

Number System - Percentages

Percentage

Percent means many hundredths. Example: $z\%$ is z percent which means z hundredths. It will be written as:

$$z\% = \frac{z}{100}$$

$$\frac{p}{q} \text{ as percent: } (\frac{p}{q} \times 100)\%$$

Commodity

If the price of a commodity increases by $R\%$, then the reduction in consumption so as not to increase the expenditure is:

$$[\frac{R}{(100 + R)} \times 100]\%$$

If the price of a commodity decreases by $R\%$, then the increase in consumption so as not to decrease the expenditure is:

$$[\frac{R}{(100 - R)} \times 100]\%$$

Population

The population of a city is P and let it increases at the rate of $R\%$ per annum:

$$\text{Population after } t \text{ years: } P(1 + \frac{R}{100})^t$$

$$\text{Population } t \text{ years ago: } \frac{P}{(1 + \frac{R}{100})^t}$$

Depreciation

Let V be the present value of machine. Suppose it depreciates at the rate of $R\%$ per annum:

$$\text{Machine's value after } t \text{ years: } P(1 - \frac{R}{100})^t$$

$$\text{Machine's value } t \text{ years ago: } \frac{P}{(1 - \frac{R}{100})^t}$$

- **If P is $R\%$ more than Q , then Q is less than P by how many percent?**

$$[\frac{R}{(100 + R)} \times 100]\%$$

- **If P is $R\%$ more than Q , then Q is more than P by how many percent?**

$$[\frac{R}{(100 - R)} \times 100]\%$$

Practice Question on Percentages

Q 1 - What is fraction equivalent of 32%.

A - $\frac{6}{30}$

B - $\frac{8}{25}$

C - $\frac{7}{50}$

D - 11:10

Q 2 - What is fraction equivalent of 160%.

A - $\frac{8}{5}$

B - $\frac{9}{5}$

C - $\frac{6}{7}$

D - $\frac{6}{23}$

Q 3 - What is decimal equivalent of 0.8%.

A - 0.008

B - 0.08

C - 0.8

D - 0.0008

Q 4 - What is decimal equivalent of 18%.

A - 0.0018

B - 0.18

C - 18

D - 0.018

Q 5 - What is decimal equivalent of 5%.

A - 0.0005

B - 0.005

C - 0.05

D - 0.5

Q 6 - What is decimal equivalent of 126%.

A - 1.26

B - 126

C - 12.6

D - 1260

Q 7 - What is decimal equivalent of 0.06%.

A - 0.6

B - 0.06

C - 0.006

D - 0.0006

Q 8 - What is $\frac{3}{4}$ as per cent?

A - 45

B - 55

C - 65

D - 75

Q 9 - 45% of 280 + 28% of 450 = ?.

A - 352

B - 252

C - 452

D - 552

Q 10 - Which is largest in $\frac{50}{3}\%$, $\frac{2}{15}$, 0.18, $\frac{3}{7}$?

A - 0.18

B - $\frac{3}{7}$

C - $\frac{2}{15}$

D - $\frac{50}{3}\%$

Q 11 - 65% of a number is 21 less than $\frac{4}{5}$ th of that number. Find the number.

A - 140

B - 130

C - 120

D - 110

Q 12 - What per cent is 120 of 90?

A - $\frac{400}{3}\%$

B - $\frac{400}{6}\%$

C - $\frac{200}{3}\%$

D - $\frac{200}{6}\%$

Q 13 - What percent is 5gm of 1kg?

A - 0.15%

B - 0.05%

C - 0.25%

D - 0.35%

Q 14 - What per cent is 120 ml of 3.5 liters?

A - $\frac{30}{7}\%$

B - $\frac{20}{7}\%$

C - $\frac{10}{7}\%$

D - $\frac{1}{7}\%$

Q 15 - If A's pay is 20% more than that of B, then what number of per penny is B's compensation not as much as that of A?

A - $\frac{50}{3}\%$

B - $\frac{60}{3}\%$

C - $\frac{70}{3}\%$

D - $\frac{80}{3}\%$

Q 16 - If A's salary is 25% not as much as that of B, then what number of per penny is B's compensation more than that of A?

A - $10/3\%$

B - $100/3\%$

C - $20/3 \%$

D - $200/3 \%$

Q 17 - If the cost of tea is expanded by 20%, by what amount of percent must the utilization of tea be lessened so as not to build the consumption?

A - $50/3\%$

B - $100/3\%$

C - $20/3\%$

D - $200/3\%$

Q 18 - If the cost of sugar falls by 10%, by how much per penny should a householder expand its utilization, so as not to diminish its use on sugar?

A - $100/9$

B - $10/9$

C - $100/3$

D - $10/3$

Q 19 - The tax on a commodity is diminished by 20% and its consumption increases by 15%. Find the effect on revenue.

A - 8% increase

B - 8% decrease

C - 10% decrease

D - 10% increase

Q 20 - The population of a town is 176400. It increases annually at the rate of 5% p.a. What will be its population after 2 years?

