Tech Note

Below, I've compiled a list of related works, along with hyperlinks to the papers, and brief descriptions of their main concepts.

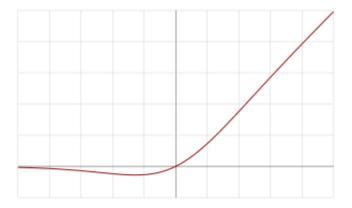
Swish

SEARCHING FOR ACTIVATION FUNCTIONS, ICLR 2018 workshop

Swish is an activation, which is defined as $f(x) = x \cdot \sigma(\beta x)$.

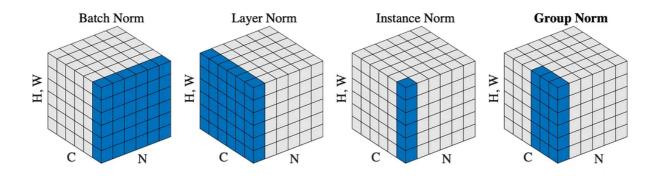
In our code, we set $\beta = 1$ in all the Swish activation, and which is also known as "Sigmoid Linear Unit (SiLU)".

• Update: Pytorch has implementation of SiLU



Group Normalization

Group Normalization, ECCV 2018

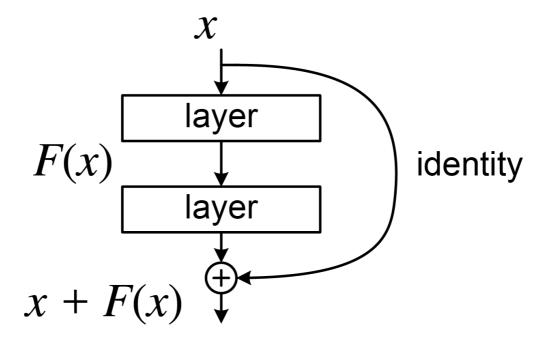


Normalization: A method to train model faster and more stable through normalization of tinputs by re-centering and re-scaling.

- Batch normalization: Normalization for each channel.
- Layer normalization: Normalization for each sample.
- Instance normalization: Normalization for each sample and each channel.
- Group normalization: Normalization for each sample group.

Note: If batch size is large enough, the performance: BN > GN > LN > IN However, BN has GPU memory issue and cannot set large batch size sometimes. Thus, we do GN in this task.

Deep Residual Learning for Image Recognition, CVPR 2016



A popular module to very learn deep model by residual learning.

Self-Attention

Attention Is All You Need, NIPS 2017

Self-attention, also known as scaled dot-product attention, is a crucial concept in the field of natural language processing (NLP) and deep learning, particularly within the context of transformer-based models. In pattern recognition task usually employ self-attention in each feature map, (therefore the weights in attention will be one by one convolution). Next, we will introduce what self-attention is.

Self-attention involves three key vectors for executing "attention to itself":

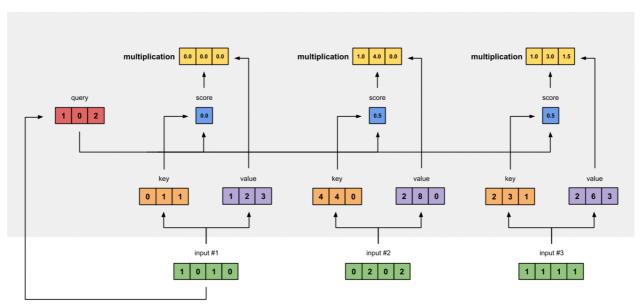
- 1. Query vectors: These query other elements in the sequence.
- 2. Key vectors: These define the importance relative to the current element.
- 3. Value vectors: These generate the output vectors.

After generating these three vectors, we follow these steps for each element:

- 1. Calculate the attention score, which is $W_{current,i} = K_{current} \cdot Q_i$, where $i \in [1,C]$, and C is the input size.
- 2. Scale and softmax the score, which means $W_{current} = \operatorname{softmax}\left(\frac{W_{current}}{\sqrt{C}}\right)$.
- 3. Generate the output, $H_{current} = W_{current} * V$.

Finally, to apply this method to convolutions, we can simply replace all linear layers with one-by-one convolutional layers, and everything will be fine.

