

Q:- A car company believes that the percentage of resident in city ABC that owns a vehicle is 60% or less. A sales Manager disagrees with this. He conducts a Hypothesis testing surveying 250 residents and found that 170 responded yes to owning a vehicle?

(a) State the Null & Alternate Hypothesis.

(b) At 10% of significance level, is there enough evidence to support the idea that vehicle ownership in city ABC is 60% or less?

⇒ Step-1 :- Null Hypothesis $\rightarrow H_0 \leq 60\%$ [i.e., Percentage of resident in city ABC that owns a vehicle is 60% or less.]

Alternate Hypothesis $\rightarrow H_1 \neq 60\%$ [i.e., Percentage of resident in city ABC that do not owns a vehicle is 60% or less.]

$n = 250$ ~~res~~ resident, $x = 170$ residents owns a vehicle

$$\hat{P} \Rightarrow \frac{x}{n} \Rightarrow \frac{170}{250} \Rightarrow 0.68$$

$$q_0 \Rightarrow 1 - P_0 \Rightarrow 1 - 0.6 \Rightarrow 0.4 \text{ (i.e. 40\%)}$$

Step-2 Significance value = 0.1 C.I = 90%. (i.e. $1 - \alpha$)

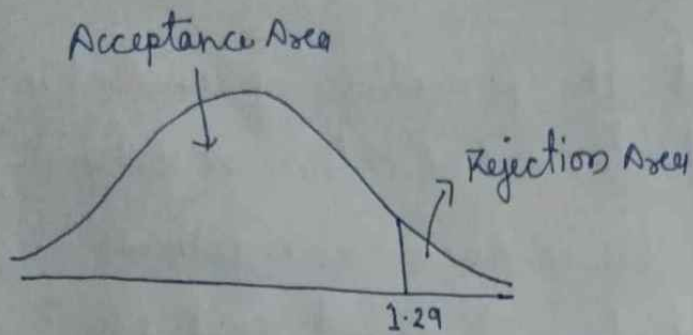
$$\Rightarrow 1 - 0.1 \Rightarrow 0.9$$

↓ at

$$+1.29$$

Step-3 Decision Boundary :-

S23



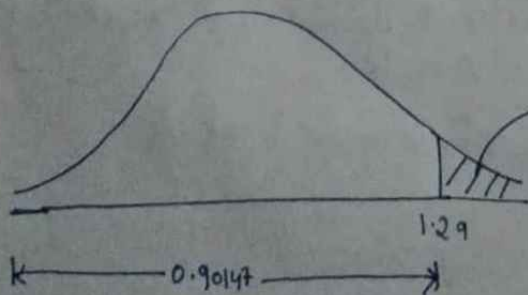
Step-4 Test Statistics :-

$$Z_{\text{test}} \Rightarrow \frac{\hat{P} - P_0}{\sqrt{\frac{P_0 q_0}{n}}} \Rightarrow \frac{0.68 - 0.6}{\sqrt{\frac{0.6 \times 0.4}{250}}} \Rightarrow \frac{0.08}{\sqrt{\frac{0.24}{250}}} \Rightarrow \frac{0.08}{\sqrt{0.00096}} \Rightarrow \frac{0.08}{0.03098} \Rightarrow 2.582$$

$\therefore Z_{\text{test}}$ i.e. 2.582 > +1.29 so reject the Null Hypothesis, the vehicle ownership in city ABC is not less than & equal to 60%.

For P-value :-

$$\text{Area of the body} = 0.90147$$



$$\begin{aligned} \text{P-value or Area of tail} &= 1 - 0.90147 \\ &= 0.09853 \end{aligned}$$

$$P\text{-value} = 0.09853$$

$$\text{Significance value } (\alpha) = 0.1$$

$\therefore \alpha > P\text{-value}$ (i.e. 0.1 > 0.09853) so rejects the Null Hypothesis.