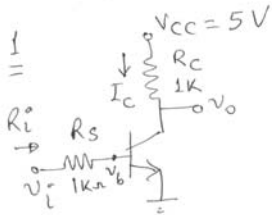


EE 210 Solⁿ to HA #8

(1)



$$I_C = 1 \text{ mA} \quad g_m = \frac{I_C}{V_T} = \frac{1}{26} \text{ V}^{-1} \quad A_{v/\text{max}} = -g_m R_C = -38.46$$

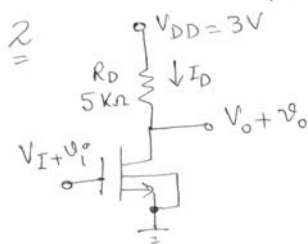
$$\text{Actual gain } A_v = -32 = -g_m (r_o \parallel R_C) \Rightarrow r_o \approx 5 \text{ k}\Omega$$

$$r_o = \frac{V_A}{I_C} \Rightarrow V_A = 5 \text{ V} \Rightarrow \text{Indicative of severe Early Effect.}$$

$$\text{With } R_S = 1 \text{ k}\Omega, \text{ using Generic Ckt. approach, } \frac{v_o}{v_b} = -32,$$

$$\& \frac{v_b}{v_i} = \frac{g_{mR}}{g_{mR} + R_S} \quad \text{with } g_{mR} \approx \beta g_m \approx \beta \frac{V_T}{I_C} = 2.6 \text{ k}\Omega \Rightarrow \frac{v_o}{v_i} = \frac{2.6}{3.6} = 0.72$$

$$\therefore \frac{v_o}{v_i} = \frac{v_o}{v_b} \times \frac{v_b}{v_i} = -32 \times 0.72 = -23, \& R_i = R_S + g_{mR} = 3.6 \text{ k}\Omega$$



Device operates at boundary betⁿ saturation & non-sat.

$$\therefore V_o = V_{DS} = V_{DS,\text{sat}} = V_{GS} - V_{TN} = \Delta V, \& V_{TN} = V_{TN0},$$

\therefore no body effect (B & S tied together). No CLM.

$$\Rightarrow I_D = \frac{K_n'}{2} \frac{W}{L} \Delta V^2 \quad \& \Delta V = V_{DD} - I_D R_D.$$

$$\text{Resulting quadratic eqn: } 5\Delta V^2 + \Delta V - 3 = 0 \Rightarrow \Delta V = \frac{0.68 \text{ V}}{\text{or } -0.88 \text{ V}}$$

$$V_{DS} = -0.88 \text{ V is absurd} \Rightarrow V_{DS} = 0.68 \text{ V} = V_{GS} - V_{TN0}$$

$$\Rightarrow V_{GS} = V_I = 1.28 \text{ V} \quad \& I_D = 462.4 \mu\text{A} \quad \& V_o = 0.68 \text{ V}$$

$$g_m = \sqrt{2K_n I_D} = 1.36 \text{ mS} \quad (\text{or } g_m = K_n \Delta V = 1.36 \text{ mS} \rightarrow \text{both should give same values})$$

$$\therefore A_v = -g_m R_D = -6.8 \Rightarrow \text{This is the max. gain attainable from this ckt.}$$

$$\text{for unity gain, } |g_m R_D| = 1 \Rightarrow g_m = \frac{1}{R_D} = 0.2 \text{ mS} = K_n (V_{GS} - V_{TN0})$$

$$\Rightarrow V_{GS} = V_I = 0.7 \text{ V}, I_D = 10 \mu\text{A}, \& V_o = V_{DS} = V_{DD} - I_D R_D = 2.95 \text{ V}$$

$$\therefore V_{DS} > V_{GS} - V_{TN}, \text{ the device is indeed operating in the saturation region.}$$

$$3 \quad g_m = \sqrt{2K_n I_D} = 282.84 \mu\text{S} \Rightarrow A_v = -g_m R_D = -2.83, R_i \rightarrow \infty, R_o = 10 \text{ k}\Omega = R_D.$$

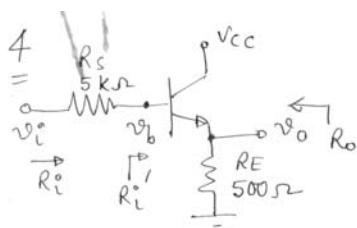
$$\text{Now, with } \lambda = 0.2 \text{ V}^{-1} \& \text{ assuming } \lambda V_{DS} \ll 1, \text{ with } I_D = 100 \mu\text{A}, g_m \text{ stays same. But } r_o = \frac{1}{\lambda I_D} = 50 \text{ k}\Omega \Rightarrow \text{New } A_v = -g_m (r_o \parallel R_D) = -2.36 \text{ (Reduction).}$$

$$R_i \rightarrow \infty, \& R_o = r_o \parallel R_D = 8.33 \text{ k}\Omega. \text{ For the device, } \Delta V = \sqrt{\frac{2I_D}{K_n' \frac{W}{L}}} = 0.707 \text{ V}$$

$$\therefore \text{Max. gain attainable from this ckt, } A_v = -\frac{2}{\lambda \times \Delta V} = -14.14$$

$$\text{Transconductance to drain current ratio } g_m/I_D = \frac{2}{\Delta V} = 2.83 \text{ V}^{-1}$$