Self-attention



Flow chart of Self-Attention

Positional Encoding

Attention Is All You Need, NIPS 2017

After applying the self-attention module in NLP, a crucial issue arises. Self-attention in NLP tasks lacks knowledge of the neuron's position within the sequence during its operation. Position is a critical factor in these tasks. Consequently, the authors introduced the idea of adding positional encoding to each neuron, using a sinusoidal embedding function, which was also introduced in the same paper 'The Attention Is All You Need'.

The provided sinusoidal embedding formula can be presented as follows:

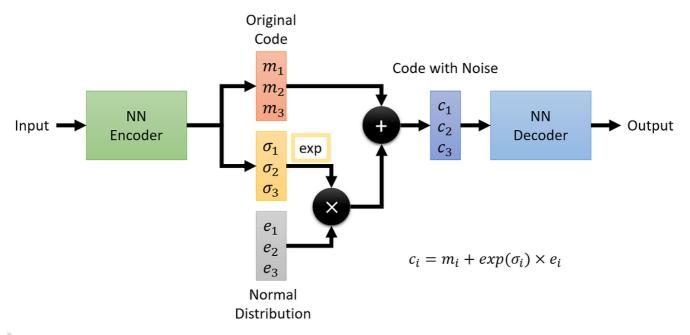
```
1 EMB[pos, 2i] = sin(pos / 10000^(2i/d_model))
2 EMB[pos, 2i+1] = cos(pos / 10000^(2i/d_model))
```

This formula is used to calculate the values for the positional encoding matrix, where pos represents the position of a token or neuron, i is the index of the dimension, and d_model is the model's dimensionality.

Variational Autoencoder (VAE)

Auto-Encoding Variational Baye, ICLR 2014

This paper introduce what VAE is.



Flow chart of VAE.

The most important thing that VAE aims to solve is to make it easier for us to generate random images from the latent space. We need to know what distribution the latent space, encoded by the encoder, follows, but this problem is quite challenging. Therefore, we can approach it from a different perspective: constraining the latent code generated by the encoder to be similar to a well-known distribution, typically a Gaussian distribution.

But how do we calculate the regularization term? Next, we will explore what the regularization term should be if we use the KL divergence to measure the distance between the latent space and a Gaussian distribution.

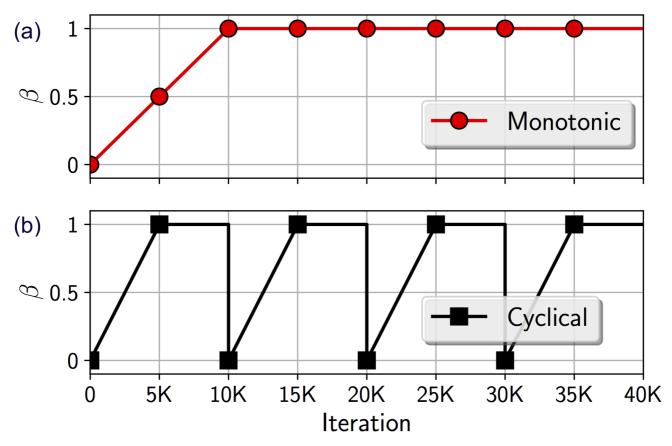
Notation: q is encoder, z is latent.

