NO2

Multiple R-squared: 0.7205, Adjusted R-squared: 0.7202 ## F-statistic: 2127 on 1 and 825 DF, p-value: < 2.2e-16



```
PT08.S4 <- lm(C6H6.GT. ~ PT08.S4.N02., airq_norm)
residuals(PT08.S4) %>% hist(main = " residuals tungsten oxide N02")
```

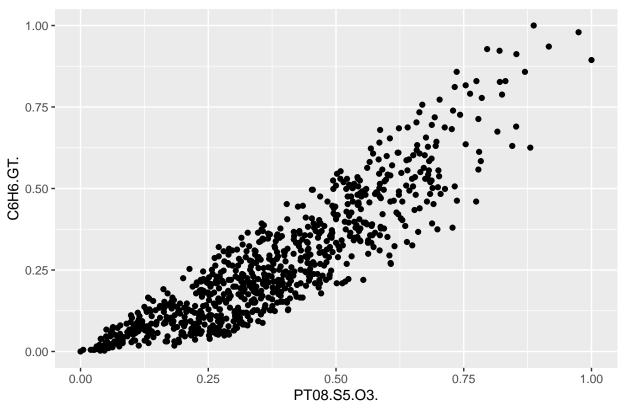
residuals tungsten oxide NO2



summary(PT08.S4)

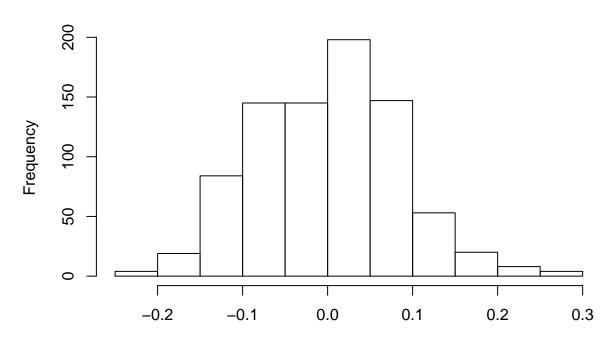
```
##
## Call:
## lm(formula = C6H6.GT. ~ PT08.S4.N02., data = airq_norm)
##
## Residuals:
       Min
                  1Q
                      Median
                                           Max
## -0.14255 -0.03663 0.00027 0.03079 0.39379
##
## Coefficients:
##
                Estimate Std. Error t value Pr(>|t|)
## (Intercept) -0.127941
                           0.004362
                                     -29.33
                                               <2e-16 ***
## PT08.S4.NO2. 1.050347
                           0.010550
                                      99.56
                                               <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.05317 on 825 degrees of freedom
## Multiple R-squared: 0.9232, Adjusted R-squared: 0.9231
## F-statistic: 9911 on 1 and 825 DF, p-value: < 2.2e-16
#ave indium oxide (PT08.S5.O3.)
ggplot(airq_norm, aes(x = PT08.S5.03.,
                  y = C6H6.GT.) +
  geom_point() +
 ggtitle("C6H6.GT. vs indium oxide / PT08.S5.03")
```

C6H6.GT. vs indium oxide / PT08.S5.O3



PT08.S5 <- lm(C6H6.GT. ~ PT08.S5.O3., airq_norm)
residuals(PT08.S5) %>% hist(main = "residuals ave indium oxide")

residuals ave indium oxide

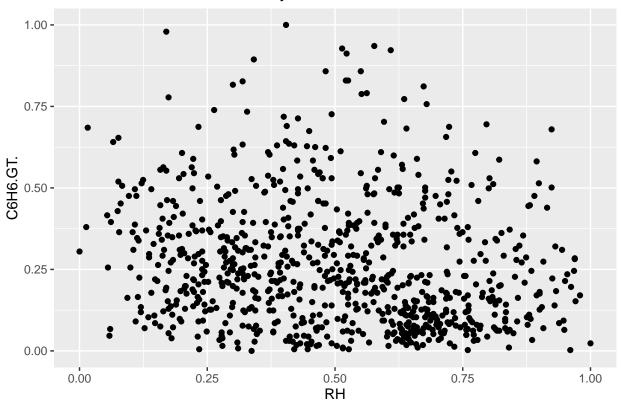


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summary(PT08.S5)