A - 194481

B - 294481

C - 394481

D - 494481

Q 1 - $88\% \text{ of } 370 + 24\% \text{ of } 210 - ? = 118$

A - 258

B - 298

C - 320

D - 18

Q 2 - If 25% of a number is subtracted from a second number, the second number reduces to its five-sixth. What is the ratio of the first number to the second number?

A - 2:3

B - 3:2

C - 1:4

D - 4:1

Q 3 - A fruit seller had some fruits. He sells 40% of them and still has 420 of them. Originally, he had how many of them?

A - 800

B - 600

C - 700

D - 900

Q 4 - Siya secures 90%, 60% and 54% marks in test papers with 100, 150 and 200 respectively as maximum marks. The percentage of her aggregate marks is?

A - 72%

B - 70%

C - 75%

D - 64%

Q 5 - A sum of Rs 817 is divided among A, B and C such that A receives 25% more than B and B receives 25% less than C. What is the A share in the amount?

A - 228

B - 247

C - 285

D - 304

Q 6 - In a recent survey 40% houses contained 2 or more people. Of those houses containing only one person, 25% were having only a male. What is the percentage of all the houses which contain exactly one females and no males?

A - 75

B - 40

C - 15

D - 45

Q 7 - Water tax is increased by 30% but its consumption is decreased by 20%. Then, the increase or decreased in the expenditure of the money is

A - no change

B - 5% increase

C - 4% decrease

D - 4 % increase

Q 8 - 150% of $14 + 75\%$ of $75 = ?$

A - 2503.5

B - 2650.5

C - 2525

D - 2558.60

Q 9 - In an examination, 60% of the candidates passed in English and 70% of the candidates passed in Mathematics but 20% failed in both the subjects. If 2500 candidates passed in both the subjects, the number of candidates that appeared in the examination was:

A - 3000

B - 3500

C - 4000

D - 5000

Q 10 - After spending 15% on raw material, 30 % on machinery, 15% on furniture, 10% on machinery, Harish had a balance of 1300. The money with him was:

A - 3568

B - 4010

C - 3952

D - 4333

1Answer - B

Explanation

$$32\% = 32/100 = 8/25.$$

2Answer - A

Explanation

$$160\% = 160/100 = 8/5$$

3Answer - A

Explanation

$$0.8\% = 0.8/100 = 0.008.$$

4Answer - B

Explanation

$$18\% = 18/100 = 0.18$$

5Answer - C

Explanation

$$5\% = 5/100 = 0.05$$

6Answer - A

Explanation

$$126\% = 126/100 = 1.26$$

7Answer - D

Explanation

$$0.06\% = 0.06/100 = 0.0006.$$

8Answer - D

Explanation

$$3/4 = (3/4 * 100)\% = 75\%$$

9Answer - B**Explanation**

$$45\% \text{ of } 280 + 28\% \text{ of } 450 = (450/100 * 280) + (28/100 * 450) \\ = (126 + 126) = 252$$

10Answer - B**Explanation**

$$162/3\% = 50/(3 * 100) = 1/6 = 0.166, 2/15 = 0.133, 3\text{rd number} = 0.18, 3/7 = 0.42. \\ \text{Clearly, } 3/7 \text{ is largest.}$$

11Answer - A**Explanation**

Let the number be x. Then,
 $(4/5 x) - (65\% \text{ of } x) = 21 \Rightarrow 4x/5 - 65x/100 = 21 \Rightarrow 4x/5 - 13x/20 = 21 \\ \Rightarrow 16x - 13x = 420 \Rightarrow 3x = 420 \Rightarrow x = 140.$
 Required number = 140.

12Answer - A**Explanation**

$$\text{Required \%} = (120/90 * 100)\% = 400/3\%$$

13Answer - B**Explanation**

$$\text{Required \%} = (5/1000 * 100)\% = 1/2\% = 0.05\%$$

14Answer - A**Explanation**

$$\text{Required \%} = (150/3500 * 100)\% = 30/7\%$$

15Answer - A**Explanation**

$$\text{B's salary is less than that of A by } \{R / ((100 + R) * 100)\}\% \\ = \{20 / ((120) * 100)\}\% = 50/3\%$$

16Answer - B**Explanation**

$$\text{B's salary is more than that of A by } \{R / ((100 - R) * 100)\}\% \\ = \{25 / ((100 - 25) * 100)\}\% = (25/75 * 100) = 100/3\%$$

17Answer - A**Explanation**

Reduction % in consumption = $\{R/((100+R)) * 100\} \% (20/120 * 100) \%$
 $= 50/3 \%$

18Answer - A**Explanation**

Increase % in consumption = $\{R/((100-R)) * 100\} \% = \{10/((100-10)) * 100\} = 100/9 \%$

19Answer - B**Explanation**

Let originally revenue obtained by Rs. x.

New revenue = (Consumption * Tax)

= (115% of 80% of Rs. x) = Rs(115/100*80/100*x)=Rs.92x/100

= 92% of the original.

Hence, the revenue is decreased by 8%.

20Answer - A**Explanation**

Population after 2 years = $\{176400 * (1+5/100)^2\}$

$176400 * 21/20 * 21/20 = 194481$.