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```
clc; clear all; close all;
```

Storing values of given parameters

```
m = 0.23; M = 0.5; l = 0.321; g = 9.8;
a = 1/(m+M);
A = [ 0 1 0 0; 3*g/(4*l-3*m*l*a) 0 0 0; 0 0 0 1; -3*m*a*g/(4-3*m*a) 0
      0 0];
B = [0; 3*a/(3*m*l*a-4*l); 0; 4*a/(4-3*m*a)];
C = [1 0 0 0];
```

Defining the open-loop transfer function

```
s = tf('s');
gs = C*(inv(s*eye(4)-A))*B
```

```
gs =
```

```
          -4.191
-----
s^2 - 1.51e-14 s - 29.98
```

Continuous-time transfer function.

Finding parameters and dominant poles by given specifications

```
Mp = 0.2; set_time = 1;
% Given Peak overshoot and settling time
zeta = sqrt((log(Mp)^2/(pi^2+(log(Mp))^2)))
% Mp = exp((-pi*zeta)/(sqrt(1-zeta^2)))
w_n = 4/(set_time*zeta)
% settling time = 4/(w_n*zeta)
d_p1 = -w_n*zeta + j*w_n*sqrt(1-zeta^2)
% desired dominant pole 1
```

```
d_p2 = -w_n*zeta - j*w_n*sqrt(1-zeta^2)
      % desired dominant pole 2
```

```
zeta =

    0.4559
```

```
w_n =

    8.7729
```

```
d_p1 =

   -4.0000 + 7.8079i
```

```
d_p2 =

   -4.0000 - 7.8079i
```

Angle contribution by desired dominant poles and compensator

```
P = pole(gs); Z = zero(gs);
      % to store the open-loop poles and zeroes respectively
mm = length(Z); n = length(P);
      % to store the number of zeroes and poles respectively
% angle contribution = (sum of angles made with the open-loop zeroes)
- (sum of angles made with the open-loop poles)
phi = sum(angle(d_p1-Z)) - sum(angle(d_p1-P));
      % phi is in radians
phi*180/pi
      % Printing phi (in degrees)

ans =

   -219.8095
```

Designing Lead Compensator

```
cz = -5.0;
      % choosing appropriate compensator zero
phi = phi + angle(d_p1-cz);
      % adding angle made by the dominant pole with the compensator
      zero
```

```

cp_angle = phi + pi;
    % angle made by the dominant pole with the compensator pole
cp = real(d_p1)-(imag(d_p1)/tan(cp_angle))
    % to find the compensator pole (considering cp_angle is +ve)

cs = tf((s-cz)/(s-cp))
    % compensator (without K)
ls = cs*gs
    % loop transfer function (without K)
K = real(evalfr(-1/ls, d_p1))
    % to find the value of gain in compensator, K = 1/|L(s)|

ss = feedback(K*ls, 1)
    % The overall closed loop system thus formed

pole(ss)
    % Closed loops poles of the combined system
Gain = evalfr(ss, 0)
    % Feed Forward gain
figure(1);
stepplot(ss/Gain);
    % to plot the step response
stepinfo(ss/Gain)
    % to get the information of the step response

cp =

    -12.4047

cs =

    s + 5
    -----
    s + 12.4

Continuous-time transfer function.

ls =

    -4.191 s - 20.95
    -----
    s^3 + 12.4 s^2 - 29.98 s - 371.9

Continuous-time transfer function.

