

Evaluation of gate designs

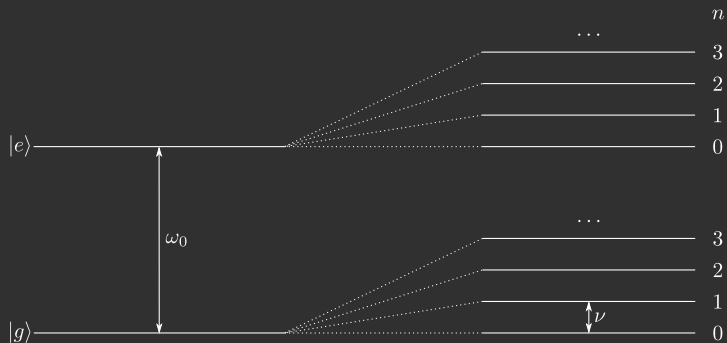
For trapped ion quantum computers

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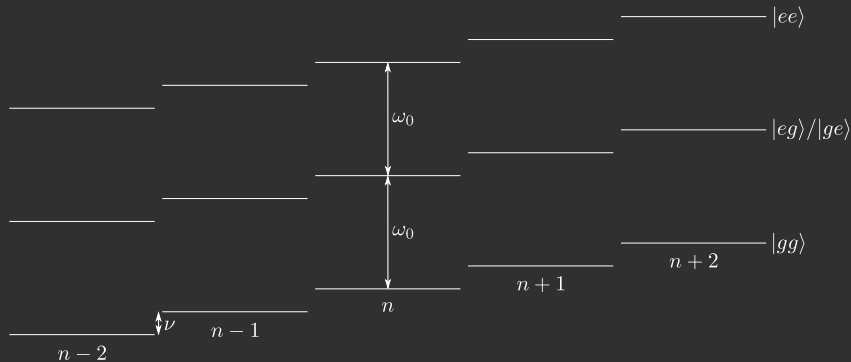
March, 2022

Energy structure



$$\hat{H} = -\frac{\hbar\omega_0}{2}\hat{\sigma}_z + \hbar\nu\left(\hat{a}^\dagger\hat{a} + \frac{1}{2}\right)$$

Energy structure



$$\hat{H} = -\frac{\hbar\omega_0}{2} \sum_i^n \hat{\sigma}_z^{(i)} + \hbar\nu \left(\hat{a}^\dagger \hat{a} + \frac{1}{2} \right)$$

Driving the system

$$\hat{H} = -\frac{\hbar\omega_0}{2} \sum_i \hat{\sigma}_z^{(i)} + \hbar\nu \left(\hat{a}^\dagger \hat{a} + \frac{1}{2} \right) + \sum_l \frac{\Omega_l}{2} \hat{\sigma}_+^{(n_l)} e^{-i(\mathbf{kz} - \omega_l t)} + h.c.$$

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$$\hat{H}_I = \sum_l \frac{\Omega_l}{2} \hat{\sigma}_+^{(n_l)} e^{-i(\eta(\hat{\tilde{a}} + \hat{\tilde{a}}^\dagger) - \Delta_l t)} + h.c.$$

