

```
% Exercise
close all; clear all;

%given data
%Young's Modulus
E_al = 75e+9; %Pa
E_ni = 209e+9; %Pa
E_sa = 197e+9; %Pa
%length
L_ad = 4; %m
L_be = 5; %m
L_cg = 2; %m
%data
P = 90e3; %N
A = 0.0004; %m^2
d = linspace(0, 16, 1600); %m

%QUESTION 1
%Force: Aluminum Alloy 1100 (al)
%matrix
force = [];

for i = 1:length(d)
    eq_1 = [1 1 1 -P];
    eq_2 = [0 10 16 -d(i)*P];
    eq_3 = [6*(L_ad/(E_al*A)) -16*(L_be/(E_al*A)) 10*(L_cg/(E_al*A)) 0];
    aug_matrix_al = [eq_1 ; eq_2 ; eq_3];
    matrix = aug_matrix_al(1:end, 1:end-1);
    b = aug_matrix_al(1:end, end);
    force = [force; transpose(matrix\b)];
end
```

```
%Elongation Percentage
perc_al_ad = max((force(:,1))/(E_al*A))*100;
perc_al_be = max((force(:,2))/(E_al*A))*100;
perc_al_cg = max((force(:,3))/(E_al*A))*100;
perc_ni_ad = max((force(:,1))/(E_ni*A))*100;
perc_ni_be = max((force(:,2))/(E_ni*A))*100;
perc_ni_cg = max((force(:,3))/(E_ni*A))*100;
perc_sa_ad = max((force(:,1))/(E_sa*A))*100;
perc_sa_be = max((force(:,2))/(E_sa*A))*100;
perc_sa_cg = max((force(:,3))/(E_sa*A))*100;
perc_al = max([perc_al_ad perc_al_be perc_al_cg])
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perc_al = 0.0443
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perc_ni = max([perc_ni_ad perc_ni_be perc_ni_cg])
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perc_ni = 0.0159
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perc_sa = max([perc_sa_ad perc_sa_be perc_sa_cg])
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perc_sa = 0.0169
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%QUESTION 2
%create F*L matrix
FL = [force(:,1).*(L_ad), force(:,2).*(L_be), force(:,3).*(L_cg)];
FL_diff = [abs(FL(:,3) - FL(:,1))];
FL_diff_min = min(FL_diff);
index = find(FL_diff == FL_diff_min, 1)
```

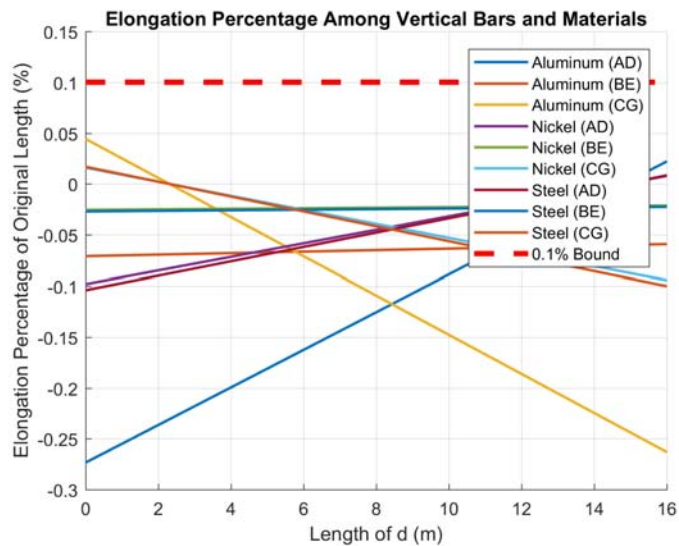
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index = 1053
```