K =

    -33.9263

```

`ss =`

$$\frac{142.2 s + 710.9}{s^3 + 12.4 s^2 + 112.2 s + 339}$$

Continuous-time transfer function.

`ans =`

`-4.0000 + 7.8079i`
`-4.0000 - 7.8079i`
`-4.4047 + 0.0000i`

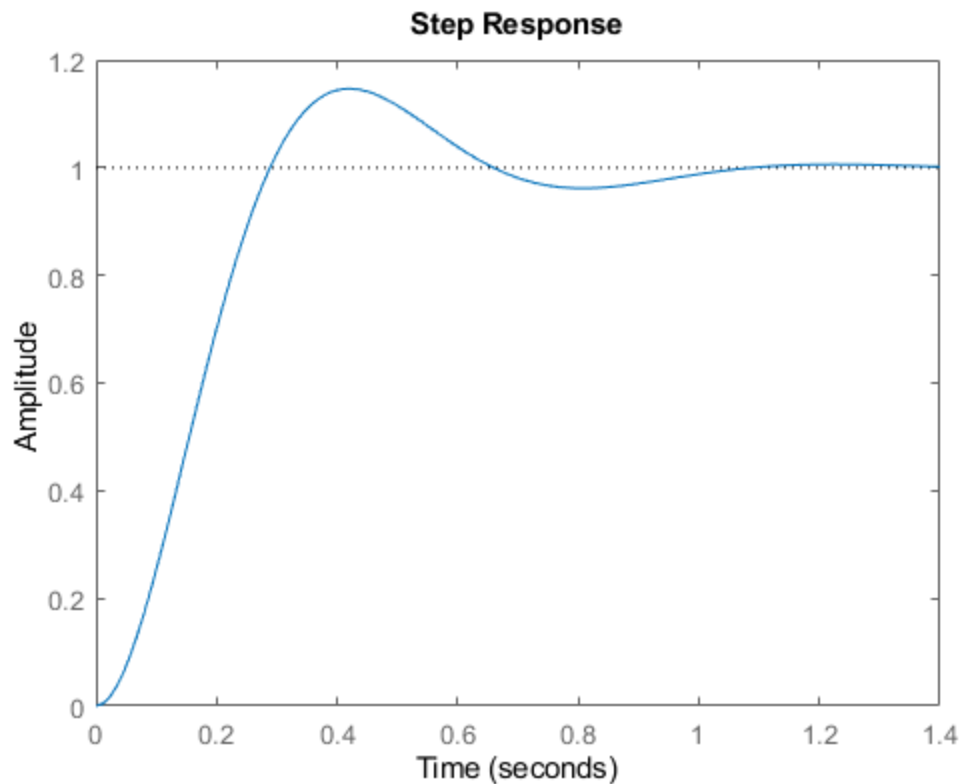
`Gain =`

`2.0971`

`ans =`

struct with fields:

`RiseTime: 0.1946`
`SettlingTime: 0.9548`
`SettlingMin: 0.9352`
`SettlingMax: 1.1465`
`Overshoot: 14.6460`
`Undershoot: 0`
`Peak: 1.1465`
`PeakTime: 0.4260`



Root Locus of the compensated system

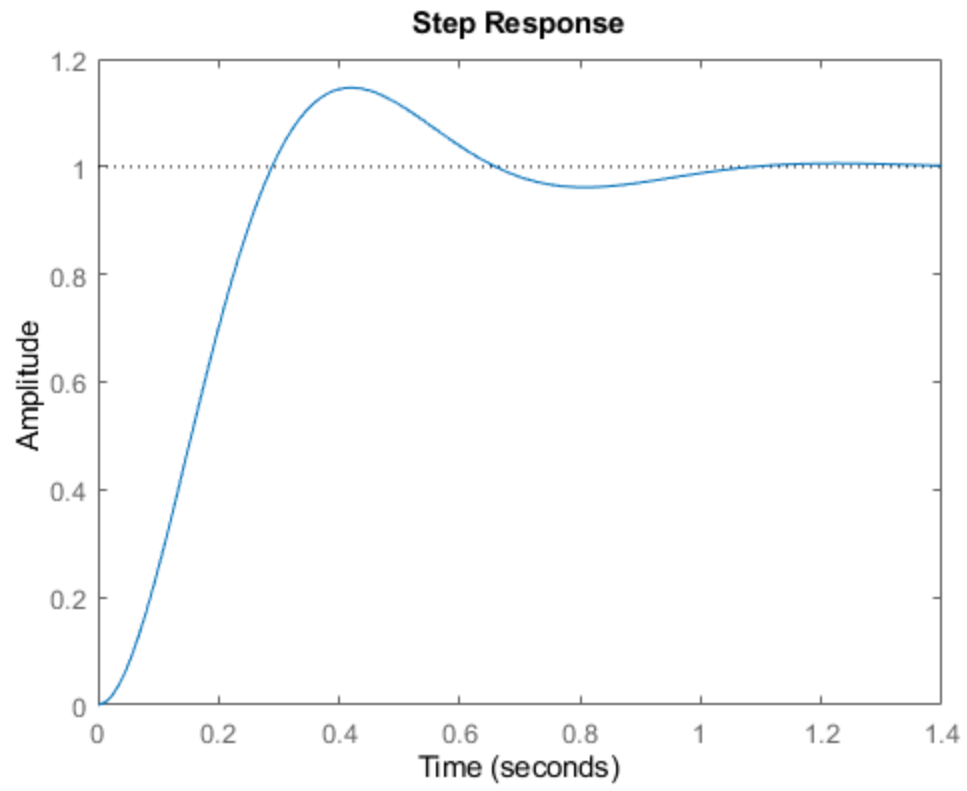
```
figure(2);
rlocus(-ls);
grid on;
delta = (length(pole(ls))-length(zero(ls)));
    % number of poles - number of zeroes
% Centroid
centroid = (sum(pole(ls))-sum(zero(ls)))/delta
    % centroid = {sum of poles - sum of zeroes}/(number of poles -
    number of zeroes)
% Asymptote angles
for i=1:delta
    asym(i)=(2*(i-1)+1)*180/delta;
end
asym

