

MODULE 3

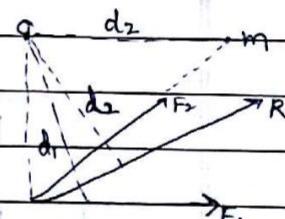
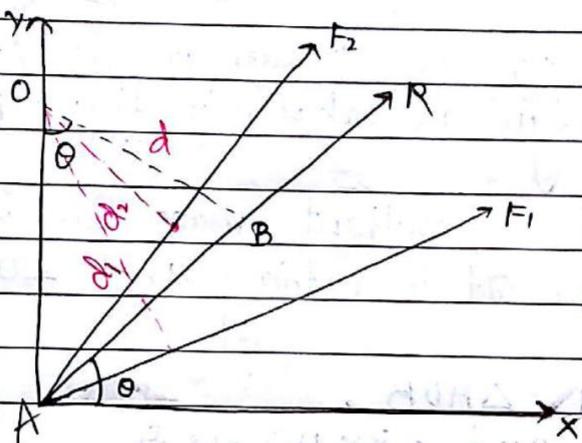
ANALYSIS OF NON-CONCURRENT FORCE SYSTEM

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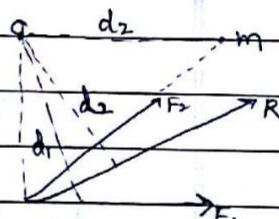
~~Imp.~~ State and prove Varignon's theorem of moment :-

Statement: It states that the algebraic sum of moments of a system of co-planar forces about a moment centre is equal to the moment of their resultant force about the same moment centre.



$O - d_2 - m$

$(R \sin \theta) = (F_1 \sin \theta)$



$O - d_2 - m$

$(R \sin \theta) = (F_1 \sin \theta)$

d_1

d_1

d_2

d_2

d

d

d_1

d_1

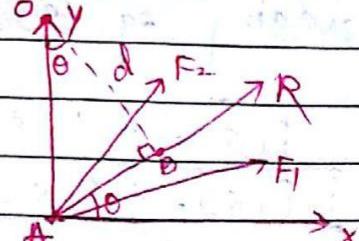
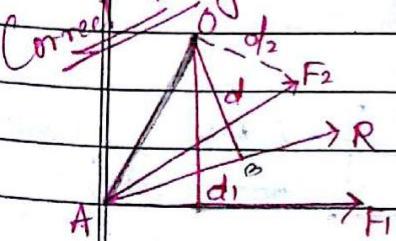
d_2

d_2

d

d

Diagram



Correct

figure (a)

figure (b)

Referring to fig (a), let R be the resultant of 2 forces F_1 and F_2 and O be the moment centre. Let D_1 , D_1 and D_2 are the moment arms of the forces R , F_1 and F_2 resp. Then according to the theorem, we have to prove

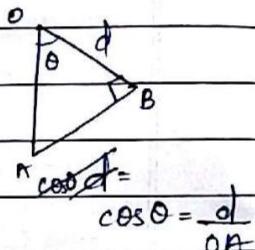
$$R \times d = F_1 \times d_1 + F_2 \times d_2$$

Join OA and Consider it as y -axis, being A as origin as shown in figure B.

Let the resultant make an angle θ wrt x -axis. If it is nothing that $\angle AOB = \theta$.

From $\triangle AOB$,

$$\begin{aligned} R \times d &= R \times AO \cos \theta \\ &= R \times \cos \theta \times AO. \\ &= AO(R_x) \end{aligned}$$



$$R \times d = AO(R_x) \quad \text{--- (1)}$$

If R_x denotes component of R in x -direction. Similarly if F_{1x} and F_{2x} are the component of F_1 and F_2 resp. in the x -direction then we can write :-

$$F_1 \times d_1 = AO(F_{1x}) \quad \text{--- (2)}$$

$$F_2 \times d_2 = AO(F_{2x}) \quad \text{--- (3)}$$

Adding eq (2) and (3) :-

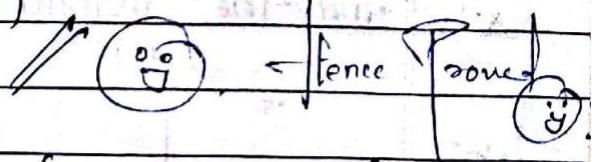
$$F_1 \times d_1 + F_2 \times d_2 = (F_{1x} + F_{2x}) AO$$

$$F_1 \times d_1 + F_2 \times d_2 = R_x AO \quad \text{--- (4)}$$

$$\text{Since } F_{1x} + F_{2x} = R_x$$

Comparing eq (1) and (4) :-

$$R \times d = F_1 \times d_1 + F_2 \times d_2$$



- (1) Locate the moment centre. (Given in ques.)
- (2) Find the moment of all the forces about the moment centre.

$$\sum H \rightarrow 0$$

$$\sum V \neq 0$$

$$R = \sqrt{(\sum H)^2 + (\sum V)^2}, \theta = \tan^{-1} \left(\frac{\sum V}{\sum H} \right)$$

From Varignon's Theorem * $d = \frac{|\text{mc}|}{R}$

- (3) Find the distance of the point.

$$d = \frac{|\text{mc}|}{R}$$

$$(4) x\text{-intercept} = \frac{|\text{mc}|}{\sum V}$$

$$(5) y\text{-intercept} = \frac{|\text{mc}|}{\sum H}$$

(3) If (x)losup1 - (x)uclsup1 = 0 then (x)uclsup1 = (x)losup1

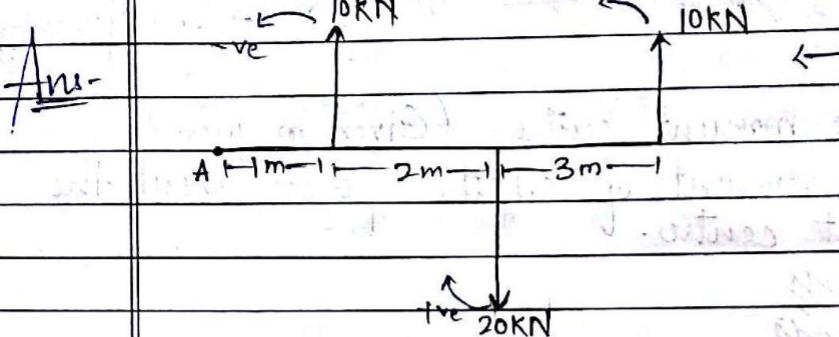
Now this can be solved following the steps
1. Take individual data first and multiply it with its weight
2. Add both the values and then divide by total weight
3. Then take the value of each item and multiply it with its weight
4. Add both the values and then divide by total weight

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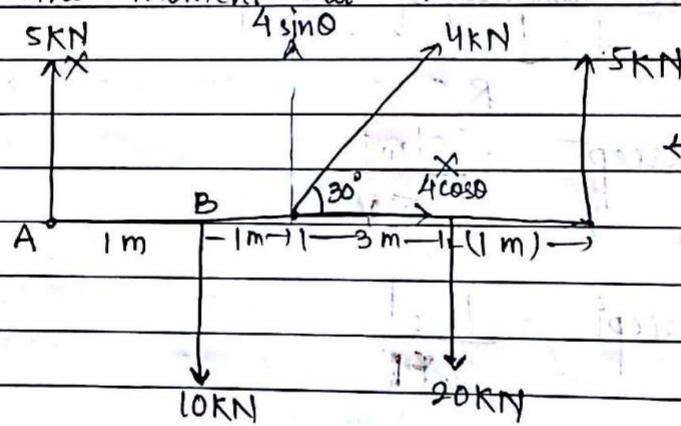
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Q.1- Find the moment @ A:



$$\begin{aligned}M_A &= (-10) \times 6 + (20)(3) - (10)(1) \\&= -60 + 60 - 10 = -10 \text{ KNm}\end{aligned}$$

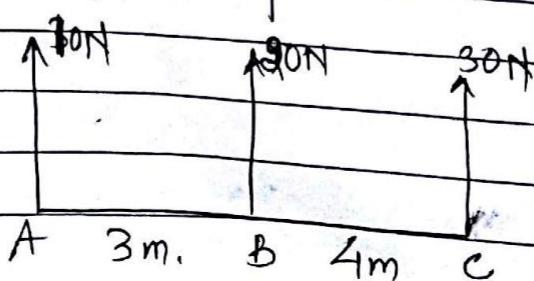
Q.2- Find the moment at A:



Ans- $M_A = (-5)(6) + (20)(5) - (4\sin 30)(2) + (10)(1)$

$$M_A = 76 \text{ KN-m}$$

Q.3- 3 like parallel forces 10, 20 and 30 N are acting on line ABC respectively. Find the magnitude, direction and distance of resultant from the point A. AB = 3m BC = 4m.



Ans- $\sum H = 0$

$$\sum V = 10 + 20 + 30 = 60,$$

$$R = \sqrt{\sum H^2 + \sum V^2} = \sqrt{(60)^2} = 60\text{N}$$

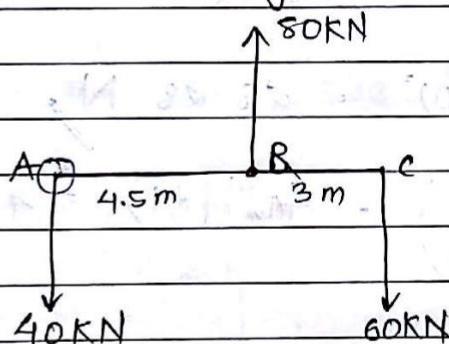
$$d = \frac{|M_A|}{R}$$

$$\begin{aligned}\sum M_A &= -(30 \times 7) - (20 \times 3) \\ &= -210 - 60 = -270.\end{aligned}$$

$$\therefore d = \frac{|-270|}{60} = \frac{270}{60} = 4.5 \text{ m}.$$

- Q.4- A coplanar parallel force system consists of 3 forces acting on a rigid base as shown in fig.
Determine the single force and its location from the point A. (resultant)

Ans-



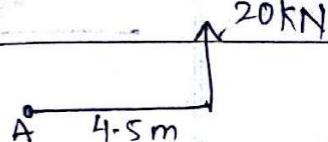
$$\sum H = 0$$

$$\sum V = 80 - 40 - 60 = 80 - 100 = -20 \text{ kN}$$

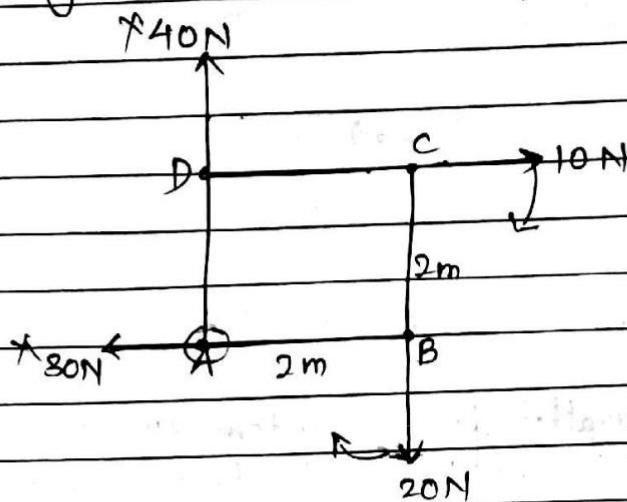
$$R = \sqrt{0^2 + (-20)^2} = 20\text{kN}$$

$$\begin{aligned}M_A &= (60 \times \frac{7.5}{18}) - (80)(4.5) + 0 \\ &= 90 \text{ Nm}\end{aligned}$$

$$\therefore d = \frac{|M_A|}{R} = \frac{90}{20} = 4.5 \text{ m.}$$



~~Q1~~ 4 forces are simultaneously acting of magnitude 10N, 20N, 30N & 40N along the 4 sides of the square of size (2x2) as shown in fig. Determine the magnitude and direction and its distance from A.



$$\sum H = 10 - 30 = -20 \text{ N.}$$

$$\sum V = 40 - 20 = 20 \text{ N.}$$

$$R = \sqrt{(-20)^2 + (20)^2} = 28.28 \text{ N,}$$

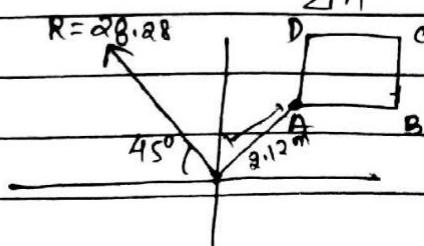
$$\theta = \tan^{-1} \left(\frac{20}{-20} \right) + \tan^{-1}(+1) = 45^\circ //$$

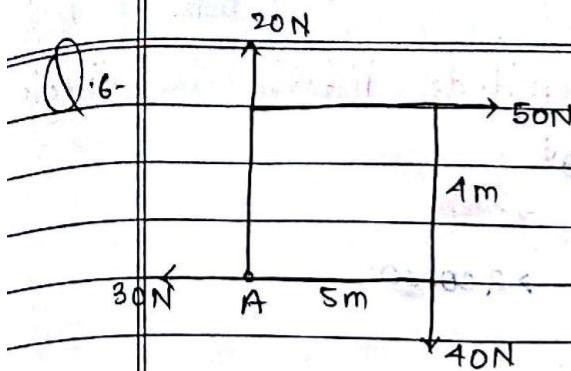
$$m_A = 10 \times 2 + 20 \times 2 = 20 + 40 = 60 \text{ Nm,}$$

$$d = \frac{|m_A|}{R} = \frac{60}{28.28} = 2.1216 \text{ m,}$$

$$x\text{-intercept} = \frac{|m_A|}{\sum V} = \frac{60}{20} = 3 \text{ m,}$$

$$y\text{-intercept} = \frac{|m_A|}{\sum H} = \frac{60}{-20} = -3 \text{ m,}$$





$$\Sigma H = 50 - 30 = 20 \text{ N.}$$

$$\Sigma V = 20 - 40 = -20 \text{ N.}$$

$$R = \sqrt{(20)^2 + (-20)^2} = 28.28 \text{ N.}$$

$$\theta = \tan^{-1}\left(\frac{20}{20}\right) = 45^\circ \text{ // } \quad \S = AM$$

