#### 1

# Assignment - 1

# LAKSHMI GAYATHRI GUDIPUDI - SM21MTECH11001

## **PROBLEM**

Find the Area of Quadrilateral when four points are given

$$\mathbf{P} = \begin{pmatrix} 2 \\ 1 \end{pmatrix}, \mathbf{Q} = \begin{pmatrix} 3 \\ 5 \end{pmatrix}, \mathbf{R} = \begin{pmatrix} -3 \\ 4 \end{pmatrix}, \mathbf{S} = \begin{pmatrix} -2 \\ -2 \end{pmatrix}$$
(1)

### **SOLUTION**

Area of a Quadrilateral PQRS is

$$Area(\Delta PQR) + Area(\Delta PRS)$$
 (2)

$$Area(\Delta PQR) = \frac{1}{2} \|(\mathbf{Q} - \mathbf{P}) \times (\mathbf{Q} - \mathbf{R})\|$$
 (3)

For two vectors  $\mathbf{a} = \begin{pmatrix} a_1 \\ a_2 \end{pmatrix}$  and  $\mathbf{b} = \begin{pmatrix} b_1 \\ b_2 \end{pmatrix}$ 

$$\|\mathbf{a} \times \mathbf{b}\| = |(a_1b_2 - a_2b_1)|$$
 (4)

$$\mathbf{Q} - \mathbf{P} = \begin{pmatrix} 1 \\ 4 \end{pmatrix}$$

$$\mathbf{Q} - \mathbf{R} = \begin{pmatrix} 6 \\ 1 \end{pmatrix}$$

$$Area(\Delta PQR) = \frac{1}{2} \|(\mathbf{Q} - \mathbf{P}) \times (\mathbf{Q} - \mathbf{R})\|$$

$$= \frac{1}{2} |(-23)| \tag{6}$$

Similarly

$$Area of(\Delta PRS) = \frac{1}{2} ||(\mathbf{S} - \mathbf{P}) \times (\mathbf{S} - \mathbf{R})||$$
 (7)

$$\mathbf{S} - \mathbf{P} = \begin{pmatrix} -4 \\ -3 \end{pmatrix}$$

$$\mathbf{S} - \mathbf{R} = \begin{pmatrix} 1 \\ -6 \end{pmatrix}$$

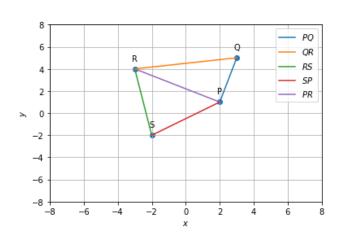
So total area of Quadrilateral PQRS is

$$Area(\Delta PQR) + Area(\Delta PRS)$$
 (9)

$$= \frac{1}{2}|(-23)| + \frac{1}{2}|(27)| \tag{10}$$

$$= (23 + 27)/2 \tag{11}$$

$$=25sq.units$$
 (12)



(5) Fig. 1. Quadrilateral PQRS

 $UsingArea of(\Delta PRS) = \frac{1}{2} ||(\mathbf{S} - \mathbf{P}) \times (\mathbf{S} - \mathbf{R})|| = \frac{1}{2} |(27)|$ (8)