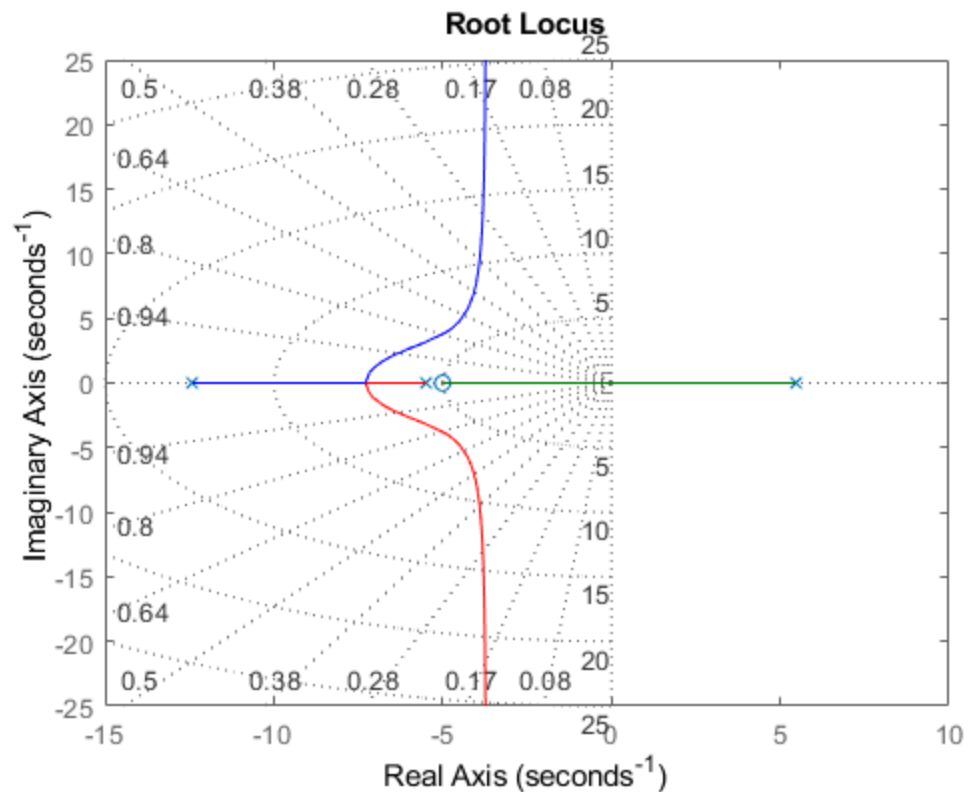
centroid =

    -3.7023

asym =

    90    270
```





Section (c) - Runge Kutta Method

```
Kr = [-9.5818 -1.2973 -0.0974 -0.2435];
f = A - B*Kr;

% Part (a)
h = 0.1;
x = zeros(4,101);
time = zeros(101);
x(:,1) = [1; 0; 1; 0];
time(1)=0;
for i=1:100
    m0 = f*x(:,i);
    m1 = f*(x(:,i)+h*m0/2);
    m2 = f*(x(:,i)+h*m1/2);
    m3 = f*(x(:,i)+h*m2);
    x(:,i+1) = x(:,i) + h*(m0+2*m1+2*m2+m3)/6;
    time(i+1)=time(i)+h;
end
figure(3);
for i=1:4
    plot(time, x(i,:))
    hold on;
end
hold off;
```

```

legend('x1', 'x2', 'x3', 'x4');
title('Response with Sampling Rate h=0.1');
ylabel('Magnitude');
xlabel('Time')