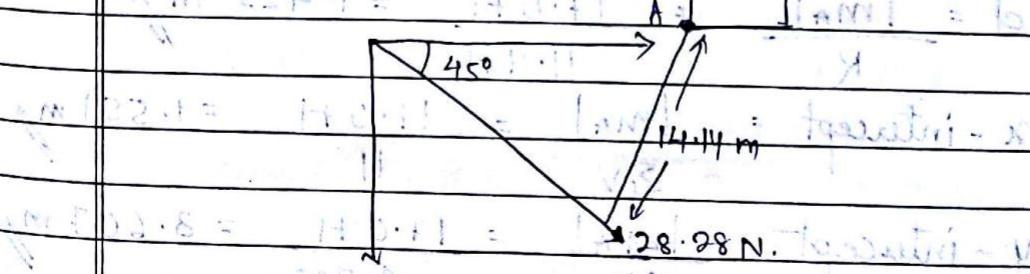
$$M_A = (50 \times 4) + (40) \times 5.5 + 2 \cdot 8 = 432 \\ = 200 + 200 = 400 \text{ Nm; } 21 - 21 = 12$$

$$d = \frac{m_A}{R} = \frac{400}{28.28} = 14.144 \text{ m.}$$

$$x\text{-intercept} = |m_A| = 400/28 = 20 \text{ m.}$$

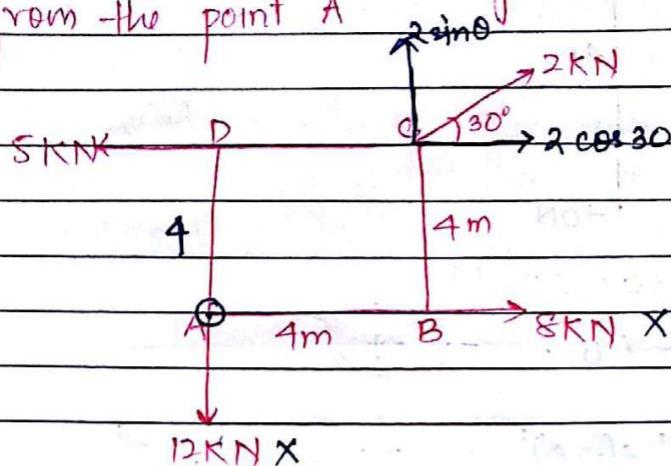
$$y\text{-intercept} = |m_A| = \frac{400}{20} = 20 \text{ m.}$$

$$m_{AB} = \frac{|m_A| + |m_B|}{2} = 10$$



Q.7. Find the resultant magnitude, distance and direction from the point A

$\sum H =$



$$M_A = ?$$

$$\Sigma H = 8 - 5 + 2 \cos 30^\circ = 4.732 \text{ KN.}$$

$$\Sigma V = -12 + 2 \sin 30^\circ = -11 \text{ KN} //$$

$$R = \sqrt{(\Sigma H)^2 + (\Sigma V)^2} = 11.974 \text{ KN} //$$

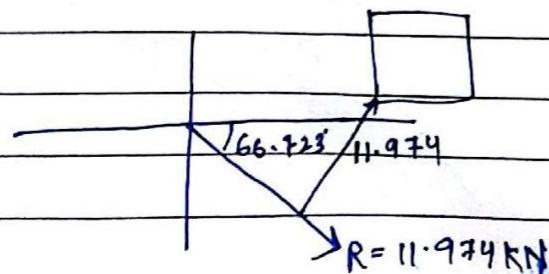
$$\theta = \tan^{-1} \left(\frac{\Sigma V}{\Sigma H} \right) = 66.723^\circ //$$

$$M_A = -2 \sin 30^\circ \times 4 + 2 \cos 30^\circ \times 4 - 5 \times 4 \\ = -17.071 \text{ Nm} //$$

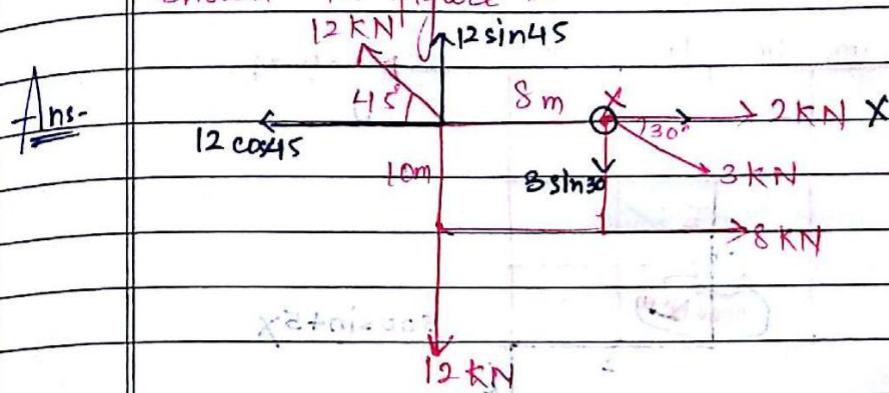
$$d = \frac{|M_A|}{R} = \frac{17.071}{11.974} = 1.425 \text{ m} //$$

$$x\text{-intercept} = \frac{|M_A|}{\Sigma V} = \frac{17.071}{11} = 1.551 \text{ m} //$$

$$y\text{-intercept} = \frac{|M_A|}{\Sigma H} = \frac{17.071}{4.732} = 3.607 \text{ m} //$$



Q.8- Find the resultant magnitude and direction of the distance from x of the force system shown in figure :-



$$\Sigma H = 2 - 12 \cos 45 + 8 + 3 \cos 30 = 4.112 \text{ KN}$$

$$\begin{aligned} \Sigma V &= 12 \sin 45 - 12 - 3 \sin 30 \\ &= -5.014 \text{ KN} \end{aligned}$$

$$R = \sqrt{\Sigma V^2 + \Sigma H^2} = \sqrt{6.4832^2 + 4.112^2} = 8.02 \text{ KN}$$

$$\theta = \tan^{-1} \left(\frac{\Sigma V}{\Sigma H} \right) = \tan^{-1} \left(\frac{-5.014}{4.112} \right) = 50.64^\circ$$

$$\begin{aligned} M_A &= (12 \sin 45 \times 8) - (12 \times 8) - (8 \times 10) \\ &= -108.117 \text{ KN-m} \end{aligned}$$

$$d = \frac{|M_A|}{R} = \frac{108.117}{8.02} = 13.488 \text{ m}$$

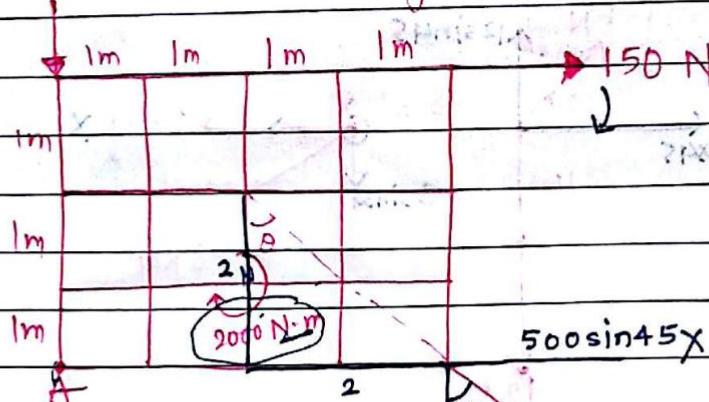
$$x\text{-intercept} = \frac{108.117}{5.014} = 21.56 \text{ m}$$

$$y\text{-intercept} = \frac{108.117}{4.112} = 26.293 \text{ m}$$

$$26.293 - 13.488 = 12.805 \text{ m}$$

$$12.805 - 21.56 = -8.755 \text{ m}$$

Ques. Find the equilibrium w.r.t A as origin of system of forces shown in figure :-



$$\text{Ans. } \tan \theta = \frac{2}{2} = 1 \Rightarrow \theta = 45^\circ \text{ and } R = 500\sqrt{2}$$

$$\sum H = 150 + 500 \sin 45^\circ = 503.55 \text{ N}$$

$$\sum V = -200 - 500 \cos 45^\circ = -553.55 \text{ N}$$

$$R = \sqrt{\sum V^2 + \sum H^2} = 748.31 \text{ N}$$

$$\theta = \tan^{-1} \left(\frac{553.55}{503.55} \right) = 47.708^\circ \text{ Ans}$$

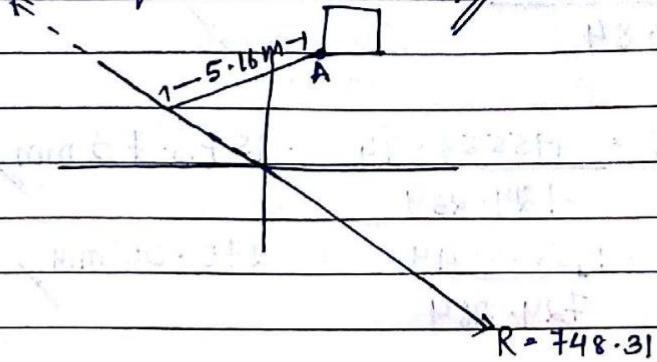
$$M_A = 2000 + 500 \cos 45^\circ \times 4 + 150 \times 3 = 3864.21 \text{ N-m}$$

$$d = \frac{3864.21}{748.31} = 5.16 \text{ m}$$

$$x\text{-intercept} = \frac{3864.21}{553.55} = 6.98 \text{ m}$$

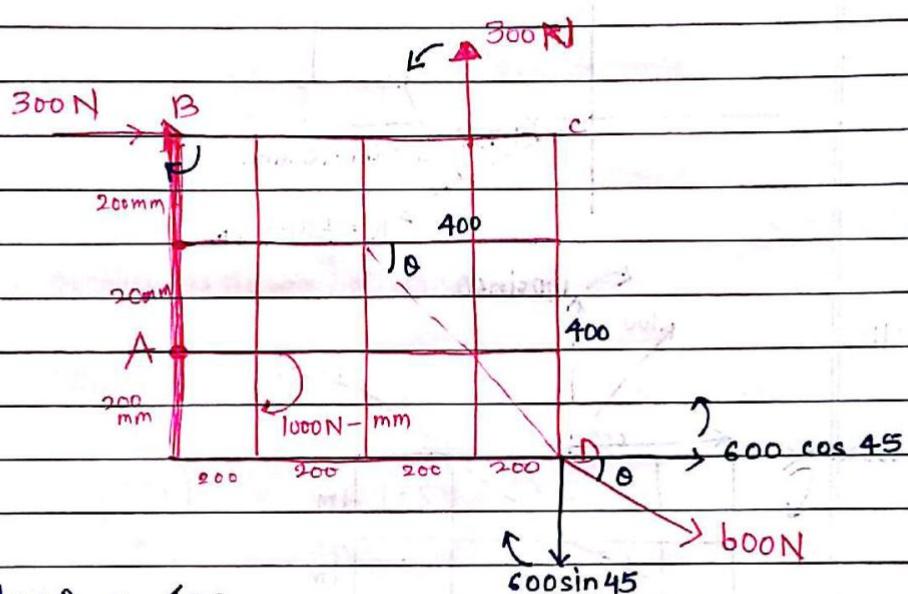
$$y\text{-intercept} = \frac{3864.21}{503.55} = 7.67 \text{ m}$$

$$R_E = \text{Equilibrium} = 748.31 \text{ N}$$



$$R = 748.31$$

(Q.10-



$$\tan \theta = \frac{400}{400}$$

$$\theta = \tan^{-1}(1) = 45^\circ$$

$$\Sigma H = 300 + 600 \cos 45 = 724.264 \text{ N}$$

$$\Sigma V = 300 - 600 \sin 45 = -124.264 \text{ N}$$

$$R = \sqrt{(724.264)^2 + (124.264)^2} = 734.84 \text{ N}$$

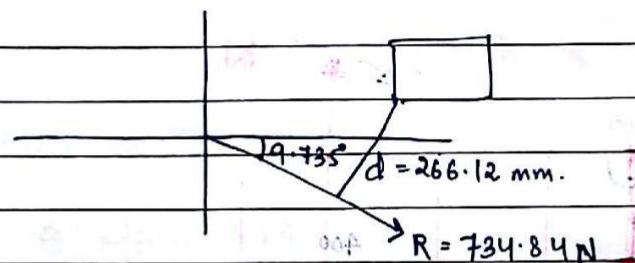
$$\theta = \tan^{-1} \left(\frac{124.264}{724.264} \right) = 9.735^\circ$$

$$\begin{aligned}
 M_A &= (300 \times 400) - 300(600) - (600 \cos 45) 200 + \\
 &\quad (600 \sin 45)(800) \\
 &= 194558.4412 \text{ N-mm} + 1000 \\
 &= 195558.4412 \text{ N-mm}
 \end{aligned}$$