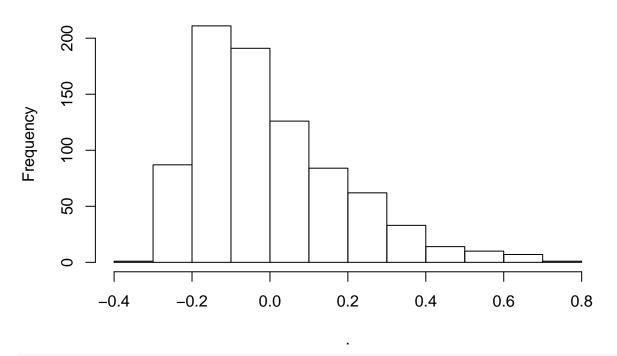
```
##
## Call:
## lm(formula = C6H6.GT. ~ PT08.S5.03., data = airq_norm)
## Residuals:
##
         Min
                    1Q
                          Median
                                                 Max
## -0.207840 -0.065510 0.006316 0.056262 0.281886
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) -0.070967
                          0.006481
                                    -10.95
                                              <2e-16 ***
## PT08.S5.03. 0.900639
                         0.015454
                                      58.28
                                              <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.08479 on 825 degrees of freedom
## Multiple R-squared: 0.8046, Adjusted R-squared: 0.8043
## F-statistic: 3396 on 1 and 825 DF, p-value: < 2.2e-16
#Relative humidity (RH) - data not linear
ggplot(airq_norm, aes(x = RH,
                  y = C6H6.GT.)) +
  geom_point() +
  ggtitle("C6H6.GT. vs Relative humidity")
```

C6H6.GT. vs Relative humidity



```
RH <- lm(C6H6.GT. ~ RH, airq_norm)
residuals(RH) %>% hist(main = "residuals relative humidity")
```

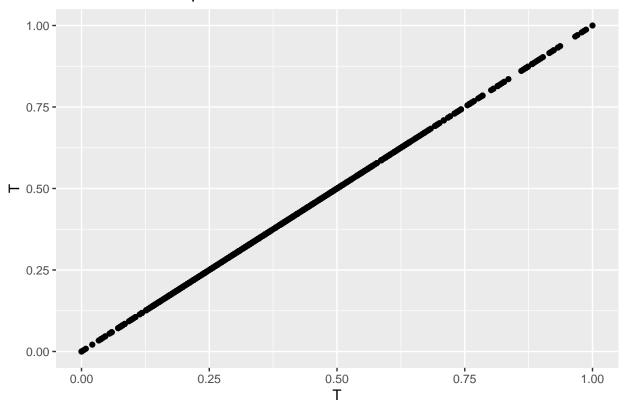
residuals relative humidity



summary(RH)

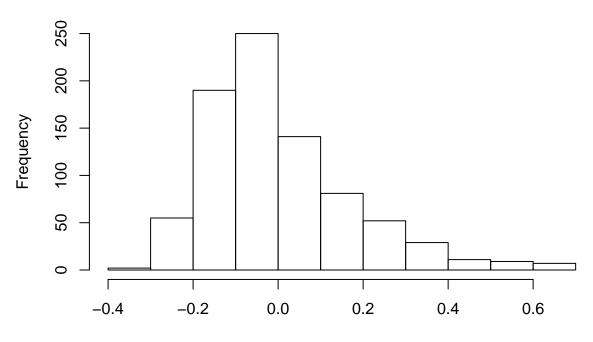
```
##
## Call:
## lm(formula = C6H6.GT. ~ RH, data = airq_norm)
##
## Residuals:
       Min
                  1Q
                      Median
                                           Max
## -0.30089 -0.14383 -0.04093 0.10237 0.71992
##
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 0.34190
                          0.01609 21.252 < 2e-16 ***
              -0.15300
                          0.02938 -5.208 2.41e-07 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.1887 on 825 degrees of freedom
                                   Adjusted R-squared: 0.03066
## Multiple R-squared: 0.03183,
## F-statistic: 27.12 on 1 and 825 DF, p-value: 2.412e-07
\#Temperature
ggplot(airq_norm, aes(x = T,
                  y = T)) +
  geom_point() +
 ggtitle("C6H6.GT. vs Temperature")
```

C6H6.GT. vs Temperature



TP <- lm(C6H6.GT. ~ T, airq_norm)
residuals(TP) %>% hist(main = "residuals temperature")

