

# Multivariate statistics

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## Today

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- Learn the basics of multivariate analysis to reveal patterns
- Use **R** to perform Unconstrained ordinations
- Learn the following methods:
  - Clustering analysis
  - Detrended correspondence analysis (DCA)
  - Principal Component Analysis (PCA)
  - Non-metric Multidimensional Scaling (NMDS)
- Break ☺
- Practice



## Required Material

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<https://github.com/lacapary/BIO503/>

## Required Material

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You are required to have downloaded and installed

```
install.packages(c("vegan",  
                  "ape",  
                  "factoextra",  
                  "dendextend"))
```

## Required Material

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Do not hesitate to ask questions!

## Recap: Linear models

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- We learned some models to study at ecological data.
- These models allowed us to ask questions such as:
  - What are the effects of precipitation and temperature on species richness? or

- How does the abundance of species change between habitats?

## Multivariate statistics

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Sometimes, we want to figure out things from ecological data that has more than one main outcome or dependent variable.

our research question might be:

- How does the plants composition change along an elevation gradient?
- What is the composition dissimilarity of plants communities?
- How closely-related are local vegetation communities in terms of their composition ?

In all these questions, the outcome is composed of several variables, e.g. usually a list of samples and the types of species in them, or a list of samples and the environment they're in.

## Multivariate statistics

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Matrix Species

Site	Species 1	Species 2	...	Species n
1	abundance 1	abundance 2	...	abundance n
2	abundance 1	abundance 2	...	abundance n
m	...	...	...	...

Matrix locations

Site	Temperature	Precipitation	...	Driver n
1	Temperature 1	Precipitation 2	...	Driver n
2	Temperature 1	Precipitation 2	...	Driver n
m	...	...	...	...

## Multivariate statistics

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Matrix algebra



## Multivariate statistics

Matrix algebra

$$\begin{matrix}
 & \begin{matrix} 1 & 2 & \dots & n \end{matrix} \\
 \begin{matrix} 1 \\ 2 \\ 3 \\ \vdots \\ m \end{matrix} & \left[ \begin{array}{cccc}
 a_{11} & a_{12} & \dots & a_{1n} \\
 a_{21} & a_{22} & \dots & a_{2n} \\
 a_{31} & a_{32} & \dots & a_{3n} \\
 \vdots & \vdots & \vdots & \vdots \\
 a_{m1} & a_{m2} & \dots & a_{mn}
 \end{array} \right]
 \end{matrix}$$

### Multivariate statistics

#### Association matrices

- Q-mode : analysis for objects or sites
- R-mode : analysis for descriptors or species

### What is ordination?

Ordination is a collective term for multivariate techniques which summarize a multidimensional dataset in such a way that when it is projected onto a low dimensional space, any intrinsic pattern the data may possess becomes apparent upon visual inspection (Pielou, 1984).

- In ecological terms, ordination helps us understand community data.
- Like how many species are in different locations. It does this by creating a simple space where similar species and samples are near each other, and different ones are far apart.
- Ideally, this space shows important environmental differences clearly.

### The data for this session?

The data originates from the research of Batterink & Wijffels (1983), published as a report in Dutch.

Table 0.1. Dune Meadow Data. Unordered table that contains 20 relevées (columns) and 30 species (rows). The right-hand column gives the abbreviation of the species names listed in the left-hand column; these abbreviations will be used throughout the book in other tables and figures. The species scores are according to the scale of van der Maarel (1979b).

	00000000011111111112	
	12345678901234567890	
1 <i>Achillea millefolium</i>	13..222..4.....2...	Ach mil
2 <i>Agrostis stolonifera</i>	..48...43..45447...5	Agr sto
3 <i>Aira praecox</i>	.....2.3.	Air pra
4 <i>Alopecurus geniculatus</i>	.272...53..85..4...	Alo gen
5 <i>Anthoxanthum odoratum</i>	....432..4.....4.4.	Ant odo
6 <i>Bellis perennis</i>	.3222...2.....2..	Bel per
7 <i>Bromus hordeaceus</i>	.4.32.2..4.....	Bro hor
8 <i>Chenopodium album</i>	.....1.....	Che alb
9 <i>Cirsium arvense</i>	...2.....	Cir arv
10 <i>Eleocharis palustris</i>	.....4.....458...4	Ele pal
11 <i>Elymus repens</i>	44444...6.....	Ely rep
12 <i>Empetrum nigrum</i>	.....2.	Emp nig
13 <i>Hypochaeris radicata</i>	.....2.....2.5.	Hyp rad
14 <i>Juncus articulatus</i>	.....44.....33...4	Jun art
15 <i>Juncus bufonius</i>	.....2.4..43.....	Jun buf
16 <i>Leontodon autumnalis</i>	.52233332352222.2562	Leo aut
17 <i>Lolium perenne</i>	75652664267.....2..	Lol per
18 <i>Plantago lanceolata</i>	....555..33.....23..	Pla lan
19 <i>Poa pratensis</i>	44542344444.2...13..	Poa pra
20 <i>Poa trivialis</i>	2765645454.49..2....	Poa tri
21 <i>Potentilla palustris</i>	.....22.....	Pot pal
22 <i>Ranunculus flammula</i>	.....2....2222...4	Ran fla
23 <i>Rumex acetosa</i>	....563.2..2.....	Rum ace
24 <i>Sagina procumbens</i>	...5...22.242.....3.	Sag pro
25 <i>Salix repens</i>	.....335	Sal rep
26 <i>Trifolium pratense</i>	....252.....	Tri pra
27 <i>Trifolium repens</i>	.52125223633261..22.	Tri rep
28 <i>Vicia lathyroides</i>	.....12.....1..	Vic lat
29 <i>Brachythecium rutabulum</i>	..2226222244..44.634	Bra rut
30 <i>Calliergonella cuspidata</i>	.....4.3...3	Cal cus

## The data for this session?

```
library(tidyverse)
```

— Attaching core tidyverse packages — tidyverse 2.0.0 —

```
✓ dplyr    1.1.4    ✓ readr    2.1.5
✓ forcats  1.0.0    ✓ stringr  1.5.1
✓ ggplot2  3.5.0    ✓ tibble   3.2.1
✓ lubridate 1.9.3    ✓ tidyr    1.3.1
✓ purrr     1.0.2
```

— Conflicts — tidyverse\_conflicts() —

```
X dplyr::filter() masks stats::filter()
X dplyr::lag()    masks stats::lag()
```

i Use the conflicted package (<<http://conflicted.r-lib.org/>>) to force all conflicts to become errors

```
library(vegan)
```



Loading required package: permute  
Loading required package: lattice  
This is vegan 2.6-4

```
# Load the community dataset which we'll use in the examples today

dune2_spe <- read_csv("Data/dune2_spe.csv")
```

```
Rows: 20 Columns: 28
— Column specification —————
Delimiter: ","
dbl (28): Achimill, Agrostol, Airaprae, Alop geni, Anthodor, Bellpere, Bromho...
```

i Use `spec()` to retrieve the full column specification for this data.  
i Specify the column types or set `show\_col\_types = FALSE` to quiet this message.

```
dune2_env <- read_csv("Data/dune2_env.csv")
```

```
Rows: 20 Columns: 5
— Column specification —————
Delimiter: ","
chr (2): Management, Use
dbl (3): A1, Moisture, Manure
```

i Use `spec()` to retrieve the full column specification for this data.  
i Specify the column types or set `show\_col\_types = FALSE` to quiet this message.

