

- *Some Definitions:*

- *Loop Gain* (L) = fA

- *Return Difference* (D) = 1 + L

- *Amount of Feedback* (N) = $20 \log_{10} D$ (dB)

- *Positive Feedback:*

- *Output fed back to the input through the mixer, but now with a positive sign*

- ⇒ *Feedback signal gets added to the input signal*

➤ *Show that under this condition:*

$$A_f(j\omega) = \frac{A(j\omega)}{1 - f(j\omega)A(j\omega)} = \frac{A(j\omega)}{1 - L(j\omega)}$$

➤ This is a *general expression*, taking both A and f as *frequency dependent*

➤ Note: As $L \rightarrow 1$, $A_f \rightarrow \infty$

- *Implies that output is possible even without any input*
- This is the *basic principle of oscillation*

- *Conditions for Oscillation:*

- Barkhausen's Criteria:*

- *L becoming unity implies that the signal has completely regenerated itself while traversing once through the loop*

- ⇒ *There is no need for any input any more, since the loop has become self-sustained!*

- *Since A and f are frequency dependent, hence, there may exist a frequency ω_0 , at which:*

$$L(j\omega_0) = f(j\omega_0)A(j\omega_0) = 1$$

- Since ω_0 is a *particular frequency*, for which *this condition holds*, hence, the output will be a *pure sinusoid* of *this frequency*
 - Similar to *picking out* f_0 only from a *Fourier Spectrum*
 - This phenomenon is known as *Sinusoidal Oscillation*
- German physicist *Heinrich Georg Barkhausen* summed this up by *two conditions*, came to be known as the *Barkhausen's Criteria*:
 1. $|L(j\omega_0)| = 1$ and
 2. $\angle L(j\omega_0) = 0^\circ$

➤ ***Barkhausen's Criteria in words:***

For a feedback system to oscillate, the magnitude of the loop gain must at least be unity, and the total phase shift around the loop should be 0° or 360°

➤ *If these criteria are satisfied exactly, then the oscillations would go on forever, and can be stopped only by shutting the power off for the system*

➤ However, for *practical circuits*, the *exact conditions for oscillations* are *very difficult to achieve*

- If $|L|$ becomes *slightly less than 1*, but $\angle L$ is *exactly 0°* , then with *each pass around the loop*, the *amplitude of oscillation* would keep on *going down*, and eventually, it will *die down* on its own
 - Thus, *under this condition*, *sustained sinusoidal oscillation won't be achieved*
- On the other hand, if $|L|$ becomes *slightly larger than unity*, but $\angle L$ is *exactly 0°* , then with *each pass around the loop*, the *amplitude* of the signal will *keep on growing*
 - Will eventually *get limited* by the *nonlinearities* present in the circuit

Stability

- *2 Types of Systems:*
 - *Stable*
 - *Unstable*
- *Stable System:*
 - *Any transient disturbance would result in a response that will die down with time*
 - *The system will be able to get rid of the disturbance on its own*

- *Unstable System:*

- *Any transient disturbance would result in a response that will persist or even blow up with time*
 - *Eventually gets limited by the nonlinearities of the system*
- *Positive feedback systems are inherently unstable*
 - *They are designed as such, e.g., oscillators*
- *Negative feedback systems are inherently stable*