residuals temperature



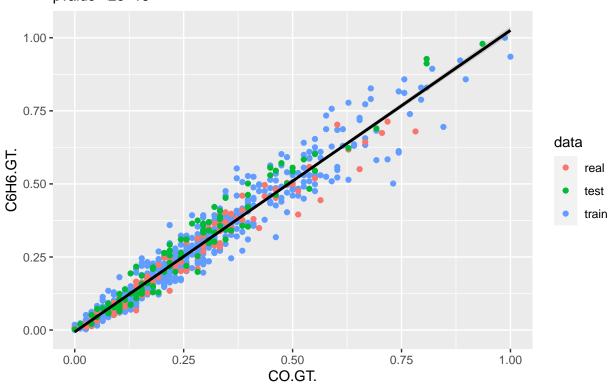
.

```
summary(TP)
##
## Call:
## lm(formula = C6H6.GT. ~ T, data = airq_norm)
## Residuals:
##
        Min
                  1Q
                       Median
                                     3Q
                                              Max
## -0.32857 -0.12436 -0.03943 0.07945 0.68720
##
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
                                     8.419
## (Intercept) 0.11080
                            0.01316
                                               <2e-16 ***
## T
                0.39392
                            0.02977 13.232
                                               <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.1742 on 825 degrees of freedom
## Multiple R-squared: 0.1751, Adjusted R-squared: 0.1741
## F-statistic: 175.1 on 1 and 825 DF, p-value: < 2.2e-16
  • For 2-3 of the models create train-test sets, plot the model, for the test set color real and predicted
    points differently; R<sup>2</sup> and p-value to title
#ave CO and NO2
set.seed(88)
data <- airq_norm
sample <- sample.int(n = nrow(data), size = floor(.75*nrow(data)))</pre>
train <- data[sample, ]</pre>
test <- data[-sample, ]</pre>
train_CO <- train[,c("C6H6.GT.", "CO.GT.")]</pre>
test_CO <- test[,c("C6H6.GT.", "CO.GT.")]
new_mod_CO <- lm(data = train_CO,</pre>
              C6H6.GT. ~ CO.GT.)
#summary
sum_CO <- summary(new_mod_CO)</pre>
print(sum_CO)
##
## Call:
## lm(formula = C6H6.GT. ~ CO.GT., data = train_CO)
##
## Residuals:
##
         Min
                     1Q
                           Median
                                          3Q
                                                   Max
## -0.244458 -0.024115 -0.002475 0.020795 0.176836
##
## Coefficients:
##
                Estimate Std. Error t value Pr(>|t|)
## (Intercept) -0.006680
                            0.003172 -2.106
                                                0.0356 *
## CO.GT.
                1.029640
                            0.010009 102.875
                                                <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

```
##
## Residual standard error: 0.04516 on 618 degrees of freedom
## Multiple R-squared: 0.9448, Adjusted R-squared: 0.9447
## F-statistic: 1.058e+04 on 1 and 618 DF, p-value: < 2.2e-16
#use model, predicts new model from newdata (test)
*predictions for new test data set, add new column
pred_CO <- predict(new_mod_CO, newdata = test_CO)</pre>
test$CO.GT._pred <- pred_CO</pre>
#make combined dataset
train_CO$data <- "train"</pre>
test_CO$data <- "test"</pre>
test_CO[1:(nrow(test_CO)/2),3] <- "real"
comb_CO <- rbind(train_CO, test_CO)</pre>
#trained and test should be similar shape
ggplot(data = comb_CO,
       aes(x = CO.GT.,
           y = C6H6.GT.
           color = data)) +
  geom_point() +
  geom_smooth(method = "lm",
              color = "black") +
  ggtitle(paste("R2", round(sum_CO$r.squared, 3),
                sep = ": "),
          paste("pvalue <2e-16" ))</pre>
```

`geom_smooth()` using formula 'y ~ x'

R2: 0.945 pvalue <2e-16



```
##
## Call:
## lm(formula = C6H6.GT. ~ NO2.GT., data = train_NO2)
## Residuals:
                 1Q Median
## -0.19968 -0.06541 -0.01496  0.04565  0.53161
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -0.15667
                          0.01117 -14.03 <2e-16 ***
## NO2.GT.
               0.91429
                          0.02277
                                    40.15
                                            <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.1012 on 618 degrees of freedom
## Multiple R-squared: 0.7229, Adjusted R-squared: 0.7225
## F-statistic: 1612 on 1 and 618 DF, p-value: < 2.2e-16
```

```
pred_NO2 <- predict(mod_NO2, newdata = test_NO2)</pre>
test$NO2.GT._pred <- pred_NO2</pre>
train_NO2$data <- "train"</pre>
test_NO2$data <- "test"</pre>
test_NO2[1:(nrow(test_NO2)/2),3] <- "real"
comb_NO2 <- rbind(train_NO2, test_NO2)</pre>
ggplot(data = comb_NO2,
       aes(x = NO2.GT.,
            y = C6H6.GT.,
            color = data)) +
  geom_point() +
  geom_smooth(method = "lm",
               color = "black") +
  ggtitle(paste("R2", round(sum_CO$r.squared, 3),
                 sep = ": "),
           paste("pvalue <2e-16" ))</pre>
```

`geom_smooth()` using formula 'y ~ x'

R2: 0.945 pvalue <2e-16