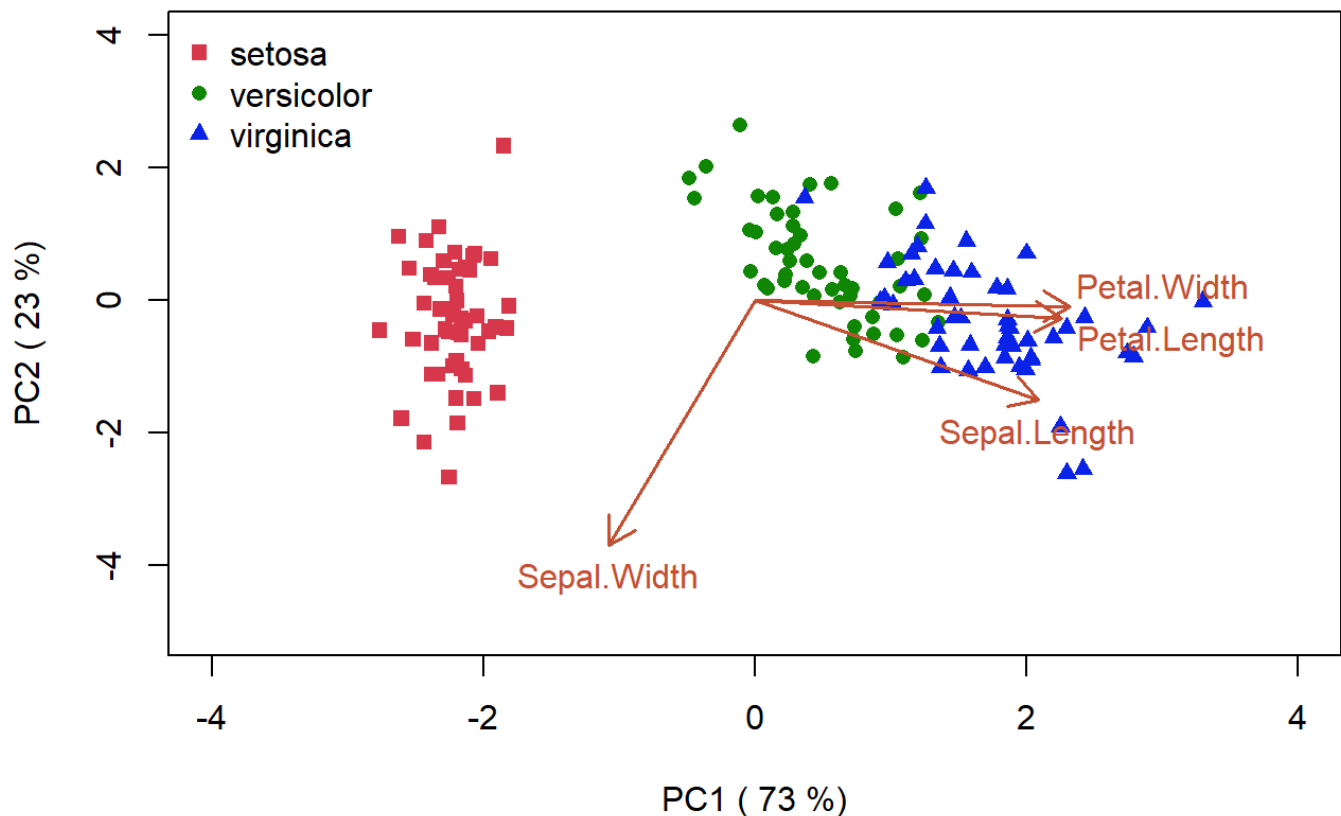
```
# Open the dataset and look if you can find any patterns
head(dune2_spe)
```

```
# A tibble: 6 × 28
  Achimill Agrostol Airaprae Alop geni Anthodor Bellpere Bromhord Chenalbu
    <dbl>    <dbl>    <dbl>    <dbl>    <dbl>    <dbl>    <dbl>    <dbl>
1         1         0         0         0         0         0         0         0
2         3         0         0         2         0         3         4         0
3         0         4         0         7         0         2         0         0
4         0         8         0         2         0         2         3         0
5         2         0         0         0         4         2         2         0
6         2         0         0         0         3         0         0         0
# i 20 more variables: Cirsarve <dbl>, Comapalu <dbl>, Eleopalv <dbl>,
#   Elymrepe <dbl>, Empenigr <dbl>, Hyporadi <dbl>, Juncarti <dbl>,
#   Juncbufo <dbl>, Lolipere <dbl>, Planlanc <dbl>, Poaprat <dbl>,
#   Poatriv <dbl>, Ranuflam <dbl>, Rumeacet <dbl>, Sagiproc <dbl>,
#   Salirepe <dbl>, Scorautu <dbl>, Trifprat <dbl>, Trifrepe <dbl>,
#   Vicilath <dbl>
```

```
head(dune2_env)
```

```
# A tibble: 6 × 5
  A1 Moisture Management Use      Manure
  <dbl>    <dbl>    <chr>    <chr>    <dbl>
1  2.8      1 SF      Haypastu    4
2  3.5      1 BF      Haypastu    2
3  4.3      2 SF      Haypastu    4
4  4.2      2 SF      Haypastu    4
5  6.3      1 HF      Hayfield    2
6  4.3      1 HF      Haypastu    2
```

## What is ordination?



## Type of ordinations?

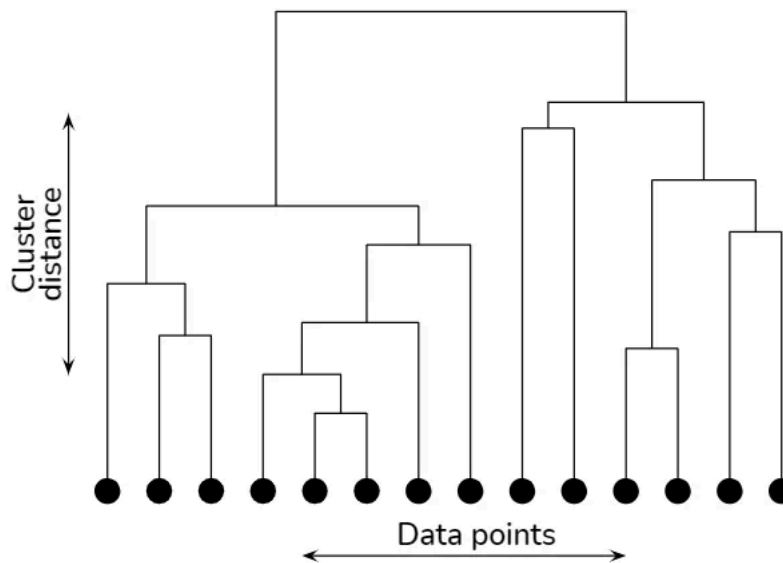
- Unconstrained Ordination: we're basically letting the data *speak for itself*. We don't impose any specific relationships or constraints between the variables.
- Constrained Ordination: we impose some restrictions or *constraints* on the analysis based on what we already know or suspect about the data.
- In simple terms, unconstrained ordination lets the data tell its story without interference, while constrained ordination guides the analysis based on what we already know or suspect.
- We are going to focus in Unconstrained Ordinations

## Ordination vs. Clustering

- Ordination and clustering are the two main classes of multivariate methods that community ecologists employ.
- To some degree, these two approaches are complementary.
- Hierarchical data clustering allows you to explore your data and look for discontinuities (e.g. gaps in your data), gradients and meaningful ecological units (e.g. groups or subgroups of species).
- Given the continuous nature of communities, ordination can be considered a more natural approach. Ordination aims at arranging samples or species continuously along gradients.

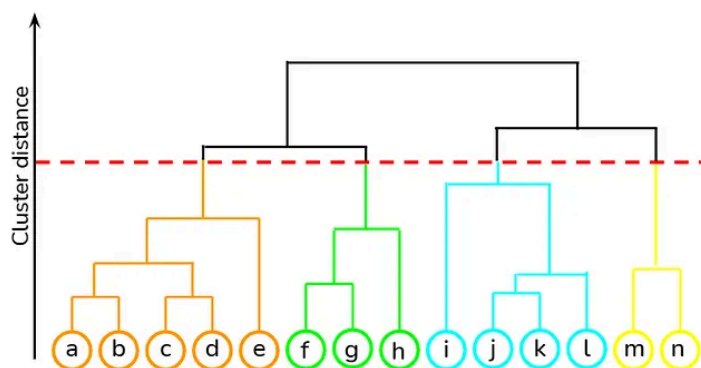
## Clustering

- Hierarchical clustering offers insight into how your biodiversity data are organized and can help you to disentangle different patterns and the scales at which they can be observed.
- Its results can be represented as dendrograms (tree-like diagrams), which describe how closely observations are.

