

Aptitude - Decimals & Fractions

Decimal Fractions

Fractions having denominators in power of 10 are called decimal fractions.

$$\begin{aligned}1/10 &= .1, 2/10 = .2, \dots \\1/100 &= .01, 2/100 = .02, \dots \\1/1000 &= .001, 2/1000 = .002, \dots\end{aligned}$$

Converting a decimal number into a fraction

In the denominator part, place 1 under decimal point and suffix with as many zeroes as is the total number of digits after decimal point. Remove the decimal point and reduce the fraction to its lowest term.

$$\begin{aligned}.56 &= 56/100 = 14/25 \\ .0024 &= 24/10000 = 3/1250\end{aligned}$$

Suffixing zeroes to the right of a decimal fraction does not change its value. Thus $0.6 = 0.60 = 0.600$ etc.

If numerator and denominator contains same number of decimal places, we can remove decimal signs from each number.

$$\begin{aligned}2.71/3.41 &= 271/341 \\ 14.4/15.6 &= 144/156 = 12/13\end{aligned}$$

Adding decimals

Place each number under each other in such a way that decimal points lies in same column. Numbers so arranged can be added in usual way.

$$\begin{array}{r}21.3 + .213 + 3.21 + .021 + 2.0031 = ? \\ 21.3 \\ .213 \\ 3.21 \\ .021 \\ 2.0031 \\ \hline 26.7471 \\ \hline\end{array}$$

Subtracting decimals

Place each number under each other in such a way that decimal points lie in same column. Numbers so arranged can be subtracted in usual way.

$$\begin{array}{r} 23.004 \\ -16.5628 \\ \hline 6.4412 \\ \hline \end{array}$$

Multiplying decimals

Multiply given numbers without considering decimal point. In product, mark the decimal point as many places of decimals as is the sum of number of decimal places in the given numbers.

$$\begin{aligned} 2.3 \times 0.12 &= ? \\ 23 \times 12 &= 276 \\ \text{Sum of decimal places} &= 1 + 2 = 3 \\ \therefore 2.3 \times 0.12 &= 0.276 \end{aligned}$$

Dividing decimals by number

Divide given decimal number without considering decimal point. In quotient, mark the decimal point as many places of decimals as is the sum of number of decimal places in the given dividend.

$$\begin{aligned} 0.63 / 9 &= ? \\ 63 / 9 &= 7 \\ \text{Decimal places in dividend} &= 2 \\ \therefore 0.63 / 9 &= 0.07 \end{aligned}$$

Dividing decimals by decimals

Multiply both dividend and divisor by such multiple of 10 so that divisor becomes a whole number. Divide dividend without considering decimal point. In quotient, mark the decimal point as many places of decimals as is the sum of number of decimal places in the given dividend.

$$\begin{aligned} 0.00042 / 0.06 &= ? \\ 0.00042 / 0.06 &= (0.00042 \times 100) / (0.06 \times 100) \\ &= 0.042 / 6 \end{aligned}$$

$$\begin{aligned} \text{Now } 42 / 6 &= 7 \\ \text{Decimal places in dividend} &= 3 \\ \therefore 0.00042 / 0.06 &= 0.007 \end{aligned}$$

Recurring Decimals

Pure recurring decimals

A decimal fraction in which all figures after decimal point are repeated is called a pure recurring decimals. For example, 0.5555, 0.323232

Converting pure recurring decimal to fraction

Put the repeating figure only once in the numerator and put as many nines in the denominator as in number of repeating figures.

Express 0.33333 in fraction.

$$0.3333 = 3/9 = 1/3$$

Express 0.2727 in fraction.

$$0.2727 = 27/99 = 3/11$$

Mixed recurring decimals

A decimal fraction in which some figures are not repeating whereas some of them are repeating, is called as mixed recurring decimals. For example, 0.534242, 0.078888.

Converting mixed recurring decimal to fraction

Put the difference of numbers formed by digits after decimal point taking repeated digits once and that formed by non-repeating number, in the numerator and put as many nines in the denominator as in number of repeating figures and annex them with as many zeroes as in the non-repeating digits.

Express 0.266666 in fraction.

$$0.26666 = (26-2)/90 = 24/90 = 4/15$$

Express 0.326868 in fraction.

$$0.326868 = (3268 - 32)/9900 = 3236/9900 = 809/2475$$

Practice Question on Decimals

Q 1 - Which is the following is fraction for 0.36?

A - $\frac{9}{25}$

B - $\frac{51}{25}$

C - $\frac{3}{400}$

D - $\frac{2081}{250}$

Q 2 - Which is the following is fraction for 2.04?

