## Performance modeling for Computer systems (Assignement 1)

## 5 mks

- 1. Consider  $Y = \sum_{i=1}^{N} X_i$  where  $X_i$  are iid random variables and N is an independent non negative integer valued random variable. Let  $M_X(t)$  and  $M_N(t)$  denote the moment generating functions for X and N respectively. Obtain the MGF  $M_Y(t)$  in terms of that of X and N.
- 2. Obtain the second moment of Poisson distribution and Geometric distribution.
- 3. Consider an  $M/G/\infty$  system. Find the distribution (pmf or cdf) of X(t) where X(t) denotes the number of jobs jobs present in the system at time t and where the service time distribution follows 1) Exponential distribution with parameter  $\mu$  2) Uniform distribution over interval [0,1].
- 4. Show that the Binomial process has independent and stationary increments.
- 5. Consider a sequence  $\{X_i\}$  of i.id exponential random variables with parameter  $\lambda$ . Define  $S_n = \sum_{i=1}^n X_i$ . Derive the pdf of  $S_n$  and obtain its mean and variance.
- 6. Prove the splitting property of the Poisson process.
- 7. Prove the merging property of the Poisson process.
- 8. For a Poisson process N(t) derive the expression for P(N(s) = k | N(t) = n) where s < t.