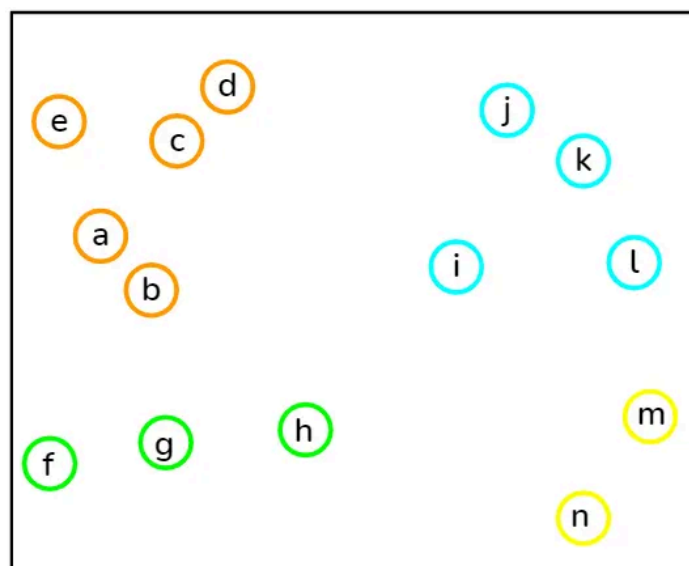


source: Prasad Pai

## Clustering



source: Prasad Pai



source: Prasad Pai

## Clustering

```
library(dendextend)
```

Registered S3 method overwritten by 'dendextend':

```
method      from
rev.hclust  vegan
```

-----  
Welcome to dendextend version 1.17.1

Type citation('dendextend') for how to cite the package.

Type browseVignettes(package = 'dendextend') for the package vignette.

The github page is: <https://github.com/talgalili/dendextend/>

Suggestions and bug-reports can be submitted at: <https://github.com/talgalili/dendextend/issues>

You may ask questions at stackoverflow, use the r and dendextend tags:

<https://stackoverflow.com/questions/tagged/dendextend>



To suppress this message use: `suppressPackageStartupMessages(library(dendextend))`

Attaching package: 'dendextend'

The following object is masked from 'package:permute':

`shuffle`

The following object is masked from 'package:stats':

`cutree`

```
dis_data<-dune2_spe %>%
  vegdist(method = "bray",upper=FALSE)

dend <- dis_data %>%
  hclust(method="ward.D2") %>%
  as.dendrogram()

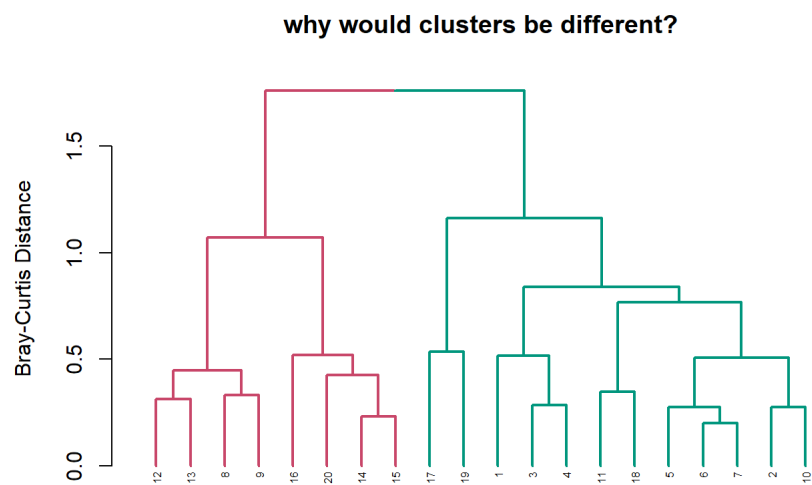
dend
```

'dendrogram' with 2 branches and 20 members total, at height 1.757535

## Clustering

```
dend.plot <- dend %>%
  set("branches_lwd", 2) %>% # Branches line width
  set("branches_k_color", k = 2) %>% # Color branches by groups
  set("labels_cex", 0.5) # Change label size

plot(dend.plot, ylab = "Bray-Curtis Distance", main = "why would clusters be different?")
```



## Clustering

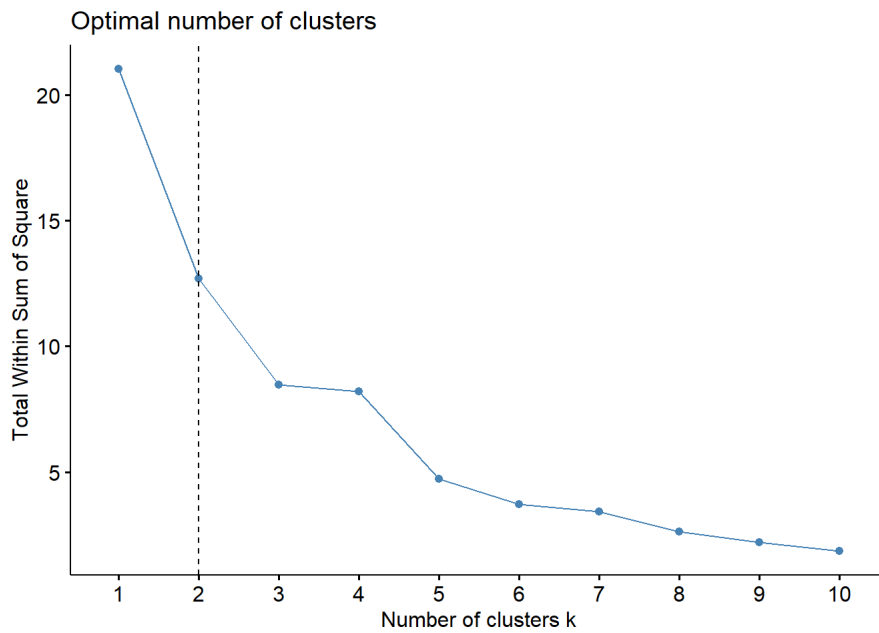
What is the ideal number of clusters?

```
library(factoextra)
```

Welcome! Want to learn more? See two factoextra-related books at <https://goo.gl/ve3wBa>

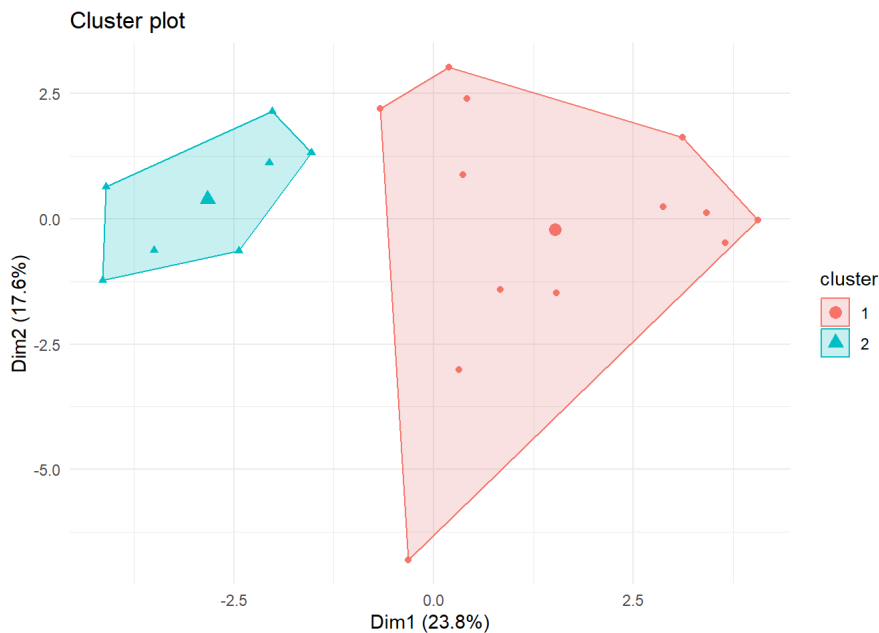
```
varespec_m<-dis_data |> as.matrix()
```

```
fviz_nbclust(varespec_m, kmeans, method = "wss") +
  geom_vline(xintercept = 2, linetype = 2)
```