$$\eta = \mathbf{kz}_0$$

$$\hat{\tilde{a}} = \hat{a} e^{-i\nu t}$$

$$\hat{\tilde{a}}^\dagger = \hat{a}^\dagger e^{i\nu t}$$

Driving the system

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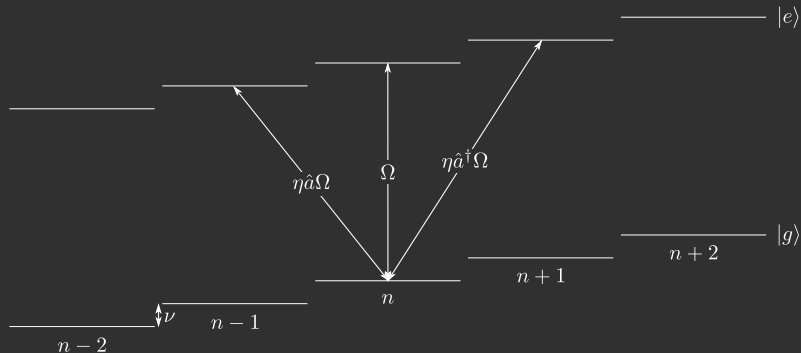
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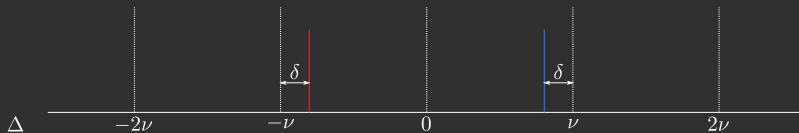
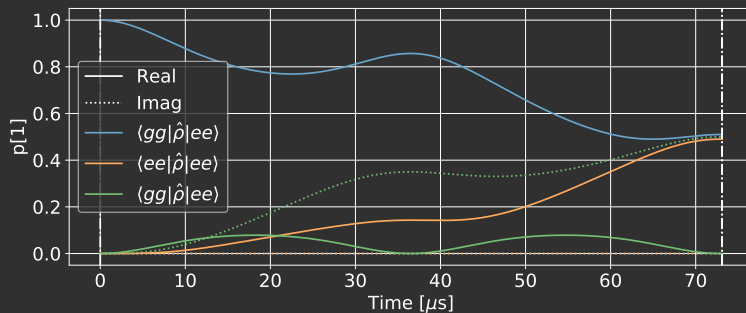
$$\hat{\hat{a}}^\dagger = \hat{a}^\dagger e^{i\nu t}$$

Lamb-Dicke regime



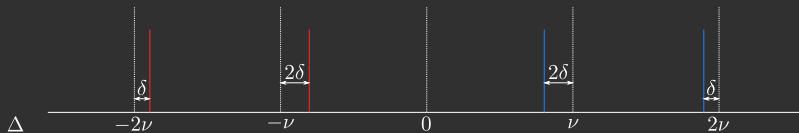
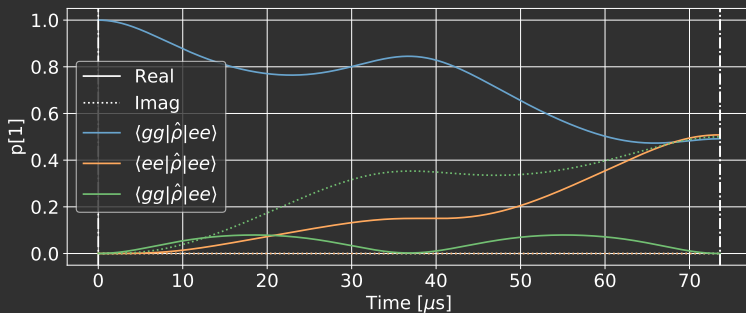
$$e^{i\eta(\hat{a}+\hat{a}^\dagger)} \cong \hat{\mathbb{1}} + i\eta(\hat{a} + \hat{a}^\dagger) + \mathcal{O}(\eta^2)$$

Mølmer-Sørensen gate¹



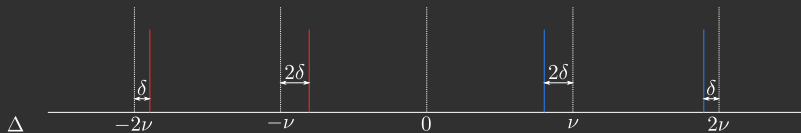
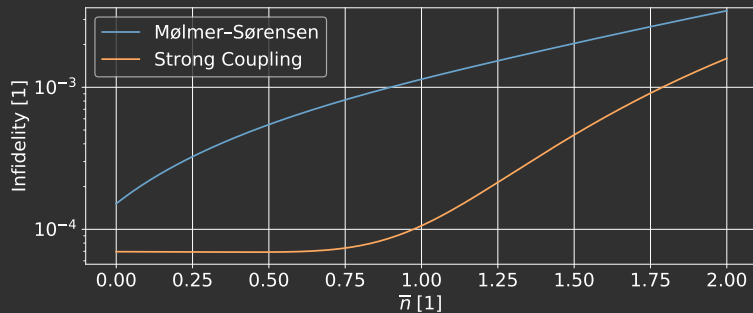
¹A. Sørensen and K. Mølmer, "Entanglement and quantum computation with ions in thermal motion," , 2000.