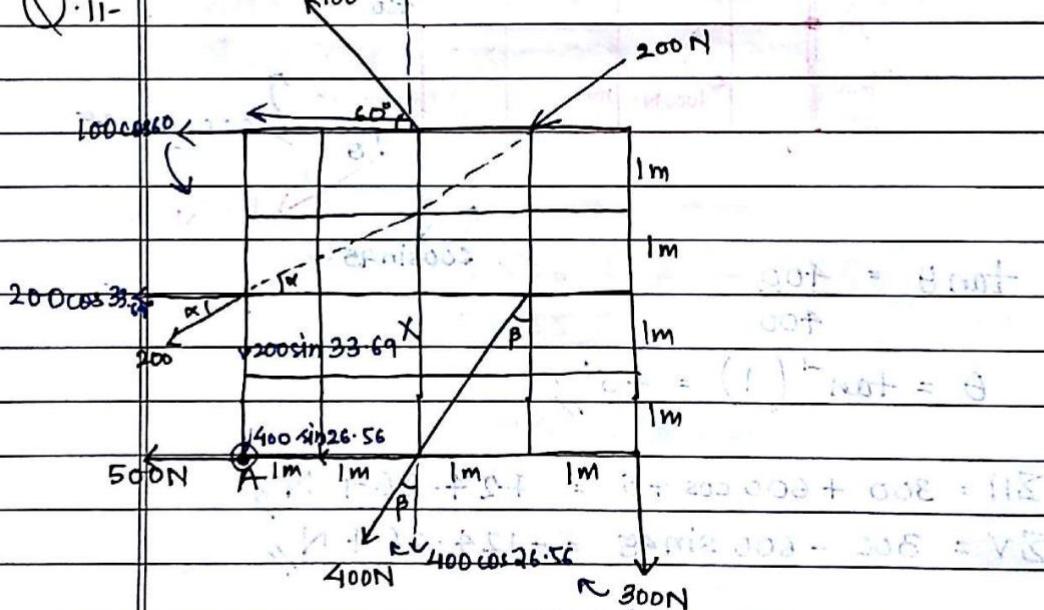
$$d = \frac{195558.4412}{734.84} = 266.12 \text{ mm}$$

$$x\text{-intercept} = \frac{195558.44}{184.264} = 1573.73 \text{ mm}$$

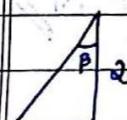
$$y\text{-intercept} = \frac{195558.44}{724.264} = 270.00 \text{ mm}$$



(Q. 11-)



Ans-



$$\tan \beta = \frac{1}{2}$$

$$\beta = \tan^{-1}(1/2) = 26.56^\circ$$

$$\tan \alpha = \frac{2}{3}$$

$$\alpha = \tan^{-1}\left(\frac{2}{3}\right) = 33.69^\circ$$

$$\begin{aligned}\Sigma H &= -500 - 200 \cos 33.69 - 100 \cos 60 - \\ &\quad 400 \sin 26.56 \\ &\quad \cancel{-850.76 N} = -895.26 N\end{aligned}$$

$$\begin{aligned}\Sigma V &= 100 \sin 60 - 200 \sin 33.69 - 400 \cos 26.56 - 300 \\ &= -682.12 N\end{aligned}$$

$$R = \sqrt{\Sigma H^2 + \Sigma V^2} = 1125.5124 N$$

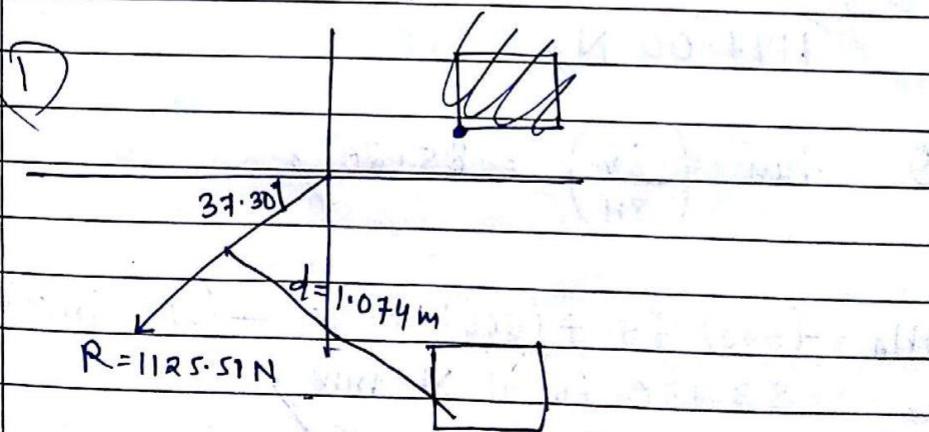
$$\theta = \tan^{-1} \left(\frac{\Sigma V}{\Sigma H} \right) = 37.30^\circ$$

$$\begin{aligned}M_A &= (-100 \sin 60) 2 - (100 \cos 60) 4 - (200 \cos 33.69) 2 \\ &\quad + (400 \cos 26.56) 2 + (300) 4 \\ &= 1209.54 Nm\end{aligned}$$

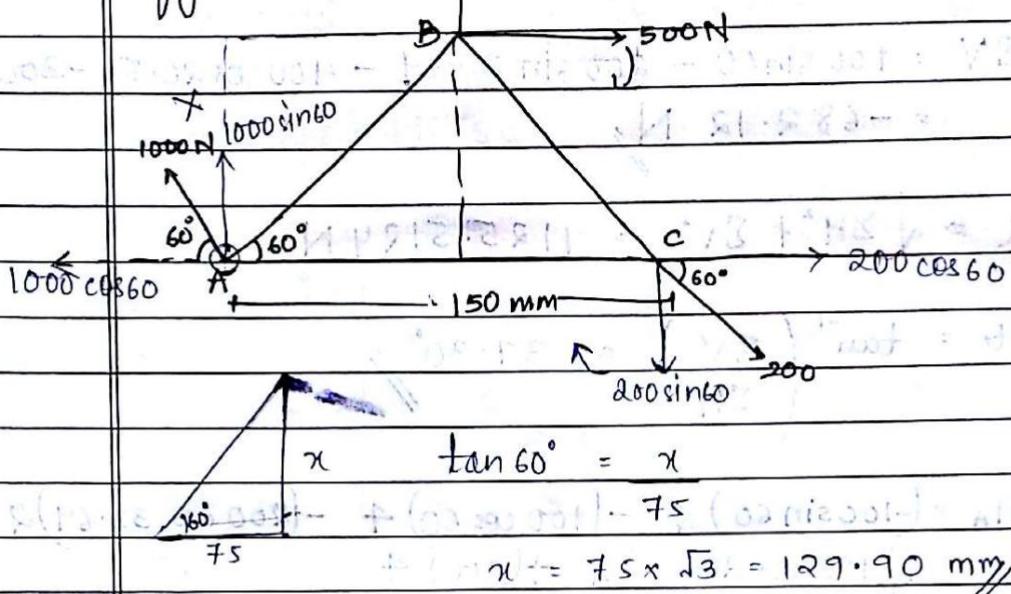
$$d = \frac{|M_A|}{R} = \frac{1209.54}{1125.5124} = 1.074 m$$

$$x\text{-intercept} = \frac{|M_A|}{\Sigma V} = \frac{1209.54}{682.12} = 1.773 m$$

$$y\text{-intercept} = \frac{|M_A|}{\Sigma H} = 1.3510 m$$



Q- Determine the resultant (a) equilibrium for a system of forces acting on an equilateral A as shown in figure:-



$$\Sigma H = 500 + 200 \cos 60 - 1000 \cos 60 \\ = 100 \text{ N}$$

$$\Sigma V = 500 - 200 \sin 60 + 1000 \sin 60 \\ = 1197.00 \text{ N}$$

$$R = \sqrt{\Sigma H^2 + \Sigma V^2}$$

$$= 1197.00 \text{ N}$$

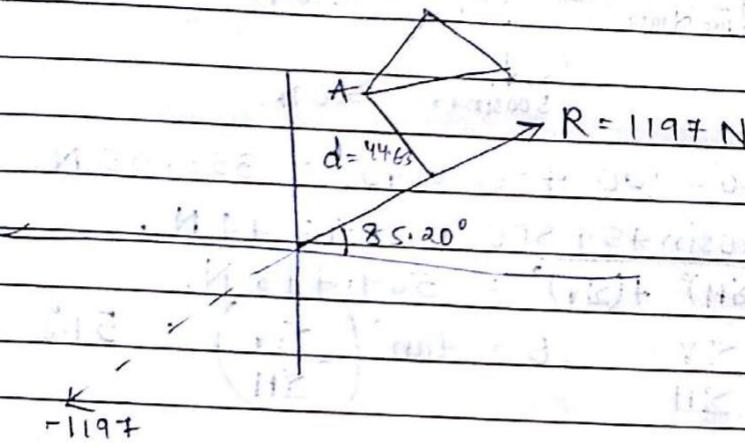
$$\theta = \tan^{-1} \left(\frac{\Sigma V}{\Sigma H} \right) = 85.20^\circ$$

$$M_A = -(500) 75 + (500) 129.90 + (200 \sin 60) 150 \\ = 53430.76211 \text{ N-mm}$$

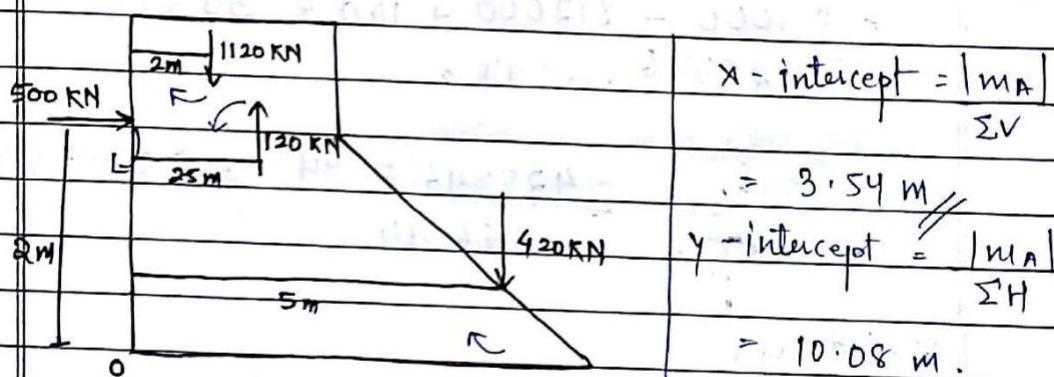
$$d = \frac{53430.76211}{1197.0} = 44.63 \text{ mm}$$

$$x\text{-intercept} = \frac{|M_A|}{\Sigma V} = \frac{534.30.7621}{1192.82} = 44.79 \text{ mm.}$$

$$y\text{-intercept} = \frac{|M_A|}{\Sigma H} = \frac{534.30.76}{1192.82} \text{ mm.}$$



(Q)

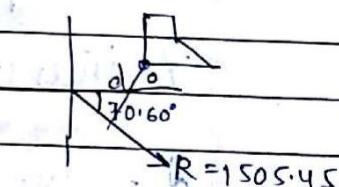


$$\Sigma H = 500 \text{ KN}$$

$$\Sigma V = -1120 + 120 - 420$$

$$= -1420 \text{ KN}$$

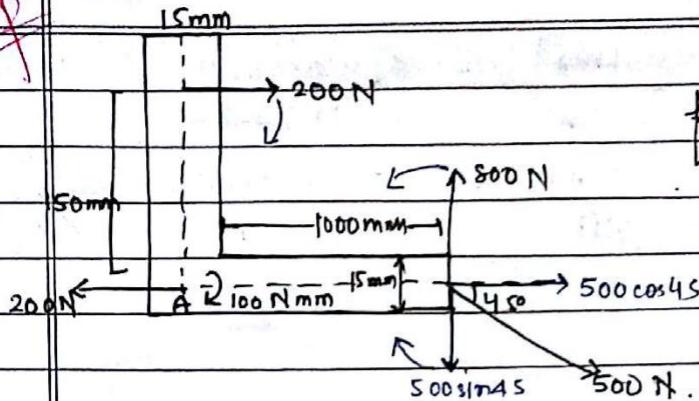
$$R = \sqrt{\Sigma H^2 + \Sigma V^2} = 1505.45 \text{ KN}$$



$$\theta = \tan^{-1} \left(\frac{\Sigma V}{\Sigma H} \right) = 70.60^\circ$$

$$M_A = (1120) \times 2 - (120) 2.5 + (420) \times 5 + (500) 2 \\ = 5040 \text{ KN-m}$$

$$d = \frac{|M_A|}{R} = \frac{5040}{1505.45} = 3.347 \text{ m}$$

~~Temp~~

find moment @ 'A'

Ans -

$$\Sigma H = 200 - 200 + 500\cos 45, = 353.55 \text{ N.}$$

$$\Sigma V = -500\sin 45 + 800 = 446.44 \text{ N.}$$

$$R = \sqrt{(\Sigma H)^2 + (\Sigma V)^2} = 569.478 \text{ N.}$$

$$\tan \theta = \frac{\Sigma V}{\Sigma H} \quad \theta = \tan^{-1} \left(\frac{\Sigma V}{\Sigma H} \right) = 51.6^\circ$$

(150+15)

$$M_A = 200 \times 150 - 800 \times (1000 + 15) + 100 + (500\sin 45) 1000 \\ = 33000 - 812000 + 100 + 353553.3906. \\ = -425346.6094 \text{ Nm}$$

$$d = \frac{M_A}{R} = \frac{-425346.6094}{446.44} = 952.75 \text{ mm.}$$

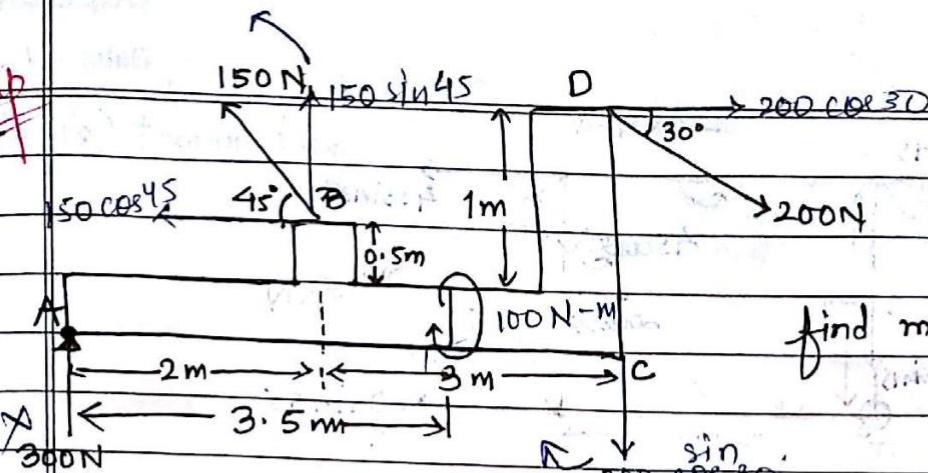
X-intercept =

$$Y \text{- intercept} = \frac{-425346.6094}{353.55} = +1203.073 \text{ mm}$$

$$d = \frac{M_A}{R} = \frac{425346.6094}{569.478} = 746.906 \text{ mm.}$$

$$R = 569.478$$





find moment @ A:

$$\text{Ans - } \sum H = -150 \cos 45 + 200 \cos 30 = 767.13 \text{ N},$$

$$\sum V = 300 + 150 \sin 45 + 200 \sin 30 = 306.06 \text{ N}$$

$$R = \sqrt{\sum V^2 + \sum H^2} = 313.335 \text{ N}$$

$$\theta = \tan^{-1} \left(\frac{\sum V}{\sum H} \right) = 77.62^\circ$$

$$\begin{aligned} M_A &= -(150 \sin 45)(2) + (200 \sin 30)(3+2) - \\ &\quad (150) \cos 45 \times 0.5 + 100 + 200 \cos 30 \times (1+0.5) \\ &= 508.040 \text{ Nm} \end{aligned}$$