## Clustering

```
fviz_cluster(kmeans(varespec_m, centers = 2), geom = "point", data = dune2_spe)+ theme_minimal()
```



## Ordinations

- Assess relationships within a set of variables (species or environmental variables)
- Find key components of variation among samples, sites, species
- Reduce the number of dimensions in multivariate data while limiting substantial loss of information
- Create new variables for use in subsequent analyses

## Doing an ordination

This ordination goes in two steps:

- First, we will perform an ordination on a species abundance matrix.
- Then we will use environmental data (samples by environmental variables) to interpret the gradients that were uncovered by the ordination.

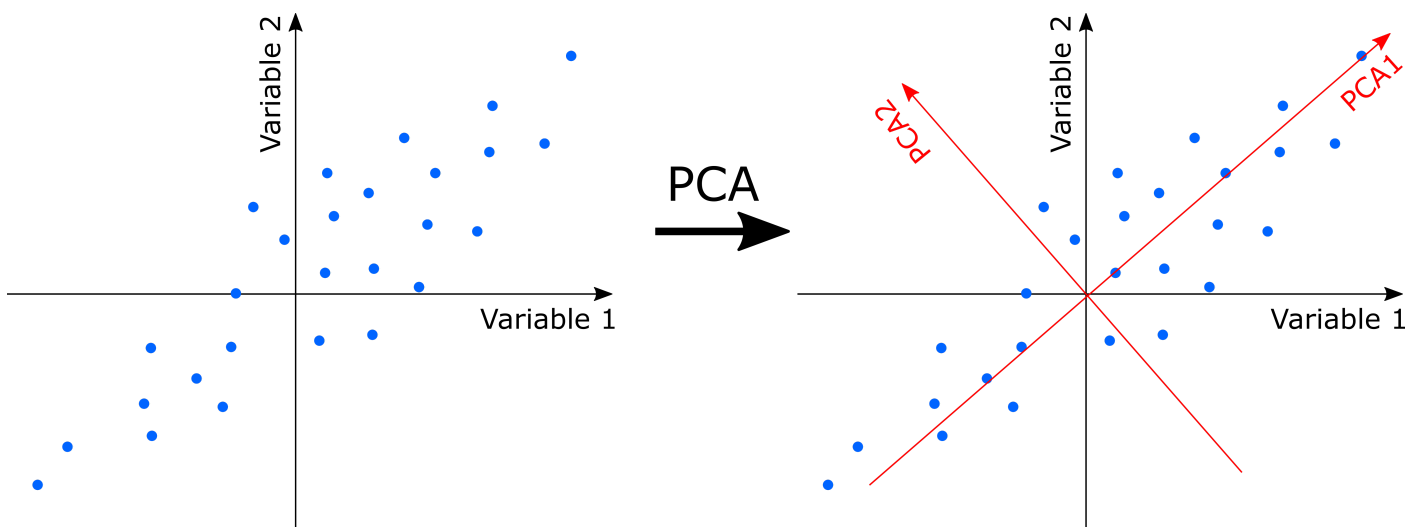
## Different ordination techniques

- Principal Component Analysis (PCA)
- Detrended Correspondence Analysis (DCA)
- Non-metric Multidimensional Scaling (NMDS)
- And MORE.....

## Principal Component Analysis (PCA)

- It is a linear dimensionality-reduction technique, i.e. it reduces strongly correlated data.
- In a nutshell, the PCA linearly transforms the feature from the original space to a new feature space, containing principal components that explain most of the variance in the dataset

## Principal Component Analysis (PCA)



source: Coding club

## Principal Component Analysis (PCA)

### Euclidean distances among samples

- The axes (also called principal components or PC) are orthogonal to each other (and thus independent).
- Each PC is associated with an eigenvalue.
- The sum of the eigenvalues will equal the sum of the variance of all variables in the data set.
- The eigenvalues represent the variance extracted by each PC, and are often expressed as a percentage of the sum of all eigenvalues (i.e. total variance).

## Principal Component Analysis (PCA)

- The relative eigenvalues thus tell how much variation that a PC is able to 'explain'.
- Axes are ranked by their eigenvalues:
  - the first axis has the highest eigenvalue and thus explains the most variance
  - the second axis has the second highest eigenvalue, etc.

## Principal Component Analysis (PCA)

```
PCA <- rda(dune2_spe, scale = FALSE) # Use scale = TRUE if your variables are on different scales (e.g. for abiotic variables).
# Here, all species are measured on the same scale
# So use scale = FALSE
PCA
```

```
Call: rda(X = dune2_spe, scale = FALSE)
```

```
              Inertia Rank  
Total              78.97  
Unconstrained    78.97   19  
Inertia is variance
```

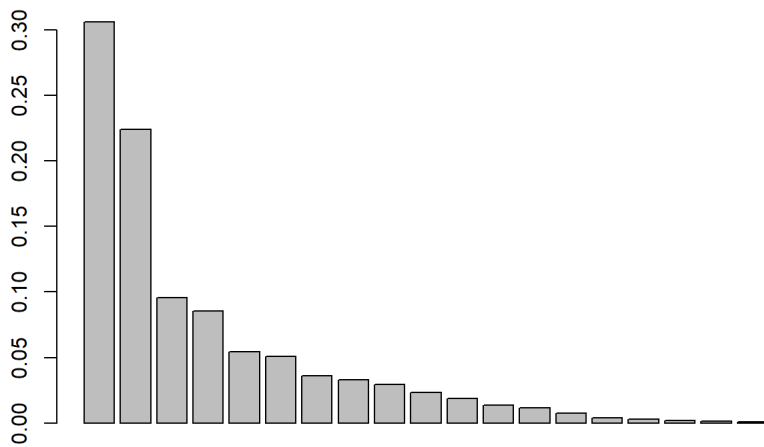
```
Eigenvalues for unconstrained axes:
```

	PC1	PC2	PC3	PC4	PC5	PC6	PC7	PC8
	24.181	17.678	7.557	6.760	4.274	4.009	2.835	2.584

(Showing 8 of 19 unconstrained eigenvalues)

## Principal Component Analysis (PCA)

```
# Now plot a bar plot of relative eigenvalues. This is the percentage variance explained by each axis  
barplot(as.vector(PCA$CA$eig)/sum(PCA$CA$eig))
```

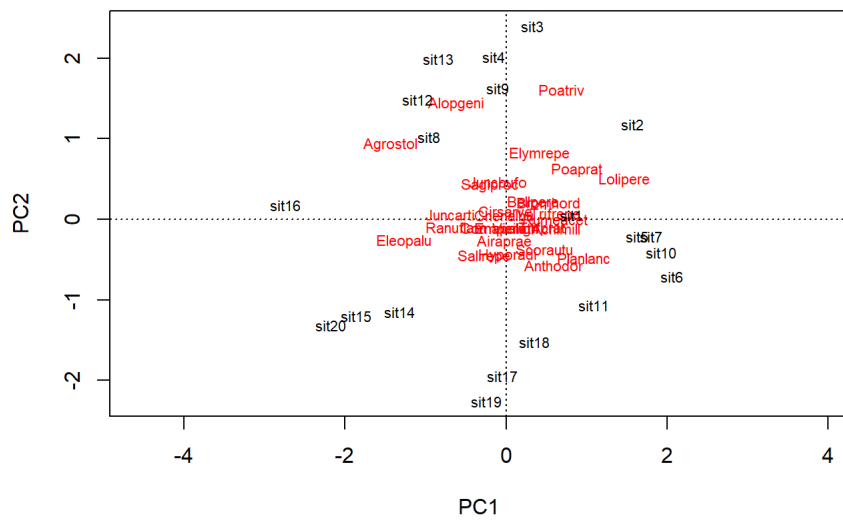


```
# Calculate the percent of variance explained by first two axes  
sum((as.vector(PCA$CA$eig)/sum(PCA$CA$eig))[1:2]) # 53%, this is ok.
```

