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Digital Image Fundamentals



Those who wish to succeed must ask the right preliminary questions.

Aristotle

Preview

This chapter is an introduction to a number of basic concepts in digital image processing that are used throughout the book. Section 2.1 summarizes some important aspects of the human visual system, including image formation in the eye and its capabilities for brightness adaptation and discrimination. Section 2.2 discusses light, other components of the electromagnetic spectrum, and their imaging characteristics. Section 2.3 discusses imaging sensors and how they are used to generate digital images. Section 2.4 introduces the concepts of uniform image sampling and intensity quantization. Additional topics discussed in that section include digital image representation, the effects of varying the number of samples and intensity levels in an image, the concepts of spatial and intensity resolution, and the principles of image interpolation. Section 2.5 deals with a variety of basic relationships between pixels. Finally, Section 2.6 is an introduction to the principal mathematical tools we use throughout the book. A second objective of that section is to help you begin developing a “feel” for how these tools are used in a variety of basic image processing tasks.

Upon completion of this chapter, readers should:

- Have an understanding of some important functions and limitations of human vision.
- Be familiar with the electromagnetic energy spectrum, including basic properties of light.
- Know how digital images are generated and represented.
- Understand the basics of image sampling and quantization.
- Be familiar with spatial and intensity resolution and their effects on image appearance.
- Have an understanding of basic geometric relationships between image pixels.
- Be familiar with the principal mathematical tools used in digital image processing.
- Be able to apply a variety of introductory digital image processing techniques.

2.1 ELEMENTS OF VISUAL PERCEPTION

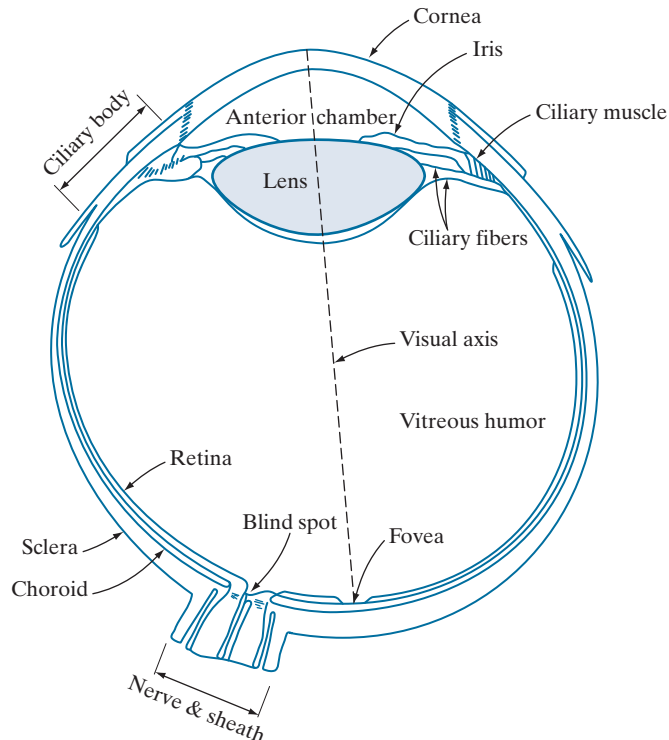
Although the field of digital image processing is built on a foundation of mathematics, human intuition and analysis often play a role in the choice of one technique versus another, and this choice often is made based on subjective, visual judgments. Thus, developing an understanding of basic characteristics of human visual perception as a first step in our journey through this book is appropriate. In particular, our interest is in the elementary mechanics of how images are formed and perceived by humans. We are interested in learning the physical limitations of human vision in terms of factors that also are used in our work with digital images. Factors such as how human and electronic imaging devices compare in terms of resolution and ability to adapt to changes in illumination are not only interesting, they are also important from a practical point of view.

STRUCTURE OF THE HUMAN EYE

Figure 2.1 shows a simplified cross section of the human eye. The eye is nearly a sphere (with a diameter of about 20 mm) enclosed by three membranes: the *cornea* and *sclera* outer cover; the *choroid*; and the *retina*. The cornea is a tough, transparent tissue that covers the anterior surface of the eye. Continuous with the cornea, the sclera is an opaque membrane that encloses the remainder of the optic globe.