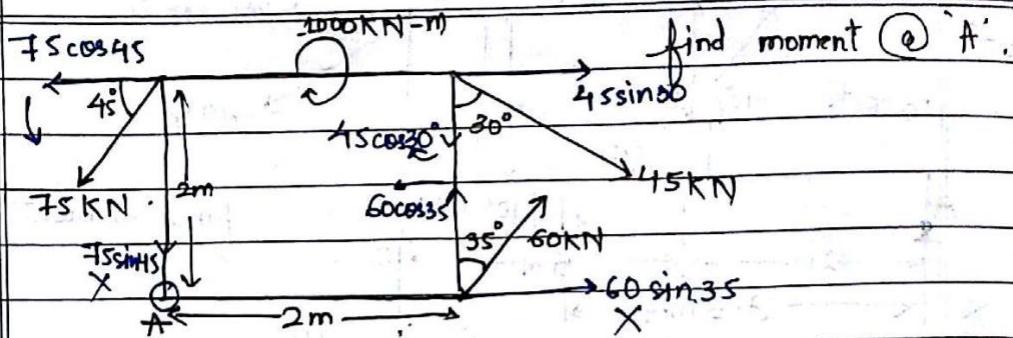
$$d = \frac{508.04}{313.335} = 1.621 \text{ m}$$

$$x\text{-intercept} = \frac{508.04}{306.06} = 1.660 \text{ m}$$

$$y\text{-intercept} = \frac{508.40}{67.13} = 7.573 \text{ m}$$

$$313.335 \text{ N}$$

Q-

Ans -

$$\Sigma H = 45 \sin 30 + 60 \sin 35 - 75 \cos 45$$

$$\therefore = 3.881 \text{ KN}$$

$$\Sigma V = -75 \sin 45 + 60 \cos 35 - 45 \cos 30 = -42.855 \text{ KN}$$

$$R = \sqrt{\Sigma H^2 + \Sigma V^2} = \sqrt{(42.85)^2 + (3.88)^2} = 43.030 \text{ KN}$$

$$\theta = \tan^{-1} \left(\frac{\Sigma V}{\Sigma H} \right) = \tan^{-1} \left(\frac{42.855}{3.881} \right) = 84.82^\circ$$

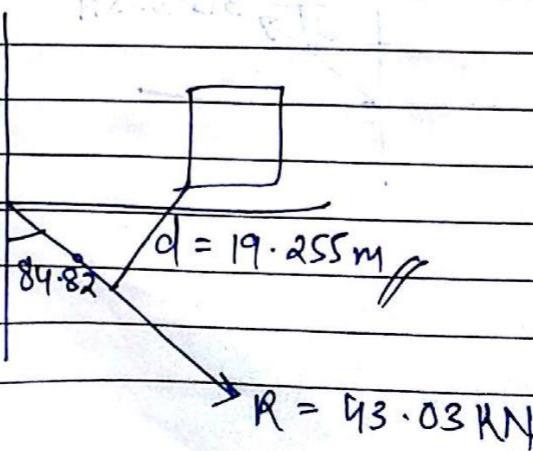
$$M_A = -(75 \cos 45) \alpha - (60 \cos 35) \alpha + (45 \cos 30) \alpha - (45 \sin 30) \alpha + 1000$$

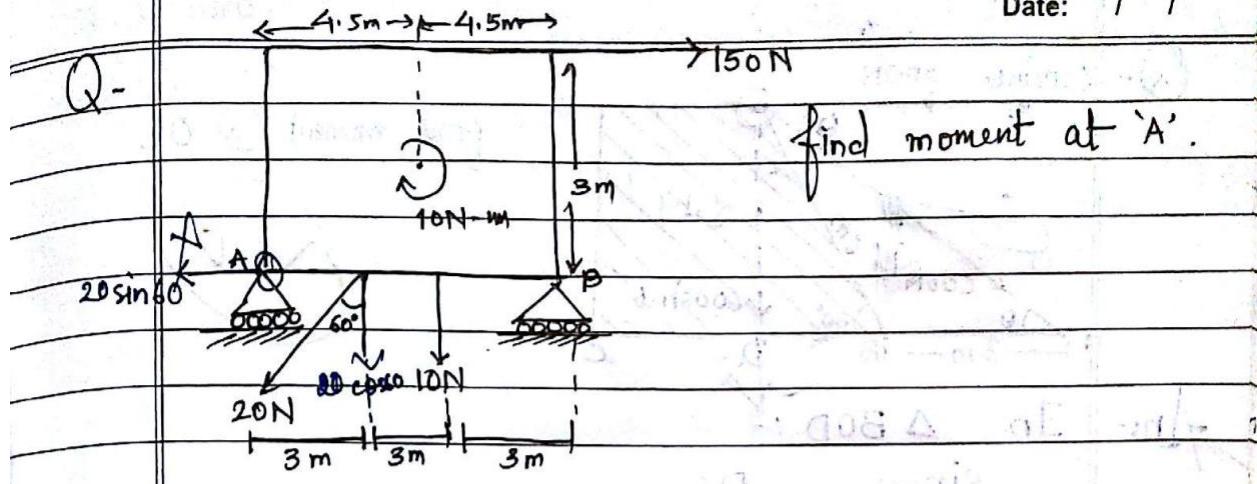
$$\Rightarrow 828.578 \text{ Nm}$$

$$d = \frac{828.578}{43.03} = 19.255 \text{ m}$$

$$x\text{-intercept} = \frac{828.578}{42.855} = 19.3344 \text{ m}$$

$$y\text{-intercept} = \frac{828.578}{3.881} = 213.496 \text{ m}$$





$$\Sigma H = 150 - 20 \sin 60 = 132.679 \text{ N}$$

$$\Sigma V = -10 - 20 \cos 60 = -20 \text{ N}$$

$$R = \sqrt{\Sigma V^2 + \Sigma H^2} = 134.1779 \text{ N}$$

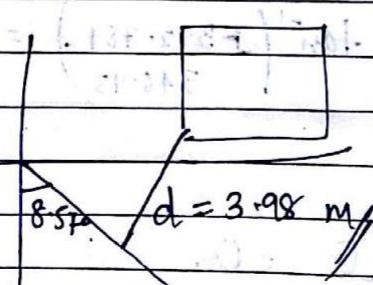
$$\theta = \tan^{-1} \left(\frac{20}{132.679} \right) = 8.57^\circ$$

$$M_A = 150 \times 3 + (10 \times 4.5) + 10 + (20 \cos 60) \times 3 \\ = 535 \text{ Nm}$$

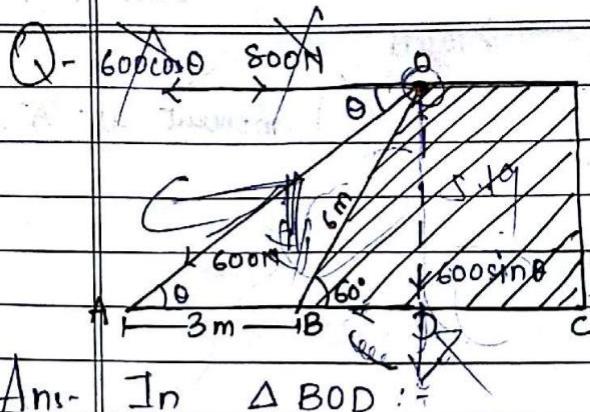
$$d = \frac{535}{134.17} = 3.98 \text{ m}$$

$$x\text{-intercept} = \frac{535}{20} = 26.75 \text{ m}$$

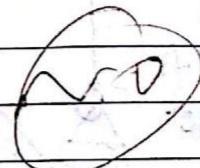
$$y\text{-intercept} = \frac{535}{132.679} = 4.032 \text{ m}$$



134.1779 N



find moment @ O.



Ans- In $\triangle BOD$:

$$\sin 60 = \frac{DO}{6}$$

$$DO = 5.196 \text{ m} //$$

$$\cos 60 = \frac{BD}{6} = \frac{\sqrt{2^2 + 3^2}}{6} = \frac{\sqrt{13}}{6}$$

$$BD = 3 \text{ m} //$$

Q. In $\triangle ADO$:

$$\tan \theta = \frac{OD}{AD} = \frac{5.196}{3+3} = \frac{5.196}{6}$$

$$\theta = 40.892^\circ //$$

$$\Sigma H = 800 - 600 \cos(40.892)$$

$$= 346.43 \text{ N} //$$

$$\Sigma V = -600 \sin(40.892) = -392.781 \text{ N}$$

$$R = \sqrt{\Sigma H^2 + \Sigma V^2} = 523.727 \text{ N} //$$

$$\theta = \tan^{-1} \left(\frac{\Sigma V}{\Sigma H} \right) = \tan^{-1} \left(\frac{-392.781}{346.43} \right) = 48.58^\circ //$$

$$M_O = 0 //$$

$$d = \frac{M_A}{R} = \frac{0}{R} = 0,$$

$$x\text{-intercept} = \frac{M_A}{\Sigma V} = \frac{0}{\Sigma V} = 0 //$$

$$\text{Y-intercept} \Rightarrow \frac{ma}{\sum H} = 0$$

Support and Support Reaction

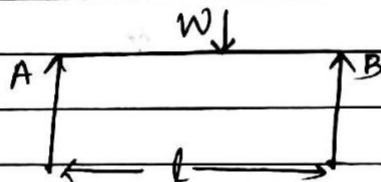
2/5/17

- Define beam on an horizontal member and what are the different types of beam.

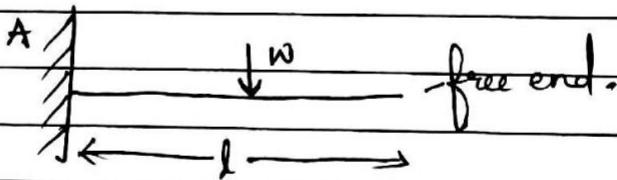
A beam is a structural member which is having longer length compared to its width or depth. It is also called as horizontal member.

Different Types of Beam :-

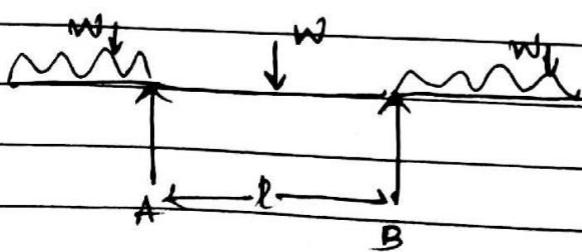
- (1) Simply Supported Beam: In this beam both ends of the beam are simply supported



- (2) Cantilever Beam :- In this beam, one end of the beam is supported and the other end is left free.



- (3) Over hanging Beam :- In this beam, a part of the beam overhangs at one end or both the ends.



45

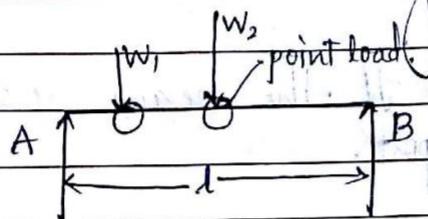
• DIFFERENT TYPES OF LOADINGS :-

(1) Point Load

(2) Uniformly Distributed Load.

(3) Uniformly Varying Load.

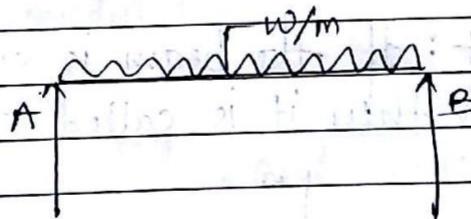
POINT LOAD :- Load is acting at a point on a beam.



Example :- two person standing on the beam.

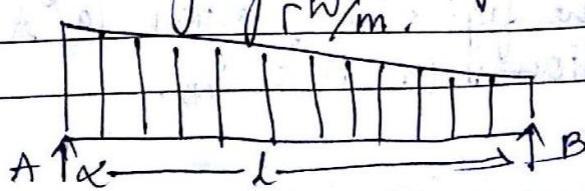
UNIFORMLY DISTRIBUTED LOAD :- Load which has got same intensity over a considerable length is called as uniformly distributed load. (UDL).

Example :- Brick wall constructed on a beam.



UNIFORMLY VARYING LOAD :- Intensity of the load increases linearly along the length is called as uniformly varying load. (UVL).

Example:- Brick Wall constructed on a beam carrying a slopy roof.

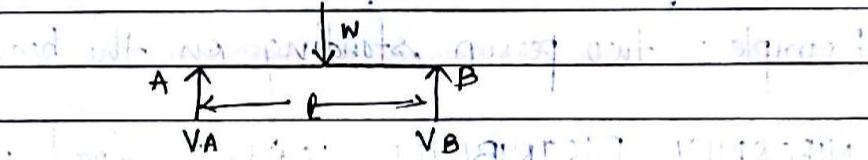


SUPPORTS :-

The diff types of supports are :-

- (1) Simply Support
- (2) Roller Support
- (3) Flanged Support
- (4) Fixed Support
- (5) Continuous Support.

