

- ***npn Ratioed CM:***

- *Q_1 - Q_2 matched pair*

- *Neglecting all I_B , $I_{E1} = I_{C1} = I_{REF}$, and $I_{E2} = I_{C2} = I_0$*

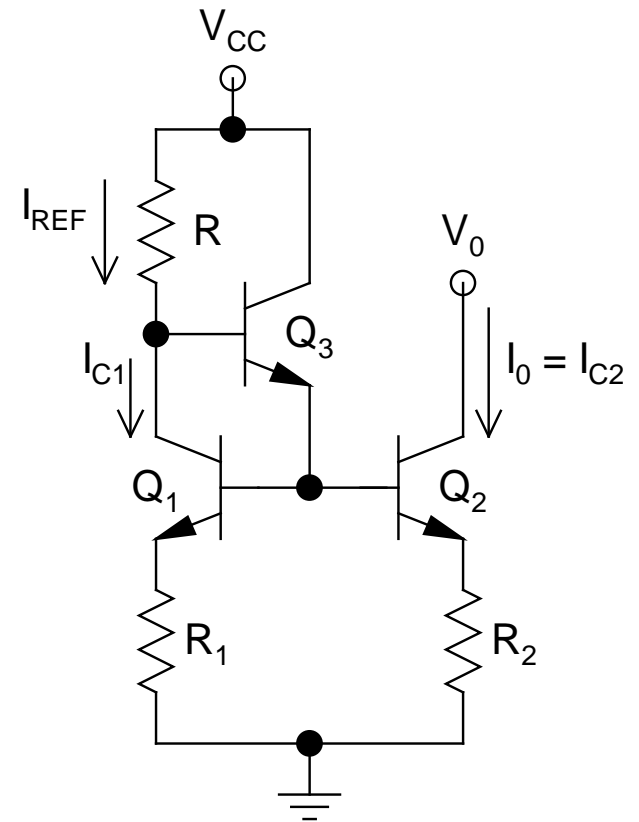
- $I_{REF} = (V_{CC} - 2V_{BE})/(R + R_1)$

- ***KVL around Q_1 - Q_2 BE loop:***

$$V_{BE1} + I_{REF}R_1 = V_{BE2} + I_0R_2$$

$$\Rightarrow I_0 = (I_{REF}R_1 + \Delta V_{BE})/R_2$$

$$\begin{aligned}\Delta V_{BE} &= V_{BE1} - V_{BE2} \\ &= V_T \ln(I_{REF}/I_0)\end{aligned}$$



➤ *Note the \ln dependence:*

- *For $I_{REF}/I_0 = 2$, $\Delta V_{BE} = 18 \text{ mV}$*

- *For $I_{REF}/I_0 = 10$, $\Delta V_{BE} = 60 \text{ mV}$*

$\Rightarrow \Delta V_{BE}$ can be neglected if $I_{REF}R_1 > 10\Delta V_{BE}$

$\Rightarrow I_0 = (R_1/R_2)I_{REF}$ (*Ratioed Mirror*)

➤ *Thus, by tinkering R_1 and R_2 , any ratio between I_0 and I_{REF} can be obtained*

- *Tremendous advantage*

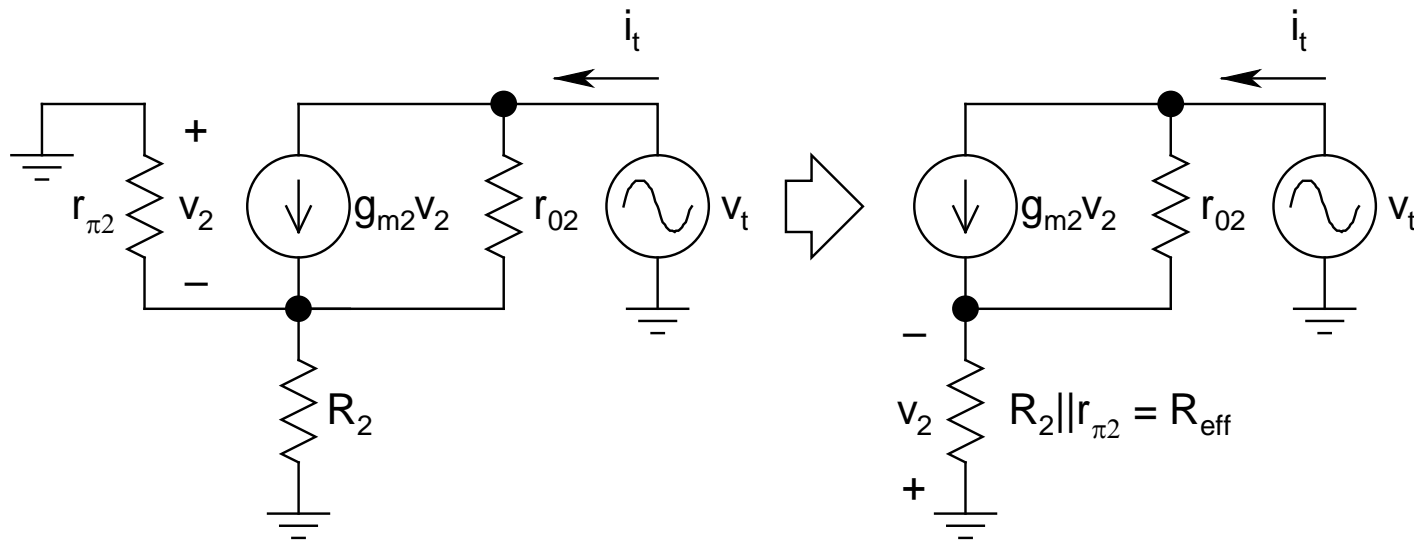
 - ❖ *Widely used*

➤ *By inspection:*

$$V_{0,\min} = V_{CE2}(\text{SS}) + I_0 R_2 = 0.2 + I_0 R_2$$

➤ **Calculation of R_0 :**

- *Golden Rule can't be used since emitter of Q_2 is not grounded (R_2 present there)*
- *Needs analysis*
 - ⇒ *Leads to a module that is frequently encountered*
- *Base of Q_1 - Q_2 at a fixed DC potential ⇒ **ac ground***



$$\begin{aligned} i_t &= g_{m2} v_2 + (v_t + v_2)/r_{02} \\ &= v_t/r_{02} + (g_{m2} + 1/r_{02}) v_2 \simeq v_t/r_{02} + g_{m2} v_2 \end{aligned}$$

$$v_2 = -i_t R_{\text{eff}}$$

$$\Rightarrow i_t = v_t/r_{02} - g_{m2} R_{\text{eff}} i_t$$

$$\Rightarrow R_0 = v_t/i_t = r_{02}(1 + g_{m2} R_{\text{eff}})$$

➤ This is a ***Golden Equation***, which would be *used frequently*

- *Carefully note the topology that produces this result*

➤ ***Exercise***: *Reverse v_2 and show that the expression for R_0 remains invariant*