The choroid lies directly below the sclera. This membrane contains a network of blood vessels that serve as the major source of nutrition to the eye. Even superficial

FIGURE 2.1
Simplified
diagram of a
cross section of
the human eye.



injury to the choroid can lead to severe eye damage as a result of inflammation that restricts blood flow. The choroid coat is heavily pigmented, which helps reduce the amount of extraneous light entering the eye and the backscatter within the optic globe. At its anterior extreme, the choroid is divided into the *ciliary body* and the *iris*. The latter contracts or expands to control the amount of light that enters the eye. The central opening of the iris (the *pupil*) varies in diameter from approximately 2 to 8 mm. The front of the iris contains the visible pigment of the eye, whereas the back contains a black pigment.

The *lens* consists of concentric layers of fibrous cells and is suspended by fibers that attach to the ciliary body. It is composed of 60% to 70% water, about 6% fat, and more protein than any other tissue in the eye. The lens is colored by a slightly yellow pigmentation that increases with age. In extreme cases, excessive clouding of the lens, referred to as *cataracts*, can lead to poor color discrimination and loss of clear vision. The lens absorbs approximately 8% of the visible light spectrum, with higher absorption at shorter wavelengths. Both infrared and ultraviolet light are absorbed by proteins within the lens and, in excessive amounts, can damage the eye.

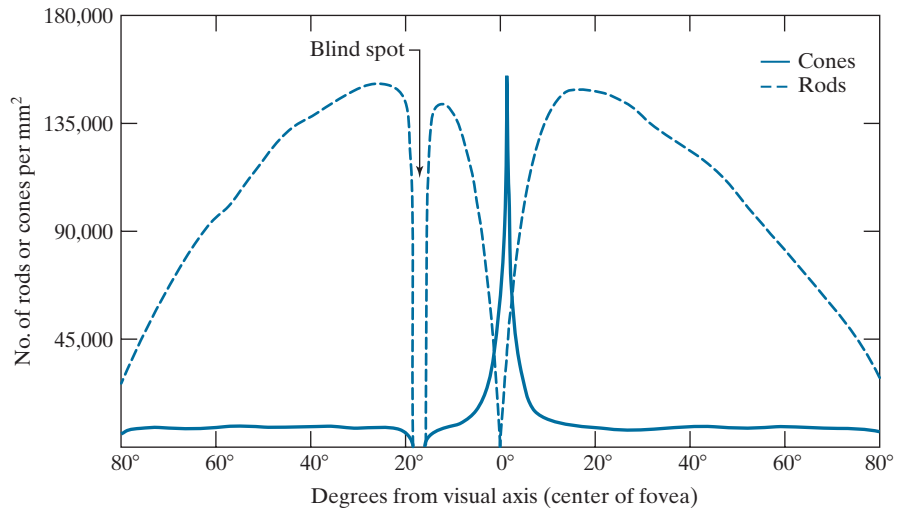
The innermost membrane of the eye is the *retina*, which lines the inside of the wall's entire posterior portion. When the eye is focused, light from an object is imaged on the retina. Pattern vision is afforded by discrete light receptors distributed over the surface of the retina. There are two types of receptors: *cones* and *rods*. There are between 6 and 7 million cones in each eye. They are located primarily in the central portion of the retina, called the *fovea*, and are highly sensitive to color. Humans can resolve fine details because each cone is connected to its own nerve end. Muscles rotate the eye until the image of a region of interest falls on the fovea. Cone vision is called *photopic* or *bright-light* vision.

The number of rods is much larger: Some 75 to 150 million are distributed over the retina. The larger area of distribution, and the fact that several rods are connected to a single nerve ending, reduces the amount of detail discernible by these receptors. Rods capture an overall image of the field of view. They are not involved in color vision, and are sensitive to low levels of illumination. For example, objects that appear brightly colored in daylight appear as colorless forms in moonlight because only the rods are stimulated. This phenomenon is known as *scotopic* or *dim-light* vision.

Figure 2.2 shows the density of rods and cones for a cross section of the right eye, passing through the region where the optic nerve emerges from the eye. The absence of receptors in this area causes the so-called *blind spot* (see Fig. 2.1). Except for this region, the distribution of receptors is radially symmetric about the fovea. Receptor density is measured in degrees from the visual axis. Note in Fig. 2.2 that cones are most dense in the center area of the fovea, and that rods increase in density from the center out to approximately 20° off axis. Then, their density decreases out to the periphery of the retina.