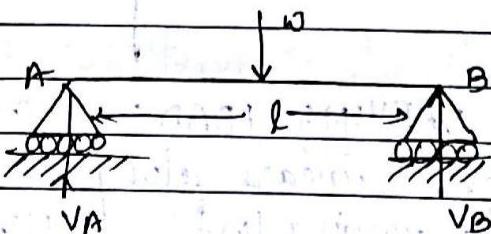
(1) Simply Support : If the beam rests simply on a support.



For a simply supported there will be only one reaction which is acting vertically upwards

From the fig. the reaction @ A is V_A and reaction @ B is V_B .

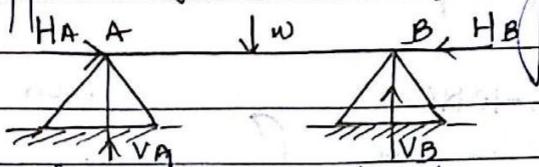
(2) Roller Support : If the beam is supported on the roller, then it is called as roller support



For roller support there will be only one reaction which is acting vertically upward

From the fig. the reaction @ A is V_A and reaction @ B is V_B .

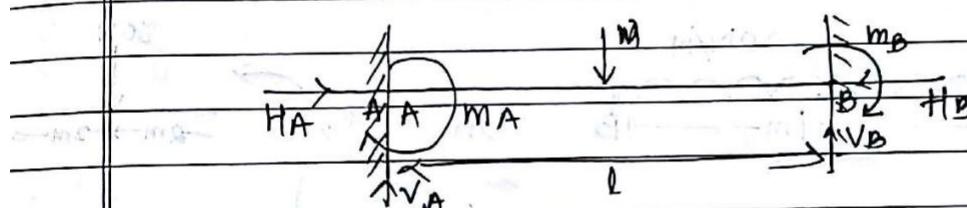
(3) Hinged Support :- If the beam is supported on the hinge or a pin then that type of support is called as hinged support.



For the hinged support there will be 2 reaction ie vertically upwards and horizontally inwards.

From the fig. - the reaction @ A is V_A and H_A and reaction @ B is V_B or H_B .

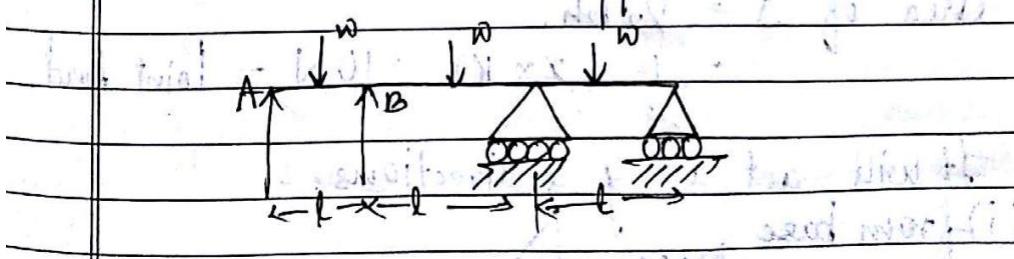
(4) Fixed Support :- If the beam is supported on one end or both the ends.



For the fixed support, there will be 3 reaction ie vertically upwards and horizontally inwards and moment.

From the fig. - the reaction @ A are V_A , H_A and M_A and reactions @ B are V_B , H_B and m_B .

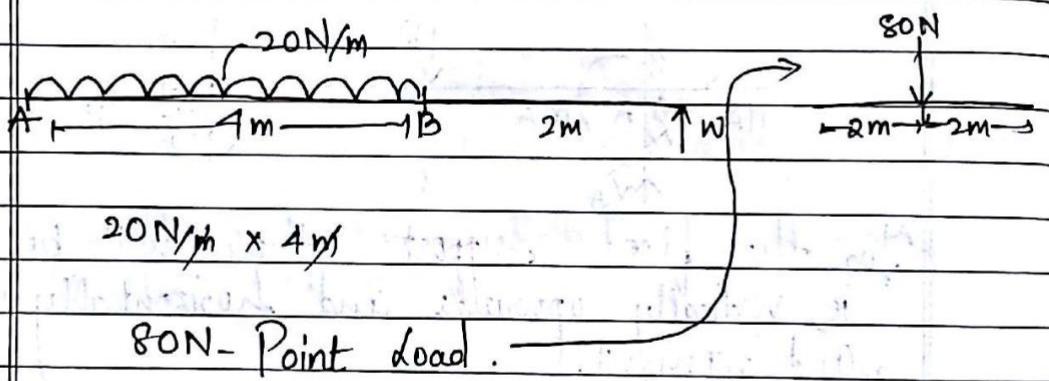
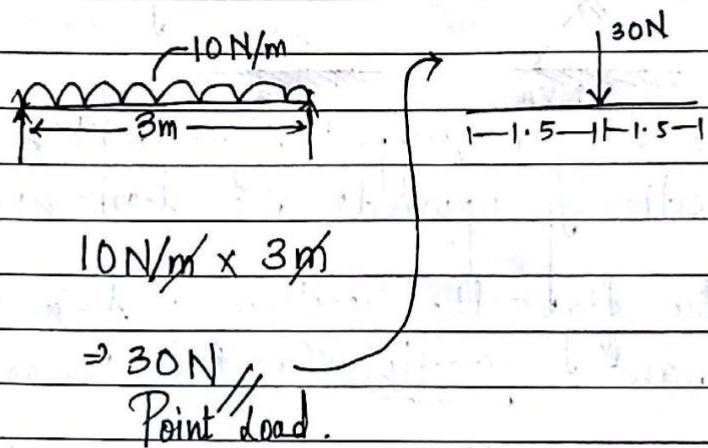
(5) CONTINUOUS SUPPORT :- If the beam is having 3 or more support.



~~5 5 ft~~

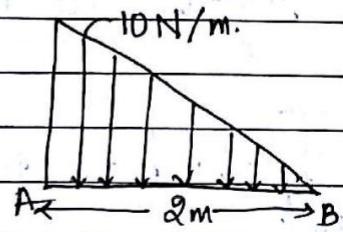
• NOTE:

(1) CONVERTING UDL TO POINT LOAD :-



(2) CONVERTING UVL TO POINT LOAD :-

(1)

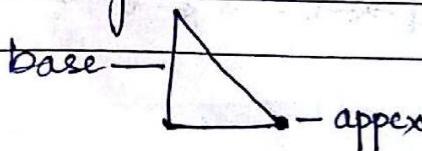


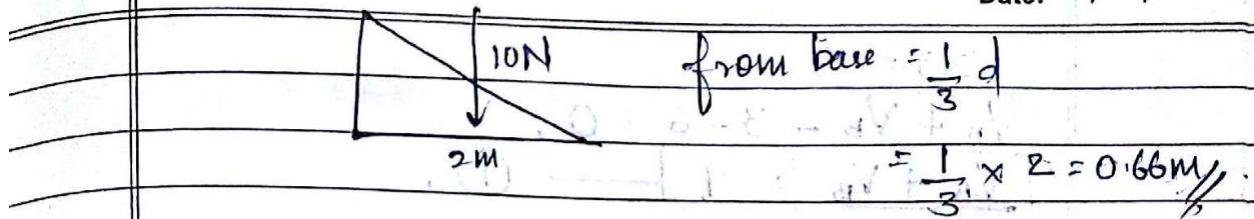
$$\text{Area of } \Delta = \frac{1}{2}bh.$$

$$= \frac{1}{2} \times 2 \times 10 = 10 \text{ N} - \text{Point Load.}$$

It will act along 2 directions:-

(i) from base

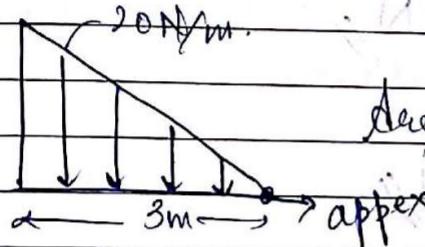




from apex = $\frac{2}{3} d$

$\frac{2}{3} \times 2 = 1.33\text{m}$

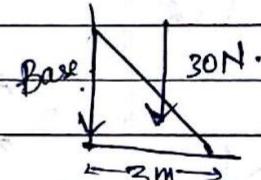
(II)



Point Load.

from base :- $\frac{1}{3} d$

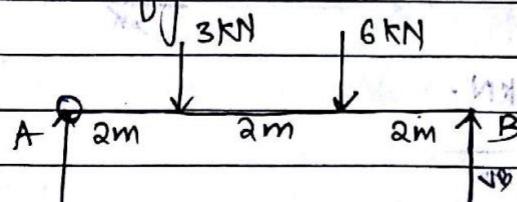
$\frac{1}{3} \times 3 = 1\text{ m}$



from apex = $\frac{2}{3} d \Rightarrow \frac{2}{3} \times 3 = 2\text{ m}$

distance from base + distance from apex = span

Q. Find the support and support reaction for the beam shown in figure :-



Support @ A - simply support \rightarrow vertically upwards.
 @ B - simply support \rightarrow vertically upwards V_A .

$$\sum V = 0$$

$$V_A + V_B - 3 \cdot 6 = 0$$

$$V_A + V_B = 18 \quad \text{--- (1)}$$

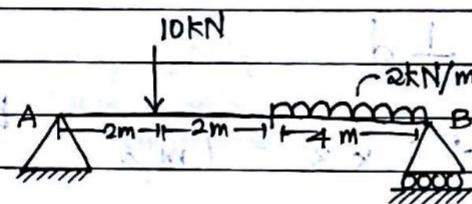
$$\sum M_A = 0$$

$$(-V_B \cdot 6) + 6 \cdot 4 + 3 \cdot 2 = 0$$

$$6 V_B = 24 + 6$$

$$V_B = \frac{30}{6} = 5 \text{ kN}$$

$$V_A = 9 - 5 = 4 \text{ kN}$$

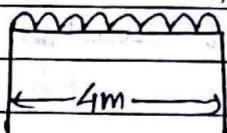


Support @ A - hinged support $\rightarrow V_A, H_A$

@ B - roller support $\rightarrow V_B \uparrow$

$$H_A = ? \quad V_A = ? \quad V_B = ?$$

$\sim 2 \text{ kNm}$

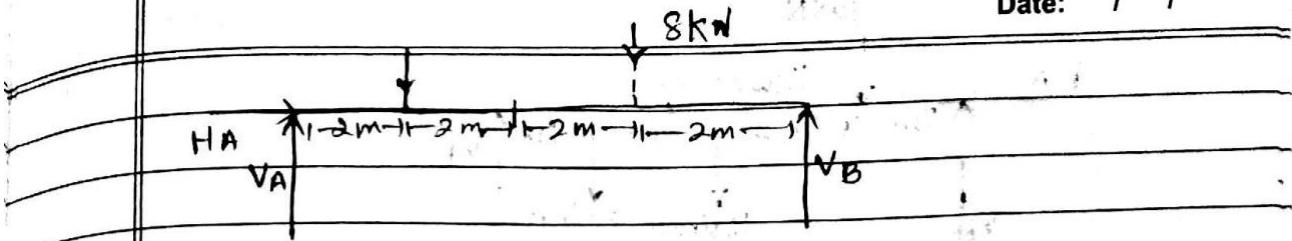


$$\text{Point Load} = 2 \text{ kN} \times 4 \text{ m} = 8 \text{ kN}$$

8 kN.

2m 1am.

Afterwards \rightarrow Free body diagram \rightarrow A is free.



$$\sum H = 0.$$

$$[H_A = 0 \text{ kN.}]$$

$$\sum V = 0.$$

$$\boxed{V_A + V_B - 10 - 8 = 0}$$

$$\Rightarrow V_A + V_B = 18 \text{ kN}$$

$$\sum M_A = 0.$$

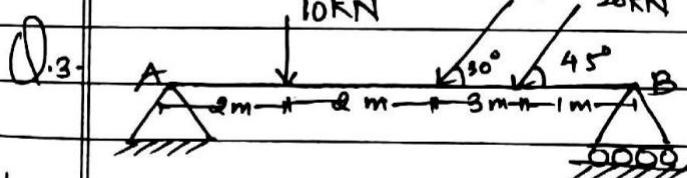
$$- V_B \times 8 + 8 \times 6 + 10 \times 2 = 0,$$

$$V_B \times 8 = 68$$

$$V_B = \frac{68}{8} = 8.5 \text{ kN.}$$

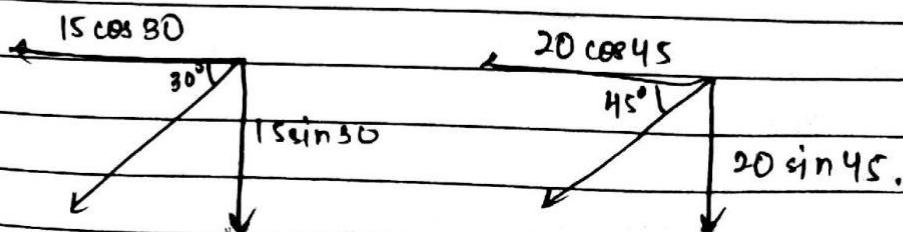
Substituting the value.