Strong coupling gate²



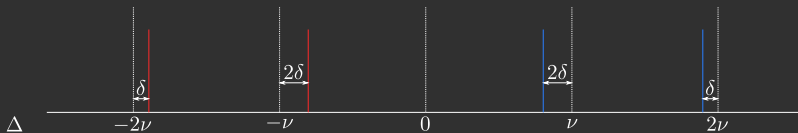
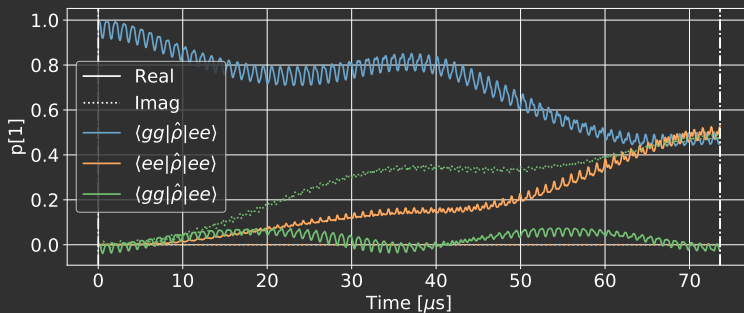
²M. Sameti, J. Lishman, and F. Mintert, "Strong-coupling quantum logic of trapped ions," 2021.

Strong coupling gate²



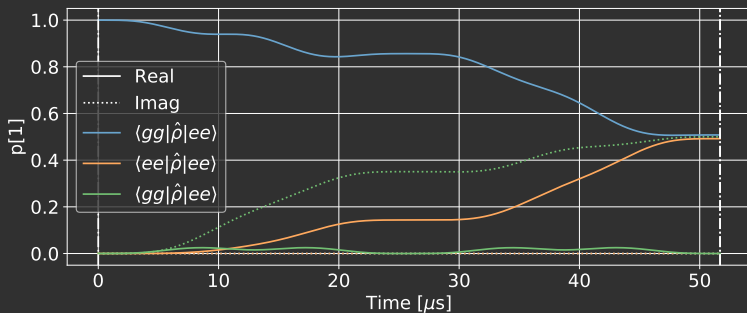
²M. Sameti, J. Lishman, and F. Mintert, "Strong-coupling quantum logic of trapped ions," 2021.

Strong coupling gate²



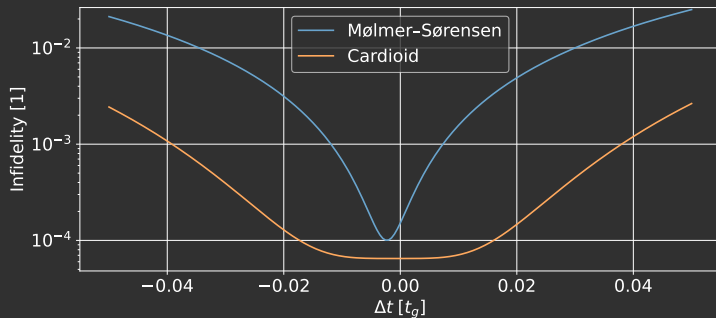
²M. Sameti, J. Lishman, and F. Mintert, "Strong-coupling quantum logic of trapped ions," 2021.

Cardioid gate³



³Y. Shapira, R. Shaniv, T. Manovitz, *et al.*, "Robust entanglement gates for trapped-ion qubits," 2018.