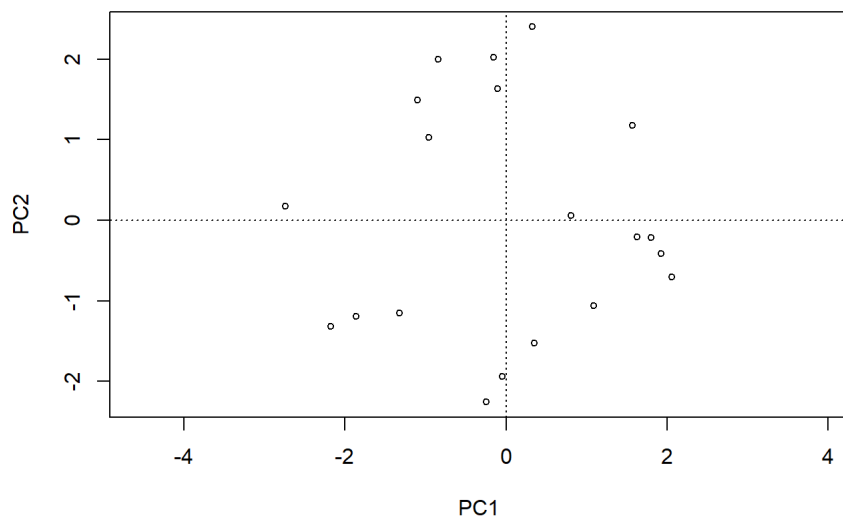
```
[1] 0.5300765
```

## Principal Component Analysis (PCA)

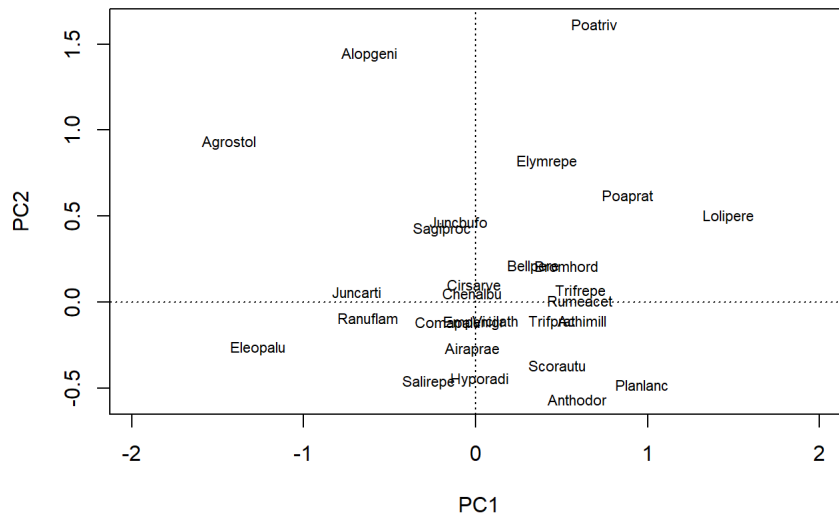
```
plot(PCA)
```



```
plot(PCA, display = "sites", type = "points")
```

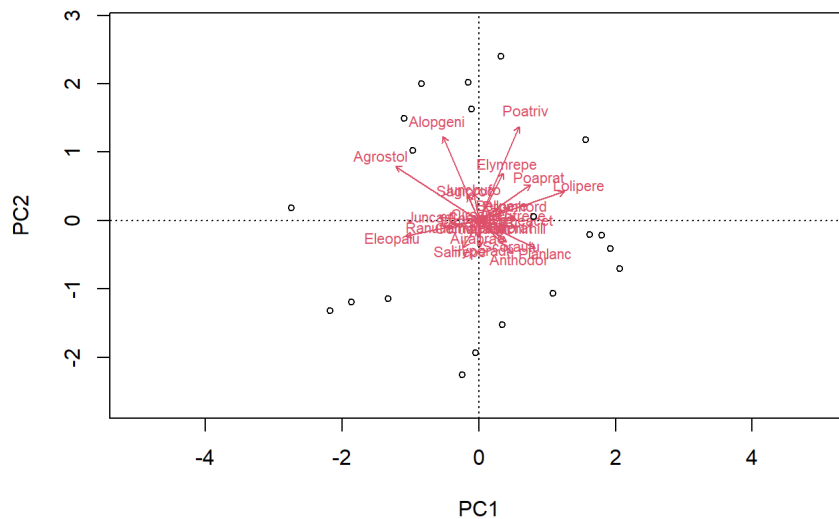


```
plot(PCA, display = "species", type = "text")
```



## Principal Component Analysis (PCA)

```
# In a biplot of a PCA, species' scores are drawn as arrows
# that point in the direction of increasing values for that variable
biplot(PCA, choices = c(1,2), type = c("text", "points"), xlim = c(-5,5)) # biplot of axis 1 vs 2
```



## Principal Component Analysis (PCA)

- This implies that the abundance of the species is continuously increasing in the direction of the arrow, and decreasing in the opposite direction.
- Thus PCA is a linear method.
- PCA is extremely useful when we expect species to be linearly (or even monotonically) related to each other.
- Unfortunately, we rarely encounter such a situation in nature.

## Environmental Variables and Triplot

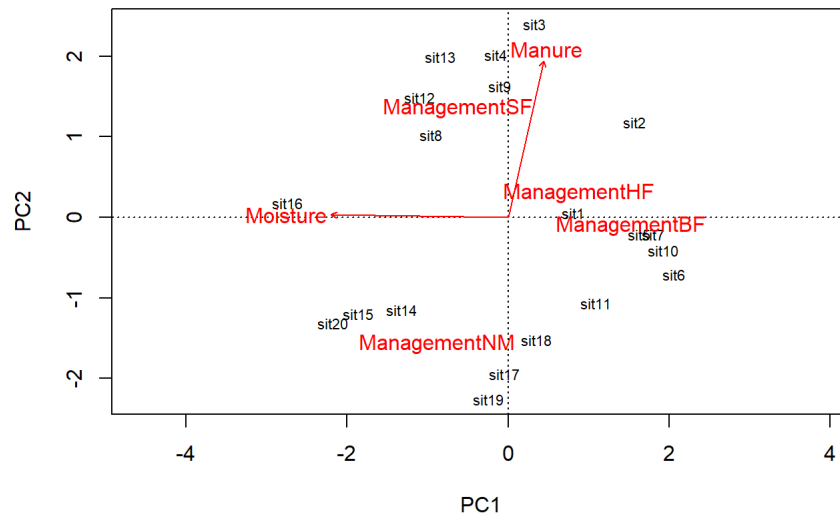
```
fit <- envfit(PCA, dune2_env, perm = 999)
```



```
scores(fit, "vectors")
```

	PC1	PC2
A1	-0.4981858	-0.11968978
Moisture	-0.8609679	0.01183937
Manure	0.1718683	0.75960897

```
plot(PCA,dis="site")  
plot(fit, p.max = 0.05, col = "red")
```