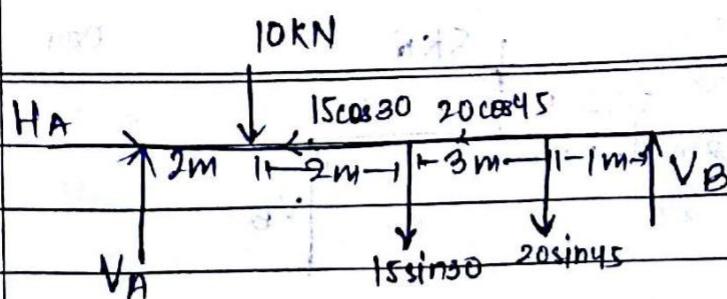
$$V_A = 18 - 8.5 = 9.5 \text{ kN.}$$



- Ans-
- ① Support @ A - hinged support $\rightarrow \uparrow V_A, \rightarrow H_A$.
 - ② Support @ B - roller support $\rightarrow V_B \uparrow$.

$$H_A = ?, V_A = ?, V_B = ?$$





$$\sum H = 0,$$

$$H_A - 15\cos 30 - 20\cos 45 = 0$$

$$H_A = 27.13 \text{ kN},$$

$$\sum V = 0.$$

$$\Rightarrow V_B + V_A - 10 - 15\sin 30 - 20\sin 45 = 0$$

$$\Rightarrow V_A + V_B = 31.64 \text{ kN} \quad \text{--- (1)}$$

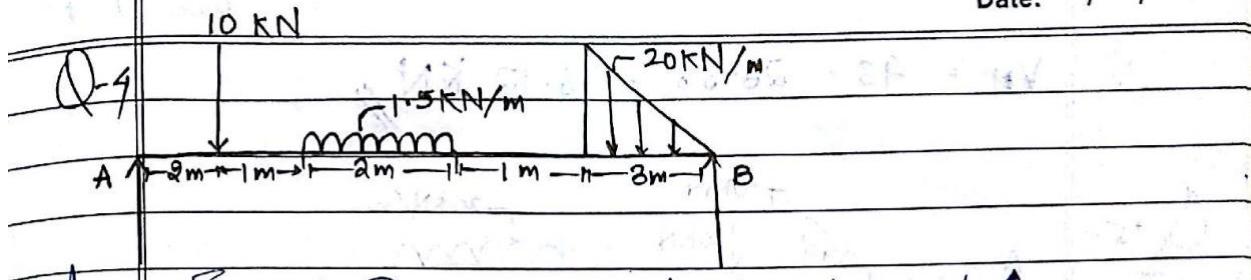
$$\sum M_A = 0,$$

$$\Rightarrow -V_B \times 8 + (20\sin 45) 7 + (15\sin 30) 4 + 10 \times 2 = 0$$

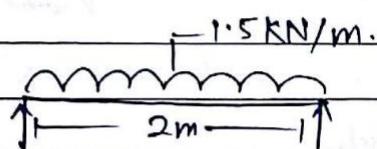
$$\Rightarrow V_B \times 8 = 148.99$$

$$\Rightarrow V_B = 148.99 / 8 = 18.62 \text{ kN}$$

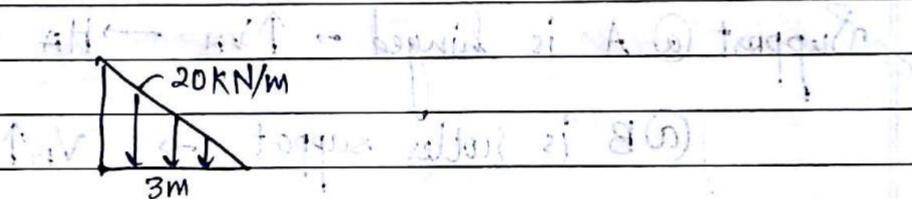
$$\therefore V_A = 31.64 - 18.62 = 13.02 \text{ kN}$$



Ans - Support @ A → simply support $\rightarrow V_A \uparrow$
 @ B → simply support $\rightarrow V_B \uparrow$.



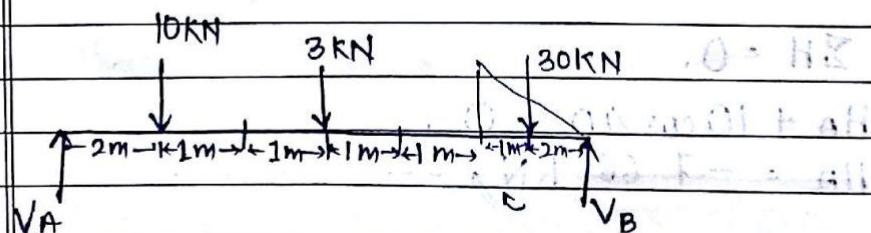
Point load $= 1.5 \text{ kN} \times 2\text{m} = 3 \text{ kN}$



Point load $= \frac{1}{3} \times b \times h = \frac{1}{3} \times 3 \times 10 = 30 \text{ kN}$

from base $= \frac{1}{3} \times d = \frac{1}{3} \times 3 = 1 \text{ m}$

from apex $= \frac{2}{3} \times d = \frac{2}{3} \times 3 = 2 \text{ m}$



$$\sum V = V_A + V_B - 10 - 3 - 30$$

$$\Rightarrow O = V_A + V_B - 43$$

$$\Rightarrow V_A + V_B = 43 \text{ kN} \quad \text{--- (1)}$$

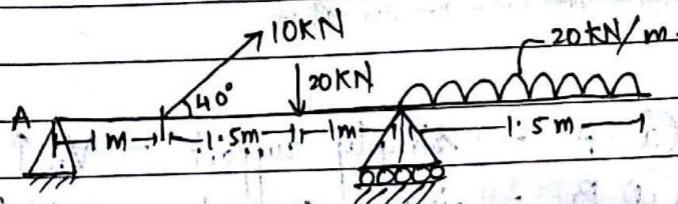
$$\sum M_A = 0$$

$$\Rightarrow V_B \times 9 + 30 \times 7 + 3 \times 4 + 10 \times 2 = 0$$

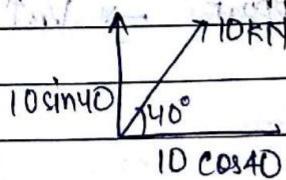
$$\Rightarrow V_B \times 9 = 242 \Rightarrow V_B = \frac{242}{9} = 26.88 \text{ kN}$$

$$\therefore V_A = 43 - 26.88 = 16.12 \text{ KN} //$$

Q. 5-



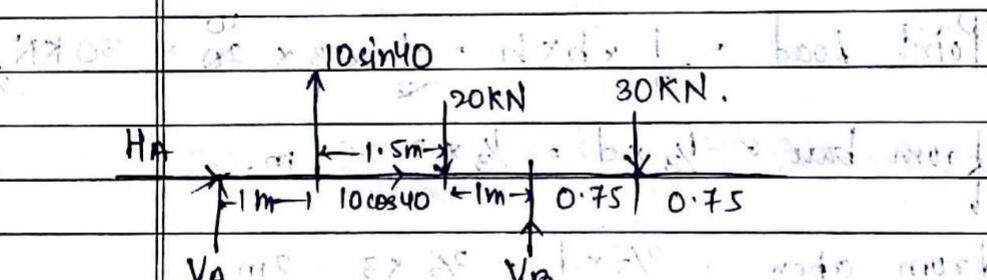
Ans -



$$\text{Spring force} = 20 \text{ kN/m} \times 1.5 \text{ m} = 30 \text{ kN.}$$

Support @ A is hinged $\rightarrow \uparrow V_A \rightarrow H_A$

@B is roller support $\rightarrow V_B \uparrow$.



$$\sum H = 0.$$

$$H_A + 10\cos 40 = 0$$

$$H_A = -7.66 \text{ KN}$$

$$\sum V = 0.$$

$$\Rightarrow V_A + V_B + 10\sin 40 - 30 - 20 = 0 \quad \text{Ans}$$

$$\Rightarrow V_A + V_B = 43.572 \text{ KN} \quad \text{Ans} \quad \text{①}$$

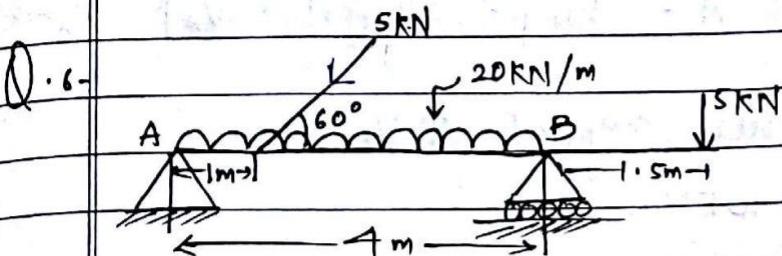
$$\sum M_A = 0$$

$$\Rightarrow (30) \times 10.41 - V_B \times 9.66 + 20(10.640 + 1)$$

$$\Rightarrow 30 \times 4.05 - V_B \times 3.5 + 20 \times 2.5 - 10 \sin 40 \times 1 = 0$$

$$\Rightarrow V_B = \frac{171.072}{3.5} = 48.87 \text{ KN} \quad //$$

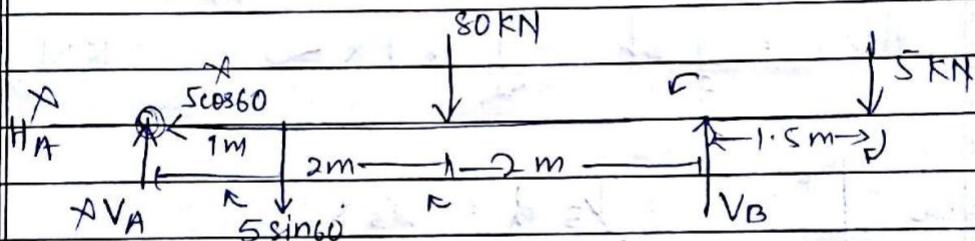
$$V_A = 43.57 - 48.87 = -5.3 \text{ KN} \quad //$$



~~Support @ A is hinged $\rightarrow V_A \uparrow \rightarrow H_A$~~

~~(a) B is roller support $\rightarrow V_B \uparrow$~~

$$\begin{array}{c} 20 \text{ kN/m} \\ \downarrow \\ \text{mmmm} \\ \xleftarrow[4 \text{ m}]{} \end{array} \rightarrow 20 \text{ kN} \times \frac{4 \text{ m}}{\text{m}} = 80 \text{ KN} \quad //$$



$$\sum H = 0$$

$$\Rightarrow H_A - 5 \cos 60 = 0$$

$$\Rightarrow H_A = 2.5 \text{ KN} \quad //$$

$$\sum V = 0$$

$$\Rightarrow V_A + V_B - 5 \sin 60 - 80 - 5 = 0$$

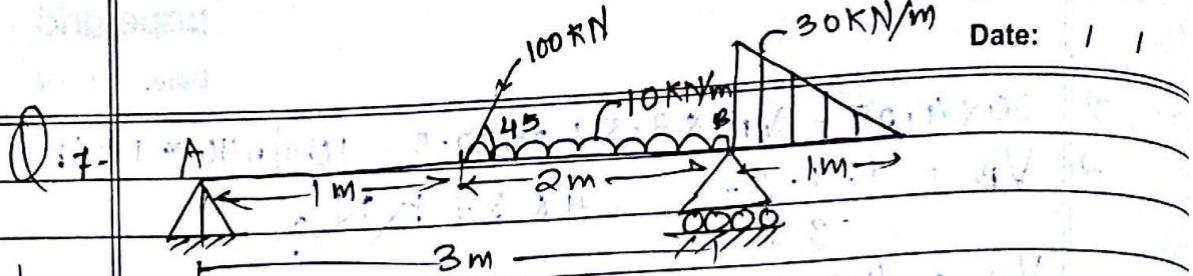
$$\Rightarrow V_A + V_B = 89.3301 \quad \text{--- (1)}$$

$$\sum M_A = 0$$

$$\Rightarrow (5 \sin 60) 1 + (80) 2 - (V_B) 4 + (5)(5.5) = 0$$

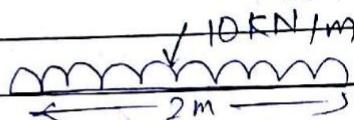
$$\Rightarrow V_B = 47.957 \text{ KN} \quad //$$

$$\therefore V_A = 89.3301 - 47.957 = 41.3731 \text{ KN} \quad //$$

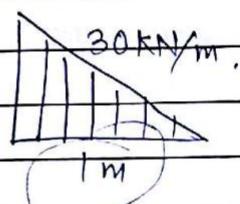


Q: 7. \checkmark Support @ A - hinged support $\rightarrow V_A \uparrow H_A \rightarrow$

@ B - roller support $\uparrow V_B$.



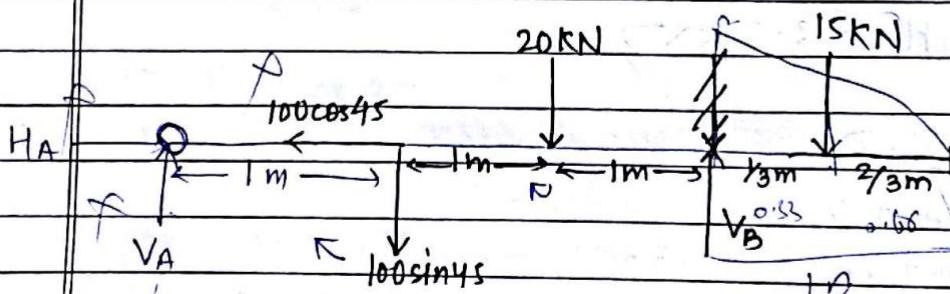
$$\text{Point Load} = \frac{10 \text{ kN}}{\text{m}} \times 2 \text{ m} = 20 \text{ kN} //.$$



$$\text{Area} = \frac{1}{2} b h = \frac{1}{2} \times 1 \times 30 = 15 \text{ kN} //.$$

$$\text{from base } = \frac{1}{3} d = \frac{1}{3} \times 1 = 0.3$$

$$\text{from apex} = \frac{2}{3} d = \frac{2}{3} \times 1 = 0.6$$



$$\sum H = 0$$

$$\Rightarrow H_A - 100 \cos 45^\circ = 0.$$

$$\Rightarrow H_A = 70.71 \text{ KN} //$$

$$\sum V = 0$$

$$\sum V = 0$$

$$\Rightarrow A V_A - 100 \sin 45 - 20 + V_B - 15 = 0$$

$$\Rightarrow V_A + V_B = 105 + 10 \quad \text{--- (1)}$$

$$\sum M_A = 0$$

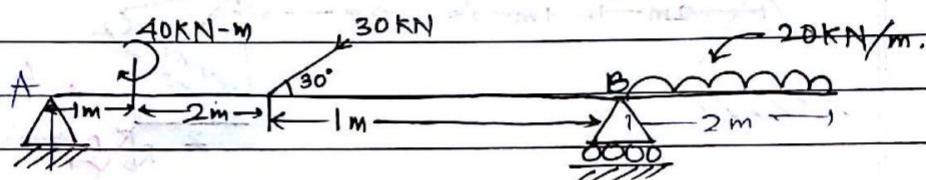
$$\Rightarrow (100 \sin 45) 1 + (20) 2 - 3 V_B + (15) \cancel{(-3)} (3 \cdot 33) = 0$$

$$\Rightarrow 3 V_B = 160.66$$

$$\Rightarrow V_B = 160.66 = 53.55 \text{ KN}$$

$$V_A = 105 + 10 = 53.55 = 52.16 \text{ KN}$$

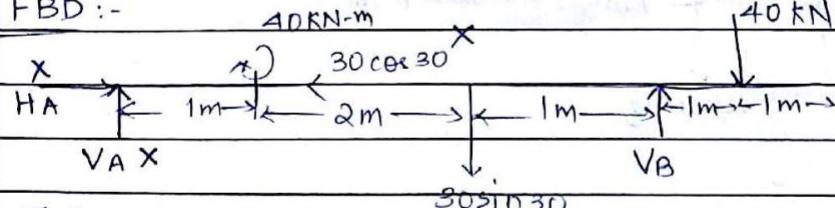
Q.8-



Anc. Support @ A is hinged $\rightarrow V_A \rightarrow H_A$,
 @ B is roller $\rightarrow V_B$.