- For an showed image x, we need to maximize the log probability (because of max likelihood) x generated by AE, p(x).
 - $\circ \log p(x) = \log \int_z p(x,z) dz = \log \int_z p(x,z) rac{q(z|x)}{q(z|x)} dz$
 - \circ By Jensen's inequality, $\log p(x) \geq \mathbb{E}_{q(z|x)} \log rac{p(x,z)}{q(z|x)} dz$
 - ullet By Bayes' theorem, $\log p(x) \geq \mathbb{E}_{q(z|x)} \log rac{p(x|z)p(z)}{q(z|x)}$
 - $lacksquare = \mathbb{E}_{q(z|x)} \log p(x|z) + \mathbb{E}_{q(z|x)} \log rac{p(z)}{q(z|x)}$
 - $ullet = \mathbb{E}_{q(z|x)} \log p(x|z) + \int_z q(z|x) \log rac{p(z)}{q(z|x)}$
 - $lacksquare = \mathbb{E}_{q(z|x)} \log p(x|z) D_{KL}[q(z|x)||p(z)]$
 - $= Maxlikelihood D_{KL}[q(z|x)||p(z)]$
- Where we assume p(z) is gaussian distribution N(0,1), and q(z|x) is $N(\mu,\sigma)$
 - \circ Recall that $N(\mu,\sigma)=rac{1}{\sigma\cdot\sqrt{2\pi}}\exp(-rac{1}{2}(rac{x-\mu}{\sigma})^2)$
 - $\log N(\mu, \sigma) = \log \frac{1}{\sqrt{2\pi}} \log \sigma \frac{1}{2} (\frac{x-\mu}{\sigma})^2$
 - $\circ \ \ D_{KL}[N(\mu,\sigma)||N(0,1)] = \int N(\mu,\sigma)[(\log \tfrac{1}{\sqrt{2\pi}} \log \tfrac{1}{\sqrt{2\pi}}) (\log \sigma \log 1) \tfrac{1}{2}((\tfrac{x-\mu}{\sigma})^2 (\tfrac{x-0}{1})^2)]dx$
 - $lacksquare = \mathbb{E}_{N(\mu,\sigma)}[-\log\sigma rac{1}{2}((rac{x-\mu}{\sigma})^2 x^2)]$
 - $lacksquare = -\log\sigma rac{1}{2\sigma^2}\mathbb{E}_{N(\mu,\sigma)}[(x-\mu)^2] + \mathbb{E}_{N(\mu,\sigma)}[x^2]$
 - $lacksquare = -\log \sigma rac{1}{2} + \mathbb{E}_{N(\mu,\sigma)}[x^2]$
 - $\sigma^2 = \mathbb{E}[x^2] \mathbb{E}[x]^2
 ightarrow \mathbb{E}[x^2] = \mu^2 + \sigma^2$
 - $lacksquare = -\log \sigma rac{1}{2} rac{1}{2}(\sigma^2 + \mu^2)$
 - $lacktriangledown = -rac{1}{2}(1 + \log \sigma^2 \sigma^2 \mu^2)$
 - Thus, the regularization term for KL divergence is $=-\frac{1}{2}(1+\log\sigma^2-\sigma^2-\mu^2)$. If we modify the encoder from an image to some μ and σ , and sample the latent variable from $N(\mu,\sigma)$, then we can apply this term.

KLD Loss Scheduler

Cyclical Annealing Schedule: A Simple Approach to Mitigating KL Vanishing (NAACL 2019)

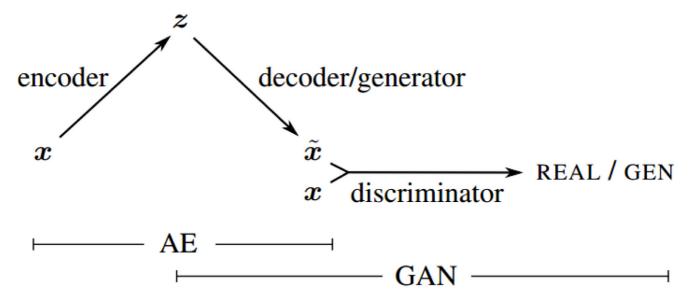
Balancing the weights of VAE_loss and KLD_loss is a challenging task. If we set VAE_loss too high, clear images won't be generated from sampling the latent space because it won't match the decoder's distribution. Conversely, if we set KLD_loss too high, the autoencoder may tend to experience mode collapse and ignore the reconstruction loss term. To mitigate this issue, we employ a technique known as the cyclical annealing scheduler, which periodically adjusts the weight of KLD_loss.



VAE-GAN

autoencoding beyond pixels using a learned similarity metric (ICML 2016)

Because the image generated from the vanilla VAE is too blurry, we can use GAN to mitigate this phenomenon. To prevent mode collapse from occurring too early, we only train the GAN part from a specific iteration.



