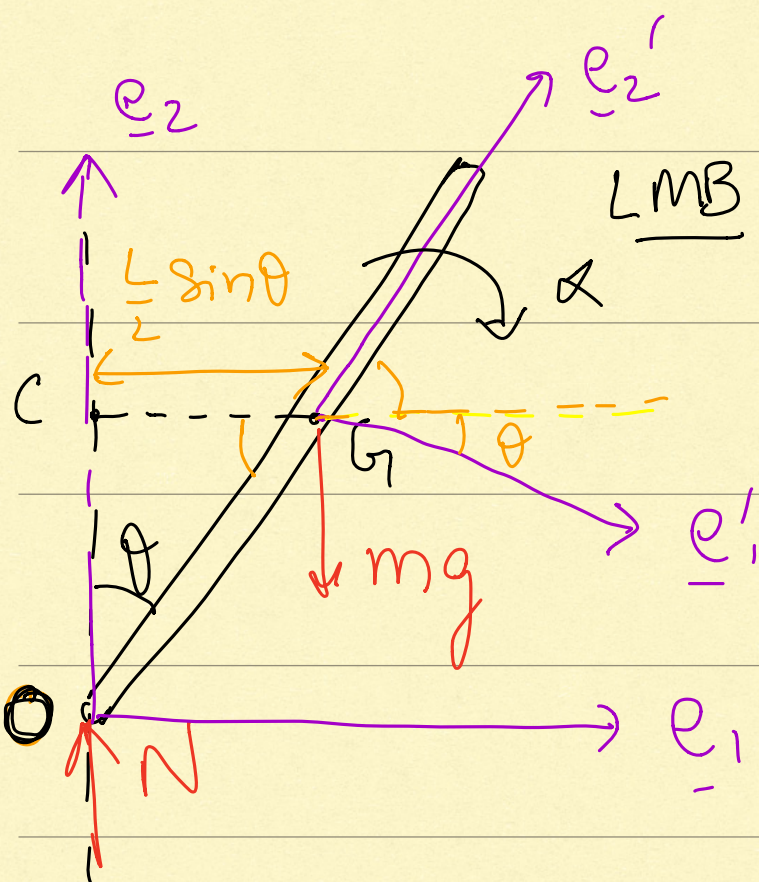


Determine the
normal reaction and
the angular acceleration
immediately after the
release of the rod.
↳ from rest

$$\underline{\omega} = 0$$



$$\underline{\Sigma F} = m \underline{a}^G$$

$$\uparrow (N - mg) \underline{e}_2$$

AMB

$$\underline{M}_C = \underline{r}^{G/C} \times m \underline{a}^G + \underline{I}_3^G \underline{\alpha}$$

↑
total Moment
about C

$$\underline{M}_c = - \left(mg \frac{L}{2} \sin \theta \right) \underline{e}_3$$

$$I_3^G = \frac{1}{12} mL^2$$

$$\underline{\alpha} = -\alpha \underline{e}_3, \quad \underline{\omega} = \underline{0}$$

$$\underline{r}_{G/O} = \frac{L}{2} \sin \theta \underline{e}_1$$

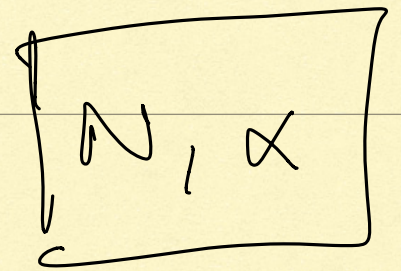
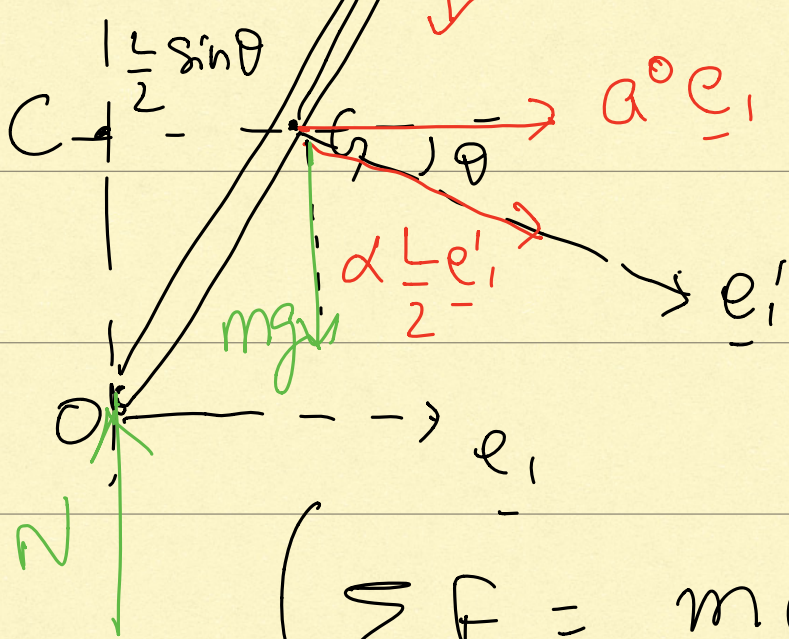
$$\underline{a}^G = \underline{a}^O + \cancel{\underline{\omega} \times (\underline{\omega} \times \underline{r}_{G/O})} + \underline{\alpha} \times \underline{r}_{G/O}$$

\swarrow \searrow
 $\underline{a}^O \underline{e}_1$ \downarrow \searrow
 $- \alpha \underline{e}_3$ $\frac{L}{2} \underline{e}_2'$

$$\underline{e}_3' = \underline{e}_3$$

$$= \underline{a}^O \underline{e}_1 + \alpha \frac{L}{2} \underline{e}_2' \quad \left. \vphantom{\frac{L}{2} \underline{e}_2'} \right\} \underline{a}^G$$

$\nearrow \underline{e}_2'$
 \swarrow
 $\underline{\alpha} = -\alpha \underline{e}_3$



$$\left(\sum \underline{F} = m \underline{a}^G \right) \cdot \underline{e}_2$$

$$N - mg = -m \alpha \frac{L}{2} \sin \theta \quad \text{--- (1)}$$

$(\underline{e}'_1 \cdot \underline{e}_2 = -\sin \theta)$

$$\left(\underline{M}_C = \underline{r}_{G/C} \times \underline{a}^G + \underline{I}_3^G \alpha \right) \cdot \underline{e}_3$$

$$-mg \frac{L}{2} \sin \theta = - \left(m \alpha \frac{L}{2} \sin \theta \right) \frac{L}{2} \sin \theta$$

$$= - \frac{1}{12} m L^2 \alpha$$

(2)

$$\Rightarrow \alpha = \frac{2g \sin \theta}{L \left(\frac{1}{3} + \sin^2 \theta \right)}$$

put in (1)

$$N = \frac{mg}{1 + 3\sin^2\theta}$$