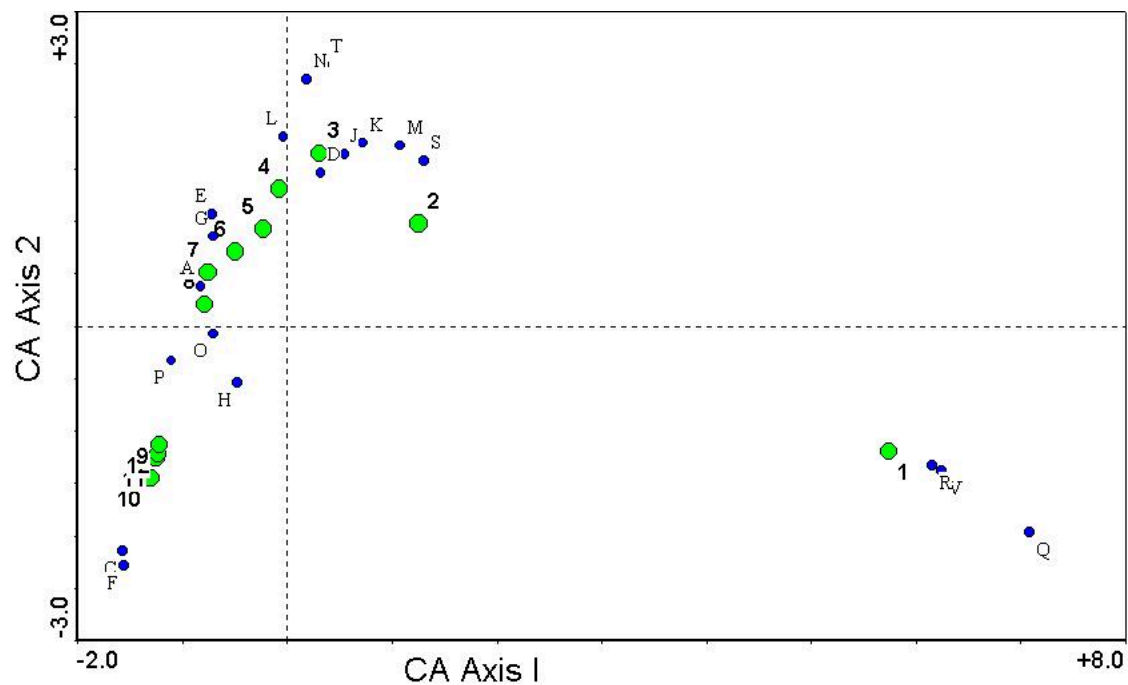


## Detrended correspondence analysis (DCA)

### chi-square distance metric among samples

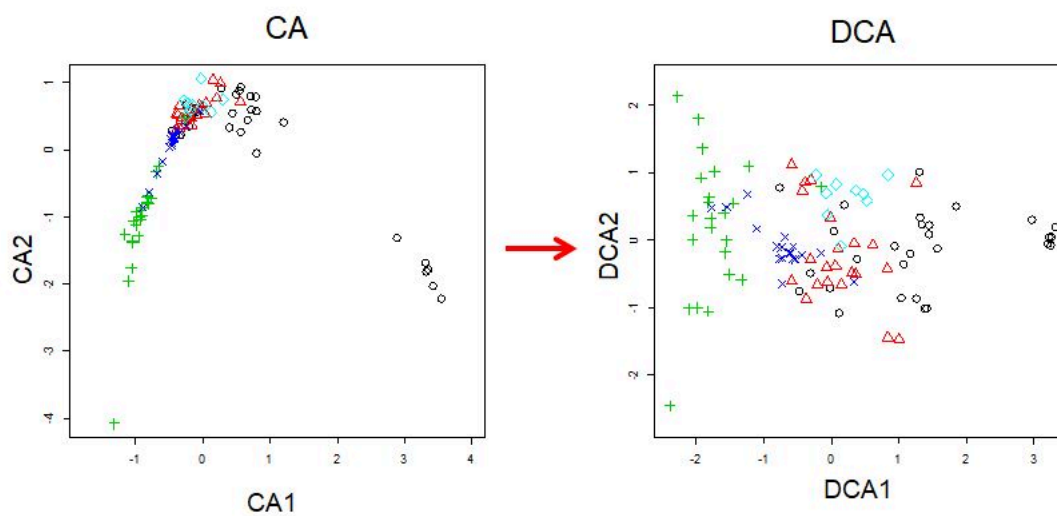
Correspondence analysis(CA) is an ordination method.

- It can calculate and display correspondence between samples and species in the same ordination space.
- It has a problem :suffers from creating often strong arch artefact in ordination diagrams. Which is caused by a non-linear correlation between first and higher axes



## Detrended correspondence analysis (DCA)

Arch can be removed by detrending (*smooths out the data to make it easier to see the main patterns*), which is the base of the detrended correspondence analysis (DCA).



source: davidzeleny

## Detrended correspondence analysis (DCA)

```
DCA<-decorana(dune2_spe)
DCA
```

Call:  
decorana(veg = dune2\_spe)

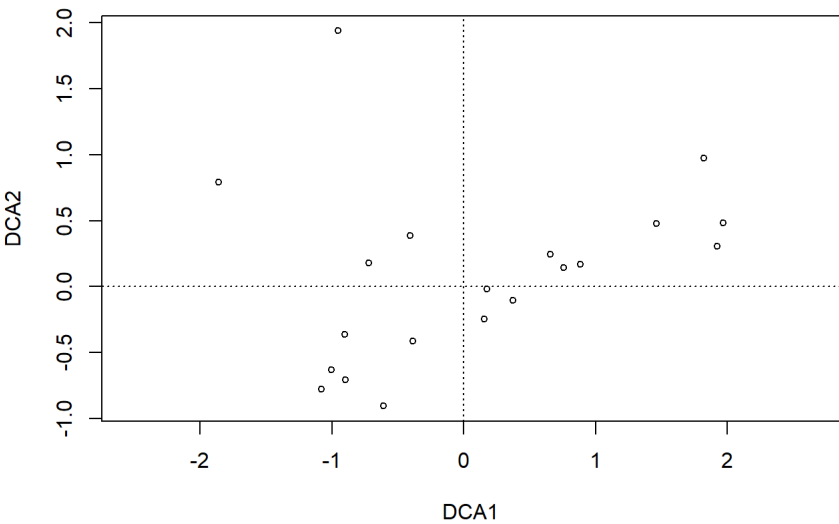
Detrended correspondence analysis with 26 segments.  
Rescaling of axes with 4 iterations.  
Total inertia (scaled Chi-square): 2.1866

DCA1 DCA2 DCA3 DCA4

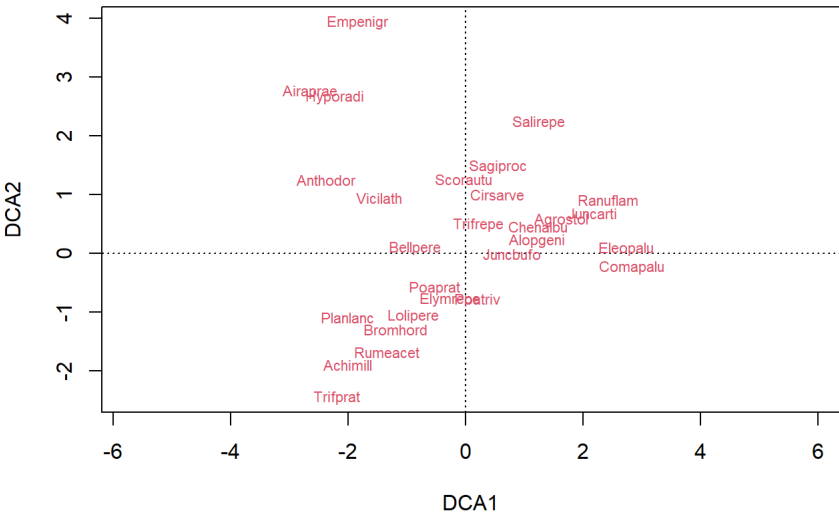
Eigenvalues            0.5392 0.3257 0.16889 0.19567  
Additive Eigenvalues 0.5392 0.3175 0.15318 0.18878  
Decorana values        0.5636 0.3194 0.07921 0.04138  
Axis lengths           3.8264 2.8444 2.03949 2.17577