The fovea itself is a circular indentation in the retina of about 1.5 mm in diameter, so it has an area of approximately 1.77 mm². As Fig. 2.2 shows, the density of cones in that area of the retina is on the order of 150,000 elements per mm². Based on these figures, the number of cones in the fovea, which is the region of highest acuity

FIGURE 2.2
Distribution of
rods and cones in
the retina.



in the eye, is about 265,000 elements. Modern electronic imaging chips exceed this number by a large factor. While the ability of humans to integrate intelligence and experience with vision makes purely quantitative comparisons somewhat superficial, keep in mind for future discussions that electronic imaging sensors can easily exceed the capability of the eye in resolving image detail.

IMAGE FORMATION IN THE EYE

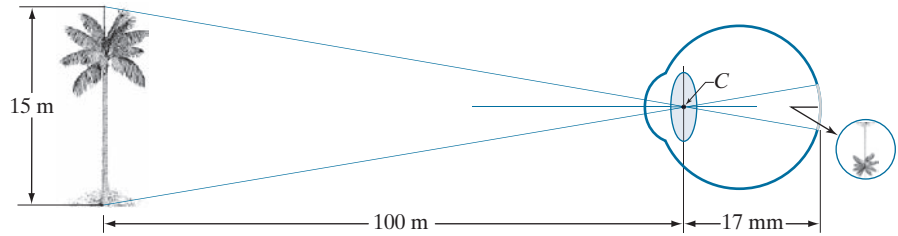
In an ordinary photographic camera, the lens has a fixed focal length. Focusing at various distances is achieved by varying the distance between the lens and the imaging plane, where the film (or imaging chip in the case of a digital camera) is located. In the human eye, the converse is true; the distance between the center of the lens and the imaging sensor (the retina) is fixed, and the focal length needed to achieve proper focus is obtained by varying the shape of the lens. The fibers in the ciliary body accomplish this by flattening or thickening the lens for distant or near objects, respectively. The distance between the center of the lens and the retina along the visual axis is approximately 17 mm. The range of focal lengths is approximately 14 mm to 17 mm, the latter taking place when the eye is relaxed and focused at distances greater than about 3 m. The geometry in Fig. 2.3 illustrates how to obtain the dimensions of an image formed on the retina. For example, suppose that a person is looking at a tree 15 m high at a distance of 100 m. Letting h denote the height of that object in the retinal image, the geometry of Fig. 2.3 yields $15/100 = h/17$ or $h = 2.5$ mm. As indicated earlier in this section, the retinal image is focused primarily on the region of the fovea. Perception then takes place by the relative excitation of light receptors, which transform radiant energy into electrical impulses that ultimately are decoded by the brain.

BRIGHTNESS ADAPTATION AND DISCRIMINATION

Because digital images are displayed as sets of discrete intensities, the eye's ability to discriminate between different intensity levels is an important consideration

FIGURE 2.3

Graphical representation of the eye looking at a palm tree. Point C is the focal center of the lens.

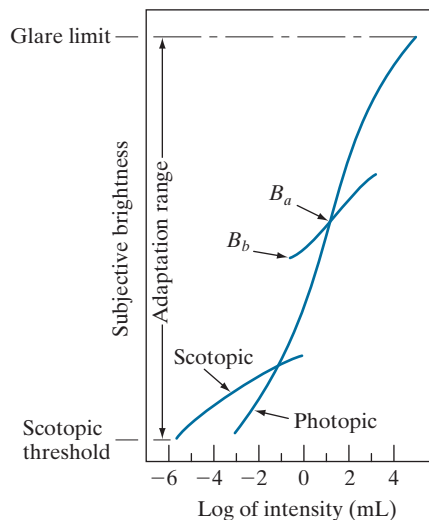


in presenting image processing results. The range of light intensity levels to which the human visual system can adapt is enormous—on the order of 10^{10} —from the scotopic threshold to the glare limit. Experimental evidence indicates that *subjective brightness* (intensity as perceived by the human visual system) is a logarithmic function of the light intensity incident on the eye. Figure 2.4, a plot of light intensity versus subjective brightness, illustrates this characteristic. The long solid curve represents the range of intensities to which the visual system can adapt. In photopic vision alone, the range is about 10^6 . The transition from scotopic to photopic vision is gradual over the approximate range from 0.001 to 0.1 millilambert (-3 to -1 mL in the log scale), as the double branches of the adaptation curve in this range show.