$$\text{Point load} \Rightarrow \frac{20 \text{ KN} \times 2 \text{ m}}{\text{m}} = 40 \text{ KN}$$

FBD :-



$$\sum H = H_A - 30 \cos 30$$

$$\Rightarrow 0 = H_A - 25.98$$

$$\Rightarrow H_A = 25.98 \text{ KN}$$

$$\sum V = 0$$

$$\Rightarrow V_A - 30 \sin 30 + V_B - 40 = 0$$

$$\Rightarrow V_A + V_B = +55 \quad \text{--- (1)}$$

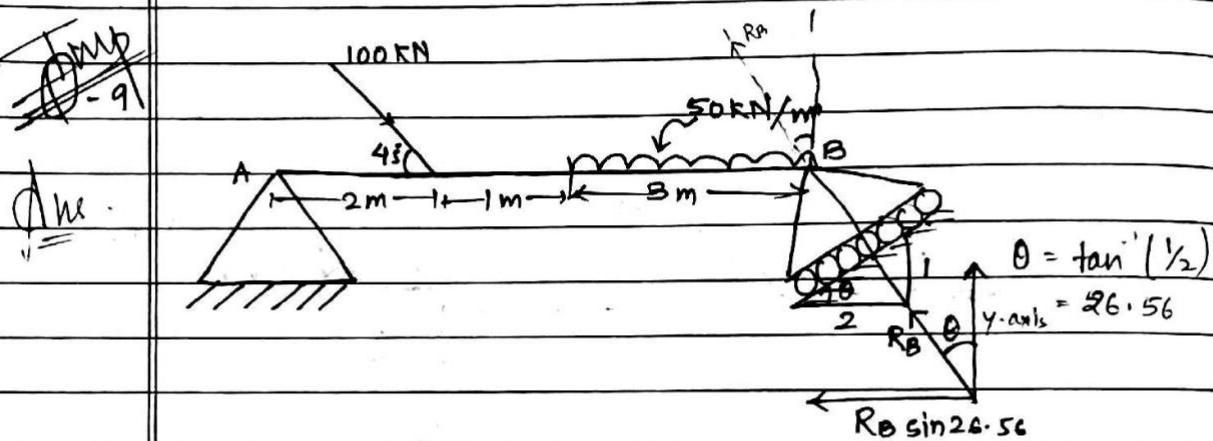
$$\sum M_A = 0$$

$$\Rightarrow 40 + (30 \sin 30) 3 - (V_B) 4 + (40) 5 = 0$$

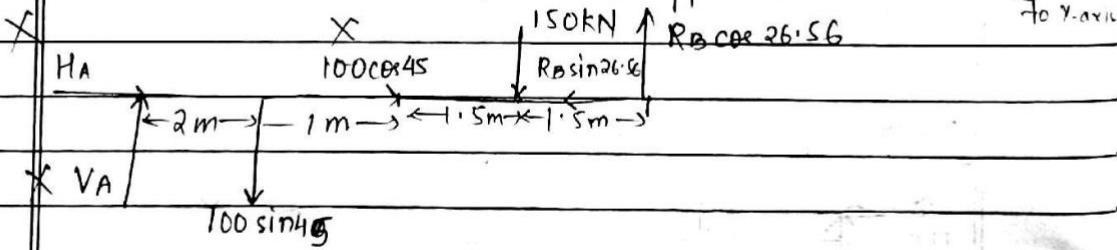
$$\Rightarrow 4 V_B = 285 \Rightarrow V_B = 71.25 \text{ KN}$$

$$\Rightarrow V_A + V_B = 55$$

$$\Rightarrow V_A = 55 - V_B = 55 - 71.25 = -16.25 \quad //$$



~~Support A is hinged support $\uparrow V_A H_A \rightarrow$~~
~~Support B is roller support R_B inclined $\angle 26.56^\circ$ to Y-axis~~



$$\Sigma V = 0$$

$$\Rightarrow V_A - 100 \sin 45 - 150 + R_B \cos 26.56 = 0$$

$$\Rightarrow V_A + R_B \cos 26.56 = 220.71 \quad \text{--- (1)}$$

$$\Sigma H = 0$$

$$H_A + 100 \cos 45 - R_B \sin 26.56 = 0$$

$$\Rightarrow H_A - R_B \sin 26.56 = -70.71 \quad \text{--- (2)}$$

$$\sum m_A = (100 \sin 45) 2 + (150)(4.5) - (R_B \cos 26.56) 6 = 0$$

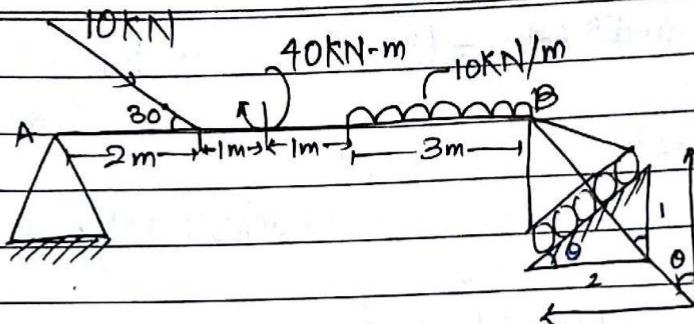
$$\Rightarrow R_B \cos 26.56 \cdot 6 = 816.421$$

$$\Rightarrow R_B = \frac{816.421}{6 \cos 26.56} = 152.124 \text{ KN} //$$

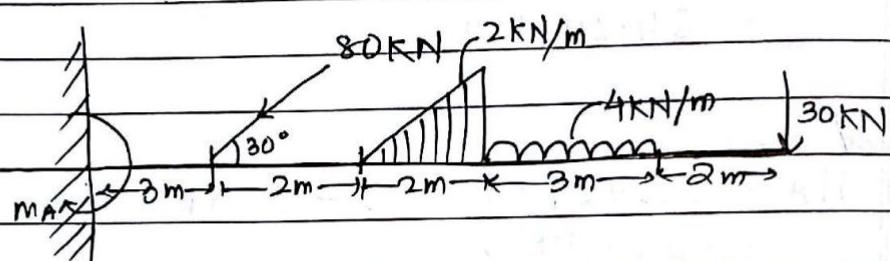
$$\begin{aligned}\Rightarrow V_A &= 220.710 - R_B \cos 26.56 \\ &= 220.710 - (152.124) \cos 26.56 \\ &= 84.64 \text{ KN}\end{aligned}$$

$$\begin{aligned}\Rightarrow H_A &= 152.124 \sin 26.56 - 70.71 \\ &= -2.69 \text{ KN} //\end{aligned}$$

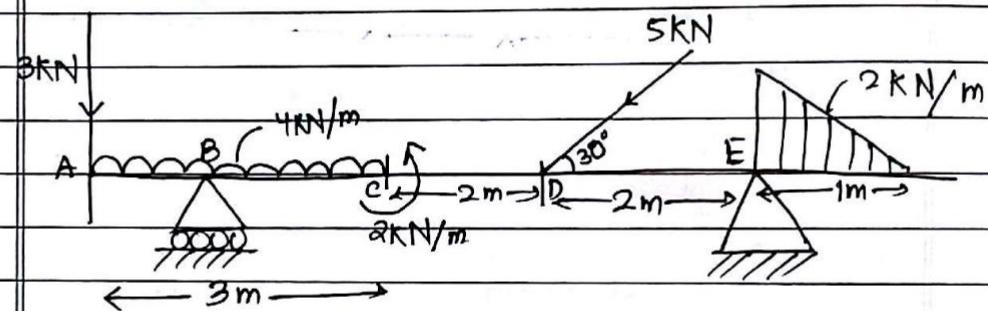
Q.1-



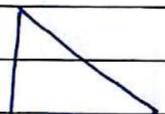
Q.2-



Q.3-



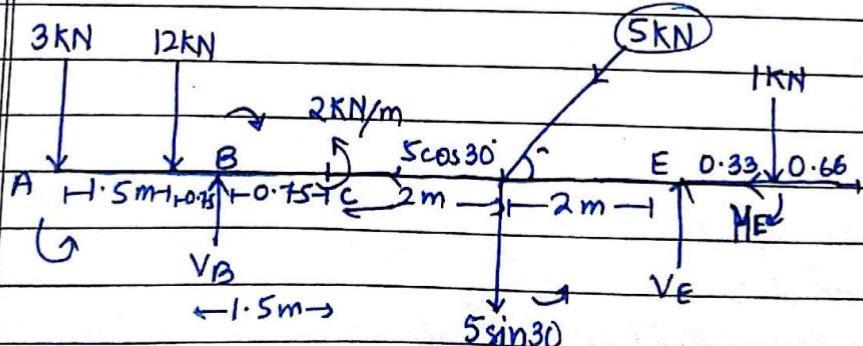
Ans 3 Point load = $4 \times 3 = 12 \text{ kN}$.



$$\frac{1}{2}bh = \frac{1}{2} \times 1 \times 2 = 1 \text{ kN}$$

from apex = $\frac{2}{3}d = \frac{2}{3} \times 1 = 0.66$

from base = $\frac{1}{3}d = \frac{1}{3} \times 1 = 0.33$.



$$\sum H = 0.$$

$$\Rightarrow H_E - 5 \cos 30 = 0$$

$$\Rightarrow H_E = -4.330 \text{ kN} //$$

$$\Rightarrow \sum V = 0$$

$$\Rightarrow -3 - 12 + V_B - 5 \sin 30 + V_E - 1 = 0$$

$$\Rightarrow V_B + V_E = 18.5 \text{ kN}$$

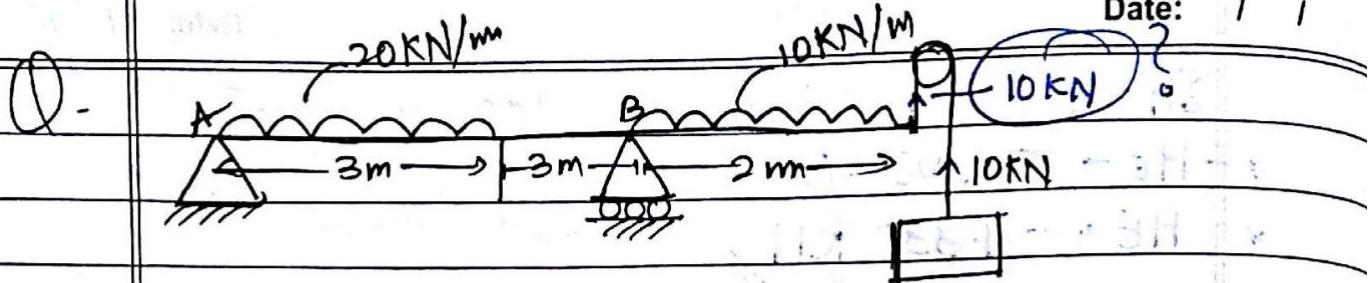
$$\Rightarrow \sum M_E = 0$$

$$\Rightarrow -(3)7 - (12)5.5 + (V_B)4.75 - 2 - (5 \sin 30)2 + (1)0.33 \\ = 0$$

$$\Rightarrow -21 - 66 + 4.75 V_B - 2 - 5 + 0.33 = 0$$

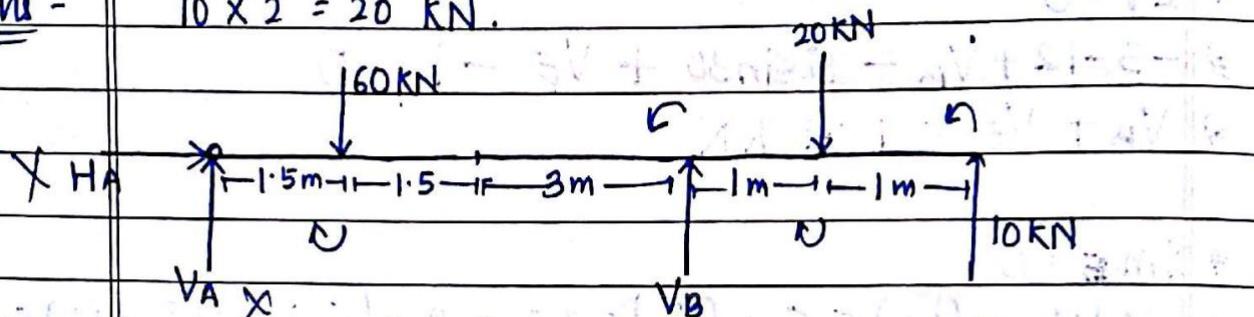
$$\Rightarrow V_B = 19.72 \text{ kN} //$$