% Part (b)
h = 1;
x = zeros(4,11);
time = zeros(11);
x(:,1) = [1; 0; 1; 0];
time(1)=0;
for i=1:10
    m0 = f*x(:,i);
    m1 = f*(x(:,i)+h*m0/2);
    m2 = f*(x(:,i)+h*m1/2);
    m3 = f*(x(:,i)+h*m2);
    x(:,i+1) = x(:,i) + h*(m0+2*m1+2*m2+m3)/6;
    time(i+1)=time(i)+h;
end
figure(4);
for i=1:4
    plot(time, x(i,:))
    hold on;
end
hold off;
legend('x1', 'x2', 'x3', 'x4');
title('Response with Sampling Rate h=1');
ylabel('Magnitude');
xlabel('Time')

%Sampling rate increased further to check if the response goes
unbounded
h = 5;
x = zeros(4,11);
time = zeros(11);
x(:,1) = [1; 0; 1; 0];
time(1)=0;
for i=1:10
    m0 = f*x(:,i);
    m1 = f*(x(:,i)+h*m0/2);
    m2 = f*(x(:,i)+h*m1/2);
    m3 = f*(x(:,i)+h*m2);
    x(:,i+1) = x(:,i) + h*(m0+2*m1+2*m2+m3)/6;
    time(i+1)=time(i)+h;
end
figure(5);
for i=1:4
    plot(time, x(i,:))
    hold on;
end
hold off;
legend('x1', 'x2', 'x3', 'x4');
title('Response with Sampling Rate h=5');
ylabel('Magnitude');