The key point in interpreting the impressive dynamic range depicted in Fig. 2.4 is that the visual system cannot operate over such a range *simultaneously*. Rather, it accomplishes this large variation by changing its overall sensitivity, a phenomenon known as *brightness adaptation*. The total range of distinct intensity levels the eye can discriminate simultaneously is rather small when compared with the total adaptation range. For a given set of conditions, the current sensitivity level of the visual system is called the *brightness adaptation level*, which may correspond, for example,

FIGURE 2.4

Range of subjective brightness sensations showing a particular adaptation level, B_a .



to brightness B_a in Fig. 2.4. The short intersecting curve represents the range of subjective brightness that the eye can perceive when adapted to *this* level. This range is rather restricted, having a level B_b at, and below which, all stimuli are perceived as indistinguishable blacks. The upper portion of the curve is not actually restricted but, if extended too far, loses its meaning because much higher intensities would simply raise the adaptation level higher than B_a .

The ability of the eye to discriminate between *changes* in light intensity at any specific adaptation level is of considerable interest. A classic experiment used to determine the capability of the human visual system for brightness discrimination consists of having a subject look at a flat, uniformly illuminated area large enough to occupy the entire field of view. This area typically is a diffuser, such as opaque glass, illuminated from behind by a light source, I , with variable intensity. To this field is added an increment of illumination, ΔI , in the form of a short-duration flash that appears as a circle in the center of the uniformly illuminated field, as Fig. 2.5 shows.

If ΔI is not bright enough, the subject says “no,” indicating no perceivable change. As ΔI gets stronger, the subject may give a positive response of “yes,” indicating a perceived change. Finally, when ΔI is strong enough, the subject will give a response of “yes” all the time. The quantity $\Delta I_c/I$, where ΔI_c is the increment of illumination discriminable 50% of the time with background illumination I , is called the *Weber ratio*. A small value of $\Delta I_c/I$ means that a small percentage change in intensity is discriminable. This represents “good” brightness discrimination. Conversely, a large value of $\Delta I_c/I$ means that a large percentage change in intensity is required for the eye to detect the change. This represents “poor” brightness discrimination.

A plot of $\Delta I_c/I$ as a function of $\log I$ has the characteristic shape shown in Fig. 2.6. This curve shows that brightness discrimination is poor (the Weber ratio is large) at low levels of illumination, and it improves significantly (the Weber ratio decreases) as background illumination increases. The two branches in the curve reflect the fact that at low levels of illumination vision is carried out by the rods, whereas, at high levels, vision is a function of cones.

If the background illumination is held constant and the intensity of the other source, instead of flashing, is now allowed to vary incrementally from never being perceived to always being perceived, the typical observer can discern a total of one to two dozen different intensity changes. Roughly, this result is related to the number of different intensities a person can see at any one *point* or *small area* in a monochrome image. This does not mean that an image can be represented by such a small number of intensity values because, as the eye roams about the image, the average

FIGURE 2.5

Basic experimental setup used to characterize brightness discrimination.

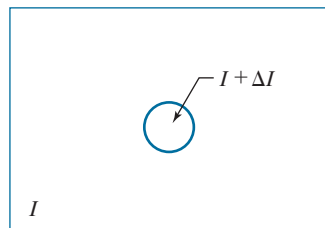
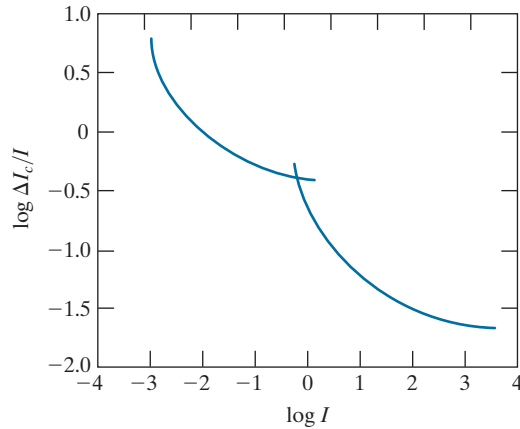


FIGURE 2.6

A typical plot of the Weber ratio as a function of intensity.



background changes, thus allowing a *different* set of incremental changes to be detected at each new adaptation level. The net result is that the eye is capable of a broader range of *overall* intensity discrimination. In fact, as we will show in Section 2.4, the eye is capable of detecting objectionable effects in monochrome images whose overall intensity is represented by fewer than approximately two dozen levels.