$$\therefore V_E = 18.5 - 19.72 = -1.22 \text{ kN} //$$



$$20 \times 3 = 60 \text{ kN.}$$

$$10 \times 2 = 20 \text{ kN.}$$



$$\sum H = 0.$$

$$\Rightarrow H_A = 0.$$

$$\sum V = 0.$$

$$\Rightarrow V_A - 60 + V_B - 20 + 10 = 0$$

$$\Rightarrow V_A + V_B = 60 + 10 \Rightarrow V_A + V_B = 70 \quad \text{--- (1)}$$

$$\sum m_A = 0$$

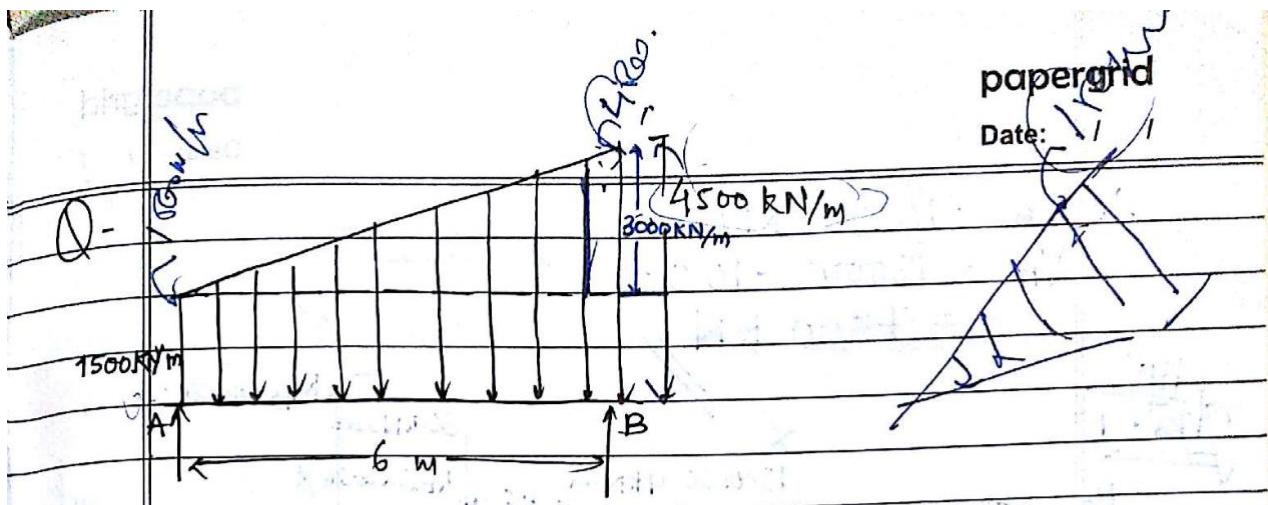
$$\Rightarrow (60) 1.5 - (V_B) (6) + (20)(7) - (10) 8 = 0$$

$$\Rightarrow \frac{150}{6} = V_B$$

$$\Rightarrow V_B = 25 \text{ kN} //$$

$$V_A = 70 - 25 = 45 \text{ kN} //$$

~~Answers~~ ☺

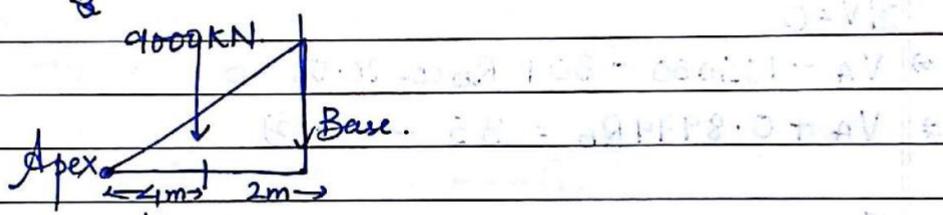


$\text{Area of } \triangle = \frac{1}{2} \times b \times h$

$$= \frac{1}{2} \times \frac{6}{2} \times 3000 = 9000 \text{ kN}$$

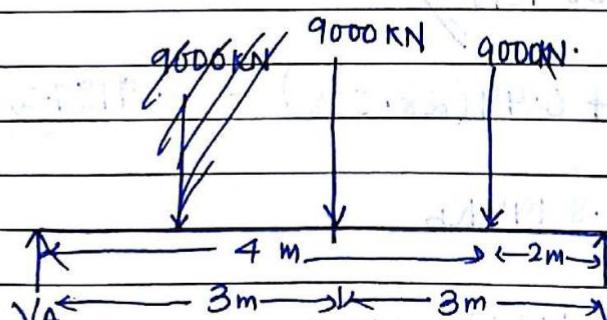
from base, from apex $= \frac{2}{3} d = \frac{2}{3} \times 6^2$

$$= \frac{1}{3} d = \frac{1}{3} \times 6 = 2 \text{ m}$$



$\text{Area of Rec.} = b \times h$

$$= 1500 \times 6 = 9000 \text{ kN}$$



$$\sum V = 0$$

$$V_A - 9000 - 9000 + V_B = 0$$

$$V_A + V_B = 18000 \quad \text{--- (1)}$$

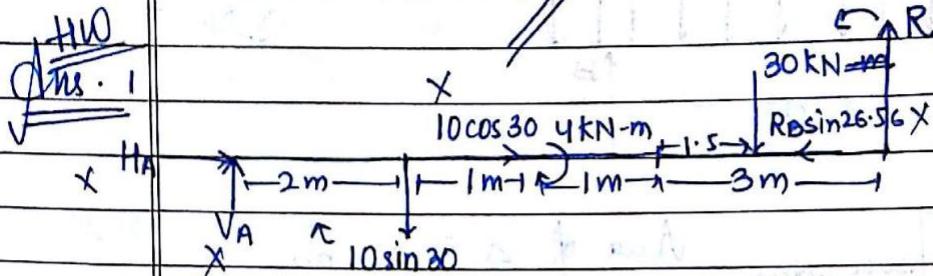
$$\sum M_A = 0$$

$$\Rightarrow (9000)3 + (9000)4 - (V_B)6 = 0$$

$$\Rightarrow V_B = 10500 \text{ kN} //$$

$$\therefore V_B = 10500 \text{ kN}$$

$$V_A = 18000 - 10500 \\ = 7500 \text{ kN}$$



$$\tan \theta = \frac{y_2}{x} \rightarrow \theta = 26.56$$

$$\sum H = 0$$

$$\Rightarrow H_A + 10 \cos 30 - R_B \sin 26.56 = 0$$

$$\Rightarrow H_A - 0.44 R_B = -8.66 \quad \text{--- (1)}$$

$$\sum V = 0$$

$$\Rightarrow V_A - 10 \sin 30 - 30 + R_B \cos 26.56 = 0$$

$$\Rightarrow V_A + 0.8944 R_B = 35 \quad \text{--- (2)}$$

$$\sum M_A = 0.$$

$$\Rightarrow (10 \sin 30) 2 + 4 + 30(5.5) - (R_B \cos 26.56) 7 = 0$$

$$\Rightarrow 179 = R_B \cos 26.56$$

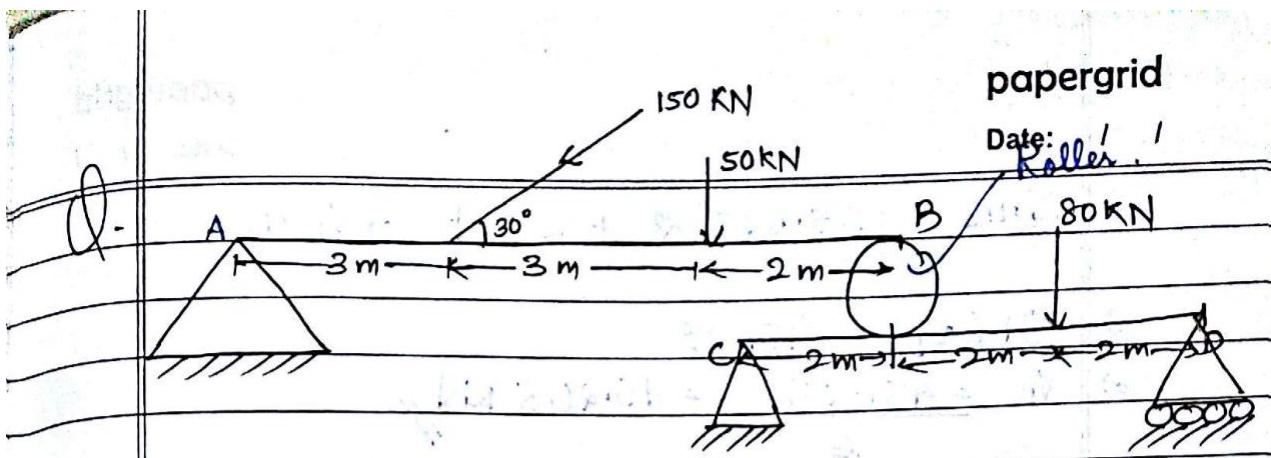
$$\Rightarrow R_B = 28.588 \text{ kN}$$

$$\Rightarrow H_A = -8.66 + 0.44(28.588) = 3.91872 \text{ kN}$$

$$\Rightarrow V_A = 35 - 0.8944 R_B$$

$$\Rightarrow V_A = 35 - (0.8944)(28.588)$$

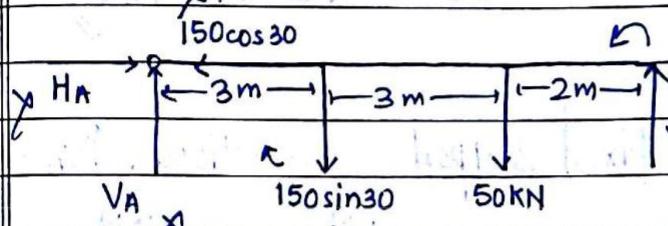
$$\Rightarrow V_A = 9.43 \text{ kN}$$



papergrid

Date: 10/10/14

Ans - FBD @ AB line :-



$$\sum H = 0$$

$$\Rightarrow H_A - 150 \cos 30 = 0$$

$$\Rightarrow H_A = 150 \cos 30 = 129.90 \text{ KN} //$$

$$\sum V = 0$$

$$\Rightarrow V_A - 150 \sin 30 - 50 + V_B = 0$$

$$\Rightarrow V_A + V_B = 125 \quad \text{--- (1)}$$

$$\sum M_A = 0$$

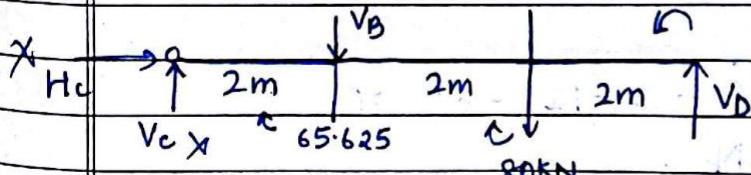
$$\Rightarrow (150 \sin 30) 3 + (50) 6 - (V_B) (8) = 0$$

$$\Rightarrow 8 V_B = 525$$

$$\Rightarrow V_B = 65.625 \text{ KN} //$$

$$\therefore V_A + V_B = 125 \Rightarrow V_A = 59.375 \text{ KN} //$$

FBD on line CD :-



$$\Rightarrow \sum H = 0$$

$$\Rightarrow H_C = 0.$$

$$\Rightarrow \sum V = 0$$

$$\Rightarrow V_C - 65.625 - 80 + V_D = 0$$

$$\Rightarrow V_C + V_D = 145.625 \quad \text{--- (1)}$$

$$\sum m_c = (65.625)2 + (80)4 - (V_D)6$$

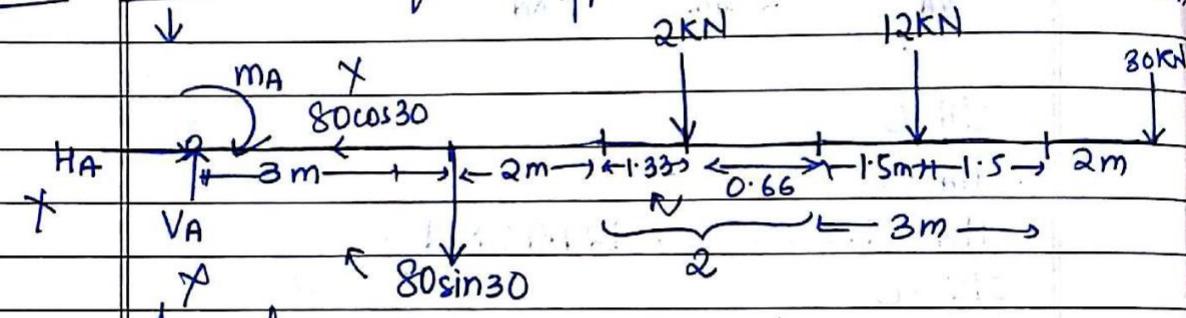
$$\Rightarrow 0 + 6V_D = 451.25$$

$$\Rightarrow V_D = \frac{451.25}{6} = 75.208 \text{ KN} //$$

$$V_c = 145.625 - 75.208 = 70.417 \text{ KN} //$$

HW
Ans. 2

FBD @ A \rightarrow fixed support - 3 reactions. $V_A \rightarrow H_A$ \nwarrow



$$\text{Area of } \Delta = \frac{1}{2}bh = \frac{1}{2} \times 2 \times 2 = 2 \text{ KN}$$

$$\text{from apex} = \frac{2}{3}d = \frac{2}{3} \times 2 = \frac{4}{3} = 1.33 \text{ m.}$$

$$\text{from base} = \frac{1}{3}d = \frac{2}{3} = 0.66 \text{ m.}$$

$$\sum H = 0$$

$$\Rightarrow H_A - 80\cos 30 = 0$$

$$\Rightarrow H_A = 69.282 \text{ KN} //$$

$$\sum V = 0$$

$$\Rightarrow V_A - 80\sin 30 - 2 - 12 - 30 = 0$$

$$\Rightarrow V_A = 84 \text{ KN} //$$

$$\sum m_A = ?$$

$$\Rightarrow (80\sin 30)3 + 2(6.33) + 12(8.5) + (30)(12)$$

$$\Rightarrow 594.66 // \text{Clockwise } \smiley$$