A - $\frac{9}{25}$

B - $\frac{51}{25}$

C - $\frac{3}{400}$

D - $\frac{2081}{250}$

Q 3 - Which is the following is fraction for .0075?

A - $\frac{9}{25}$

B - $\frac{51}{25}$

C - $\frac{3}{400}$

D - $\frac{2081}{250}$

Q 4 - Which is the following is fraction for 8.324?

A - $\frac{9}{25}$

B - $\frac{51}{25}$

C - $\frac{3}{400}$

D - $\frac{2081}{250}$

Q 5 - Which of the following is the correct ascending order for $\frac{3}{8}$, $\frac{7}{12}$, $\frac{2}{3}$, $\frac{16}{25}$, $\frac{14}{15}$?

A - $\frac{3}{8} < \frac{7}{12} < \frac{2}{3} < \frac{16}{25} < \frac{14}{15}$

B - $\frac{3}{8} < \frac{7}{12} < \frac{16}{25} < \frac{2}{3} < \frac{14}{15}$

C - $\frac{7}{12} < \frac{3}{8} < \frac{2}{3} < \frac{16}{25} < \frac{14}{15}$

D - $\frac{2}{3} < \frac{7}{12} < \frac{3}{8} < \frac{16}{25} < \frac{14}{15}$

Q 6 - Which of the following is the correct descending order for $\frac{3}{5}$, $\frac{4}{7}$, $\frac{8}{9}$, $\frac{9}{11}$, $\frac{13}{15}$?

A - $\frac{3}{5} > \frac{4}{7} > \frac{8}{9} > \frac{9}{11} > \frac{13}{15}$

B - $\frac{8}{9} > \frac{13}{15} > \frac{9}{11} > \frac{3}{5} > \frac{4}{7}$

C - $\frac{13}{15} > \frac{8}{9} > \frac{9}{11} > \frac{3}{5} > \frac{4}{7}$

D - $\frac{13}{15} > \frac{8}{9} > \frac{3}{5} > \frac{9}{11} > \frac{4}{7}$

Q 7 - Which of the following is the H.C.F. of 1.5, 3 and 0.6?

A - 0.3

B - 0.1

C - 0.2

D - 0.6

Q 8 - Which of the following is the L.C.M. of 1.5, 3 and 0.6?

A - 3

B - 2

C - 1

D - 6

Q 9 - $34.64 + 2.9 + 107.035 + .0086 = ?$

A - 141.5436

B - 144.5836

C - 134.5678

D - 132.8765

Q 10 - $3.004 - 1.2996 = ?$

A - 1.7044

B - 0.7262

C - 1.6723

D - 0.3456

Q 11 - Which of the following is the result when 6.2958 is subtracted from 10?

A - 3.7042

B - 3.8675

C - 2.8762

D - 3.8762

Q 12 - $1.71 \times 1.3 = ?$

A - 3.213

B - 2.223

C - 1.223

D - 3.213

Q 13 - $3.746 \times 11.4 = ?$

A - 42.7044

B - 40.7654

C - 34.8762

D - 42.7862

Q 14 - $.5 \times 0.5 \times .005 \times 50 = ?$

A - .00625

B - .0625

C - .625

D - 6.25

Q 15 - If $172 \times 38 = 6536$, what is 1.72×0.38 ?

A - 65.36

B - 0.06536

C - 0.6536

D - 6.536

Q 16 - $0.0182 / 14 = ?$

A - 13

B - 0.013

C - 0.0013

D - 1.3

Q 17 - $40.40 / 0.0008 = ?$.

A - 50.5

B - 505

C - 5050

D - 50500

Q 18 - $0.001 / ? = 0.1$

A - 0.1

B - 0.01

C - 0.001

D - 1.0

Q 19 - What is fraction for 0.313131?

A - 3/7

B - 4/9

C - 3/9

D - 31/99

Q 20 - What is fraction for 0.5366666?

A - 61/300

B - 69/550

C - 161/300

D - 8/45

Q 1 - $(0.46-0.046)/(0.0046/46)=?$

A - 0.414

B - 0.0414

C - 414

D - 4140

Q 2 - $(1.1^3+0.064)/(1.1^2-0.4^4+0.16^2)=?$

A - 1

B - 1.25

C - 1.5

D - 1.75

Q 3 - $(0.036-0.018)/(0.0036/36)=?$

A - 2

B - 6

C - 12

D - 18

Q 4 - How many digits are there to the right of decimal in the product of 32.182×36.42 ?