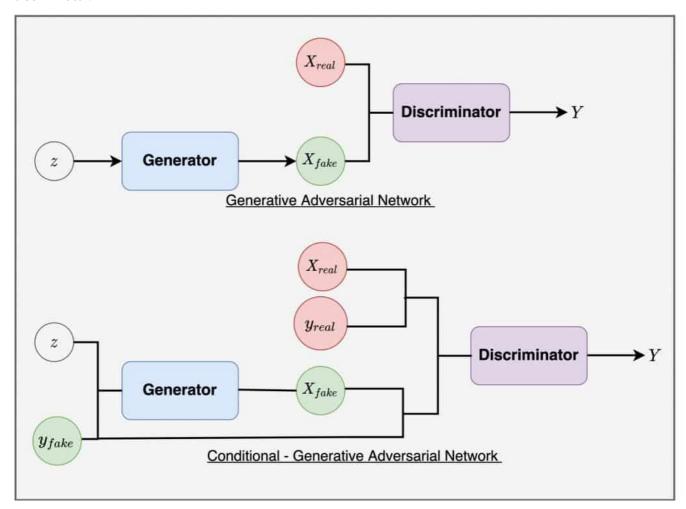
Conditional GAN & PatchGAN

Image-to-Image Translation with Conditional Adversarial Networks (CVPR 2017)

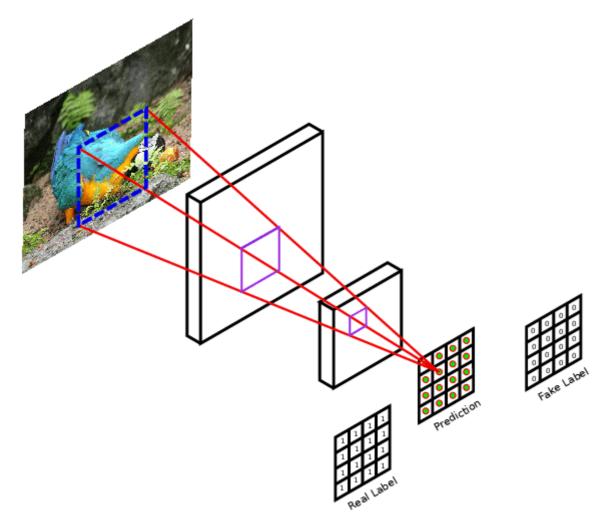
We have incorporated two concepts from this paper: conditional GAN and Patch GAN.

Our task is to reconstruct brains, and we have observed that each brain generates 32 images with different z-index values. This additional information enables us to implement conditional GAN, leveraging this extra condition to enhance the quality of randomly generated images.

Instead of using regular embedding, we have opted for sinusoidal embedding in the z-index and have added these positional encodings after the feature map passes through the convolutional layers in both the autoencoder and discriminator.



The original discriminator in GANs aims to predict whether the entire image is real or fake, whereas PatchGAN is designed to predict the reality of individual patches or windows within the image. I believe that this approach provides better guidance to the generator for capturing and generating detailed features in the image.



VQVAE

Neural Discrete Representation Learning (NIPS 2017)

Because the latent space in VAE is continuous, it is challenging to sample from it, even with the addition of a KLD regularization term during VAE training to constrain the latent space to be similar to the Normal Distribution N(0, 1). This paper introduces a method to discretize the latent space, making it possible to sample from a discrete space. Furthermore, since the latent space is discrete and reduced in size, we can employ an powerful auto-regressive model to generate the latent values. For instance, the author of this paper uses PixelCNN as the decoder.

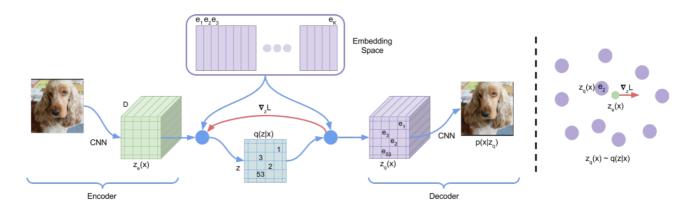


Figure 1: Left: A figure describing the VQ-VAE. Right: Visualisation of the embedding space. The output of the encoder z(x) is mapped to the nearest point e_2 . The gradient $\nabla_z L$ (in red) will push the encoder to change its output, which could alter the configuration in the next forward pass.