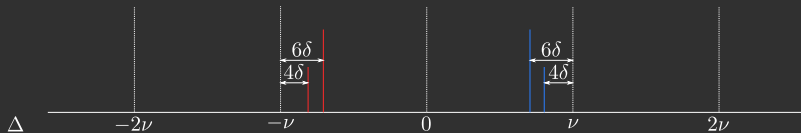
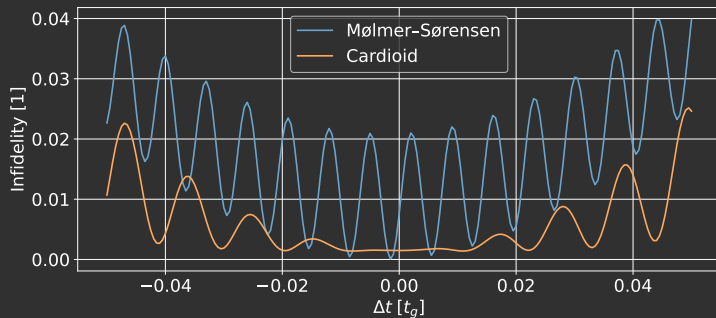
Cardioid gate³



³Y. Shapira, R. Shaniv, T. Manovitz, *et al.*, "Robust entanglement gates for trapped-ion qubits," 2018.

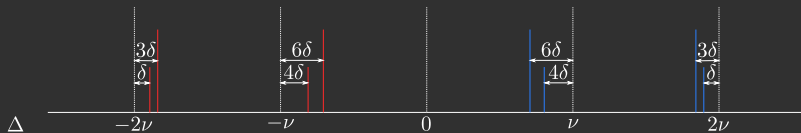
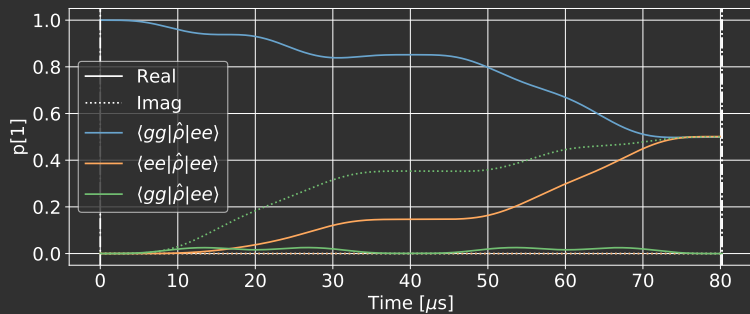
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Cardioid gate³

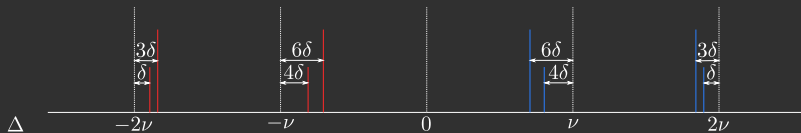
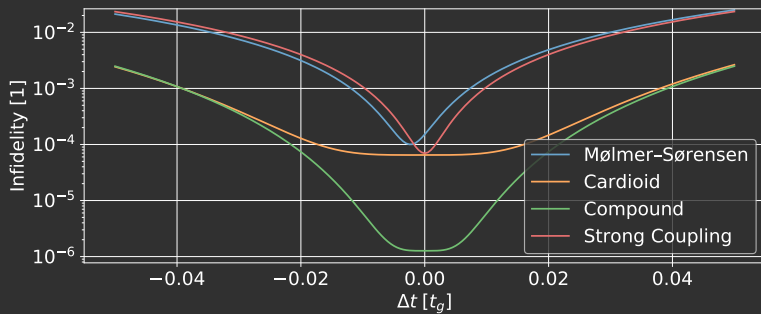


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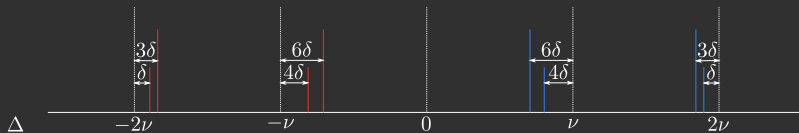
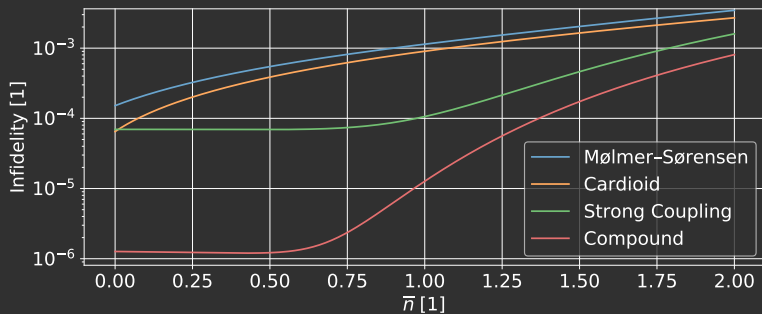
Compound gate