```
%2 PLOTS
%1) forces on aluminum, nickel, steel alloy
bound = [];
bound(1:length(d)) = 0.1;
hold on;
plot(d, ((force(:,1))/(E_al*A))*100, 'LineWidth', 1.5);
plot(d, ((force(:,2))/(E_al*A))*100, 'LineWidth', 1.5);
plot(d, ((force(:,3))/(E_al*A))*100, 'LineWidth', 1.5);
plot(d, ((force(:,1))/(E_ni*A))*100, 'LineWidth', 1.5);
plot(d, ((force(:,2))/(E_ni*A))*100, 'LineWidth', 1.5);
plot(d, ((force(:,3))/(E_ni*A))*100, 'LineWidth', 1.5);
plot(d, ((force(:,1))/(E_sa*A))*100, 'LineWidth', 1.5);
```

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plot(d, ((force(:,2))/(E_sa*A))*100, 'LineWidth', 1.5);
plot(d, ((force(:,3))/(E_sa*A))*100, 'LineWidth', 1.5);
plot(d, bound, '--r', 'LineWidth', 3);
grid on;
hold off;
title('Elongation Percentage Among Vertical Bars and Materials');
xlabel('Length of d (m)');
ylabel('Elongation Percentage of Original Length (%)');
legend('Aluminum (AD)', 'Aluminum (BE)', 'Aluminum (CG)', 'Nickel (AD)', 'Nickel (BE)', 'Nickel (CG)', 'Steel (AD)', 'Steel (BE)', 'Steel (CG)', '0.1% Bound');

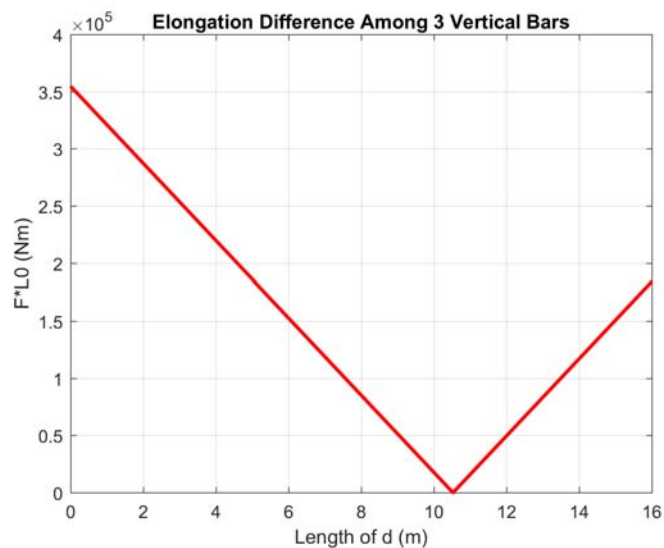
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```

%2) minimum
figure;
plot(d, FL_diff, '-r', 'LineWidth', 2);
grid on;
title('Elongation Difference Among 3 Vertical Bars');
xlabel('Length of d (m)');
ylabel('F*L0 (Nm)');

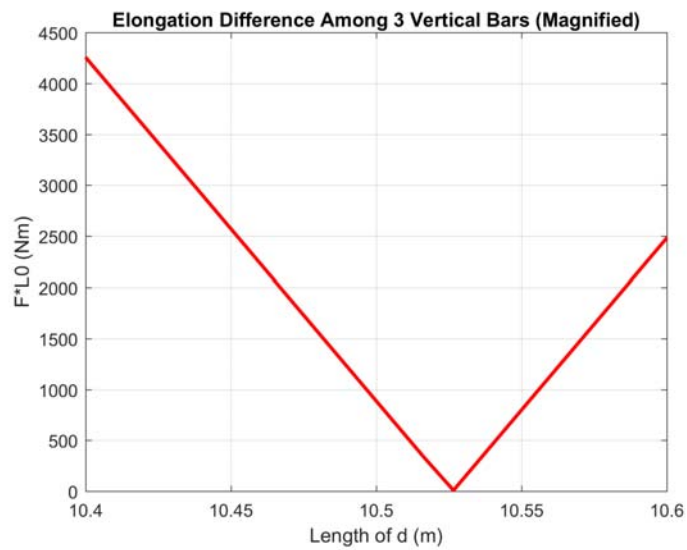
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```

figure;
plot(d, FL_diff, '-r', 'LineWidth', 2);
xlim([10.4 10.6]);
grid on;
title('Elongation Difference Among 3 Vertical Bars (Magnified)');
xlabel('Length of d (m)');
ylabel('F*L0 (Nm)');

```



%ANSWERS

%1) While all three materials were able to elongate less than 0.1% of their original length ( $0 \text{ m} \leq d \leq 16 \text{ m}$ ), the material I would recommend is Aluminum Alloy 1100 due to its lower density and thus, weight.

%2) After comparing the elongation of each of the 3 vertical bars at the entire range of d,  $d = 10.53 \text{ m}$  seems to be where all three bars elongate the same distance and thus, keeping the horizontal bar leveled.