$$1/V_T \text{ at room temp} = 38.46 \text{ V}^{-1}. \therefore \text{MOSFETs have much lower } g_m/I_D.$$



$$g_{mE} \approx \frac{V_T}{I_C} = 26 \Omega \quad r_{\pi} = \beta g_{mE} = 2.6 \text{ k}\Omega \quad (2)$$

$$R_i' = R_s + g_{mE} + (\beta + 1) R_E = 5 \text{ k} + 2.6 \text{ k} + 101 \times 500 \Omega = 58.1 \text{ k}$$

$$R_o = R_E \parallel (g_{mE} + \frac{R_s}{\beta + 1}) = 500 \parallel (26 + \frac{5 \text{ k}}{101}) = 65.6 \Omega$$

$$\frac{v_o}{v_b} = \frac{R_E}{g_{mE} + R_E} = \frac{500}{500 + 26} = 0.9506 \quad R_i' = g_{mE} + (\beta + 1) R_E = 53.1 \text{ k}$$

$$\Rightarrow \frac{v_b}{v_i} = \frac{R_i'}{R_i' + R_s} = \frac{53.1 \text{ k}}{58.1 \text{ k}} = 0.9139 \Rightarrow A_v = \frac{v_o}{v_b} \times \frac{v_b}{v_i} = 0.8688 \approx 0.87$$

5 i) Ignoring body effect & with $R \rightarrow \infty$, $I_D = 200 \mu\text{A}$, $V_{TN} = V_{TN0} = 0.7 \text{ V}$
 $I_D = \frac{K_n'}{2} \frac{W}{L} (V_{GS} - V_{TN0})^2 = 200 \mu\text{A} \Rightarrow V_{GS} - V_{TN0} = 1 \text{ V} \Rightarrow V_{GS} = 1.7 \text{ V}$, $V_o = 3 - V_{GS}$
 $= 1.3 \text{ V}$, & $V_{DS} = 5 - V_o = 3.7 \text{ V}$. $V_{DS} > (V_{GS} - V_T) \rightarrow \text{Saturated}$.

$$A_v = \frac{g_m R_s}{1 + (g_m + g_{mb}) R_s} \quad \text{with } R_s \rightarrow \infty, g_{mb} \text{ does not exist} \Rightarrow \boxed{A_v \rightarrow 1}$$

ii) $V_{GS} = -V_o$, $V_{TN} = V_{TN0} + \gamma(\sqrt{2\phi_F + V_o} - \sqrt{2\phi_F})$ & $I_D = 200 \mu\text{A}$.
 Easiest way is to iterate these simultaneous eqns, with initial guess $V_o = 1.3 \text{ V}$,
 which is the answer for part i). After a few iterations, it converges to

$$V_o = 1.09 \text{ V}, V_{TN} = 0.91 \text{ V}, V_{GS} = 1.91 \text{ V}, V_{DS} = 3.91 \text{ V}. \quad (\text{Saturated})$$

$$\chi = \frac{\gamma}{2\sqrt{2\phi_F + V_o}} = 0.154 \quad A_v = \frac{g_m R_s}{1 + (g_m + g_{mb}) R_s} \approx \frac{g_m}{g_m + g_{mb}} = \frac{1}{1 + \chi} = 0.867 \quad (\text{Reduction})$$

$$6 \text{ i) } R \text{ is finite } (100 \text{ k}\Omega) \Rightarrow I_D = 200 \mu\text{A} + \frac{V_o}{100 \text{ k}} \quad V_{GS} - V_{TN} = \sqrt{\frac{2 I_D}{K_n' \frac{W}{L}}}$$

$$V_o = 3 - V_{GS} \quad V_{TN} = V_{TN0} + \gamma(\sqrt{2\phi_F + V_o} - \sqrt{2\phi_F})$$

This set of eqns. need to be iterated with initial guess $V_o = 1.09 \text{ V}$ (p.5, p.ii).
 After a few iterations, converges to $V_o = 1.067 \text{ V}$, $I_D = 210.67 \mu\text{A}$, $V_{GS} = 1.933 \text{ V}$,
 $V_{TN} = 0.907 \text{ V}$, & $V_{DS} = 3.933 \text{ V}$ (Saturated). $\chi = 0.155$

$$A_v = \frac{g_m R_s}{1 + (g_m + g_{mb}) R_s} = \frac{g_m R}{1 + (1 + \chi) g_m R} = 0.866 \quad (g_m = \sqrt{2 K_n' I_D} = 4.1 \times 10^{-4} \text{ S})$$

ii) For this case, $R = 10 \text{ k}\Omega$, which changes I_D to $I_D = 200 \mu\text{A} + \frac{V_o}{10 \text{ k}}$. Rest of the
 eqns. remain same. A few iterations give $V_o = 0.911 \text{ V}$, $I_D = 291.1 \mu\text{A}$, $V_{GS} =$
 2.089 V , $V_{TN} = 0.882 \text{ V}$, $V_{DS} = 4.089 \text{ V}$ (Saturated). $\chi = 0.163$

$$g_m = 4.826 \times 10^{-4} \text{ S} \Rightarrow A_v = \frac{g_m R}{1 + (1 + \chi) g_m R} = 0.73$$

(Note the drastic reduction in A_v as R is reduced).