A - 6

B - 5

C - 4

D - 3

Q 5 - What is the value of 3.14×10^6

A - 314

B - 3140

C - 3140000

D - 31400

Q 6 - $12.1 / 19.8 = ?$

A - $7/9$

B - $11/18$

C - $13/17$

D - $11/19$

Q 7 - $(6.5 \times 4.7 + 6.5 \times 5.3) / (1.3 \times 7.9 - 1.3 \times 6.9) = ?$

A - 3.9

B - 39

C - 34.45

D - 50

Q 8 - $(.538 \times .538 - .462 \times .462) / 1 - .924 = ?$

A - $.076$

B - 1.042

C - 1

D - 2

Q 9 - $0.535353 = ?$

A - $53/100$

B - $53/90$

C - $53/99$

D - $26/45$

Q 10 - 312 Rs were divided among 60 boys and some girls in such a way that each boy got 3.6 Rs and each girl got 2.40. How many girls were there?

A - 35

B - 40

C - 60

D - 65

1 Answer - A**Explanation**

$$0.36 = 36/100 = 9/25$$

2Answer - B**Explanation**

$$2.04 = 204/100 = 51/25$$

3Answer - C**Explanation**

$$.0075 = 75/10000 = 3/400$$

4Answer - D**Explanation**

$$8.324 = 8324/1000 = 2081/250.$$

5Answer - B**Explanation**

$$3/8 = 0.375, 7/12 = 0.583, 2/3 = 0.666, 16/25 = 0.64 \text{ and } 14/15 = 0.933$$

$$\text{As } .375 < .583 < .64 < .666 < .933$$

$$\therefore 3/8 < 7/12 < 2/3 < 16/25 < 14/15$$

6Answer - B**Explanation**

$$3/5 = 0.6, 4/7 = 0.571, 8/9 = 0.888, 9/11 = 0.818, 13/15 = 0.866$$

$$\text{As } 0.888 > 0.866 > 0.818 > 0.6 > 0.571$$

$$\therefore 8/9 > 13/15 > 9/11 > 3/5 > 4/7$$

7Answer - A**Explanation**

Make same numbers of decimal places in the given numbers.

Numbers become 1.5, 3.0 and 0.6

Without decimal places, these numbers are 15, 30 and 6.

$$\text{H.C.F. of } 15, 30 \text{ and } 6 = 3$$

$$\therefore \text{H.C.F. of given numbers} = 0.3$$

8Answer - A**Explanation**

Make same numbers of decimal places in the given numbers.

Numbers become 1.5, 3.0 and 0.6

Without decimal places, these numbers are 15, 30 and 6.

L.C.M. of 15, 30 and 6 = 30

\therefore L.C.M. of given numbers = 3

9Answer - B

Explanation

We have

34.64

2.9

107.035

.0086

144.5836

$\therefore 34.64 + 2.9 + 107.035 + .0086 = 144.5836$

10Answer - A

Explanation

We have

3.004

-1.2996

1.7044

$\therefore 3.004 - 1.2996 = 1.7044$

11Answer - A

Explanation

We have

10.0000

- 6.2958

3.7042

$\therefore 10 - 6.2958 = 3.7042$

12Answer - B

Explanation

$171 \times 13 = 2223$

Here sum of decimal places = $2 + 1 = 3$

$\therefore 1.71 \times 1.3 = 2.223$

13Answer - A

Explanation

3746

$$\begin{array}{r}
 \times 114 \\
 \hline
 14984 \\
 3746x \\
 3746xx \\
 \hline
 427044 \\
 \hline
 \end{array}$$

Here sum of decimal places = $3 + 3 = 6$
 $\therefore 3.746 \times 11.4 = 42.7044$

14Answer - A

Explanation

We have $5 \times 5 \times 5 \times 50 = 6250$
Sum of decimal places = $1 + 2 + 3 = 6$
 $\therefore .5 \times 0.5 \times .005 \times 50 = 0.00625.$

15Answer - B

Explanation

Sum of decimal places = $2 + 3 = 5$
 $\therefore 1.72 \times 0.38 = 0.06536.$

16Answer - C

Explanation

$182 / 14 = 13$
Dividend contains 4 places of decimals.
 $\therefore 0.0182 / 14 = 0.0013$

17Answer - D

Explanation

$40.40 / 0.0008 = (40.40 \times 10000) / (8 \times 10000) = 404000 / 8 = 50500$

18Answer - B

Explanation

Let $0.001/x = 0.1$
 $\Rightarrow x = (0.001/0.1) \times (10/10) = .01/1 = .01$

19Answer - B

Explanation

$= 0.313131 = 31/99$

20Answer - C

Explanation

$0.5366666 = (536 - 53)/900 = 483/900 = 161/300.$