The next problem is how to discretize the latent space while still allowing for network updates through gradients. The discretization layer is not differentiable. To address this challenge, VQVAE employs three losses:

- 1. Reconstruction Loss: This is equivalent to VAE.
- 2. Loss to make the embedding layer (or discrete latent) similar to the latent vector generated by the encoder.

- 3. The same as 2, but in reversed.
 - Note that we don't want the encoder to generate the discrete latent directly, so this term is multiplied by beta, with the beta value in the paper set to 0.25.

After applying these three losses, your VQVAE will be successfully trained.

Furthermore, there's VQVAE2, which discretizes the latent space into two layers. However, due to time constraints, I don't have the opportunity to explore this approach.



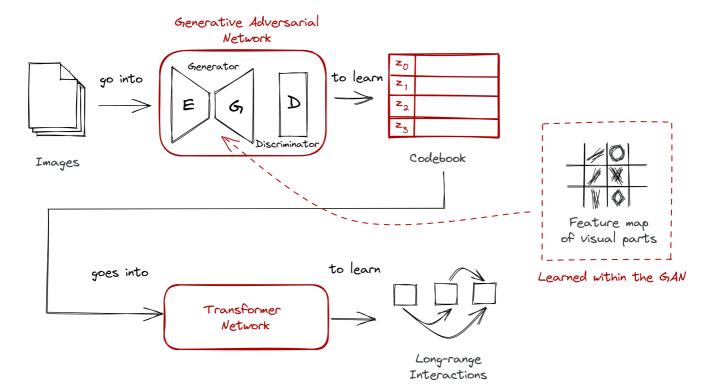
- (a) Overview of the architecture of our hierarchical VQ-VAE. The encoders and decoders consist of deep neural networks. The input to the model is a 256×256 image that is compressed to quantized latent maps of size 64×64 and 32×32 for the bottom and top levels, respectively. The decoder reconstructs the image from the two latent maps.
- (b) Multi-stage image generation. The top-level PixelCNN prior is conditioned on the class label, the bottom level PixelCNN is conditioned on the class label as well as the first level code. Thanks to the feed-forward decoder, the mapping between latents to pixels is fast. (The example image with a parrot is generated with this model).

VQGAN

<u>VQGAN (Taming Transformers for High-Resolution Image Synthesis, CVPR 2021)</u>

This paper improves VQVAE with two key concepts:

- 1. It adds a GAN component (or discriminator) at the end of the VAE.
- 2. It utilizes a transformer, as opposed to PixelCNN, for sampling in the latent space.



Denoising Diffusion Probabilistic Models (NIPS 2020)

Diffusion Probabilistic Models (DDPM) is a generative modeling approach that represents data as the result of a diffusion process. It models how data evolves over time, adding noise gradually according to a schedule. Invertible neural networks are used to capture this process, enabling the generation of data samples and likelihood estimation. DDPM is known for its ability to generate high-quality data samples.



To elaborate:

- Let x_t represent an image subjected to the addition of Gaussian noise over T times. The weight of the noise and image should be $x_{t+1} = x_t \cdot \sqrt{1-\beta_{t+1}} + N(0,I) \cdot \sqrt{\beta_{t+1}}$, where β is a sequence from 0 to 1. In DDPM paper, author set β equals to linspace(0.002, 1, T=1000)
 - And we have

$$x_t = x_0 \cdot \sqrt{1-eta_1} \cdot \sqrt{1-eta_2} \dots \sqrt{1-eta_t} + N(0,I)(\sqrt{eta_1}\sqrt{1-eta_2} \dots \sqrt{1-eta_t}) + \dots + N(0,I) \cdot \sqrt{eta_t}$$

- 1. For convenience, we let $lpha_t=1-eta_t, ar{lpha}_t=\prod_{i=1}^t lpha_t.$
- 2. The formula for the summation of two normal distributions:

$$N(\mu_X,\sigma_X^2)+N(\mu_Y,\sigma_Y^2)=N(\mu_X+\mu_Y,\sigma_X^2+\sigma_Y^2).$$

$$\qquad \quad \bullet \quad \sqrt{1-\beta_2}(\sqrt{\beta_1}N(0,I)) + \sqrt{\beta_2}N(0,I) = N(0,\beta_1\cdot(1-\beta_2)) + N(0,\beta_2)$$