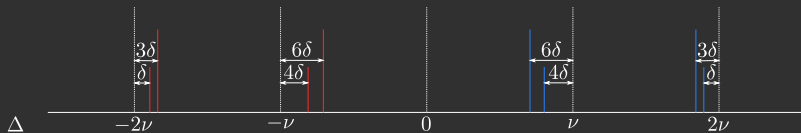
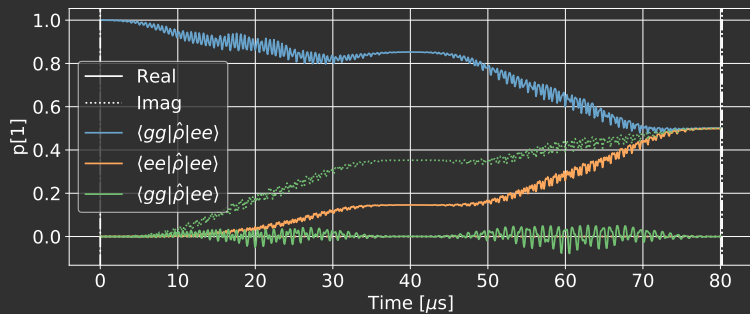
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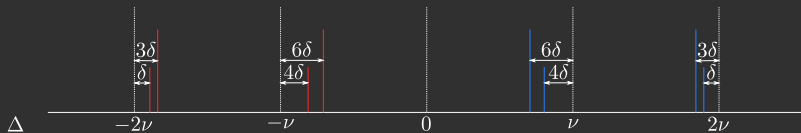
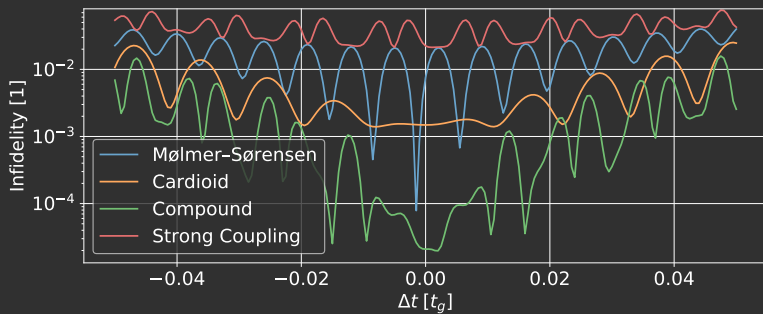
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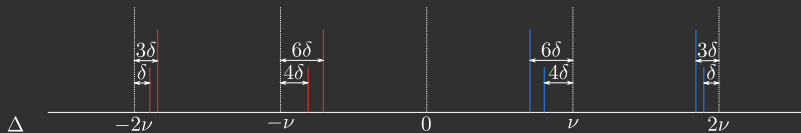
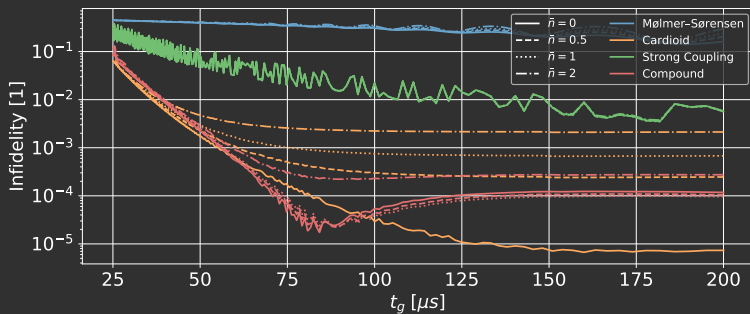
Compound gate



Compound gate



Compound gate



Dynamical decoupling

a

b

Thank you for the attention