

➤ Also, for a *two-pole system*, the *phase reaches -180° only when the frequency becomes infinite (mathematically)*

⇒ *There is no physically achievable frequency when this can happen*

⇒ *Unconditional Stability*

- *System With Three (or More) Poles:*

➤ *Actual mathematical analysis quite tedious*

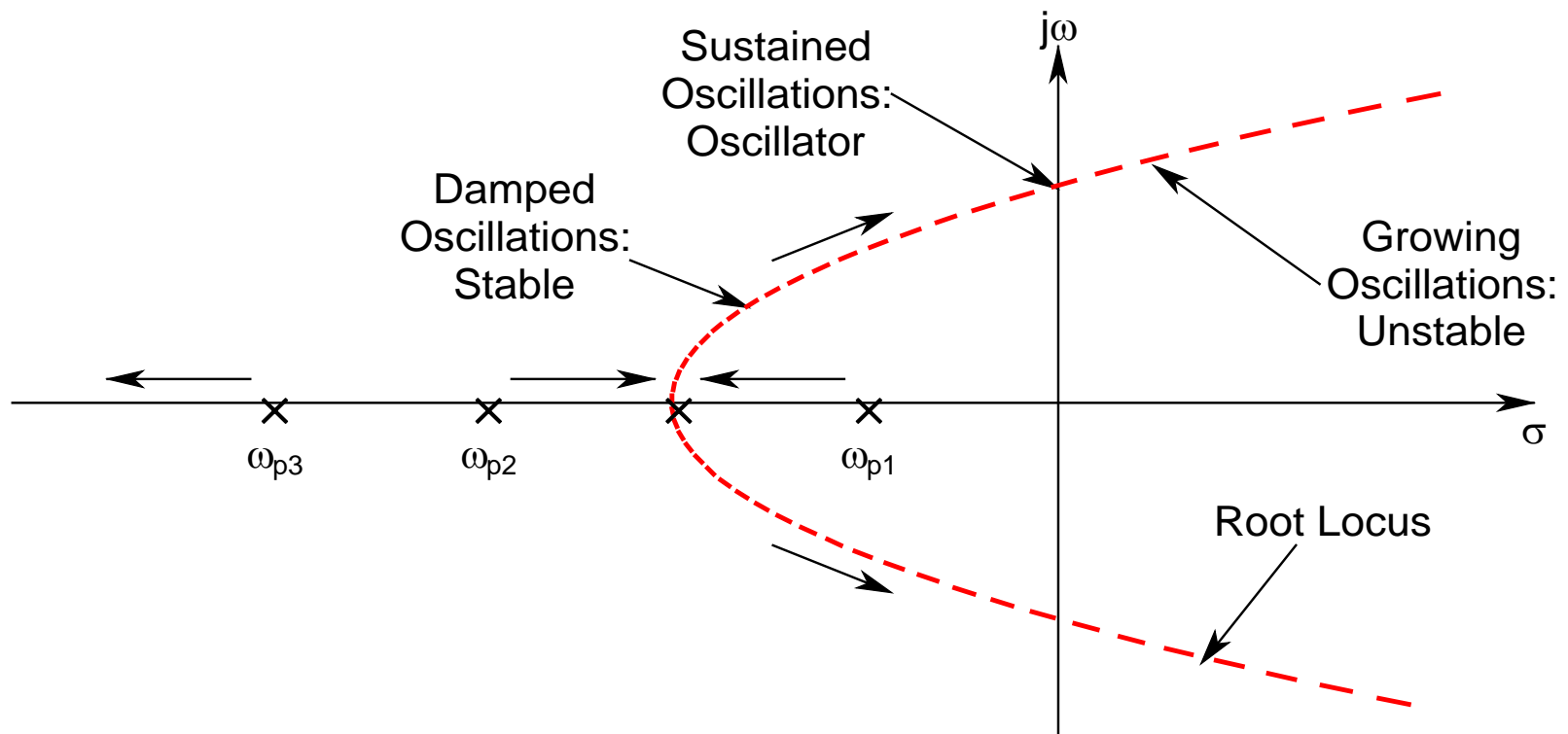
➤ It can be shown that as the *amount of feedback (D) is increased:*

- *The highest frequency pole (ω_{p3}) moves outward along the $-\sigma$ -axis*

- *The other two poles (ω_{p1} and ω_{p2}) move towards each other (similar to a two-pole system)*
- *As D is increased further, these two poles eventually merge, and then start having imaginary components*
- *Their real part also keeps on changing with D , keeping the nature of complex conjugacy intact, and moves right in the s-plane*
- *The path traced out by these poles is known as the root locus*
- *For a particular value of D , this root locus intersects the imaginary axis of the s-plane at two symmetric points*

- *Under this condition, sustained sinusoidal oscillation can be achieved, since it now has a complex conjugate pair of poles without any real part (ω_{p3} will be so large that it will be inconsequential)*
- *With further increase in D , the root locus enters the RHP with the poles now having positive real part*
 - \Rightarrow *Potentially dangerous situation in terms of stability*
- *In terms of phase, the total can be -270°*
 - \Rightarrow *There exists a particular value of f , for which the phase will become -180°*

- *Under this condition, if the magnitude of the loop gain is exactly unity, then the system will break out into spontaneous oscillation, however, the amplitude will be controlled*
 \Rightarrow *Sustained sinusoidal oscillation*
- *This particular value of f is known as the critical feedback factor (f_{crit}) for oscillation*
 - ❖ For $f < f_{crit}$, the *system will be stable*
 - ❖ For $f > f_{crit}$, the *system will be unstable*
- Thus, the system is *NOT Unconditionally Stable*, but *stable only till a specific value of f*
 - ❖ Known as *Conditionally Stable System*



Root Locus of the Poles of a Three-Pole System as D is Increased

Stability Study Using Bode Plot

- The *most convenient* and the *most useful*
- *Recall: Single- and Two-Pole Systems are unconditionally stable*
- Consider a *Three-Pole System*, with the *pole frequencies* at ω_1 , ω_2 , and ω_3 , with $\omega_3 = 100\omega_2$, and $\omega_2 > 100\omega_1$
- *Note: $A = L$ if $f = 1$ (100% feedback)*
- Refer to the next slide (*Bode Plot*)