$$ullet = N(0, eta_1 \cdot (1 - eta_2) + eta_2) = N(0, 1 - (1 - eta_1)(1 - eta_2)) = N(0, 1 - lpha_1 \cdot lpha_2)$$

$$\qquad \text{Similarly, } \sqrt{1-\beta_3}N(0,1-\alpha_1\cdot\alpha_2) + \sqrt{\beta_3}N(0,I) = N(0,(1-\alpha_1\cdot\alpha_2)\cdot(1-\beta_3) + \beta_3)$$

$$= N(0, 1 - \alpha_1 \cdot \alpha_2 + \alpha_1 \cdot \alpha_2 \cdot \beta_3)$$

$$= N(0, 1 - \alpha_1 \cdot \alpha_2 \cdot (1 - \beta_3)) = N(0, 1 - \alpha_1 \cdot \alpha_2 \cdot \alpha_3)$$

- lacksquare Here we can find the pattern that the noise of x_t will be $N(0,1-arlpha_t)=\sqrt{1-arlpha_t}\cdot N(0,I)$
- Finally, we have $x_t = x_0 \cdot \sqrt{\bar{\alpha}_t} + N(0, I) \cdot \sqrt{1 \bar{\alpha}_t}$. We aim to train the model to predict the noise given x_t and its time t.
- For inference, due to the lengthy proof, we skip the derivation and utilize the formula provided in the paper.

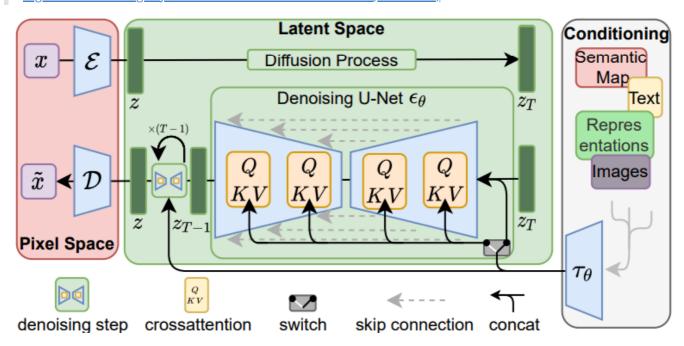
Algorithm 1 Training	Algorithm 2 Sampling
1: repeat 2: $\mathbf{x}_0 \sim q(\mathbf{x}_0)$ 3: $t \sim \text{Uniform}(\{1, \dots, T\})$ 4: $\boldsymbol{\epsilon} \sim \mathcal{N}(0, \mathbf{I})$ 5: Take gradient descent step on $\nabla_{\theta} \left\ \boldsymbol{\epsilon} - \boldsymbol{\epsilon}_{\theta} (\sqrt{\bar{\alpha}_t} \mathbf{x}_0 + \sqrt{1 - \bar{\alpha}_t} \boldsymbol{\epsilon}, t) \right\ ^2$ 6: until converged	1: $\mathbf{x}_{T} \sim \mathcal{N}(0, \mathbf{I})$ 2: for $t = T, \dots, 1$ do 3: $\mathbf{z} \sim \mathcal{N}(0, \mathbf{I})$ if $t > 1$, else $\mathbf{z} = 0$ 4: $\mathbf{x}_{t-1} = \frac{1}{\sqrt{\alpha_{t}}} \left(\mathbf{x}_{t} - \frac{1-\alpha_{t}}{\sqrt{1-\bar{\alpha}_{t}}} \boldsymbol{\epsilon}_{\theta}(\mathbf{x}_{t}, t) \right) + \sigma_{t} \mathbf{z}$ 5: end for 6: return \mathbf{x}_{0}

• where σ_t is $\sqrt{\beta_t}$. We'll generate new noise when sampling.

Nevertheless, training a diffusion model on raw images is a time-consuming process. To strike a balance, there's a compromise method: applying DDPM to a smaller latent space, which is generated by the VAE's encoder. This approach is one of the main contributions to stable diffusion.

Stable Diffusion

High-Resolution Image Synthesis with Latent Diffusion Models (CVPR 2022)



Stable diffusion comprises with two key contributions: DDPM on the latent space and cross-attention across different modalities. However, since the OASIS dataset lacks of other conditions, we did not implement cross-attention in this repository.