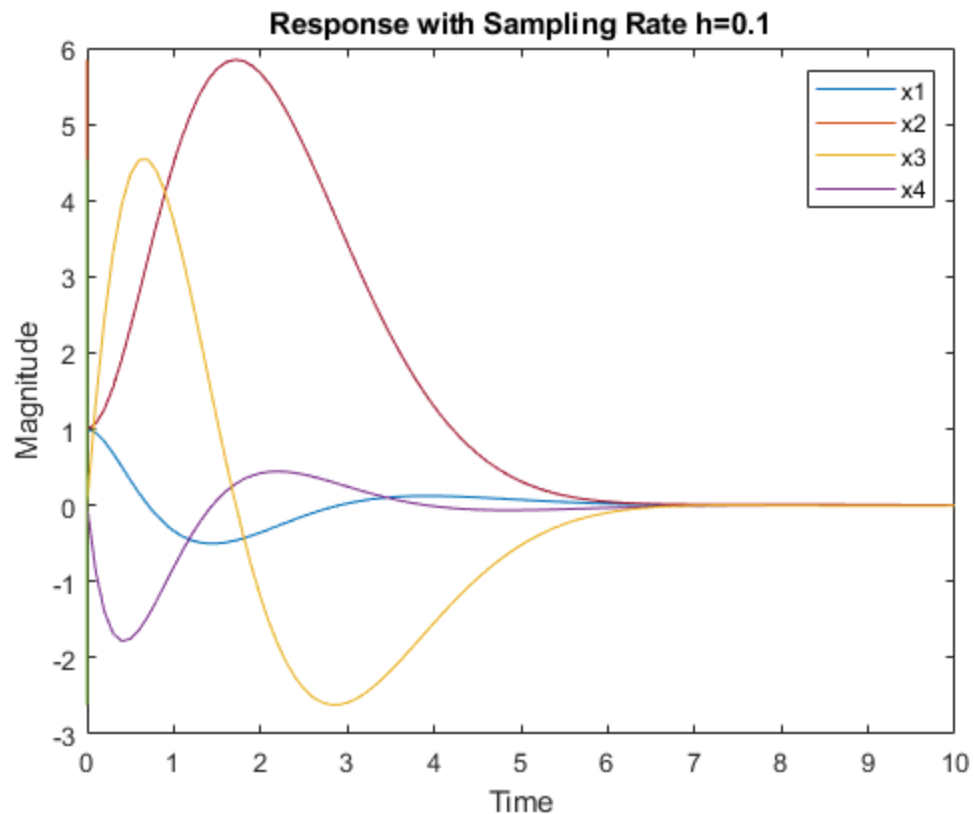
```

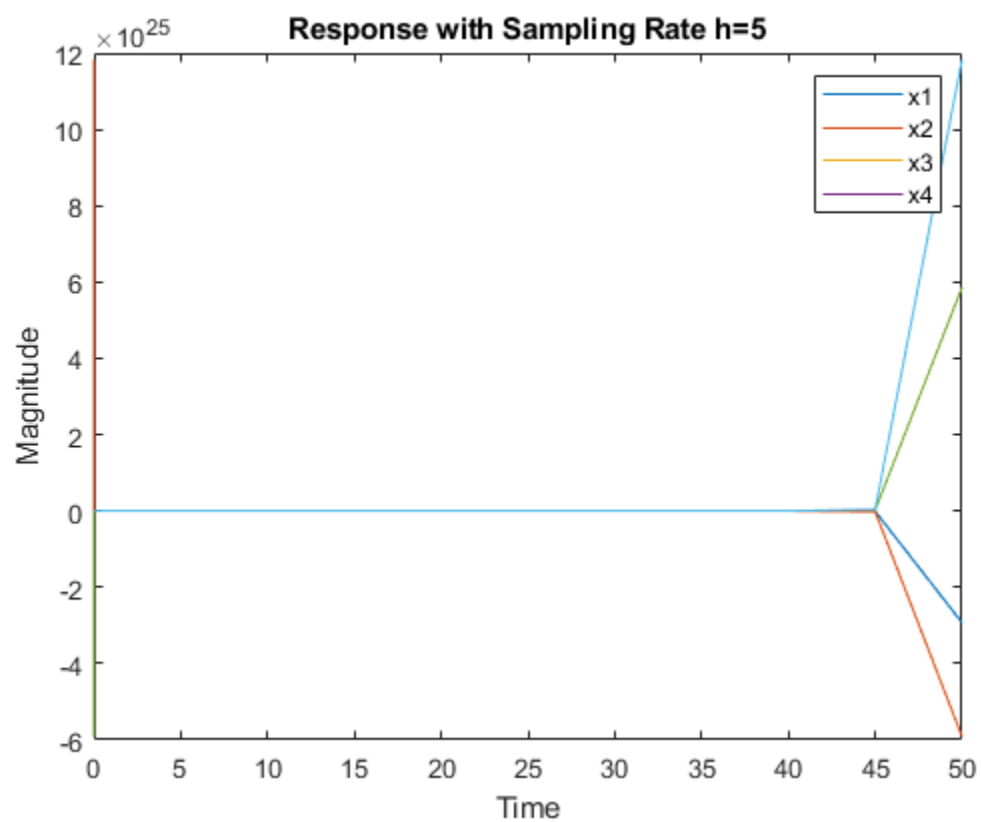
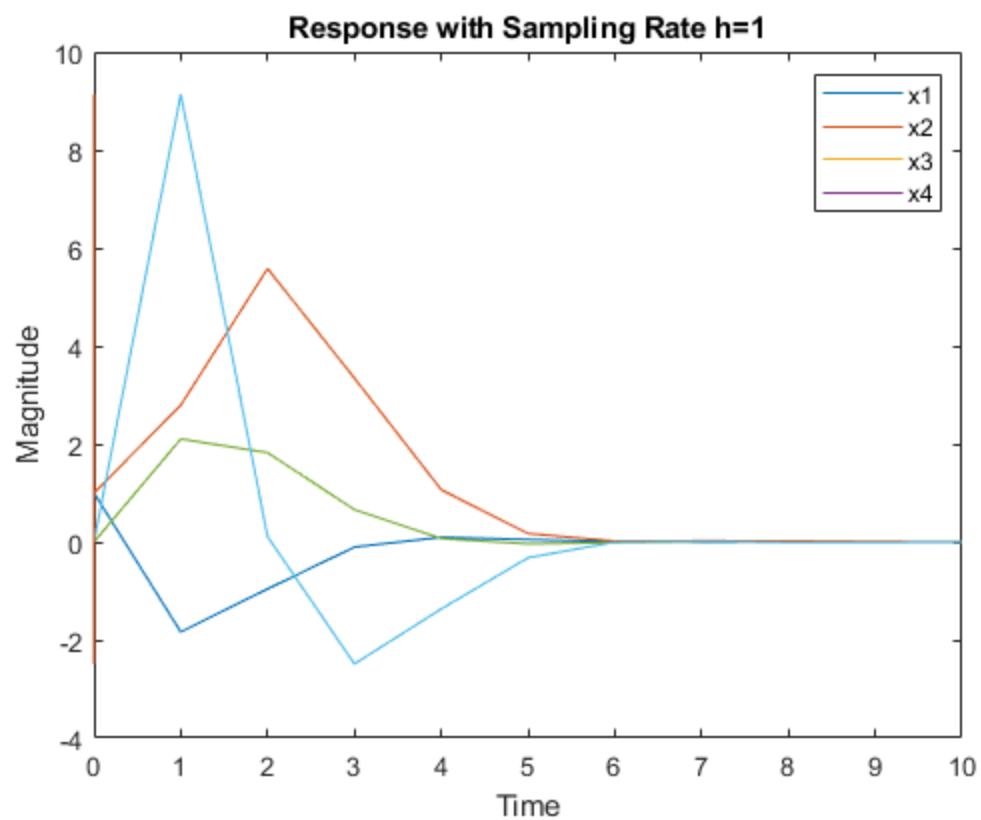
```