Two phenomena demonstrate that perceived brightness is not a simple function of intensity. The first is based on the fact that the visual system tends to undershoot or overshoot around the boundary of regions of different intensities. Figure 2.7(a) shows a striking example of this phenomenon. Although the intensity of the stripes

a
b
c

FIGURE 2.7

Illustration of the Mach band effect. Perceived intensity is not a simple function of actual intensity.

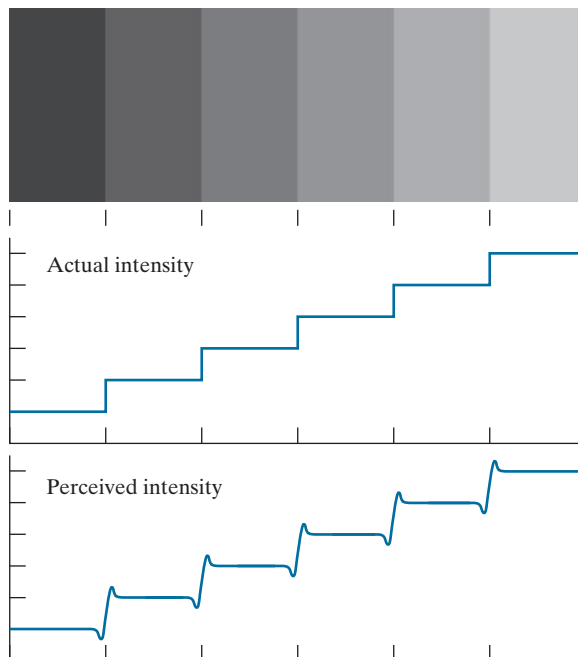




FIGURE 2.8 Examples of simultaneous contrast. All the inner squares have the same intensity, but they appear progressively darker as the background becomes lighter.

is constant [see Fig. 2.7(b)], we actually perceive a brightness pattern that is strongly scalloped near the boundaries, as Fig. 2.7(c) shows. These perceived scalloped bands are called *Mach bands* after Ernst Mach, who first described the phenomenon in 1865.

The second phenomenon, called *simultaneous contrast*, is that a region's perceived brightness does not depend only on its intensity, as Fig. 2.8 demonstrates. All the center squares have exactly the same intensity, but each appears to the eye to become darker as the background gets lighter. A more familiar example is a piece of paper that looks white when lying on a desk, but can appear totally black when used to shield the eyes while looking directly at a bright sky.

Other examples of human perception phenomena are *optical illusions*, in which the eye fills in nonexisting details or wrongly perceives geometrical properties of objects. Figure 2.9 shows some examples. In Fig. 2.9(a), the outline of a square is seen clearly, despite the fact that no lines defining such a figure are part of the image. The same effect, this time with a circle, can be seen in Fig. 2.9(b); note how just a few lines are sufficient to give the illusion of a complete circle. The two horizontal line segments in Fig. 2.9(c) are of the same length, but one appears shorter than the other. Finally, all long lines in Fig. 2.9(d) are equidistant and parallel. Yet, the crosshatching creates the illusion that those lines are far from being parallel.

2.2 LIGHT AND THE ELECTROMAGNETIC SPECTRUM

The electromagnetic spectrum was introduced in Section 1.3. We now consider this topic in more detail. In 1666, Sir Isaac Newton discovered that when a beam of sunlight passes through a glass prism, the emerging beam of light is not white but consists instead of a continuous spectrum of colors ranging from violet at one end to red at the other. As Fig. 2.10 shows, the range of colors we perceive in visible light is a small portion of the electromagnetic spectrum. On one end of the spectrum are radio waves with wavelengths billions of times longer than those of visible light. On the other end of the spectrum are gamma rays with wavelengths millions of times smaller than those of visible light. We showed examples in Section 1.3 of images in most of the bands in the EM spectrum.