1

Assignment - 1

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PROBLEM

Find the Area of Quadrilateral when four points are given

$$\mathbf{P} = \begin{pmatrix} 2 \\ 1 \end{pmatrix}, \mathbf{Q} = \begin{pmatrix} 3 \\ 5 \end{pmatrix}, \mathbf{R} = \begin{pmatrix} -3 \\ 4 \end{pmatrix}, \mathbf{S} = \begin{pmatrix} -2 \\ -2 \end{pmatrix}$$
(1)

SOLUTION

Area of a Quadrilateral PQRS is

$$Area(\Delta PQR) + Area(\Delta PRS)$$
 (2)

$$Area(\Delta PQR) = \frac{1}{2} [|(\mathbf{Q} - \mathbf{P})\mathbf{x}(\mathbf{Q} - \mathbf{R})|]$$
 (3)

For two vectors
$$\mathbf{a} = \begin{pmatrix} a1 \\ a2 \end{pmatrix}$$
 and $\mathbf{b} = \begin{pmatrix} b1 \\ b2 \end{pmatrix}$

$$[|\mathbf{axb}|] = |a1b2 - a2b1| \tag{4}$$

$$Q - P = \begin{pmatrix} 1 \\ 4 \end{pmatrix}$$

$$Q - R = \begin{pmatrix} 6\\1 \end{pmatrix}$$

$$UsingArea(\Delta PQR) = \frac{1}{2} [|(\mathbf{Q} - \mathbf{P})\mathbf{x}(\mathbf{Q} - \mathbf{R})|]$$
(5)

$$= \frac{1}{2} \left| (-23) \right| \tag{6}$$

Similarly

$$Area of(\Delta PRS) = \frac{1}{2} [|(\mathbf{S} - \mathbf{P})\mathbf{x}(\mathbf{S} - \mathbf{R})|]$$
 (7)

$$S - P = \begin{pmatrix} -4 \\ -3 \end{pmatrix}$$

$$S - R = \begin{pmatrix} 1 \\ -6 \end{pmatrix}$$

So total area of Quadrilateral PQRS is

$$Area(\Delta PQR) + Area(\Delta PRS)$$
 (9)

$$= \frac{1}{2}|(-23)| + \frac{1}{2}|(27)| \tag{10}$$

$$= (23 + 27)/2 \tag{11}$$

$$= 25 sq.units \tag{12}$$



Fig. 1. Quadrilateral PQRS

$$UsingArea of(\Delta PRS) = \frac{1}{2} [|(\mathbf{S} - \mathbf{P})\mathbf{x}(\mathbf{S} - \mathbf{R})|] = \frac{1}{2} |(27)|$$
(8)