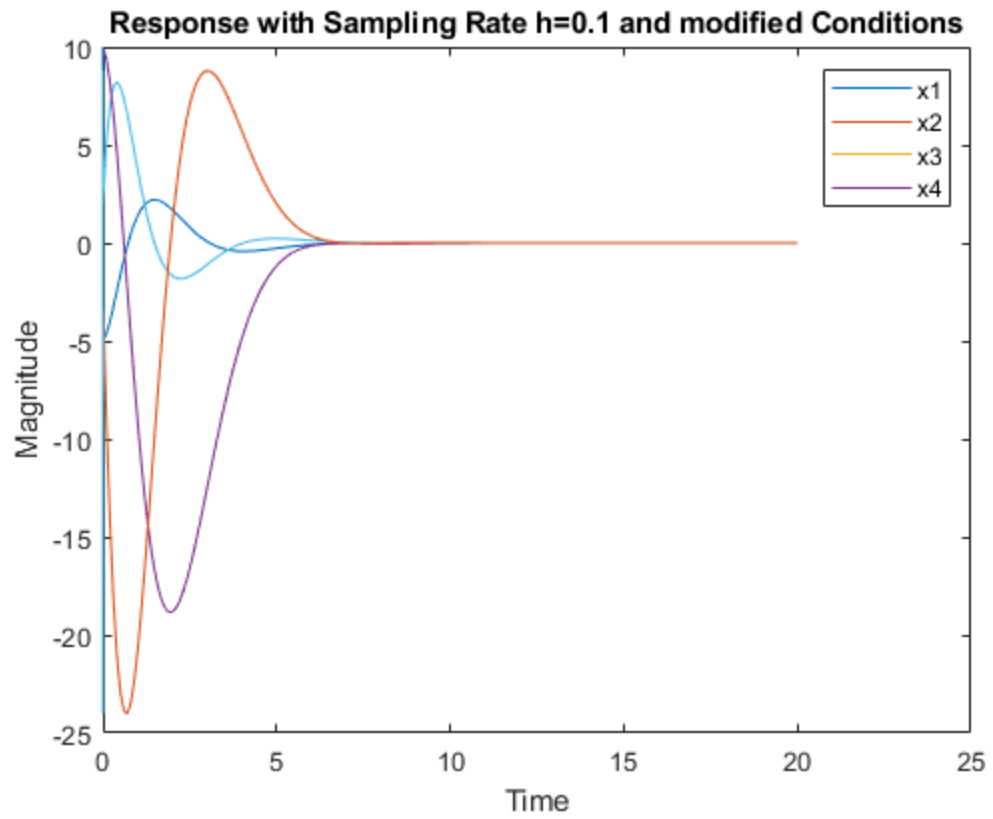
xlabel('Time')

% Part (c)
h = 0.1;
x = zeros(4,201);
time = zeros(201);
x(:,1) = [-5; 2; 10; -3];
time(1)=0;
for i=1:200
    m0 = f*x(:,i);
    m1 = f*(x(:,i)+h*m0/2);
    m2 = f*(x(:,i)+h*m1/2);
    m3 = f*(x(:,i)+h*m2);
    x(:,i+1) = x(:,i) + h*(m0+2*m1+2*m2+m3)/6;
    time(i+1)=time(i)+h;
end
figure(6);
for i=1:4
    plot(time, x(i,:))
    hold on;
end
hold off;
legend('x1', 'x2', 'x3', 'x4');
title('Response with Sampling Rate h=0.1 and modified Conditions');
ylabel('Magnitude');
xlabel('Time')

```







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