## Detrended correspondence analysis (DCA)

```
ordiplot (DCA, display = 'sites', type = 'p')
```



```
ordiplot (DCA, display = 'species', type = 't')
```



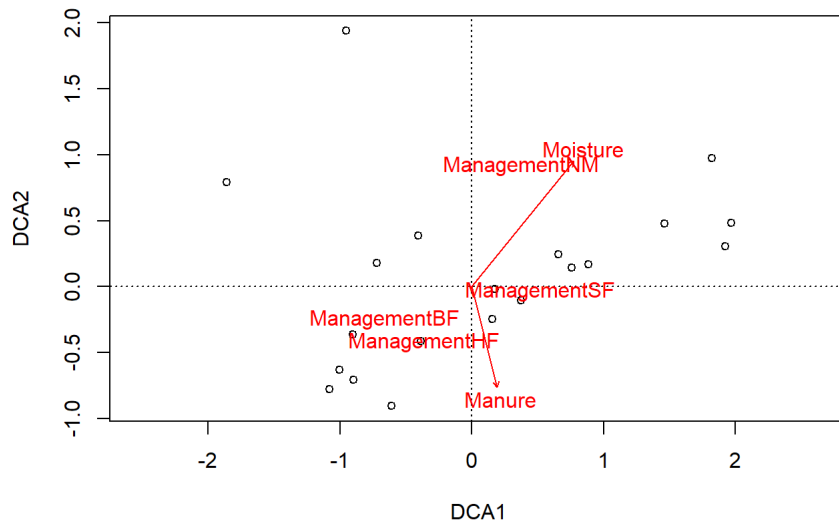
## Triplot

```
fit <- envfit(DCA, dune2_env, perm = 999)  
scores(fit, "vectors")
```

	DCA1	DCA2
A1	0.5149060	0.01196127

Moisture 0.5571229 0.68949173  
Manure 0.1388042 -0.55260255

```
plot(DCA,dis="site")  
plot(fit, p.max = 0.05, col = "red")
```



## Non-metric Multidimensional Scaling (NMDS)

- It uses an iterative optimization algorithm to find the best representation of distances in reduced space.
- NMDS is not an eigenanalysis. This has three important consequences:
  - There is no unique ordination result
  - The axes of the ordination are not ordered according to the variance they explain
  - The number of dimensions of the low-dimensional space must be specified before running the analysis

## Non-metric Multidimensional Scaling (NMDS)

- The lower the stress value (a measure of goodness-of-fit), the better the representation of objects in the ordination-space is.
- `distance` specifies the distance metric to use
- `k` specifies the number of dimensions.

## Non-metric Multidimensional Scaling (NMDS)

Methodology of NMDS:

Step 1: Perform NMDS with 1 to 10 dimensions Step 2: Check the stress vs dimension plot Step 3: Choose optimal number of dimensions Step 4: Perform final NMDS with that number of dimensions Step 5: Check for convergent solution and final stress

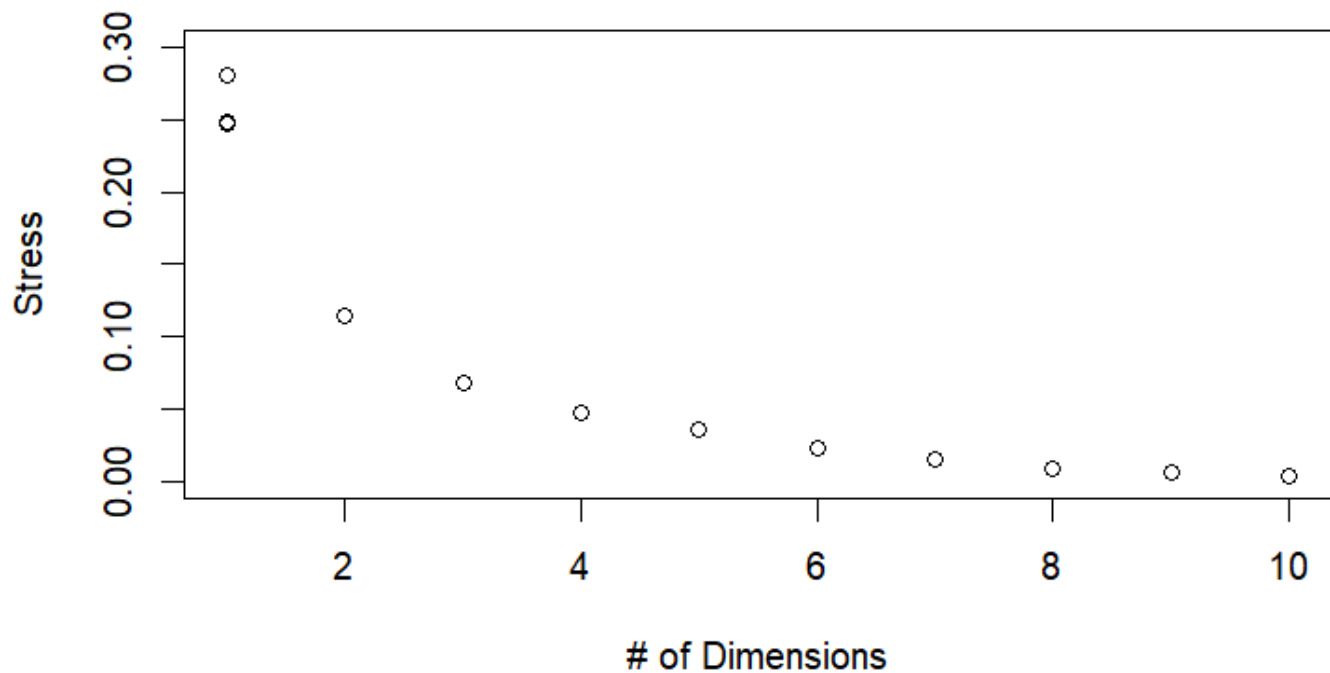
## Non-metric Multidimensional Scaling (NMDS)

```
# First step is to calculate a distance matrix. See PCOA for more information about the distance measures  
# Here we use bray-curtis distance, which is recommended for abundance data  
dist <- vegdist(dune2_spe, method = "bray")  
  
# In this part, we define a function NMDS.scree() that automatically  
# performs a NMDS for 1-10 dimensions and plots the nr of dimensions vs the stress  
NMDS.scree <- function(x) { #where x is the name of the data frame variable  
  plot(rep(1, 10), replicate(10, metaMDS(x, autotransform = F, k = 1)$stress), xlim = c(1, 10), ylim = c(0, 0.30), xlab = "# of Dimensions", ylab = "Stress",  
    for (i in 1:10) {  
      points(rep(i + 1, 10), replicate(10, metaMDS(x, autotransform = F, k = i + 1)$stress))  
    }  
  }
```

```
}  
NMDS.scree(dist)
```

## Non-metric Multidimensional Scaling (NMDS)

### NMDS stress plot



## Non-metric Multidimensional Scaling (NMDS)

```
# Because the final result depends on the initial  
# random placement of the points  
# we'll set a seed to make the results reproducible  
set.seed(2)  
  
# Here, we perform the final analysis and check the result  
NMDS1 <- metaMDS(dist, k = 3, trymax = 100, trace = F)  
# Do you know what the trymax = 100 and trace = F means?  
# Let's check the results  
NMDS1
```

Call:

```
metaMDS(comm = dist, k = 3, trymax = 100, trace = F)
```

global Multidimensional Scaling using monoMDS

Data: dist

Distance: bray

Dimensions: 3

Stress: 0.06826238

Stress type 1, weak ties

Best solution was repeated 5 times in 20 tries

The best solution was from try 9 (random start)

Scaling: centring, PC rotation, halfchange scaling

Species: scores missing

```
# If you don't provide a dissimilarity matrix, metaMDS automatically applies Bray-Curtis. So in our case, the results would have to be the same as NMDS2
NMDS2 <- metaMDS(dune2_spe, k = 2, trymax = 100, trace = F)
NMDS2
```

Call:

```
metaMDS(comm = dune2_spe, k = 2, trymax = 100, trace = F)
```

global Multidimensional Scaling using monoMDS

Data: dune2\_spe

Distance: bray

Dimensions: 2

Stress: 0.1149964

Stress type 1, weak ties

Best solution was repeated 10 times in 20 tries

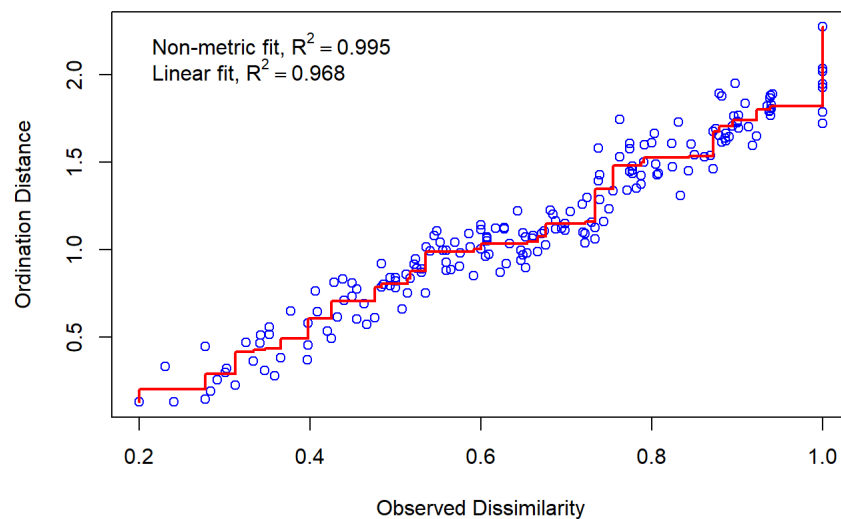
The best solution was from try 10 (random start)

Scaling: centring, PC rotation, halfchange scaling

Species: expanded scores based on 'dune2\_spe'

## Non-metric Multidimensional Scaling (NMDS)

```
stressplot(NMDS1)
```

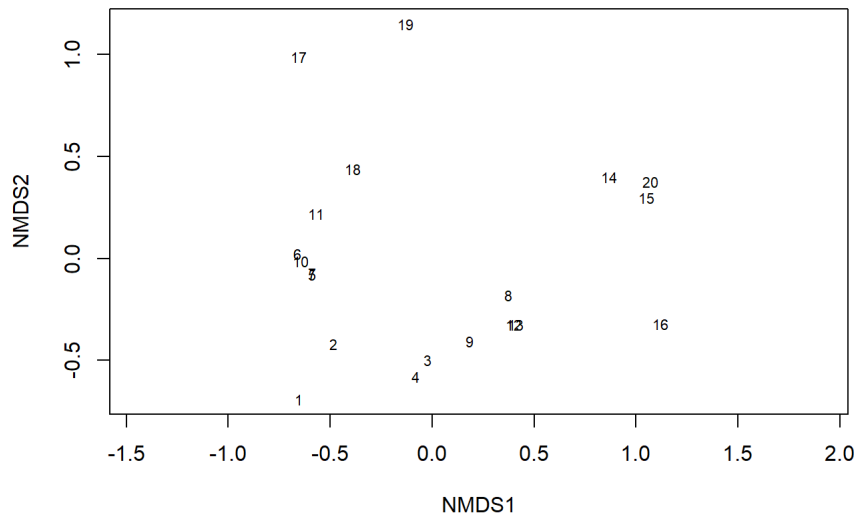


## Non-metric Multidimensional Scaling (NMDS)

```
plot(NMDS1, type = "t")
```

species scores not available



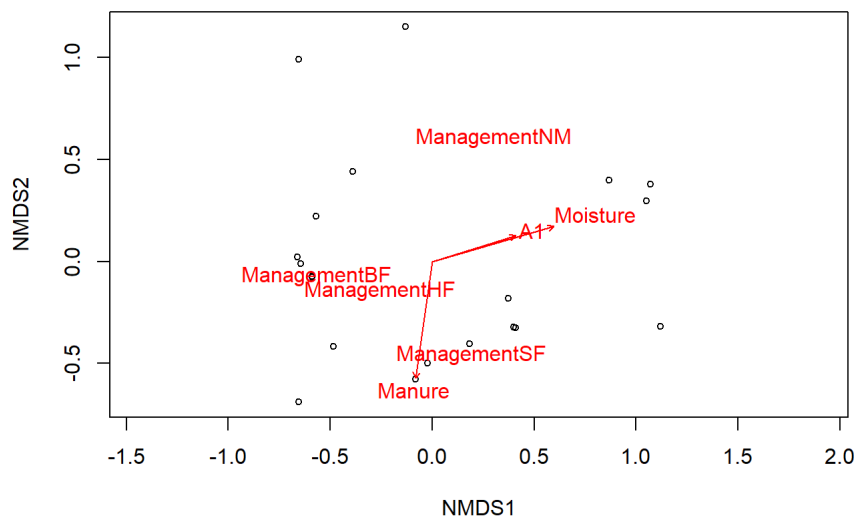


#Triplot

```
fit <- envfit(NMDS1, dune2_env, perm = 999)
scores(fit, "vectors")
```

	NMDS1	NMDS2
A1	0.5926574	0.1838978
Moisture	0.8639184	0.2488776
Manure	-0.1197459	-0.8307617

```
plot(NMDS1,dis="site")
plot(fit, p.max = 0.05, col = "red")
```



## Ordihull

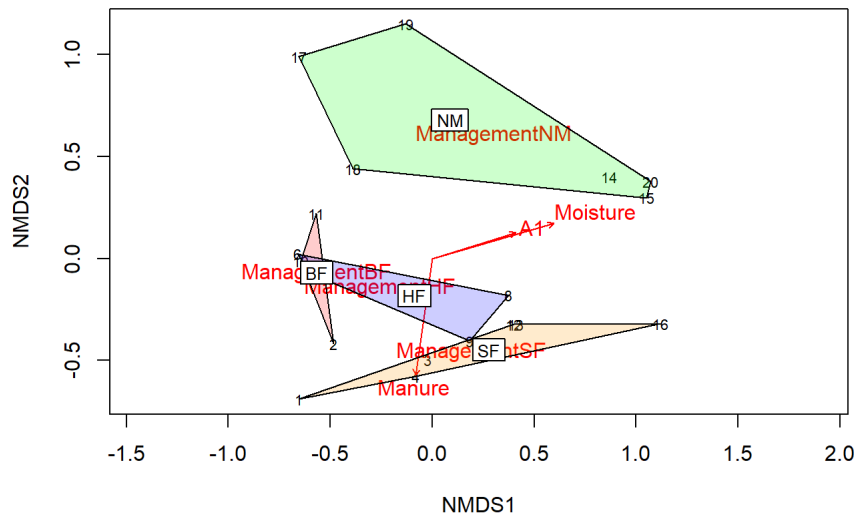
```
group_colors <- c("red", "blue", "green", "orange")

# Plot the NMDS1 ordination with no points plotted initially
plot(NMDS1, type="t")
plot(fit, p.max = 0.05, col = "red")
```

```
# Add convex hulls around groups defined by the 'Management' variable,
# and label the points with their corresponding group names
with(dune2_env, ordihull(NMDS1, Management,
  draw = 'polygon',
  alpha = 50,
  label = TRUE,col = group_colors ))
```

## Ordihull

species scores not available



## BREAK

